



## **Annual variations in GPS-measured vertical displacements near Upernavik Isstrøm (Greenland) and contributions from surface mass loading**

Annual GPS Verticals in Greenland

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## RESEARCH ARTICLE

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## Key Points:

- Atmospheric pressure loading contributes to half of the GPS vertical displacements at annual periods
- Annual verticals are sensitive to ice mass balance over 85% of the entire ice sheet
- Differential verticals between stations are useful to constrain ice mass changes within 120 km

## Supporting Information:

- Supporting Information S1

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## Annual variations in GPS-measured vertical displacements near Upernavik Isstrøm (Greenland) and contributions from surface mass loading

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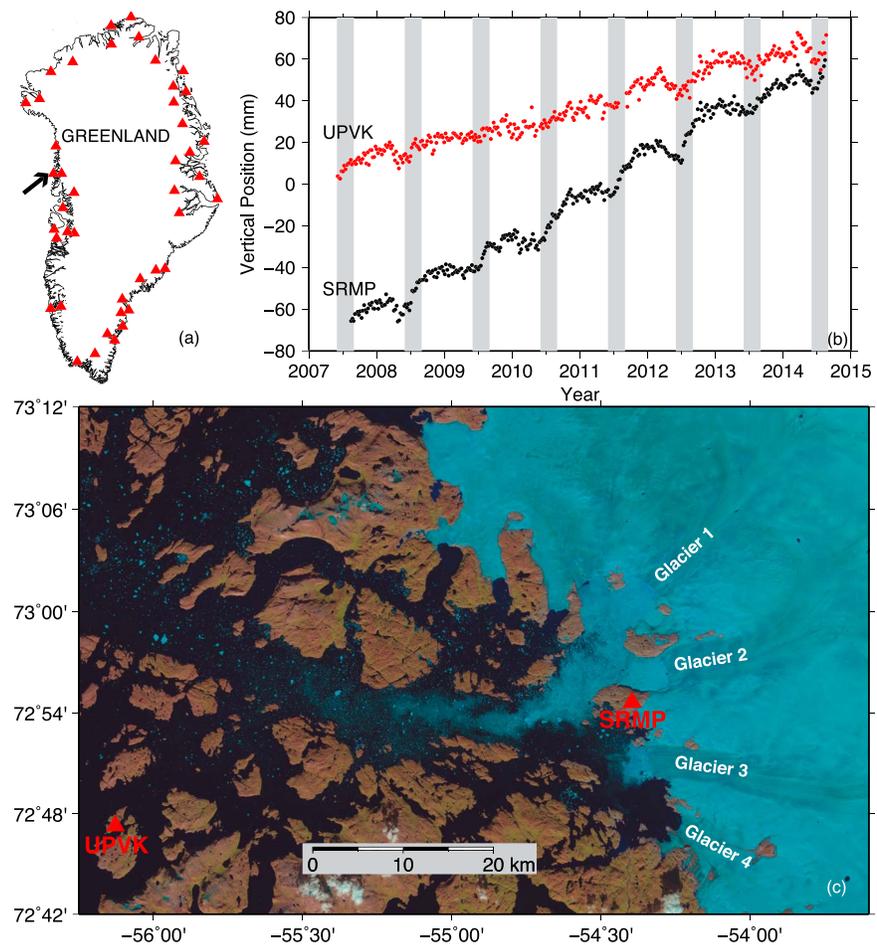
**Abstract** In response to present-day ice mass loss on and near the Greenland Ice Sheet, steady crustal uplifts have been observed from the network of Global Positioning System (GPS) stations mounted on bedrock. In addition to the secular uplift trends, the GPS time series also show prominent annual variability. Here we examine the annual changes of the vertical displacements measured at two GPS stations (SRMP and UPVK) near Upernavik Isstrøm in western Greenland. We model elastic loading displacements due to various surface mass loading including three nonice components: atmospheric pressure, ocean bottom pressure, continental water storage, and one ice component, i.e., surface mass balance (SMB). We find that the contribution from atmospheric pressure changes can explain 46% and 78% of the annual amplitude observed in the GPS verticals at SRMP and UPVK, respectively. We also show that removing the predicted loading displacements due to SMB adversely increases the annual variance of the GPS residuals. However, using the GPS data alone, we cannot identify the exact cause(s) of this discrepancy because the annual loading displacements are sensitive to the SMB changes from over 85% of the ice sheet area. Alternatively, by differencing vertical displacements between the two stations, we find a good agreement between the modeled differential SMB loading displacements and the GPS residuals after removing nonice components. Our study highlights the necessity of correcting for nonice loading contributions in the GPS measurements of crustal deformation to infer ice mass changes in Greenland at annual periods.

### 1. Introduction

Since 2007, more than 50 continuous Global Positioning System (GPS) stations have been established around the Greenland Ice Sheet (GrIS) in a network called GNET (Figure 1a). These stations, mounted on bedrock, aim to measure the solid Earth's response to glacial mass changes on the ice sheet. Specifically, there are two geophysical signals of primary concern: the visco-elastic response of the Earth to glacial history over the past thousands of years in a global scale, or the glacio-isostatic adjustment (GIA), and the elastic response to present-day variations on and near the GrIS. Using GPS data at pre-GNET stations in Greenland, earlier studies used the observed uplift and subsidence to quantify both elastic and visco-elastic processes [e.g., Wahr *et al.*, 2001; Khan *et al.*, 2007, 2008; Jiang *et al.*, 2010; Khan *et al.*, 2016].

In a network-wide study, Bevis *et al.* [2012] reported steady uplift at all the GNET stations in the past few years, predominantly due to the ongoing ice mass loss. Several local-scale studies used uplift at individual stations to infer multiyear mass loss from nearby outlet glaciers [e.g., Khan *et al.*, 2010; Nielsen *et al.*, 2012; Bevan *et al.*, 2015]. For instance, Figure 1b shows the time series of GPS vertical coordinates at two stations, both of which exhibit strong uplift trends. Such trends are caused by the secular mass loss from the nearby glaciers [Nielsen *et al.*, 2012].

In addition to the secular uplift trends, the GNET GPS time series also show prominent annual variability [Bevis *et al.*, 2012]. The observed annual variability, if due to surface mass loading, must be purely elastic and synchronous with the surface mass changes. Bevis *et al.* [2012] argued that the annual cycle of displacement recorded by all GNET stations is driven by both seasonal cycles in ice mass and seasonal cycles in air mass. We confirm this hypothesis by using two GNET stations to show that the maximum of the annual uplift cycle occurs roughly 3 months after the minimum of the annual ice mass cycle. We postulate that this phase offset



**Figure 1.** (a) Map of GNET stations (red triangles) around Greenland. The arrow points to the area near Upernavik Isstrøm. (b) Time series of vertical positions measured at GPS stations SRMP (black) and UPVK (red). The gray bars denote June–July–August (JJA) in each year (same in all the time series plots shown in this paper). (c) A Landsat image of Upernavik Isstrøm taken on 30 July 2015. Red triangles mark the location of the two GPS stations. Snow and ice appear in blue.

arises because various surface mass components, including ice, atmosphere, and water (on land and in the ocean), would all contribute to the amplitude and phase of the annual crustal deformation. However, there has been a lack of assessment of the annual loading from these various sources at individual GNET stations, which hinders the detection and subsequent analysis of glacial mass variability at annual scales in the GPS coordinate time series. Mismodeling of annual loading signals may also introduce uncertainties in the estimation of secular deformation trends [Santamaría-Gómez and Mémin, 2015].

In this paper, we study the annual GPS vertical coordinate time series (hereafter referred to as “GPS data”) with the primary goal of separating the nonice and ice loading sources by modeling the contributions from atmospheric pressure (ATM), ocean bottom pressure (OBP), and continental water storage (CWS). Here we only use two GPS stations near Upernavik Isstrøm on the western coast of Greenland. This local-scale study facilitates detailed analyses and comparisons of various loading contributions. A local perspective also allows us to ignore complications in the observations of uplift due to the significant spatial variability expected from different surface mass components on and near the ice sheet. Also, by taking the difference between these two nearby stations, we would eliminate some common errors in the GPS data.

The second goal of this paper is to assess the possibility of further distinguishing between crustal deformation driven by changes in surface mass balance (SMB) and by glacial dynamics through an SMB model. SMB is the difference between accumulation processes (such as snowfall) and ablation processes (such as surface melting that becomes runoff). Accumulation and runoff are well known to vary strongly at annual and interannual time scales, largely driven by changes in weather conditions [Abdalati and Steffen, 2001; Hanna et al., 2011]. Glacial

dynamics refers to the flow of ice from the interior of the ice sheet outward through outlet and land-terminating glaciers. Numerous studies have reported marked seasonal changes in ice dynamics at many major outlet glaciers and also near the margin of the ice sheet [e.g., *Joughin et al.*, 2008; *Sole et al.*, 2011]. These seasonal changes of ice motions redistribute ice mass and alter total mass balance at outlet glaciers.

