Fatigue Load Sensitivity Based Optimal Active Power Dispatch For Wind Farms

Zhao, Haoran; Wu, Qiuwei; Huang, Shaojun; Shahidehpour, Mohammad ; Guo, Qinglai; Sun, Hongbin

Published in:
IEEE Transactions on Sustainable Energy

Link to article, DOI:
[10.1109/TSTE.2017.2673122](https://doi.org/10.1109/TSTE.2017.2673122)

Publication date:
2017

Document Version
Peer reviewed version

[Link back to DTU Orbit](#)

Citation (APA):
Zhao, H., Wu, Q., Huang, S., Shahidehpour, M., Guo, Q., & Sun, H. (2017). Fatigue Load Sensitivity Based Optimal Active Power Dispatch For Wind Farms. *IEEE Transactions on Sustainable Energy*, 8(3), 1247-1259. <https://doi.org/10.1109/TSTE.2017.2673122>

General rights

Copyright and moral rights for the publications made accessible in the public portal are retained by the authors and/or other copyright owners and it is a condition of accessing publications that users recognise and abide by the legal requirements associated with these rights.

- Users may download and print one copy of any publication from the public portal for the purpose of private study or research.
- You may not further distribute the material or use it for any profit-making activity or commercial gain
- You may freely distribute the URL identifying the publication in the public portal

If you believe that this document breaches copyright please contact us providing details, and we will remove access to the work immediately and investigate your claim.

Fatigue Load Sensitivity Based Optimal Active Power Dispatch For Wind Farms

Haoran Zhao, Qiuwei Wu, Shaojun Huang, Mohammad Shahidehpour, Qinglai Guo and Hongbin Sun

Abstract—This paper proposes an optimal active power dispatch algorithm for wind farms based on Wind Turbine (WT) load sensitivity. The control objectives include tracking power references from the system operator and minimizing fatigue loads experienced by WTs. The sensitivity of WT fatigue loads to power references is defined which simplifies the formulation of the optimal power dispatch problem. Since the sensitivity value is calculated at the local WT controller, the computation burden of the central wind farm controller is largely reduced. Moreover, explicit analytical equations of the fatigue load sensitivity are derived, which significantly improves the computation efficiency of the local WT controller. The proposed algorithm can be implemented in different active power control schemes. Case studies were conducted with a wind farm under balance control for both low and high wind conditions. By comparing the rainflow cycles and Damage Equivalent Load (DEL), the efficacy of the proposed algorithm is verified.

Index Terms—Fatigue load, load sensitivity, optimal active power dispatch, wind farm, wind turbine.

I. INTRODUCTION

NOWADAYS, wind power is the fastest growing Renewable Energy Resource (RES). According to the report of the European Wind Energy Association (EWEA), the newly installed wind power capacity of EU in 2014 is 12.8 GW [1]. By the end of 2015, the cumulative capacity of wind power had reached 141.6 GW, which can meet around 11.4% of Europe's electricity demand.

With the increasing penetration level, variability and uncertainty of wind power have brought new technical challenges to power system operation [2]–[4]. The technical requirements for wind power integration are more stringent [5]. For the active power, different control requirements are specified, such as balance control, delta limitation, ramp rate limitation, etc. [6]. In other words, a wind farm shall be capable of tracking the power reference from the system operator.

With fast development of power electronics, controllability of modern Wind Turbines (WTs) has been largely improved.

When required wind farm power is less than the maximum available power, WTs will limit power production and operate in the derated mode. In order to achieve specific control objectives, it is very important to optimally dispatch power references to individual WTs.

The initial dispatch schemes for wind farms only focus on the power reference tracking. The power reference is proportionally distributed to individual WTs according to either the available power [7] or the actual output power [8]. Fatigue loads (load for short hereinafter) experienced by WTs, which has a significant impact on the lifetime of WTs, are not considered.

In recent studies, several multi-objective dispatch algorithms have been proposed [9]–[18]. The studies of [9]–[11] focus on the multi-objective control at the WT level. On top of providing the desired power production, mechanical loads are minimized by coordinating the pitch angle and electrical torque. For the wind farm level control, as long as the power requirement specified by the system operator is met, loads can be minimized by coordination among WTs [19]. The optimal control problem is either solved in a centralized manner [12]–[14] or a distributed manner [15]–[18]. For the former case, the wind farm model is formulated as a coupled, constrained Multiple Input and Multiple Output (MIMO) system whose order drastically grows with increasing the number of WTs. Since a modern large-scale wind farm may consist of several hundred WTs, the computation burden of the centralized control scheme is quite heavy and it cannot be used for real-time application. For the latter case, the distributed control scheme can efficiently reduce the computation burden. However, in order to guarantee the optimality, the iteration among WTs is required which implies high sampling communication required.

In this paper, a load sensitivity based optimal active power dispatch algorithm is proposed for wind farms to overcome the aforementioned problems. It minimizes WT loads while tracking the wind farm power reference. The proposed approach includes the following two aspects. Firstly, the sensitivity of WT fatigue loads to power references is defined and introduced as the signal exchanged between the central and local controllers. Secondly, explicit expression of the WT load sensitivities are derived.

The main contribution is that the proposed scheme enables efficient implementation of the optimal wind farm control, especially for large-scale wind farms. The proposed scheme is solved in the centralized manner. Compared with the other central optimal wind farm control schemes, the formulation of the optimal dispatch algorithm is simplified. Most of

H. Zhao and S. Huang are with Center for Electric Power and Energy (CEE), Department of Electrical Engineering, Technical University of Denmark (DTU), Kgs. Lyngby, 2800 Denmark (e-mail: hzhao@elektro.dtu.dk; shuang@elektro.dtu.dk).

Q. Wu is with Center for Electric and Energy (CEE), Department of Electrical Engineering, Technical University of Denmark (DTU), Kgs. Lyngby, 2800 Denmark, and School of Electrical Engineering, Shandong University, China (e-mail: qw@elektro.dtu.dk).

M. Shahidehpour is with Electrical and Computer Engineering Department, Illinois Institute of Technology (IIT), Chicago, IL 60616, USA (e-mail: ms@iit.edu).

Q. Guo and H. Sun are with Department of Electrical Engineering, Tsinghua University, Beijing, 100084 China (e-mail: guoqinglai@tsinghua.edu.cn; shb@mail.tsinghua.edu.cn).

the computation task is undertaken by the local controller and solved in parallel. The explicit expressions of the load sensitivities can reduce the online computation burden of the local controller. Moreover, the optimal control problem is formulated as a standard Quadratic Programming (QP) problem and can be efficiently solved. Compared with the distributed control scheme, the global optimum of the QP problem can be obtained without additional iterations.

The paper is organized as follows. Section II describes the structure of the wind farm control based on the load sensitivity. The modeling and operation of a power-controlled WT are introduced in Section III and Section IV, respectively. The explicit equations of load sensitivities are derived in Section V. Section VI explains the formulation of the optimal dispatch algorithm. Case studies are presented and discussed in Section VII, followed by conclusions.

II. LOAD SENSITIVITY BASED WIND FARM CONTROL STRUCTURE

The proposed wind farm control structure is shown in Fig. 1. According to the requirement of the system operator and the available power $P_{\text{avi}}^{\text{wfc}}$, the active power control scheme of the wind farm is decided. The power reference of the wind farm $P_{\text{ref}}^{\text{wfc}}$ is calculated and delivered to the wind farm controller. In the optimal wind farm control schemes of the previous studies, the measurements of individual WTs are sent directly to the central wind farm controller and the optimization problem is formulated based on a complicated wind farm model.

Fig. 1. Wind farm control structure.

In the proposed wind farm control, the load sensitivity $\frac{\partial L}{\partial P_{\text{ref}}^{\text{wt}}}$ and the power reference constraints of individual WTs ($[P_{\text{min}}^{\text{wt}}, P_{\text{max}}^{\text{wt}}]$) are used for the formulation of the optimal dispatch problem. They are calculated locally and sent to the wind farm controller. The details of calculating $\frac{\partial L}{\partial P_{\text{ref}}^{\text{wt}}}$ and constraints ($[P_{\text{min}}^{\text{wt}}, P_{\text{max}}^{\text{wt}}]$) are described in Section IV and Section V, respectively. By solving the optimization problem, the power references of individual WTs $P_{\text{ref}}^{\text{wt}}$ are updated for each interval of wind farm control. During the control interval, based on $P_{\text{ref}}^{\text{wt}}$, a torque reference T_{g_ref} for the local torque control and a pitch angle reference θ_{ref} for the pitch actuator are generated. The control interval of the local controller is smaller.

III. MODELING OF A POWER-CONTROLLED WT

In the wind farm control, the role of individual WTs is an actuator, which operates in a derated condition and tracks $P_{\text{ref}}^{\text{wt}}$. The power-controlled WT model developed by National Renewable Energy Laboratory (NREL) is used to represent a variable speed pitch-controlled WT [20], [21]. The model structure is shown in Fig. 2.

Fig. 2. Power-controlled WT model [21].

Normally, the sampling time of the wind farm controller t_s is in seconds [17]. Therefore, the fast dynamics in the generator and pitch actuator can be ignored [12]. Moreover, the oscillations in the shaft torsion and tower nodding are disregarded to reduce the model complexity. In this study, a simplified nonlinear WT model with its local control is introduced in the wind farm control, which is used to calculate the load sensitivities. Its controller and operation are described in Section IV.

A. Aerodynamics

The aerodynamic torque T_a and thrust force F_t are the main sources of nonlinearities [22], calculated by,

$$T_a = \frac{0.5\pi\rho R^2 v_r^3 C_p(\lambda, \theta)}{\omega_r}, \quad (1)$$

$$F_t = 0.5\pi\rho R^2 v_r^2 C_t(\lambda, \theta), \quad (2)$$

where C_p and C_t are the power coefficient and thrust coefficient, respectively, R is the length of the blade, ρ is the air density, v_r is the effective wind speed on the rotor, and λ is the tip speed ratio, defined by $\lambda \triangleq \frac{\omega_r R}{v_r}$.

