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Computational Design of Biomimetic Phosphate 1 Scavengers 2

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21 1 Abstract

22 Phosphorous has long been the target of much research, but in recent years the focus has 23 shifted from being limited only to reducing its detrimental environmental impact, to also looking 24 at how it is linked to the global food security. Therefore, the interest in finding novel techniques 25 for phosphorous recovery, as well as improving existing techniques, has increased. In this study 26 we apply a hybrid simulation approach of molecular dynamics and quantum mechanics to 27 investigate the binding modes of phosphate anions by a small intrinsically disordered peptide. 28 Our results confirm that the conformational ensemble of the peptide is significantly changed, or 29 stabilized, by the binding of phosphate anions and that binding does not take place purely as a 30 result of a stable P-loop binding nest, but rather that multiple binding modes may be involved. 31 Such small synthetic peptides capable of binding phosphate could be the starting point of new 32 novel technological approaches towards phosphorus recovery, and they represent an excellent 33 model system for investigating the nature and dynamics of functional de novo designed 34 intrinsically disordered proteins.

2 Introduction

35

Phosphorous (P) is an essential element in terms of sustaining the world's current and
future food supply, for which there is no substitute.¹⁻³ Given that the current P supply is based on
the gradual depletion of limited fossil reserves, an increasing demand for P necessitates a change
towards more sustainable practices where P is recovered from the large waste streams. The
lifetime of remaining high quality phosphate rocks is still being debated, estimates varying from a
few decades to a few hundred years.^{3,4} There is however a general consensus that P is becoming
more and more difficult to access, costs are increasing, more waste is being produced, and the

global demand is expected to increase.^{4,5} Meanwhile, only a fraction of the mined P makes it into
the intended plants and animals which humans consume, while most is lost along the way causing
serious environmental problems e.g. by eutrophication of lakes, reservoirs, estuaries, and parts of
the ocean.^{2,4,6,7}

47 The topic of P has been a point of interest for waste-water treatment engineers for 48 decades.⁸ The main attention has however so far been focused almost exclusively on reducing 49 eutrophication, so while many of the now common techniques for P treatment, e.g. chemical 50 precipitation⁸ and enhanced biological phosphorus removal⁹ (EBPR), are highly efficient for the 51 job they were designed for, they are not necessarily effective in terms of recovering P from its 52 large waste flows, which have different characteristics from the commonly treated domestic 53 wastewater flows and are not always easily intercepted (e.g. erosion and runoff²). One of the 54 current main technologies, optimized for P removal but also applicable to recovery to some 55 extent, is EBPR, where polyphosphate accumulating organisms are used to capture and store high 56 amounts of P in their heterotrophic biomass. These organic biosolids may subsequently need to 57 be treated prior to reuse of the P, or they may be used directly in agricultural settings, e.g. as a 58 slow-release fertilizer. EBPR however faces several limitations, perhaps the most serious being 59 that energy recovery (methane production) must be carried out in a strictly anaerobic system, 60 which is not easily combined with the aerobic and anaerobic conditions needed in EBPR-based 61 waster water treatment.^{2,10}

Biological techniques such as EBPR are encouraged by the fact that certain
microorganisms flourish in P-limited environments by having developed efficient enzymes and
proteins that bind with high specificity and reversibility to phosphorus compounds.^{11,12} This
makes biomimetic approaches for P recovery generally interesting, and we recently did a

66 statistical analysis of how proteins in nature bind different phosphorus compounds in order to 67 reveal common binding site characteristics.¹³ One of the most common ways in which proteins 68 bind phosphates non-covalently, and in particular the β -phosphate of ATP and GTP, is through the 69 P-loop, which is characterized by the consensus sequence Gly-Xxx-Xxx-Xxx-Gly-Lys-70 (Ser,Thr).¹⁴⁻¹⁸ Inspection of the three-dimensional structure of P-loops reveals that it is 71 remarkably well conserved throughout nature, and the main conformation of the sequence is 72 generally found to form a feature resembling an anion-binding nest.^{19,20} A classic "nest" feature in 73 biochemistry is defined to consist of three amino acids, and can be either in a LR or RL 74 configuration, depending on the main chain dihedral angles of the two first residues.²¹ The anion-75 binding nest seen for the P-loops is formally a series of overlapping nests, typically in an LRLR 76 conformation for the Xxx-Xxx-Gly-Lys part of the consensus sequence.²² Although the P-loop nest 77 structure is expected to be essential for binding of the phosphate anion, the anion is also expected 78 to stabilize the nest conformation, which has been demonstrated for some P-loop proteins by X-79 ray crystallography; i.e. the P-loop without the anion is supposedly fairly flexible and without any 80 stable structure.^{23,24}

