



## Dynamic exergoeconomic analysis of a heat pump system used for ancillary services in an integrated energy system

Meesenburg, Wiebke; Ommen, Torben; Elmegaard, Brian

*Published in:*  
Energy

*Link to article, DOI:*  
[10.1016/j.energy.2018.03.093](https://doi.org/10.1016/j.energy.2018.03.093)

*Publication date:*  
2018

*Document Version*  
Peer reviewed version

[Link back to DTU Orbit](#)

*Citation (APA):*  
Meesenburg, W., Ommen, T., & Elmegaard, B. (2018). Dynamic exergoeconomic analysis of a heat pump system used for ancillary services in an integrated energy system. *Energy*, 152, 154-165.  
<https://doi.org/10.1016/j.energy.2018.03.093>

---

### General rights

Copyright and moral rights for the publications made accessible in the public portal are retained by the authors and/or other copyright owners and it is a condition of accessing publications that users recognise and abide by the legal requirements associated with these rights.

- Users may download and print one copy of any publication from the public portal for the purpose of private study or research.
- You may not further distribute the material or use it for any profit-making activity or commercial gain
- You may freely distribute the URL identifying the publication in the public portal

If you believe that this document breaches copyright please contact us providing details, and we will remove access to the work immediately and investigate your claim.

# Accepted Manuscript

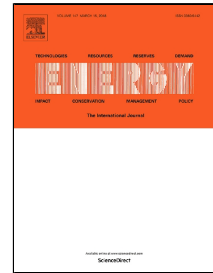
Dynamic exergoeconomic analysis of a heat pump system used for ancillary services in an integrated energy system

Wiebke Meesenburg, Torben Ommen, Brian Elmegaard

PII: S0360-5442(18)30502-4  
DOI: 10.1016/j.energy.2018.03.093  
Reference: EGY 12551  
To appear in: *Energy*  
Received Date: 20 November 2017  
Revised Date: 09 March 2018  
Accepted Date: 17 March 2018

Please cite this article as: Wiebke Meesenburg, Torben Ommen, Brian Elmegaard, Dynamic exergoeconomic analysis of a heat pump system used for ancillary services in an integrated energy system, *Energy* (2018), doi: 10.1016/j.energy.2018.03.093

This is a PDF file of an unedited manuscript that has been accepted for publication. As a service to our customers we are providing this early version of the manuscript. The manuscript will undergo copyediting, typesetting, and review of the resulting proof before it is published in its final form. Please note that during the production process errors may be discovered which could affect the content, and all legal disclaimers that apply to the journal pertain.



# Dynamic exergoeconomic analysis of a heat pump system used for ancillary services in an integrated energy system

Wiebke Meesenburg<sup>\*1</sup>, Torben Ommen<sup>1</sup>, Brian Elmegaard<sup>1</sup>

<sup>1</sup>Department of Mechanical Engineering, Technical University of Denmark, Lyngby, Denmark

Keywords: Dynamic exergoeconomic analysis, integrated energy systems, heat pump, flexibility, ancillary services

## 1 Abstract

2 The integration of different energy sectors, such as the electricity and heating sector, is an effective way  
3 to integrate large shares of renewable energy into the energy system. Heat pumps allow efficient heat  
4 production based on electricity. As such, they may be used to provide two different services - the  
5 generation of heat and the provision of demand flexibility as ancillary services for the power system. The  
6 paper presents a method to assess the impact of providing demand flexibility on the performance of the  
7 conversion system based on a dynamic exergoeconomic analysis. A way to allocate the cost of heat and  
8 flexibility products based on the difference in exergy destruction was proposed. The method was  
9 applied to a case of a groundwater-source heat pump system supplying a district heating island system.  
10 It was found that providing demand flexibility causes higher exergy destruction, mainly due to heat  
11 losses during storage and the need to reheat the fluid using an electric heater. The major part of the  
12 additional exergy destruction was not related to heat pump regulation. When providing flexibility the  
13 overall cost of the system increased and according to the proposed allocation, demand flexibility  
14 accounted for 12 % of the overall cost.

---

\* Corresponding author: [wmeese@mek.dtu.dk](mailto:wmeese@mek.dtu.dk)

## 16 1 Introduction

17 The future Danish energy system will be characterized by high shares of transient renewable power  
18 production [1]. One of the main challenges imposed by this is to design future energy systems to be able  
19 to balance high shares of fluctuating power and to achieve an efficient use of the energy available. This  
20 challenge may be met by integrating the power, heating and mobility sectors. Synergies can be  
21 exploited, and it is expected that it will be possible to allocate higher shares of renewable energy,  
22 increase the overall energy efficiency of the system and help to ensure a reliable and resilient energy  
23 system [2].

24 The heating sector can absorb large amounts of electricity and additionally offers the possibility to store  
25 the energy as heat in heat storages, buildings and district heating systems [3]. Different technologies are  
26 available to couple the heating and electricity sector by converting one energy form into another, such  
27 as heat pumps and electric heaters. Mathiesen and Lund [4] found that large scale heat pumps are  
28 especially promising to efficiently integrate large amounts of renewable energy into the system.  
29 However, the ability and limitations of large heat pumps to provide demand flexibility need further  
30 investigation [5].