B. Drive Train

The drive train is considered to be rigidly coupled and the single-mass model is used in this study, where the rotor mass J_r and generator mass J_g are merged into one equivalent mass J_t [23], expressed by,

$$J_t = J_r + \eta_g^2 J_g. \quad (3)$$

According to the low-shaft motion equation,

$$\dot{\omega}_r = \frac{1}{J_t} (T_a - \eta_g T_g), \quad (4)$$

$$\omega_g = \eta_g \omega_r, \quad (5)$$

where ω_r and ω_g are the rotor and generator speeds, respectively, and η_g is the gear box ratio.

C. Generator

In the torque control loop, the vector control is used to ensure a fast (in milliseconds) and accurate response [24]. Since the dynamic is neglected, the generator torque T_g is approximately equal to its reference, i.e.,

$$T_g \approx T_{g_ref}. \quad (6)$$

D. Tower

The tower dynamics is not included in the simplified WT model. According to [14], [25], it is assumed the fore-aft bending moment at the tower base M_t can be approximately derived by,

$$M_t \approx H \cdot F_t, \quad (7)$$

where H indicates the tower height.

IV. OPERATION AND CONTROL OF WTS IN A WIND FARM

Conventionally, WTs are controlled to track its Optimal Regimes Characteristic (ORC), as shown in Fig. 3. The polyhedron marked in the figure shows the feasible operation area where the power coefficient $C_p > 0$. Define the rated wind speed as v_{rated} and the rated power as P_{rated}^{wt} . When $v_w \leq v_{rated}$, the pitch control is deactivated ($\theta = 0$) and T_g is regulated to track the optimal rotor speed. The maximum available wind power is extracted ($P_{ref}^{wt} = P_{avi}^{wt} \leq P_{rated}^{wt}$). When $v_w > v_{rated}$, T_g is kept at its rated value and the pitch control is activated to prevent the generator speed ω_g from over-speeding. The captured wind power is limited to the rated value ($P_{ref}^{wt} = P_{rated}^{wt}$).

Fig. 3. Operation regions of WT [16].

In [20], the WT operates in the power maximization mode. In this study, the WT operates in the derated mode, i.e., $P_{ref}^{wt} < P_{avi}^{wt}$. Different from the region definition in [20], the operation area is below the ORC and can be divided into two regions according to the status of the pitch control, as shown in Fig. 3. In order to follow P_{ref}^{wt} , the pitch angle reference θ_{ref} and generator torque reference T_{g_ref} are computed by the WT controller and then sent to the pitch actuator and generator, respectively.

A. Region I

The pitch control is activated. The captured power is controlled by regulating θ_{ref} and T_{g_ref} . The measured generator speed ω_g is filtered by a low-pass filter and the filtered speed ω_f is derived by,

$$\omega_f = \frac{1}{1 + s\tau_f} \omega_g, \quad (8)$$

where τ_f is the time constant of the filter.

According to the deviation of ω_f from its rated value ω_{g_rate} , θ_{ref} is obtained by the gain-scheduled PI controller,

$$\theta_{ref} = \frac{K_p}{K_c} (\omega_f - \omega_{g_rate}) + \frac{K_i}{K_c} \frac{\omega_f - \omega_{g_rate}}{s}, \quad (9)$$

where K_p and K_i are proportional and integral gains of the PI controller, respectively, and K_c is the correction factor. In [21], K_c is a function of θ , i.e., $K_c = K_0 + K_\theta \theta$, where K_0 and K_θ are the constants.

T_{g_ref} is calculated by,

$$T_{g_ref} = \frac{P_{ref}^{wt}}{\omega_f}. \quad (10)$$

B. Region II

The pitch control is deactivated, i.e., $\theta_{ref} = 0$. The captured power is only controlled by regulating T_{g_ref} , which is also calculated by (10).

V. SENSITIVITY CALCULATION OF WT LOAD

The fatigue loads of WTs can be divided into aerodynamic and gravity loads (external), and structural loads (internal) [26]. In this paper, the fatigue loads mainly focus on the loads of the drive train due to the torsion of the shaft and the loads of the tower structure due to the tower deflection. Compared with static loads, the dynamic stress causing structural damage of WTs is a much bigger issue. By damping the fluctuations of low-speed shaft torque T_s and thrust force F_t , the related fatigue loads can be reduced. Accordingly, for the drive train loads, the load sensitivity $\frac{\partial L}{\partial P_{ref}^{wt}}$ can be represented by $\frac{\partial T_{ref}}{\partial P_{ref}^{wt}}$. For the tower structure loads, $\frac{\partial L}{\partial P_{ref}^{wt}}$ can be represented by $\frac{\partial F_{ref}}{\partial P_{ref}^{wt}}$. If both drive train and tower structure loads are considered, $\frac{\partial L}{\partial P_{ref}^{wt}}$ can be represented by the combination of $\frac{\partial T_s}{\partial P_{ref}^{wt}}$ and $\frac{\partial F_t}{\partial P_{ref}^{wt}}$.

A. Incremental State Space Model

Suppose the time of the operating point is t_0 . The wind speed v_r is a variable which can either be measured or estimated [27]. In this study, v_r is estimated. The value at $t = t_0$ is v_{r0} and assumed to be constant for the short control period. The measured power production, generator speed, filtered speed and pitch angle at $t = t_0$ are defined as P_{g0} , ω_{g0} , ω_{f0} , and θ_0 , respectively. According to (1) and (10), the aerodynamic torque and generator torque at $t = t_0$ can be calculated and are defined as T_{g0} and T_{a0} , respectively.

Based on linearization of the simplified nonlinear WT model at the operating point, the incremental state space model for Region I is derived by the following steps. Then, the model

for Region II can be derived by neglecting the term related to the pitch angle. The sign Δ indicates the increment of a variable.

Step 1: Derivative equations of $\Delta\omega_g$, $\Delta\omega_f$ and $\Delta\beta$.

Based on (4) and (5),

$$\Delta\dot{\omega}_g = \frac{\eta_g}{J_t}(\Delta T_a - \eta_g \Delta T_g) + \frac{\eta_g}{J_t}(T_{a0} - \eta_g T_{g0}). \quad (11)$$

Based on (8),

$$\Delta\dot{\omega}_f = -\frac{1}{\tau_f}\Delta\omega_f + \frac{1}{\tau_f}\Delta\omega_g. \quad (12)$$

By defining $\beta \triangleq K_c\theta = K_0\theta + K_\theta\theta^2$, (8) is transformed into,

$$\beta = K_p(\omega_f - \omega_{g_rate}) + K_i \frac{\omega_f - \omega_{g_rate}}{s}. \quad (13)$$

Based on (12) and (13),

$$\begin{aligned} \Delta\dot{\beta} &= K_p\Delta\dot{\omega}_f + K_i(\omega_{f0} + \Delta\omega_f - \omega_{g_rated}) \\ &= \frac{K_p}{\tau_f}\Delta\omega_g + \left(-\frac{K_p}{\tau_f} + K_i\right)\Delta\omega_f + K_i(\omega_{f0} - \omega_{g_rated}). \end{aligned} \quad (14)$$

Step 2: Calculation of ΔT_a and ΔT_g .

Equation (10) is nonlinear. It could be approximately calculated around the operating point according to the Taylor series,

$$\Delta T_g \approx -\frac{P_{g0}}{\omega_{f0}^2}\Delta\omega_f + \frac{1}{\omega_{f0}}\Delta P_{ref}^{wt}. \quad (15)$$

Similarly, according to (1), ΔT_a can be calculated by,

$$\Delta T_a \approx \left.\frac{\partial T_a}{\partial \omega_g}\right|_{(\omega_{g0}, v_{r0}, \theta_0)}\Delta\omega_g + \left.\frac{\partial T_a}{\partial \beta}\right|_{(\omega_{g0}, v_{r0}, \theta_0)}\Delta\beta. \quad (16)$$

In the following, $\frac{\partial T_a}{\partial \omega_g}$ and $\frac{\partial T_a}{\partial \beta}$ are used for $\frac{\partial T_a}{\partial \omega_g}|_{(\omega_{g0}, v_{r0}, \theta_0)}$ and $\frac{\partial T_a}{\partial \beta}|_{(\omega_{g0}, v_{r0}, \theta_0)}$, respectively.

Step 3: Calculation of $\frac{\partial T_a}{\partial \omega_g}$ and $\frac{\partial T_a}{\partial \beta}$.

By defining $P_0 \triangleq 0.5\pi\rho R^2 v_{r0}^3$, the partial derivatives of T_a are derived according to (1),

$$\frac{\partial T_a}{\partial \omega_g} = -\frac{\eta_g P_0 C_p(\omega_{g0}, v_{r0}, \theta_0)}{\omega_{g0}^2} + \frac{\eta_g P_0}{\omega_{g0}} \frac{\partial C_p(\omega_g, v_{r0}, \theta_0)}{\partial \omega_g}, \quad (17)$$

$$\frac{\partial T_a}{\partial \theta} = \frac{\eta_g P_0}{\omega_{g0}} \frac{\partial C_p(\omega_{g0}, v_{r0}, \theta)}{\partial \theta}. \quad (18)$$

Accordingly,

$$\frac{\partial T_a}{\partial \beta} = \frac{\partial T_a}{\partial \theta} \frac{\partial \theta}{\partial \beta} = \frac{\partial T_a}{\partial \theta} \frac{1}{K_0 + 2K_\theta\theta_0}. \quad (19)$$

Step 4: Calculation of $\frac{\partial C_p}{\partial \omega_g}$ and $\frac{\partial C_p}{\partial \theta}$.

