Oxide Modules

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22.1 Introduction

TE oxides have been considered as promising materials due to their non-toxicity, low cost, and chemical stability at high temperatures [1–3]. Studied results show great potential for applications in TEG at high temperature and have thus drawn much attention over the years. This chapter targets to summarize the research and development of exploring the usage of TE oxide-based materials for high-temperature TEGs. The performance of oxide-based materials and devices in the first part of this chapter will be considered under the ideal theoretical condition of no parasitic losses and disregard other factors such as mechanical properties, thermal expansion coefficient, and chemical stability.

In general, the conversion efficiency of a TEG is governed by device figure of merit $ZT$.

\[
ZT = \frac{S^2T}{KR},
\]

where $S$, $K$ and $R$ are the total Seebeck coefficient, the total thermal conductance, and the total resistance of the module, respectively.
The maximum conversion efficiency of TE module is often given as
\[
\eta_{\text{max}} = \frac{T_h - T_c}{T_h} \frac{\sqrt{1 + Z^2 T} - 1}{\sqrt{1 + Z^2 T} + (T_c/T_h)}.
\] (22.2)

The first term of Equation 22.2 is known as the Carnot efficiency, which is the upper limit conversion efficiency at infinite ZT, as shown in Figure 22.1. The second term is the contribution by the intrinsic properties of the TE materials, i.e., Seebeck coefficient and electrical and thermal conductivities. It is clearly seen that the maximum conversion efficiency of module increases by increasing the hot side temperature as a result of the contribution from the first term in Equation 22.2, i.e., Carnot efficiency. For high-temperature TEG application in air, devices fabricated from intermetallic compounds often show oxidation, sublimation, and volatility processes in the high-temperature range [4,5]. Therefore, encapsulation is needed to protect the devices. By considering the reasons mentioned earlier, the high-temperature oxide TE module is of great interest in high-temperature heat–electricity conversion, e.g., waste heat recovery from steel industrial and thermal power plants.

### 22.2 Calculated Efficiency of All Oxide Materials and Modules

There have been many studies over the years on the development of high-performance TE oxide materials. Figure 22.2a and b shows a selection of the state-of-the-art material figure of merit ZT (Z = S²/ρκ), for p-type and n-type oxide materials. Oxide materials exhibit widely their peak ZT values ranging from 0.1 at 1173 K for NiO [6], NdCoO₃ [7], and LaSrCuO₄ [8], 0.2 for Ca₂Co₂O₆ [9], and 0.65 for Ca₃Co₄O₉ nanocomposite [10] at 1173 K and to the value of
close to 1 at 1000 K for Na$_2$CoO$_4$ [11] and over 1 at 900 K for BiCuSeO [12]. For n-type oxide materials, the LaNiO$_3$ [13,14] attains the lowest magnitude of $ZT < 0.05$ in the temperature range of 300–1100 K. Perovskites BaSrPbO$_3$ [15], CaMnO$_3$ [16], and SrTiO$_3$ [17] obtain a medium $ZT$ value of around 0.3 at 1173 K, while dual doped ZnO [18] presents the highest peak $ZT$ value of 0.65 at 1173 K. Since most oxide materials (except BiCuSeO) have a small $ZT$ value in the low and mid-temperature ranges of 300–700 K, TEG-based oxide has gained much interest mainly for high-temperature waste heat harvesting applications, e.g., steel or cement industrials.

To estimate the efficiency of oxide materials under the actual working condition, we have used numerical modeling [1,19–21].

The efficiency of a single material can be expressed as [1,20,21]

