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Bubbles in graphene - a computational study

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Bubbles in graphene - a computational study

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Abstract. Strain-induced deformations in graphene are predicted to give rise to large pseudomagnetic fields. We examine theoretically the case of gas-inflated bubbles to determine whether signatures of such fields are present in the local density of states. Sharp-edged bubbles are found to induce Friedel-type oscillations which can envelope pseudo-Landau level features in certain regions of the bubble. However, bubbles which minimise interference effects are also unsuitable for pseudo-Landau level formation due to more spatially varying field profiles.

1. Introduction

Strain engineering has been proposed as a method to manipulate the electronic, optical and magnetic properties of graphene [1–10]. It is based on the close relation between the structural and electronic properties of graphene. An inhomogeneous strain field can introduce pseudomagnetic fields (PMFs), [1, 4, 5] where the altered tight binding hoppings mimic the role of a gauge field in the low energy effective Dirac model of graphene [11, 12]. Guinea *et al* [1] demonstrated that nearly homogeneous PMFs can be generated by applying triaxial strain. One of the most striking consequences of homogeneous PMFs is the appearance of a Landau-like quantization. [1, 8] Scanning tunnelling spectroscopy on bubble-like deformations has observed pseudo-Landau levels (pLLs) corresponding to PMFs stronger than 300 T [2, 3]. Deformations can be induced in graphene samples by different techniques like pressurizing suspended graphene [5, 13] or by exploiting the thermal expansion coefficients of different substrates [3]. As a result, introducing nonuniform strain distributions at the nanoscale is a promising route towards strain engineering. The standard theoretical approach to treat strain effects employs continuum mechanics to obtain the strain field. The strain field can then be coupled to an effective Dirac model of graphene to study the generation of PMFs in various geometries. In most studies, only the PMF distribution is considered as opposed to experimentally observable quantities like local density of states (LDOS). This study calculates the LDOS of such systems without applying periodicity, which can introduce spurious interactions between neighboring bubbles.

2. Model

2.1. Patched Green's function approach

The patched Green's function approach, developed in Ref [14], treats device 'patches' embedded within an extended two dimensional system described by a tight-binding Hamiltonian. This approach allows us to insert a single bubble into an otherwise pristine infinite graphene sheet, and avoids issues such as interferences between a bubble and its periodic images or system



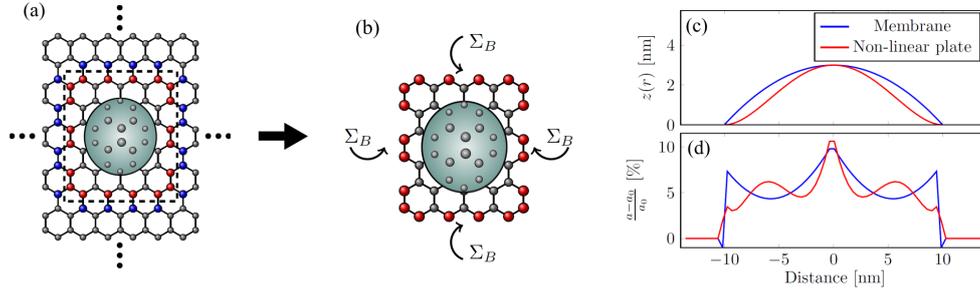


Figure 1. The patched GF method describes the extended graphene sheet away from the bubble device region (a) with a self energy term Σ_B (b). We consider membrane and non-linear plate type bubbles with radially dependent (c) height and (d) strain profiles.

edges. The extended part of the system is treated through a self-energy Σ_B entering the device area. The self-energy is written in terms of Green's functions (GFs) of an infinite, pristine sheet so that it can be calculated using methods taking advantage of periodicity and analytic integrability [15]. The device region Hamiltonian can be tridiagonalized allowing the device region GF to be treated using an adaptive recursive method allowing for efficient calculation of local properties, such as LDOS, everywhere in the device region surrounding a bubble.