The function $C_p(\omega_g, v_r, \theta)$ is nonlinear. Normally, it can be expressed in two formats. For the first format, C_p is described by an empirical formula [28], e.g.,

$$\begin{aligned} C_p(\omega_g, v_r, \theta) &= 0.22\left(\frac{116}{\lambda_i} - 0.4\theta - 5\right)e^{\frac{12.5}{\lambda_i}}, \quad (20) \\ \frac{1}{\lambda_i} &= \frac{1}{\lambda + 0.08\theta} - \frac{0.035}{\theta^3 + 1}, \quad \lambda = \frac{\eta_g \omega_g R}{v_r}. \end{aligned}$$

For the second format, C_p is described in a lookup table derived from the geometry of the blades with inputs λ and

θ [21], as shown in Fig. 4. The differences of λ and θ of neighbouring cells are $\Delta\lambda_{tab}$ and $\Delta\theta_{tab}$, respectively. In this study, the second format is used. The corresponding data for this study can be accessed in the wind turbine model of SimWindFarm—a publicly available Simulink toolbox for dynamic wind farm modeling, simulation, and control [21]. The plot of $C_p(\lambda, \theta)$ based on the lookup table is shown in Fig. 5.

λ	λ_{min}	$\lambda_{min} + \Delta\lambda_{tab}$	$\dots$	λ_{max}
θ				
θ_{min}				
$\theta_{min} + \Delta\theta_{tab}$				
$\vdots$				
θ_{max}				

Fig. 4. Lookup table format of $C_p(\lambda, \theta)$.

Fig. 5. $C_p(\lambda, \theta)$ based on the data from SimWindFarm [21].

According to v_{r0} , ω_{g0} , and θ_0 , the power coefficient at the operating point C_{p0} can be obtained based on the lookup table, i.e., $C_{p0} = C_{p(n,m)}$, where n and m are the corresponding row and column indices, respectively. $\frac{\partial C_p}{\partial \omega_g}$ and $\frac{\partial C_p}{\partial \theta}$ can be calculated by,

$$\frac{\partial C_p}{\partial \omega_g} = \frac{R\eta_g}{v_{r0}} \frac{\partial C_p}{\partial \lambda}, \quad \frac{\partial C_p}{\partial \lambda} \approx \frac{C_{p(n,m+1)} - C_{p0}}{\Delta\lambda_{tab}}, \quad (21)$$

$$\frac{\partial C_p}{\partial \theta} \approx \frac{C_{p(n+1,m)} - C_{p0}}{\Delta\theta_{tab}}. \quad (22)$$

Step 5: Formulation of the state space model.

According to (11)-(22), the continuous state space model for Region I is formulated as,

$$\dot{x} = \mathbf{A_I}x + \mathbf{B_I}\Delta P_{ref}^{wt} + \mathbf{E_I}, \quad (23)$$

with

$$\begin{aligned} x &= [\Delta\omega_g, \Delta\beta, \Delta\omega_f]', \\ \mathbf{A_I} &= \begin{bmatrix} \frac{\eta_g}{J_t} \frac{\partial T_a}{\partial \omega_g} & \frac{\eta_g}{J_t} \frac{\partial T_a}{\partial \beta} & \frac{\eta_g^2 P_{g0}}{J_t \omega_{f0}^2} \\ \frac{K_p}{\tau_f} & 0 & -\frac{K_p}{\tau_f} + K_i \\ \frac{1}{\tau_f} & 0 & -\frac{1}{\tau_f} \end{bmatrix}, \end{aligned}$$

$$B_I = \begin{bmatrix} -\frac{\eta_g^2}{J_t \omega_{f0}} \\ 0 \\ 0 \end{bmatrix}, \quad E_I = \begin{bmatrix} \frac{\eta_g}{J_t} (T_{a0} - \eta_g T_{g0}) \\ K_i (\omega_{f0} - \omega_{g_rated}) \\ 0 \end{bmatrix}.$$

For Region II, the terms related to the pitch angle is neglected,

$$x = [\Delta\omega_g, \Delta\omega_f]',$$

$$A_{II} = \begin{bmatrix} \frac{\eta_g}{J_t} \frac{\partial T_a}{\partial \omega_g} & \frac{\eta_g^2 P_{g0}}{J_t \omega_{f0}^2} \\ \frac{1}{\tau_f} & -\frac{1}{\tau_f} \end{bmatrix}, B_{II} = \begin{bmatrix} -\frac{\eta_g^2}{J_t \omega_{f0}} \\ 0 \end{bmatrix},$$

$$E_{II} = \begin{bmatrix} \frac{\eta_g}{J_t} (T_{a0} - \eta_g T_{g0}) \\ 0 \end{bmatrix}.$$

Step 5: Discretization.

The continuous state space model (23) is discretized with the sampling period t_s .

For Region I, the discrete state space model is,

$$x(k+1) = A_I^d x(k) + B_I^d \Delta P_{ref}^{wt} + E_I^d, \quad (24)$$

with

$$A_I^d = e^{A_I t_s}, B_I^d = \int_0^{t_s} (e^{A_I t} B_I) dt, E_I^d = \int_0^{t_s} (e^{A_I t} E_I) dt,$$

where k is the step index.

For Region II, the discrete state space model is,

$$x(k+1) = A_{II}^d x(k) + B_{II}^d \Delta P_{ref}^{wt} + E_{II}^d, \quad (25)$$

with

$$A_{II}^d = e^{A_{II} t_s}, B_{II}^d = \int_0^{t_s} (e^{A_{II} t} B_{II}) dt, E_{II}^d = \int_0^{t_s} (e^{A_{II} t} E_{II}) dt.$$

B. Calculation of $\frac{\partial T_s}{\partial P_{ref}^{wt}}$

The shaft torque T_s twists the low-speed shaft. According to the motion equation,

$$\dot{\omega}_r = \frac{1}{J_r} (T_a - T_s) \Rightarrow T_s = T_a - J_r \omega_r. \quad (26)$$

Substituting (3) and (4) into (26),

$$\begin{aligned} T_s &= T_a - J_r \omega_r = T_a - \frac{J_r}{J_t} (T_a - \eta_g T_g) \\ &= \frac{J_t - J_r}{J_t} T_a + \frac{\eta_g J_r}{J_t} T_g \\ &= \frac{\eta_g^2 J_g}{J_t} T_a + \frac{\eta_g J_r}{J_t} T_g. \end{aligned} \quad (27)$$

Accordingly,

$$\Delta T_s = \frac{\eta_g^2 J_g}{J_t} \Delta T_a + \frac{\eta_g J_r}{J_t} \Delta T_g. \quad (28)$$

During the sampling period, the operation region of the WT may stay or change to another. When the current operating point is in Region I, i.e., $\theta_0 > 0$, with the increase of ΔP_{ref}^{wt} , $\theta_0 + \Delta\theta$ will decrease. If $\theta_0 + \Delta\theta = 0$, the system will transit into Region II. The corresponding ΔP_{ref}^{wt} is defined by $\Delta P_{I \rightarrow II}^{wt}$, which can be considered as the threshold.

According to (24),

$$\Delta\beta = B_I^d(2,1) \Delta P_{ref}^{wt} + E_I^d(2,1), \quad (29)$$

where $B_I^d(2,1)$ and $E_I^d(2,1)$ are the matrix elements of B_I^d and E_I^d , respectively. Since $\frac{\Delta\beta}{\Delta\theta} \approx \frac{\partial\beta}{\partial\theta} = K_0 + 2K_\theta\theta_0$,

$$\Delta\theta = \frac{B_I^d(2,1) \Delta P_{ref}^{wt} + E_I^d(2,1)}{K_0 + 2K_\theta\theta_0}. \quad (30)$$

According to $\Delta\theta = -\theta_0$, $\Delta P_{I \rightarrow II}^{wt}$ can be derived by,

$$\Delta P_{I \rightarrow II}^{wt} = \frac{-\theta_0(K_0 + 2K_\theta\theta_0) - E_I^d(2,1)}{B_I^d(2,1)}. \quad (31)$$

When the current operating point is in Region II, i.e., $\theta_0 = 0$, with the decrease of ΔP_{ref}^{wt} , $\omega_{f0} + \Delta\omega_f$ will increase. If $\omega_{f0} + \Delta\omega_f = \omega_{g_rated}$, the system will transit into Region I. The corresponding ΔP_{ref}^{wt} is defined by $\Delta P_{II \rightarrow I}^{wt}$, which can be considered as the threshold.

According to (25),

$$\Delta\omega_f = B_{II}^d(2,1) \Delta P_{ref}^{wt} + E_{II}^d(2,1), \quad (32)$$

where $B_{II}^d(2,1)$ and $E_{II}^d(2,1)$ are the matrix elements of B_{II}^d and E_{II}^d , respectively.

According to $\omega_{f0} + \Delta\omega_f = \omega_{g_rated}$, $\Delta P_{II \rightarrow I}^{wt}$ can be derived by,

$$\Delta P_{II \rightarrow I}^{wt} = \frac{\omega_{g_rated} - \omega_{f0} - E_{II}^d(2,1)}{B_{II}^d(2,1)}. \quad (33)$$

In the following, 4 cases are summarized to calculate $\frac{\partial T_s}{\partial P_{ref}^{wt}}$.

Case 1: Region I $\rightarrow$ Region I.

If $\Delta P_{ref}^{wt} \leq \Delta P_{I \rightarrow II}^{wt}$, the system stays in Region I. Based on (15) and (16), (28) can be transformed into,

$$\Delta T_s = C_I^{T_s} \Delta x + D_I^{T_s} \Delta P_{ref}^{wt}, \quad (34)$$

with

$$C_I^{T_s} = \begin{bmatrix} \frac{\eta_g^2 J_g}{J_t} \frac{\partial T_a}{\partial \omega_g} & \frac{\eta_g^2 J_g}{J_t} \frac{\partial T_a}{\partial \beta} & -\frac{P_{g0} \eta_g J_r}{\omega_{f0}^2 J_t} \end{bmatrix},$$

$$D_I^{T_s} = \frac{\eta_g J_r}{J_t \omega_{f0}}.$$

Based on (24) and (34),

$$\Delta T_s(k+1) = (C_I^{T_s} B_I^d + D_I^{T_s}) \Delta P_{ref}^{wt} + C_I^{T_s} E_I^d. \quad (35)$$

Hence,

$$\frac{\partial T_s}{\partial P_{ref}^{wt}} \approx \frac{\Delta T_s}{\Delta P_{ref}^{wt}} = S_1^{T_s} + \frac{Y_1^{T_s}}{\Delta P_{ref}^{wt}}, \quad (36)$$

with $S_1^{T_s} = C_I^{T_s} B_I^d + D_I^{T_s}$, $Y_1^{T_s} = C_I^{T_s} E_I^d$. The subscript of $S_1^{T_s}$ and $Y_1^{T_s}$ indicates the case index.