81 Recently, a hexapeptide with the sequence Ser-Gly-Ala-Gly-Lys-Thr (SGAGKT) was 82 synthesized Bianchi *et al.* based on the P-loop consensus sequence.²⁵ The two glycines in this 83 peptide were introduced to promote a natural LRLR conformation, and the peptide in its lysineprotonated zwitter-ionic state was found be a capable binder of phosphate anions PO_4^{3-} and HPO_4^{2-} , 84 whereas $H_2PO_4^{1-}$ and H_3PO_4 were found not to be bound. From their studies, it is expected that the 85 86 synthetic peptide form a classical LRLR nest structure when binding of the anion. Due to its small 87 size, it is reasonable to assume that when unbound in solution this peptide does not posses a well-88 defined secondary structure and instead exists as a dynamic ensemble of conformations which 89 may posses transient residual secondary structure, or consist of multiple structures that rapidly

90 exchange.²⁶ As such it is not unreasonable to assume that the peptide might potentially have a 91 nature similar to intrinsically disordered proteins (IDPs), IDPs having received increasing interest 92 in the scientific community in recent years,²⁷ given that they compose approximately 20% of the 93 proteome.²⁸ Conventionally, when a given ligand binds to an IDP, the favorable free energy from 94 binding is offset by the loss in conformational entropy, resulting in complexes that can be highly 95 specific with low overall binding energies.²⁹ For the SGAGKT peptide, however, binding of the 96 phosphate anions has experimentally been found to be attributed to favorable entropic 97 contributions.²⁵

98 In order to further investigate the nature of how the P-loop binds and interacts with 99 phosphate, in this study we apply molecular dynamics (MD), accelerated molecular dynamics 100 (aMD) and semi-empirical quantum mechanics (QM) in a hybrid approach (QM/MM) to simulate 101 how the phosphate anion is bound by the peptide SGAGKT, and demonstrate how these results 102 correlate with experimental data. MD is a simulation technique which can be used for simulating 103 the physical movements of atoms in molecules in the context of classical dynamics, using 104 empirically determined forcefields.³⁰ For more details on the approach see Appendix A. Our 105 simulations confirm the suspected intrinsically disordered nature of the peptide in the absence of 106 an anion, and demonstrate how the addition of an anion stabilizes the conformational space. They 107 also suggest, however, that the phosphate anions are not completely stably bound in a singular P-108 loop nest structure, as hypothesized in literature, but rather that multiple binding conformations 109 exist; this translates to a very reversible binding mechanism, and is therefore of considerable 110 interest for applications involving phosphorus recovery. The use of a phosphate-binding peptide 111 in a biomimetic system represents a model where there is no need for growing heterotrophic 112 bacteria. Despite such technology still being at its infant state, it may thus potentially be superior

113 to current technologies such as EBPR, and it is therefore an appealing area of research in the114 future of resource recovery.

- 115 3 Materials and Methods
- 116 **3.1** Model System

117 All MD simulations were run using the molecular modeling packages Amber14 and 118 AmberTools14.³⁰ To set up a given peptide simulation, first the fully extended peptide was created 119 using the module LEaP in AmberTools14. For peptide-anion systems, the anion was added randomly to the system on a sphere 100Å away from the peptide, hereafter it was translated to 120 121 3.5Å proximity of the closest atom in the peptide, thereby ensuring random starting positions. All 122 systems were built with LEaP using the ff14SB force field parameters³¹ and were explicitly 123 solvated using the TIP3P model for water³² in rectangular boxes with 10.0Å to each edge from the 124 system of interest. This resulted in each simulation having between 1450 and 1650 water 125 molecules. To minimize system complexity no counter ions were included in the simulations.

