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## Prediction of Acid Dissociation Constants of Organic Compounds Using Group Contribution Methods

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#### Abstract

In this paper, group contribution (GC) property models for the estimation of acid dissociation constants ( $K_a$ ) of organic compounds are presented. Three GC models are developed to predict the negative logarithm of the acid dissociation constant  $pK_a$ : a) a linear GC model for amino acids using 180 data-points with average absolute error of 0.23; b) a non-linear GC model for organic compounds using 1622 data-points with average absolute error of 1.18; c) an artificial neural network (ANN) based GC model for the organic compounds with average absolute error of 0.17. For each of the developed model, uncertainty estimates for the predicted  $pK_a$  values are also provided. The model details, regressed parameters and application examples are highlighted.

**Keywords:** Acid Dissociation Constant,  $pK_a$ , Group Contribution Method, Artificial Neural Network, Amino Acids, Organic Compounds

#### **1. Introduction**

The acid dissociation constant ( $K_a$ ) of a compound, which expresses the extent to which the compound in its aqueous solution is dissociated into its ionic form, is sought after by many chemists, biochemists and product formulators. Although experimental measurements would yield the most satisfactory results, it is not always convenient to setup and conduct experiments for  $K_a$  determination. This is because the organic compounds that weakly dissociate lack adequate spectral differences in the dissociated and undissociated forms. Besides, in the cases where a compound is unstable or is insufficiently soluble in water, experimental  $K_a$  determination is impossible (Tong and Wen, 2008).

The currently available  $pK_a$  (negative logarithm of  $K_a$ ) compilations provide values for only a small fraction of known or possible acids and bases (Perrin, Dempsey and Serjeant, 1981). This motivates the development of advanced  $pK_a$  prediction models.

This paper is organized as follows. First, we give a definition on  $pK_a$  and highlight its significance in several research areas (Section 1.1). After a brief introduction of the main existing methods for  $pK_a$  prediction (Section 1.2), we focus on the powerful group contribution (GC) methods and present more details about these methods in Section 2. Three different GC models are then developed to predict  $pK_a$  for amino acids and other classes of organic compounds. The performances of these models are evaluated and compared in Section 3.1. Finally, in Section 3.2, several examples are shown to help the reader in understanding how to apply the developed models for predicting  $pK_a$ .

#### 1.1 Definition and Significance of *pK*<sub>a</sub>

In aqueous solution, acids (generically represented by HA) undergo a protolytic reaction with water. This equilibrium reaction is given as:

$$HA + H_2 0 \leftrightarrow H_3 0^+ + A^- \tag{1}$$

The equilibrium constant (in this case, the acid dissociation constant  $K_a$ ) for the reaction given in Eq. (1) is expressed as Eq. (2), which relates the activity of the dissociated form of the acid ( $a_{A^-}$ ) to the activity of its undissociated form ( $a_{HA}$ )

$$K_a = \frac{\left[a_{H_3O^+}\right]\left[a_{A^-}\right]}{\left[a_{H_2O}\right]\left[a_{HA}\right]}$$

As the  $K_a$  measurements are generally made in dilute aqueous solutions, the concentration of water remains nearly constant and therefore, its activity can be taken as unity. The general expression of  $K_a$  is then derived from Eq. (2), as

$$K_a = \frac{[a_{H3O^+}][a_{A^-}]}{[a_{HA}]}$$
(3)

By taking negative logarithm on both sides of Eq. (3) and rearranging the terms, the relation between the pH of the solution and the  $pK_a$  of HA can be obtained, given as Eq. (5).

$$-\log(K_a) = -\log([a_{H30^+}]) - \log(\frac{[a_A^-]}{[a_{HA}]})$$
(4)

$$=> pK_a = pH + \log\left(\frac{[a_{HA}]}{[a_A^-]}\right) \tag{5}$$

In the special case, when the activity of HA equals that of  $A^-$ ,  $pK_a$  is identical to pH.

 $pK_a$  is very significant in many different areas. For example, during liquid-liquid extraction, when an organic compound is to be separated from an aqueous solution, the undissociated form of the compound usually is more soluble in the organic phase. Hence, the pH of the aqueous phase can be adjusted to its optimum value if the  $pK_a$  of the organic compound is known (Green and Perry, 2008). In preparative chemistry, considering the effects of pH on the properties of reactants as well as the possible intermediates and products, conditions for synthesis are selected by making use of  $pK_a$  (Perrin, Dempsey and Serjeant, 1981).

#### 1.2 Existing Methods for *pK*<sup>*a*</sup> Prediction

Nowadays a large number of experimental  $pK_a$  data are available, thus one can predict  $pK_a$  of new compounds by extrapolating or interpolating the  $pK_a$  of database compounds of the same type. Besides this, theoretical calculations and semi-empirical correlations based on thermodynamics and quantum chemical foundations have also been used for  $pK_a$  prediction in various works (e.g., Jensen, Swain and Olsen, 2017 use isodemic reactions, where the  $pK_a$ is estimated relative to a chemically related reference compound, to make COSMO-based and SMD-based predictions. The  $pK_a$  values of 53 amine groups in 48 druglike compounds are computed.)

#### 1.2.1 Linear Free Energy Relationships (LFER)

The Hammett-Taft equation quantifies the electronic effect of organic functional groups (or substituents) on other groups to which they are attached. This equation is a linear free energy relationship (LFER). It is widely used for  $pK_a$  prediction (Metzler, 2012) and is as shown in Eq. (6).

$$pK_a = pK_a^0 - \rho \sum \sigma_i \tag{6}$$

where  $pK_a^0$  indicates the  $pK_a$  value for unsubstituted reference compounds;  $\sigma_i$  is the substituent constant for the substituent *i*; and  $\rho$  is the proportionality constant for the particular equilibrium dissociation reaction i.e. it is the measure of the sensitivity of the reaction to the presence of electron-withdrawing or electron-donating substituents, for example the  $\rho$  for phenylacetic acids is 0.49, while that for phenols is 2.23. It should be noted that, currently only a limited number of substituent constants are available, which limits the applicability of the LFER method for  $pK_a$  prediction.

#### **1.2.2 Theoretical calculations**

There are several first-principle theory based methods for  $pK_a$  prediction. The Kirkwood-Westheimer equation (Kirkwood and Westheimer, 1938) quantifies  $\Delta pK_a$  for a charged or a dipolar substituent as follows,

$$\Delta p K_a = \frac{e\mu cos\phi}{2.3 \ kTR^2 D_{eff}}$$

(7)

In Eq. (7),  $\phi$  is the angle between the line joining the centre of the ionizing group to the centre of the dipole and the axis of the dipole, *e* is the electronic charge, *k* is the Boltzmann constant, *T* is the temperature in K,  $\mu$  is the dipole moment, *R* is the distance between two charges,  $D_{eff}$  is the effective dielectric constant. The largest limitation of the Kirkwood-Westheimer method is that it is applicable only to ellipsoidal molecules with point charges at their foci only.

 $pK_a$  can also be estimated based on thermodynamic cycles that relate the gas phase to the solution phase, where state-of-the-art quantum chemical techniques coupled with an appropriate solvation model are used (Shields and Seybold, 2013). Jang *et al.* (2001) predicted the  $pK_a$  values for a series of 5-substituted uracil derivatives using density functional theory (DFT) calculations in combination with the Poisson-Boltzmann continuum-solvation model (Im, Beglov and Roux, 1998).

