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Hybrid excitations due to crystal field, spin-orbit coupling, and spin waves in LiFePO₄Yuen Yiu,¹ Manh Duc Le,² Rasmus Toft-Petersen,³ Georg Ehlers,⁴ Robert J. McQueeney,¹ and David Vaknin¹¹*DMSE, Ames Laboratory and Department of Physics and Astronomy, Iowa State University, Ames, Iowa, USA*²*ISIS Neutron and Muon Source, Rutherford Appleton Laboratory, Didcot OX11 0QX, United Kingdom*³*Helmholtz-Zentrum Berlin für Materialien und Energie, Berlin, Germany*⁴*Quantum Condensed Matter Division, Oak Ridge National Laboratory, Oak Ridge, Tennessee, USA*

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We report on the spin waves and crystal field excitations in single crystal LiFePO₄ by inelastic neutron scattering over a wide range of temperatures, below and above the antiferromagnetic transition of this system. In particular, we find extra excitations below $T_N = 50$ K that are nearly dispersionless and are most intense around magnetic zone centers. We show that these excitations correspond to transitions between thermally occupied excited states of Fe²⁺ due to splitting of the $S = 2$ levels that arise from the crystal field and spin-orbit interactions. These excitations are further amplified by the highly distorted nature of the oxygen octahedron surrounding the iron atoms. Above T_N , magnetic fluctuations are observed up to at least 720 K, with an additional inelastic excitation around 4 meV, which we attribute to single-ion effects, as its intensity weakens slightly at 720 K compared to 100 K, which is consistent with the calculated cross sections using a single-ion model. Our theoretical analysis, using the MF-RPA model, provides both detailed spectra of the Fe d shell and estimates of the average ordered magnetic moment and T_N . By applying the MF-RPA model to a number of existing spin-wave results from other LiMPO₄ ($M = \text{Mn, Co, and Ni}$), we are able to obtain reasonable predictions for the moment sizes and transition temperatures.

DOI: [10.1103/PhysRevB.95.104409](https://doi.org/10.1103/PhysRevB.95.104409)**I. INTRODUCTION**

Various members of the lithium-orthophosphates have gained renewed attention in the last decade as candidates for electrodes in lithium-based rechargeable batteries [1–4] by virtue of their high Li-ion conductivity through channels that are present in their olivine crystal structure [1,5,6]. However, although most research efforts have recently been focused on their electrochemical properties, they have long been known to exhibit intriguing magnetic properties. In particular, the transition-metal-based lithium-orthophosphates display a strong magnetoelectric (ME) effect, where an applied magnetic field induces an electric polarization and vice versa, an applied electric field induces a magnetization. Naturally the ME effect is invoked by the coupling among orbital, magnetic, and electrostatic degrees of freedom that have been at the forefront of recent research in condensed matter physics. Prominent examples of such coupling have been found in the iron- and copper-based unconventional superconductors [7,8], the giant magnetoresistance in Mn-based oxides [9,10], or the magnetoelectric effect in transition metal oxides [11,12]. While the physical mechanisms linking these degrees of freedom may be unclear in general, for many magnetoelectric materials it is accepted that the spin-orbit coupling (SOC) drives the coupling between the magnetic and structural or electric order parameters [13]. The SOC can also lead to higher order asymmetric exchange terms such as the Dzyaloshinskii-Moriya interaction and can lift the degeneracy of crystal field levels. In the case of the lithium-orthophosphates, it has been observed that the relative strength of the ME effect correlates with the effective total orbital moment with LiCoPO₄ ($L = 3$) and LiMnPO₄ ($L = 0$) displaying the largest and smallest ME coefficients [14–17]. Here we report on the magnetic excitations of LiFePO₄ and expand on recent elastic and inelastic neutron studies of the

lithium-orthophosphates [18–20]. Similar to other lithium-orthophosphates, LiFePO₄ possesses an intricate magnetic structure, where the Fe²⁺ moments ($S = 2; L = 2$) order antiferromagnetically at $T_N = 50$ K with moments pointing mainly along the b direction [21,22]. However, subsequent studies have revealed a zero field spin canting along a and c , which are both forbidden by $Pnma$ symmetry, hinting that the crystal structure symmetry might be lower than $Pnma$ below T_N [23]. The observed spin canting implies the presence of Dzyaloshinsky-Moriya (DM) interactions, which can be linked to the ME response. The local symmetry of the magnetically ordered Fe sublattice may also be reflected by the crystal field level structure of Fe²⁺ [24].