## 2. Study Area and Method

### 2.1. Upernavik Isstrøm and the Nearby GPS Stations

Upernavik Isstrøm consists of four glaciers, denoted as Glaciers 1–4 proceeding from north to south (Figure 1c). In 2011, the GPS station SRMP (54.3937°W, 72.9107°N) was located only 1.5 km west of the Glacier 2's frontal position, whereas UPVK (56.1280°W, 72.7883°N) is on an island 65 km further west of the glaciers.

Previous studies have focused on quantifying multiyear changes of this glacier complex [*Nielsen et al.*, 2012; *Khan et al.*, 2013]. They have estimated an ice mass loss rate of 6.7 Gt/yr for the period of 2005–2010, with dynamic changes accounting for 80% of the total mass loss and the remaining 20% due to negative SMB. However, the four glaciers have exhibited asynchronous dynamical changes in the past decade; significant retreat and speedup have been observed at Glacier 1 with only moderate or little change at the other three glaciers [*Nielsen et al.*, 2012; *Andresen et al.*, 2014; *Larsen et al.*, 2016].

### 2.2. GPS Data Analysis

We process the GPS data using conventional methods detailed in *Khan et al.* [2010]. We use the GIPSY-OASIS v6.3 software package developed at the Jet Propulsion Laboratory (JPL). We use the JPL final orbit products and take the satellite antenna phase center offsets into account (antenna phase center file igs08\_1869.atx). The atmospheric delay parameters are calculated from the global VMF1FGRID grid files at 6 h intervals [*Boehm et al.*, 2006; *Kouba*, 2008]. We apply the second-order ionospheric correction. At the operational level of GPS data analysis, we remove the ocean tidal loading (OTL) displacements calculated using the online automatic loading provider [*Scherneck and Bos*, 2002], applied to the Finite Element Solution 2004 ocean tide model. The OTL displacements are in a reference frame fixed to the center of mass. We estimate uncertainties in the daily GPS positioning solutions by accounting for temporally correlated errors as a combination of Gaussian and flicker noise [*Williams et al.*, 2004; *Khan et al.*, 2010]. We use an elevation-dependent weighting function (sine of elevation angle) in the error estimation. We obtain time series of daily positioning solutions and their errors in the local east, north, and up directions in the International Global Navigation Satellite Systems Service 2008 (IGS08) frame [*Altamimi et al.*, 2012]. In this realization of the International Terrestrial Reference Frame, the frame origin is in the center of surface figure (CF) at annual time scales [*Dong et al.*, 2003]. The UPVK antenna was replaced on 16 September 2008. We estimate and correct for an offset on this day at this station. For the sake of visual clarity, all the time series figures presented in this paper are resampled to weekly intervals.

Because of our focus on the annual signal, we only analyze and interpret the detrended GPS data. We restrict our analysis to the GPS vertical coordinate time series as the annual amplitudes in these data are about 1 order of magnitude larger than in the horizontal coordinates (more in section 3.1). Using least squares estimation weighted with the GPS positioning errors, we fit and remove a linear trend from each GPS time series. Because we have removed the linear trends, any secular geophysical contributions (such as GIA and tectonic motion) or errors (such as reference frame drift) have also been removed and are thus not considered here.

### 2.3. Modeling Displacements due to Surface Loading

To quantify the glaciological contributions to the annual vertical coordinate signal from the two GPS stations, we must model and remove other nonice loading contributions. Given any grid of surface mass changes, we use the elastic loading Green's functions calculated based on the preliminary reference Earth model (PREM) with continental crust to estimate the displacement response at the two GPS stations [*Dziewonski and Anderson*, 1981; *Jentzsch*, 1997]. Table 1 summarizes the source models we use to quantify surface mass variations, which are described in detail below. The modeled loading displacements are in the frame fixed to the center of mass of the solid Earth, which is close to the CF [*Blewitt*, 2003]. For simplicity, we ignore the difference between these two reference frames (which only introduce differences of up to 0.6% in the modeled time series) and do not transform the loading displacements into the CF. All the loading displacement time series are resampled to match the daily GPS data.

**Table 1.** Source Models of Surface Mass Changes

Surface Mass Component	Source Model	Temporal Intervals	Grid Spacing	Spatial Extent
Atmospheric pressure	NCEP	6 h	2.5° by 2.5°	Global
Ocean bottom pressure	ECCO	12 h	1° by 1° (except near the equator)	80°S–80°N
Continental water storage	GLDAS-Noah	monthly	1° by 1°	Global, excluding ice sheets and permafrost areas
Ice surface mass balance	RACMO2.3	monthly	~11 km by 11 km	Greenland and surroundings (52.1–87.3°N, –120.85–42.35°E)

To derive the surface deformation from atmospheric mass variability we use the surface pressure provided by the National Center for Environmental Prediction (NCEP) reanalysis data [Kalnay *et al.*, 1996]. This data set is provided as a global grid with a spacing of 2.5° by 2.5° and a temporal sampling of 6 h. Because we are only interested in relative temporal changes, we remove a 30 year (1980–2010) mean of atmospheric pressure from each 6 h grid. Finally, we assume that the oceans respond to the atmospheric pressure changes as an inverted barometer (IB) and introduce a globally uniform pressure change at the ocean bottom to conserve ocean mass [van Dam and Wahr, 1987]. For simplicity, in the remainder of this paper, we refer to the combined loading effects due to atmospheric pressure and IB ocean bottom pressure as the atmospheric pressure (ATM) loading.

We use the “Estimating the Circulation and Climate of the Ocean” (ECCO) data set to quantify the non-IB ocean bottom pressure changes, referred to as OBP in the remainder of this paper. The version used is JPL’s Kalman filter (kf66b) series, which assimilates altimetric heights, Expendable Bathythermograph profiles, and other in situ ocean data [Fukumori, 2002; Kim *et al.*, 2007]. The model used is the parallel version of the primitive equation Massachusetts Institute of Technology ocean global circulation model. The data cover the area from 80°S to 80°N. The horizontal grid spacing is 1° over most of the globe except within a band of 20° around the equator. The meridional grid spacing is gradually reduced to 0.3° within 10° of the equator. The ECCO OBP data are provided at 12 h intervals. We note that oceanographic data have poor coverage in the Labrador Sea (southwest off Greenland), which may affect the accuracy of ECCO OBP data.

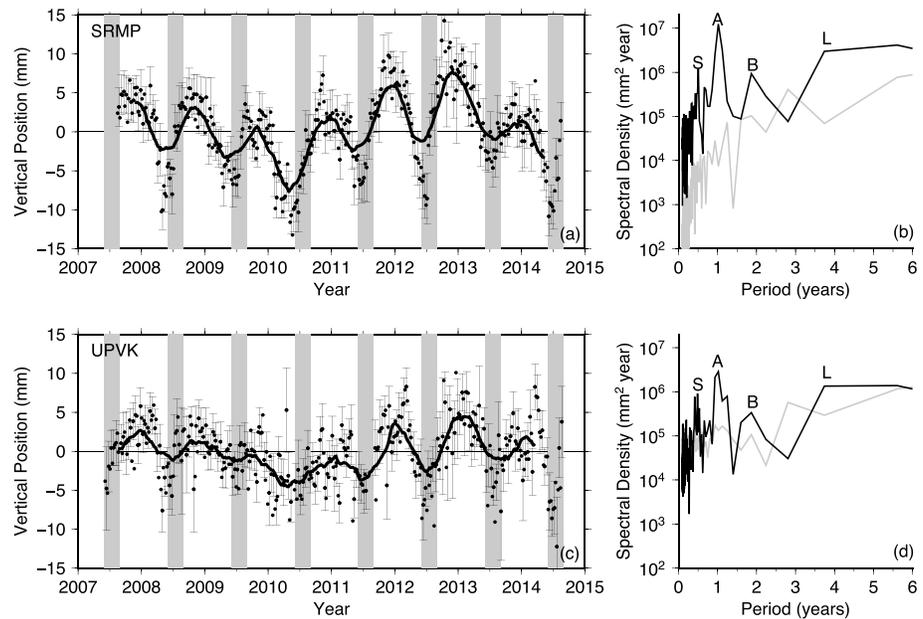
We use the Noah land hydrology model (version 2.7.1) in the Global Land Data Assimilation System (GLDAS) to quantify continental water mass changes at monthly intervals [Rodell *et al.*, 2004] (obtained from <http://grace.jpl.nasa.gov>). The global, 1° by 1° product provides a sum of water stored as soil moisture, snow, and canopy but not including groundwater or the water storage changes in rivers or lakes. It also excludes water storage estimates from the Greenland Ice Sheet and permafrost areas.

