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# Linear combination of auditory steady-state responses evoked by co-modulated tones

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**Abstract:** Up to medium intensities and in the 80–100-Hz region, the auditory steady-state response (ASSR) to a multi-tone carrier is commonly considered to be a linear sum of the dipoles from each tone specific ASSR generator. Here, this hypothesis was investigated when a *unique* modulation frequency is used for all carrier components. Listeners were presented with a co-modulated dual-frequency carrier (1 and 4 kHz), from which the modulator starting phase  $\Phi_i$  of the 1-kHz component was systematically varied. The results support the hypothesis of a linear superposition of the dipoles originating from different frequency specific ASSR generators.

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## 1. Introduction

The auditory steady-state response (ASSR) is an auditory evoked potential which follows the repetition rate, defined by the modulation frequency  $f_m$ , of an ongoing sound signal (Picton *et al.*, 2003). For repetition rates between 80 and 100 Hz, the ASSR has been shown to arise from brainstem sources, while at lower rates (below 40 Hz), mostly sub-cortical and cortical sources are involved (Herdman *et al.*, 2002a).

When evoking the ASSR with sinusoidally amplitude-modulated (SAM) tones, an activation of auditory nerve fibers within a narrow region of the basilar membrane (Picton *et al.*, 2003) is assumed. The response to multiple SAM tone carriers with differing modulation frequencies has been shown to be a linear combination of the responses to each SAM component in the 80–100 Hz range of repetition rates (e.g., Herdman *et al.*, 2002b). However, for modulation frequencies around and below 40 Hz, multiple ASSR components do not combine linearly (John *et al.*, 1998), presumably because of interactions within the sub-cortical and cortical sources of the ASSR.

At higher stimulation levels, this linear combination of the ASSR components does not hold (Picton *et al.*, 2007). This can be explained by the nonlinear mechanics of the auditory periphery: a travelling wave excited by a pure tone carrier does not only result in an isolated vibration around the peak region of the carrier, but also evokes vibrations basal to that region. Stimuli presented at higher levels and composed of multiple frequency components are thus likely interacting across different regions along the basilar membrane. The contribution of different tonotopic regions to the ASSR has also been addressed in the context of chirp-evoked ASSRs (Elberling *et al.*, 2007), where it was found that the amplitude of the ASSR can be increased by stimulation with chirps accounting for the dispersion properties of the basilar membrane. For these stimuli, it is, however, not clear how each tonotopic region contributes to the measured ASSR other than that the overall amplitude increases.

For binaural stimulation with modulation frequencies around 80 Hz, a linear combination of ASSRs has been shown, also for components having the same modulation frequency, suggesting either the independence of two separate sources, or the linearity of a unique source of ASSR (e.g., Poelmans *et al.*, 2012).

Here, the assumption of a linear, monaural superposition of multiple co-modulated sources of ASSR in the 80 Hz region was investigated. The ASSR was recorded with electroencephalography (EEG), and was evoked by two SAM tones centred, respectively, at 1 and 4 kHz. Both carriers were modulated with the same modulation frequency but with a relative phase that was varied across conditions. It is

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hypothesized that the overall response measured using EEG is the vector sum of the ASSR evoked by each SAM tone separately, and will be sensitive to the relative modulator phase between the SAM tones.

The results will contribute to the understanding of how multiple sources of ASSR combine into the electrical signal measured at the scalp.

## 2. Methods

### 2.1 Subjects

Nine subjects participated in the experiment. Their hearing thresholds were below 20 dB hearing level at all audiometric frequencies (125 Hz to 8 kHz), and the mean age was 29.8 years, ranging from 25 to 40 years. The experimental procedure was approved by the Danish Science-Ethics Committee (ref. number H-3-2013-004), and written informed consent was obtained from all subjects before data collection.