Several inelastic neutron scattering (INS) efforts have measured the spin-wave spectrum in LiFePO₄ in restricted regions of the Brillouin zone [23,25]. The most comprehensive model for LiFePO₄ deduced from these measurements includes five exchange interaction terms (one in-plane nearest neighbor, two in-plane next-nearest neighbors, and two out-of-plane interactions), and two single-ion anisotropy terms (along a and c). In this study we complete the INS picture for spin waves measured along all directions a , b , and c and compare our results with the existing Hamiltonian. We also report on new low-energy excitations found below the spin-waves excitations, which persist from below T_N up to 720 K. We argue that such excitations are due to a single-ion splitting of the $S = 2$ manifold from the crystal field, spin-orbit, and ordered moment exchange field. Modifications of the existing spin Hamiltonian model to include these hybrid interactions accounts for the new excitations.

II. EXPERIMENTAL DETAILS

For the inelastic neutron scattering experiment, a single crystalline sample of LiFePO₄ was used. The crystal was

selected from a batch of single crystals synthesized using the standard flux growth method, using the same recipe prescribed in Ref. [23]. The high quality single crystal weighs approximately 200 mg, and its structure and stoichiometry were confirmed by laboratory x ray and by single crystal neutron diffraction [23]. Inelastic neutron scattering (INS) data were collected at the Cold Neutron Chopper Spectrometer (CNCS) [26] of the Spallation Neutron Source, Oak Ridge National Laboratory. The sample was aligned with the bc plane horizontal with some detector coverage along the a (vertical) direction. The incident neutron energy was set at $E_i = 12$ meV for the optimal resolution and flux for the (\mathbf{Q}, ω) region of relevant interest. INS data were collected at three separate temperatures $T = 35, 100,$ and 720 K.

III. RESULTS AND DISCUSSION

Figures 2(a)–2(c) show contour plots of the INS data collected at $T = 35$ K along the $(H10)$, $(0K0)$, and $(00L)$ reciprocal space directions, with an incident neutron energy of $E_i = 12$ meV and integrated over a range of $|Q_\perp|$ of ± 0.25 reciprocal lattice units. Along $(0K0)$ two spin-wave branches are clearly visible, as expected by the known antiferromagnetic structure, which contains spins precessing perpendicular to the moment direction (along b) [23]. One branch where the two oppositely aligned spins precess in-phase, and one branch where the two precess out-of-phase. Also shown in Fig. 2 are dotted lines obtained from linear spin-wave calculations using the existing spin Hamiltonian described below [23]:

$$\mathcal{H} = \frac{1}{2} \sum_{i,j} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j + \mathcal{H}_{\text{SIA}}. \quad (1)$$

The Hamiltonian considers five exchange interaction terms, among them are one nearest neighbor J_{bc} , two next-nearest neighbors J_b and J_c , and two out-of-plane interactions J_{ab} and J_{ac} as shown in Fig. 1. Previous reports based on single crystal data found magnetic anisotropy along a and c [21,25], and as a result the Hamiltonian requires the inclusion of single-ion

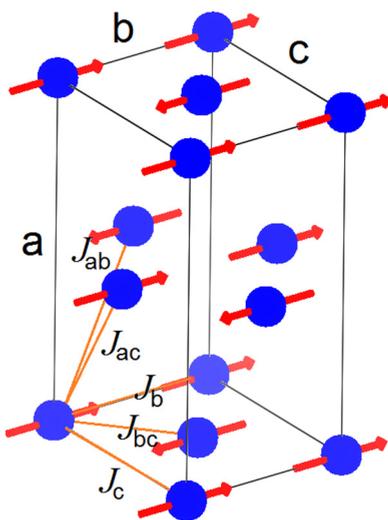


FIG. 1. The magnetic unit cell, spin structure, and the exchange J_{bc} , J_b , J_c , J_{ab} , and J_{ac} , as listed in Table I.