To further partition glacial mass changes into SMB and dynamic components, we model loading from SMB using the climate simulation from the Regional Atmospheric Climate Model version 2.3 (RACMO2.3) [Noël *et al.*, 2015]. The monthly SMB fields from 1958 to 2014 are provided on a grid of about 11 km by 11 km. We use the same ice mask as prescribed in RACMO2.3, which is on the same grid as the SMB fields. Following van den Broeke *et al.* [2009], we remove the 1961–1990 mean from the monthly fields, then integrate them over time, and obtain a time series of mass balance for our study period of 2007.5 to 2014.7. The choice of the reference period only influences the secular trend but will have no impact on our detrended time series.

### 3. Results

#### 3.1. GPS Solutions and Modeled Loading Displacements

The detrended GPS time series at SRMP shows a prominent annual signal over the entire 7 years (Figure 2a). Further, we observe a strong peak at the annual period in the power spectrum of the GPS data (see Figure 2b periodogram). In addition to the annual changes, the GPS time series is also characterized by quasi 4-year as well as moderate semiannual and biannual cycles (Figures 2a and 2b). In comparison, the GPS time series at UPVK exhibits similar annual variability but is slightly reduced in amplitude (Figures 2c and 2d). The annual signal weakened between 2007.5 and 2011.5 and became more pronounced afterward. The UPVK periodogram also shows peaks at semiannual, biannual, and quasi 4-year periods (Figure 2d).



**Figure 2.** (a) Time series of detrended vertical positions (black dots) at SRMP. For clarity,  $1\sigma$  uncertainties are shown as error bars at every other GPS solution. The solid line is the smoothed time series after applying a 6 month moving average. (b) Periodogram of the GPS vertical positions at SRMP. “S,” “A,” “B,” and “L” mark the spectrum peaks at the semiannual, annual, biannual, and longer (~4 years) periods, respectively. The gray line is the periodogram of the GPS errors. (c and d) Similar to Figures 2a and 2b, respectively, but for the UPVK station.

To account for these periodicities, we model the detrended GPS time series of vertical coordinates  $H$  as a Fourier series composed of four harmonics:

$$H(t) = \sum_{i=1}^4 A_i \cos \left[ \frac{2\pi}{T_i} (t - t_0^i) \right], \quad (1)$$

where  $t$  is the time (units: days); the four periods ( $T_i, i=1-4$ ) are one solar year (365.24 days), half, two, and four solar years; and  $A_i$  and  $t_0^i$  are the amplitude and phase for the  $i$ th period. Using this model to fit the detrended GPS data, we obtain the best fit annual amplitudes as 4.8 mm and 2.3 mm at SRMP and UPVK, respectively (Table 2). The annual cycles at these two stations peak around 1 December and 1 January, respectively.

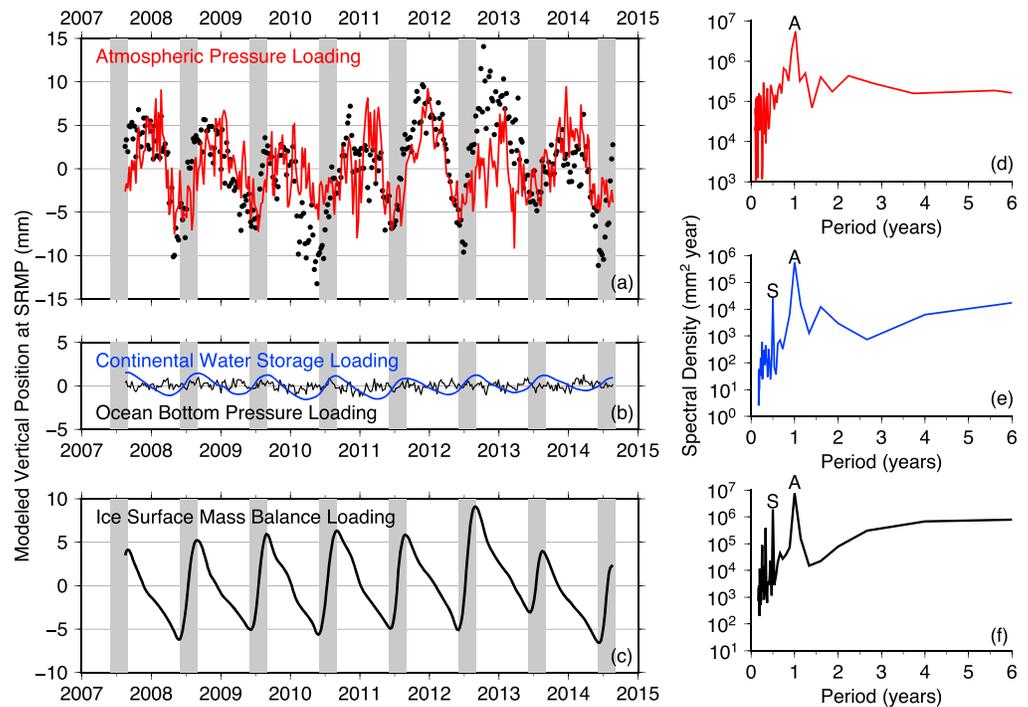
We also fit the GPS horizontal time series with the same harmonic model but find small annual amplitudes. The best fit annual amplitudes are only 0.40 mm (east-west components at SRMP), 0.68 mm (north-south components at SRMP), 0.23 mm (east-west components at UPVK), and 0.86 mm (north-south components at UPVK), which are 3 to 10 times smaller than the annual vertical amplitudes (see Figure S1 in the supporting information). Horizontal displacements may help in loading studies by providing more constraints, especially on the azimuthal directions of surface mass changes [e.g., *Grapenthin et al., 2006; Wahr et al., 2013*]. However, further analysis and interpretation of horizontal displacements are beyond the scope of this study.

The time series of modeled vertical loading displacements due to various surface mass changes show strong annual variability, moderate semiannual variability, and no significant variability at other periods

**Table 2.** Annual Amplitudes and Phases of the GPS Data and Modeled Vertical Loading Displacements From Various Surface Mass Changes<sup>a</sup>

Components	SRMP		UPVK	
	Amplitude (mm)	Phase (Day of Year Since 1 January)	Amplitude (mm)	Phase (Day of Year Since 1 January)
GPS	4.8 ± 0.1	331 ± 2	2.3 ± 0.1	365 ± 3
Atmospheric pressure	3.4 ± 0.1	362 ± 2	2.8 ± 0.1	360 ± 2
Continental water storage	1.1 ± 0.1	258 ± 1	1.1 ± 0.1	257 ± 1
Ice surface mass balance	4.3 ± 0.3	284 ± 4	2.0 ± 0.2	283 ± 4

<sup>a</sup>The uncertainties refer to the  $1\sigma$  root-mean-square errors. The loading displacements due to ocean bottom pressure changes show little annual changes (smaller than 0.1 mm at SRMP and 0.2 mm at UPVK), which are not included in this table.



**Figure 3.** Modeled elastic vertical displacements at SRMP in response to the various loads. All the time series have been detrended. (a) The red line shows the vertical displacements due to atmospheric pressure loading. The black dots are the same GPS data as presented in Figure 2a; they are shown here again to allow for a direct comparison with the modeled displacements. (b) The blue line shows the continental water mass loading displacements. The thin black line shows the ocean bottom pressure loading displacements. (c) Ice surface mass balance loading displacements. (d–f) The periodograms of the corresponding atmospheric pressure loading, continental water mass loading, and ice surface mass balance loading, respectively. “S” and “A” indicate the spectrum peaks at semiannual and annual periods, respectively.