### 2.2 Stimulus and apparatus

Seven different stimuli were used to elicit ASSRs, consisting of two SAM tones,  $s_{1k}$  and  $s_{4k}$ , and of five combined versions of those same tones with varied modulator starting phases of  $s_{1k}$ . The carrier frequencies of the two tones,  $f_{1k}$  and  $f_{4k}$ , were set, respectively, at 1 and 4 kHz. The carriers were 100% modulated at a frequency  $f_m$  of 88 Hz, as shown in Eqs. (1) and (2),

$$s_{1k}(t) = a_{1k} \sin(2\pi f_{1k}t) \left( \frac{1 + \sin(2\pi f_m t + \Phi_i)}{2} \right), \quad (1)$$

$$s_{4k}(t) = a_{4k} \sin(2\pi f_{4k}t) \left( \frac{1 + \sin(2\pi f_m t)}{2} \right). \quad (2)$$

When  $s_{1k}$  was presented in isolation, its modulator starting phase  $\Phi_i$  was set to 0. For the five co-modulated conditions, stimuli were created by setting  $\Phi_i$  to values distributed around the unit circle ( $c^{\Phi_i} = s_{1k}^{\Phi_i} + s_{4k}$ ;  $\Phi_i = 2i\pi/5$ ,  $i = 0, 1, \dots, 4$ ), while  $s_{4k}$  was kept the same.

To avoid distortions in the co-modulated conditions, the two carriers were played separately through two ER-2 earphones mounted on an ER-10B+ probe (Etymotic Research, Inc.), and connected to the computer through a Phonitor mini amplifier (SPL electronics GmbH) and a Fireface UCX sound card (Audio AG). Both  $a_{1k}$  and  $a_{4k}$  were adjusted to deliver  $s_{1k}$  and  $s_{4k}$  at 65 dB sound pressure level (SPL) in isolation, using a B&K 4137 ear coupler and a B&K 2636 sound level meter (Brüel & Kjær A/S).

### 2.3 ASSR recording and analysis

Subjects were seated in a double-walled, electrically shielded, sound-attenuating booth. They were instructed to relax and stay calm. They watched a silent film with subtitles throughout the whole recording session, and were awake at all time. The stimulated ear was randomized across subjects, and the opposite ear was occluded with an ear plug, to avoid acoustical cross-talk.

EEG signals were recorded using a BioSemi ActiveTwo system (Biosemi B.V.), sampled at 8192 Hz, and analyzed offline with MATLAB (The MathWorks, Inc.).

A vertical electrode montage was used, using the 10/20 system, with two electrodes: P9 or P10 at the left or right mastoid, respectively, and Cz at the vertex. If the right ear was stimulated, the difference between Cz and P10 was computed, while Cz and P9 were used for the left ear stimulation. Each stimulus condition was recorded for approximately 10 min (608 s). The signal was cut into epochs of 16 s, and any epoch exceeding 80  $\mu$ V was discarded from the processing. A weighted averaging method based on the standard deviation in each epoch (John *et al.*, 2001) was then applied to obtain a single 16-s epoch, from which the fast Fourier transform (FFT) was computed with a bin width of 0.0625 Hz. A F-ratio was computed between the power of the FFT bin at 88 Hz (chi-squared variable with 2 degrees of freedom) and the power of the EEG background noise (96 neighbouring bins,  $\pm 3$  Hz,  $96 \times 2$  degrees of freedom). The ASSR was deemed above the noise floor when the null hypothesis that both noise and ASSR component came from the same F distribution was rejected ( $p \leq 0.01$ , Dobie and Wilson, 1996). This corresponds to a signal-to-noise ratio above or equal to 6.73 dB [=  $10 \log_{10}(P_{\text{signal+noise}}/P_{\text{noise}})$ ].

Due to anatomical differences (head size, neural sources), inter-subject variability in the group delay (and therefore the phase) is expected. Because of this, co-modulated responses are likely to be in/out of phase for different values of  $\Phi_i$  across listeners. Measured amplitude responses to the  $c^{\Phi_i}$  stimuli were therefore shifted to have their maximum value at  $\Phi_i=0$  rad (Riecke *et al.*, 2015).

Before computing the phase of the co-modulated ASSRs, the response to  $s_{4k}$  in isolation was subtracted ( $\text{ASSR}(c^{\Phi_i}) - \text{ASSR}(s_{4k})$ ). In the case of linearity, the phase of this vector subtraction should therefore equal  $\Phi_i$ , the phase of  $s_{1k}$ . Again, to account for inter-subject variability in group delay, the phase of the afore-mentioned subtraction was shifted to be 0 rad for  $\Phi_0$ . Unless specified, the  $\Phi_0$  condition was removed from all statistical analysis, as data for this point do not satisfy independence requirements.