Even though theoretical calculations can yield good results in predicting  $pK_a$ , these methods are not very attractive for some applications due to their high computational cost. For instance, in drug formulation design, the  $pK_a$  of active ingredients (AIs) is a very important property for selecting AIs because the  $pK_a$  value indicates the aqueous solubility of the AI and the ability of the AI to permeate through the gastro-intestinal membrane. In order to

perform a fast AI pre-screening, a quick and reliable  $pK_a$  prediction method is more preferable than an accurate but very computationally expensive one.

#### 1.2.3 Group contribution based methods

The compounds of the same class usually have small differences in their  $pK_a$  values. For example, the  $pK_a$  of 1-aminoheptane is 10.67 at 25 °C, which is just slightly lower than the  $pK_a$  value of 10.70 for ethylamine. In general, the  $pK_a$  of primary amines falls into the range of 10.6 ± 0.2. Also, if the alkyl-chain-substituted amines are compared with cyclic amines, the  $pK_a$  is raised by 0.2 units for one ring and 0.3 units for two rings (Perrin, Dempsey and Serjeant, 1981). By employing analogical methods, one can perform  $pK_a$  estimations. However, in order to accurately predict  $pK_a$  for a certain compound, one needs quite a lot of information about other compounds with similar molecular structures.

As indicated in the three types of prediction methods (see Sections 1.2.1 - 1.2.3), all have certain limitations, which motivates the development of new methods for fast and reliable  $pK_a$  predictions. It is also clear that the  $pK_a$  value or the degree to which a compound dissociates in its aqueous solution depends mostly on the molecular structure of the compound. This inspires us to develop group contribution (GC) based models that are applicable to all different classes of organic compounds.

#### 1.3 pK<sub>a</sub> of Amino acids

Amino acid molecules have at least one acidic group and one basic group. This allows intramolecular acid-base equilibrium reaction resulting in the formation of a dipolar tautomeric ion known as the zwitterion or internal salt (Cheung, 1995). The dissociation of amino acids in aqueous solutions is represented as follows.

$$H_3N^+$$
. R. COOH  $(R^+) + H_2O \rightleftharpoons H_3N^+$ . R. COO<sup>-</sup> $(R^{\pm}) + H_3O^+$ 

where 
$$K_{a1} = \frac{[a_{R^{\pm}}][a_{H_3O^+}]}{[a_{R^+}]}$$

and

$$H_3N^+$$
. R.  $COO^-(R^{\pm}) + H_2O \rightleftharpoons H_2N$ . R.  $COO^-(R^-) + H_3O^+$ 

where 
$$K_{a2} = \frac{[a_{R^-}][a_{H_3O^+}]}{[a_{R^{\pm}}]}$$

From above, we know that an amino acid typically has at least two dissociation constants with the first one corresponding to the case when the COOH group is deprotonated and the second one corresponding to the case when the  $H_3N^+$  group gets deprotonated in aqueous solution. Considering this unique behaviour, amino acids have been considered separately from other organic compounds in this work in the same way as in our previous GC-based property estimation models for amino acids (Jhamb *et al.* 2018).

#### 2. Methods and Tools used for *pK*<sub>a</sub> Model Development

#### **2.1 Experimental Dataset**

In the present study, the first dataset (dataset – 1) comprises experimental  $pK_a$  values of 180 amino acids while the second dataset (dataset – 2) contains  $pK_a$  values of 1622 organic compounds that are not amino acids. The experimentally measured  $pK_a$  values in both datasets are collected from the KT-Consortium database and handbooks containing the dissociation constants of organic compounds (Kortüm, Vogel and Andrussow, 1961; Perrin, 1965). Table 1 provides an overview of the datasets used for developing GC-based  $pK_a$  prediction models. The 180 amino acids in dataset – 1 are grouped according to the amino acid type. For instance, totally 13 amino acids including L-Alanine, N-acetyl-L-Alanine, and N-ethyl-L-Alanine are classified into the 'L-Alanine' group. Similarly, the 1622 organic compounds are also classified into several groups.

(8)

| Dataset – 1                          |                                  | Dataset – 2                           |                                  |  |  |
|--------------------------------------|----------------------------------|---------------------------------------|----------------------------------|--|--|
| Derivatives of following amino acids | Number of<br>data points<br>(ND) | Classes of organic compounds          | Number of<br>data points<br>(ND) |  |  |
| L-Alanine                            | 13                               | Ethers                                | 3                                |  |  |
| β-L-Alanine                          | 1                                | Derivatives of alkanes                | 6                                |  |  |
| L-Arginine                           | 1                                | Amines                                | 253                              |  |  |
| L-Asparagine                         | 3                                | Aromatics                             | 161                              |  |  |
| L-Aspartic acid                      | 2                                | Carboxylic acids                      | 323                              |  |  |
| L-Cysteine                           | 9                                | Sulfonic acids                        | 7                                |  |  |
| L-Glutamine                          | 1                                | Nitriles                              | 9                                |  |  |
| L-Glutamic acid                      | 12                               | Aldehydes                             | 16                               |  |  |
| Glycine                              | 23                               | Amides                                | 61                               |  |  |
| L-Histidine                          | 8                                | Sulfonamides                          | 60                               |  |  |
| L-Isoleucine                         | 2                                | Alcohols and thiols                   | 105                              |  |  |
| L-Leucine                            | 6                                | Ketones                               | 76                               |  |  |
| L-Lysine                             | 2                                | Hydrazines                            | 13                               |  |  |
| L-Methionine                         | 1                                | Heterocyclic [1 ring, 1 heteroatom]   | 80                               |  |  |
| L-Ornithine                          | 2                                | Heterocyclic [1 ring, 2 heteroatoms]  | 109                              |  |  |
| L-Proline                            | 2                                | Heterocyclic [1 ring, 3 heteroatoms]  | 2                                |  |  |
| L-Phenylalanine                      | 10                               | Heterocyclic [1 ring, 4 heteroatoms]  | 1                                |  |  |
| L-Serine                             | 7                                | Heterocyclic [2 rings, 1 heteroatom]  | 31                               |  |  |
| L-Threonine                          | 3                                | Heterocyclic [2 rings, 2 heteroatoms] | 9                                |  |  |
| L-Tyrosine                           | 10                               | Heterocyclic [2 rings, 3 heteroatoms] | 4                                |  |  |
| L-Tryptophan                         | 2                                | Heterocyclic [2 rings, 4 heteroatoms] | 5                                |  |  |
| L-Valine                             | 5                                | Heterocyclic [3 rings, 1 heteroatom]  | 12                               |  |  |
| Aminobenzoic acids                   | 16                               | Heterocyclic [3 rings, 2 heteroatoms] | 3                                |  |  |
| Aminonaphthalene sulfonic acids      | 2                                | Others                                | 273                              |  |  |
| Aminobenzenesulfonic acids           | 3                                |                                       |                                  |  |  |
| Aminosulfonic acids                  | 1                                |                                       |                                  |  |  |
| Aminophosphonic acids                | 4                                |                                       |                                  |  |  |
| Others                               | 29                               |                                       |                                  |  |  |
| Total                                | 180                              | Total                                 | 1622                             |  |  |

### Table 1: Overview of the datasets used for model development

From Section 1.3, it is known that amino acids generally have at least two groups which can dissociate and hence possess at least two  $pK_a$  values correspondingly. Notably, for amino acids with a polar or an electrically charged side chain, there is even a third dissociation constant as well. For example, L-Cysteine has a thiol group (–SH) in its side chain which can also get deprotonated besides the –COOH and –NH<sub>3</sub><sup>+</sup> groups.