Case 2: Region II $\rightarrow$ Region II.

If $\Delta P_{ref}^{wt} > \Delta P_{II \rightarrow I}^{wt}$, the system stays in Region II. Based on (15) and (16), (28) can be transformed into,

$$\Delta T_s = C_{II}^{T_s} \Delta x + D_{II}^{T_s} \Delta P_{ref}^{wt}, \quad (37)$$

with

$$C_{II}^{T_s} = \begin{bmatrix} \frac{\eta_g^2 J_g}{J_t} \frac{\partial T_a}{\partial \omega_g} & -\frac{P_{g0} \eta_g J_r}{\omega_{f0}^2 J_t} \end{bmatrix}, D_{II}^{T_s} = \frac{\eta_g J_r}{J_t \omega_{f0}}.$$

Based on (25) and (37),

$$\Delta T_s(k+1) = (C_{II}^{Ts} B_{II}^d + D_{II}^{Ts}) \Delta P_{ref}^{wt} + C_{II}^{Ts} E_{II}^d. \quad (38)$$

Hence,

$$\frac{\partial T_s}{\partial P_{ref}^{wt}} \approx \frac{\Delta T_s}{\Delta P_{ref}^{wt}} = S_2^{Ts} + \frac{Y_2^{Ts}}{\Delta P_{ref}^{wt}}, \quad (39)$$

$$\text{with } S_2^{Ts} = C_{II}^{Ts} B_{II}^d + D_{II}^{Ts}, Y_2^{Ts} = C_{II}^{Ts} E_{II}^d.$$

Case 3: Region I → Region II.

If $\Delta P_{ref}^{wt} > \Delta P_{I \rightarrow II}^{wt}$, the system transits from Region I to Region II. In that case, ΔP_{ref}^{wt} could be divided into two parts: $\Delta P_{I \rightarrow II}^{wt}$ and $\Delta P_{ref}^{wt} - \Delta P_{I \rightarrow II}^{wt}$. The former part works in Region I and the latter part works in Region II.

Accordingly, $\Delta T_s(k+1)$ can be approximately calculated by,

$$\begin{aligned} \Delta T_s(k+1) &\approx S_1^{Ts} \Delta P_{I \rightarrow II}^{wt} + Y_1^{Ts} \\ &\quad + S_2^{Ts} (\Delta P_{ref}^{wt} - \Delta P_{I \rightarrow II}^{wt}) + Y_2^{Ts} \\ &\approx S_2^{Ts} \Delta P_{ref}^{wt} + Y_1^{Ts} + Y_2^{Ts} + (S_1^{Ts} - S_2^{Ts}) \Delta P_{I \rightarrow II}^{wt}. \end{aligned} \quad (40)$$

Hence,

$$\frac{\partial T_s}{\partial P_{ref}^{wt}} \approx \frac{\Delta T_s}{\Delta P_{ref}^{wt}} = S_3^{Ts} + \frac{Y_3^{Ts}}{\Delta P_{ref}^{wt}}, \quad (41)$$

$$\text{with } S_3^{Ts} = S_2^{Ts}, Y_3^{Ts} = Y_1^{Ts} + Y_2^{Ts} + (S_1^{Ts} - S_2^{Ts}) \Delta P_{I \rightarrow II}^{wt}.$$

Case 4: Region II → Region I.

If $\Delta P_{ref}^{wt} \leq \Delta P_{II \rightarrow I}^{wt}$, the system transits from Region II to Region I. Similarly, ΔP_{ref}^{wt} could be divided into two parts: $\Delta P_{II \rightarrow I}^{wt}$ and $\Delta P_{ref}^{wt} - \Delta P_{II \rightarrow I}^{wt}$. The former part works in Region II and the latter part works in Region I. $\Delta T_s(k+1)$ can be approximately calculated by,

$$\begin{aligned} \Delta T_s(k+1) &\approx S_2^{Ts} \Delta P_{II \rightarrow I}^{wt} + Y_2^{Ts} \\ &\quad + S_1^{Ts} (\Delta P_{ref}^{wt} - \Delta P_{II \rightarrow I}^{wt}) + S_1^{Ts} \\ &\approx S_1^{Ts} \Delta P_{ref}^{wt} + Y_2^{Ts} + Y_1^{Ts} + (S_2^{Ts} - S_1^{Ts}) \Delta P_{II \rightarrow I}^{wt}. \end{aligned} \quad (42)$$

Hence,

$$\frac{\partial T_s}{\partial P_{ref}^{wt}} \approx \frac{\Delta T_s}{\Delta P_{ref}^{wt}} = S_4^{Ts} + \frac{Y_4^{Ts}}{\Delta P_{ref}^{wt}}, \quad (43)$$

$$\text{with } S_4^{Ts} = S_1^{Ts}, Y_4^{Ts} = Y_2^{Ts} + Y_1^{Ts} + (S_2^{Ts} - S_1^{Ts}) \Delta P_{II \rightarrow I}^{wt}.$$

In the following, for generality, the subscripts of S^{Ts} and Y^{Ts} are omitted. Based on the measurements, S^{Ts} and Y^{Ts} can be calculated explicitly, which are sent to the wind farm controller to formulate the optimal dispatch algorithm.

C. Calculation of $\frac{\partial F_t}{\partial P_{ref}^{wt}}$

Similar to $\frac{\partial T_s}{\partial P_{ref}^{wt}}$, 4 cases are summarized to calculate $\frac{\partial F_t}{\partial P_{ref}^{wt}}$.

Case 1: Region I → Region I.

If $\Delta P_{ref}^{wt} \leq \Delta P_{I \rightarrow I}^{wt}$, the system stays in Region I. F_t can be calculated by,

$$\Delta F_t = C_I^{Ft} x, \quad (44)$$

$$\text{with } C_I^{Ft} = [\frac{\partial F_t}{\partial \omega_g} \quad \frac{\partial F_t}{\partial \beta} \quad 0].$$

Based on (24) and (44),

$$\Delta F_t(k+1) = C_I^{Ft} B_I^d \Delta P_{ref}^{wt} + C_I^{Ft} E_I^d. \quad (45)$$

Hence,

$$\frac{\partial F_t}{\partial P_{ref}^{wt}} \approx \frac{\Delta F_t}{\Delta P_{ref}^{wt}} = S_1^{Ft} + \frac{Y_1^{Ft}}{\Delta P_{ref}^{wt}}, \quad (46)$$

with $S_1^{Ft} = C_I^{Ft} B_I^d$, $Y_1^{Ft} = C_I^{Ft} E_I^d$. The subscript of S_1^{Ft} and Y_1^{Ft} indicates the case index.

Case 2: Region II → Region II.

If $\Delta P_{ref}^{wt} > \Delta P_{II \rightarrow I}^{wt}$, the system stays in Region II. F_t can be calculated by,

$$\Delta F_t = C_{II}^{Ft} x, \quad (47)$$

$$\text{with } C_{II}^{Ft} = [\frac{\partial F_t}{\partial \omega_g} \quad 0].$$

Based on (25) and (47),

$$\Delta F_t(k+1) = C_{II}^{Ft} B_{II}^d \Delta P_{ref}^{wt} + C_{II}^{Ft} E_{II}^d. \quad (48)$$

Hence,

$$\frac{\partial F_t}{\partial P_{ref}^{wt}} \approx \frac{\Delta F_t}{\Delta P_{ref}^{wt}} = S_2^{Ft} + \frac{Y_2^{Ft}}{\Delta P_{ref}^{wt}}, \quad (49)$$

$$\text{with } S_2^{Ft} = C_{II}^{Ft} B_{II}^d, Y_2^{Ft} = C_{II}^{Ft} E_{II}^d.$$

Case 3: Region I → Region II.

If $\Delta P_{ref}^{wt} > \Delta P_{I \rightarrow II}^{wt}$, the system transits from Region I to Region II. $\Delta F_t(k+1)$ can be approximately calculated by,

$$\begin{aligned} \Delta F_t(k+1) &\approx S_1^{Ft} \Delta P_{I \rightarrow II}^{wt} + Y_1^{Ft} \\ &\quad + S_2^{Ft} (\Delta P_{ref}^{wt} - \Delta P_{I \rightarrow II}^{wt}) + Y_2^{Ft} \\ &\approx S_2^{Ft} \Delta P_{ref}^{wt} + Y_1^{Ft} + Y_2^{Ft} + (S_1^{Ft} - S_2^{Ft}) \Delta P_{I \rightarrow II}^{wt}. \end{aligned} \quad (50)$$

Hence,

$$\frac{\partial F_t}{\partial P_{ref}^{wt}} \approx \frac{\Delta F_t}{\Delta P_{ref}^{wt}} = S_3^{Ft} + \frac{Y_3^{Ft}}{\Delta P_{ref}^{wt}}, \quad (51)$$

$$\text{with } S_3^{Ft} = S_2^{Ft}, Y_3^{Ft} = Y_1^{Ft} + Y_2^{Ft} + (S_1^{Ft} - S_2^{Ft}) \Delta P_{I \rightarrow II}^{wt}.$$

Case 4: Region II → Region I.