$$\eta = 1 - \frac{S_c T_c + 1/u_c}{S_h T_h + 1/u_h}, \quad (22.3)$$

where $S$, $T$, $u$, $S_h$, $T_h$, and $u_h$ are the Seebeck coefficient, temperature, and reduced current density at the cold- (subscript by c) and hot-side (subscript by h) temperatures, respectively. The relative current density (reduced current
density) \( \eta = J/\kappa \nabla T \) is defined as the ratio of the electrical current density \( J \) to the conduction heat flux \( \kappa \) \[1,20,21\]. In this calculation, the cold-side temperature is fixed at 300 K while the temperature of the hot side is varied. It should be noted that neither heat losses nor electrical losses are included in these calculations. Therefore, the obtained values can be considered as the upper limit performance achievable from the intrinsic TE properties. Figure 22.2c and d shows the calculated efficiency as a function of the hot-side temperature (cold side fixed at 300 K) for p-type and n-type oxide materials as a single element. For the conversion efficiency of all p-type curves in Figure 22.2c, the order of efficiency values of a single material has a similar tendency with \( ZT \) curves, as shown in Figure 22.2a. With the smallest \( ZT \) values, NiO, NdCoO\(_3\), and LaSrCuO\(_4\) have a maximum efficiency of less than 1% in the whole temperature of 300 and 1173 K. Although the \( ZT \) value of Ca\(_3\)Co\(_2\)O\(_9\) rapidly increases with increasing temperature (Figure 22.2a), its conversion efficiency is still lower than 1% due to low-performance contribution in the whole temperature range. With the maximum conversion efficiency of 5.4%, the Ca\(_3\)Co\(_2\)O\(_9\) is the most the promising p-type oxide material for temperature region of above 1000 K, while below 1000 K, Na\(_2\)CoO\(_4\) and BiCuSeO oxyselenides exhibit conversion efficiencies of 10% and 12%, respectively. As for the n-type, LaNiO\(_3\) shows an efficiency value which is lower than 0.1%, while BaSrPbO\(_3\) shows a maximum value of around 2%. Interestingly, although the peak \( ZT \) of SrTiO\(_3\) exhibits lower value, its maximum conversion efficiency is higher than that of dual doped ZnO; it is due to the conversion efficiency results from the accumulated performance of the whole working temperature range. The \( ZT \) value of CaMnO\(_3\) is higher than that of the dual doped ZnO at temperatures below 600 K, while it is significantly lower in the temperature region of above 600 K, as shown in Figure 22.2b. However, the efficiency value of CaMnO\(_3\) is higher than the efficiency of dual doped ZnO in the whole temperature range from 300 to 1000 K. In fact, the total conversion efficiency can be calculated as \( \eta = \eta_c \eta_r \), where \( \eta_c = (T_h - T_c)/T_c \) is the Carnot efficiency, and \( \eta_r = \frac{[1 - \mu (S/z)]}{[1 + (1/\mu ST)]} \) is the reduced efficiency \[21\]. Mathematically, \( \eta_r \) maximizes when \( \mu = \sqrt{1 + zT - 1}/zT = s \), which is called the compatibility factor \[21,22\]. In case where \( s = \mu \), the material can obtain the maximum achievable total conversion efficiency. The smaller the value of \( (s - \mu) \), the larger achievable total conversion efficiency is obtained. Therefore, \( s \) and \( \mu \) values are important parameters and are needed to be considered for designing high-efficiency materials \[1,23,24\].

By connecting the p-type and n-type oxide elements, the efficiency of a unicouple can be computed as

\[
\eta_{\text{unicouple}} = 1 - \frac{S_{c,p} T_{c,p} + 1/\mu_{c,p} - S_{c,n} T_{n,c} - 1/\mu_{c,n}}{S_{h,p} T_{h,p} + 1/\mu_{h,p} - S_{h,n} T_{n,h} - 1/\mu_{h,n}}, \tag{22.4}
\]

where the subscripts n and p symbolize the n- and p-type legs. The calculated efficiency using Equation 22.4 for some promising unicouple-based oxide TE materials are summarized in Table 22.1. The hot-side temperature is defined by...
the limited stability of the comprising TE materials, e.g., 900 K for any unicouple made by p-BiCuSeO and n-SrTiO3. It can be seen that the combination of p- and n-type oxides resulted in different conversion efficiencies; the unicouples with Ca3Co2O6 show the smallest values ranging from 0.9% to 1.7%; in contrast, the unicouple of p-BiCuSeO and n-SrTiO3 exhibits the highest conversion efficiency of up to 7.9%. For the highest hot-side temperature of 1173 K, the p-type Ca3Co4O9 combines with either n-type ZnO or CaMnO3, showing a 5% efficiency, which is comparable with that of a current commercially available TE module based on Bi-Te materials. These results suggest that oxide TE materials have a great potential for high-temperature TEG for waste heat harvesting.

### TABLE 22.1 Calculated Maximum Conversion Efficiency of Unicouples with Various Maximum Hot-Side Temperatures and the Combination of p–n Oxide Leg

<table>
<thead>
<tr>
<th>Material</th>
<th>Ca3Co4O9 (T_{hot}/1173 K)</th>
<th>Ca3Co2O6 (T_{hot}/1173 K)</th>
<th>Na2CoO4 (T_{hot}/1000 K)</th>
<th>BiCuSeO (T_{hot}/900 K)</th>
</tr>
</thead>
<tbody>
<tr>
<td>ZnO (T_{hot}/1173 K)</td>
<td>5.3</td>
<td>1.4</td>
<td>6.1</td>
<td>5.2</td>
</tr>
<tr>
<td>CaMnO3 (T_{hot}/1173 K)</td>
<td>5.0</td>
<td>1.7</td>
<td>5.7</td>
<td>5.1</td>
</tr>
<tr>
<td>Ba0.2Sr0.8PbO3 (T_{hot}/1000 K)</td>
<td>2.9</td>
<td>0.9</td>
<td>3.1</td>
<td>3.6</td>
</tr>
<tr>
<td>SrTiO3 (T_{hot}/900 K)</td>
<td>4.1</td>
<td>0.89</td>
<td>7.0</td>
<td>7.9</td>
</tr>
</tbody>
</table>