For the amino acids included in dataset – 1, only the first dissociation constant has been chosen, i.e., the  $pK_a$  value corresponding to the deprotonation of the –COOH, –SO<sub>3</sub>H, or – PO<sub>3</sub>H<sub>2</sub> group, depending on whether the amino acid is carboxylic, sulphonic, or phosphonic. For amino acid esters where these three groups do not exist, the  $pK_a$  associated with the deprotonation of the –NH<sub>3</sub><sup>+</sup> group has been chosen.

When developing property models, the experimental dataset is often divided into a training set and a validation set. This approach should not be employed for GC models since the validation set is usually formed by randomly selecting the experimental data points. When some data points (or compounds) are selected for validation, some of the functional groups and model parameters may be excluded for model training, which will thereby limit the application domain of the resulting model. On the other hand, when only a proportion of the experimental data are used for parameter regression, large uncertainties of predicted property values could be resulted (Hukkerikar *et al.*, 2012).

#### 2.2 Group Contribution Methods

Several group contribution (GC) methods have been developed for pure-component property predictions, for instance, Joback and Reid (1987), Lyman *et al.* (1990), Marrero and Gani (2001), Hukkerikar *et al.* (2012) etc. In this work, the Marrero and Gani (MG) GC method, also used previously for amino acids (Jhamb *et al.* 2018) and other organic compounds (Hukkerikar *et al.* 2012), has been used.

In the MG GC method, a multilevel scheme is adopted where the property estimation is performed at three levels. The first level has a large number of simple groups that allow for the representation of a wide variety of organic molecules. The second level of estimation involves groups that can capture the proximity effects and can differentiate among isomers. The third level estimation includes groups that provide a further more detailed description of the molecular structures; hence, this level allows estimation of complex heterocyclic and poly-functional acyclic molecules. The MG GC-model has the form (Marrero and Gani, 2001),

$$f(X) = \sum_{i} N_i C_i + w \sum_{j} M_j D_j + z \sum_{k} O_k E_k$$
(10)

Here, the function f(X) is a function of property *X*. This may contain additional adjustable model parameters (universal constants) depending on the property involved. In Eq. (10),  $C_i$  is the contribution of the first-order group of type-*i* that occurs  $N_i$  times.  $D_j$  is the contribution of the second-order group of type-*j* that occurs  $M_j$  times.  $E_k$  is the contribution of the third-order group of type-*k* that has  $O_k$  occurrences in a component. *w* and *z* are weighting factors set to 1 or 0 depending on whether the second and third order groups are used for property prediction or not. Therefore, Eq. (10) is a general model for all the properties and the definition of f(X)is specific for each property *X*.

In this work, the set of groups proposed for the prediction of physical properties of amino acids by Jhamb *et al.* (2018) to account for zwitterionic structures and the amphoteric nature of amino acids has been used. That is, the  $pK_a$  prediction for amino acids in this work makes use of the traditional MG-GC groups along with these newly introduced groups.

#### 2.2.1 Linear GC model

As described by Constantinou and Gani (1994) and later by Marrero and Gani (2001), the selection of an appropriate function f(X) has to achieve additivity in the contributions  $C_i$ ,  $D_i$ ,

and  $E_k$  in order to demonstrate the best possible fit of the experimental data. In addition, the expressions should be able to provide sufficient extrapolating ability and therefore ensure a wide range of applicability.

In this work, a linear property model function was first selected for the prediction of  $pK_a$  of amino acids in dataset – 1 and all the other organic compounds in dataset – 2.

$$pK_a - pK_{a0} = \sum_i N_i C_i + w \sum_j M_j D_j + z \sum_k O_k E_k$$
(11)

In Eq. (11),  $pK_a$  is the negative logarithm of the acid dissociation constant and  $pK_{a0}$  is an adjustable model parameter.  $C_i$ ,  $D_j$ , and  $E_k$  are group contributions to be regressed. Note that both *w* and *z* are set to 1, which means the second- and third-order groups are also considered in model development.

#### 2.2.2 Nonlinear GC model

Besides the above linear GC model, a  $4^{\text{th}}$ -order polynomial GC model was also tested for  $pK_a$  prediction, as shown below.

$$a (pK_a)^4 + b (pK_a)^3 + c (pK_a)^2 + pK_a + pK_{a0} = \sum_i N_i C_i + w \sum_j M_j D_j + z \sum_k O_k E_k$$
(12)

 $pK_a$  is the negative logarithm of the acid dissociation constant; *a*, *b*, *c* and  $pK_{a0}$  are adjustable model parameters;  $C_i$ ,  $D_j$ , and  $E_k$  are group contributions to be regressed. *w* and *z* are set to 1.

#### 2.2.3 Artificial Neural Network GC model

Artificial Neural Network (ANN)-GC method has been widely used to predict physical, thermodynamic, and transport properties, such as vapor-liquid equilibrium data (Petersen, Fredenslund and Rasmussen, 1994), solubility data (Gharagheizi *et al.*, 2011a), flash point (Gharagheizi, Alamdari and Angaji, 2008) and surface tension (Gharagheizi *et al.*, 2011b). In this work, a very popular ANN architecture (Bishop 1995) comprising of a three-layer feed

forward neural network including an input layer, a hidden layer, and an output layer, is employed as shown in Figure 1. The input layer receives molecular structure information, in this work these are the 144 first-order groups present in the molecule, indicated by the input vector p with a size of 144×1. The hidden layer transfers the information received from the input layer and delivers it to the output layer where the  $pK_a$  value is predicted.



Figure 1: Schematic structure of the employed three-layer artificial neural network (the sizes of weight matrices  $W_1$  and  $W_2$  and bias vectors  $b_1$  and  $b_2$  are given in the brackets)

The number of neurons in the hidden layer, also the number of rows in the weight matrix  $W_1$ , is an important adjustable parameter for network training. The selection of this number depends fully on the specific problem being solved. Generally, with too few neurons the network may not be powerful enough for predicting properties. However, with a too large number of neurons, the network tends to perform "over-fitting". In this work, we started to train the ANN with 5 neurons in the hidden layer and gradually increased the number until no significant improvement in the performance of the network (or a desired accuracy) was achieved. By following this procedure, 20 neurons in the hidden layer were finally identified. Therefore, the final three-layer ANN has a 144-20-1 architecture. As illustrated in Figure 1, for a specific compound with a known group composition vector p, the output from the hidden layer  $f_1(a_1)$  is calculated by Eq. (13) and the output from the output layer  $f_2(a_2)$  (i.e., predicted  $pK_a$ ) is determined by Eq. (14).

$$f_1(a_1) = f_1(W_1 \times p + b_1) \tag{13}$$

$$f_2(a_2) = f_2(W_2 \times f_1(a_1) + b_2) \tag{14}$$

A sigmoid transfer function and a linear transfer function were employed in the hidden layer and in the output layer, respectively. The combination of a sigmoid and a linear transfer function has been shown to be very powerful for building three-layer feed forward neural networks. The mathematical formulations of the employed transfer functions are given as follows.

$$f_1(x) = \frac{1}{1 + e^{-x}} \tag{15}$$

$$f_2(x) = x \tag{16}$$

#### 2.3 Parameter Regression and Uncertainty Analysis

The Levenberg–Marquardt optimization algorithm (Levenberg, 1944; Marquardt, 1963) implemented in MATLAB was employed to regress the parameters in the linear and nonlinear GC models. The minimization of the objective function S(P), defined as the sum of squares of the difference between the experimental  $pK_a^{exp}$  and model predicted  $pK_a^{pred}$ , provides the values of unknown parameters  $P^*$ .

$$S(\mathbf{P}) = \sum_{j=1}^{N} (pK_{a_j}^{exp} - pK_{a_j}^{pred})^2$$
(17)

The subscript j indicates the compound and N is the total number of compounds in the dataset.