If $\Delta P_{ref}^{wt} \leq \Delta P_{II \rightarrow I}^{wt}$, the system transits from Region II to Region I. $\Delta F_t(k+1)$ can be approximately calculated by,

$$\begin{aligned} \Delta F_t(k+1) &\approx S_2^{Ft} \Delta P_{II \rightarrow I}^{wt} + Y_2^{Ft} \\ &\quad + S_1^{Ft} (\Delta P_{ref}^{wt} - \Delta P_{II \rightarrow I}^{wt}) + S_1^{Ft} \\ &\approx S_1^{Ft} \Delta P_{ref}^{wt} + Y_2^{Ft} + Y_1^{Ft} + (S_2^{Ft} - S_1^{Ft}) \Delta P_{II \rightarrow I}^{wt}. \end{aligned} \quad (52)$$

Hence,

$$\frac{\partial F_t}{\partial P_{ref}^{wt}} \approx \frac{\Delta F_t}{\Delta P_{ref}^{wt}} = S_4^{Ft} + \frac{Y_4^{Ft}}{\Delta P_{ref}^{wt}}, \quad (53)$$

$$\text{with } S_4^{Ft} = S_1^{Ft}, Y_4^{Ft} = Y_2^{Ft} + Y_1^{Ft} + (S_2^{Ft} - S_1^{Ft}) \Delta P_{II \rightarrow I}^{wt}.$$

According to (2), $\frac{\partial F_t}{\partial \omega_g}$ and $\frac{\partial F_t}{\partial \beta}$ in (44) and (47) are the functions of $\frac{\partial C_t}{\partial \omega_g}$ and $\frac{\partial C_t}{\partial \beta}$, respectively, i.e.,

$$\frac{\partial F_t}{\partial \omega_g} = \frac{P_0}{v_{r0}} \frac{\partial C_t}{\partial \omega_g}, \quad \frac{\partial F_t}{\partial \beta} = \frac{P_0}{v_{r0}} \frac{\partial C_t}{\partial \beta}. \quad (54)$$

The function C_t is nonlinear. Similar to C_p , C_t is also described in a lookup table derived from the geometry of the blades with inputs λ and θ [21]. The corresponding data for this study can be obtained in the wind turbine model of SimWindFarm. The plot of $C_t(\lambda, \theta)$ based on the lookup table is shown in Fig. 6.

Fig. 6. $C_t(\lambda, \theta)$ based on the data from SimWindFarm [21].

According to v_{r0} , ω_{g0} , and θ_0 , the power coefficient at the operating point C_{t0} can be found based on the lookup table, i.e., $C_{t0} = C_{t(n,m)}$, where n and m are the corresponding row and column indices, respectively. $\frac{\partial C_t}{\partial \omega_g}$ and $\frac{\partial C_t}{\partial \beta}$ can be calculated by,

$$\frac{\partial C_t}{\partial \omega_g} = \frac{R\eta_g}{v_{r0}} \frac{\partial C_t}{\partial \lambda}, \quad \frac{\partial C_t}{\partial \lambda} \approx \frac{C_{t(n,m+1)} - C_{t0}}{\Delta \lambda_{\text{tab}}}, \quad (55)$$

$$\frac{\partial C_t}{\partial \beta} = \frac{\partial C_t}{\partial \theta} \frac{1}{K_0 + 2K_\theta \theta_0}, \quad \frac{\partial C_t}{\partial \theta} \approx \frac{C_{t(n+1,m)} - C_{t0}}{\Delta \theta_{\text{tab}}}. \quad (56)$$

In the following, for generality, the subscripts of S^{F_t} and Y^{F_t} are omitted. Based on the measurements, S^{F_t} and Y^{F_t} can be calculated explicitly, which are sent to the wind farm controller to formulate the optimal dispatch algorithm.

VI. FORMULATION OF OPTIMAL DISPATCH ALGORITHM

A. Cost Function

Conventionally, the dispatch algorithm is based on a proportional distribution of the available active power [7]. Suppose a wind farm consists of N_{wt} WTs. According to [7], the power reference of the i th WT is calculated by,

$$P_{\text{ref}}^{\text{wt},i} = \alpha_i P_{\text{ref}}^{\text{wfc}}, \quad \alpha_i = \frac{P_{\text{avi}}^{\text{wt},i}}{P_{\text{avi}}^{\text{wfc}}}, \quad P_{\text{avi}}^{\text{wfc}} = \sum_{i=1}^{N_{\text{wt}}} P_{\text{avi}}^{\text{wt},i}, \quad (57)$$

where α_i is the distribution factor of the i th WT and $P_{\text{avi}}^{\text{wt},i}$ is the available power of the i th WT.

In this study, based on the proportional dispatch algorithm, the control objective is to dynamically redistribute power to minimize the fatigue loads experienced by the WTs while tracking $P_{\text{ref}}^{\text{wfc}}$ all the time. The $P_{\text{ref}}^{\text{wfc}}$ tracking is regarded as an equality constraint, described in Section VI-B. The minimization of the fatigue loads implies the minimization of the variation of T_s and F_t , which is included in the cost function.

By defining the control vector u_{ref} ,

$$u_{\text{ref}} \triangleq [\Delta P_{\text{ref}}^{\text{wt},1}, \dots, \Delta P_{\text{ref}}^{\text{wt},N_{\text{wt}}}]', \quad u_{\text{ref}} \in \mathbb{R}^{N_{\text{wt}} \times 1},$$

the optimization problem can be formulated as,

$$\begin{aligned} \min_{u_{\text{ref}}} \sum_{i=1}^{N_{\text{wt}}} & \underbrace{\|u_{\text{ref}}^i + P_{g0}^i - \alpha_i P_{\text{ref}}^{\text{wfc}}\|_{Q_P}^2}_{\text{Term 1}} \\ & + \underbrace{\left\| \frac{\partial T_s^i}{\partial P_{\text{ref}}^{\text{wt},i}} u_{\text{ref}}^i \right\|_{Q_{T_s}}^2}_{\text{Term 2}} + \underbrace{\left\| \frac{\partial F_t^i}{\partial P_{\text{ref}}^{\text{wt},i}} u_{\text{ref}}^i \right\|_{Q_{F_t}}^2}_{\text{Term 3}}, \end{aligned} \quad (58)$$

where Q_P is the weighting factor which penalizes the deviation of $P_{\text{ref}}^{\text{wt},i}$ to its proportional value, Q_{T_s} is the weighting factor which penalizes the variation of T_s , and Q_{F_t} is the weighting factor which penalizes the variation of F_t .

As shown in Term 1 of (58), u_{ref}^i is around $\alpha_i P_{\text{ref}}^{\text{wfc}} - P_{g0}^i$. Therefore, by assuming $u_{\text{ref}}^i \approx \alpha_i P_{\text{ref}}^{\text{wfc}} - P_{g0}^i$, the case index of the system during the control interval (Case 1~Case 4) in Subsection V-B and Subsection V-C could be estimated. Accordingly, S^{T_s-i} and S^{F_t-i} could be decided. Term 2 and Term 3 in (58) can be transformed into,

$$\min_{u_{\text{ref}}} \sum_{i=1}^{N_{\text{wt}}} \|S^{T_s-i} u_{\text{ref}}^i + Y^{T_s-i}\|_{Q_{T_s}}^2 + \|S^{F_t-i} u_{\text{ref}}^i + Y^{F_t-i}\|_{Q_{F_t}}^2. \quad (59)$$

B. Constraints

The constraints are summarized as follows:

1) *Power Reference Tracking*: According to $P_{\text{ref}}^{\text{wfc}}$, the total power reference increments of WTs should follow,

$$\sum_{i=1}^{N_{\text{wt}}} u_{\text{ref}}^i = P_{\text{ref}}^{\text{wfc}} - P_{\text{wfc}}, \quad (60)$$

where P_{wfc} is the measured output of the wind farm.

2) *Local WT Constraint*: For individual WTs, there exists the available power limit,

$$u_{\text{ref}} \in [-P_{g0}, P_{\text{avi}}^{\text{wt}} - P_{g0}]. \quad (61)$$

For generality, the turbine index i is omitted.

Besides, as mentioned in Subsection VI-A, the case index of the system is estimated based on $\alpha P_{\text{ref}}^{\text{wfc}} - P_{g0}$. Accordingly, u_{ref} should be limited in the local constraint to guarantee that the system will be in the estimated case, i.e.,

$$\begin{cases} \text{If } \alpha P_{\text{ref}}^{\text{wfc}} - P_{g0} \leq \Delta P_{\text{I} \rightarrow \text{II}}^{\text{wt}} (\text{Case 1}), u_{\text{ref}} \leq \Delta P_{\text{I} \rightarrow \text{II}}^{\text{wt}}, \\ \text{If } \alpha P_{\text{ref}}^{\text{wfc}} - P_{g0} > \Delta P_{\text{II} \rightarrow \text{I}}^{\text{wt}} (\text{Case 2}), u_{\text{ref}} > \Delta P_{\text{II} \rightarrow \text{I}}^{\text{wt}}, \\ \text{If } \alpha P_{\text{ref}}^{\text{wfc}} - P_{g0} > \Delta P_{\text{I} \rightarrow \text{II}}^{\text{wt}} (\text{Case 3}), u_{\text{ref}} > \Delta P_{\text{I} \rightarrow \text{II}}^{\text{wt}}, \\ \text{If } \alpha P_{\text{ref}}^{\text{wfc}} - P_{g0} \leq \Delta P_{\text{II} \rightarrow \text{I}}^{\text{wt}} (\text{Case 4}), u_{\text{ref}} \leq \Delta P_{\text{II} \rightarrow \text{I}}^{\text{wt}}. \end{cases} \quad (62)$$

By merging (61) and (62), the feasible operation range of u_{ref} can be derived,

$$u_{\text{ref}} \in [u_{\min}, u_{\max}]. \quad (63)$$

Accordingly, $P_{\min}^{\text{wt}} = P_{g0} + u_{\min}$ and $P_{\max}^{\text{wt}} = P_{g0} + u_{\max}$.