31 In this study, we focus on the integration between the heating and the power system by analyzing a  
32 heat pump system supplying a district heating island system. Further, the system acts as a controllable  
33 load in the power system, i.e. the heat pump electricity consumption changes according to signals from  
34 the power system operator [6]. Previous studies showed that the integration of the electricity and the  
35 heating sectors offers the possibility to decouple electricity supply and demand constraints and can  
36 provide balancing service to the power sector [7]. Stinner et al. [8] confirmed that balancing services  
37 from lower voltage levels are necessary in energy systems with a high share of renewables to balance  
38 the distribution and transmission grids. Further, controlling the load of heat pumps flexibly can reduce

39 CO<sub>2</sub> emissions and lower CO<sub>2</sub> abatement cost, while the overall electricity consumption may increase  
40 [9].

41 The considered conversion system provides two different products – the heat supplied to the district  
42 heating grid and the ancillary service to the electricity grid. This has several consequences for the  
43 operation of the heat pump. Firstly, the operation strategy has to take the demand of heat and power  
44 regulation into consideration. Secondly, the ability to provide flexibility comes at the cost of increased  
45 investment cost for a larger conversion system. Thirdly, the flexible operation leads to additional losses  
46 in the conversion system. The three consequences open for investigations of the valuation of the  
47 different products and the additional cost of flexible operation.

48 Ulbig & Andersson define the operational flexibility of a power system as the technical ability of a power  
49 system to modulate the power feed-in or load over time [10]. Extending this definition to integrated  
50 energy systems, we propose to define flexibility as the technical ability of a energy conversion system to  
51 adapt the power feed-in, load or conversion into other forms of energy in order to optimize security of  
52 supply, cost and/or environmental impact of the overall energy system.

53 Different studies have been carried out in an effort to determine the value of flexibility provided by heat  
54 pumps and electric heaters. Three general approaches were identified.

55 The first approach is to define an average flexibility value by considering the differences between supply  
56 and demand [7], [11], [12]. This approach is based on the idea that the unit that adapts to the state of  
57 the system, and thus decreases the difference between supply and demand, provides a balancing  
58 service to the system.

59 The second approach takes the specifications regarding ramping rates and capacities of the different  
60 components into consideration. In this way it evaluates the actual potential of a component to react to

61 regulation needs of the system at a certain point in time with respect to the current state of component  
62 operation [10-12].

63 The third approach is to evaluate the flexibility of a unit by evaluating the cost effectiveness of an  
64 increase of flexibility. Blarke & Lund [15] defined the cost effectiveness of the storage or relocation  
65 option as the shadow cost associated with increased flexibility of a certain unit. Meibom et al. [16]  
66 propose to evaluate the impact of heat pumps and electric boilers according to their influence on the  
67 price of regulating power.

68 All these approaches value flexibility according to the benefit of the power system or of the overall  
69 energy system. However, it is important to assess which cost is associated with providing ancillary  
70 services for the heat pump system operator, as this is valuable information when deciding on the  
71 operation strategy and the system design. The analysis of the actual changes induced to the conversion  
72 system and the associated costs requires a more detailed method than suggested by the above  
73 references.

74 In the present study, the performance of a conversion system was analyzed using an exergoeconomic  
75 approach. A dynamic model of the system was simulated and a dynamic exergoeconomic analysis was  
76 conducted in order to reveal the exergy destruction connected to the flexible operation of the system  
77 and where and when it occurs. The method of exergoeconomic analysis is a combination of an exergy  
78 analysis and economic principles and is used to obtain information about how to design and operate  
79 energy conversion systems in a cost-effective way [17]. It enables the allocation of cost to multiple  
80 products of any energy conversion plant based on a framework that consistently connects economics  
81 and thermodynamics. Usually, an exergoeconomic analysis is conducted assuming steady state  
82 processes. Sayadi et al. [18] conducted a dynamic exergy and exergoeconomic analysis for a building

83 envelope. Sangi et al. [19] presented an approach, to conduct a quasi-dynamic exergoeconomic analysis  
84 by analyzing the result of each time step for a dynamic simulation of a building heating system.

85 In this paper, we used a dynamic exergoeconomic analysis to assess the system performance. The  
86 method is extended by the definition of exergy fuel and exergy product for the stratified storage tank  
87 and an approach to allocate the cost to both products of the system – heat and demand flexibility. In  
88 section 2 we describe the method, including a description of the case study, the mathematical model,  
89 exergy and exergoeconomic analysis. Section 3 presents the results found for the case study and section  
90 4 discusses the results and the method that was used. Finally, in section 5 the conclusions are  
91 presented.

## 92 2 Method

93 The paper presents an approach to use dynamic exergoeconomic analysis to assess the performance of  
94 a conversion unit in an integrated energy system. Further, we propose a way to allocate the cost  
95 between heat and demand flexibility. The method is applied to a case presented in the following.

### 96 2.1 Case study

97 The case studied was a district heating island system that was designed for the Ocean Quay cruise ship  
98 terminal in Copenhagen. The system was designed to supply three terminal buildings and a large  
99 warehouse with heat for space heating and domestic hot water. The heat pump replaced the formerly  
100 implemented oil burners and has a nominal capacity of 800 kW. Figure 1 shows a sketch of the described  
101 system and all water and electricity flows in the system. The heat source for the heat pump was  
102 groundwater delivered by the groundwater (GW) pump. Further, the system comprised a stratified  
103 storage tank of 120 m<sup>3</sup>, a district heating (DH) pump and two electric boilers of 100 kW each. The heat  
104 demand, including distribution losses, was lumped into a heat demand model and it was assumed that

105 the heat pump system should supply a constant temperature of 70 °C into the DH grid (Stream 8 in  
 106 Figure 1). Table 1 summarizes the capacity of the components used in the assessed case.