### 22.3 Oxide Module Construction and Characterization

Figure 22.3 shows the process steps for a typical module fabrication and characterization. The p- and n-type material processing first optimizes their

![Figure 22.3](image)
TE properties. The solid-state reaction is the preferred synthesis method for fabricating the oxide TE powder materials. For densification, hot press or SPS techniques are often used [19,25–28]. Following the synthesis and the densification, the TE properties of the materials are measured as a function of the temperature and fed into a numerical model, where the optimal output performance of the module is then calculated for a given optimized geometry of the legs and number of p–n couples [25]. The p- and n-type legs were then cut into the dimensions suggested by the modeling results. The unicouple contains two TE materials, n- and p-type, coupled together with a metal electrode. Silver (Ag) is the most used material for electrodes in module assembly [8,25–45] since it has high electrical and thermal conductivities and can resist high temperature in air.

The joining of Ag electrodes with TE legs is often done by the brazing method with filler materials which can be either pure Ag [25,28,35], Pt paste [29], Ag paste [31,33,38–45] or a mixture of Ag and oxide powder [30,32,37] depending on the materials in use. Joining by diffusion between oxide materials and Ag electrodes was also suggested, as described by Souma et al. [26,27]. This technique can tightly join two materials, be faster than brazing joining method, and does not require a filler metal. One of the crucial demands from the joining contacts is low electrical resistance and stability. A low resistance and stable contact are required since they ensure high performance and long-term stability of the TE module. Figure 22.4 shows typical experimental results of contact resistances of single p-type Ca₃Co₄O₉, single-segmented p-type Ca₃Co₄O₉/HH alloy, and n-type-doped ZnO oxide with Ag electrode using brazing joining method [19,25]. There is no sign of cracks or air gap observed at the interfaces, which results in low contact resistance.

![Figure 22.4](image)

**FIGURE 22.4** Picture of interface and contact resistance of the Ag with p-type and n-type oxide materials. (Hung, L. T. et al.: Segmented thermoelectric oxide-based module for high-temperature waste heat harvesting. *Energy Technology*. 2015. 3. 1143–1151. Copyright Wiley-VCH Verlag GmbH & Co. KGaA. Reproduced with permission.)
in the range of 100–500 $\mu\Omega$ cm$^2$ [19,25]. The entire module with the electrical insulation substrate is finally assembled by hot press method. It is crucial that each step in Figure 22.3 should be properly done, and any failure in one of the steps must be carefully checked or come back to optimize the previous steps.

### 22.4 All Oxide Thermoelectric Modules

Table 22.2 is a summary of TE oxide modules reported in the literature over the last 16 years. The size of those modules is varied largely from a TEG module comprising of a single unicouple up to 140 unicouples. Although the $ZT$ value of 0.93 at 960 K of the p-type NaCo$_2$O$_4$ is very high, only a few oxide modules have been studied using NaCo$_2$O$_4$ [26,27,36] as p-type leg. The p-type Ca$_3$Co$_4$O$_9$ is mostly used because this material is highly stable at a high temperature in air [46]. For n-type, CaMnO$_3$ or doped ZnO are dominated materials since the higher $ZT$ n-type SrTiO$_3$ is not stable in air at an elevated temperature [2]. As shown in Table 22.2, the power generation characteristics have been conducted under various conditions of the hot- and cold-side temperatures, resulting in differences in open circuit voltage and maximum output power. To give a comparison of studied oxide modules, the power density is often used [25,39,45]. However, one should be careful when using the value of power density, which might also lead to an unreasonable conclusion, because the power density depends on the length and the number of the TE legs. A more clear explanation can be described in the following.

The performance of module comprising p–n couples can be expressed in terms of the output voltage and current values. The open circuit voltage $V_{OC}$ can be directly calculated from the definition of the Seebeck coefficient as [47]

$$V_{OC} = n \int_{T_c}^{T_h} \{ S_p (T) - S_n (T) \} dT,$$

(22.5)

where $n$ is the number of p–n couples, $S_p$ and $S_n$ are the Seebeck coefficients of p- and n-type legs, respectively. Moreover, the value of the electric current $I$ can be calculated from Ohm’s law as

$$I = \frac{V_{OC}}{R_{\text{int}} + R_{\text{load}}},$$

(22.6)

where $R_{\text{int}}$ is the total of the internal resistances of the module that is contributed by the sum of the resistances of the p–n legs, and $R_{\text{load}}$ is the external resistive load. The internal resistance can be described as $R_{\text{int}} = R_{\text{legs}} + R_C$. 
### TABLE 22.2 Power Generation Characteristics of Oxide-Based TE Modules Reported in the Literature