2.2. Strain model

We consider two possibilities for the shape of a gas inflated bubble – the *membrane* and *non-linear plate* models. [16] The former is suitable for very large bubbles where bending stiffness can be neglected, whereas the latter is more appropriate for including bending effects near the edges of smaller bubbles. Membrane bubbles therefore have very sharp edges, whereas the edges are smoother in the non-linear plate bubbles. While these continuum models have been found to agree well with experimental shape profiles, more accurate modeling of bubble shapes and strain distributions can be achieved using molecular dynamics simulations. [5, 17, 18]

Using the deformation field \mathbf{u} the position of the atom i initially at \mathbf{R}_i^0 becomes $\mathbf{R}_i = \mathbf{R}_i^0 + \mathbf{u}$. The new bond lengths are afterwards determined as $d_{ij} = |\mathbf{R}_i - \mathbf{R}_j|$. Hoppings are modified according to $t_{ij} = t_0 e^{-\beta(d_{ij}/a_0 - 1)}$, where $t_0 \approx 2.7$ eV is the pristine coupling, $a_0 = 1.42 \text{ \AA}$ is the carbon-carbon distance and $\beta \approx \partial \log(t)/\partial \log(a)|_{a=a_0} \approx 3.37$ [7]. The strain tensor created by the strain field, $\epsilon_{ij} = \frac{1}{2}(\partial_j u_i + \partial_i u_j + \partial_i z \partial_j z)$, gives rise to a gauge field [11],

$$\mathbf{A} = -\frac{\hbar\beta}{2ea_0} \begin{pmatrix} \epsilon_{xx} - \epsilon_{yy} \\ 2\epsilon_{xy} \end{pmatrix}, \quad (1)$$

with the resulting PMF given by $\mathbf{B}_s = \nabla \times \mathbf{A}$. Table 1 shows the height profile, in-plane displacements and PMFs for the two types of bubbles considered here.

3. Results

The LDOS at individual sites, as well as the average DOS, can be quickly calculated using the above techniques. Fig. 2a shows the averaged DOS for membrane (blue) and non-linear plate (red) model bubbles. For the membrane model, we previously distinguished between two different type of oscillations [14]. Sharp peaks, such as those highlighted by the blue circle and triangle, showing an energy dependence, $E_n \sim \sqrt{n}$, are consistent with pLLs arising due to the PMF. In addition, the periodic oscillations at higher energies are Friedel-type oscillations arising due to electron scattering at the sharp edges of the membrane bubble.

Model type	$z(r, \theta)$	$\mathbf{u}(r, \theta) = \begin{pmatrix} u_r \\ u_\theta \end{pmatrix}$	$B_s(r, \theta)$
Membrane	$h_0 \left(1 - \frac{r^2}{R^2}\right)$	$\begin{pmatrix} u_0 \frac{r}{R} \left(1 - \frac{r}{R}\right) \\ 0 \end{pmatrix}$	$\frac{\hbar\beta u_0}{2ea_0 R^2} \sin(3\theta)$
Nonlinear plate	$h_0 \left(1 - \frac{r^2}{R^2}\right)^2$	$\begin{pmatrix} r(R-r)(c_1 + c_2 r) \\ 0 \end{pmatrix}$	$\frac{\hbar\beta}{2ea_0} \left[(c_1 - c_2 R) - \frac{32h_0^2 r^3}{R^6} \left(1 - \frac{r^2}{R^2}\right) \right] \sin(3\theta)$

Table 1. Height profile $z(r, \theta)$, in-plane displacements $\mathbf{u}(r, \theta)$ and PMF distributions $B_s(r, \theta)$ for the membrane and non-linear plate bubbles, where R and h_0 are the bubble radius and height respectively, and $u_0 = 1.136h_0^2/R$, $c_1 = 1.308h_0^2/R^3$ and $c_2 = -1.931h_0^2/R^4$. [16]