TABLE I. Exchange interactions J_{ij} and single ion anisotropy D_a and D_c (in meV) used in calculating the spin waves shown in Fig. 2. H_{mf} is calculated from the J_{ij} 's in the mean-field approximation. Fe-Fe distances obtained from the structure given in Ref. [23] are given in column 4 and column 5 indicates whether the interaction is mediated by a corner- or edge-shared PO_4 tetrahedron (see text, the FeO_6 octahedra connected by J_{bc} are corner-shared).

	Figs. 2(a)–2(c) Ref. [23]	Figs. 2(d)–2(f) This study	Fe-Fe distance (Å)	Via
J_{bc}	0.77 (2)	0.46 (2)	3.871	
J_b	0.30 (2)	0.09 (1)	6.011	corner
J_c	0.14 (2)	0.01 (1)	4.695	edge
J_{ab}	0.14 (2)	0.09 (1)	6.563	corner
J_{ac}	0.05 (1)	0.01 (1)	5.583	edge
D_a	0.62 (1)	0.86 (2)		
D_c	1.56 (4)	2.23 (2)		
H_{mf}	4.84	3.69		
T_N (K)	73	62		

anisotropy (SIA) terms D_a and D_c , allowing for an anisotropic hard plane while the easy axis b direction is set by $D_b = 0$. For the linear spin-wave calculation shown here, the J and D values from previously published inelastic single crystal data of the same crystal are used [23]. These values are listed in Table I. Figure 1 shows the magnetic unit cell, spin structure, and the exchange couplings used for spin dynamics analysis in this study and Ref. [23].

A. Zeeman splitting

As illustrated in Figs. 2(a)–2(c), the linear spin-wave calculations (white dotted lines) track the measured magnon dispersion closely, however it does not account for the extra excitations visible near 4.5 meV indicated by the red arrows. These extra excitations are nearly dispersionless in energy and centered around the magnetic zone centers. We argue that these extra excitations arise from transitions from a thermally populated excited state of the spin $S = 2$ multiplet that are not considered by spin-wave theory, which is a $T = 0$ theory and maps the spin ground state to a vacuum state and transitions from (to) this state to (from) the n th excited state to creation (annihilation) of n magnons. The 4.5 meV excitation corresponds to a transition between two excited states, $n = 1$ and $n = 2$, as illustrated schematically in Fig. 3. We thus use the mean-field random-phase approximation (MF-RPA) [27] to calculate the higher temperature magnetic spectrum.

Figure 3 shows schematically how the different single-ion interactions splits the d -electron energy levels. The largest energy splitting, of the order of an electron volt, is from the crystal field, which only acts on the orbital angular momentum, leaving the spin states degenerate. In the lithium-orthophosphates, the Fe^{2+} ions are located at a low (monoclinic C_s) symmetry site, so the crystal field splitting lifts all orbital degeneracy resulting in five orbital singlets, which each have a fivefold spin degeneracy. The on-site spin-orbit interaction is much weaker than the crystal field interaction in transition metals and only splits the spin states by a few meV. Finally, in the ordered phase, the ordered moments generate an internal