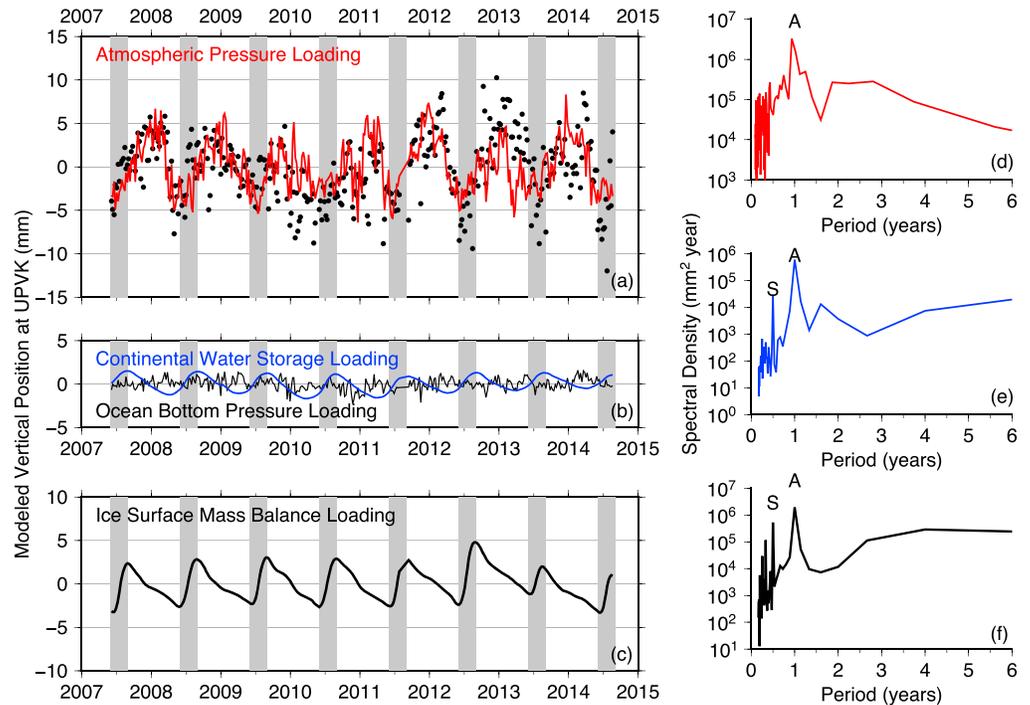
(Figures 3 and 4). We therefore only include the annual and semiannual terms in the time series model of our modeled loading displacements. At SRMP and UPVK, the modeled ATM loading displacements have amplitudes of 3.4 mm and 2.8 mm, respectively. The maximum for both stations occurs around 1 January, similar to the annual phase of the GPS observations. Loading displacements due to changes in CWS are nearly identical at the two stations, dominated by an annual cycle with amplitudes of only 1.1 mm, peaking around 15 September (Figures 3b, 3e, 4b, and 4e). This is expected because the CWS over the ice sheet is eliminated in the GLDAS model so that the annual signal is driven by mass changes in the far field. The amplitude of the annual loading displacements due to OBP changes is smaller than 0.2 mm, almost negligible (Figures 3b and 4b).

The SMB loading displacements are characterized by strong annual, moderate semiannual, and weak biannual cycles (Figures 3c, 3f, 4c, and 4f). At SRMP, the annual amplitude of the SMB loading displacements is 4.3 mm, larger than that of the ATM loading. At UPVK, which is further away from the ice sheet, the annual amplitude of the SMB loading displacements is 2.0 mm, smaller than that of the ATM loading. Including both annual and semiannual cycles, the overall SMB loading displacements peak around 1 September, the end of summer melting season (Figures 3c and 4c).

Interannual variations are also evident in the SMB loading displacement time series. For instance, the net SMB uplift at SRMP during June–July–August (JJA) in 2012 was ~14 mm or 4 mm larger than the mean net uplift (~10 mm) during the same summer months in 2008 to 2011 (Figure 3c). In contrast, the net SMB maxima during JJA in 2013 and 2014 were ~6 mm and ~8 mm, respectively, smaller than the 2008–2011 mean.

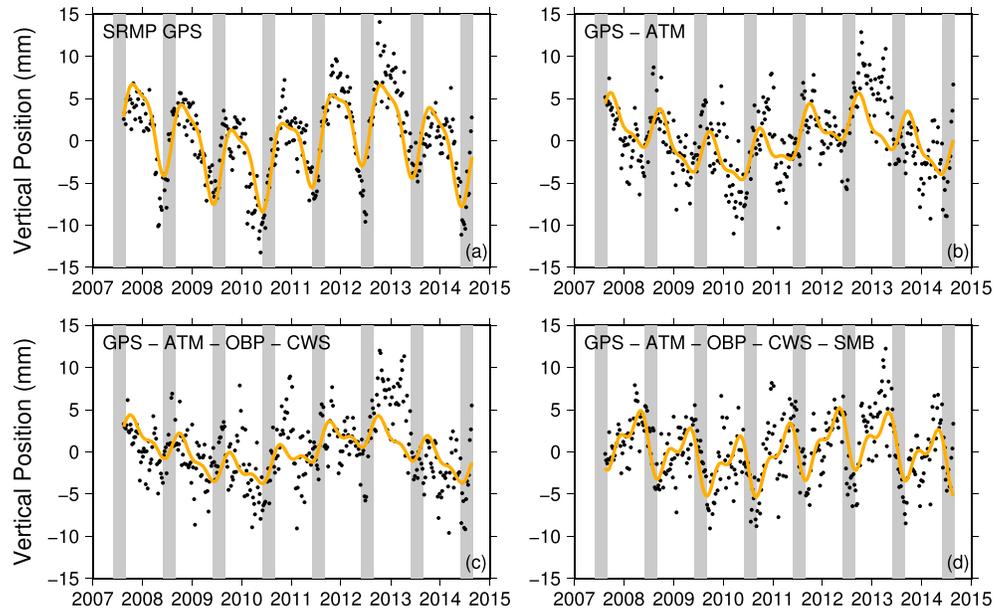
### 3.2. GPS Residuals After Removing Modeled Loading Displacements

We remove the modeled displacements from the GPS vertical displacements in the following sequential steps: (1) the ATM loading displacements, (2) the loading displacements due to OBP and CWS combined, and (3) the SMB loading displacements. Figures 5 and 6 show the residuals obtained after each step.



**Figure 4.** (a–f) Similar to Figure 3 but for the modeled vertical displacements at UPVK in response to various loading sources.

We evaluate the residuals in two ways. First, we calculate the amplitude and phase of the best fit annual to the residuals obtained after each correction step (Table 3). After removing the modeled atmospheric loading displacements, the annual amplitudes decrease by 2.2 mm (46%) and 1.8 mm (78%) from the original GPS amplitudes at SRMP and UPVK, respectively (also compare Figure 5b with Figure 5a and Figure 6b with



**Figure 5.** Time series of GPS vertical positions (black dots) after removing the modeled loading displacements at SRMP. (a) The same GPS as shown in Figure 2a. The orange line shows the best fit four-harmonic model using equation (1). (b) The residuals after removing the modeled ATM loading. (c) The residuals after further removing OBP and CWS. (d) The residuals after removing all the modeled surface mass loading components, including the SMB.

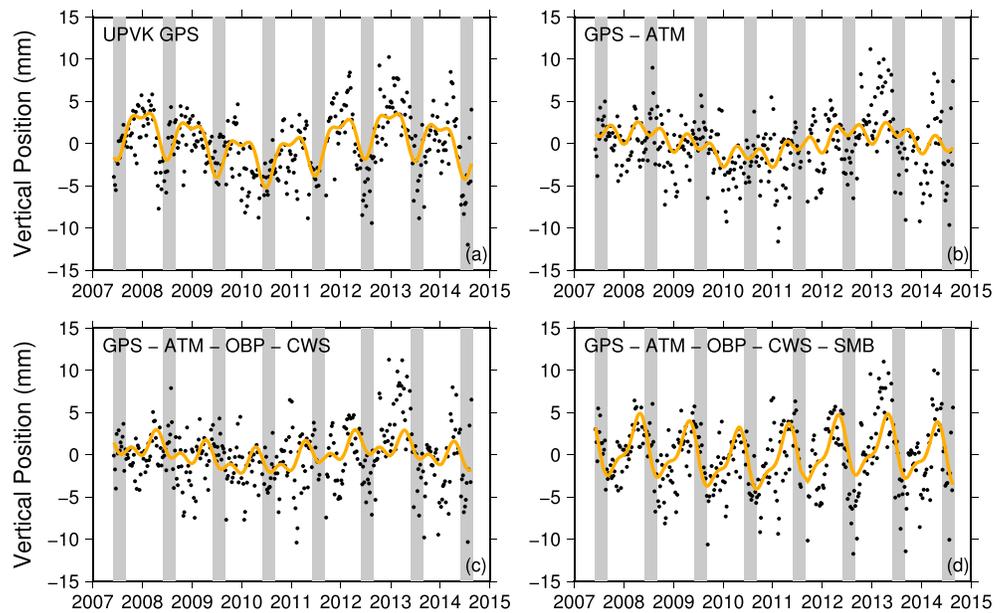


Figure 6. (a–d) Similar to Figure 5 but for the vertical residuals at UPVK after removing the modeled loading displacements.

Figure 6a). After the further removal of the modeled displacements due to OBP and CWS loading, the annual amplitude decreases by 0.8 mm to 1.8 mm at SRMP (also Figure 5c) but instead increases by 0.7 mm to 1.2 mm at UPVK (also Figure 6c). Taken together, removing all the nonice components reduces the annual amplitudes by 3 mm (63%) at SRMP and 1.1 mm (48%) at UPVK. Finally, and unexpectedly, after the removal of the modeled SMB loading displacements, the annual amplitudes increase by 0.9 mm (50%) and 2 mm (167%) from the previous step at SRMP and UPVK, respectively (also see Figures 5d and 6d). Comparing Figure 5d with Figure 5c, we also note a phase shift from the 309th day of year for the residuals after the removal of the nonice components to the 85th day of year after the further removal of the SMB components (Table 3). In contrast, the phase shift between these two steps is negligible at UPVK (Figures 6c and 6d and Table 3).