The derived optimization problem can be reformulated as a standard Quadratic Programming (QP) problem, whose rank is equal to the number of WTs. It can be efficiently solved by a number of commercial solvers.

C. Discussion

The computation task of the optimal wind farm control mainly consists of formulating and solving the optimal problem. Accordingly, the improvement with the proposed method can be described in the following two aspects.

1) *Formulation of the optimal problem:* With the proposed method, the operation region can be determined according to the measurements. Accordingly, the offline calculated parameters of the region can be derived and the load sensitivities can be calculated based on the explicit equations. As such, a part of the computation burden required for the online computation can be removed. Moreover, the task has been distributed to local controllers, which can be solved in parallel. With increasing the number of WTs, this efficiency improvement becomes higher. Therefore, the dedicated controller is computationally viable for implementation in large wind farms.

2) *Solution of the optimal problem:* The time complexity, expressed by $\mathcal{O}$, is used to indicate the amount of time taken by an algorithm. As mentioned in [29], QP problems can be solved roughly with the same efficiency as LP problems. The time complexity of the practical algorithm to solve LP problem with n variables and m constraints requires roughly $\mathcal{O}(n^3 m^{0.5} + n^2 m^{1.5})$. Compared with the method in [14], the formulated optimal problem of the proposed method has reduced optimization variables ($n = N_{wt}$) and constraints ($m = N_{wt} + 1$). The corresponding time complexity of the proposed method is less.

VII. CASE STUDIES

A wind farm comprised of 10×5 MW WTs is used as the test system. The wind field modeling considering turbulences and wake effects for the wind farm is generated from SimWind-Farm [21]. The control period of the wind farm control t_s is set as 1 s.

Fig. 7. P_{avi}^{wfc} and P_{wfc}^{ref} under both low and high wind conditions.

In order to test the efficacy of the developed dispatch algorithm, the operation of the wind farm under both low and high conditions were studied. The available power of the wind farm P_{avi}^{wfc} under both conditions is shown in Fig. 7. The typical active control scheme, balance control mode, is used in this study, where the wind farm production is reduced to specified constant levels [30]. The simulation results of the proposed optimal algorithm (“OPT”) are compared with the conventional proportional dispatch algorithm in [7] (“CON”).

The dynamic turbine behavior in a simulated wind field yields time series of loads or stresses. Through post-processing, the fatigue cycles based on the rainflow counting method is derived to evaluate the performance of the proposed scheme [31]. Besides, the Damage Equivalent Load (DEL), based on Miner’s rule and dependent on materials properties specified by the slope of the S-N curve, is used to quantify the load minimization. In this study, the related calculations are completed by MCrunch, developed by NREL [32].

A. Decision of Weighting Factors

The control objective of the cost function (58) consists of the following two parts, which represent the minimization of ΔT_s and ΔF_t , respectively,

$$\text{Obj1} \triangleq \sum_{i=1}^{N_{wt}} \|\Delta T_s^i\|^2, \text{Obj2} \triangleq \sum_{i=1}^{N_{wt}} \|\Delta F_t^i\|^2. \quad (64)$$

The weighting factors for Obj1 and Obj2 are Q_{T_s} and Q_{F_t} . They can be considered as a whole part, which represents the load minimization of the wind farm. By defining $Q_{Load} \triangleq Q_{T_s} + Q_{F_t}$, it is obvious that larger $\frac{Q_{Load}}{Q_P}$ can lead to a better performance of the load alleviation. In this study, $Q_P = 1$ and $Q_{Load} = 600$. By defining $\gamma \triangleq \frac{Q_{T_s}}{Q_{Load}}$,

$$Q_{T_s} = \gamma Q_{Load}, Q_{F_t} = (1 - \gamma) Q_{Load}. \quad (65)$$

Fig. 8 shows the Pareto frontier under both low and high wind conditions. By increasing the ratio γ , Obj1 decreases while Obj2 increases. For the low wind condition, it can be observed that $\gamma = 0.0017$ is the optimum solution. A significant reduction of ΔF_t (Obj2) can be observed, which is from 1 to 0.33 (67%). Comparably, the reduction of ΔT_s (Obj1) is not sensitive, which is from 1 to 0.81 (19%). For the high wind condition, it can be observed that $\gamma = 0.003$ is the optimum solution. The reduction of ΔF_t (Obj2) is from 1 to 0.83 (17%). Comparably, the reduction of ΔT_s (Obj1) is similar, which is from 1 to 0.84 (16%).

Fig. 8. Pareto frontier under low and high wind conditions.

It can be observed that the optimum γ is related to the available power. In this study, γ is adaptive to different wind conditions and can be approximately calculated by,

$$\gamma \approx \frac{\sum_{i=1}^{N_{wt}} P_{avi_max}^{wfc}}{18000}, P_{avi_max}^{wfc} = 0.5\pi\rho R^2 v_r^3 C_p^{max}, \quad (66)$$

where $C_p^{\max}$ is the maximum power coefficient. The unit of $P_{\text{avi}}^{\text{wt}}$ is in MW. Accordingly, Q_{T_s} and Q_{F_t} can be derived, which are used for the following case scenarios.

B. Operation under Low Wind Condition

The average wind speeds of all WTs (v_{avr}) in the wind farm are listed in Table II, which range from 8.85 m/s to 9.97 m/s. As shown in Fig. 9, three scenarios are defined according to different $P_{\text{ref}}^{\text{wfc}}$: $P_{\text{ref}}^{\text{wfc}} = 20$ MW (Scenario 1), $P_{\text{ref}}^{\text{wfc}} = 17.5$ MW (Scenario 2), and $P_{\text{ref}}^{\text{wfc}} = 15$ MW (Scenario 3). The simulation time is 300 s.

Fig. 9. $P_{\text{avi}}^{\text{wfc}}$ and $P_{\text{ref}}^{\text{wfc}}$ under the low wind condition.

1) *Power Reference Tracking*: To evaluate the tracking performance, the Root Mean Square Errors (RMSEs) for both algorithms are calculated and listed in Table I. Both values are identical and quite small, which implies the same tracking performances of both algorithms.

TABLE I
RMSE COMPARISON UNDER LOW WIND CONDITION

Scenario	CON	OPT
Scenario 1	0.012 MW	0.012 MW
Scenario 2	0.003 MW	0.003 MW
Scenario 3	0.003 MW	0.003 MW

2) *Fatigue Loads Reduction*: Firstly, more details of the simulation result for Scenario 2 are shown. A representative WT (WT08) is used as an example. The variations of T_s with the two algorithms are shown in Fig. 10(a). Compared with the CON, the variation of the shaft torque ΔT_s is reduced with the OPT. According to the cumulative rainflow cycles in Fig. 10(b), less cycles are found for the OPT, which implies less fatigue loads experienced by the WT.

The variations of M_t with the two algorithms are shown in Fig. 11(a). Compared with the CON, the variation of ΔM_t is reduced with the OPT. According to the cumulative rainflow cycles in Fig. 11(b), less cycles are found in the large tower bending moment for the OPT, which implies less fatigue loads experienced by the WT.

The calculated DELs of T_s and M_t for all WTs are listed in Table II and III, respectively. As shown in Table II, with the OPT, most DELs are reduced. From the whole wind farm point of view, the total DEL of T_s is reduced by 2.11%. Similarly,

Fig. 10. T_s of WT08 for Scenario 2.

Fig. 11. M_t of WT08 for Scenario 2.

as shown in Table III, most DELs are reduced. The reduction of the total DEL of M_t is 11.36%.

The simulation results of Scenario 1–3 are summarized in Table IV. As mentioned in Section VII-A, ΔF_t is more sensitive under the load wind condition. Therefore, for the DELs of M_t , the reductions of the OPT are significant, which range from 11.36% to 13.32%. Comparably, the changes of the DELs of T_s for the OPT are limited, which range from 0.73% to -2.11% .

C. Operation under High Wind Condition

The average wind speeds of all WTs (v_{avr}) in the wind farm are listed in Table VI, which range from 12.85 m/s to 13.97 m/s. As shown in Fig. 12, three scenarios are defined according to different $P_{\text{ref}}^{\text{wfc}}$: $P_{\text{ref}}^{\text{wfc}} = 45$ MW (Scenario 4),

TABLE II
DELS OF WTs (T_s) FOR SCENARIO 2

No.	v_{avr} in m/s	DEL (CON) in MNm	DEL (OPT) in MNm	Percentage
WT01	8.85	1.88	1.86	-1.06%
WT02	9.09	2.10	2.07	-1.43%
WT03	9.46	1.75	1.64	-6.29%
WT04	9.10	1.86	1.74	-6.45%
WT05	9.75	1.47	1.51	2.72%
WT06	9.09	1.59	1.57	-1.26%
WT07	9.50	1.93	1.88	-2.59%
WT08	9.97	1.54	1.51	-1.95%
WT09	9.24	1.95	1.91	-2.05%
WT10	9.45	2.39	2.38	-0.42%
Summary		18.46	18.07	-2.11%

TABLE III
DELS OF WTs (M_t) FOR SCENARIO 2

No.	v_{avr} in m/s	DEL (CON) in MNm	DEL (OPT) in MNm	Percentage
WT01	8.85	26.70	26.00	-2.62%
WT02	9.09	31.72	25.15	-23.87%
WT03	9.46	27.77	21.19	-23.69%
WT04	9.10	34.94	27.95	-20.01%
WT05	9.75	19.35	20.16	4.19%
WT06	9.09	18.86	19.29	-2.28%
WT07	9.50	20.42	21.64	5.97%
WT08	9.97	22.82	20.02	-12.27%
WT09	9.24	33.41	30.32	-9.25%
WT10	9.45	33.40	28.06	-15.99%
Summary		269.39	238.78	-11.36%

TABLE IV
COMPARISON OF DELS FOR DIFFERENT SCENARIOS

Scenario	Type	DEL (CON) in MNm	DEL (OPT) in MNm	Percentage
Scenario 1	T_s	21.94	22.20	0.73%
	M_t	404.16	350.34	-13.32%
Scenario 2	T_s	18.46	18.07	-2.11%
	M_t	269.39	238.78	-11.36%
Scenario 3	T_s	14.86	14.82	-0.27%
	M_t	213.19	187.63	-11.99%

$P_{ref}^{wfc} = 42.5$ MW (Scenario 5), and $P_{ref}^{wfc} = 40$ MW (Scenario 6). The simulation time is 300 s.