In the ANN-GC model, there are four fitting parameters, two weight matrices ( $W_1$  and  $W_2$ ) and two bias vectors ( $b_1$  and  $b_2$ ). They were obtained by minimizing an objective function, which in this work is the Mean Square Error (MSE) between the output (predicted  $pK_a$ ) and

the experimental  $pK_a$  for all the compounds in the dataset. This optimization process was also performed by using the Levenberg-Marquardt algorithm, which is available in the neural network toolbox of MATLAB.

$$MSE = S(\mathbf{P})/N$$

After the estimation of model parameters, uncertainty analysis can be performed to quantify the uncertainties in the predicted property values. The methodology discussed in Hukkerikar *et al.* (2012) is employed to estimate confidence interval of the predicted  $pK_a$  at the  $\alpha_t$ significance level.

$$pK_{a_{(1-\alpha_{t})}}^{pred} = pK_{a}^{pred} \pm \sqrt{diag(J(\boldsymbol{P}^{*}) COV(\boldsymbol{P}^{*}) J(\boldsymbol{P}^{*})^{T})} \cdot t\left(v, \frac{\alpha_{t}}{2}\right)$$
(19)

where the Jacobian matrix  $J(\mathbf{P}^*)$  calculated using  $\partial f/\partial \mathbf{P}^*$  represents the local sensitivity of the property model f to variations in the estimated parameter values  $\mathbf{P}^*$ .  $COV(\mathbf{P}^*)$  is the covariance matrix of the estimated model parameters. v is the degrees of freedom (the total number of data points minus the number of unknown parameters).  $t\left(v, \frac{\alpha_t}{2}\right)$  is the t-distribution value corresponding to the v degrees of freedom and  $\alpha_t/2$  percentile ( $\alpha_t$  is 0.05 for 95% confidence interval). The property prediction method can be considered as reliable if the experimental value falls into the calculated confidence interval.

#### 2.4 Statistical Performance Indicators

The evaluation of performance of the developed models is based on the determination of statistical indicators listed in Table 2.

(18)

| Table 2:                     | Statistical perform      | ance indicators used in this work  |
|------------------------------|--------------------------|--|
| Indicator                    | Abbreviation             | Formula  |
| Average<br>Absolute Error    | AAE                      | $AAE = \frac{1}{N} \sum_{j} \left  pK_{a_{j}}^{exp} - pK_{a_{j}}^{pred} \right $   |
| Coefficient of determination | $R^2$                    | $R^{2} = 1 - \left[ \frac{\sum_{j} (pK_{a_{j}}^{exp} - pK_{a_{j}}^{pred})^{2}}{\sum_{j} (pK_{a_{j}}^{exp} - \mu)^{2}} \right]$ |
| $\mu$ is the average of th   | e experimental $pK_a$ in | the dataset  |

#### **3. Results and Discussions**

Three GC (linear, nonlinear, and ANN-based) models are developed to predict  $pK_a$  for amino acids and other classes of organic compounds. The performances of these models in predicting  $pK_a$  are evaluated in Section 3.1. Several examples are shown in Section 3.2 to help the reader in understanding how to apply the developed models for  $pK_a$  prediction.

#### 3.1 Model Performances

#### 3.1.1 Linear GC model

The regressed model parameters  $pK_{a0}$ ,  $C_i$ ,  $D_j$ , and  $E_k$  are provided in the Supporting Information. The performance statistics of the developed linear GC model for predicting the  $pK_a$  of amino acids in dataset – 1 and the organic compounds in dataset – 2 are given in Table 3.



Table 3: Performance statistics of the developed linear GC model for the two datasets

For a clearer illustration, the statistical indicators of the model for different classes of compounds in both datasets have also been provided in Table 4.

| Derivatives of following amino  | AAE  | $R^2$ | Classes of organic compounds          | AAE  | R <sup>2</sup> |
|---------------------------------|------|-------|---------------------------------------|------|----------------|
| acius                           | 0.20 | 0.96  | Ethers                                | 7.02 | 757 02         |
| B L Alanine                     | 0.20 | 0.90  | Derivatives of alkanes                | 1.18 | 3.73           |
| J Argining                      | 0.05 |       | Aminos                                | 1.10 | -5.25          |
| L-Arginine<br>L Asparagine      | 0.00 | 0.00  | Aromatics                             | 1.05 | 0.01           |
| L-Aspartia acid                 | 0.15 | 0.99  | Corboxylic acids                      | 1.00 | 0.91           |
| L-Aspartic actu                 | 0.22 | 0.98  | Sulfonic acids                        | 3.16 | 0.51           |
| L-Cysteme<br>L Glutamina        | 0.17 | 0.99  | Nitrilos                              | 3.10 | -0.10          |
| L-Olutamine                     | 0.74 | 0.06  | Aldebydes                             | 1.26 | -0.00          |
| Clusing                         | 0.24 | 0.90  | Amidan                                | 2.04 | 0.30           |
|                                 | 0.25 | 0.95  | Annues                                | 2.04 | 0.37           |
| L-Histidine                     | 0.20 | 0.99  |                                       | 1.40 | -0.33          |
| L-Isoleucine                    | 0.12 | 0.56  | Alconois and thiois                   | 2.29 | 0.22           |
| L-Leucine                       | 0.31 | 0.97  | Ketones                               | 2.19 | 0.40           |
| L-Lysine                        | 0.64 | 0.67  | Hydrazines                            | 1.38 | 0.60           |
| L-Methionine                    | 0.06 |       | Heterocyclic [1 ring, 1 heteroatom]   | 1.74 | 0.43           |
| L-Ornithine                     | 0.40 | 0.89  | Heterocyclic [1 ring, 2 heteroatoms]  | 1.50 | 0.57           |
| L-Proline                       | 0.00 | 1.00  | Heterocyclic [1 ring, 3 heteroatoms]  | 2.14 | 0.45           |
| L-Phenylalanine                 | 0.37 | 0.88  | Heterocyclic [1 ring, 4 heteroatoms]  | 0.09 |                |
| L-Serine                        | 0.11 | 0.99  | Heterocyclic [2 rings, 1 heteroatom]  | 1.66 | -0.05          |
| L-Threonine                     | 0.12 | 0.48  | Heterocyclic [2 rings, 2 heteroatoms] | 2.67 | -0.32          |
| L-Tyrosine                      | 0.29 | 0.98  | Heterocyclic [2 rings, 3 heteroatoms] | 1.31 | -1.38          |
| L-Tryptophan                    | 0.00 | 1.00  | Heterocyclic [2 rings, 4 heteroatoms] | 1.50 | 0.46           |
| L-Valine                        | 0.28 | 0.13  | Heterocyclic [3 rings, 1 heteroatom]  | 1.54 | 0.42           |
| Aminobenzoic acids              | 0.21 | 0.80  | Heterocyclic [3 rings, 2 heteroatoms] | 2.43 | 0.97           |
| Aminonaphthalene sulfonic acids | 0.32 | 0.88  | Others                                | 1.54 | 0.57           |
| Aminobenzenesulfonic acids      | 0.37 | 0.98  |                                       |      |                |
| Aminosulfonic acids             | 0.00 |       |                                       |      |                |
| Aminophosphonic acids           | 0.09 | 1.00  |                                       |      |                |
| Others                          | 0.26 | 0.91  |                                       |      |                |

Table 4: Statistical indicators of the linear GC model for different classes of amino acids (dataset - 1) and other organic compounds (dataset - 2)

Figure 2 shows the absolute error between the linear-GC-model predicted  $pK_a$  and experimental  $pK_a$  for the 180 amino acids in dataset – 1. The compounds in dataset – 1 are first sorted according to the ascending order of the absolute error and the error is then plotted as the Y-axis value against the X-axis of 1 to 180. As illustrated, the absolute error in prediction for 158 amino acids is less than 0.5, while for 15 amino acids is between 0.5 and

1.0. Typically, N-substituted amino acids have absolute errors greater than 1.0. The maximum observed absolute error is 1.86 for 3-(dimethylamino) propanoic acid.