We also calculate the weighted root-mean-square (WRMS) of the residuals and the corresponding ratio of WRMS reduction after removing each loading component. We decompose each of the residuals time series into long-period and short-period components, separated by 0.5 year. Table 4 lists the calculated ration of WRMS reduction from the original GPS vertical time series. Because of our focus on the annual signatures, here we only summarize the results using the long-period components. At SRMP, ATM loading can explain 26% of the WRMS for the long-period components, followed by the SMB (24%), the CWS (4%), and negligibly but reversely from the OBP (−0.6%). Overall, these modeled loading displacements account for 41% of the WRMS at the long periods. At UPVK, the ATM loading reduces the WRMS for the long-period components by 21%. The CWS and SMB instead increase the WRMS by 5% and 4%, respectively. Overall, these modeled loading displacements unfavorably increase the WRMS at the long periods by 3%.

Table 3. Best Fit Amplitude and Phase of Annual Cycles After the Sequential Steps: (1) Removing the Atmospheric Pressure (ATM) Loading Displacements, (2) Removing the Loading Displacements From Ocean Bottom Pressure (OBP) and Continental Water Storage (CWS) Combined, and (3) Removing the SMB Loading Displacements<sup>a</sup>

	SRMP		UPVK	
	Amplitude (mm)	Phase (Day of Year Since 1 January)	Amplitude (mm)	Phase (Day of Year Since 1 January)
GPS	4.8 ± 0.1	331 ± 2	2.3 ± 0.1	365 ± 3
After removing ATM	2.6 ± 0.1	287 ± 3	0.5 ± 0.1	158 ± 10
After further removing OBP and CWS	1.8 ± 0.1	309 ± 3	1.2 ± 0.1	94 ± 5
After further removing SMB	2.7 ± 0.1	85 ± 2	3.2 ± 0.1	99 ± 2

<sup>a</sup>The “GPS” row is the same as listed in Table 2.

**Table 4.** Ratios of WRMS Reduction in Vertical Position Time Series, After Removing Individual Loading Sources<sup>a</sup>

	Ratio of WRMS Reduction at SRMP (%)		Ratio of WRMS Reduction at UPVK (%)	
	Long Period	Short Period	Long Period	Short Period
ATM removed	26	−14	21	−6
OBP removed	−0.6	2	3	3
CWS removed	4	0.1	−5	0
SMB removed	24	0.7	−4	0.9
All removed	41	−16	−3	−6

<sup>a</sup>Columns “Long Period” and “Short Period” list the ratios calculated using the components at longer and shorter than the semiannual period, respectively.

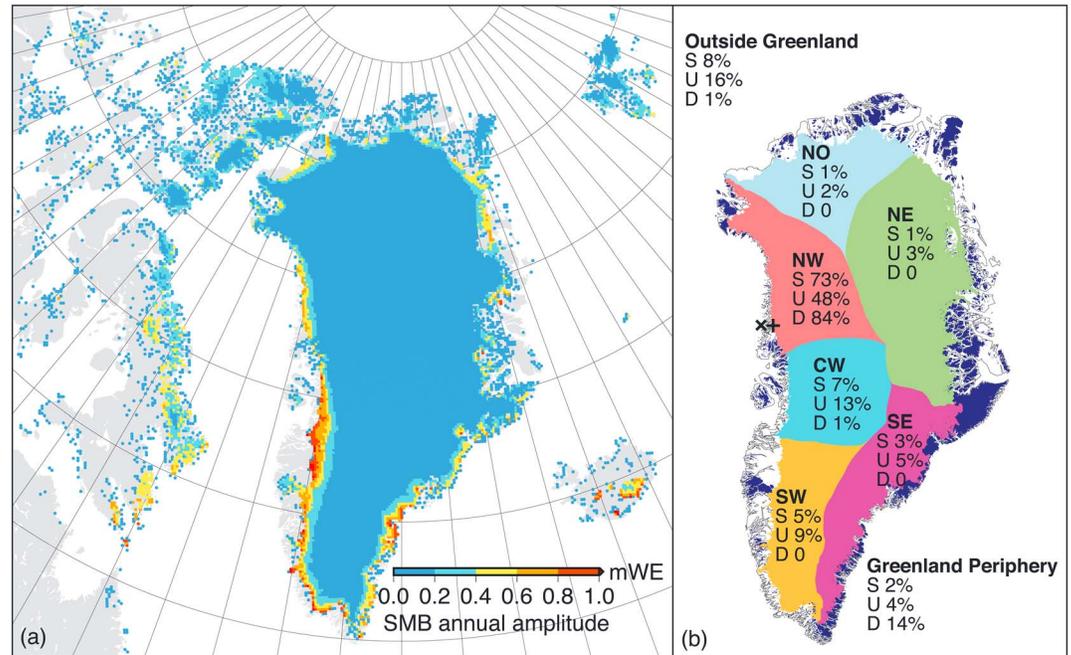
In summary, the combined facts that the removal of SMB loading (1) increases the annual amplitudes of the GPS residuals at both stations, (2) shifts the annual phase by 224 days at SRMP, and (3) increases the WRMS at UPVK for the long-period components indicate that the modeled SMB loading increases the annual variance of the GPS residuals after the removal of the nonice loading. This contradicts to our expectation that the SMB loading should partly explain the GPS residuals. The residuals obtained after the further removal of the SMB loading (i.e., Figures 5d and 6d) are questionable and cannot be used to interpret the contribution from the glacial dynamics to the total ice mass changes.

## 4. Discussion

### 4.1. Performance of Modeled Surface Mass-Loading Displacements

We use alternative elastic Earth models to assess the uncertainties of the modeled SMB loading displacements. We perform the same elastic loading calculation as described in section 2.3 but using the following six one-dimensional spherical models: (1) an older, poorly constrained Gutenberg-Bullen A model; (2) the PREM with oceanic crust; (3) the PREM with the crustal structure as modeled in Crust 2.0 with hard sediments; (4) the PREM with the crustal structure as modeled in Crust 2.0 with soft sediments; (5) the ak135 model; and (6) the iasp91 model. The elastic loading Green’s functions for models (1) and (2) are provided in *Farrell* [1972] and *Jentzsch* [1997], respectively; the others are provided in *Wang et al.* [2012]. Together with the PREM continental-crust model that we have adopted as a baseline, we analyze the ensemble of these seven sets of modeled vertical displacements due to the same SMB loading. We find that these Earth models give similar displacements (Figure S2). Take the monthly displacement values at SRMP as an example: our calculations show that the standard deviation of the ensemble is less than 0.43 mm; the maximum difference between the displacements from the baseline model and the ensemble mean is only 0.2 mm. The best fit annual amplitude of the ensemble mean is 4.1 mm with a 5% variance. This, again, is very close to the best fit annual amplitude of 4.2 mm based on the baseline model. Among all the Earth models considered, the PREM oceanic-crust model gives the largest differences from the baseline model with an annual amplitude that is 0.4 mm (10%) smaller. These similarities are because (1) the loading Green’s functions of these spherical Earth models differ mostly in the near field (shorter than 100 km from the loads) [*Wang et al.*, 2012], and (2) as will be shown later in this section and Figures 7 and 8, a significant portion of the SMB loading fields is located in the far field and contributes to the loading displacements at the annual period. We note that the analysis described above does not quantify the effects of lateral variations of crustal structure on the modeled loading displacements. However, according to *Dill et al.* [2015], such effects cause a maximum of 10% in the annual vertical displacements over western Greenland.

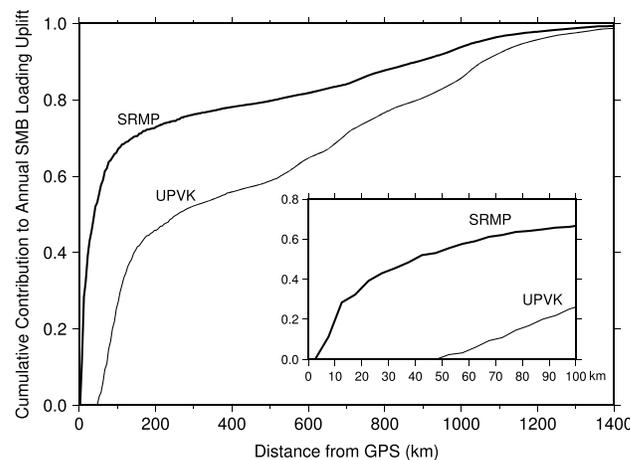
We also assess the variances in the SMB models using four other sets of regional atmospheric climate model outputs. These alternative models include the earlier RACMO version 2.1 model [*van den Broeke et al.*, 2009; *van Angelen et al.*, 2012] and the MAR v3.5.2 with three different forcing models (ERA-Interim, NCEP-NCARv1, and 20CRv2) [*Fettweis et al.*, 2013]. Our calculated loading displacements based on these five models have similar annual cycles (Figure S3). For instance, the ensemble mean of the annual amplitude is 4.1 mm at SRMP with a standard deviation of 0.2 mm. This is very similar to the 4.2 mm obtained using the RACMO2.3 outputs.