126 The systems were minimized for 10,000 steps: 5,000 steps using a steepest descent 127 algorithm and 5,000 steps using a conjugated gradient algorithm. Heating of the system to 300K 128 over 0.8ns was then performed with a weak restraint of 1 kcal/mol on the peptide-anion, and 129 afterwards the systems were equilibrated for 0.2 ns without any restraints at 300K. Heating was 130 performed under constant volume and temperature (NVT ensemble). Equilibration and 131 production runs were performed at 300K using the Langevin thermostat with a collision 132 frequency of 1 ps⁻¹, and the pressure was set to 1 bar using the Berendsen barostat (NPT 133 ensemble). Hydrogens were restrained using SHAKE³³, non-bonded interactions were cut off at

134 10.0 Å, and full electrostatics for the periodic system were calculated using the Particle Mesh
135 Ewald approach.³⁴

In all peptide-anion simulations, the phosphate anions were marked as quantum regions
and treated using the semi-empirical PM6 hamiltonian with dispersion correction as implemented
in Amber14.^{30,35} SHAKE restriction was used on all hydrogens in the QM region and all simulations
were performed with a 2 fs timestep. The *sander* module of Amber14 was used for QM/MM
simulations and *pmemd.cuda* was used for all peptide-only simulations.

141 3.2 aMD simulations

For all aMD simulations the average potential and dihedral energies were first obtained from 2 ns
cMD runs on the same system. The hexapeptide SGAGKT has 74 atoms, and with the
approximation that each residue has an energy contribution of 3.5 kcal/mol, the values for the
parameters required for the aMD runs (see Appendix A) were calculated using empirical
estimates as specified in Eqs. 1-4, where αD and αP are added to the average values obtained from
the cMD simulations in order to account for the degrees of freedom in the peptide.³⁶

148

149 **Equation 1**

150

$$\alpha D = \frac{1}{5} \cdot 6 \cdot 3.5 \frac{\text{kcal}}{\text{mol}} = 4.2 \frac{\text{kcal}}{\text{mol}}$$

151 Equation 2

152

 $Ed = Ed_{avg} + \alpha D$

153	Equation 3	
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154	$\alpha P = \frac{1}{5} \frac{\text{kcal}}{\text{mol} \cdot \text{atoms}} \cdot 28 \text{ atoms} = 5.6 \frac{\text{kcal}}{\text{mol}}$
155	Equation 4
156	$Ep = Ep_{avg} + \alpha P$
157	
150	m]

To obtain the canonical ensemble the trajectories were reweighted through cumulant expansion
to the second order, using the python toolkit provided McCammon group.³⁷

160 3.3 Cluster Analysis & Principal Component Analysis

161 Clustering of trajectories and principal component analysis (PCA) were performed with 162 CPPTRAJ, which is the native post-processing utility of Amber14.³⁸ Clustering was done both with 163 an agglomerative hierarchical algorithm with ε set to 3.0 and using the DBSCAN³⁹ algorithm with 164 ε set to 1.2 and the minimum points set to 20. The distance metric used for both algorithms was 165 the root mean square deviation (RMSd) of all atoms in the peptide except for hydrogens. To 166 reduce processing time, a "sieve" value was chosen such that for a given trajectory, only 20,000 167 evenly spaced frames from the trajectory were used, and afterwards sieved frames were added 168 back into the clusters if applicable given the value of ε .

A powerful way to improve the information gained from clustering algorithms, is to combine it
with principal component analysis (PCA)⁴⁰, where the overall motions of the trajectories are
represented in a lower dimensional space by mapping the trajectories to a set of eigenvectors
calculated from the covariance matrix of the atoms.^{41,42} These eigenvectors are referred to as
"modes" throughout this work, such that each mode corresponds to a certain type of motion of the

peptide. Prior to all PCA the trajectories were RMS fitted to the overall average structure first, and
the coordinate covariance matrix was then calculated for all heavy atoms in the peptide. The
trajectories were projected along the calculated modes in order to obtain a time series of PCA
projection values for each mode.

The Kullback-Leibler divergence (KLD) has previously been shown to be a good indicator of
convergence between two independent simulations.⁴³⁻⁴⁶ Briefly, the KLD can be defined as

180 **Equation 5**

181

$$KLD(t) = \sum_{i} P(t,i) \cdot \ln\left(\frac{P(t,i)}{Q(t,i)}\right)$$

D () | |

182 where P(t, i) and Q(t, i) are the probability distributions of two independent simulations with t 183 being the time and *i* being the bin index. Practically, the KLD is a measure of information 184 difference between the two probability distributions, and as such when it converges towards zero 185 the distributions can be said to have converged. To calculate the KLD between two simulations, 186 PCA was first performed on the combined trajectory of the two simulations, and then the 187 normalized probability distributions along the first (largest) eigenvector for each simulation were 188 used in Eq. 5. For all histograms a total of 400 bins were used and a Gaussian kernel density 189 estimator, a fundamental method for estimating probability density / data smoothing, was used to 190 reduce the amount of bins with no population.⁴³

Structure alignment was done using the Kabsch algorithm, which is a method for calculating the
optional rotation matrix that minimize the RMSd between two sets of points.⁴⁷ As such it can be
used to align peptide structures and superposition them on top of each other.

