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*Published in:*  
Energy and Buildings

*Link to article, DOI:*  
[10.1016/j.enbuild.2017.06.038](https://doi.org/10.1016/j.enbuild.2017.06.038)

*Publication date:*  
2017

*Document Version*  
Peer reviewed version

[Link back to DTU Orbit](#)

*Citation (APA):*  
Elarga, H., Fantucci, S., Serra, V., Zecchin, R., & Benini, E. (2017). Experimental and numerical analyses on thermal performance of different typologies of PCMs integrated in the roof space. *Energy and Buildings*, 150, 546-557. <https://doi.org/10.1016/j.enbuild.2017.06.038>

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1 **Experimental and numerical analyses on thermal performance of different typologies of PCMs**  
2 **integrated in the roof space**

3  
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15

16 **ABSTRACT**

17 The study investigates the thermal performances of Phase Change Materials (PCM) integrated in a roof space to be used  
18 as a residential attic in Torino, Italy. Three different solutions were applied to a roof continuously monitored under  
19 summer climatic conditions. The roof was divided into three portions, one, the bare roof, representing the reference case  
20 without PCMs, the other two integrating two PCM's typologies with different melting/solidification temperatures range.  
21 A numerical model was furthermore developed implementing the equivalent capacitance numerical method to describe  
22 the substance phase transition and the measured data set were used for its validation. The study demonstrates that PCM-  
23 enhanced components are a promising solution toward a higher thermal performance efficiency in roof attic spaces  
24 during summer season. Experimental results showed a reduction of the ongoing heat peak load between 13% and 59%  
25 depending on the PCM typology, highlighting that to reach the expected performance the proper PCM type should be  
26 carefully selected.

27

28 **Keywords:** PCM; Roof attic space; RC model; Numerical simulations; Experimental analysis

29

30 **1. Introduction**

31 The Climate change is jeopardizing living sustainability on the planet. This change is affecting different life aspects  
32 such as water resources, coastal zone, marine systems and energy consumption[1]. Concerning the latter aspect, the  
33 building sector is estimated to be ~40% from the total energy consumption in EU. Space heating and cooling energy  
34 demands from the building envelope represent about 47% of the total energy demands within a typical  
35 residential/commercial building [2]. Generally, in residential buildings, the surface that has the largest exposure to the  
36 outdoor environment and, consequently, most subjected to the climate change is represented by the roof. Indeed the  
37 U.S. Department of energy estimate that the roof attic space alone are responsible for 12%-14% of the energy required  
38 for space heating and cooling in U.S.[3]. This aspect assumes relevant importance since the conversion of roof attic in  
39 habitable spaces represents one of the principal interventions to increase the density of urban area without consuming

40 new soil. In Italy, several policies at regional level have promoted this retrofit action, which presents an added value to  
41 other conventional interventions aimed at refurbishing buildings envelope and building services [4]. A key issue in the  
42 conversion of attic space is represented by the thermal refurbishment of the roof, which presents, with respect to a  
43 typical dwelling unit a larger exposed area, responsible of high thermal gains/losses respectively in summer and winter  
44 [5]. As far as the energy retrofit of an existing roof, the addition of new insulation layers raises particular issues which  
45 have to be duly taken into account as the height reduction of the internal space and the structural load increase on the  
46 existing roof. In the latest years, a number of technologies have been developed to improve winter and summer  
47 behavior of roofs components and overcome these limitations through reduced thickness and weight of super insulating  
48 materials [6][7][8], radiant heat barriers [9][10], ventilated air cavity [11][12][13], and cool materials [14][15][16]. A  
49 different approach, so far not so investigated in this kind of application, is to improve the dynamic thermal properties of  
50 the roof assembly by implementing Phase Change Materials (PCMs) [17],[18]. These are characterized by high thermal  
51 capacitance within their transition phase, stabilizing the indoor surface temperatures and delaying the thermal wave  
52 during the night hours, when coupling this strategy with passive cooling strategies (e.g. night ventilation) the heat stored  
53 during daytime can be efficiently removed (discharging phase).

54

### 55 **1.1 PCMs implementation in building components**

56 PCMs in buildings can be integrated as passive or active systems [19]. Several case studies demonstrates that PCMs  
57 should be incorporated into walls, roofs, windows, thermal insulation materials and furniture [20]. Kuznik et al. [21]  
58 investigated a renovation project in the south of France using PCM wallboards. The analysis was carried out by testing  
59 two rooms renovated with and without PCMs, they concluded that the PCMs increased the indoor thermal comfort, but  
60 for several days the applied PCM appeared unable to use its latent heat storage capacity due to the incomplete discharge  
61 overnight. This fact has highlighted the importance of the PCM system design to allow for the complete charge and  
62 discharge processes. Xu et al. [22] investigated the thermal performance of a PCM floor system in passive solar  
63 buildings. The study highlighted that the performances are affected by several factors such as layer thickness, melting  
64 temperature, thermal conductivity and latent heat of fusion of PCMs, choice of covering material and the presence of air  
65 gap between PCM and covering material. The results showed that the thickness of PCM should not be greater than 20  
66 mm and the latent heat of fusion and thermal conductivity of PCM should respectively exceed 120 kJ/kg and 0.5 W/(m  
67 K). In [23] the performance of a plaster embedding PCM, applied to the internal side of the walls was investigated, from  
68 the embodied energy and operational energy point of view, concluding that for the analyzed case study (a simple  
69 rectangular room located in Italy), the high embodied energy of the PCM plaster was not counter balanced by the  
70 benefits in terms of operational energy reduction (nevertheless the improvement of comfort conditions are not  
71 considered in the analysis). The performance of PCMs integrated in roofs are investigated by several authors. An  
72 experimental investigation on a roof coupled with PCMs and cool materials is presented in [24], where a PCM mixture  
73 encapsulated in polyethylene pipes placed in the external side of the roof (under the mortar levelling layer). Three test  
74 rooms were monitored in order to compare the influence of PCMs layer and the coupling of PCM and cool roof  
75 technology on the same roof section without PCM. The results are promising, showing an average reduction of the  
76 indoor roof peak temperature, respectively of 0.58°C for the PCM embedded roof and 0.84°C for the PCM embedded  
77 cool roof. The application of PCM in polyurethane roof membranes was investigated in [25]. The results of the in-lab  
78 characterization, demonstrate that the proposed prototype of waterproof membrane could represent an effective passive  
79 cooling solution, combining the effect of cool roofs and latent heat capacity due to the presence of PCM. Furthermore  
80 the application of PCM in walls and roof was simulated in [26], implementing Fanger model to control the HVAC

81 system. Results highlight the potential of PCM in enhancing the energy efficiency of buildings. In particular, PCM 10  
82 mm thick and melting temperature of 27°C allows the highest annual energy savings with the shorter payback period.

83 In this paper, experimental and numerical analyses were carried out on an existing residential building roof integrated  
84 with PCMs, with the aims to:

- 85 • Evaluate the thermal improvements due to PCMs integration in the summer season;
- 86 • Investigate the effects of the PCMs transition temperature on the roof global performance;
- 87 • Develop and validate a numerical model to be used to extend the analyses to other roofs typologies and  
88 locations.

## 89 **2. Experimental analysis of PCMs integrated in a roof component**

### 90 **2.1 Case study description**

91 The experimental campaign was carried out during summer 2016 in San Francesco al Campo - Turin (Italy 45.23 N,  
92 7.66 E). The selected case study is represented by an attic space of a residential building under refurbishment. The  
93 existing roof is a timber-frame double pitched roof, with clay roof tiles as external covering.

94 The roof was divided in three different portions in which different roof assemblies were installed. The Configuration A  
95 (reference case) consists of four layers (roof clay tiles, air permeable gap, XPS insulation and gypsum board). In order  
96 to analyse the influence of the PCM integration in building components and understand the thermal trends of this  
97 technology, two different PCM types were used, RT28HC and RT35 [27] (Table 1), respectively installed in  
98 configurations B and C. The configurations are composed by hollow polycarbonate panels filled with PCM (already  
99 adopted in [28] (Fig.1) and were installed between the gypsum board and the XPS layers (Fig.2). Technical  
100 specifications of roof sections are summarised in Table 2.