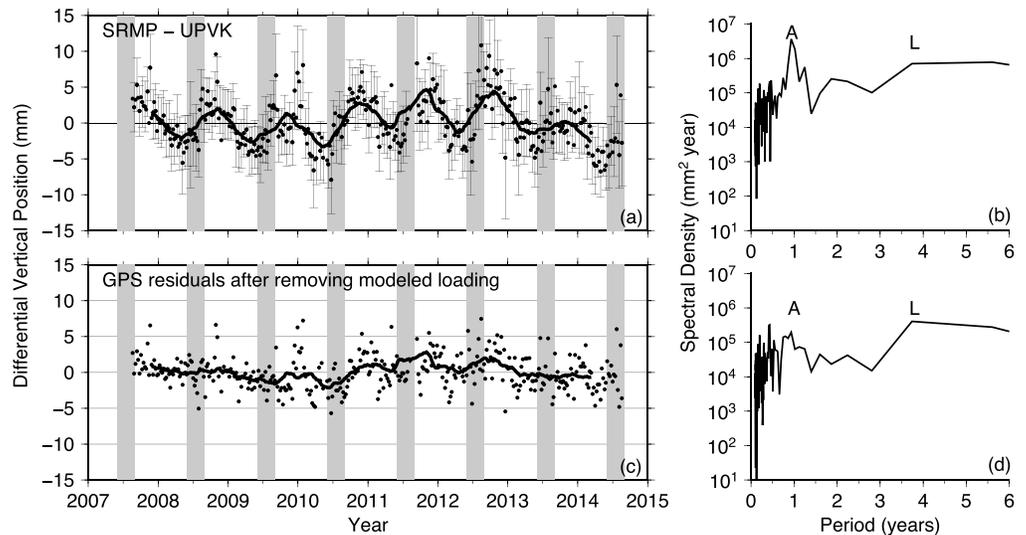
**Figure 7.** (a) Map of the annual amplitude of SMB (units: meters water equivalent or mWE), obtained from the RACMO2.3 monthly SMB fields from 2007.5 to 2014.7. (b) Map of major drainage basins of the Greenland Ice Sheet (labeled as “NW” for northwest, “CW” for central-west, “SW” for southwest, “SE” for southeast, “NE” for northeast, and “NO” for north) and peripheral glaciers in Greenland (dark blue). The plus and cross symbols mark the positions of SRMP and UPVK, respectively. Under each unit label is a list of contributions in percentage from each unit to the annual amplitude of SMB loading displacements at SRMP (“S”), UPVK (“U”), and the station difference (“D”). “D 0” means that the contribution to the station difference is smaller than 1% and negligible.

In fact, the annual SMB vertical loading displacements at the two GPS stations are attributed to surface ice mass changes over large portions of the GrIS. We first use the RACMO2.3 outputs to estimate the annual SMB changes over the entire model domain during our study period. Figure 7a shows the best fit annual amplitude. We then calculate the total contribution to the annual SMB loading displacement from each of the following units: the six major drainage basins of the GrIS (based on *Rignot et al.*

[2011]), glaciers around the periphery of Greenland (based on the Randolph Glacier Inventory 5.0; <http://www.glims.org/RGI/>), and ice fields outside Greenland (including the Canadian Arctic, Svalbard, Jan Mayen, and Iceland). Figure 7b summarizes their contributions. At SRMP, 73% of the annual loading displacements originate from the northwest drainage basin, followed by much smaller contributions from outside Greenland (8%), the central-west (7%), southwest (5%), and southeast (3%) drainage basins. At UPVK, the order of contribution is similar to that of the SRMP: 48% is from the northwest drainage basin, followed by outside Greenland (16%), the central-west (13%), southwest (9%), and southeast (5%) drainage basins. The contributions from the



**Figure 8.** Cumulative contribution to the annual SMB loading uplift at SRMP (thick line) and UPVK (thin line), normalized with the total annual amplitude at each station. The inset shows a zoom-in distance range of 0–100 km.



**Figure 9.** Similar to Figure 2 but for (a) time series of the differences between the detrended vertical positions measured at SRMP and UPVK and (b) its periodogram. (c) Time series of the residuals after removing the modeled loading from the differential GPS and (d) its periodogram.

remaining units are small at both stations. Figure 8 shows the cumulative contribution to the annual SMB loading displacement from surface ice sources located at different distances. At SRMP, ~70% of the annual loading displacements originate from surface ice mass variations within ~100 km. However, the remaining 30% is attributed to surface ice mass within 1200 km radius (~85% of the entire ice sheet area and outside Greenland). At UPVK, which is located further away from the ice sheet, 50% of its annual SMB loading displacements originate from surface ice mass within 200 km.

**4.2. Differential Vertical Displacements Between the Two Stations**

In the GPS data analysis, a few mismodeled or unmodeled factors may also result in errors with annual signature and thus affect our interpretation. As summarized in Dong et al. [2002], some factors are local at individual stations such as multipath and snow cover on the receiver antenna, and some factors are regional or global, such as the reference frame, mismodeled wet tropospheric delay, and errors in orbital modeling. Even though significant improvements have been made in the GPS analysis in the past decade, some of these errors are not well understood or corrected and thus may remain.

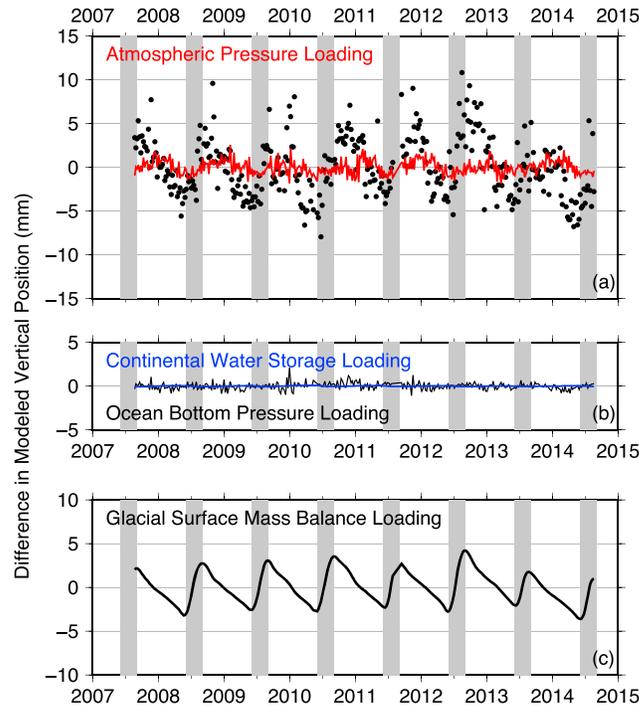
Here we examine the differences between SRMP and UPVK, in which we have eliminated the common errors in the GPS data. The station difference still shows a strong annual variability with an amplitude of 3.1 mm (Figures 9a and 9b and Table 5). However, we also have removed any common geophysical signals.

To further quantify what may have been removed, we take the difference of the modeled surface mass loading displacements between the two stations. Figure 10 shows these differential time series. Table 5 lists the annual amplitudes of the differential loading displacements: 0.6 mm for the ATM loading, nearly zero (0.1 mm) for the OBP, zero for the CWS, and 2.2 mm for the SMB loading. Compared with the Table 2 results for SRMP, we have removed 2.8 mm (82%) of the ATM loading, 2.1 mm (49%) of the SMB loading, and nearly the entire of the OBP and CWS.

**Table 5.** Similar to Table 2 but for the Differential Verticals Between SRMP and UPVK<sup>a</sup>

Components	SRMP Minus UPVK	
	Amplitude (mm)	Phase (Day of Year Since 1 January)
GPS	3.1 ± 0.2	303 ± 3
Atmospheric pressure	0.6 ± 0.1	2 ± 3
Ice surface mass balance	2.2 ± 0.1	286 ± 1

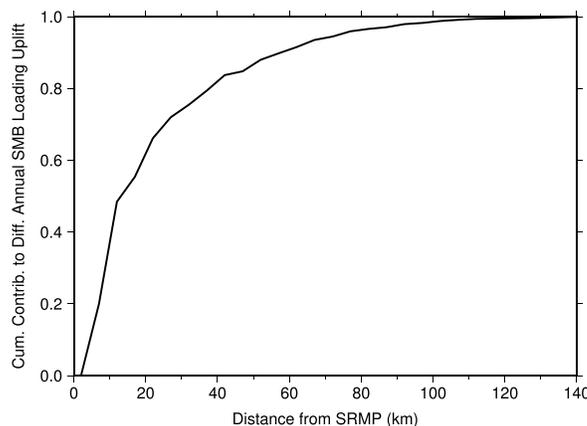
<sup>a</sup>We exclude the differential ocean bottom pressure and continental water storage loading displacements as their annual changes are smaller than 0.1 mm.