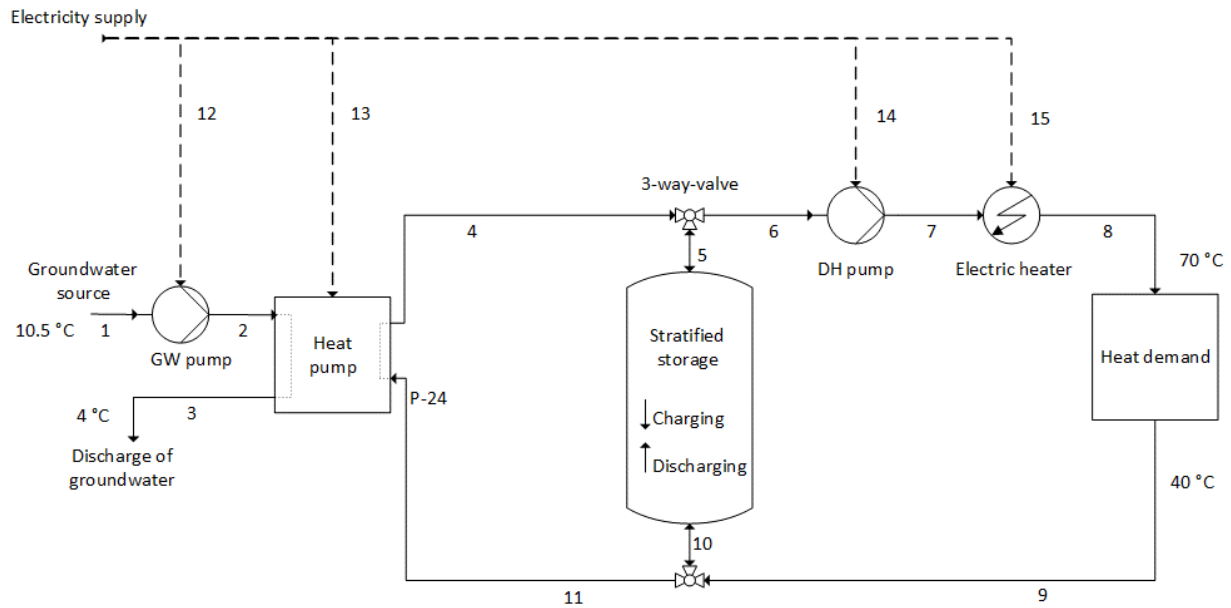


Figure 1 Sketch of the considered heat pump system in, Copenhagen, solid lines – water, dashed lines – electricity

Table 1 Specification of units in the considered system

Unit	Capacity
Heat pump minimum heating capacity	150 kW
Heat pump nominal heating capacity	800 kW
Electric boiler capacity	2 · 100 kW
District heating pump design flow	2 · 16.7 $\frac{\text{kg}}{\text{s}}$
Groundwater pump design flow	2 · 44.3 $\frac{\text{kg}}{\text{s}}$
Stratified Storage tank	120 m <sup>3</sup>



107 To compare the results on an energy basis we defined the seasonal heat pump COP and the seasonal  
 108 system coefficient of performance (SCOP) as

$$\text{COP}_{\text{season}} = \frac{Q_{\text{heat}}}{W_{\text{HP}}} \quad (1)$$

$$\text{SCOP}_{\text{season}} = \frac{Q_{\text{heat}}}{\sum_k W_k} \quad (2)$$

109 where  $Q_{\text{heat}}$  denotes the annual amount of heat delivered into the DH network,  $W_k$  is the annual  
 110 amount of electric energy supplied to component  $k$  and accordingly  $W_{\text{HP}}$  is the annual amount of  
 111 electric energy supplied to the heat pump.. In the sum all electrical components, i.e. the heat pump, the  
 112 electric heater, the groundwater pump and the DH pump were considered.

## 113 2.2 Model

114 The model was formulated in Modelica [20] and implemented in Dymola [21]. It contained seven main  
 115 component models representing a heat pump, an electric boiler, a stratified storage tank, two pumps, a  
 116 lumped heat demand model, two three-way-valves and a central control unit. Models for the heat  
 117 demand, the heat pump, the control unit and stratified storage tank are further described below. All  
 118 models were based on energy, mass and impulse balance equations. When not indicated differently,  
 119 pressure losses were neglected. The pump model was adapted from an existing model from the TIL  
 120 library [22]. The pump efficiency was implemented as a quadratic function, obtained from  
 121 manufacturer's data [23,24].

### 122 *Heat demand model*

123 The heat demand model was a simplified model of the demand side of the system. It included the  
 124 accumulated demand of all buildings and the heat losses in the distribution system. The demand was  
 125 measured demand data of the system on hourly basis for the year 2012 [25]. In practice, the heat

126 demand would be forecasted and the operation schedule of the day ahead would be optimized.  
 127 However, for the current study a simplified approach was chosen. Based on the demand data, the  
 128 required mass flow for each time step was calculated which was used to control the district heating  
 129 pump supplying the network. It was assumed that the building substations are designed to cool the  
 130 district heating water to a constant return temperature of 40 °C (Stream 9 Figure 1). The actually  
 131 supplied heat was calculated from an energy balance in the model. The system pressure loss was  
 132 estimated to be at 3 bar, independently of the flow.

### 133 *Heat pump model*

134 The heat pump was a two stage ammonia heat pump with open intercooler. It was equipped with a  
 135 piston compressor, which was controlled via a variable frequency drive. Brackish groundwater at 10.5 °C  
 136 was the heat source. It was assumed that the groundwater can be cooled to 4 °C before being  
 137 discharged into the sea.