101

### 102 **2.2 Measurement methodology**

103 The thermal performance assessment of the three configurations through experimental data analyses has been divided  
104 into two tracks:

- 105 • The comparison of indoor surface temperatures and heat fluxes between Config. A vs Config. B and Config.  
106 A vs Config. C;
- 107 • The comparison of the PCMs surface temperature profiles of Config. B vs Config. C;

108 The monitored roof sections are South South-West exposed with a slope of 28°. During the monitoring period, the  
109 indoor space (floor area ~ 110 m<sup>2</sup>) was in free-floating regime with high ventilation rate. The air exchanges were  
110 guaranteed by:

- 111 • The infiltration through the roof tiles;
- 112 • The presence of an open window (~1.25 m<sup>2</sup>).

113 The monitoring system aimed at assessing the surface temperatures and the energy transmission variation due to the  
114 presence of PCMs was composed by 20 type-T thermocouples, 3 heat flux meter sensors and 1 pyranometer connected  
115 to a data logger DT600 with channel expansion module. The measurements were carried out with a time interval of 5  
116 minutes.

117 The outdoor boundary conditions (air temperature, relative humidity, wind speed and direction) were continuously  
118 monitored by means of a weather station installed above the roof-top (Fig. 3). Moreover, the second class pyranometer  
119 LP02 (calibration uncertainty  $\leq 1.8\%$ ) was installed for the measurement of the incident global solar radiation (Fig. 3).  
120 Temperatures across the roof sections were measured by means of type-T thermocouples (nominal accuracy  $\pm 0.25$  K)  
121 (Fig. 4). Moreover, the heat fluxes were measured by means of HFP01 heat flux sensors (measurement uncertainty  $\pm$   
122 5%) placed in the indoor side (Fig.5).

123  
124 In order to avoid the influence of the radiation heat exchange between the roof and the indoor surrounding surfaces  
125 (floor, walls), the indoor surfaces of the samples were covered with a radiant barrier (aluminium shine foil).  
126 The roof clay tiles are characterised by high air permeability, due to the joints of the tiles allowing air exchanges  
127 between the cavity and the outside. A characterization of the infiltration rate in the cavity below the roof tiles was  
128 carried out by means of the tracer-gas technique. To this purpose, a small scale sealed room was built under the roof  
129 portion without the insulation layers (Fig.6). The measurements were repeated several times during the monitoring days  
130 and an average infiltration rate  $\sim 3.3$  (m<sup>3</sup>/h)/m<sup>2</sup> was estimated. It is important to remark that this infiltration rate value is  
131 strictly dependent by the wind speed; the measurements were carried out with low wind speed ( $v < 7$  km/h) in line with  
132 the site average values.

133

### 134 **2.3 Experimental results**

135 The experimental results were used to compare the thermal performance of the different roof configurations and to  
136 validate a numerical model. One week of experimental results (from 13<sup>th</sup> to 20<sup>th</sup> August) representative of the summer  
137 conditions is reported in Fig.7.

138 In the monitored week, the outdoor temperature (black line) was between  $\sim 16^\circ\text{C}$  (minimum night temperature) and  
139  $\sim 32^\circ\text{C}$  (maximum daily temperature), while the indoor temperatures were between  $\sim 20^\circ\text{C}$  and  $\sim 33^\circ\text{C}$ . The wind speed  
140 (black points) was in line with the average conditions of Turin (IT) wind zone, which is generally characterized by low  
141 wind velocity ( $v < 10$  km/h) except for the afternoon of 16<sup>th</sup> August ( $v > 15$  km/h) due to the presence of a summer  
142 storm.

143 During the sunny days (13<sup>th</sup>, 14<sup>th</sup> and 17<sup>th</sup> August) the incident global solar radiation reached a peak of  $\sim 1000$  Wm<sup>-2</sup> at  
144 2:00 pm.

145

#### 146 **2.3.1 Indoor surface temperatures and heat fluxes**

147 A comparison between the indoor surface temperature and heat fluxes between the reference configuration A (no  
148 PCMs) and configuration B (PCM RT28-HC) is presented in Fig. 8 while a comparison between A and C (PCMs RT35)  
149 is reported in Fig. 9. The indoor surface temperatures of the roof ( $T_{s,i}$ ) are plotted in black continuous line for  
150 configuration A and grey continuous lines for configurations B and C with PCM, while the heat fluxes crossing the roof  
151 are plotted in dashed lines.

152 In Fig. 10, the thermal performance profiles (i.e inner surface temperature and heat flux) for the three configurations on  
153 August 17<sup>th</sup> are illustrated. The reference configuration A (black line) presents the highest surface temperature during  
154 daytime ( $37.3^\circ\text{C}$ ), reaching its peak between 4:00 pm and 5:00 pm. These temperature profile is followed by  
155 configuration C (PCMs-RT35) reaching  $35.2^\circ\text{C}$  (grey line) and B (RT28HC) with  $29.1^\circ\text{C}$  (dashed grey line)  
156 demonstrating the capability of PCM layers to reduce the indoor surface peak temperatures during daytime. As

157 expected; during the night and in the early morning, configuration A shows lower temperatures due to the lack of  
158 dynamic thermal inertia, i.e. heat charging and discharging capability of the PCM layer in the latter two cases.

159 In Table 3 the results reported in Fig. 10, are summarized highlighting the peak difference among the three  
160 configurations in terms of indoor surface temperatures  $T_{si}$ , as far as the heat fluxes and energy crossing the roof are  
161 concerned, while in Table 4 the ongoing energy loads and outgoing energy removed from the indoor space are  
162 compared for different time intervals during the day, highlighting that:

- 163 • During the night and in early morning (00:00 am – 8:00 am) configuration B is characterized by the highest  
164 value of ongoing energy ( $\sim 100$  Wh/m<sup>2</sup>). This is due to its higher temperature if compared to configuration C,  
165 while the reference configuration A, without PCMs, is only subject to heat losses.
- 166 • In the morning (8:00 am – 12:00 am) configuration C is characterized by high value of heat losses ( $\sim 48$   
167 Wh/m<sup>2</sup>), while configuration B presents both energy loads and losses with a positive energy balance of 11.7  
168 Wh/m<sup>2</sup>.
- 169 • In the afternoon (12:00 am – 4:00 pm) both configurations B and C present a good capability in removing the  
170 heat from the indoor space with 40.0 and 64.6 Wh/m<sup>2</sup> of energy losses respectively, while Configuration A is  
171 characterized by  $\sim 17$  Wh/m<sup>2</sup> of energy loss;
- 172 • In the evening (4:00 pm – 8:00 pm) configuration B continues to remove heat from the indoor space (working  
173 in its melting phase), while configuration C is characterized by higher temperature and lower value of heat  
174 loads (solid phase);
- 175 • Later in the evening (8:00 pm – 00:00 am) configuration C presents high value of heat load ( $\sim 49$  Wh/m<sup>2</sup>),  
176 while in both the other configurations A and B the heat loads are significantly lower (respectively  $\sim 17$  and  $\sim 11$   
177 Wh/m<sup>2</sup>).

178

### 179 2.3.2 Surface temperature profiles of the PCM layer

180 To highlight the importance of PCM type selection, the temperature profiles of the inner PCM layer for configuration B  
181 vs configuration C is shown in Fig. 11. Configuration B has a flattered surface temperature between 26°C and 30°C,  
182 which indicates that the substance is in its transition phase with the higher values of equivalent specific heat capacity.  
183 Until the approaching of mid-day (time interval which is defined by higher values of the solar radiation intensity and  
184 external air temperature values), the PCM (RT28-HC) temperature has increased slightly, however it did not exceed the  
185 upper limit of phase change range to totally turned to the liquid phase. On the other hand; in configuration C (RT 35),  
186 the PCM mostly is in solid state, since the melting starts at 34 °C, and accordingly the specific heat capacity is in its  
187 minimum value of 2 kJ/kg K.

188 To conclude; PCM RT28-HC shows a better exploitation of the phase transition during the day, allowing to contain the  
189 heat gains and accordingly to improve the overall thermal behavior during daytime. Nevertheless, during the night PCM  
190 RT28-HC shows higher values of heat loads released to the indoor space if compared to RT35. This behavior has to be  
191 carefully taken into account during the design phase according to the final use of the indoor space and users' occupancy  
192 profiles.