<table>
<thead>
<tr>
<th>Ref.</th>
<th>Year</th>
<th>Materials</th>
<th>No. of p–n Couples</th>
<th>Jointing Technique</th>
<th>$T_{\text{hot}}$ (K)</th>
<th>$\Delta T$ (K)</th>
<th>$V_{\text{OC}}$ (V)</th>
<th>$P_{\text{max}}$ (mW)</th>
<th>Leg Size (mm)</th>
<th>Power Density (mW/cm²)</th>
<th>Efficiency [%]</th>
</tr>
</thead>
<tbody>
<tr>
<td>[28]</td>
<td>2001</td>
<td>p-Li$<em>{0.025}$Ni$</em>{0.975}$O$<em>{n}$-Ba$</em>{0.2}$Sr$_{0.8}$PbO$_3$</td>
<td>1</td>
<td>Cosintering, cold side Ag paste</td>
<td>978</td>
<td>552</td>
<td>0.12</td>
<td>0.12</td>
<td>7.91</td>
<td>3 × 4 × 14</td>
<td>32.9</td>
</tr>
<tr>
<td>[28]</td>
<td>2001</td>
<td>p-Li$<em>{0.025}$Ni$</em>{0.975}$O$<em>{n}$-Ba$</em>{0.2}$Sr$_{0.8}$PbO$_3$</td>
<td>4</td>
<td>Cosintering, cold side Ag paste</td>
<td>1164</td>
<td>539</td>
<td>0.4</td>
<td>0.1</td>
<td>34.4</td>
<td>3 × 4 × 14</td>
<td>35.8</td>
</tr>
<tr>
<td>Matsubara et al. [29]</td>
<td>2001</td>
<td>p-Ca$<em>2$Gd$</em>{0.2}$Co$<em>4$O$<em>9$-Ca$</em>{0.92}$La$</em>{0.08}$MnO$_3$</td>
<td>8</td>
<td>Pt paste</td>
<td>1046</td>
<td>390</td>
<td>0.98</td>
<td>0.12</td>
<td>63.5</td>
<td>3 × 3 × 25</td>
<td>44.1</td>
</tr>
<tr>
<td>Funahashi et al. [30]</td>
<td>2004</td>
<td>p-Ca$<em>2$Bi$</em>{0.3}$Co$<em>4$O$<em>9$-La$</em>{0.9}$Bi$</em>{0.1}$NiO$_3$</td>
<td>1</td>
<td>Ag paste, 6 wt.% oxide powder</td>
<td>1073</td>
<td>500</td>
<td>0.1</td>
<td>0.1</td>
<td>94</td>
<td>3.7 × 4–5.5 × 4.7</td>
<td>317–280a</td>
</tr>
<tr>
<td>Reddy et al. [31]</td>
<td>2005</td>
<td>p-Ca$_2$Co$<em>4$O$<em>9$-n-Ca$</em>{0.95}$Sm$</em>{0.05}$MnO$_3$</td>
<td>2</td>
<td>Ag paste</td>
<td>1025</td>
<td>925</td>
<td>0.4</td>
<td>0.2</td>
<td>31.5–24.5</td>
<td>4 × 4 × 5</td>
<td>98.4</td>
</tr>
<tr>
<td>Funahashi et al. [32]</td>
<td>2006</td>
<td>p-Ca$<em>2$Bi$</em>{0.3}$Co$<em>4$O$<em>9$-n-La$</em>{0.9}$Bi$</em>{0.1}$NiO$_3$</td>
<td>140</td>
<td>Ag paste, 6 wt.% oxide powder</td>
<td>1072</td>
<td>551</td>
<td>4.5</td>