138 A dynamic energy balance for the heat pump was used to describe the model.

$$\frac{dQ_{HP}}{dt} = \dot{Q}_{eva} + \dot{W}_{HP} + \dot{Q}_{con} \quad (1)$$

139 The term  $dQ_{HP}/dt$  represents the changed heat flow due to inertia in the heat pump.  $\dot{Q}_{eva}$  is the heat  
 140 flow in the evaporator,  $\dot{W}_{HP}$  is the power uptake of the compressor and  $\dot{Q}_{con}$  represent the condenser  
 141 heat load.

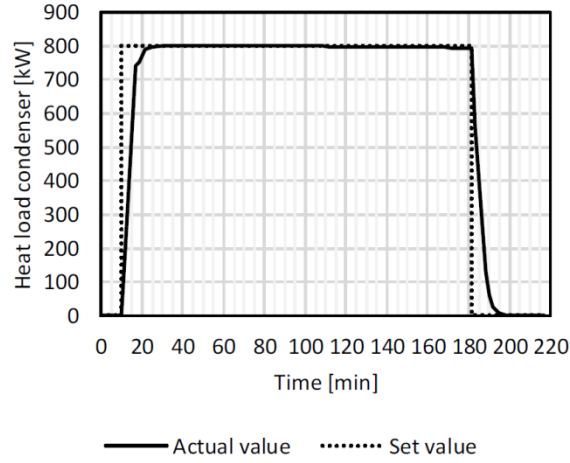


Figure 2 Steady state set value and actual value of condenser heat load for start-up and shut-down

142 The heat pump is implemented as a black box. Thus, a function for the actual heat output from the  
 143 condenser during load changes was implemented to represent the dynamic start-up and load changing  
 144 characteristics of the heat pump. Full heat production is not available during start-up compared to an  
 145 theoretic instantaneous start-up, and heat will still be rejected after shut-off of the compressor  
 146 (Figure 2). It was assumed that the dynamic heat load at the condenser follows a first order  
 147 characteristic, which was included as function for the actual heat load  $\dot{Q}_{\text{con}}$  into the model.

$$\frac{d\dot{Q}_{\text{con}}}{dt} = \begin{cases} k_1 \cdot (\dot{Q}_{\text{con,ss}} - \dot{Q}_{\text{con}}) & \text{for } (\dot{Q}_{\text{con,ss}} - \dot{Q}_{\text{con}}) > 0 \text{ (ramp - up)} \\ k_2 \cdot (\dot{Q}_{\text{con,ss}} - \dot{Q}_{\text{con}}) & \text{for } (\dot{Q}_{\text{con,ss}} - \dot{Q}_{\text{con}}) \leq 0 \text{ (ramp - down)} \end{cases} \quad (2)$$

148 The parameters  $k_1 = 0.0016$  and  $k_2 = 0.0018$  were chosen to represent a start-up time of 15 minutes  
 149 and a shut-down time of 20 minutes. The term  $\dot{Q}_{\text{con,ss}}$  represents the condenser heat load in steady  
 150 state, which was calculated from the coefficient of performance (COP) in steady state. It was assumed  
 151 that COP in steady-state depends solely on the sink and source temperatures and a given exergy  
 152 efficiency  $\epsilon_{\text{ss}}$  [26].

$$\text{COP}_{\text{ss}} = \left( 1 - \frac{T_{m,\text{source}}}{T_0} * \left( \frac{1}{\epsilon_{\text{ss}}} * \left( \frac{T_0}{T_{m,\text{sink}}} - 1 \right) + 1 \right) \right)^{-1} \quad (3)$$

$$T_{m,i} = \frac{T_{out,i} - T_{in,i}}{\ln\left(\frac{T_{out,i}}{T_{in,i}}\right)} \quad (4)$$

$$\dot{W}_{el,HP} = \frac{\dot{Q}_{con,ss}}{COP_{ss}} \quad (5)$$

153  $T_{m,i}$  is the logarithmic mean temperature and  $T_0$  is the reference state temperature.  $\epsilon_{ss}$  represents the  
 154 steady-state exergy efficiency of the heat pump. It was assumed to have a constant value of 0.5. The  
 155 part-load COP of a frequency controlled heat pump would typically increase for decreasing load,  
 156 reaching a maximum at approx. 50 % [27]. However, we assumed constant part load efficiency.  
 157 The resulting actual COP was calculated from the condenser heat load and the power uptake.

$$COP = \frac{\dot{Q}_{con}}{\dot{W}_{HP}} \quad (6)$$

158 The model further included energy, mass and impulse balance (no pressure loss) equations for the  
 159 evaporator and the condenser. The heat pump was controlled according to the desired heat output at  
 160 the condenser using an external control unit.

#### 161 *Control unit*

162 The described system was controlled using a central control unit, which contained the algorithm  
 163 according to which the heat pump, the three-way-valve, the pumps and the electric heater were  
 164 controlled. Via the three-way-valve at the top of the stratified storage tank the charging and discharging  
 165 of the tank was controlled, by setting a value for the ratio between the flow into the storage and the  
 166 flow from the HP. The pumps were controlled to deliver the necessary mass flow to the heat demand  
 167 model and the heat pump, respectively. The electric heater heated the DH supply flow to 70 °C if the  
 168 temperature supplied was lower.