193

## 194 3. Development of a numerical model

195 A finite difference model was developed to estimate the heat transfer mechanism in the monitored case studies and to  
 196 build a theoretical basis for better explaining the measured data. In the numerical model the solution domain is defined  
 197 by a number of grid points in which the derived linear equations form a matrix system as shown in Eq. (1), where A is  
 198 the matrix of coefficients, X is the vector of unknowns and B is the column vector of known terms. The system is solved  
 199 by inverting the matrix to obtain the temperature values X.

$$[A] \{X\} = \{B\} \quad (1)$$

200 According to nodes energy balance, the numerical solving scheme starts from the initial conditions of temperatures till  
 201 the nodal temperature  $T_{n,i}$  is obtained. Nevertheless, there is an iterative cycle which is of key importance in the code. A  
 202 temperature correction scheme is followed by saving the solution of the matrix in the previous iteration and solving the  
 203 system until the convergence criteria is reached (difference between the current temperature and the values of the  
 204 previous time step  $\leq 0.5^\circ\text{C}$ ). The code thus saves and starts a new time step implementing the previously solved time  
 205 step nodal temperatures values as the initial condition (Fig.12).

### 206 3.1 Numerical simulation of PCMs

207 There are several methods to take into account the transient physical state of PCM, such as enthalpy method or the  
 208 equivalent heat capacity method, which was implemented in the present study. The technique has been proposed in [29]  
 209 and [30] and it is based on the linear approximation of the heat flux between PCM nodes. The grid was numerically  
 210 solved using the implicit fixed scheme that employs linearization, initial conditions and adopts an iterative procedure  
 211 until convergence is obtained **Error! Reference source not found.**[31].

212 For each node, the  $C^*_{PCM}$  as a function of  $T_{PCM}$  was evaluated using a continuous linear function determined by the  
 213 physical properties of the PCM ( $T_{PCM,in}$ ,  $T_{PCM,m}$ ,  $h_{PCM}$ ,  $C_{PCM,s}$ ,  $C_{PCM,l}$ ) which are provided by the manufacturer [27]. The  
 214 linear employed equations indicated in Fig.13 and listed from Eq.(2) to Eq.(5) allow to determine the specific heat  
 215 capacity of PCM as a function of  $T_{PCM}$ . Furthermore,  $C^*_{PCM,m}$ , which is the maximum specific heat capacity of the  
 216 considered PCM, is defined by Eq.(6).

Value of specific heat capacity Temperature range

$$C^*_{PCM}(T_{PCM}) = C_{PCM,s} \quad T_{PCM} \leq T_{PCM,s} \quad (2)$$

$$C^*_{PCM}(T_{PCM}) = C_{PCM,s} + \frac{C^*_{PCM,m} - C_{PCM,s}}{T_{PCM,m} - T_{PCM,s}} (T_{PCM} - T_{PCM,s}) \quad T_{PCM,s} < T_{PCM} \leq T_{PCM,m} \quad (3)$$

$$C^*_{PCM}(T_{PCM}) = C_{PCM,l} + \frac{C^*_{PCM,m} - C_{PCM,l}}{T_{PCM,m} - T_{PCM,l}} (T_{PCM} - T_{PCM,l}) \quad T_{PCM,m} > T_{PCM} > T_{PCM,l} \quad (4)$$

$$C^*_{PCM}(T_{PCM}) = C_{PCM,l} \quad T_{PCM} \geq T_{PCM,l} \quad (5)$$

$$C^*_{PCM,m} = \frac{T_{pcm,s} - T_{pcm,m}}{\Delta T_h} \cdot C_{PCM,s} + \frac{T_{pcm,m} - T_{pcm,l}}{\Delta T_h} \cdot C_{PCM,l} + \frac{2h_{pcm}}{\Delta T_h} \quad (6)$$

217 Where:  $\Delta T_h = T_{PCM,l} - T_{PCM,s}$ .

218 The thermal properties of each node inserted in the PCM layer, (e.g. specific heat capacity and density) are evaluated as  
 219 a function of the previous time step temperature input  $T_p^\circ$ . In the present study 1 cm thickness PCM layer is discretised  
 220 into three homogenous layers, therefore the energy balance equation (Eq.7) of each PCM node is:

$$\rho_p C_p^* (T) \frac{T_p - T_p^\circ}{\Delta \tau} = \frac{K_p}{\Delta x} (T_{p-1} - T_p) + \frac{K_p}{\Delta x} (T_{p+1} - T_p) \quad (7)$$

221

### 222 3.2 RC modelling

223 The thermal resistance is defined as the ratio of the temperature difference between two thermal nodes,  $(T_i - T_{i+1})$  and the  
 224 heat transfer  $Q$  that flows between the two thermal nodes. This is analogous to Ohm's law, in which the electrical  
 225 resistance is defined as the ratio between the voltage drop across a resistor and its current flow. Thermal resistances  $R_k$ ,  
 226  $R_c$  and  $R_{rad}$  represents respectively conduction, convection, and radiation heat transfer between the wall layers and they  
 227 are determined respectively through Eq. (8), (9), and (10).

$$R_k = \frac{x}{\lambda} \quad (8)$$

$$R_c = \frac{1}{h_c} \quad (9)$$

$$R_{rad} = \frac{1}{h_r} \quad (10)$$

228 The convection heat transfer coefficients have been evaluated by different empirical laws:

229 • For the outdoor surface the McAdams correlation [32] was adopted Eq. (11);

$$h_c = 5.62 + 3.9 v \quad (11)$$

230 • For the free convection in the natural ventilated air cavity [33]:

$$h_c = 1.52 \cdot |\Delta T|^{1/3} \quad (12)$$

231 Where  $\Delta T$  is the maximum difference value of the roof tile layer and the air cavity or the XPS layer and the air cavity.

232 • For the indoor layer, the convection heat transfer is considered free convection, since there is no serving

233 HVAC system, and is evaluated by Eq. (13) [34]:

$$h_c = \left\{ \left[ 1.5 \cdot \left| \frac{\Delta T}{H} \right|^{0.25} \right]^6 + \left[ 1.23 \cdot (\Delta T)^{0.33} \right]^6 \right\}^{1/6} \quad (13)$$

234 Where  $\Delta T$  is the difference between the indoor air temperature and the indoor surface temperature, while  $H$  is the floor  
 235 height.

236 For the radiation heat exchange Eq. (14) and (15) was used [35].

$$R_{rad} = \frac{\left[ \frac{1}{\epsilon_1} + \frac{1}{\epsilon_2} - 1 \right]}{\left[ 4 \cdot \sigma \cdot T_{avg}^3 \right]} \quad (14)$$



237 And hence:

$$h_r = \frac{4 \sigma (T_{avg})^3}{\left(\frac{1}{\varepsilon_1} + \frac{1}{\varepsilon_2} - 1\right)} \quad (15)$$

238 Where:  $T_{avg}$  is the average temperature of the two opposite surfaces, which has been evaluated as function of  
239 temperature previous time step values.

240

### 241 3.3 Numerical Model A (without PCM)

242 Model A (Config. A) is considered as the comparison reference case (Fig.14a). The specific heat capacity of the roof  
243 tiles and gypsum board are considerably higher than the XPS layer, hence each layer is represented in the RC scheme  
244 (Fig.14b) by two conductance resistances and a capacitance. The mathematical equations for the eight nodes are  
245 classified in equations from (16) to (24).

- 246 • For nodes 1 and 8, the heat transfer through the outer and inner layers of the roof surface is described by two  
247 thermal resistances, the convection heat transfer with the ambient conditions and the conduction transfer within  
248 the layer itself.

$$T_1 \left( -\frac{1}{R_{co}} - \frac{1}{R_{kB}} \right) + T_2 \left( \frac{1}{R_{kB}} \right) = -\frac{1}{R_{co}} T_e - I \cdot \alpha_B \quad (16)$$

$$T_8 \left( -\frac{1}{R_{ci}} - \frac{1}{R_{k-gyp}} \right) + T_7 \left( \frac{1}{R_{k-gyp}} \right) = -\frac{1}{R_{ci}} T_i \quad (17)$$

- 249 • For nodes 2 and 7, the energy have included the thermal storage influence and nodal temperature changes with  
250 the time. Taking into consideration that  $T_n^\circ$  is the node temperature evaluated at the previous time step.