<td>0.03</td>
<td>150</td>
<td>1.3 × 6 × 5</td>
<td>31.7</td>
</tr>
<tr>
<td>Souma et al. [26]</td>
<td>2006</td>
<td>p-NaCo$<em>2$O$<em>4$-n-Zn$</em>{0.99}$Al$</em>{0.01}$O</td>
<td>12</td>
<td>Diffusion welding</td>
<td>839</td>
<td>462</td>
<td>0.8</td>
<td>0.06</td>
<td>58</td>
<td>3 × 4 × 10</td>
<td>20.1</td>
</tr>
<tr>
<td>Urata et al. [33]</td>
<td>2006</td>
<td>p-Ca$<em>2$Bi$</em>{0.3}$Co$<em>4$O$<em>9$-n-Co$</em>{0.95}$Mn$</em>{0.05}$O$_3$</td>
<td>8</td>
<td>Ag paste</td>
<td>987</td>
<td>565</td>
<td>1</td>
<td>0.12</td>
<td>170</td>
<td>5 × 5 × 4.5</td>
<td>42.5</td>
</tr>
<tr>
<td>Funahashi et al. [34]</td>
<td>2007</td>
<td>p-Ca$<em>2$Bi$</em>{0.3}$Co$<em>4$O$<em>9$-n-La$</em>{0.9}$Bi$</em>{0.1}$NiO$_3$</td>
<td>1</td>
<td>Ag paste</td>
<td>1073</td>
<td>500</td>
<td>0.1</td>
<td>0.1</td>
<td>177</td>
<td>3.7 × 4–5.5 × 4.7</td>
<td>528–598a</td>
</tr>
<tr>
<td>Urata et al. [35]</td>
<td>2007</td>
<td>p-Ca$<em>2$Bi$</em>{0.3}$Co$<em>4$O$<em>9$-n-Co$</em>{0.95}$Mn$</em>{0.05}$O$_3$</td>
<td>8</td>
<td>Ag</td>
<td>1273</td>
<td>975</td>
<td>0.7</td>
<td>0.09</td>
<td>340</td>
<td>5 × 5 × 4.5</td>
<td>85</td>
</tr>
<tr>
<td>Souma et al. [27]</td>
<td>2008</td>
<td>p-NaCo$<em>2$O$<em>4$-n-Zn$</em>{0.99}$Al$</em>{0.01}$O</td>
<td>12</td>
<td>Diffusion welding</td>
<td>934</td>
<td>455</td>
<td>0.8</td>
<td>0.067</td>
<td>52.5</td>
<td>3 × 4 × 10</td>
<td>18.2</td>
</tr>
<tr>
<td>Park et al. [36]</td>
<td>2009</td>
<td>p-Na(Co$<em>{0.95}$Ni$</em>{0.05}$)$<em>2$O$<em>4$-n-Zn$</em>{0.99}$Sn$</em>{0.01}$O</td>
<td>1</td>
<td>Ag paste</td>
<td>923</td>
<td>422</td>
<td>0.14</td>
<td>0.14</td>
<td>0.027</td>
<td>7 × 7 × 17</td>
<td>0.03</td>
</tr>
<tr>
<td>Tomeš et al. [8]</td>
<td>2010</td>
<td>p-La$<em>{1.98}$Sr$</em>{0.02}$CuO$<em>4$-n-Co$</em>{0.95}$Mn$_{0.05}$O$_3$</td>
<td>2</td>
<td>Ag paste</td>
<td>941</td>
<td>622</td>
<td>0.664</td>
<td>0.23</td>
<td>88.8</td>
<td>4.5 × 4.5 × 5</td>
<td>109.6</td>
</tr>
</tbody>
</table>