169 The operation of the heat pump was based on a simple, heuristic approach, which does not utilize  
170 variations in the electricity price, but is only based on the heat demand, the state of the storage and a  
171 regulation signal. This approach was chosen to focus on the effect of the provision of ancillary services  
172 for the electricity system. The algorithm changed the mode of operation of the system according to up-  
173 and down regulation signals, which were taken from data of hourly realized up- and down-regulation  
174 from the Transmission System Operator Energinet.dk's market data from 2012 [28]. The model does not  
175 include the prices for regulating power, but aims at quantifying the true cost of providing this. The  
176 results may be compared to the actual prices in the regulating market.

177 The up- and down regulation signals from Energinet are based on the generation side, i.e. an up-  
178 regulation signal means that the current demand is too high. The heat pump would react to this by  
179 reducing the power uptake. Accordingly, a down regulation signal would cause the heat pump to switch  
180 to full load. When the storage level and the current heat demand allowed for variation of the heat pump  
181 load, the heat pump was ramped up to full load in case of a down-regulation signal and shut-off for an  
182 up-regulation. This was done using a PI-controller ( $k = 0.08$ ,  $\tau = 50$  s) where the desired heat output  
183 was the set value, the actual heat load was the input and the power uptake of the compressor was the  
184 output signal. In practice, the load of the heat pump could be increased or reduced to another value  
185 than full load or no production. However, the considered heat pump is small in terms of its electricity  
186 regulation ability and would have to be aggregated to actually act on the regulation market. Therefore,  
187 we chose to only consider the maximum provision of regulation power. Figure 3 shows a flow diagram of  
188 the control algorithm for flexible operation. If no regulation signals were considered, the algorithm  
189 would follow only the left branch (regulating signal: none). The different paths of the algorithm ended  
190 up in 4 different operation modes for the heat pump:

- 191 • HP part load = heat demand: The heat pump is operated in part load according to the heat  
192 demand.

- 193 • HP off: The heat pump is shut-off or remains off.
- 194 • HP minimum load: The heat pump is operated at lowest part load (150 kW).
- 195 • HP maximum load: The heat pump is operated at full load.

ACCEPTED MANUSCRIPT

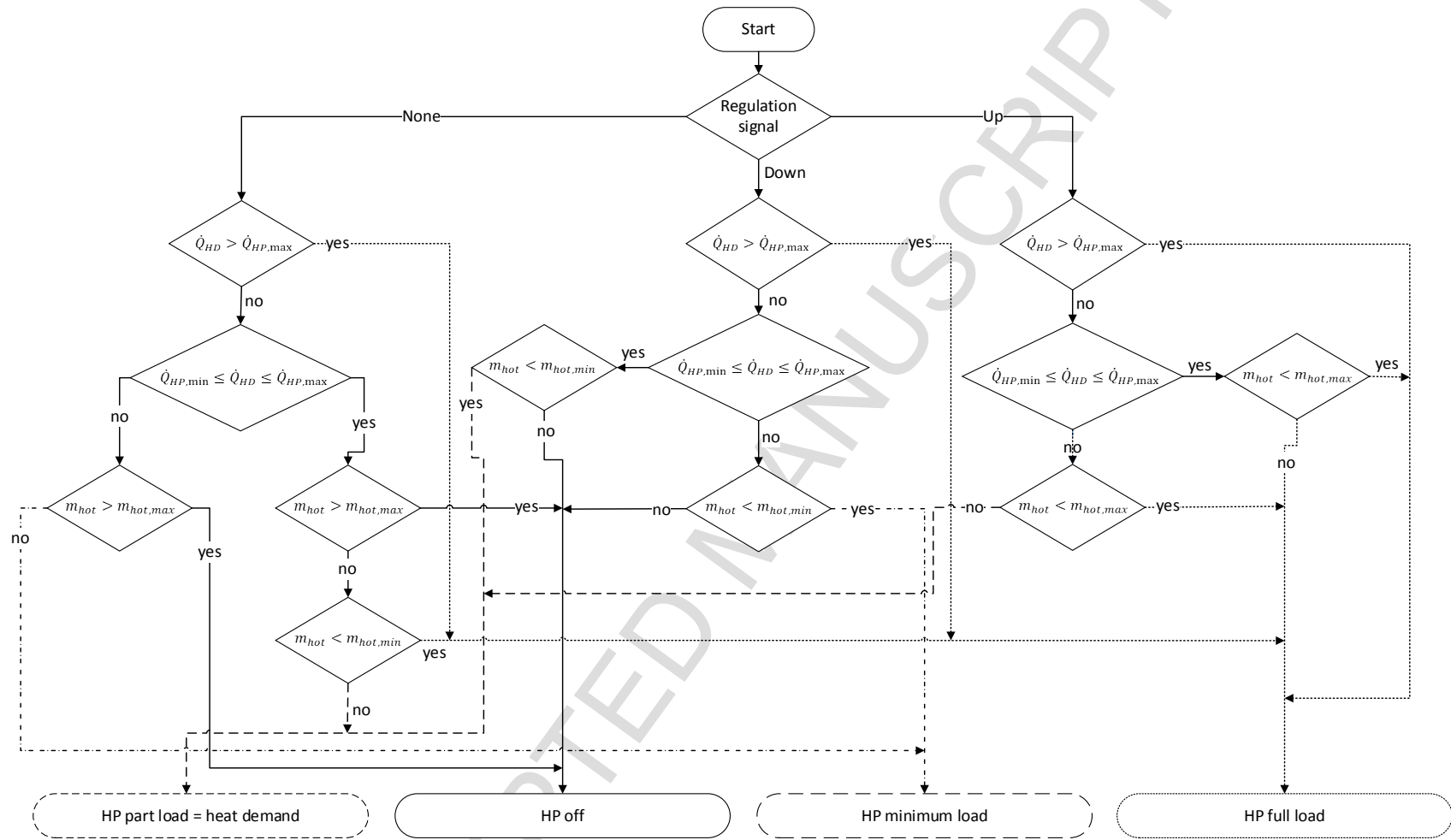


Figure 3 Structure of control algorithm for flexible operation. HD- Heat demand, HP\_min/max – Heat pump minimum load/full load, m\_hot – mass of hot water in the storage, m\_hot\_min/max – minimum/maximum mass of hot water in the storage, HD – Heat demand.