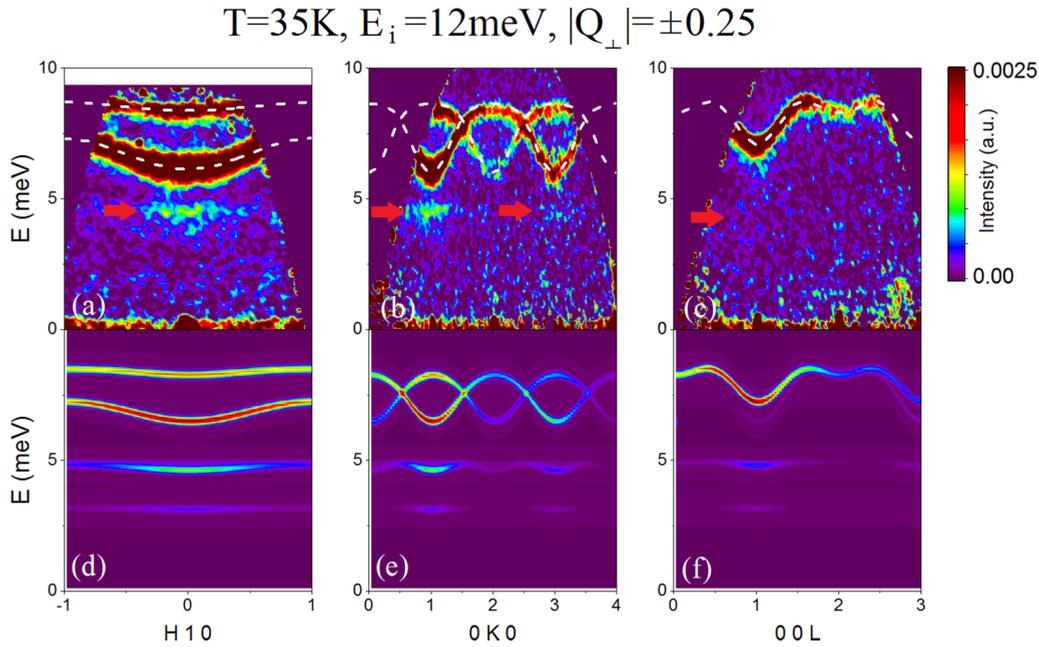


FIG. 2. (a)–(c) Contour plots of energy transfer from the inelastic neutron scattering (INS) data collected at $T = 35$ K along $(H10)$, $(0K0)$, and $(00L)$. The dashed lines are calculated linear spin-wave dispersions based on the model described in the text. The red arrows indicate extra excitations visible around 4.5 meV that corresponds to Zeeman splitting levels by internal mean field induced by the ordered moments. (d)–(f) Virtual INS data calculated based on the same model using mean-field random-phase approximation. As can be seen the simulation correctly predicts the *hybrid* extra excitations near 4.5 meV in addition to an extra less intense excitation near 3 meV, both originating from *internal-Zeeman* splitting.

magnetic field which further Zeeman splits the spin energy levels.

The effects of the spin-orbit and crystal field interactions on the $S = 2$ levels can be parametrized by the single-ion anisotropy parameters D_a and D_c , while the Heisenberg term leads to a Zeeman-like interaction, in the mean-field (MF) approximation. Thus we can rewrite Eq. (1) in the MF

approximation as an effective single-ion Hamiltonian:

$$\mathcal{H}_{\text{mf}}^{(1)} = \mathcal{H}_{\text{SIA}} + \mathcal{H}_{\text{Zeeman}}, \quad (2)$$

where, after choosing the moment direction as the quantization axis, that is $z||b$,

$$\mathcal{H}_{\text{SIA}} = D_a \hat{S}_x^2 + D_c \hat{S}_y^2, \quad (3)$$

$$\mathcal{H}_{\text{Zeeman}} = -H_{\text{mf}} \hat{S}_z, \quad (4)$$

where D_a , D_c , and H_{mf} (which depends on the J_{ij} parameters) are given in Table I. Diagonalizing this Hamiltonian in the $|S_z\rangle$ basis with the Zeeman term results in the level scheme shown in Table II for the ordered (AFM) phase, whereas setting $H_{\text{mf}} = 0$ gives the level scheme shown for the paramagnetic phase. Furthermore, inspection of the results of diagonalizing the Hamiltonian with different values of D_a , D_c , and H_{mf} shows that when $H_{\text{mf}} > (D_a + D_c)$, the difference in energy between the $n = 1$ and $n = 2$ levels is $\Delta_{12} = H_{\text{mf}} + (D_a + D_c)/2$.

The parameters given in Table I are determined by fitting the measured data at 35 K using the MF-RPA as implemented in the program McPhase [28–30] within the data analysis environment provided by the program Horace [31].

In order to find starting parameters for the fit, we generate 10^5 random sets of exchange J_{ij} and single-ion anisotropy D_α parameters and then use the previously reported 2 K data and linear spin-wave model [23] to filter out parameter sets which do not reproduce the low temperature dispersion. This procedure produces several sets of parameters which differ from the published set by having smaller J_{ij} but larger D_α parameters, which although having slightly higher χ^2 values