(Continued)
<table>
<thead>
<tr>
<th>Ref.</th>
<th>Year</th>
<th>Materials</th>
<th>No. of p-n Couples</th>
<th>Jointing Technique</th>
<th>$T_{\text{hot}}$ (K)</th>
<th>$\Delta T$ (K)</th>
<th>$V_{OC}$ (V)</th>
<th>$V_{OC}$/Couples (V)</th>
<th>$P_{\text{max}}$ (mW)</th>
<th>Leg Size (mm)</th>
<th>Power Density (mW/cm$^2$)</th>
<th>Efficiency [%]</th>
<th>Cal</th>
<th>Mea</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tomeš et al. [37]</td>
<td>2010</td>
<td>$p$-GdCo$<em>{0.95}$Ni$</em>{0.05}$O$<em>3$ $n$-CaMn$</em>{0.98}$Mo$_{0.02}$O$_3$</td>
<td>2</td>
<td>Ag/CuO paste</td>
<td>800</td>
<td>500</td>
<td>0.34</td>
<td>0.17</td>
<td>40</td>
<td>$4 \times 4 \times 5$</td>
<td>62.5</td>
<td>–</td>
<td>–</td>
<td></td>
</tr>
<tr>
<td>Choi et al. [38]</td>
<td>2011</td>
<td>$p$-Ca$_3$Co$_4$O$_9$ $n$-(ZnO)$_7$In$_2$O$_3$</td>
<td>44</td>
<td>Ag paste</td>
<td>1100</td>
<td>673</td>
<td>1.8</td>
<td>0.04</td>
<td>423</td>
<td>$15 \times 15 \times 27$</td>
<td>2.1</td>
<td>–</td>
<td>–</td>
<td></td>
</tr>
<tr>
<td>Lim et al. [39]</td>
<td>2011</td>
<td>$p$-Ca$_3$Co$<em>4$O$<em>9$ $n$-Ca$</em>{0.9}$Nd$</em>{0.1}$MnO$_3$</td>
<td>1</td>
<td>Ag paste</td>
<td>1175</td>
<td>727</td>
<td>0.19</td>
<td>0.19</td>
<td>95</td>
<td>$8.5 \times 6 \times 10$</td>
<td>93.2</td>
<td>–</td>
<td>–</td>
<td></td>
</tr>
<tr>
<td>Inagoya et al. [40]</td>
<td>2011</td>
<td>$p$Nd$<em>{0.995}$Ca$</em>{0.005}$CoO$<em>3$ $n$-LaCo$</em>{0.99}$Mn$_{0.01}$O$_3$</td>
<td>10</td>
<td>Ag paste</td>
<td>704</td>
<td>399</td>
<td>1</td>
<td>0.44</td>
<td>23 mm$^2 \times 20$</td>
<td>9.6</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td></td>
</tr>
<tr>
<td>Han et al. [41]</td>
<td>2011</td>
<td>$p$-Ca$<em>3$Co$<em>4$Ag$</em>{0.2}$O$<em>9$ $n$-Ca$</em>{0.98}$Sm$</em>{0.02}$O$_3$</td>
<td>2</td>
<td>Ag paste</td>
<td>873</td>
<td>523</td>
<td>0.33</td>
<td>0.16</td>
<td>36.8</td>
<td>$3 \times 6 \times 6$</td>
<td>51.1</td>
<td>–</td>
<td>–</td>
<td></td>
</tr>
<tr>
<td>Funahashi [42]</td>
<td>2011</td>
<td>$p$-Ca$<em>3$Bi$</em>{0.3}$Co$<em>4$O$<em>9$ $n$-Ca$</em>{0.98}$Sm$</em>{0.02}$O$_3$</td>
<td>108</td>
<td>Ag paste</td>
<td>873</td>
<td>400</td>
<td>10.5</td>
<td>0.097</td>
<td>12000</td>
<td>$7 \times 3.5 \times 5$</td>
<td>226.7$^b$</td>
<td>–</td>
<td>–</td>
<td></td>
</tr>
<tr>
<td>Park and Lee [43]</td>
<td>2013</td>
<td>$p$-Ca$<em>{0.92}$Co$</em>{0.08}$O$<em>3$ $n$-Ca$</em>{0.9}$Yb$_{0.1}$MnO$_3$</td>
<td>4</td>
<td>Ag paste</td>
<td>937</td>
<td>321</td>
<td>0.28</td>
<td>0.07</td>
<td>31</td>
<td>$7 \times 9 \times 25$</td>
<td>6.15</td>
<td>–</td>
<td>–</td>
<td></td>
</tr>
<tr>
<td>Mele et al. [44]</td>
<td>2014</td>
<td>$p$-Ca$_3$Co$<em>4$O$<em>9$ $n$-Ca$</em>{0.98}$Dy$</em>{0.02}$MnO$_3$</td>
<td>6</td>
<td>Ag paste</td>
<td>773</td>
<td>248</td>
<td>0.12</td>
<td>0.02</td>
<td>2.26</td>
<td>$4 \times 4 \times 10$</td>
<td>1.2</td>
<td>–</td>
<td>–</td>
<td></td>
</tr>
<tr>
<td>Saucke et al. [45]</td>
<td>2015</td>
<td>$p$-Ca$<em>{0.99}$Co$</em>{0.01}$O$<em>3$ $n$-Zn$</em>{0.09}$Al$_{0.01}$O$_2$</td>
<td>2</td>
<td>Ag paste</td>
<td>1051</td>
<td>727</td>
<td>0.36</td>
<td>0.18</td>
<td>200.4</td>
<td>$40.77 \text{ mm}^2 \times 4$</td>
<td>491$^c$</td>
<td>1.08</td>
<td>1.08</td>
<td></td>
</tr>
<tr>
<td>Hung et al. [25]</td>
<td>2015</td>
<td>$p$-Ca$_3$Co$<em>4$O$<em>9$ $n$-Zn$</em>{0.09}$Al$</em>{0.01}$O$_2$</td>
<td>4</td>
<td>Ag</td>
<td>1173</td>
<td>700</td>
<td>0.67</td>
<td>0.17</td>
<td>256</td>
<td>$4 \times 4 \times 8$</td>
<td>200</td>
<td>0.72</td>
<td>0.37</td>
<td></td>
</tr>
<tr>
<td>Hung et al. [25]</td>
<td>2015</td>
<td>$p$Hf/Co$_3$Co$<em>4$O$<em>9$ $n$-Zn$</em>{0.09}$Al$</em>{0.01}$O$_2$</td>
<td>4</td>
<td>Ag</td>
<td>1173</td>
<td>700</td>
<td>0.76</td>
<td>0.19</td>
<td>829</td>
<td>$4 \times 4 \times 8$</td>
<td>650</td>
<td>1.8</td>
<td>1.16</td>
<td></td>
</tr>
</tbody>
</table>