196 *Stratified storage tank*

197 The stratified storage tank was modelled using a one dimensional discretization [29] (Figure 4). The tank  
 198 was divided into 100 layers from top to bottom. For each layer dynamic mass and energy balances were  
 199 solved. It was assumed that the fluid inside each layer was ideally mixed and thus had constant  
 200 properties. Heat losses to the environment and between layers were considered. Pressure differences  
 201 across the tank were neglected as well as increased mixing between the layers during charging and  
 202 discharging. The minimum and maximum amount of hot water is limited by the inlet design and was  
 203 assumed to be 1/12 and 11/12 of the total stored mass, respectively.

### 204 2.3 Exergy analysis

205 As reference state the groundwater temperature ( $T_0 = 10.5\text{ }^\circ\text{C}$ ) at atmospheric pressure ( $p_0$   
 206  $= 1.013\text{ bar}$ ) was chosen. The groundwater temperature was assumed to be constant throughout the  
 207 year. All material streams were assumed to be water and no reactions occur at any place in the system.  
 208 So, the chemical exergy would be equal for all streams and can be neglected [17].

209 To conduct the exergy analysis of the system, balance equations were formulated for all components.

210 The balance equation for a general control volume can be formulated as

$$\frac{dE}{dt} = \sum_i \dot{m}_i \cdot e_i + \sum_j \dot{E}_{Q,j} + \sum_l \dot{W}_l - \dot{E}_L - \dot{E}_D \quad (7)$$

211 where  $E$  is the exergy content of the control volume, the first sum denotes the exergy content of the  
 212 material streams entering and exiting the control volume which is calculated as the product of mass flow  
 213  $\dot{m}$  and specific exergy  $e$ . The second sum is the sum of all exergy flows related to heat flows  $\dot{E}_{Q,j}$  and the  
 214 third sum considers power flows  $\dot{W}_l$ .  $\dot{E}_L$  is the exergy loss to the environment and  $\dot{E}_D$  denotes the  
 215 exergy destruction within the control volume. All entering flows are accounted as positive by sign  
 216 convention.



- 217 For the exergy analysis, exergy fuel and product were defined for all components (Table 2). The exergy  
 218 efficiency of every component can be calculated according to:

$$\epsilon_k = \frac{\dot{E}_{P,k}}{\dot{E}_{F,k}} \quad (8)$$

Table 2 Exergy fuel and -product and specific cost per unit of exergy fuel and product for the components used in the case study. Charging and discharging refer to charging/discharging of the storage tank. When there is no flow in or out of the tank, the equations for discharging are valid.

	Exergy fuel $\dot{E}_{F,i}/$ Specific cost per unit of exergy fuel $c_F$	Exergy product $\dot{E}_{P,i}/$ Specific cost per unit of exergy product $c_P$	Auxiliary equations
Heat pump	$\dot{E}_F = \begin{cases} \dot{W}_{13} + \frac{dE_{HP}}{dt} & \text{:if } \frac{dE_{HP}}{dt} < 0 \\ \dot{W}_{13} & \text{:else} \end{cases}$  $c_F = c_{el}$	$\dot{E}_P = \begin{cases} \dot{E}_4 - \dot{E}_{11} + \frac{dE_{HP}}{dt} & \text{:if } \frac{dE_{HP}}{dt} > 0 \\ \dot{E}_4 - \dot{E}_{11} & \text{:else} \end{cases}$  $c_P = \frac{\dot{C}_4 - \dot{C}_{11}}{\dot{E}_4 - \dot{E}_{11}}$	$c_3 = c_F$
3-way- valve	$\dot{E}_F = \begin{cases} \dot{E}_4 & \text{:charging} \\ \dot{E}_4 + \dot{E}_5 & \text{:discharging} \end{cases}$  $c_F = \begin{cases} \frac{\dot{C}_4}{\dot{E}_4} & \text{:charging} \\ \frac{\dot{C}_4 + \dot{C}_5}{\dot{E}_4 + \dot{E}_5} & \text{:discharging} \end{cases}$	$\dot{E}_P = \begin{cases} \dot{E}_5 + \dot{E}_6 & \text{:charging} \\ \dot{E}_6 & \text{:discharging} \end{cases}$  $c_P = \begin{cases} \frac{\dot{C}_5 + \dot{C}_6}{\dot{E}_5 + \dot{E}_6} & \text{:charging} \\ \frac{\dot{C}_6}{\dot{E}_6} & \text{:discharging} \end{cases}$	$c_5 = c_6$ (for charging)
DH Pump	$\dot{E}_F = \dot{W}_{14}$  $c_F = c_{el}$	$\dot{E}_P = \dot{E}_7 - \dot{E}_6$  $c_P = \frac{\dot{C}_7 - \dot{C}_6}{\dot{E}_7 - \dot{E}_6}$	
GW Pump	$\dot{E}_F = \dot{W}_{12}$  $c_F = c_{el}$	$\dot{E}_P = \dot{E}_2 - \dot{E}_1$  $c_P = \frac{\dot{C}_2 - \dot{C}_1}{\dot{E}_2 - \dot{E}_1}$	
Electric heater	$\dot{E}_F = \dot{W}_{15}$  $c_F = c_{el}$	$\dot{E}_P = \dot{E}_8 - \dot{E}_7$  $c_P = \frac{\dot{C}_8 - \dot{C}_7}{\dot{E}_8 - \dot{E}_7}$	
Stratified storage tank	$\dot{E}_F = \begin{cases} \dot{E}_5 & \text{:charging} \\ \frac{dE_{hot}}{dt} & \text{:discharging} \end{cases}$	$\dot{E}_P = \begin{cases} \frac{dE_{hot}}{dt} & \text{:charging} \\ \dot{E}_5 & \text{:discharging} \end{cases}$	$c_{10} = \frac{C_{cold}}{E_{cold}}$ (for charging)