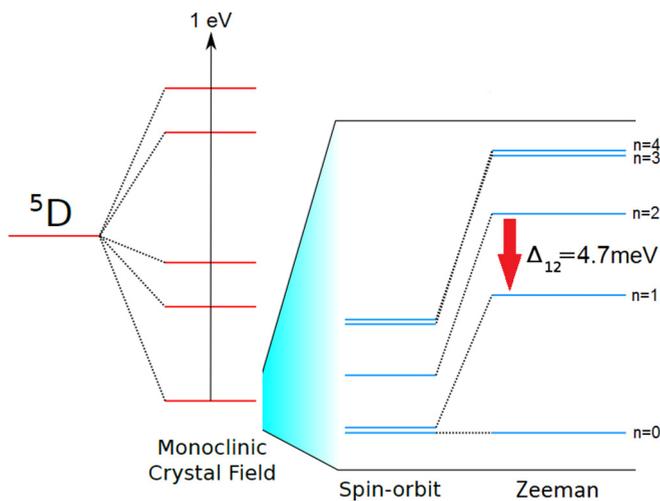


FIG. 3. Multielectron states arising from the crystal field splitting, each of these orbital singlets has a fivefold spin degeneracy. The ground state multiplet is further split as indicated by the blue lines, either by spin-orbit coupling or internal magnetic field when the system is magnetically ordered.

TABLE II. Calculated level scheme due to the crystal field and spin-orbit interactions, parametrized by the single-ion parameters $D_a = 0.86$, $D_c = 2.23$ meV, in the paramagnetic phase and in the magnetically ordered phase with an additional Zeeman splitting term parametrized by $H_{\text{mf}} = 3.69$ meV. The calculated wave functions of each state in the $|S_z\rangle$ basis are listed in the last column.

	Energy (meV)	Calculated wave function
Paramagnetic phase		
$n = 0$	0	$0.67 (S_z = -2\rangle + S_z = 2\rangle) + 0.32 S_z = 0\rangle$
1	0.81	$1/\sqrt{2} (S_z = -2\rangle - S_z = 2\rangle)$
2	3.39	$1/\sqrt{2} (S_z = -1\rangle + S_z = 1\rangle)$
3	7.49	$1/\sqrt{2} (S_z = -1\rangle - S_z = 1\rangle)$
4	7.79	$-0.23 (S_z = -2\rangle + S_z = 2\rangle) + 0.95 S_z = 0\rangle$
Ordered phase		
$n = 0$	0	$0.99 S_z = 2\rangle + 0.12 S_z = 0\rangle$
1	8.00	$0.97 S_z = 1\rangle + 0.25 S_z = -1\rangle$
2	12.73	$0.80 S_z = 0\rangle + 0.60 S_z = -2\rangle$
3	16.21	$0.80 S_z = -2\rangle + 0.60 S_z = 0\rangle$
4	16.45	$0.97 S_z = -1\rangle + 0.25 S_z = 1\rangle$

still fit the 2 K data well. This is because the calculated spin-wave bandwidth and energy gap are governed by both the J_{ij} and D_α parameters in a complex fashion, so that the same bandwidth and gap can result from smaller J_{ij} and larger D_α parameters. However, as H_{mf} is determined by the exchange parameters J_{ij} , and has a larger effect on the energy $\Delta_{12} = E_2 - E_1$ of the excited state transition, weaker J_{ij} parameters fit the 35 K measurements better, as the H_{mf} from the parameters of Ref. [23] overestimates the energy of the excited state mode.

Furthermore, the MF-RPA predicts the physical properties better, since the calculated transition temperature in the mean-field approximation is $T_N^{\text{mf}} = 73$ K for the parameters of Ref. [23] compared to $T_N^{\text{mf}} = 62$ K for the set obtained from the fit of the neutron spectrum at 35 K, as presented in Figs. 2(d)–2(f).

The spin waves, which correspond to the $n = 0$ to $n = 1$ transitions as listed in Table II, are split into two modes by single-ion anisotropy, with a total cross section of 361 mb/sr/Fe and approximately 2/3 the weight in the lower energy mode at the zone center. Our calculations predict the excited state transition from $n = 1$ to $n = 2$ to have a cross section about 10% of the spin waves, which is close to the experimentally determined ratio of the 4.5 meV peak area to the sum of the 6 and 8.5 meV peak areas of 9.5%. The fourth mode, expected to be around 3.7 meV, corresponds to an excited state transition from the $n = 2$ to the $n = 4$ level, only has a calculated cross section of 7 mb/sr/Fe²⁺ compared to 36 mb/sr/Fe²⁺ of the 4.5 meV mode, and is probably too weak to be observed experimentally.