194 4 Results & Discussion

195

4.1 Sampling the peptide conformational ensemble

Peptide-only cMD simulations were performed using the GPU-accelerated pmemd.cuda module of
Amber14, which enabled simulation times for each simulation of 100 – 200 ns/day with a single
NVidia Tesla M2050 node. To test whether the conformational ensemble for these simulations had
converged, KLD between the major modes of a PCA decomposition of a combined trajectory for
two independent simulations was calculated.

201 In Fig 1a, the KLD of the first three PCA modes are shown for the two peptide-only simulations, 202 confirming that after around 1 μ s the value is less than 0.02, which is used as the threshold value 203 for declaring convergence.^{43,45} Correspondingly, in Fig. 1b the RMSd frequencies for these two 204 simulations are shown after the 1 µs of simulation; i.e. it is a normalized frequency plot of RMSd 205 values, where the RMSd values have been calculated between each frame in the trajectories and a 206 common reference structure. Based on Fig. 1 it can be concluded that the conformational 207 ensemble of the peptide-only simulations are well-converged after 1 μ s of cMD simulation, 208 however it is noted how the KLD of mode 1 and 2 increases drastically at around 400 ns which 209 can be attributed to the two simulations exploring different parts of the conformational space at 210 that point. This highlights the dangers of interpreting too short simulations with KLD. It was 211 visually confirmed from the trajectories that during the simulation, the peptide undergoes such 212 large changes in conformation that additional cMD runs are deemed unlikely to change the 213 conformational space investigated or the obtained ensemble.

214

4.2 Restriction of the conformational space by HPO_4^{2-}

215 Introducing the phosphate anion into the system means it is no longer possible to use the 216 GPU implementation of pmemd in Amber14, since QM is not currently supported in the pmemd 217 modules. As a result, simulation times were limited to approximately 5 - 7 ns/day for each 218 simulation when using 16 cpu cores (Intel Xeon E5-2680, 2.80 GHz) with the sander module of Amber14. Four independent simulations were carried out with the peptide $-HPO_4^{2-}$ system for 219 100 ns. In Fig 2, 2d RMSd plots for a simulation of the peptide $-HPO_4^{2-}$ system, and a simulation of 220 221 a peptide-only system are shown. Despite the fact that neither of these systems are converged 222 after 100 ns, the seen behavior was consistently observed for all four anion simulations: the conformations sampled by the peptide throughout the simulation in the peptide-HPO $_4^{2-}$ systems 223 224 are retained for longer periods of time and appear more "stable" on the 100 ns timescale, whereas 225 the conformations sampled in the peptide-only simulations change more rapidly.

226 4.3 Enhanced sampling with aMD

227 The issue of poor conformational sampling of multiple-molecule systems in MD is a long-228 standing problem, and several attempts have been made to use different enhanced sampling 229 techniques to describe atomistic systems with varying levels of success. Here we use aMD to see if 230 we can improve the sampling time of the canonical ensemble for both peptide-only and peptide-HPO $_4^{2-}$ simulations. In the case of peptide-only simulations, it was found that the KLD for 231 two aMD simulations go below 0.02 already after 50-100 ns, and is further reduced to $\sim 10^{-3}$ after 232 233 the full 1 µs run (see supplementary information, Fig. S1). Considering that for cMD simulations 234 convergence was declared only after 700 ns, aMD clearly represents a powerful way of increasing 235 the sampling time for the conformational ensemble of the peptide-only simulations. For it to be 236 truly useful, reweighting must be performed to obtain the original ensemble – using a cumulant

expansion algorithm to the second order, this reweighting was found to successfully reproduce
the canonical ensembles from 50 ns aMD peptide-only simulations (see supplementary
information, Fig. S2). The challenge, then, is whether or not aMD can similarly be used to simulate
converged ensembles for the peptide-anion systems investigated in this work as well.