$^a$ The reported data from the same author is somewhat inconsistent. In addition, the theoretical calculation under ideal conditions, i.e., no losses shows the maximum power density of 200 mW/cm$^2$. Therefore, experimental needs to be confirmed.

$^b$ The value is calculated based on the experimental data in the article.

$^c$ The length of the legs is computed from the ratio of volume and area.
and $R_{\text{Load}}$, where $R_{\text{legs}}$ is the sum of the resistances of the p–n legs without metal electrodes, and $R_C$ is the contact resistance contribution from all interfacial contact between electrodes and the legs. The output power as a function of electric current and the resistive load is given by

$$P = I^2 R_{\text{Load}} = V_{\text{OC}}^2 \left( \frac{R_{\text{Load}}}{R_{\text{int}} + R_{\text{Load}}} \right)^2. \quad (22.7)$$

The maximum output power is obtained when the external load resistance is equal to the internal resistance ($R_{\text{int}} = R_{\text{Load}}$):

$$P_{\text{Max}} = \frac{V_{\text{OC}}^2}{4R_{\text{int}}} = \frac{V_{\text{OC}}^2}{4R_C + 4R_{\text{legs}}} = \frac{V_{\text{OC}}^2}{4R_C + 4n\left[\rho_p \left(l_p / A_p\right) + \rho_n \left(l_n / A_n\right)\right]}, \quad (22.8)$$

where $\rho_p$, $\rho_n$, $A_p$, $A_n$, $l_p$, and $l_n$ are values of the electrical resistivity, cross-sectional area, and length of the p-type (subscript p) and n-type (subscript n), respectively.

It is clearly seen from Equations 22.5 and 22.8 that the maximum output power is proportional to the total number of the p–n couples and Seebeck coefficient, but its magnitude is inversely proportional to the length of p-type and n-type legs, i.e., the shorter length will provide higher output power.

The power density is defined as the ratio of $P_{\text{Max}}$ divided by the total area times the number of legs $n(A_p + A_n)$:

$$P_{\text{density}} = \frac{P_{\text{Max}}}{n(A_p + A_n)}. \quad (22.9)$$

Equations 22.8 and 22.9 indicate that the power density increases by decreasing the length of the TE legs as result of increasing $P_{\text{Max}}$. As presented in Table 22.2, the highest value of power density falls on the modules with a short leg length such as those in the studies by Funahashi [42] and Saucke et al. In contrast, the module constructed from a longer length has a low value of powder density, e.g., from the studies by Souma et al. [26] and Matsubara et al. [29].

To compare the performance of modules, the conversion efficiency $\eta$, which is the ratio of electric power to the total heat input, is a more appropriate way to use [47]. $\eta$ can be defined as:

$$\eta = \frac{P}{Q_h} = \frac{P}{K(T_h - T_i) + V_{\text{OC}} T_i I - 0.5 I^2 R_{\text{legs}}}. \quad (22.10)$$

Equations 22.7 and 22.10 imply that the efficiency value of the devices is independent from the length of TE legs. As can be seen from Table 22.2, there
is only a few research reported on the value of efficiency making it difficult to collect the data. This may be because the measurement of the heat flux on the hot side of the TEG is complicated especially in the high-temperature range. The maximum obtained efficiency value of all studied data is currently less than 2%, and this value is far from theoretical calculation values, as listed in Table 22.1. One of the main sources, which lead to low conversion efficiency value, is the contact resistances, i.e., high electrical and thermal contact resistances at the interface of oxide materials and metal electrodes. In the experiment, the contact resistance of oxide–metal is in the range of 25–400 $\mu\Omega$ cm$^2$ for Ag and Ca$_3$Co$_4$O$_9$ [19,25,45], and it is in the range of 100–500 $\mu\Omega$ cm$^2$ for Ag and doped ZnO [25]. Figure 22.5 gives an example of how contact resistance influences the output performance of the oxide module. An interfacial contact resistance of 248 m$\Omega$ leads to the suppression of the maximum output power from 575 mW for the ideal theoretical condition to 256 mW for the practically measured condition. Therefore, the study of interfacial contact resistance is a critical area of research to improve the performance of any TEG. In summary, although considerable attempts have been made to produce highly efficient TE oxide modules, the performance of those reported oxide TEGs is still low due to the low performance of oxide materials in the low-mid temperature and high interfacial oxide–metal contact resistances.