### 3. Results

#### 3.1 Responses to single carriers

The amplitudes of the ASSRs were above the noise floor for 8 out of 9 subjects in response to  $s_{1k}$ , and 7 out of 9 in response to  $s_{4k}$ . They were similar in amplitude [Fig. 1(B)] and comparable in value to previously reported amplitudes at those stimulation levels (Picton *et al.*, 2007). Overall (including the responses to co-modulated carriers), mean amplitude and standard deviation of the significant ASSRs were, respectively, 52.5 and 26.5 nV. One subject had higher noise levels (mean/s.d. of 48.9/4.3 nV versus a mean and s.d. of, respectively, 10.7 and 2.5 nV for the other subjects). Since this subject did show significant ASSRs in some conditions, it was not excluded. We, however, controlled for every statistical analysis that removing this subject did not change the main conclusions.

The difference in phase between the responses to  $s_{1k}$  and  $s_{4k}$  was  $103^\circ$ , as shown in Fig. 1(A). In order to link the ASSR phase to an estimate of cochlear travel time, and assuming a linear phase of the frequency components along the cochlea, this phase corresponds to a latency difference of 3.3 ms for a modulation frequency of 88 Hz ( $103/360 \times 88$ ). This difference was statistically significant (paired-sample *t*-test with the seven subjects having both responses above significance;  $df = 6$ ;  $p = 0.0019$ ,  $t = 5.2691$ , 95% confidence interval = 1.7–4.8 ms).

#### 3.2 Co-modulated responses

By combining Eqs. (1) and (2), one can hypothesize that the mean vector sum of all co-modulated responses should equal the response to  $s_{4k}$  in isolation, as shown in Eqs. (3)–(5) and Fig. 1,

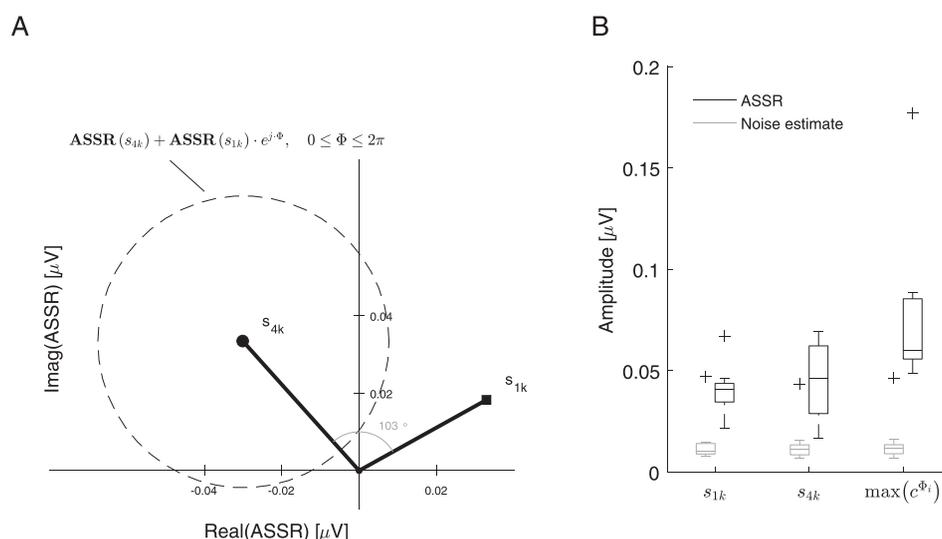


Fig. 1. (A) Averaged complex-valued ASSRs across subjects in response to the  $s_{1k}$  (square) and  $s_{4k}$  (circle) stimuli. Shown with a dashed line is the expected co-modulated response (linear vector summation) when varying  $\Phi_i$ , the modulator starting phase of  $s_{1k}$ . (B) Across-subject distribution of ASSR amplitudes (black) and of noise estimates (grey) in response to the  $s_{1k}$ ,  $s_{4k}$ , and  $c^{\Phi_i}$  stimuli. For  $c^{\Phi_i}$ , only the maximum amplitude across all angles is shown. Lower and Upper limits of the boxes: 25th and 75th percentiles. Horizontal line: median. Whiskers: 25th (or 75th) percentile minus (or plus) 1.5 the interquartile range.