251

$$T_1 \left( \frac{1}{R_{kB}} \right) + T_2 \left( \frac{-2}{R_{kB}} - \frac{\rho \Delta x_{br} c_{br}}{\Delta \tau} \right) + T_3 \left( \frac{1}{R_{kB}} \right) = -\frac{\rho \Delta x_{br} c_{br}}{\Delta \tau} T_2^\circ \quad (18)$$

$$T_6 \left( \frac{1}{R_{k-gyp}} \right) + T_7 \left( \frac{-2}{R_{k-gyp}} - \frac{\rho \Delta x_{gyp} c_{gyp}}{\Delta \tau} \right) + T_8 \left( \frac{1}{R_{k-gyp}} \right) = -\frac{\rho \Delta x_{gyp} c_{gyp}}{\Delta \tau} T_7^\circ \quad (19)$$

- 252 • The radiation heat exchange coefficient  $h_r$  between nodes 3 and 5 is considered as a function in nodal  
253 temperatures Eq. (20). The average temperature of the two opposed surface is evaluated in the previous time  
254 step.

$$T_{avg} = \frac{T_3^\circ + T_5^\circ}{2} \quad (20)$$

- 255 • The convection heat transfer within the air cavity and the conduction heat transfer through the element are  
256 showed in the energy balance Eq. (21) and (22)

$$T_2\left(\frac{1}{R_{kB}}\right) + T_3\left(\frac{-1}{R_{kB}} - \frac{1}{R_c} - \frac{1}{R_r}\right) + T_4\left(\frac{1}{R_c}\right) + T_5\left(\frac{1}{R_r}\right) = 0 \quad (21)$$

$$T_3\left(\frac{1}{R_r}\right) + T_4\left(\frac{1}{R_c}\right) + T_5\left(\frac{-1}{R_{k-xps}} - \frac{1}{R_c} - \frac{1}{R_r}\right) + T_6\left(\frac{1}{R_{k-xps}}\right) = 0 \quad (22)$$

- 257 • In Node 4, the infiltration airflow rate  $m_v$  was estimated by the experimental measurements see Section 2.1.  
258 Accordingly, the air cavity node energy balance is:

$$T_3\left(\frac{1}{R_c}\right) + T_4\left(-\frac{2}{R_c} - m_v C\right) + T_5\left(\frac{1}{R_c}\right) = -m_v C T_v \quad (23)$$

- 259 • In Node 6, the energy balance of the interaction node between two layers of the XPS and gypsum board is:

$$T_5\left(\frac{1}{R_{k-xps}}\right) + T_6\left(\frac{-1}{R_{k-xps}} - \frac{1}{R_{k-gyp}}\right) + T_7\left(\frac{1}{R_{k-gyp}}\right) = 0 \quad (24)$$

260

### 261 3.4 Numerical Models B and C integrating PCM

262 The schematic description of cases B and C (Fig.15a) is similar to case A apart from the PCM layer analysis. One of the  
263 study focal points is to investigate the influence of PCM melting and specific heat capacity values on the overall energy  
264 balance. The RC model is illustrated in Fig.15b.

265 Each homogenous sub-layer (from the three nodes representing the PCM layer) is represented by a conductive  
266 resistance and a capacitance. For the sake of brevity, the resulting thermal balance equation Eq. (24) is shown for node  
267 (8)

$$\left(\frac{k_p}{x_p}\right)_{p7} T_{p7} + \left(-2\frac{k_p}{x_p} - \frac{\rho \cdot x_p \cdot c_{p2}}{\Delta\tau}\right) T_{p8} + \left(\frac{k_p}{x_p}\right)_{p9} T_{p9} = -I \cdot \left(\frac{a_{p2}}{2}\right) - \left(\frac{\rho \cdot x_p \cdot c_{p2}}{\Delta\tau}\right) \cdot (T_{p8})^{\tau-1} \quad (25)$$

### 268 3.5 Model validation

269 For the determination of the numerical model's reliability, the Root Mean Square Error (RMSE [°C]) calculated  
270 according to Eq. (26) were used:

$$RMSE = \sqrt{n^{-1} \cdot \sum_{j=1}^n (s_j - e_j)^2} \quad (26)$$

271 Where:  $s_j$  and  $e_j$  are respectively the predicted values and measured values for times  $j$ , and  $n$  is the number of values of  
272 the series.

273 For the validation of the numerical models, a comparison between the measured values of the inner and outer roof  
274 surfaces was carried out. Furthermore, the measured set of data has been analyzed to optimize the implementation  
275 decision of PCM in buildings and the influence of the PCM material proper selection.

#### 276 3.5.1 Numerical results and model validation

277 Among the seven monitored days presented in section 2.3, August 16<sup>th</sup> was selected for the model validation because it  
278 is characterized by different weather conditions during the same day (including summer storm and rain), so as the  
279 numerical model response could be evaluated under variable climatic boundary conditions. The comparison between  
280 numerical and experimental results is plotted in Fig. 16, 17 and 18 respectively for Configurations A, B and C for the  
281 outdoor and indoor surface temperatures. For the determination of the indoor surface temperature, it is to underline that  
282 indoor zone is not thermally controlled, and windows are kept open day and night.  
283 The RMSE have been estimated for all experimentally investigated surfaces, and temperatures nodes have been ordered  
284 according to Figures 16-18. Values are summarized in Table 6. RMSE results in a range between 0.4 °C (inner surface)  
285 and 4 °C (outer roof tiles surface). The difference appearing in the outdoor surface temperature during night hours is  
286 justified considering that the numerical model neglects the radiation heat exchange between the outer surface with the  
287 sky and adjacent surfaces. Moreover as explained in section 2.3, between 3:00 and 5:00 pm, a summer storm occurred,  
288 which explains the reason of the mismatch between measured and predicted values, in fact the numerical model has  
289 neglected the effect of roof tiles cooling caused by rain water. On the other hand, some parameters controlling the heat  
290 transfer in buildings are complex to be predicted (e.g. surface heat transfer coefficient), for all these reasons, the  
291 numerical models accuracy is considered acceptable, especially because the difference between the experimental and  
292 calculated results have been decreased in the peak time and the two temperature profiles were matched, as shown in  
293 Figures (17) and (18).

294

#### 295 **4. Conclusions**

296 In this study, a roof-mounted PCM filled panels with different melting temperature were monitored and compared with a  
297 reference roof without PCM layer. The analyses focused on the temperature and heat flux peaks reduction, highlighting  
298 that the presence of PCM layers obtains:

- 299 • A reduction in the indoor surface peak temperature of ~ 2.2°C and ~ 8.2°C respectively for the RT35 and the  
300 RT28HC configurations;
- 301 • A contribution in removing heat from the indoor attic during daytime, in particular RT 35 configuration, is able  
302 to remove heat mainly during the morning, while RT 28 HC configuration during the afternoon (characterized  
303 by higher air temperature and incident solar radiation).

304 These results demonstrate the importance of the proper PCM selection. In fact PCM which mainly works in its transition  
305 phase (RT28HC) shows higher capability to reduce the heat load in the below attic space during the hottest hours of the  
306 day. Meanwhile a more evident ceiling surface temperature reduction should contribute to the improvement of the indoor  
307 comfort condition.

308 The analysis on the energy flows highlights that both PCM configurations determines heat loads released to the indoor  
309 environment during their discharging phase. These results underline the importance of coupling PCM with passive night  
310 cooling strategies (e.g. night ventilation) to guarantee the efficacy of the PCM in reducing the daily heat loads.

311 Moreover, a numerical RC model implementing the PCM behavior was developed. The model was validated through a  
312 comparison with the measured data, showing a RMSE between 0.4°C (indoor surface temperature) and 4°C (outdoor  
313 surface temperature), according to the magnitude of the temperature variation during the day. The whole year  
314 measurements on the presented roof are still in progress and a more complete picture of the influence of PCMs layer on  
315 the overall energy balance will be thus possible. Implementing PCMs in roof attic is a promising solution to enforce; peak  
316 load savings with a range of ~13 to ~59% and to take advantage of all unused areas in residential houses keeping  
317 acceptable thermal conditions. However, it is important to take into consideration that it may not always be a suitable

318 efficient application for all climatic conditions. Exploratory numerical simulations have to be carried out during the early  
319 design stages to ensure the benefits achievable by using PCM.

320 The developed numerical model needs further improvements and modifications to expand the results on urban scale level.

321 Future work plan is focusing on coupling TRNSYS software to the 1-D model in order to investigate the behavior of  
322 building components implementing PCMs; in particular, the thermal optimization in different climatic conditions for  
323 different roofs assemblies.