The newly fitted exchange parameters indicate that the nearest-neighbor superexchange interaction J_{bc} between Fe²⁺ ions via a single oxygen ligand as more dominant than previously expected, with $J_{bc}/J_b \approx 5$ (this study) rather than $J_{bc}/J_b \approx 2.5$ (previous study [23]). Furthermore, J_b and J_{ab} have similar magnitudes and are both larger than J_c and J_{ac} , but connect Fe²⁺ ions which are further apart (see Table I). This

may be because while the superexchange interaction in J_b and J_{ab} follows a relatively direct path through a corner-shared PO₄ tetrahedron, the J_c and J_{ac} interactions are mediated by a more zigzag path through an edge-shared tetrahedron. However, we should note that while the new parameters may be in better accord with physical intuition than those obtained in Ref. [23], neither parameter sets, both deduced under the approximations of mean field and linear spin-wave theory, may truly reflect the actual exchange interactions.

One striking consequence of the newly fitted exchange parameters is to indicate that LiFePO₄ is more unfrustrated than previously thought—and hence, due to the dominance of the nearest-neighbor interaction—further away from stabilizing an incommensurate structure such as what is observed in LiNiPO₄. On the other hand, the enhancement of the single-ion anisotropy, which is primarily an orbital effect, suggests a stronger influence from spin-orbit coupling than previously considered, which indirectly supports the model of magnetoelectric coupling in orthophosphates arises from Dzyaloshinskii-Moriya interactions.

However, a potential shortfall of modeling the spin-orbit and crystal field interactions using the effective SIA parameters D_a and D_c is that it ignores higher order and odd-component crystal field terms which are permitted here because of the low symmetry of the crystallographic site occupied by the Fe²⁺ ions. Using the full crystal field Hamiltonian

$$\mathcal{H}_{\text{CF}}^i = \lambda \mathbf{L}_i \cdot \mathbf{S}_i + \sum_{k=2,4} \sum_{q=-k}^k B_k^q O_k^q \quad (5)$$

in place of \mathcal{H}_{SIA} requires many more parameters, including the on-site spin-orbit coupling λ and the crystal field parameters B_k^q . The O_k^q are the Stevens crystal field operators, which are Hermitian higher order products of angular momentum operators. We choose to restrict $\lambda = 12.75$ meV to the free-ion value determined by optical spectroscopy and atomic calculations [32,33], and use the point-charge model to determine the B_k^q parameters, including charges within a cutoff range of 3.3 Å from the Fe²⁺ ions. The point charge model has known shortcomings, such as not accounting for charge transfer or bonding effects, but allows us to reduce the number of parameters to three: the effective charges on each ligand atomic species. Starting parameters are obtained by requiring the point charges to approximately reproduce the energy level scheme in Table II. Fitting the 35 K inelastic data set with this effective charge model, we obtained $q_O = -1.87(3) |e|$ for the oxygen ligands, $q_P = 0.58(3) |e|$ for the phosphorus, and $q_{\text{Li}} = 0.04(2) |e|$ for the lithium.

q_O , q_P , and q_{Li} are values of the effective ionic charges of the oxygen, phosphorus, and lithium ions surrounding the magnetic Fe²⁺ ions in the point charge model. They can be considered as parametrization of the relative effects of each neighboring ligand on the crystal field affecting the Fe²⁺ spins. Thus, the model implies that the mobile Li ions contribute very little to the anisotropy of the iron spins, as expected, while the largest effect is due to the distorted oxygen octahedron, and a smaller contribution from the phosphorus. The calculations does give the b direction as the easy direction, but overestimates the ordered moment

TABLE III. Calculated and reported moment directions and sizes for LiMPO_4 . Calculations for Co [34], Ni [18], and Mn [20] are based on reported values of exchange parameters. Note that a small amount of canting present in LiFePO_4 has been omitted here [23].