Figure 2: Absolute error between the linear-GC-model predicted  $pK_a$  and experimental  $pK_a$ for the 180 amino acids in dataset – 1

It can be concluded that the linear GC model shows a high performance in predicting the  $pK_a$  for amino acids. However, for the other organic compounds in dataset – 2, a satisfactory prediction cannot be achieved by employing linear GC correlations. In the next section, nonlinear GC models are developed for both datasets.

#### 3.1.2 Nonlinear GC model

The regressed model parameters *a*, *b*, *c*,  $pK_{a0}$ ,  $C_i$ ,  $D_j$ , and  $E_k$  (see Eq. 12) are provided in the Supporting Information. The performance statistics of the developed nonlinear GC model for both datasets are given in Table 5. As can be seen, compared to the linear GC model, a significant improvement in the accuracy of  $pK_a$  prediction has been obtained for both datasets.



Table 5: Performance statistics of the developed nonlinear GC model for the two datasets

The statistical indicators of the nonlinear GC model for different classes of amino acids (dataset - 1) and organic compounds (dataset - 2) are presented in Table 6. It is seen that the model can accurately predict the  $pK_a$  for all kinds of amino acids. However, it is not able to successfully represent the  $pK_a$  for some other compounds, for example, the ethers, derivatives of alkanes, and hydrazines. Besides, for heterocyclic compounds with 3 heteroatoms, the model does not perform well either.

| Derivatives of following amino acids | AAE                   | R <sup>2</sup> | Classes of organic compounds          | AAE  | R <sup>2</sup> |
|--------------------------------------|-----------------------|----------------|---------------------------------------|------|----------------|
| L-Alanine                            | 0.01                  | 1.00           | Ethers                                | 3.16 | -153.92        |
| β-L-Alanine                          | 0.03                  |                | Derivatives of alkanes                | 0.69 | 0.19           |
| L-Arginine                           | 0.00                  |                | Amines                                | 1.12 | 0.79           |
| L-Asparagine                         | 3.97×10 <sup>-3</sup> | 0.99           | Aromatics                             | 1.59 | 0.66           |
| L-Aspartic acid                      | 0.02                  | 0.99           | Carboxylic acids                      | 0.88 | 0.57           |
| L-Cysteine                           | 0.03                  | 1.00           | Sulfonic acids                        | 1.94 | 0.65           |
| L-Glutamine                          | 0.04                  |                | Nitriles                              | 2.31 | 0.70           |
| L-Glutamic acid                      | 0.02                  | 1.00           | Aldehydes                             | 0.88 | 0.90           |
| Glycine                              | 0.04                  | 1.00           | Amides                                | 1.06 | 0.85           |
| L-Histidine                          | 0.02                  | 1.00           | Sulfonamides                          | 1.00 | 0.42           |
| L-Isoleucine                         | 0.02                  | 0.89           | Alcohols and thiols                   | 1.15 | 0.83           |
| L-Leucine                            | 0.02                  | 1.00           | Ketones                               | 1.13 | 0.87           |
| L-Lysine                             | 0.03                  | 1.00           | Hydrazines                            | 1.72 | 0.38           |
| L-Methionine                         | 3.00×10 <sup>-3</sup> |                | Heterocyclic [1 ring, 1 heteroatom]   | 1.61 | 0.69           |
| L-Ornithine                          | 0.03                  | 0.99           | Heterocyclic [1 ring, 2 heteroatoms]  | 1.41 | 0.68           |
| L-Proline                            | 0.06                  | 1.00           | Heterocyclic [1 ring, 3 heteroatoms]  | 2.13 | 0.56           |
| L-Phenylalanine                      | 0.08                  | 1.00           | Heterocyclic [1 ring, 4 heteroatoms]  | 1.59 |                |
| L-Serine                             | 0.04                  | 1.00           | Heterocyclic [2 rings, 1 heteroatom]  | 1.40 | 0.54           |
| L-Threonine                          | 0.02                  | 0.99           | Heterocyclic [2 rings, 2 heteroatoms] | 1.67 | 0.46           |
| L-Tyrosine                           | 0.01                  | 1.00           | Heterocyclic [2 rings, 3 heteroatoms] | 1.74 | -2.60          |
| L-Tryptophan                         | 0.00                  | 0.99           | Heterocyclic [2 rings, 4 heteroatoms] | 0.51 | 0.94           |
| L-Valine                             | 0.02                  | 0.99           | Heterocyclic [3 rings, 1 heteroatom]  | 0.99 | 0.79           |
| Aminobenzoic acids                   | 0.01                  | 1.00           | Heterocyclic [3 rings, 2 heteroatoms] | 1.05 | 0.83           |
| Aminonaphthalene sulfonic acids      | 0.04                  | 0.99           | Others                                | 1.09 | 0.78           |
| Aminobenzenesulfonic acids           | 0.00                  | 1.00           |                                       |      |                |
| Aminosulfonic acids                  | 0.02                  |                |                                       |      |                |
| Aminophosphonic acids                | 0.04                  | 1.00           |                                       |      |                |
| Others                               | 1.30×10 <sup>-3</sup> | 1.00           |                                       |      |                |

Table 6: Statistical indicators of the nonlinear GC model for different classes of amino acids (dataset - 1) and other organic compounds (dataset - 2)

Figure 3 shows the absolute error between the nonlinear-GC-model predicted  $pK_a$  and experimental  $pK_a$  for the 1622 organic compounds in dataset – 2. As indicated, the absolute error of 507 compounds is less than 0.5 and that of 351 compounds falls into the range of 0.5

to 1.0. 300 compounds have the error larger than 2.0 and the maximum observed absolute error is 8.69.



Figure 3: Absolute error between the nonlinear-GC-model predicted  $pK_a$  and experimental  $pK_a$  for the 1622 organic compounds in dataset – 2

It can be concluded that the nonlinear GC model performs very well in predicting  $pK_a$  for amino acids. However, the accuracy of the model for estimating  $pK_a$  of the other 1622 organic compounds still needs to be improved.

#### 3.1.3 ANN-GC model

The ANN-GC model has been developed for predicting  $pK_a$  of the 1622 organic compounds in dataset – 2. The regressed parameters  $W_1$ ,  $W_2$ ,  $b_1$ , and  $b_2$  are provided in Table S4 of the Supporting Information. The overall model performance and the performance indicators for different classes of compounds are shown in Table 7 and Table 8, respectively.