324

325 **Acronyms**

326

PCM	Phase Change Material
XPS	Extruded Polystyrene
TES	Thermal Energy Storage
HVAC	Heating Ventilation and Air Conditioning
RMSE	Root Mean Square Error
SF <sub>6</sub>	Sulphur Hexafluoride

327

328 **Nomenclature**

A	Cross section area	m <sup>2</sup>
T	Temperature	°C
hc	Convection heat transfer coefficient	W m <sup>-2</sup> K <sup>-1</sup>
R <sub>C</sub>	Specific convection thermal resistance	m <sup>2</sup> K W <sup>-1</sup>
R <sub>K</sub>	Specific conduction thermal resistance	m <sup>2</sup> K W <sup>-1</sup>
R <sub>rad</sub>	Specific radiation thermal resistance	m <sup>2</sup> K W <sup>-1</sup>
Pr	Prandtl number	(-)
C	Specific heat capacity	J kg <sup>-1</sup> K <sup>-1</sup>
C*	Equivalent Specific heat capacity	J kg <sup>-1</sup> K <sup>-1</sup>
H	Height of the surface	m
h	Specific enthalpy of fusion	kJ kg <sup>-1</sup>
h <sub>0</sub>	Outside convection heat transfer coefficient	W m <sup>-2</sup> K <sup>-1</sup>
h <sub>c</sub>	Cavity convection heat transfer coefficient	W m <sup>-2</sup> K <sup>-1</sup>
h <sub>i</sub>	Inside convection heat transfer coefficient	W m <sup>-2</sup> K <sup>-1</sup>
IL	Internal Loads	W
I	Impinged solar radiation	W m <sup>-2</sup>
K	Thermal conductivity coefficient	W m <sup>-1</sup> K <sup>-1</sup>

	x	Layer thickness	m
329			
330	<b>Greek symbols</b>		
	$\alpha$	Short wave solar absorption coefficient	(-)
	v	Wind velocity	(m/s)
	$\varepsilon$	Long wave radiation emissivity	(-)
	$\rho$	Air density	kg/m <sup>3</sup>
	$\sigma$	Stefan-Boltzmann constant, (5.67 x 10 <sup>-8</sup> )	W/(m <sup>2</sup> K <sup>4</sup> )
	$\Delta T_h$	Temperature range of phase change	°C
	$\tau$	Time step	s
	$\beta$	Liquid fraction	%
	$\Phi$	Heat flux	W m <sup>-2</sup>
	$\lambda$	Thermal conductivity	W/mK
331			
332	<b>Subscripts</b>		
	s	Solid state	
	l	Liquid state	
	h	PCM Melting/solidification temperature range difference	
	m	Melting peak	
	P	PCM node	
	r	Reference	
	i	Indoor	
	o	Outdoor	
333			
334	<b>Superscripts</b>		
	°	Previous time step	
	*	Equivalent	
335			
336			

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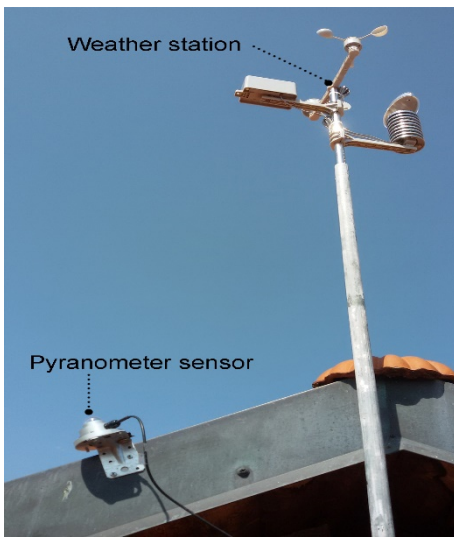


*Fig.1 PCM polycarbonate layer*

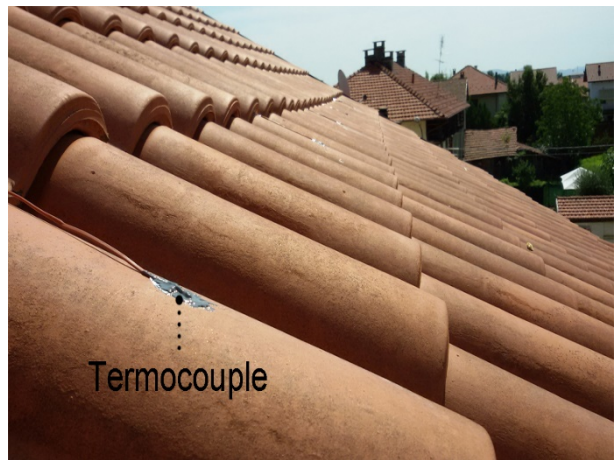


*Fig.2 Installation of a PCM filled panel*

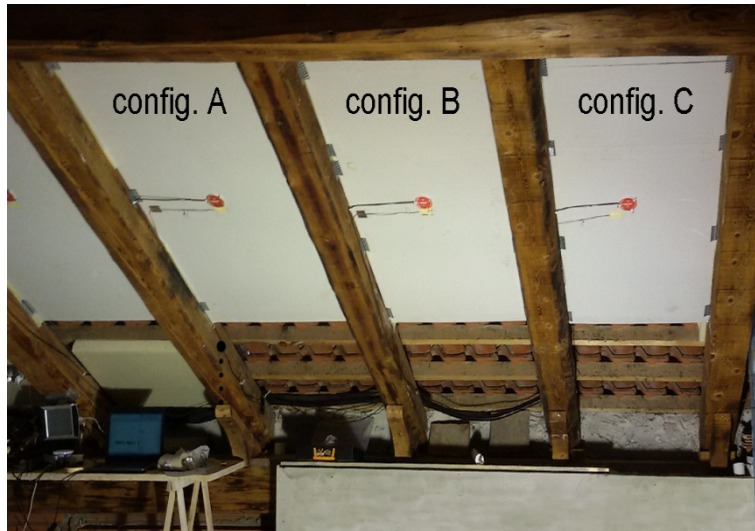
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*Fig.3 Weather station and pyranometer sensor*