In Fig. 3 the KLD's between four independent 100 ns cMD and aMD peptide $-HPO_4^{2-}$ 241 simulations are shown. The KLD for the cMD peptide $- HPO_4^{2-}$ simulations are not seen to 242 243 decrease notably, meaning that the conformational ensembles have not converged during the 100 244 ns of simulation time. Compared to the cMD simulations, it is clear from Fig. 3 that aMD increases 245 sampling speed, but also that despite the relatively large boost from aMD (avg. 4.5 kcal/mol), it 246 does not reach full convergence (KLD < 0.02) after 100 ns. Given that it takes the conformational 247 ensembles of peptide-only simulations on the order of 1 µs to converge using cMD and 50-100 ns 248 using aMD, it is no surprise that a peptide-anion system does not converge during 100 ns. The 249 introduction of an anion into the system significantly complicates the system and thereby the 250 required time for the ensemble to converge; it is noted that the ligand will likely also spend a 251 certain amount of time in an unbound state, such that the convergence time should be at least that 252 of the peptide-only system. One can only speculate about the time-scale required for the ensemble of the peptide $-HPO_4^{2-}$ system to converge fully, but it is likely to be on the order of several micro-253 254 seconds if not even in the milli-second range for cMD and micro-seconds for aMD.

Recalling that a KLD plot for two simulations is created from the overlap between the PCA histograms, KLD values of 0.1 in the case of the aMD peptide—HPO₄^{2–} system clearly indicate that the four simulations presented in Fig. 3 sample similar motions and conformations and there is a significant overlap. As such, these close-to-converged ensembles can still be analyzed in terms of which conformations are present, with the precaution that the true frequency of eachconformation in the ensemble is unknown.

261 4.4 Cluster & PCA analyses

MD trajectories can contain on the order of millions of frames, so in order to obtain a
qualitative picture of a given system's properties, reduced representations of the trajectories must
be constructed first. The two most commonly used techniques for creating such reduced
representations are principal component analysis (PCA) and clustering algorithms.⁴⁰

266 Clustering algorithms can be separated into two basic types; hierarchical and partitioning 267 algorithms.⁴⁸ In hierarchical algorithms the decomposition can be viewed in the form of a 268 dendrogram, i.e. a tree where the dataset D is split into smaller subsets such that each node of the 269 tree represents a cluster. This can be done either from the leaves up (agglomerative approach) or 270 from the root down (*divisive approach*). Regardless of the approach, the hierarchical algorithms 271 require the input of a termination condition, e.g. a critical distance between each cluster – this is 272 the main problem with those kind of algorithms, since the clusters are sensitive to small changes 273 in the termination condition as well as noise in the dataset. With partitioning algorithms the 274 dataset D is initially split into a set of k clusters and then an iterative strategy is used to optimize 275 some objective function. These algorithms require k as an input parameter, which limits their use 276 since enough knowledge about the domain may not be known beforehand.

An alternative clustering approach to the two basic types are density based clustering
algorithms, where clustering is performed based on definitions of densities and connectivities in
the dataset.^{39,49,50} One of the most common of these is the DBSCAN algorithm³⁹, which creates
clusters based on a simple notion of density-connectivity between points in the dataset. The
DBSCAN algorithm requires the input parameter for minimum points in a given cluster and *ε*

282 which characterizes the ε -neighbourhood of a given point, i.e. the connectivity of points in the 283 cluster. DBSCAN filters out points in the dataset that do not belong in a given cluster as "noise", 284 which would otherwise be added into the closest cluster in other algorithms (e.g. the 285 hierarchical). It furthermore supports an effective heuristic denoted the *sorted k-dist graph*, i.e. a 286 sorted list of the Kth farthest distance for each point in the dataset, which helps the user in 287 determining the two input parameters.³⁹ Clustering is inherently a highly complicated task, and 288 the DBSCAN algorithm suffers from several disadvantages, e.g. it expects a density drop to detect 289 the borders of the clusters, which means it might not be able to detect some of the more intrinsic 290 clusters present in natural dataset. The DBSCAN algorithm has been revisited in the form of 291 several extensions and modifications since its first description⁵¹⁻⁵³, however the algorithm in its 292 original form has stood the test-of-time and is generally considered a powerful clustering 293 algorithm.

294To determine binding modes for the SGAGKT peptide to phosphate anions, we used both a295hierarchical agglomerative algorithm and the DBSCAN algorithm. The cutoff used for the296hierarchical algorithm was set to 3Å, which was empirically determined to result in297approximately 10-20 clusters for each simulation. For DBSCAN the minimum points and ε298parameters were set to approximately 20 and 1.2 respectively, based on k-dist plots (See299supplementary information, Fig. S3).