$$c_F = \begin{cases} \dot{C}_5 & \text{:charging} \\ \frac{dC_{hot}}{dt} & \text{:discharging} \end{cases} \quad c_P = \begin{cases} \frac{dC_{hot}}{dt} & \text{:charging} \\ \dot{C}_5 & \text{:discharging} \end{cases}$$

219 *Heat pump*

220 The exergy efficiency of the heat pump was defined as the increase of exergy of the DH water in the  
 221 condenser over the power input into the compressor. As the groundwater was cooled down from the  
 222 reference state temperature in the evaporator, it's exergy content increased. However, the cold stream  
 223 was not a useful product in this case as it was discharged into the environment and represented an  
 224 exergy loss of the system. A cost can be assigned to the exergy loss by assuming that the exergy loss is  
 225 covered through the supply of a corresponding amount of fuel (auxiliary equation) [30].

226 *Three-way-valve*

227 The three-way-valve controlled the mass flow to and from the stratified storage tank. The exergy fuel  
 228 and product were different during charging or discharging of the tank. The purpose of mixing in the  
 229 three-way-valve was to vary between two different heat sources (the heat pump and the storage) and  
 230 not to heat up the stream from the storage using the stream from the heat pump. Thus the above  
 231 definition of exergy fuel and product is chosen [17].

232 *Stratified storage tank*

233 To define the exergy fuel and product of the stratified storage tank, the tank was divided into a hot and  
 234 a cold control volume (Figure 4). We assumed that the purpose of the tank is to store hot water, and  
 235 that the cold water is only used to fill up the tank volume that is not used by the hot water. Both control  
 236 volumes were thus variable in size and additional mass balances for the control volumes are needed.

$$m_{hot} + m_{cold} = \bar{\rho} \cdot V_{storage} \quad (9)$$

$$m_{hot} = \frac{N_{hot}}{N} \cdot \bar{\rho} \cdot V_{storage} \quad (10)$$

237  $m_{hot}$ ,  $m_{cold}$  denote the mass of the hot and cold control volumes, respectively.  $N_{hot}$  is the number of  
 238 layers with hot fluid which are defined as all layers with a temperature above 60 °C,  $\bar{\rho}$  is the mean water  
 239 density in the storage and  $V_{storage}$  is the overall volume of the storage tank. Calculating  $m_{hot}$  in the  
 240 presented way, has the advantage that the mass flow from the hot to the cold volume due to decrease  
 241 in temperature can be easily accounted for.

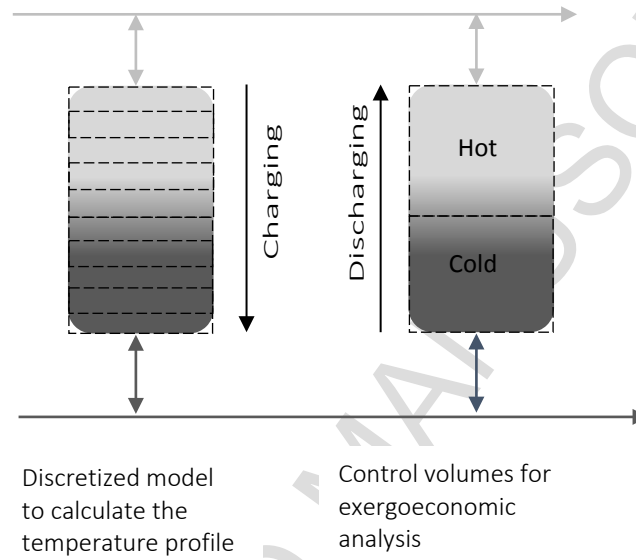


Figure 4 One-dimensional discretization of storage tank and division into hot and cold control volume

242 The exergy fuel during charging was defined as the exergy of the hot water coming in at the top of the  
 243 tank (stream 5) and the product was the increase in stored exergy inside the hot control volume of the  
 244 tank. The amount of stored exergy was calculated for both control volumes as

$$\frac{d(E_{hot} + E_{cold})}{dt} = \dot{m}_5 \cdot e_5 - \dot{m}_{10} \cdot e_{10} - \dot{E}_D \quad (11)$$

$$E_{hot} = \sum_{n=1}^{N_{hot}} (m_n \cdot e_n) \quad (12)$$

245 where  $E_{hot}$ ,  $E_{cold}$  denote the exergy stored in the hot and cold volume respectively.  $m_n$  is the mass and  
 246  $e_n$  the specific exergy of layer  $n$ . The volume work due to variation of the control volume size was found