M	Calc. moment (a, b, c) (in μ_B)	Expt. moment (a, b, c) (in μ_B)
Fe	(0, 4.67, 0)	(0, 4.09, 0) [23,35]
Co	(0, 3.87, 0)	(0, 3.35, 0) [36]
Ni	(0.41, 0, 2.80)	(0.3, 0, 2.2) [18]
Mn	(5.00, 0, 0)	(4.29, 0, 0) [20,37]

$\mu_{\text{calc}} = 4.67 \mu_B$ compared to a measured value of $4.09(4) \mu_B$ [23].

More importantly, the calculated inelastic neutron spectrum is virtually identical to that shown in Figs. 2(d)–2(f) using the SIA parameters D_a and D_c . Thus, the higher order crystal field terms appear to have little effect on the dispersion or intensities of the spin waves or excited state transition. This can be understood by reference to Table II, where we see that the ground state ($n = 0$) and the first excited state ($n = 1$) are both nearly pure states, that is the $n = 0$ state is 99% $|S_z = +2\rangle$ and the $n = 1$ state is 98% $|S_z = +1\rangle$, so the wave functions and hence the transition matrix elements which determine dispersion and scattering intensity are dominated by the ordered phase Zeeman field.

Nonetheless, the point charge model does show us that the b easy-axis direction and anisotropic hard plane can be explained by the distorted geometry of the oxygen octahedron surrounding the Fe^{2+} spins. Indeed, applying the same point charge model as fitted to the inelastic neutron scattering data from LiFePO_4 to other lithium-orthophosphates satisfactorily reproduces the measured ordered moment directions in LiMPO_4 , although the magnitude of the ordered moments are overestimated by MF-RPA. Table III provides a list of magnetic moment sizes and orientations calculated using the point charge model, with comparison to the reported values for LiMPO_4 ($M = \text{Fe, Co, Ni, and Mn}$).

B. Spin-orbit splitting

Figure 4 shows the energy responses of INS intensity around (010) and (001) at $T = 35$ and 100 K. In order to correctly analyze the energy response, the negative energy transfer portion (i.e., neutron energy gain) of the data have been processed using the principle of detailed balance [38]. The spectrum at $T = 35$ K, which is below T_N and in the spin ordered phase, shows well defined peaks that correspond to the spin-wave branches. The red arrows indicate the extra excitations observed near 4.5 meV as shown above. Above $T_N = 50$ K the system becomes paramagnetic and both the magnon dispersions and the hybrid 4.5 meV excitation disappear.

Figure 5(a) shows a closer look of the INS energy responses at higher temperatures 100, 296, and 720 K. At these temperatures the spectra are relatively broad in energy, which includes a Lorentzian component centering at 0 meV and a Gaussian component centering near 4 meV, all represented as dashed lines in Fig. 5(a). The Lorentzian response is expected

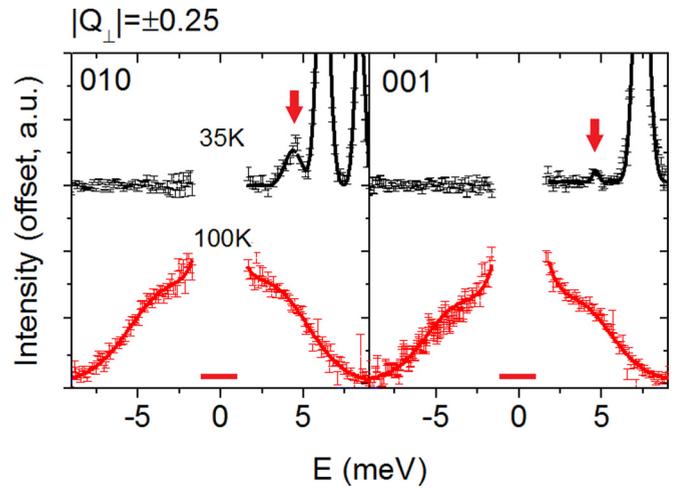


FIG. 4. Energy transfer at (010) and (001) for $T = 35$ and 100 K. The integrated Q range is ± 0.25 r.l.u. along each direction. The red arrows indicates the extra excitation observed near 4 meV along both directions. The thick red bar represents approximately the instrumental resolution width. Both the 35 and 100 K data have both been normalized by incident monitor counts.

of magnetic fluctuations that are quasielastic in nature and short lived in time, however, there is little change in intensity and width over a temperature range many times T_N .