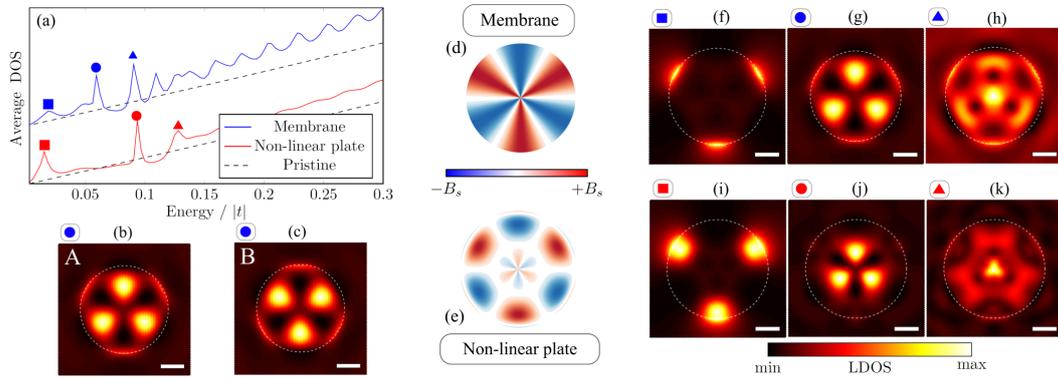


Figure 2. a) shows the averaged DOS with each bubble model with $R = 10\text{nm}$ and $h_0 = 3\text{nm}$, similar in scale to previous theoretical and experimental studies [2, 5]. Important peaks in each are highlighted by symbols. b,c) LDOS maps for the membrane model at the circle energy for the A and B sublattices. d,e) PMF distributions for each bubble type f-k) A sublattice LDOS maps for the peaks highlighted in a). The LDOS map scale bar is 5nm.

Before discussing the interplay between the different oscillation types, we note that both vary independently with position throughout the bubble region. The position dependence of the pLLs arises due to the non-uniform PMF distribution, which is plotted in Fig. 2d. This takes maximum amplitudes along the armchair directions which occur every 60° , but is only three-fold symmetric due to a sign change between two consecutive maxima. Unlike real magnetic fields, PMFs conserve time-reversal symmetry by taking opposite signs in the K and K' valleys of graphene. This leads to a strong sublattice polarisation [14, 19, 20], which is clearly visible for the LDOS maps shown in Fig. 2b-c, where the circle LDOS peak from Fig. 2a is localized in different regions on different sublattices. Comparison to Fig. 2d confirm that these correspond to a change in the sign of the PMF. We note that this first “pseudomagnetic peak” is localized along armchair directions where the PMFs are largest and reasonably constant. The position dependence of the Friedel oscillations meanwhile emerges from interference between electrons scattered at different sides of the bubble. The interplay of both oscillation types in membrane bubbles leads to the Friedel type acting as an envelope and quenching the LDOS signature of pLLs in certain regions of the bubble, as is clear for the dark spots in the LDOS map for the higher energy in Fig. 2h. STS measurements taken at such a spot would completely omit this peak due to the enveloping effects of the edge-induced Friedel oscillations.

To detect PMF signatures in gas-inflated bubbles, it may be worth considering softer edge profiles, such as the non-linear plate, which should give rise to weaker Friedel oscillations. This is clear from the averaged curve in Fig. 2a, where higher energy oscillations are considerably

suppressed compared to the membrane case. However, here there is also an absence of sharp pLL peaks following a \sqrt{n} distribution, with the possible exception of the red circle peak. This is consistent with the PMF distribution for this bubble type, plotted in Fig. 2e, which has a radial fluctuation in the sign and strength of the PMF. The center of the bubble has a distribution similar to the membrane case, and the central region of the LDOS map in Fig 2j resembles that of the corresponding membrane model peak (Fig 2g). We note also that the Friedel features for the higher energy in Fig. 2k (which does not fit the \sqrt{n} distribution) are more blurred than for the membrane case, as expected for scattering from a less-sharp bubble edge. Thus it seems that bubble shapes which reduce Friedel oscillations also effectively remove pLL effects due to the less uniform PMFs induced by their strain profiles.

Finally, the square symbol energy peak at low energies in both bubble types is a state localized near the bubble edge (Figs. 2f,i). It is not directly related to pseudomagnetic effects, but emerges due to the interface between the pristine region outside the bubble and the strained, perturbed region within. The localized states at this boundary act somewhat like a potential, and induce the scattering which lies behind the Friedel oscillations in these bubbles. These states are far less localized in the non-linear plate bubble than the membrane bubble, due to an edge which is no longer as sharp. This in turn leads to the smoothening and averaging out of the Friedel oscillations that we observed earlier for the non-linear plate bubbles.

4. Conclusions

We studied theoretically the local and averaged densities of states in gas-inflated graphene bubbles embedded in infinite graphene sheets using the patched Green's function approach. We determined that pLL features in sharp-edged bubbles may be hidden by interference effects due to electron scattering at the bubble edges. Softer-edged bubbles were found to display weaker interference effects, however their shape profiles also resulted in PMF distributions unsuitable for pLL formation. Our results suggest that it will be difficult to obtain reliable pLL features in such gas inflated systems, unlike bubbles formed on substrates which often display the triaxial-type strain that is predicted to give a more appropriate, uniform PMF for Landau level formation [1].

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