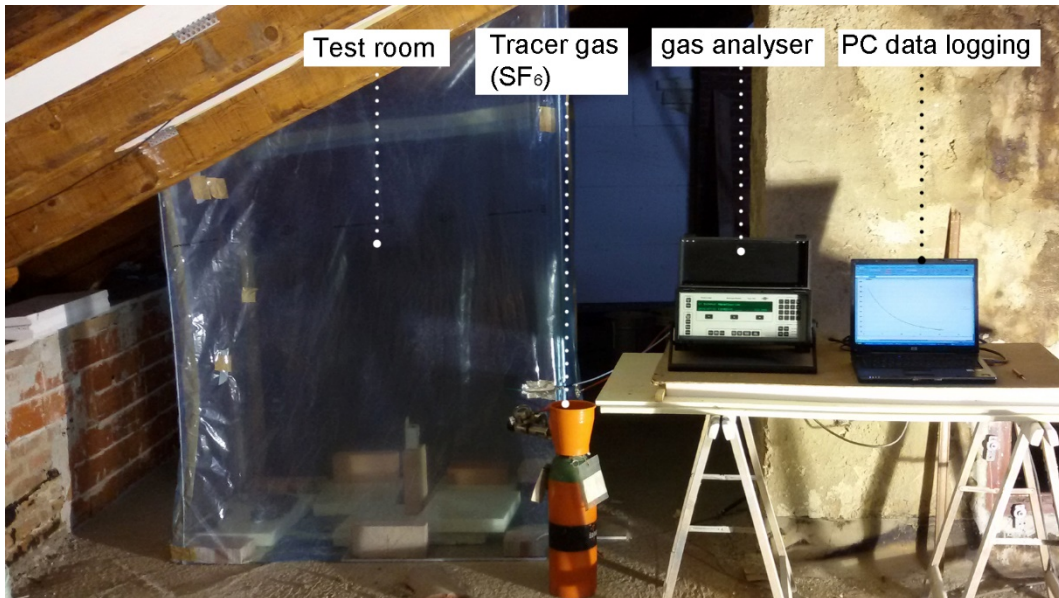


*Fig. 4 Thermocouples installed above the roof tiles*



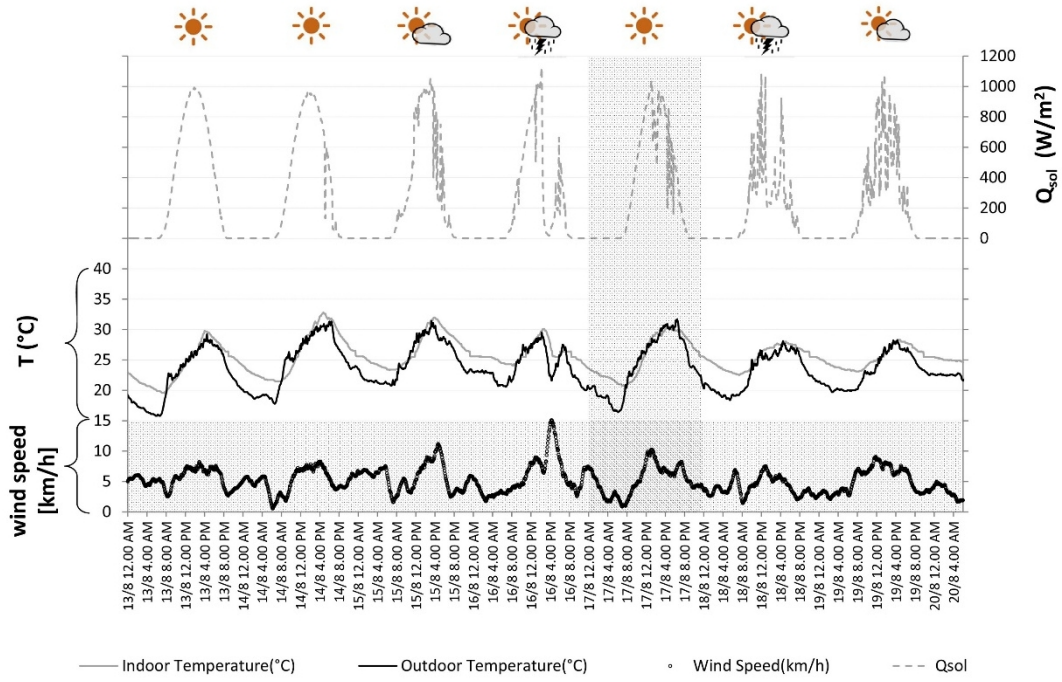
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*Fig. 5 From left to right, Configurations A, B and C with heat flux sensors and thermocouples placed in the indoor side*



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*Fig. 6. Tracer gas technique used for the determination of the air infiltration rate under the roof tiles.*



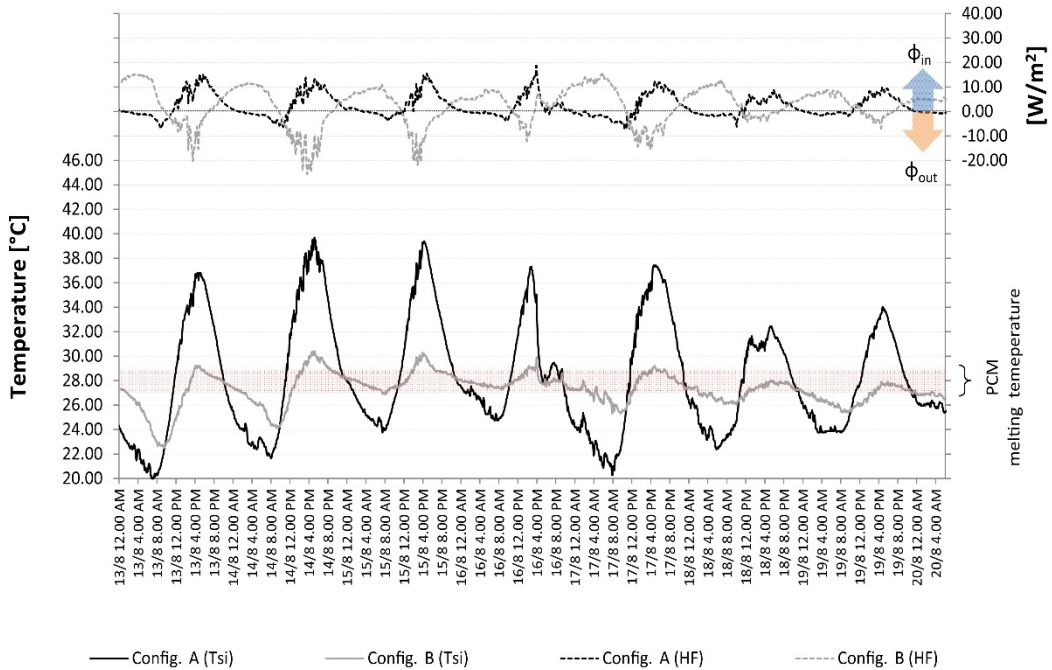
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Fig. 7. Boundary conditions from 13<sup>th</sup> to 20<sup>th</sup> august. Incident solar radiation (dashed grey line), indoor temperature (grey line), outdoor temperature (black line) and wind speed (black dots).

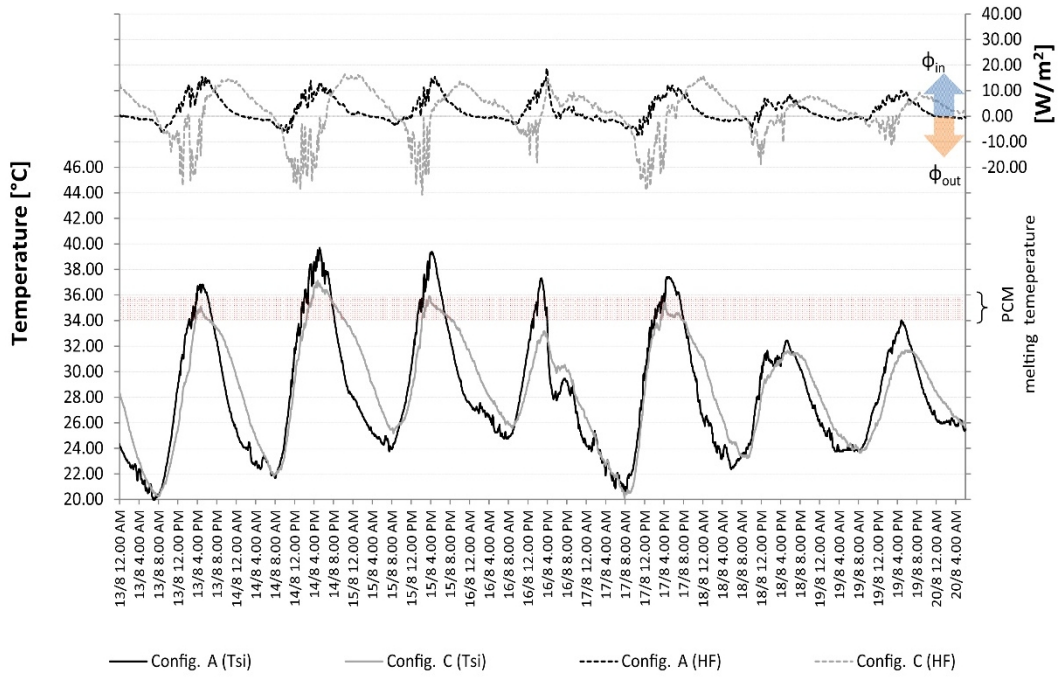


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Fig. 8. Comparison between configuration A, reference roof without PCMs (black), and configuration B, roof with PCM-RT28HC (grey), heat fluxes (dashed lines) and indoor surface temperatures (continuous lines).



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18 Fig. 9. Comparison between Configuration A, reference roof without PCMs. (black), and configuration C, roof with  
 19 PCMs-RT35 (grey), heat fluxes (dashed lines) and indoor surface temperatures (continuous lines).

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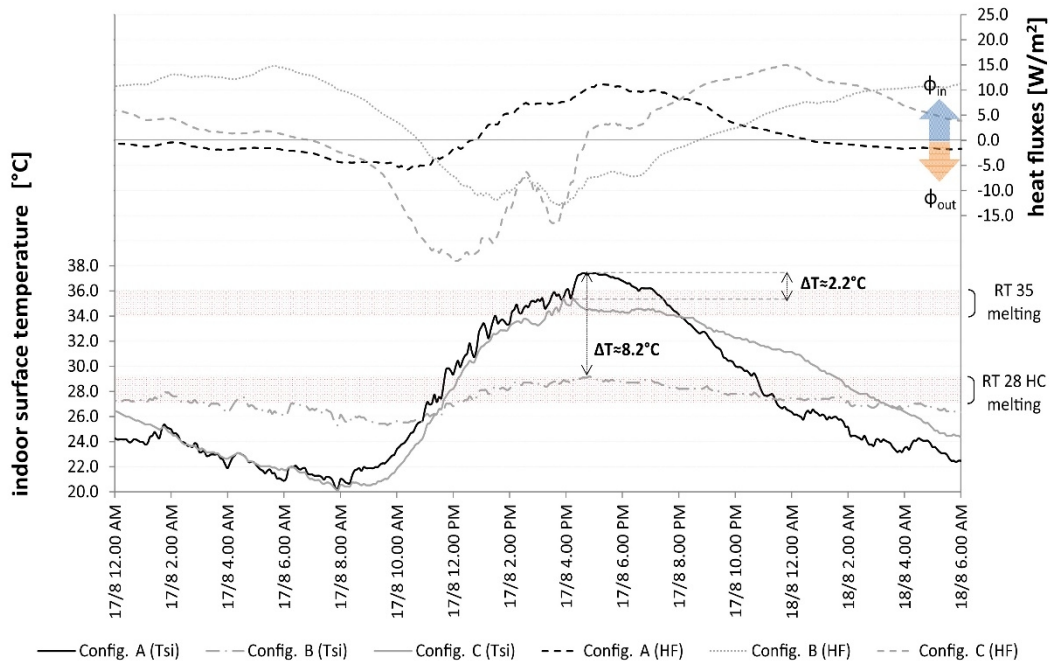


Fig. 10. Comparison between Configuration A (reference roof without PCM), B (PCM-RT28HC) and C (PCM-RT35)(grey). Selected day: August 17<sup>th</sup>.