Table 7: Performance statistics of the developed ANN-GC model for dataset -2

| Classes of organic compounds          | AAE                   | $\mathbb{R}^2$ |
|---------------------------------------|-----------------------|----------------|
| Ethers                                | 1.12×10 <sup>-6</sup> | 1.00           |
| Derivatives of alkanes                | 2.57×10 <sup>-6</sup> | 1.00           |
| Amines                                | 0.24                  | 0.98           |
| Aromatics                             | 0.28                  | 0.98           |
| Carboxylic acids                      | 0.13                  | 0.96           |
| Sulfonic acids                        | 1.62×10 <sup>-6</sup> | 1.00           |
| Nitriles                              | 0.28                  | 0.99           |
| Aldehydes                             | 0.27                  | 0.98           |
| Amides                                | 0.13                  | 0.99           |
| Sulfonamides                          | 0.14                  | 0.79           |
| Alcohols and thiols                   | 0.07                  | 0.99           |
| Ketones                               | 0.12                  | 0.99           |
| Hydrazines                            | 5.68×10 <sup>-6</sup> | 1.00           |
| Heterocyclic [1 ring, 1 heteroatom]   | 0.31                  | 0.97           |
| Heterocyclic [1 ring, 2 heteroatoms]  | 0.27                  | 0.96           |
| Heterocyclic [1 ring, 3 heteroatoms]  | 1.57×10 <sup>-6</sup> | 1.00           |
| Heterocyclic [1 ring, 4 heteroatoms]  | 1.15×10 <sup>-8</sup> |                |
| Heterocyclic [2 rings, 1 heteroatom]  | 0.44                  | 0.90           |
| Heterocyclic [2 rings, 2 heteroatoms] | 0.46                  | 0.93           |
| Heterocyclic [2 rings, 3 heteroatoms] | 1.83×10 <sup>-6</sup> | 1.00           |
| Heterocyclic [2 rings, 4 heteroatoms] | 1.57×10 <sup>-6</sup> | 1.00           |
| Heterocyclic [3 rings, 1 heteroatom]  | 0.99                  | 0.76           |
| Heterocyclic [3 rings, 2 heteroatoms] | 0.51                  | 0.92           |
| Others                                | 0.01                  | 0.99           |
|                                       |                       |                |

Table 8: Statistical indicators of the ANN-GC model for different classes of organic compounds in dataset -2

Figure 4 shows the absolute error between the ANN-GC-model predicted  $pK_a$  and experimental  $pK_a$  for the 1622 organic compounds in dataset – 2. As seen, 89% of the 1622 compounds have absolute errors less than 0.5 and about 95% have absolute errors less than 1.0. The absolute error plot together with the estimated performance statistics indicates that the developed ANN-GC model can well represent the  $pK_a$  of the organic compounds.



Figure 4: Absolute error between the ANN-GC-model predicted  $pK_a$  and experimental  $pK_a$ for the 1622 organic compounds in dataset – 2

#### **3.2. Application Examples**

In this section, three examples are provided where the linear GC model, nonlinear GC model, and ANN-GC model are employed to predict  $pK_a$ . The non-linear model for amino acids and the ANN-GC model for organic compounds will be available in ProPred (a property prediction tool within ICAS (Gani *et al.*, 1997). The examples given below are from a prototype of ProPred.

#### **3.2.1** Prediction of $pK_a$ using the linear and non-linear GC models (amino acids)

Since the linear and non-linear GC model performs well for amino acids only, an example for the prediction of  $pK_a$  of N-Acetyl L-Alanine is shown in Table 9.

| Table 9: Prediction of $pK_a$ for N-Acetyl L-Alanine (CAS: 97-69-8) using the linear and non- |
|---|
| linear GC models  |

| <b>Compound:</b><br>N-Acetyl L-Alanine<br><u>Molecular formula</u> : C <sub>5</sub> H <sub>9</sub> NO <sub>3</sub> | Molecular structure<br>O NH OH<br>O |   |                    |  |  |  |  |
|--|-------------------------------------|---|--------------------|--|--|--|--|
| First-order groups   | Occurrences (N <sub>i</sub> )       | Group co                                    | ntribution $(C_i)$ |  |  |  |  |
|  |                                     | Linear Model                                | Non-linear Model   |  |  |  |  |
| CH <sub>3</sub>  | 2                                   | 0.3417                                      | 0.0194             |  |  |  |  |
| СН   | 1                                   | -0.3425                                     | -0.0336            |  |  |  |  |
| СООН   | 1                                   | 1.4441                                      | -0.0912            |  |  |  |  |
| NHCO   | 1                                   | 0.4817                                      | 0.0277             |  |  |  |  |
| Second-order groups  | Occurrences (M <sub>j</sub> )       | Group contribution ( <i>D<sub>j</sub></i> ) |                    |  |  |  |  |
|  |                                     | Linear Model                                | Non-linear Model   |  |  |  |  |
| CH <sub>m</sub> (NH <sub>n</sub> )-COOH (m, n in 02)   | 1                                   | -2.8272                                     | 0.1457             |  |  |  |  |
| Third-order groups   | Occurrences $(O_k)$                 | Group co                                    | ntribution $(E_k)$ |  |  |  |  |
|  |                                     | Linear Model                                | Non-linear Model   |  |  |  |  |
| $O=C-NH-CH_n-COOH (n \text{ in } 02)$  | 1                                   | 0.1240                                      | -0.0482            |  |  |  |  |

Table 9 lists the number of occurrences and the contribution of first-order, second-order, and third-order groups present in the N-Acetyl L-Alanine molecule. According to Eq. (11) where  $pK_{a0} = 3.0683$ , the predicted  $pK_a$  of N-Acetyl L-Alanine is 2.63. According to Eq. (19), the calculated 95% confidence interval of the estimated  $pK_a$  is 1.79. It can be observed that the experimental  $pK_a$  (2.34) falls in the range of [0.84, 4.42], which indicates the reliability of the model. On the other hand, according to Eq. (12) where  $pK_{a0} = -1.0206$ , a = -0.0016, b = 0.0393 and c = -0.3250, the predicted  $pK_a$  for N-Acetyl L-Alanine is 2.38 which implies that in the case of amino acids both the linear and non-linear GC model have a good performance.

#### 3.2.2 Prediction of *pK*<sub>a</sub> using the nonlinear GC model for Bentazon (CAS: 25057-89-0)

In order to illustrate the  $pK_a$  prediction using the nonlinear GC model, an example with 1H-2,1,3-Benzothiadiazin-4(3H)-one, 3-(1-methylethyl)-2,2-dioxide, which is used as a herbicide, is shown in Table 10.

# Table 10: Prediction of $pK_a$ for 1H-2,1,3-Benzothiadiazin-4(3H)-one, 3-(1-methylethyl)-2,2-dioxide (CAS: 25057-89-0) using the nonlinear GC model

| Compound:  | Molecula                      | ar structure                                |
|--|-------------------------------|---|
| 1H-2,1,3-Benzothiadiazin-4(3H)-one, 3-   |                               |   |
| (1-methylethyl)-2,2-dioxide  | 0                             |   |
| Molecular formula: C <sub>10</sub> H <sub>12</sub> N <sub>2</sub> O <sub>3</sub> S | NH                            |   |
|  | S                             |   |
|  | 0- \<br>N                     |   |
|  |                               |   |
|  |                               | Ó   |
|  | ١                             |   |
| First-order groups   | Occurrences (N <sub>i</sub> ) | Group contribution (C <sub>i</sub> )        |
| CH <sub>3</sub>  | 2                             | 0.1322                                      |
| СН   | 1                             | -0.0182                                     |
| aCH  | 4                             | 0.0869                                      |
| aC fused with non-aromatic ring  | 2                             | -0.6176                                     |
| NH (cyc)   | 1                             | 0.4334                                      |
| N (cyc)  | 1                             | 0.1982                                      |
| CO (cyc)   | 1                             | 0.2178                                      |
| $SO_2$ (cyc)   | 1                             | 0.4380                                      |
|  |                               |   |
| Second-order groups  | Occurrences (M <sub>j</sub> ) | Group contribution $(D_j)$                  |
| (CH <sub>3</sub> ) <sub>2</sub> CH   | 1                             | -0.0544                                     |
| Third-order groups   | Occurrences $(O_k)$           | Group contribution ( <i>E<sub>k</sub></i> ) |
| aC-CO <sub>cyc</sub> (fused rings)   | 1                             | 0.1754                                      |
| aC-NH <sub>ncyc</sub> (fused rings) (n in 01)                                      | 1                             | 0.2404                                      |
| AROM.FUSED[2]  | 1                             | -0.2189                                     |
| According to Eq. (12), the predicted $pK_a$ is 2.4                                 | .7                            |   |
| (where, $a = 3.759 \times 10^{-4}$ , $b = -0.0072$ , $c = -0.04$                   | 431, $pK_{a0} = -1.3231$ )    |   |
| The experimental $pK_a$ is 2.92. Hence, the abso                                   | lute deviation is 0.45.       |   |

#### 3.2.3 Prediction of *pK*<sub>a</sub> using the ANN-GC model for Bentazon (CAS: 25057-89-0)

To compare the ANN-GC model with the nonlinear GC model, the  $pK_a$  prediction for the same compound, 1H-2,1,3-Benzothiadiazin-4(3H)-one, 3-(1-methylethyl)-2,2-dioxide is shown in Table 11.