In Fig. 4, clustering results are presented for peptide-only (1 μs cMD) along the PCA
projections for the two major modes (comprising ~ 60% of the total peptide motion, see
supplementary information, Fig. S4-S6). It is clearly observed how the two different clustering
algorithms are different in terms of how they cluster the trajectories. The DBSCAN algorithm sorts
out a large part of the trajectory as noise (78 ± 1% for peptide-only simulations), whereas the

305 hierarchical algorithm clusters all points together based on their closeness to each other. The peptide bound to HPO_4^{2-} does show transiently stable conformations as evident from the DBSCAN 306 307 analysis (see supporting information, Fig. S7), however, the majority of the time is spent in 308 conformations of a more disordered nature (57 \pm 10% is filtered off as noise), at least within the 309 DBSCAN terminology and the algorithm input parameters. The same is evident from the free energy profiles, where local minima are observed for both the peptide-only and peptide-HP 0_4^{2-} 310 311 simulations; the barriers around these minima are however fairly broad and smooth, which 312 reflects the disordered nature of the peptide.

313 In Fig. 5 aligned superpositions of the different clusters are presented for four 100 ns 314 peptide-HPO₄²⁻ simulations and two 1 μ s peptide-only simulations, which is done to visualize the 315 difference between the semi-stable DBSCAN conformations and the hierarchical clusters of the 316 peptide. In Fig. 5a-b all the DBSCAN clusters, containing both peptide and anion, are shown – it is 317 evident that these have a tendency towards the expected P-loop structure, where the backbone and the lysine side-chain folds around the anion in a nest structure. In the case of peptide-HPO₄²⁻ 318 simulations, $57 \pm 10\%$ of the ensemble was filtered off as noise by the DBSCAN algorithm: 319 320 compared to the 78 \pm 1% for peptide-only simulations, this again shows that the anion stabilizes 321 the disordered ensemble. The hierarchical clusters shown in Fig. 5c-d on the other hand display 322 much more variation in the peptide-anion interaction: in a significant amount of the clusters the 323 anion is found to be interacting with the more or less extended peptide by only 1-3 hydrogen 324 bonds without any nest-like structure. For the peptide-only simulations the DBSCAN clusters in a 325 similar fashion reveal a series of semi-stable nest-like states (Fig. 5e), where the backbone is 326 folded up in a nest with the lysine chain is in a more or less indeterminate orientation. The 327 hierarchical clusters on the other hand show the disordered nature of the peptide – and it is in 328 this disordered state that the peptide spends most of its time (Fig. 5f).

329	In the original paper where Bianchi et al. synthesized and investigated SGAGKT
330	experimentally, they found that the peptide in its lysine-protonated zwitterionic state bound to
331	HPO_4^{2-} with $\Delta G = -4 \pm 0.1$ kcal/mol, whereas $H_2PO_4^{1-}$ was found not to be bound. The ensembles
332	of our peptide– HPO_4^{2-} simulations are not fully converged, but can still be considered close-to-
333	converged. It is therefore interesting to see how these ensembles compare against the
334	experimental binding energy; this can be done using a method known as molecular mechanics
335	Poisson-Boltzmann surface area (MM-PBSA), which is a post-processing approach to estimating
336	free energies and binding energies of molecules in solution. ⁵⁴ For the combined 400 ns trajectory
337	of the peptide–HPO $_4^{2-}$ simulations, this approach calculates an average favorable binding free
338	energy of 1.72 \pm 0.28 kcal/mol. For 200 ns peptide-H ₂ PO ₄ ¹⁻ simulations, an average favorable
339	binding free energy of 1.45 \pm 0.24 kcal/mol was found, indicating that also this anion is bound by
340	the peptide, albeit more weakly, which can likely be attributed to the less electronegative nature
341	of $H_2PO_4^{1-}$. Looking at the binding energy distributions obtained from MM-PBSA (see
342	supplementary information, Fig. S8), it is observed that these are markedly different for the two
343	anions, with HPO_4^{2-} having a broader distribution that is shifted towards more favorable binding
344	energies compared to $H_2PO_4^{1-}$ which is more centered around $\Delta G = 0$, and it is clear from the
345	energy distributions that there is a difference between how $H_2PO_4^{1-}$ and HPO_4^{2-} bind to the
346	peptide. The discrepancy with experimental results can be attributed to the close-to-converged
347	nature of the simulations, the inadequacy of MM-PBSA in describing binding energies in such
348	highly dynamic systems, as well as the presence of 1M NMe $_4$ Cl in the experimental setup; such
349	additional ions are likely to influence the system in a way that is not accounted for in the present
350	theoretical model. The DBSCAN algorithm furthermore reveals that that 84 \pm 3% of the trajectory
351	for the peptide $-H_2PO_4^{1-}$ simulations is filtered off as noise, indicating significant less stable
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structures for this system compared to peptide $-HPO_4^{2-}$. Looking at the hierarchical clusters for the peptide $-H_2PO_4^{1-}$ simulations, many of them represent states in which the anion is not bound 353 (see supplementary information, Fig. S9). Altogether, simulations qualitatively show that there is 354 a clear difference between how $H_2PO_4^{1-}$ and HPO_4^{2-} are bound by the peptide, which is consistent 355 356 with the experimental observations.