Broad excitations are detected around 3.4(4) meV at 100 K and 4.2(7) meV at 720 K, determined by the fitted Gaussian curves as represented by the dashed Gaussian lines in Fig. 5(a). Since the internal fields generated by the ordered moments should be absent at these temperatures, these excitations cannot

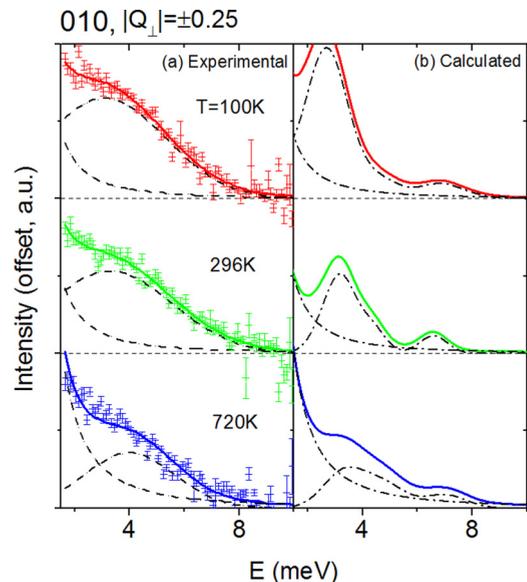


FIG. 5. (a) Measured energy transfer at (010) for $T = 100, 296,$ and 720 K. The dashed lines show the fitted Lorentzian centered at $E = 0$ and a Gaussian centered near 4 meV. The solid colored lines show the sum of the fitted Lorentzian and Gaussian curves. (b) Calculated energy transfer at (010) for the same temperatures. (Note: The Lorentzian component centered on zero energy here is not calculated. Instead the fitted peak from the data is used.)

be the same as that discussed above, seen at 35 K. However, as shown in Table II, in the paramagnetic phase the spin-orbit and crystal field interactions combined still splits the $S = 2$ levels, for instance the energy for a $n = 2$ to 0 transition is 3.39 meV, which may be what is observed at 100 K. At 720 K we should expect that all the excited states are populated, allowing higher transitions to have greater spectral weight, and shifting the observed peak to a higher energy. However, the data are much broader than the instrumental resolution, and the MF-RPA theory we have used to analyze the low temperature data does not account for thermal broadening of the excitations. Instead we have convoluted the calculation with Gaussian curves with a full width at half maximum of 1.2 meV to obtain the curves in Fig. 5, whereas instrumental resolution at these energy transfers is expected to be less than 0.5 meV. It can be seen that this still does not fully account for the measurements. In addition, the calculations predict that the intensity should fall off much faster with increasing temperature than is observed: the calculated intensity ratio of the peak area at 720 vs 100 K is 0.35, which is half that observed ($I_{720\text{K}}/I_{100\text{K}} \approx 0.7$). Thus, while the energies of the peaks observed at high temperatures may be satisfactorily explained by the MF-RPA theory, their intensity and linewidths require a more sophisticated approach.

IV. SUMMARY

In summary, we present inelastic neutron scattering results in LiFePO₄ that complements a previous spin-wave excitations study. In particular, we find an extra excitation at 4.5 meV at $T = 35\text{ K} < T_N$ that is nearly dispersionless and is

most intense around magnetic zone centers. We show that these excitations correspond to transitions between thermally occupied excited states of Fe²⁺ due to splitting of the $S = 2$ levels that arise from the effects of the crystal field and spin-orbit interactions amplified by the highly distorted nature of the oxygen octahedron surrounding the iron spins. Above T_N the magnetic fluctuations are observed to relatively high temperatures, with little temperature dependence between 100 and 720 K. Additional excitations, broad in energy, are observed around 4 meV that are due to the single-ion splittings caused by the spin-orbit and crystal field interactions. These excitations weaken slightly at 720 K compared to 100 K, consistent with the calculated cross sections from our single-ion model. Our theoretical analysis using the MF-RPA model provides detailed spectra of the d shell in LiFePO₄ and also enables estimates of the average ordered magnetic moment and T_N . Applying it to spin-wave results of other members of the LiMPO₄ ($M = \text{Mn, Co, and Ni}$) compounds provides reasonable ordered moments and transition temperatures showing the approach is robust.

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