# Table 11: Prediction of $pK_a$ for 1H-2,1,3-Benzothiadiazin-4(3H)-one, 3-(1-methylethyl)-2,2-dioxide (CAS: 25057-89-0) using the ANN-GC model

| Compound:                                 | Compound: Molecular structure      |                  |         |                           |              |                           |                        |              |
|---|------------------------------------|------------------|---------|---------------------------|--------------|---------------------------|------------------------|--------------|
| 1H-2,1,3-Benzothiadiazin-4(3H)-one, 3-(1- |                                    |                  |         |                           | 0            |                           | 7                      |              |
| methylethyl)-2,2-d                        | ioxide                             |                  |         |                           | U N          | $\mathbb{H}_{\mathbb{A}}$ | ) \                    |              |
| Molecular formula                         | $: C_{10}H_{12}N_2O_3S$            | 5                |         |                           | _s           | $  \subseteq$             | $\rangle$              |              |
|   | 10 12 2 3                          |                  |         |                           | 0            | $\rightarrow$             |                        |              |
|   |                                    |                  |         |                           | N-           |                           |                        |              |
|   |                                    |                  |         |                           |              | //                        |                        |              |
|   |                                    |                  |         |                           | $\backslash$ | 0                         |                        |              |
|   |                                    |                  |         |                           | 1            |                           |                        |              |
| E'mat and an                              |                                    |                  |         |                           |              |                           |                        | 50           |
| First-order                               | CH <sub>3</sub>                    | CH               | aCH     | aC                        | NH(cyc)      | N(cyc)                    | CO(cyc)                | $SO_2$       |
| groups                                    |                                    |                  |         |                           |              |                           |                        | (696)        |
| Occurrences                               | 2                                  | 1                | 4       | 2                         | 1            | 1                         | 1                      | 1            |
|   | $\mathbf{W}_1$                     |                  |         |                           |              |                           |                        |              |
|   | [-1.6829                           | 6.4756           | 1.7533  | 0.7377                    | 0.443        | 0.9212                    | 2.6333                 | -0.1755      |
|   | 1.0509                             | -0.2184          | -2.1471 | -1.2136                   | 1.4681       | 0.8396                    | -1.0455                | 7.3758       |
|   | 3.619                              | -2.4328          | 1.6553  | 2.1358                    | -0.222       | -1.2836                   | -6.3658                | 1.3176       |
|   | 4.7908                             | -4.4383          | 0.8453  | 1.6746                    | -0.3299      | -2.5009                   | 3.159                  | -0.1221      |
|   | 0.8226                             | 1.2565           | 0.5366  | -0.1923                   | 0.1443       | -6.606                    | -0.5895                | 0.6971       |
|   | 2.7329                             | 6.3506           | 2.4439  | 5.4217                    | -4.8977      | 1.3109                    | -5.2433                | 0.7122       |
|   | -8.9644                            | -19.3123         | 11.4152 | 2.9152                    | -17.5028     | 5.2274                    | 10.238                 | -8.6289      |
|   | 0.8619                             | 0.5316           | -3.2969 | 3.7527                    | 11.7938      | -1.2256                   | -5.6679                | -5.3864      |
|   | 1.1437                             | -2.4476          | 0.1281  | 1.5644                    | 1.1092       | 10.2064                   | 0.2857                 | 0.1515       |
|   | -0.6423                            | 0.226            | -1.544  | 0.1394                    | 5.3677       | -0.5433                   | -2.6248                | 4.8043       |
|   | 1.1433                             | -2.3074          | 1.388   | 2.2463                    | 2.8746       | 1.9733                    | -0.0806                | 3.7311       |
|   | 4.6161                             | 2.011            | -3.8926 | 4.5683                    | -6.1653      | -13.1146                  | -1.5625                | 7.5796       |
|   | 2.7842                             | -1.8139          | -1.0137 | -0.2305                   | -5.2968      | -1.779                    | 2.0042                 | 0.471        |
|   | 2.9091                             | -3.0596          | 0.6423  | -1.0794                   | -0.5082      | 1.0108                    | 1.4972                 | 6.0197       |
|   | -5.2623                            | 6.3213           | -4.5124 | -0.5687                   | -2.2154      | 11.0957                   | 0.5727                 | 9.6914       |
|   | -0.0379                            | 2.157            | 1.4917  | -0.9739                   | 2.458        | 5.8252                    | 0.2285                 | 5.0562       |
|   | 6.3547                             | 6.897            | 0.7735  | -2.2172                   | -3.7028      | 1.37                      | 10.668                 | 1.3711       |
|   | -3.5484                            | 20.4593          | 2.7547  | 9.418                     | 6.3029       | 3.7152                    | 8.6495                 | 3.7617       |
|   | 3.0958                             | -13.0759         | 3.5244  | -5.4662                   | 13.0565      | -12.2072                  | 2.812                  | 3.5092       |
|   | 5.4879                             | -5.8329          | -0.0789 | 2.5132                    | -8.8739      | 5.0805                    | -4.625                 | -0.7204]     |
| b <sub>1</sub> Ti                         | ransformation<br>of W <sub>2</sub> | n b <sub>2</sub> | Input   | variable <i>p</i>         | = [2 1 4 2   | 2 1 1 1 1]'               | (the zero e            | elements are |
| -15.6497                                  | 11.2478                            | -2.347           | 9 remov | red) By fo                | llowing Ea   | IS (13-16)                | $nK^{\text{pred}} = C$ | 29211 The    |
| 1.5128                                    | -15.9438                           |                  | Temov   | <i>ca)</i> . <i>by</i> 10 | nowing Eq    | [5. (15 10),              | pria – z               | 2.9211. 1110 |
| -15.1206                                  | -6.0101                            |                  | evneri  | mental valu               | f = of nK is | 2.92 Hence                | e the absolu           | te deviation |
| -3.8606                                   | -14.6460                           |                  | схрен   | incinal van               | $p r_a$ is   | 2.92. 110100              | , uie absolu           |              |
| -8.8757                                   | -12.7365                           |                  | ia 0.00 | 111                       |              |                           |                        |              |
| -24.9630                                  | 8.3284                             |                  | 18 0.00 | )11.                      |              |                           |                        |              |
| 9.1079                                    | -9.0066                            |                  |         |                           |              |                           |                        |              |
| 13.3214                                   | 9.7666                             |                  |         |                           |              |                           |                        |              |
| 6.9750                                    | -15.2921                           |                  |         |                           |              |                           |                        |              |
| -1.21//                                   | -12.5122                           |                  |         |                           |              |                           |                        |              |
| -3.3103                                   | 5 2121                             |                  |         |                           |              |                           |                        |              |
| -1.5351                                   | 18 8958                            |                  |         |                           |              |                           |                        |              |
| 1.6159                                    | 13.7597                            |                  |         |                           |              |                           |                        |              |
| 9.8148                                    | 5.9600                             |                  |         |                           |              |                           |                        |              |
| -4.6202                                   | -18.6921                           |                  |         |                           |              |                           |                        |              |
| 4.1303                                    | 17.3304                            |                  |         |                           |              |                           |                        |              |
| 0.1458                                    | 6.0333                             |                  |         |                           |              |                           |                        |              |
| -18.9379                                  | 6.0589                             |                  |         |                           |              |                           |                        |              |
| 27.8468                                   | -5.7745                            |                  |         |                           |              |                           |                        |              |

Two more examples for  $pK_a$  prediction using the nonlinear GC model and the ANN-GC model can be found in the supporting information (Tables S6 – S7).