1) *Power Reference Tracking*: To evaluate the tracking performance, the RMSEs for both algorithms are calculated and listed in Table V. Both values are quite small, which shows good tracking performances of both algorithms. Most values of the OPT are the same as these of the CON.

2) *Fatigue Loads Reduction*: Firstly, more details of the simulation result for Scenario 5 are shown. A representative WT (WT05) is used as an example. The variations of T_s with the two algorithms are shown in Fig. 13(a). Compared

Fig. 12. P_{avi}^{wfc} and P_{ref}^{wfc} under the high wind condition.

TABLE V
RMSE COMPARISON UNDER HIGH WIND CONDITION

Scenario	CON	OPT
Scenario 4	0.010 MW	0.009 MW
Scenario 5	0.009 MW	0.009 MW
Scenario 6	0.008 MW	0.008 MW

with the CON, the variation of ΔT_s is reduced with the OPT. According to the cumulative rainflow cycles in Fig. 13(b), less cycles are found for the OPT, which implies less fatigue loads experienced by the WT.

Fig. 13. T_s of WT05 for Scenario 5.

The variations of M_t with the two algorithms are shown in Fig. 14(a). Compared with the CON, the variation of ΔM_t is reduced with the OPT. According to the cumulative rainflow cycles in Fig. 14(b), less cycles are found in the large tower moment for the OPT, which implies less fatigue loads experienced by the WT.

The calculated DELs of T_s and M_t for all WTs are listed in Table VI and VII, respectively. As shown in Table VI, compared with the CON, all the DELs are reduced with the OPT. The reduction values are from 0.00% to 39.62%. From

Fig. 14. M_t of WT05 for Scenario 5.

the whole wind farm point of view, the total DEL of T_s is reduced by 14.88%. Similarly, as shown in Table VII, most DELs are reduced. The reduction of the total DEL of M_t is 21.19%.

TABLE VI
DELS OF WTs (T_s) FOR SCENARIO 5

No.	v_{avr} in m/s	DEL (CON) in MNm	DEL (OPT) in MNm	Percentage
WT01	12.85	1.44	1.21	-15.97%
WT02	13.09	1.37	1.19	-13.14%
WT03	13.46	1.35	1.11	-17.78%
WT04	13.10	1.52	1.43	-5.92%
WT05	13.75	0.53	0.32	-39.62%
WT06	13.09	0.61	0.45	-26.23%
WT07	13.50	0.36	0.32	-11.11%
WT08	13.97	0.57	0.57	-0.00%
WT09	13.24	0.45	0.36	-20.00%
WT10	13.45	1.21	1.05	-13.22%
Summary		9.41	8.01	-14.88%

The simulation results of Scenario 4–6 are summarized in Table VIII. Compared with the CON, the DELs of both T_s and M_t with the OPT are reduced significantly. Specifically, for T_s , the reduction values range from 10.97% to 20.77%. For M_t , the reduction values range from 16.24% to 25.37%.

3) *Discussion:* The relation between the DEL value and P_{ref}^{wfc} is analyzed. By taking the DEL value of $P_{ref}^{wfc} = 45$ MW as the reference, different P_{ref}^{wfc} are sampled and the corresponding DELs in p.u. are calculated. According to these points, the fitted curve can be derived based on the nonlinear least square algorithm, as shown in Fig. 15. It can be observed that the DEL can be reduced by decreasing the wind power generation. However, with smaller P_{ref}^{wfc} , the reduction sensitivity becomes smaller. For the wind farm operator, the damage to the WTs might be also considered to decide P_{ref}^{wfc} .

TABLE VII
DELS OF WTs (M_t) FOR SCENARIO 5

No.	v_{avr} in m/s	DEL (CON) in MNm	DEL (OPT) in MNm	Percentage
WT01	12.85	57.75	45.07	-21.96%
WT02	13.09	48.66	46.41	-4.62%
WT03	13.46	46.16	44.13	-4.40%
WT04	13.10	41.88	42.09	0.50%
WT05	13.75	61.38	27.65	-54.95%
WT06	13.09	49.60	26.56	-46.45%
WT07	13.50	27.31	24.39	-10.69%
WT08	13.97	51.74	48.97	-5.35%
WT09	13.24	32.40	28.54	-11.91%
WT10	13.45	54.32	37.54	-30.89%
Summary		471.20	371.35	-21.19%

TABLE VIII
COMPARISON OF DELS FOR DIFFERENT SCENARIOS

Scenario	Type	DEL (CON) in MNm	DEL (OPT) in MNm	Percentage
Scenario 4	T_s	10.67	9.5	-10.97%
	M_t	513.57	430.16	-16.24%
Scenario 5	T_s	9.41	8.01	-14.88%
	M_t	471.20	371.35	-21.19%
Scenario 6	T_s	8.86	7.02	-20.77%
	M_t	431.44	321.99	-25.37%

Sometimes, it might be more beneficial to sacrifice P_{ref}^{wfc} to reduce the damages to the WTs. How to evaluate the economical benefit of the DEL reduction and strike a balance between the DEL reduction and wind power generation will be studied in the future work.

Fig. 15. Relation between DEL and P_{ref}^{wfc} .

VIII. CONCLUSION

In this paper, an optimal dispatch algorithm based on fatigue load sensitivity is developed for the active power control of wind farms. The load sensitivity and feasible range of the power reference for individual WTs are used to formulate the optimal dispatch problem, which are calculated locally. With this configuration, most computation tasks are distributed to the local WT controllers. The complicated wind farm model is not required and the computation burden of the wind farm controller is largely reduced. Moreover, the explicit analytical equations of the load sensitivity are derived to improve the computation efficiency of the local controller. The proposed dispatch algorithm is suitable for real-time control of large-scale wind farms. Case studies show the developed algorithm can achieve good performances of power tracking. Moreover, the fatigue loads experienced by WTs are largely alleviated.

APPENDIX

The parameters of 5 MW wind turbine model are listed in Table IX.

TABLE IX
PARAMETER OF 5 MW WIND TURBINE MODEL

Symbol	Description	value
η	Multiplier ratio	97
R	Rotor blade length (m)	63
H	Height of the rotor center (m)	87.6
J_r	Rotor inertia ($\text{kg}\cdot\text{m}^2$)	$3.544 \cdot 10^7$
J_g	Generator inertia ($\text{kg}\cdot\text{m}^2$)	534.116
k_{sh}	Drive train spring constant ($\text{N}\cdot\text{m}/\text{rad}$)	$8.676 \cdot 10^8$
c_{sh}	Drive train damping constant ($\text{N}\cdot\text{m}\cdot\text{s}/\text{rad}$)	$6.215 \cdot 10^6$
M_{tow}	Integrated tower mass (kg)	$3.475 \cdot 10^5$
ω_{g_rated}	Rated generator speed (rad/s)	122.91
ω_{r_rated}	Rated rotor speed (rad/s)	1.26
θ_{max}	Max. pitch angle (deg)	90
θ_{min}	Min. pitch angle (deg)	0
K_p	Proportional gain of the pitch control	0.2143
K_i	Integral gain of the pitch control	0.0918
K_0	Gain scheduling coefficient	1
K_θ	Gain scheduling coefficient	2.1323

REFERENCES

- [1] I. Pineda *et al.*, "Wind in power-2015 European statistics," EWEA, Brussels, Belgium, Tech. Rep., Feb. 2016.
- [2] M. Kayikci and J. V. Milanović, "Dynamic contribution of DFIG-based wind plants to system frequency disturbances," *IEEE Trans. Power Syst.*, vol. 24, no. 2, pp. 859–867, May 2009.
- [3] C. Wan, Z. Xu, P. Pinson *et al.*, "Probabilistic forecasting of wind power generation using extreme learning machine," *IEEE Trans. Power Syst.*, vol. 29, no. 3, pp. 1033–1044, May 2014.
- [4] C. Wan, Z. Xu, P. Pinson *et al.*, "Optimal prediction intervals of wind power generation," *IEEE Trans. Power Syst.*, vol. 29, no. 3, pp. 1166–1174, May 2014.
- [5] M. Tsili and S. Papathanassiou, "A review of grid code technical requirements for wind farms," *IET Renew. Power Gen.*, vol. 3, no. 3, pp. 308–332, Sep. 2009.