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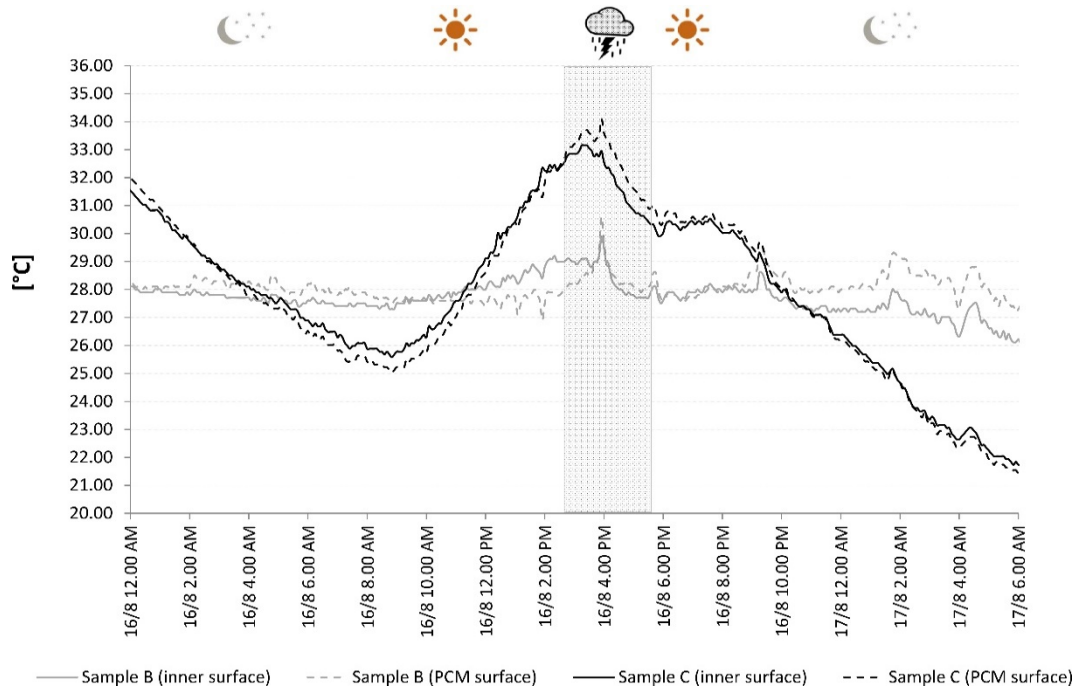


Fig. 11. Comparison between configurations B and C, PCM Surface temperature

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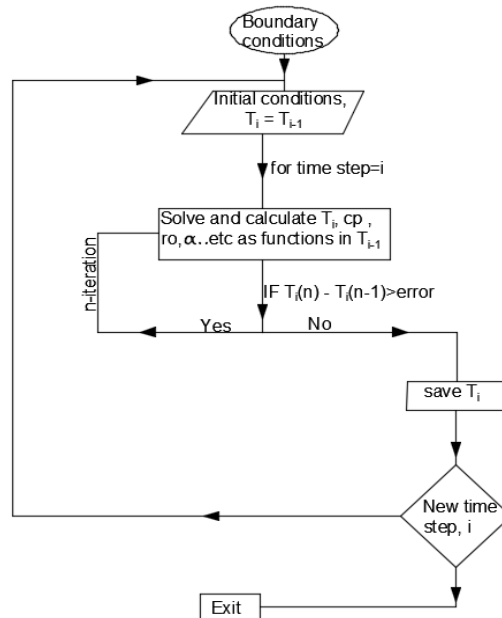


Fig. 12. Numerical code flowchart

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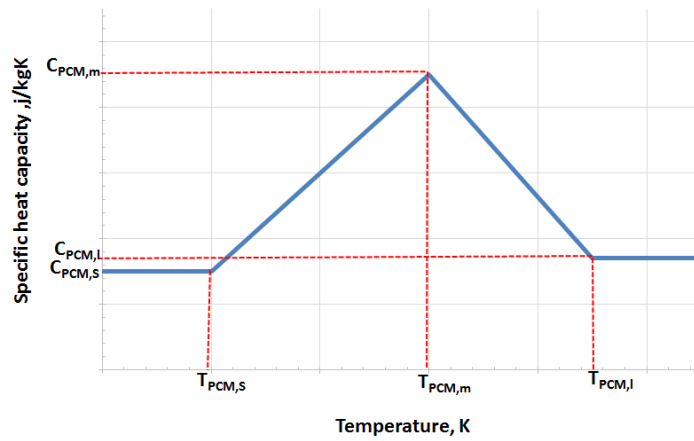
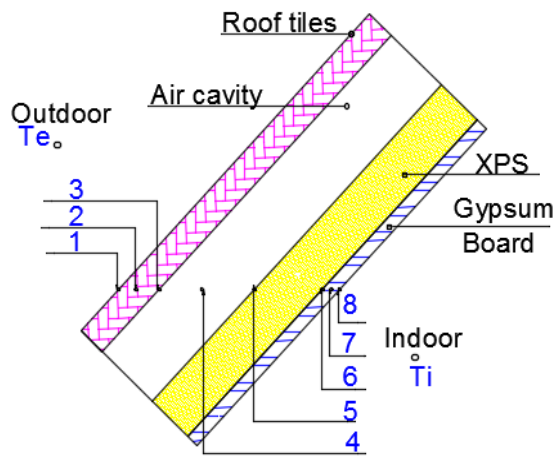
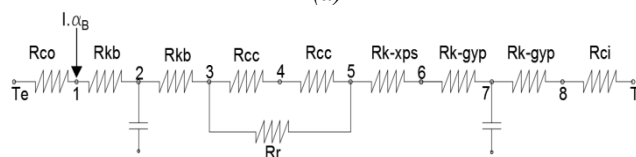


Fig.13. Specific heat capacity as a function of PCM temperature

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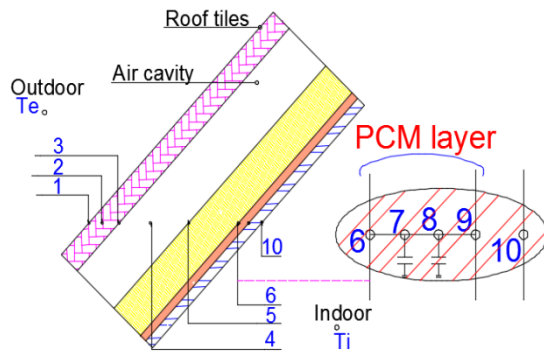
(a)



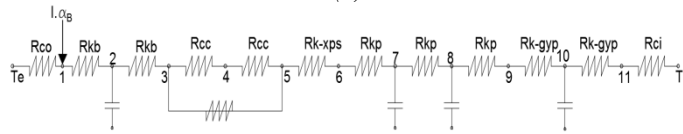
(b)

Fig. 14.(Model -A), (a) Scheme, (b) RC model

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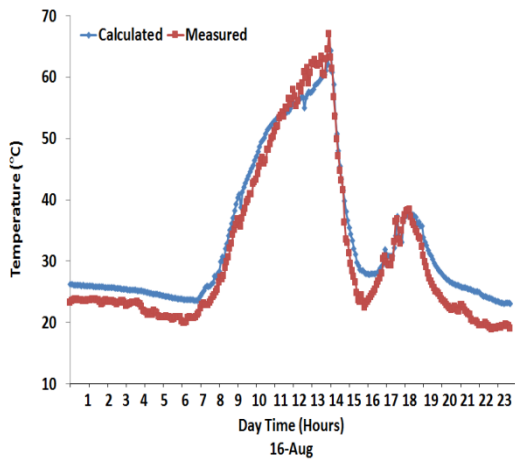


(a)