#### 4. Conclusion

CCE

The prediction of acid dissociation constant ( $K_a$ ) is very significant in many areas. In this work, three GC property models have been developed and tested for the estimation of the  $pK_a$  of organic compounds including amino acids. The linear GC model has a good performance ( $R^2 = 0.96$ , AAE = 0.23) only for amino acids. For the other classes of compounds, a nonlinear GC model and an ANN-GC model have been developed. The nonlinear GC model has a moderate prediction quality ( $R^2 = 0.81$ , AAE = 1.18) whereas the ANN-GC model gives a much better estimation ( $R^2 = 0.98$ , AAE = 0.17).

The developed models enable fast and preliminary  $pK_a$  estimations in the cases where the experimental measurements are difficult or not feasible. Currently, these models are being incorporated into a computer-aided molecular design framework to identify and analyse promising molecules with desirable properties.

#### References

- Bettelheim, F., Brown, W., Campbell, M., Farrell, S., 2007. *Introduction to Organic and Biochemistry*. Belmont CA: Thomson Brooks/Cole.
- 2. Bishop, C.M., 1995. Neural Networks for Pattern Recognition. Oxford University Press.
- Cheung, E., 1995. Substituent Effects on the Tautomerization of Amino Acids. Master of Science. Texas Tech University.
- Gani R., Hytoft G., Jaksland C., Jensen A.K., 1997. An integrated computer aided system for integrated design of chemical processes. *Computers Chemical Engineering* 21(10), 1135–1146
- Gharagheizi, F., Eslamimanesh, A., Mohammadi, A.H., Richon, D., 2011a. Representation/prediction of solubilities of pure compounds in water using artificial neural network– group contribution method. *Journal of Chemical & Engineering Data* 56(4), 720-726.
- Gharagheizi, F., Alamdari, R.F., Angaji, M.T., 2008. A new neural network group contribution method for estimation of flash point temperature of pure components. *Energy & Fuels* 22(3), 1628-1635.
- Gharagheizi, F., Eslamimanesh, A., Mohammadi, A.H., Richon, D., 2011b. Use of artificial neural network-group contribution method to determine surface tension of pure compounds. *Journal of Chemical & Engineering Data* 56(5), 2587-2601.
- Green, D., Perry, R., 2008. Perrys's Chemical Engineers' Handbook. 8th ed. New York: McGraw-Hill.
- Hukkerikar, A.S., Sarup, B., Kante, T.A., Abildkov, J., Sin, G., Gani, R., 2012. Groupcontribution+ (GC+) based estimation of properties of pure components: Improved property estimation and uncertainty analysis, *Fluid Phase Equilibria* 321, 25–43

- 10. Hukkerikar, A.S., Kalakul, S., Sarup, B., Young, D.Y., Sin, G., Gani, R., 2012. Estimation of environment-related properties of chemicals for design of sustainable processes: development of group-contribution+ (GC+) property models and uncertainty analysis. *Journal of Chemical Information and Modeling* 52(11), 2823-2839
- Hukkerikar, A.S., Meier, R.J., Gani, R., 2013. A method to estimate the enthalpy of formation of organic compounds with chemical accuracy. *Fluid Phase Equilibria* 348, 23-32.
- Im, W., Beglov, D. and Roux, B., 1998. Continuum solvation model: Computation of electrostatic forces from numerical solutions to the Poisson-Boltzmann equation. *Computer Physics Communications*, 111, 59-75.
- Jang, Y., Sowers, L., Çağin, T., Goddard, W., 2001. First Principles Calculation of pKa Values for 5-Substituted Uracils. *The Journal of Physical Chemistry A* 105(1), 274-280.
- Jensen, J., Swain, C., Olsen, L., 2017. Prediction of pKa Values for Druglike Molecules Using Semiempirical Quantum Chemical Methods. *The Journal of Physical Chemistry A* 121(3), 699-707.
- 15. Jhamb, S., Liang, X., Gani, R., Hukkerikar, A., 2018. Estimation of physical properties of amino acids by group-contribution method. *Chemical Engineering Science* 175, 148-161.
- 16. Kirkwood, J. and Westheimer, F., 1938. The electrostatic influence of substituents on the dissociation constants of organic acids. I. *The Journal of Chemical Physics* 6(9), 506-512.
- 17. Kortüm, G., Vogel, W., Andrussow, K., 1961. *Dissociation Constants of Organic Acids in Aqueous Solution*. London: Butterworths.
- 18. Levenberg, K., 1944. A method for the solution of certain non-linear problems in least squares. *Quarterly of Applied Mathematics* 2(2), 164-168.

- 19. Marquardt, D., 1963. An algorithm for least-squares estimation of nonlinear parameters. *Journal of the Society for Industrial and Applied Mathematics* 11(2), 431-441.
- 20. Marrero, J., Gani, R., 2001. Group-contribution based estimation of pure component properties. *Fluid Phase Equilibria* 183-184, 183-208.
- 21. Marrero, J., Gani, R., 2002. Group-contribution-based estimation of octanol/water partition coefficient and aqueous solubility. *Industrial & Engineering Chemistry Research* 41(25), 6623-6633.
- 22. Metzler, D., 2012. Chapter 3: Energetics of Biochemical Reactions. In: *Biochemistry: The Chemical Reactions of Living Cells, Volume 1*. New York, USA: Academic Press Inc., 176 178.
- 23. Peck, T., Hill, S., 2014. *Pharmacology for Anaesthesia and Intensive Care*. Cambridge University Press.
- 24. Perrin, D., 1965. *Dissociation Constants of Organic Bases in Aqueous Solution*. London: Butterworth.
- 25. Perrin, D., Dempsey, B., Serjeant, E., 1981. pK<sub>a</sub> Prediction for Organic Acids and Bases.London: Chapman & Hall.
- 26. Petersen, R., Fredenslund, A., Rasmussen, P., 1994. Artificial neural networks as a predictive tool for vapor-liquid equilibrium. *Computers & Chemical Engineering* 18, S63-S67.
- 27. Shields, G.C., Seybold, P.G., 2013. *Computational Approaches for the Prediction of pKa Values.* Boca, Raton, Florida: CRC Press.
- 28. Tong, W., Wen, H., 2008. Preformulation Aspects of Insoluble Compounds. In: R. Liu, ed., *Water-Insoluble Drug Formulation*, 2nd ed. Boca, Raton, Florida: CRC Press, 62-87.

## Highlights

- Prediction of acid dissociation constants (Ka) for a large set of organic compounds
- The Marrero and Gani Group Contribution (MG-GC) method to develop the property models
- Linear and nonlinear GC models for amino acids and other classes of compounds
- An Artificial Neural Network (ANN) based GC model for organic compounds
- Modeling details and model parameters provided
- Accuracy of the models demonstrated through application examples

#### Graphical abstract