$$\frac{1}{5} \sum_{i=0}^4 \text{ASSR}(c^{\Phi_i}) = \frac{1}{5} \sum_{i=0}^4 \left( \text{ASSR}(s_{4k}) + \text{ASSR}(s_{1k}) e^{j(2i\pi/5)} \right) \tag{3}$$

$$= \text{ASSR}(s_{4k}) + \text{ASSR}(s_{1k}) \sum_{i=0}^4 e^{j(2i\pi/5)} \tag{4}$$

$$= \text{ASSR}(s_{4k}). \tag{5}$$

A t-test comparing the mean vector sum of all co-modulated responses to the response to  $s_{4k}$  in isolation showed no significant difference ( $df=6$ ,  $p_{real}=0.7617$ ,  $t_{real}=-0.3173$ ,  $p_{imaginary}=0.5832$ ,  $t_{imaginary}=-0.5798$ , Pearson's  $r=0.8322$  when pooling real and imaginary values,  $r=0.8310$  when removing the subject with high noise level). This t-test excluded two subjects who had missing data in one condition (hence  $df=6$ ), and was run on both real and imaginary parts of the ASSR, as they can be considered to be independent variables (Dobie and Wilson, 1996).

*Amplitude.* As shown in Fig. 1(B), the individual maximum for each subject across all co-modulated conditions was significantly larger than the response to the single carriers in isolation (pairwise t-Tests, paired data within subjects, Bonferroni corrections,  $p=0.00023$  and  $p=0.000232$  for  $s_{1k}$  and  $s_{4k}$ , respectively). The data were log-transformed for this test to account for the presence of a subject with higher overall amplitudes. Figure 2(A) shows the amplitudes obtained for all co-modulated stimuli, with the individual responses aligned to be largest at  $\Phi_0=0$  rad, and normalized by their value at  $\Phi_0$ . A multilevel approach for repeated measures was employed, with the subjects as a random factor (Field *et al.*, 2012), and failed to show a significant effect of  $\Phi_i$  on the relative amplitude as plotted in Fig. 2(A) [ $\chi^2(3)=6.98$ ,  $p=0.0726$ , data points below the noise floor excluded]. By adding the points below the noise floor in this statistical analysis, the effect of  $\Phi_i$  becomes significant [ $\chi^2(3)=13.67$ ,  $p=0.0034$ ]. It is worth noticing that conditions  $\Phi_2$  and  $\Phi_3$  had the highest number of recordings below the noise floor [Fig. 2(B)], where  $s_{1k}$  and  $s_{4k}$  were expected to be out of phase.

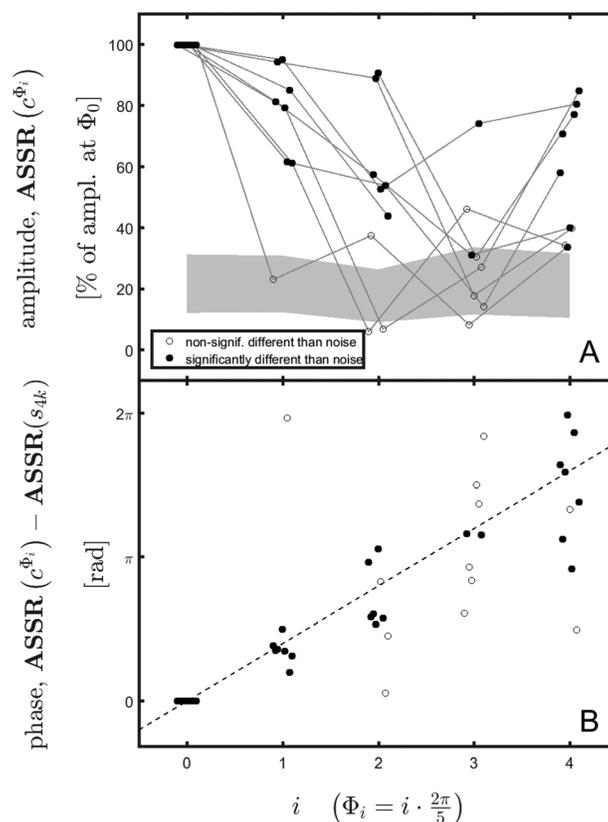


Fig. 2. (A) Amplitudes of individual co-modulated responses, shifted to have their maximum at  $\Phi_0$ , and normalized by their value at  $\Phi_0$ . A small jitter has been added to the x axis to improve readability, and the noise floor excursion (min to max) is shown with the grey shaded area. As noise levels differed across subjects, it can be seen that the amplitude (on a relative scale) required to have a significant response varies across subjects. (B) Phase of the vector subtraction  $\text{ASSR}(c^{\Phi_i}) - \text{ASSR}(s_{4k})$  (which should be  $\Phi_i$  in case of linearity), normalized to be 0 at  $\Phi_0$  and wrapped between 0 and  $2\pi$ .