**Figure 10.** (a–c) Similar to Figure 3 but for the differences of modeled vertical displacements between SRMP and UPVK.

After the station differencing, the SMB signals become the most dominant component among all the modeled surface mass displacements at annual periods. We conduct a similar sensitivity analysis to the one described in section 4.1 but for the differential SMB loading displacements. Compared with the individual sensitivity curves shown in Figure 8, the differential sensitivity (Figure 11) reveals a significant contribution from nearby surface ice: SMB changes within 40 km from SRMP contribute to about 80% of the differential SMB loading displacements at the annual period. There is little sensitivity to SMB beyond 120 km from SRMP. This is also confirmed by our estimated contributions from different units to the annual differential SMB uplift (summarized in Figure 7b). As expected, the northwest drainage basin is the dominant contributor (84%), followed by the peripheral glaciers (15%), and merely 1% from the central-west drainage basin. Contributions from the other units are negligible.

Lastly, we remove modeled differential loading displacements from the measured differential GPS in sequential steps as described in section 3.2. Tables 6 and 7 list the best fit annual amplitudes/phases and ratios of WRMS reduction. We observe that the differential SMB match with the differential GPS the best. Removing the differential SMB can reduce the WRMS of the long-period components by 47%. Removing all the modeled differential loading displacements, the annual amplitude is reduced to 0.7 mm (or 23% of the differential GPS before the corrections) and the WRMS reduction of the long-period components is 55%. Figures 9c and 9d show the time series and periodogram of the residuals after removing all the modeled loading components. From these figures, it is evident that the models significantly reduce the annual amplitude and data variance.



**Figure 11.** Similar to Figure 8 but for the cumulative contribution to the differential SMB loading uplift between SRMP and UPVK.

Although the differential SMB loading displacements match the differential GPS residuals well, we cannot uniquely confirm the accuracy of the SMB model in the near field of the GPS stations. This is because by taking station difference, we have removed 2.1 mm of common SMB loading signals. These common SMB loading signals originate from all the ice fields. We cannot rule out the possibility that the deficits in the SMB model (if any) might be localized in near field. Theoretically, an extreme case is that an SMB bias is at a point location, which may cause a similar bias in the annual loading at both stations.

**Table 6.** Similar to Table 3 but for the Differential Vertical Displacements Between SRMP and UPVK

	SRMP Minus UPVK	
	Amplitude (mm)	Phase (Day of Year Since 1 January)
GPS	3.1 ± 0.2	304 ± 3
After removing ATM	2.9 ± 0.2	293 ± 3
After further removing OBP and CWS	2.8 ± 0.2	295 ± 3
After further removing SMB	0.7 ± 0.2	321 ± 11

However, taking a station difference would have removed such common bias and still gives good residual results as presented above.

### 4.3. Unmodeled GPS Draconitic Errors and Surface Mass Loading Displacements

In addition to annual periodicity, many GPS position time series have a 351.2 day harmonic at the GPS draconitic year as well as its higher harmonics [Ray *et al.*, 2008; Amiri-Simkooei, 2013]. However, we have chosen to exclude the draconitic harmonics in the Fourier series model (equation (1)) for two reasons. First, neither of the 8 year GPS time series at SRMP or UPVK shows a peak at 351.2 days (Figures 2a and 2c). Second, we find that including the draconitic harmonics in the least squares fitting using the daily GPS data results in a strong negative correlation between the draconitic and annual cycles. Such a trade-off indicates an overfitting problem and that the GPS data used in this study are not able to separate the draconitic and annual cycles. However, because the draconitic signals are so close to a pure annual, they may still contribute to the annual amplitude and phase in the GPS data. Quantifying such error will become feasible as the GPS time series are getting longer.

The CWS loading model based on GLDAS excludes groundwater, river and lakes, and permafrost. The unmodeled vertical displacements due to these water mass changes are expected to have annual variability, but their amplitudes are smaller than our modeled CWS loading. Depending on the annual phases of these mass sources, they may not add constructively. Including these terms may help to reduce the overestimation of CWS loading at UPVK.

## 5. Conclusions

To quantitatively interpret the annual changes of the vertical displacements measured at two GNET GPS stations, 65 km apart near Upernavik Isstrøm, we present a systematic study to model and correct various surface mass loading components. Among all the nonice mass changes, atmospheric pressure changes introduce the largest annual changes at both stations, followed by continental water storage, with negligible contributions from ocean bottom pressure. Removing the nonice loading contributions can reduce the annual amplitudes by at least 50%. This suggests the need for applying this correction before using annual GPS signals to infer ice mass changes.

Our modeled SMB loading based on RACMO2.3 increases the annual variance of the GPS residuals, which makes it difficult to estimate contributions from the annual variability of glacial dynamics to the total ice mass balance. Our analysis reveals that GPS verticals at individual stations are sensitive to annual ice mass changes over 85% of the entire ice sheet and outside Greenland. This long-distance sensitivity indicates the nonuniqueness and therefore the difficulty of using GPS data alone to quantitatively identify possible defects in the SMB model, especially their locations.

**Table 7.** Similar to Table 4 but for the Differential Vertical Displacements Between SRMP and UPVK<sup>a</sup>

	Ratio of WRMS Reduction (%)	
	Long Periods	Short Periods
ATM removed	4	3
OBP removed	3	0.2
SMB removed	47	-0.5
All removed	55	2

<sup>a</sup>The differential CWS loading displacements are nearly zero and therefore not included in the table.

Alternatively, by taking station difference, we find a good match between the modeled SMB loading and the estimated GPS vertical displacements. Our forward modeling shows the sensitivity of the differential loading displacements to local SMB changes. This suggests that differential displacements measured at a local GPS network can potentially help to place constraints on estimates of annual glacial mass balance obtained, for instance, from glaciological estimates.