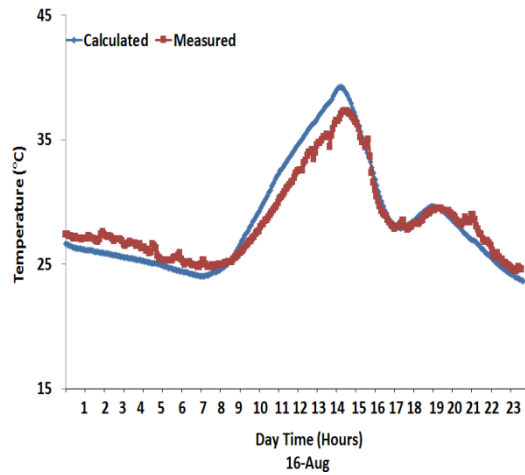


(b)

Fig. 15. (Model –B&C), (a) Scheme, (b) RC model, PCM nodes (7,8)



(a)



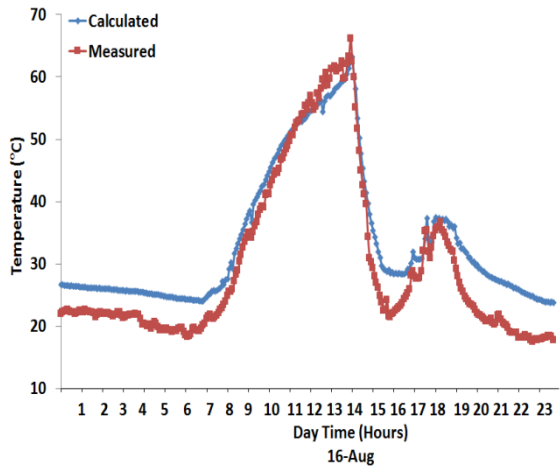
(b)

Fig. 16 Configuration A (reference config.) - Comparison between measured and predicted values. (a) outdoor surface temperature, (b) indoor surface temperature

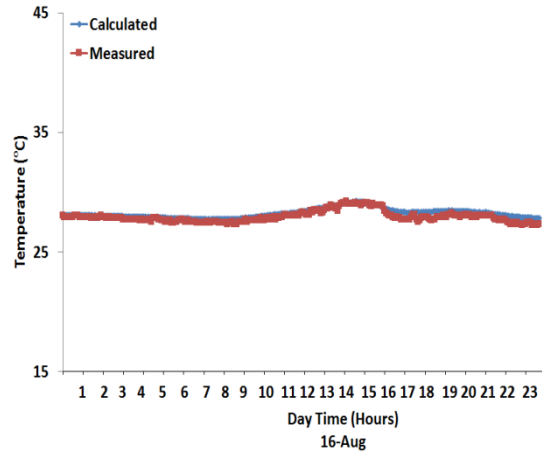
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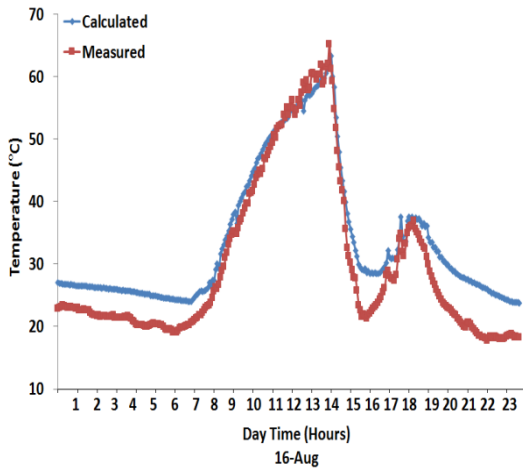
(a)



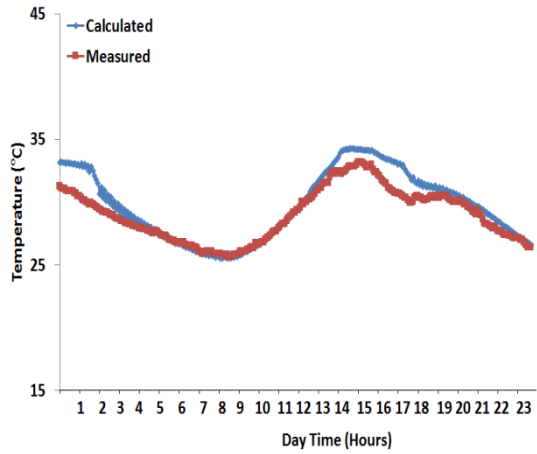
(b)

Fig. 17 Configuration B (RT28 HC) - Comparison between measured and predicted values. (a) outdoor surface temperature, (b) indoor surface temperature

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(a)



(b)

Fig. 18 Configuration C (RT35) - Comparison between measured and predicted values. (a) outdoor surface temperature, (b) indoor surface temperature

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Table 1. PCM physical properties **Error! Reference source not found.**

PCM name	RT28	RT35
Solid temperature (lower limit of phase change range)	27°C	34°C
Nominal melting temperature	28°C	35°C
Liquid temperature (upper limit of phase change range)	29°C	36°C
Specific heat Capacity [kJ kg <sup>-1</sup> K <sup>-1</sup> ]	2	2
Latent heat of fusion [kJ kg <sup>-1</sup> ]	250	160

Table 2. Roof section: material properties. Layer 04 is included only in configurations B and C.  
(data retrieved from **Error! Reference source not found.**)

Layer	Material	s (mm)	$\rho$ (kg m <sup>-3</sup> )	$\lambda$ (W m <sup>-1</sup> K <sup>-1</sup> )	cp (J kg <sup>-1</sup> K <sup>-1</sup> )	$\alpha$ (-)
01	brick tiles	30	1700	0.7	840	0.55*
02	air gap	70	1.2	N.A.	1020	N.A.
03	XPS	50	32	0.034	1500	N.A.
04 (config. B and C only)	PCM	10	800	0.14	2000	N.A.
05	gypsum board	9.5	800	0.2	1000	N.A.

Table 3. Peak of temperature (August 17<sup>th</sup>)

Configuration	peak temperature (°C)			difference of Tsi (°C)	
	A	B	C	B vs A	C vs A
T <sub>si, max</sub> (12 am-00 pm)	37.3	29.1	35.2	8.2	2.1
T <sub>si, min</sub> (00 pm-12 am)	20.2	25.4	20.2	5.2	0.0

Table 4. Energy loads and losses for different time intervals (August 17<sup>th</sup>)

Time interval	Configuration A (reference roof no PCM)			Configuration B (RT28HC-PCM)			Configuration C (RT35-PCM)		
	Energy losses (Wh/m <sup>2</sup> )	Energy loads (Wh/m <sup>2</sup> )	Energy balance (Wh/m <sup>2</sup> )	Energy losses (Wh/m <sup>2</sup> )	Energy loads (Wh/m <sup>2</sup> )	Energy balance (Wh/m <sup>2</sup> )	Energy losses (Wh/m <sup>2</sup> )	Energy loads (Wh/m <sup>2</sup> )	Energy balance (Wh/m <sup>2</sup> )
00:00 am – 8:00 am	-13.3	-	<b>-13.3</b>	-	100.3	<b>100.3</b>	-1.1	18.3	<b>17.2</b>
8:00 am – 12:00 am	-17.9	-	<b>-17.9</b>	-4.5	16.1	<b>11.7</b>	-47.7	-	<b>-47.7</b>
12:00 am – 16:00 am	-0.8	17.4	<b>16.6</b>	-40.0	-	<b>-40.0</b>	-64.6	-	<b>64.6</b>
16:00 am – 20:00 am	-	39.3	<b>39.3</b>	-26.4	-	<b>-26.4</b>	-4.5	13.1	<b>8.7</b>
20:00 am – 00:00 am	-	16.9	<b>16.9</b>	-0.6	11.1	<b>10.5</b>	-	49.1	<b>49.1</b>

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Table 5. RMSE for each nodes,  $T_1$  is the outdoor surface temperature,  $T_{10}$  is the indoor surface temperature, except for configuration A in which  $T_8$  correspond to the inner layer.

node	Config. A	Config. B	Config. C
$T_1$	3.4°C	3.8 °C	4.0°C
$T_3$	3.2°C	3.5 °C	4.0°C
$T_4$	3.3°C	3.2 °C	3.8°C
$T_5$	3.5°C	3.5°C	3.2°C
$T_6$	1.2°C	0.5 °C	0.5°C
$T_8$	1.9°C	n/a	n/a
$T_9$	n/a	0.5°C	0.5°C
$T_{10}$	n/a	0.4 °C	0.4°C

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