- [6] P. E. Sørensen, A. D. Hansen, K. Thomsen *et al.*, "Operation and control of large wind turbines and wind farms," Risø Nat. Lab., Roskilde, Denmark, Tech. Rep. Risø-R-1532, Sep. 2005.
- [7] P. E. Sørensen, A. D. Hansen, F. Iov *et al.*, "Wind farm models and control strategies," Risø Nat. Lab., Roskilde, Tech. Rep. Risø-R-1464, Aug. 2005.
- [8] Z. Lubosny and J. W. Bialek, "Supervisory control of a wind farm," *IEEE Trans. Power Syst.*, vol. 22, no. 3, pp. 985–994, Jul. 2007.
- [9] N. Khezami, N. B. Braiek, and X. Guillaud, "Wind turbine power tracking using an improved multimodel quadratic approach," *ISA Trans.*, vol. 49, no. 3, pp. 326–334, Jul. 2010.
- [10] H. Camblong, S. Nourdine, I. Vechiu, and G. Tapia, "Control of wind turbines for fatigue loads reduction and contribution to the grid primary frequency regulation," *Energy*, vol. 48, no. 1, pp. 284–291, Dec. 2012.
- [11] J. B. Berglind, R. Wisniewski, and M. Soltani, "Fatigue load modeling and control for wind turbines based on hysteresis operators," in *IEEE American Control Conf.*, Chicago, IL, 2015, pp. 3721–3727.
- [12] V. Spudić, M. Jelavić, and M. Baotić, "Wind turbine power references in coordinated control of wind farms," *Automatika—Journal for Control, Measurement, Electronics, Computing and Communications*, vol. 52, no. 2, pp. 82–94, Jul. 2011.
- [13] V. Spudić, M. Jelavić, M. Baotić *et al.*, "Hierarchical wind farm control for power/load optimization," in *The Science of making Torque from Wind (Torque2010)*, Heraklion, Greece, 2010.
- [14] V. Spudić, "Coordinated optimal control of wind farm active power," Ph.D. dissertation, Dept. Control Comput. Eng., Univ. of Zagreb, Zagreb, Croatia, 2012.
- [15] B. Biegel, D. Madjidian, V. Spudić *et al.*, "Distributed low-complexity controller for wind power plant in derated operation," in *IEEE Int. Conf. Control Applicat. (CCA)*, Hyderabad, India, 2013, pp. 146–151.
- [16] H. Zhao, Q. Wu, Q. Guo *et al.*, "Distributed model predictive control of a wind farm for optimal active power control- Part I: Clustering-based wind turbine model linearization," *IEEE Trans. Sustain. Energy*, vol. 6, no. 3, pp. 831–839, Jul. 2015.
- [17] H. Zhao, Q. Wu, Q. Guo *et al.*, "Distributed model predictive control of a wind farm for optimal active power control-Part II: Implementation with clustering-based piece-wise affine wind turbine model," *IEEE Trans. Sustain. Energy*, vol. 6, no. 3, pp. 840–849, Jul. 2015.
- [18] V. Spudić, C. Conte, M. Baotić *et al.*, "Cooperative distributed model predictive control for wind farms," *Optim. Control Appl. Methods*, vol. 36, no. 3, pp. 333–352, May 2015.
- [19] T. Knudsen, T. Bak, and M. Svenstrup, "Survey of wind farm controlpower and fatigue optimization," *Wind Energy*, vol. 18, no. 8, pp. 1333–1351, Aug. 2015.
- [20] J. M. Jonkman, S. Butterfield *et al.*, "Definition of a 5-MW reference wind turbine for offshore system development", Nat. Renew. Energy Lab., Denver, CO, Tech. Rep. NREL/TP-500-38060, Feb. 2009.
- [21] J. D. Grunnet, M. Soltani, T. Knudsen *et al.*, "Aeolus toolbox for dynamic wind farm model, simulation and control," in *The European Wind Energy Conf. & Exhib.*, Warsaw, Poland, Apr. 2010.
- [22] M. Vašak, N. Hure, and N. Perić, "Identification of a discrete-time piecewise affine model of a pitch-controlled wind turbine," in *Proc. the 34th Int. Conv. MIPRO*, Opatija, Croatia, May 2011, pp. 744–749.
- [23] *Handbook of wind power systems*, Springer, Berlin, Germany, Jan. 2014.
- [24] O. Anaya-Lara, N. Jenkins *et al.*, *Wind energy generation: modelling and control*, Chichester, UK: John Wiley & Sons Ltd, Jul. 2009.
- [25] J. F. Manwell, J. G. McGowan *et al.*, *Wind energy explained: theory, design and application*, 2nd ed., Chichester, UK: John Wiley & Sons Ltd, Dec. 2009.
- [26] T. K. Barlas and G. Van Kuik, "Review of state of the art in smart rotor control research for wind turbines," *Prog. Aerosp. Sci.*, vol. 46, no. 1, pp. 1–27, Jan. 2010.
- [27] M. N. Soltani, T. Knudsen, M. Svenstrup *et al.*, "Estimation of rotor effective wind speed: A comparison," *IEEE Trans. Control Syst. Technol.*, vol. 21, no. 4, pp. 1155–1167, Jun. 2013.
- [28] T. Ackermann *et al.*, *Wind power in power systems*, 2nd ed., Chichester, UK: John Wiley & Sons Ltd, Jan. 2005.
- [29] M. Baotić, "Optimal control of piecewise affine systemsa multi-parametric approach," Ph.D. dissertation, ETH Zürich, Zürich, Switzerland, Jul. 2005.
- [30] I. Munteanu, A. Bratcu *et al.*, *Optimal control of wind energy systems: towards a global approach*, 1st ed., London, UK: Springer, 2008.
- [31] *Wind energy handbook*, 2nd ed., John Wiley & Sons Ltd, Chichester, UK, May 2011.
- [32] *MCrunch user's guide for version 1.00*, 1st ed., Nat. Renew. Energy Lab., Denver, CO, May 2008.

Haoran Zhao (S'12-M'15) received the B.E. degree in electrical engineering and automation from Shandong University, Jinan, China, in 2005, the M.E. degree in electrical engineering and automation from the Technical University of Berlin, Berlin, Germany, in 2009, and the Ph.D. degree in electrical engineering from the Technical University of Denmark, Kgs. Lyngby, Denmark, in 2015.

He is a Postdoc with the Center for Electric Technology, Technical University of Denmark. He worked as Electrical Engineer with State Grid Corporation of China (SGCC), Beijing, China, in 2005. From 2010 to 2011, he worked as Application Developer with DlgSILENT GmbH, Gomarinen, Germany. His research interests include modeling and integration study of wind power, control of energy storage system, and voltage stability analysis.

Mohammad Shahidehpour (F'01) is the Bodine Chair Professor with the Department of Electrical and Computer Engineering, the Director of the Robert W. Galvin Center for Electricity Innovation, and an Associate Director of WISER with the Illinois Institute of Technology, Chicago, IL, USA.

He was a recipient of the IEEE PES Outstanding Power Engineering Educator Award, the IEEE PES Outstanding Engineer Award, and the Chicago Chapter. He is the Holder of Nourbakhshian Endowed Chair Professorship, University of Kashan, Iran, and Otto Monsted Professorship, Technical University of Denmark. He is a Research Professor with King Abdulaziz University, Saudi Arabia, the Sharif University of Technology, Iran, as well as several universities in China, including Tsinghua University, Xian Jiaotong University, Nanjing University, North China Electric Power University, and Hunan University. He is an IEEE PES Distinguished Lecturer, and served as the VP of Publications for the IEEE Power and Energy Society, the Editor-in-Chief of the IEEE TRANSACTIONS ON POWER SYSTEMS, and the Founding Editor-in-Chief of the IEEE TRANSACTIONS ON SMART GRID.

Dr. Shahidehpour is a member of the U.S. National Academy of Engineering.

Qiuwei Wu (M'08-SM'15) obtained the B. Eng. and M. Eng. in Power System and Its Automation from Nanjing University of Science and Technology, Nanjing, China, in 2000 and 2003, respectively. He obtained the PhD degree in Power System Engineering from Nanyang Technological University, Singapore, in 2009.

He was a senior R&D engineer with VESTAS Technology R&D Singapore Pte Ltd from Mar. 2008 to Oct. 2009. He has been working at Department of Electrical Engineering, Technical University of Denmark (DTU) since Nov. 2009 (PostDoc Nov. 2009-Oct. 2010, Assistant Professor Nov. 2010-Aug. 2013, Associate Professor since Sept. 2013). He was a visiting scholar at Department of Industrial Engineering & Operations Research (IEOR), University of California, Berkeley, from Feb. 2012 to May 2012 funded by Danish Agency for Science, Technology and Innovation (DASTI), Denmark. He has been a visiting professor named by Y. Xue, an Academician of Chinese Academy of Engineering, at Shandong University, China, since Nov. 2015.

His research interests are smart grids, wind power, electric vehicle, active distribution networks, electricity market, and smart energy systems. He is an Editor of IEEE Transactions on Smart Grid and IEEE Power Engineering Letters. He is also an Associate Editor of International Journal of Electrical Power and Energy Systems.

Qinglai Guo (M'09-SM'14) was born in Jilin, China, on March 6, 1979. He received the B.S. and Ph.D. degrees in electrical engineering from Tsinghua University, Beijing, China, in 2000 and 2005, respectively.

He is currently an Associate Professor with Tsinghua University. His research interests include smart grids, cyber-physical systems, and electrical power control center applications.

Prof. Guo is a member of CIGRE C2.13 Task Force on Voltage/Var support in System Operations.

Hongbin Sun (M'00-SM'12) received double B.S. degrees in electrical engineering and physics from Tsinghua University, Beijing, China, in 1992, and the Ph.D. degree in electrical engineering from Tsinghua University in 1997.

He is now the Changjiang Scholar of Education Ministry of China, full Professor of Electrical Engineering with Tsinghua University and Assistant Director with the State Key Laboratory of Power Systems, China. From 2007 to 2008, he was a Visiting Professor with the School of EECS at Washington State University, Pullman, WA, USA. He has authored more than 300 academic papers. His research interests include smart grids, renewable generation integration, and electrical power control center applications.

He is a Fellow of IET. He is a member of IEEE PES CAMS Cascading Failure Task Force and CIGRE C2.13 Task Force on Voltage/Var support in System Operations. He was the recipient of the China National Technology Innovation Award in 2008, the National Distinguished Teacher Award in China in 2009, and the National Science Fund for Distinguished Young Scholars of China in 2010.

Shaojun Huang (S'13) obtained the B.Eng. from the Department of Electrical Engineering, Tsinghua University, Beijing, China, in 2001. He obtained the MSc from the Department of Energy Technology, Aalborg University, Denmark, in 2013.

Currently, he is a Postdoc in the Centre for Electric Power and Energy, Department of Electrical Engineering, Technical University of Denmark.

His research interests are congestion management for distribution networks with high penetration of distributed energy resources.