357 High-resolution simulations such as the ones presented in this study are very difficult to 358 interpret, since in addition to their inherent approximations in the form of choice of force field 359 parameterization etc, their complexity necessitates the use of enhanced sampling techniques in 360 order to reach convergence of the molecular ensembles, which in turn bias the obtained results. 361 Despite these limitations, such simulations do provide insight into the dynamics at the molecular 362 scale that can otherwise be difficult to obtain experimentally. Using accelerated molecular 363 dynamics, which implicitly conserves the overall energy landscape of the system, we are able to 364 obtain fully-converged peptide-only ensembles, and close-to-converged peptide-anion ensembles, 365 which can then be reweighted to the canonical ensembles. The expected intrinsically disordered 366 conformation of the peptide is confirmed from the simulations alongside with a transiently semi-367 stable nest structure, and it is shown that this conformational ensemble of structures is stabilized upon HPO_4^{2-} binding, which is in accordance with expectations and theories in the literature: 368 however, albeit there is a clear tendency for the peptide to bind the HPO_4^{2-} anion using a P-loop 369 nest structure, slightly over half of the structures in the ensemble bind, or simply interact, with 370 371 the anion in more loosely defined conformations. As such the binding process should not be 372 considered in terms of the anion being tightly bound by the peptide in a single conformation, such 373 as is the case for many conventional protein-ligand systems; rather it is a much more dynamic

binding effect with multiple structured states that can rapidly interchange and either bind, orrelease the anion.

376 It is important to remark that simulations were limited to the zwitterionic peptide with a protonated lysine residue, in the absence of any other ions such as Na⁺ or Mg²⁺ cations. The 377 378 influence of such additional species in the simulation is not immediately clear, as they may both 379 work to facilitate binding as is often observed in nature¹³, or to disturb the binding energetics of 380 the system. Bianchi et al. who synthesized the SGAGKT peptide performed their experimental 381 studies in NMe₄Cl solutions²⁵, indicating that in this solution the peptide is capable of binding the 382 phosphate anion. It is however not apparent how the presence of other species may influence the 383 enthalpy and entropy contributions to the binding affinity.

384 Despite the complicated binding mechanism and model approximations (protonation states, absence of counter ions, choice of force field, neglect of potential cooperative binding etc.), 385 386 the theoretical model used here found that the peptide is capable of distinguishing between HPO_4^{2-} and $\mathrm{H_2PO}_4^{1-}$, which is consistent with experimental results and shows that despite the 387 388 presence of only 6 amino acid residues, the peptide has very specific binding properties. The 389 nature of the SGAGKT peptide in terms of binding phosphate anions, i.e. its reversible binding 390 effect and specificity, makes it very interesting for development of new technologies for P 391 recovery, where a too strong binding may be counter-productive when it comes to the recovery 392 process. In such applications, a dynamic/reversible binding mechanism such as the one observed 393 for the peptide may be advantageous in terms of a subsequent recovery step.

394

Appendix A: Sampling Considerations

A key drawback of the classical MD approach is the assumption that the electrostatic
properties of molecules can be represented using point charges at the nuclear sites.⁵⁵ In this

respect, QM provides a more rigorous treatment of the quantum chemical nature of the system at
the price of a higher computational cost. For the system investigated in this report, we use QM
specifically to describe the negatively charged phosphate anion, where the electronic structure is
expected to be highly polarized, something which is not accounted for in the classical MD
approach. For more thorough information about the benefits and limitations of the QM/MM
approach in Amber14, the reader is referred reviews on the subject.⁵⁶

403 One of the key challenges in MD is to obtain "adequate" sampling of the conformational 404 space of the system, such that all-important conformational states are sampled close to their 405 Boltzmann-weighted ones. From such well-converged ensembles, one can calculate various 406 thermodynamic properties, and thereby validate the simulation against experimental data. Even 407 with recent advances in computing power, which have made microsecond and even millisecond 408 time scale available to certain researchers,^{57–59} it can however still be difficult to obtain well-409 converged ensembles of biological molecules using MD.^{45,60} The issue at hand is that the systems 410 of interest in chemistry, physics and biology are characterized by the presence of a number of 411 metastable states, which are separated by large barriers in the energy landscape, meaning that the 412 system is easily trapped in a local minimum during a MD simulation. When two or more biomolecules are present, such as is the case in binding events between a IDP and its ligand, the 413 414 situation is often complicated even further and generally equilibrium simulations of coupled 415 folding and binding events at atomistic resolution are considered out-of-reach for the average 416 researcher⁶¹, and instead coarse-grained representations of the systems are used.⁶²