22.5 Segmented Oxide-Based Modules

As aforementioned, one of the main drawbacks of reported oxide TEG is the low performance of oxide materials in the temperature range of 300–700 K. In this context, there are two possible solutions where oxide TEG can be
combined with other materials: either in cascaded or segmented generators. In a cascade generator, the oxide TEG is stacked with other high-performance TEG working at a mid-low temperature that is normally made of alloys. By this way, the performance of the module can be improved with about twice compared to that of single oxide-based module [42]. However, this type of module often requires an additional electronic device to collect the maximum output of two electric circuits in each single stage. The electrical wires are needed for the connection, and hence, a large amount of heat losses exists in electrical connection wires either heat conductance loss due to the low electrical resistivity or Joule heating loss due to the high electrical resistance [48]. In contrast, a segmented TEG requires only a single electric circuit. In a segmented TE module, the p-type and/or n-type legs are designed by a segmentation of different materials with their highest value of $ZT$. One of the criteria to ensure an improvement in efficiency is that the difference in compatibility factor \( s = \left( \frac{1 + zT}{T} \right) \) values of the selected materials have to be within a factor of two [1,20,22,49]. According to Hung et al. [50], the high conversion efficiency of 12.2% can be achieved in a unicouple of segmented p-type $\text{Ca}_3\text{Co}_4\text{O}_9$ and n-type dual doped $\text{ZnO}$ with state-of-the-art TE materials of, e.g., $\text{BiTe}$, $\text{PbTe}$, and HH alloys. Figure 22.6 shows the result of a segmented oxide module using n-type $\text{Zn}_{0.98}\text{Al}_{0.02}\text{O}$ and segmented p-type half-Heusler-$\text{Ca}_3\text{Co}_4\text{O}_9$. Its performance was analyzed and compared to nonsegmented module with similar dimension under the same testing conditions. The obtained output power of those modules under the same measurement conditions clearly indicates that segmentation is an effective way to boot up the performance of oxide module. An efficiency of 1.16% is achieved for segmented module, which is three times higher than that of nonsegmented one, as shown in Table 22.2. Furthermore, the conversion

\[ T_{\text{hot}} = 1173 \text{ K} \]
\[ T_{\text{cold}} = \sim 473 \text{ K} \]

**FIGURE 22.6** Power generation characteristics of 4 p–n couples oxide module using n-type $\text{Zn}_{0.98}\text{Al}_{0.02}$ and p-type $\text{Ca}_3\text{Co}_4\text{O}_9$ and 4 p–n couples segmented oxide module using n-type $\text{Zn}_{0.98}\text{Al}_{0.02}$ and segmented p-type half-Heusler-$\text{Ca}_3\text{Co}_4\text{O}_9$. (Hung, L. T. et al.: Segmented thermoelectric oxide-based module for high-temperature waste heat harvesting. *Energy Technology*. 2015. 3. 1143–1151. Copyright Wiley-VCH Verlag GmbH & Co. KGaA. Reproduced with permission.)
efficiency of 5% has also been achieved in single p-type segmented leg of misfit-layered cobaltite and HH alloy [19]. In both cases, the segmented legs are highly stable at a high temperature in air.

22.6 Outlook and Challenges

Oxide TE modules have been rapidly developed in the last 16 years with many attempts to improve the conversion efficiency of TEG modules for high-temperature waste heat harvesting. Some of the efforts have been successfully realized, and promising devices are now commercially available [51]. The theoretical calculation has pointed out that TEG with the efficiency of 7.9% could be possibly obtained in oxide materials if parasitic losses can be minimized.

There is a big gap existing between the performance of materials and performance of devices. Although many studies have been conducted to improve the performance of oxide materials, the maximum conversion efficiency of current oxide module is still lower than 2%. In fact, TE properties of oxide materials are studied as a function of temperature, thermal cycling, or heat treatment duration in which all parasitic losses were disregarded. In practice, oxide TE legs in module operate under a large temperature gradient and generating power conditions with the contribution of electrical and thermal losses. Thus, studying the performance of oxide material under working conditions would help reduce the currently existing gap of materials and devices.

We have also clearly pointed out that one of the main sources leading to the decrease in the performance of oxide TEG is the contact resistances. Understanding the contact resistance requires more study to theoretically clarify the origin of the resistance and to not only make a good electrical connection but also have durability from thermal cycling and large temperature span. Also, studying metal–oxide interfacial contact resistances under module level could be an important topic.

The combination of taking the advantages of oxides and other intermetallic alloys in segmented TEG has been realized as one of the most efficient ways to produce high efficiency. The stable and high conversion efficiency of 5% was achieved on segmented p-type-based oxide materials. The future study, therefore, should target segmented n-type oxide materials.

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