To assess whether the proportion of significant points was the same between different  $\Phi_i$  conditions, a Cochran Q test was used, and showed a significant effect of  $\Phi_i$  ( $Q = 8.4000$ ,  $df = 3$ ,  $p = 0.0384$ ).

*Phase.* Figure 2(B) shows the phase values corresponding to Fig. 2(A), re-referenced to be 0 for  $\Phi_0$  and wrapped between 0 and  $2\pi$ .  $\Phi_i$  had a significant effect on the ASSR phase [ $\chi^2(3) = 37.8$ ,  $p < 0.0001$ ]. This effect was well fitted by a linear regression (intercept =  $-0.1255$ , slope =  $0.9967$ , 95% confidence interval =  $0.75$ – $1.19$ ,  $r^2 = 0.7956$ ).

#### 4. Discussion

In the 80–100-Hz range, it has been hypothesized that the ASSR evoked by SAM tones with different modulation frequencies is the linear superposition of the response to the SAM tones presented alone. This assumption has been shown to hold true if the carrier frequencies are separated at least by an octave, and if medium levels are used (Herdman *et al.*, 2002b). The present study supports the hypothesis of a linear superposition, and expands it to the case of carriers modulated with a unique modulation frequency presented monaurally (this has already been shown binaurally, e.g., in Poelmans *et al.*, 2012). However, because the ASSR measured by EEG is a gross potential, it cannot be distinguished whether the observed effects in the presented paradigm are due to a superposition of two independent sources contributing to the ASSR or if the effects are due to neural interactions within a single source of the ASSR.

##### 4.1 Linearity of the co-modulated conditions

Under our linearity assumption, and because  $\Phi_i$  was evenly distributed around the unit circle, summing all co-modulated responses should not be significantly different than the response to  $s_{4k}$  in isolation, and this is indeed what we could see in our recordings.

Additionally, manipulating the modulator starting phase of  $s_{1k}$  in the co-modulated conditions had a significant effect on both phase and amplitude of the ASSR. This effect was consistent with a linear sum when analyzing the co-modulated phase response [Fig. 2(B)], while the individual patterns of the amplitude were more variable [Fig. 2(A)]. These deviations seen in the amplitude of the co-modulated responses might be due to the inherent test-retest variability of the ASSR. Finally, when both single carriers were supposedly out of phase (conditions  $\Phi_2$  and  $\Phi_3$  in Fig. 2), it was often impossible to record a significant response, even with 10 min of recording and median noise levels of 10.9 nV.

Taken together, these results support the hypothesis of a linear superposition, and that distinct neural populations are represented in the ASSR, even when using a unique modulation frequency. John *et al.* (2003) measured the ASSR of 4 SAM tones at 0.5, 1, 2, and 4 kHz, co-modulated and in isolation. The co-modulated response was 25% lower than expected by a linear vector superposition of the responses in isolation. This reduction, not seen in our study, might be explained by the fact that they used four carriers separated by only one octave (while we used only two carriers separated by two octaves). This might have led to interactions at the level of the basilar membrane, such as mutual suppression.

In contrast to multi-tone carrier ASSRs, single-evoked ASSR growth functions do not show a saturation for stimulus levels above 60 dB SPL (Picton *et al.*, 2007). Based on the results of the present study, one might however speculate that responses evoked by off-frequency regions also contribute to the measured amplitude in single-evoked ASSRs, and that the measured ASSR is a linear combination of responses evoked by on- and multiple off-frequency regions with different relative phase.

##### 4.2 Further use of this paradigm

As linearity seems to be respected with this paradigm, any measured non-linearity could be used as a marker for envelope interactions at the level of the cochlea. An example is for cochlear implant users, where the spread of electrical current produces marked envelope interactions in a behavioural task (Galvin *et al.*, 2015).

#### 5. Conclusions

This study suggests that the ASSR at 88 Hz with co-modulated carriers presented monaurally is a linear sum of the response to each carrier, as supported by the phase behaviour of the co-modulated response and the vector sum of all co-modulated responses.

Such a paradigm, where the phase difference between co-modulated carriers is varied, is therefore suitable for analyzing envelope interactions with a unique modulation frequency and at peripheral levels of the auditory system.

Raw data files (.bdf and stimuli files) are accessible on Zenodo (Guérit *et al.*, 2017).

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