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## References

- Abdalati, W., and K. Steffen (2001), Greenland Ice Sheet melt extent: 1979–1999, *J. Geophys. Res.*, *106*(D24), 33,983–33,988, doi:10.1029/2001JD900181.
- Altamimi, Z., L. Métivier, and X. Collilieux (2012), ITRF2008 plate motion model, *J. Geophys. Res.*, *117*, B07402, doi:10.1029/2011JB008930.
- Amiri-Simkooei, A. R. (2013), On the nature of GPS draconitic year periodic pattern in multivariate position time series, *J. Geophys. Res. Solid Earth*, *118*, 2500–2511, doi:10.1002/jgrb.50199.
- Andresen, C. S., K. K. Kjeldsen, B. E. Harden, N. Norgaard-Pedersen, and K. H. Kjær (2014), Outlet glacier dynamics and bathymetry at Upernavik Isstrøm and Upernavik Isfjord, north-west Greenland, *Geol. Surv. Den. Greenl. Bull.*, *31*, 79–82.
- Bevan, S. L., A. Luckman, S. A. Khan, and T. Murray (2015), Seasonal dynamic thinning at Helheim Glacier, *Earth Planet. Sci. Lett.*, *415*, 47–53, doi:10.1016/j.epsl.2015.01.031.
- Bevis, M., et al. (2012), Bedrock displacements in Greenland manifest ice mass variations, climate cycles and climate change, *Proc. Natl. Acad. Sci. U.S.A.*, *109*(30), 11,944–11,948, doi:10.1073/pnas.1204664109.
- Blewitt, G. (2003), Self-consistency in reference frames, geocenter definition, and surface loading of the solid Earth, *J. Geophys. Res.*, *108*(B2), 2103, doi:10.1029/2002JB002082.
- Boehm, J., B. Werl, and H. Schuh (2006), Troposphere mapping functions for GPS and very long baseline interferometry from European Centre for Medium-Range Weather Forecasts operational analysis data, *J. Geophys. Res.*, *111*, B02406, doi:10.1029/2005JB003629.
- Dill, R., V. Klemann, Z. Martinec, and M. Tesaro (2015), Applying local Green's functions to study the influence of the crustal structure on hydrological loading displacements, *J. Geodyn.*, *88*, 14–22, doi:10.1016/j.jog.2015.04.005.
- Dong, D., P. Fang, Y. Bock, M. K. Cheng, and S. Miyazaki (2002), Anatomy of apparent seasonal variations from GPS-derived site position time series, *J. Geophys. Res.*, *107*(B4), 2075, doi:10.1029/2001JB000573.
- Dong, D., T. Yunck, and M. Hefflin (2003), Origin of the International Terrestrial Reference Frame, *J. Geophys. Res.*, *108*(B4), 2200, doi:10.1029/2002JB002035.
- Dziewonski, A., and D. Anderson (1981), Preliminary Reference Earth Model (PREM), *Phys. Earth Planet. Inter.*, *25*(4), 297–356.
- Farrell, W. E. (1972), Deformation of Earth by surface loads, *Rev. Geophys. Space Phys.*, *10*(3), 761–797.
- Fettweis, X., B. Franco, M. Tedesco, J. H. van Angelen, J. T. M. Lenaerts, M. R. van den Broeke, and H. Gallee (2013), Estimating the Greenland Ice Sheet surface mass balance contribution to future sea level rise using the regional atmospheric climate model MAR, *Cryosphere*, *7*, 469–489, doi:10.5194/tc-7-469-2013.
- Fukumori, I. (2002), A partitioned Kalman filter and smoother, *Mon. Weather Rev.*, *130*(5), 1370–1383.
- Grapenthin, R., F. Sigmundsson, H. Geirsson, T. Árnadóttir, and V. Pínel (2006), Icelandic rhythmicity: Annual modulation of land elevation and plate spreading by snow load, *Geophys. Res. Lett.*, *33*, L24305, doi:10.1029/2006GL028081.
- Hanna, E., P. Huybrechts, J. Cappelen, K. Steffen, R. C. Bales, E. Burgess, J. R. McConnell, J. Peder Steffensen, M. Van den Broeke, and L. Wake (2011), Greenland Ice Sheet surface mass balance 1870 to 2010 based on Twentieth Century Reanalysis, and links with global climate forcing, *J. Geophys. Res.*, *116*, D24121, doi:10.1029/2011JD016387.
- Jentzsch, G. (1997), Earth tides and ocean tidal loading, in *Tidal Phenomena*, edited by H. Wilhelm, W. Zurn, and H. G. Wenzel, pp. 145–171, Springer, Berlin.
- Jiang, Y., T. H. Dixon, and S. Wdowinski (2010), Accelerating uplift in the North Atlantic region as an indicator of ice loss, *Nat. Geosci.*, *3*(6), 404–407, doi:10.1038/ngeo845.
- Joughin, I., S. B. Das, M. A. King, B. E. Smith, I. M. Howat, and T. Moon (2008), Seasonal speedup along the western flank of the Greenland Ice Sheet, *Science*, *320*(5877), 781–783, doi:10.1126/science.1153288.
- Kalnay, E., et al. (1996), The NCEP/NCAR 40-year reanalysis project, *Bull. Am. Meteorol. Soc.*, *77*(3), 437–471.
- Khan, S. A., J. Wahr, L. A. Stearns, G. S. Hamilton, T. van Dam, K. M. Larson, and O. Francis (2007), Elastic uplift in southeast Greenland due to rapid ice mass loss, *Geophys. Res. Lett.*, *34*, L21701, doi:10.1029/2007GL031468.
- Khan, S. A., J. Wahr, E. Leuliette, T. van Dam, K. M. Larson, and O. Francis (2008), Geodetic measurements of postglacial adjustments in Greenland, *J. Geophys. Res.*, *113*, B02402, doi:10.1029/2007JB004956.
- Khan, S. A., L. Liu, J. Wahr, I. Howat, I. Joughin, T. van Dam, and K. Fleming (2010), GPS measurements of crustal uplift near Jakobshavn Isbræ to glacial ice mass loss, *J. Geophys. Res.*, *115*, B09405, doi:10.1029/2010JB007490.
- Khan, S. A., et al. (2013), Recurring dynamically induced thinning during 1985 to 2010 on Upernavik Isstrøm, West Greenland, *J. Geophys. Res. Earth Surf.*, *118*, 111–121, doi:10.1029/2012JF002481.
- Khan, S. A., et al. (2016), Geodetic measurements reveal similarities between post-Last Glacial Maximum and present-day mass loss from the Greenland Ice Sheet, *Sci. Adv.*, *2*(9), doi:10.1126/sciadv.1600931.
- Kim, S.-B., T. Lee, and I. Fukumori (2007), Mechanisms controlling the interannual variation of mixed layer temperature averaged over the Niño-3 region, *J. Clim.*, *20*(15), 3822–3843, doi:10.1175/JCLI4206.1.
- Kouba, J. (2008), Implementation and testing of the gridded Vienna Mapping Function 1 (VMF1), *J. Geod.*, *82*(4-5), 193–205, doi:10.1007/s00190-007-0170-0.
- Larsen, S. H., S. A. Khan, A. P. Ahlstrøm, C. S. Hvidberg, M. J. Willis, and S. B. Andersen (2016), Increased mass loss and asynchronous behavior of marine-terminating outlet glaciers at Upernavik Isstrøm, NW Greenland, *J. Geophys. Res. Earth Surf.*, *121*, 241–256, doi:10.1002/2015JF003507.
- Nielsen, K., S. A. Khan, N. J. Korsgaard, K. H. Kjær, J. Wahr, M. Bevis, L. A. Stearns, and L. H. Timm (2012), Crustal uplift due to ice mass variability on Upernavik Isstrøm, West Greenland, *Earth Planet. Sci. Lett.*, *353–354*, 182–189, doi:10.1016/j.epsl.2012.08.024.
- Noël, B., W. J. van de Berg, E. van Meijgaard, P. Kuipers Munneke, R. S. W. van de Wal, and M. R. van den Broeke (2015), Evaluation of the updated regional climate model RACMO2.3: Summer snowfall impact on the Greenland Ice Sheet, *Cryosphere*, *9*(5), 1831–1844, doi:10.5194/tc-9-1831-2015.
- Ray, J., Z. Altamimi, X. Collilieux, and T. van Dam (2008), Anomalous harmonics in the spectra of GPS position estimates, *GPS Solutions*, *12*(1), 55–64, doi:10.1007/s10291-007-0067-7.
- Rignot, E., I. Velicogna, M. R. van den Broeke, A. Monaghan, and J. T. M. Lenaerts (2011), Acceleration of the contribution of the Greenland and Antarctic Ice Sheets to sea level rise, *Geophys. Res. Lett.*, *38*, L05503, doi:10.1029/2011GL046583.
- Rodell, M., P. Houser, et al. (2004), The global land data assimilation system, *Bull. Am. Meteorol. Soc.*, *85*(3), 381–394.
- Santamaría-Gómez, A., and A. Mémin (2015), Geodetic secular velocity errors due to interannual surface loading deformation, *Geophys. J. Int.*, *202*(2), 763–767, doi:10.1093/gji/ggv190.
- Scherneck, H.-G., and M. S. Bos (2002), Ocean tide and atmospheric loading, IVS 2002 General Meeting Proceedings, Tsukuba, Japan, February 4–7, 2002, pp. 205–214. [Available at <http://holt.oso.chalmers.se/loading> (lastly accessed on December 29, 2015).]

- Sole, A. J., D. W. F. Mair, P. W. Nienow, I. D. Bartholomew, M. A. King, M. J. Burke, and I. Joughin (2011), Seasonal speedup of a Greenland marine-terminating outlet glacier forced by surface melt-induced changes in subglacial hydrology, *J. Geophys. Res.*, *116*, F03014, doi:10.1029/2010JF001948.
- van Angelen, J., J. Lenaerts, S. Lhermitte, X. Fettweis, P. Kuipers Munneke, M. Broeke, E. V. Meijgaard, and C. Smeets (2012), Sensitivity of Greenland Ice Sheet surface mass balance to surface albedo parameterization: A study with a regional climate model, *Cryosphere*, *6*(5), 1175–1186.
- van Dam, T., and J. Wahr (1987), Displacements of the Earth's surface due to atmospheric loading: Effects on gravity and baseline measurements, *J. Geophys. Res.*, *92*(B2), 1281–1286, doi:10.1029/JB092iB02p01281.
- van den Broeke, M., J. Bamber, J. Ettema, E. Rignot, E. Schrama, W. J. van de Berg, E. van Meijgaard, I. Velicogna, and B. Wouters (2009), Partitioning recent Greenland mass loss, *Science*, *326*(5955), 984–986.
- Wahr, J., T. van Dam, K. Larson, and O. Francis (2001), Geodetic measurements in Greenland and their implications, *J. Geophys. Res.*, *106*(B8), 16,567–16,581, doi:10.1029/2001JB000211.
- Wahr, J., S. A. Khan, T. Dam, L. Liu, J. H. Angelen, M. R. Broeke, and C. M. Meertens (2013), The use of GPS horizontals for loading studies, with applications to Northern California and southeast Greenland, *J. Geophys. Res. Solid Earth*, *118*, 1795–1806, doi:10.1002/jgrb.50104.
- Wang, H., L. Xiang, L. Jia, L. Jiang, Z. Wang, B. Hu, and P. Gao (2012), Load Love numbers and Green's functions for elastic Earth models PREM, iasp91, ak135, and modified models with refined crustal structure from Crust 2.0, *Comput. Geosci.*, *49*, 190–199, doi:10.1016/j.cageo.2012.06.022.
- Williams, S. D. P., Y. Bock, P. Fang, P. Jamason, R. M. Nikolaidis, L. Prawirodirdjo, M. Miller, and D. J. Johnson (2004), Error analysis of continuous GPS position time series, *J. Geophys. Res.*, *109*, B03412, doi:10.1029/2003JB002741.