417 In the case of atomistic simulations, various techniques to improve sampling have been
418 explored, e.g. self-guided Langevin dynamics (SGLD)⁶³, accelerated MD (aMD)⁶⁴, and different
419 variations of replica exchange MD (REMD).⁶⁵⁻⁶⁷ The different enhanced sampling techniques all

420 serve to increase sampling, but each also has its own set of disadvantages; e.g. REMD in general 421 requires running N non-interacting replicas of the system, which may be prohibitive, temperature 422 REMD (T-REMD) cannot guarantee convergence since not all barriers in a system are necessarily 423 temperature-dependent⁶⁸, reservoir REMD (R-REMD) is dependent on knowledge contained in a 424 pre-generated reservoir of structures⁶⁰, and in SGLD, which accelerates low-frequency motion in 425 the system, the ensemble has to be reweighted afterwards to obtain the canonical ensemble.⁶³ In 426 aMD a bias potential is introduced into the conventional MD (cMD) simulation which in practice 427 lowers the height of local energy barriers, such that the sampling can continue faster; it inherently 428 represents an increased sampling method where only a single copy of the system is simulated, 429 and it does not require any previous information about the energy landscape or conformation 430 space of the system.⁶⁴ The aMD modification is defined as: 431

432 **Equation 1**

433

434

435 **Equation 2**

436

437

$$\Delta V(r) = \frac{(Ep - V(r))^2}{(\alpha P + Ep - V(r))} + \frac{(Ed - Vd(r))^2}{(\alpha D + Ed - Vd(r))}$$

 $V(r)^* = V(r) + \Delta V(r)$

438 where V(r) is the traditional MD potential, $V(r)^*$ is the modified potential, Vd(r) is a torsion 439 potential, $\Delta V(r)$ is the applied bias, *Ed* and *Ep* are the average dihedral and potential energies, and 440 αP and αD are factors for determining the strength of the applied boost (i.e. high values reduce 441 the boost). This potential is proportionally bigger for deep regions in the energy landscape, and 442 smaller for high-energy regions, thus conserving the shape of the landscape such that minima are 443 still minima, and vice versa for barriers. This means that in theory the original canonical ensemble 444 can be recovered exactly by reweighting the distribution.⁶⁴ In practice reweighting of biased 445 ensembles can however be challenging due to statistical errors^{69,70}, and several algorithms for the 446 task have been proposed, see ref(³⁷). Previous studies have demonstrated how 500 ns aMD 447 simulations could successfully be used to recover the correct canonical ensembles when 448 compared to millisecond MD simulations and experimental data³⁶, truly highlighting the power of 449 aMD to obtain converged ensembles on a scale otherwise only available to a limited number of 450 researchers.



FIGURE 1: Results from peptide-only simulations in explicit water showing (a) KLD of the
first three PCA modes and (b) Frequency of RMSd values of frames in the trajectory
compared to common reference structure (the fully extended peptide).





FIGURE 3: KLD of four independent cMD (a) and aMD (b) peptide-HPO₄²⁻ simuations (1-4)
performed in explicit water. For each simulation the KLD is calculated against all the
other simulations.



FIGURE 4: PCA projections for the two first (largest) modes of a 1 μs cMD peptide-only
simulation. Free energy profiles (a), hierarchical clusters (b) and DBSCAN clusters (c).





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488	
489	Abbreviations
490	aMD, Accelerated Molecular Dynamics
491	cMD, Conventional Molecular Dynamics
492	EBPR, Enhanced Biological Phosphorus Removal
493	IDP, Intrinsically Disordered Protein
494	KLD, Kullback-Leibler Divergence
495	MD, Molecular Dynamics
496	MM-PBSA, Molecular Mechanics Poisson Boltzmann Surface Area
497	PCA, Principal Component Analysis
498	QM, Quantum Mechanics
499	REMD, Replica Exchange Molecular Dynamics
500	RMSd, Root Mean Square Deviation
501	SGLD, Self-Guided Langevin Dynamics
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