247 to be small compared to the exergy of stored heat and was neglected. The heat loss from the storage is  
 248 accounted for as exergy destruction  $\dot{E}_D$ . Assuming that the water in the tank behaves as an ideal liquid,  
 249 the specific exergy  $e_n$  for every discretization layer can be calculated from temperatures obtained from  
 250 the energy balances for every control volume [31].

$$e_n = c_{p,H_2O} \cdot (T_n - T_0) - T_0 \cdot c_{p,H_2O} \cdot \ln\left(\frac{T_n}{T_0}\right) \quad (13)$$

251 An overall exergy efficiency for the storage was calculated as the ratio of the integrals of the output  
 252 from - and the input into the hot control volume.

$$\epsilon_{storage,tot} = \frac{\int \dot{E}_{5,out} dt}{\int \dot{E}_{5,in} dt} \quad (14)$$

253 *System exergy efficiency*

254 The exergy efficiency of the overall system for every time step had to take the storage of exergy in the  
 255 storage tank into consideration. During charging the exergy stream into the storage represented a  
 256 product of the system, whereas during discharging the exergy stream out of the tank was a fuel to the  
 257 overall system:

$$\epsilon_{system} = \begin{cases} \frac{\dot{E}_{heat} + \frac{d(E_{hot} + dE_{cold})}{dt}}{\sum_k \dot{W}_k} & \text{if charging} \\ \frac{\dot{E}_{heat}}{\sum_k \dot{W}_k + \left| \frac{dE_{hot} + dE_{cold}}{dt} \right|} & \text{if discharging} \end{cases} \quad (15)$$

258 The annual mean exergy efficiency was calculated according to the following equation.

$$\epsilon_{\text{system,tot}} = \frac{E_{\text{heat}}}{\sum_k W_k} \quad (16)$$

259  $E_{\text{heat}}$  denotes the overall amount of exergy of heat supplied per year and  $W_k$  is the overall amount of  
 260 electric energy of component  $k$  per year.

## 261 2.4 Exergoeconomic analysis

262 Within an exergoeconomic analysis a cost is assigned to all exergy streams. This allows to determine the  
 263 cost of exergy destruction in every component, which can give useful information about the sources of  
 264 costs throughout the system and how they can be lowered [17].

265 In order to assign a cost to every exergy stream a dynamic cost balance for every component was set up,

$$\frac{dC}{dt} = \sum_i \dot{C}_i + \sum_k c_{\text{el}} \cdot \dot{W}_k + \dot{Z} \quad (17)$$

266  $C$  denotes the cost that accumulates within the component,  $\dot{C}_i$  is the cost streams associated with  
 267 material streams,  $c_{\text{el}}$  is the electricity cost in the respective time step and  $\dot{Z}$  denotes the levelized cost  
 268 stream of the component. The cost stream of the component includes investment cost, capital cost, and  
 269 operation and maintenance costs for the estimated lifetime of the respective component. It was  
 270 calculated as described in [17]. However, the cost was not levelized to the full load hours per year but to  
 271 the actual operation hours per year and  $\dot{Z}$  was only considered when the respective component was in  
 272 operation. The DH network was existent and we assumed that the operation and maintenance costs are  
 273 the same for any kind of heat supplying system. Thus, the costs of the DH network were neglected in the  
 274 present work.

275 The economic data used to calculate  $\dot{Z}$  is summarized in Table 3. An average annual discount rate of 4 %  
 276 and a nominal escalation rate of 2 % for operation and maintenance cost was assumed [32].

277 The cost of electricity used in this study is historic spot market prices for Eastern Denmark 2012 from  
 278 NordPool [33]. 59 DKK/MWh transmission net tariff and 24 DKK/MWh system tariff were included [33].  
 279 Administration, and trading and unbalance cost were assumed to be 3 DKK/MWh and 2 DKK/MWh,  
 280 respectively.

Table 3 Economic data case study

Unit	Capacity	Total capital investment [DKK]	Plant economic life [a]	Operation hours per year [h/a]		Fixed O&M cost 1st year [DKK]	Source
				Non-flex.	flexible		
Heat pump	800 kW	560.000	25	7527	6917	3000	[34]
El. heater	200 kW	150.000	20	1233	3000	220	[34]
DH pump	2×16.7 kg/s	30.000	10	8760	8760	440	[23]
GW pump	2×44.3 kg/s	40.000	10	7527	6917	440	[23]
Storage tank	120 m <sup>3</sup>	31.200	40	8760	8760	700	[34]
Drilling		900.000	40	7527	6917	18000	[35]

## 281 2.5 Allocation of cost

282 The allocation of cost to both products of the heat pump system, i.e. heat supply and provision of  
 283 demand flexibility, is a central question when operating energy conversion units in an integrated energy  
 284 system. The characteristics of both products are different. Heat is an output from the system and so is  
 285 the related heating service. Electricity is an input into the system, but the corresponding flexibility is a  
 286 service provided by the system, see Figure 5. The cost of providing flexibility is not directly connected to  
 287 the electricity stream and all extra cost will be reflected in the heat generation cost. However, as the  
 288 source of cost difference was not the supply of heat but the additional exergy destruction due to the  
 289 provision of flexibility, the cost should be allocated accordingly. The exergy destruction related to  
 290 flexible operation does not only occur at the same time as the provision of regulation power. Thus, we  
 291 chose an integral approach to determine the cost related to flexible operation.

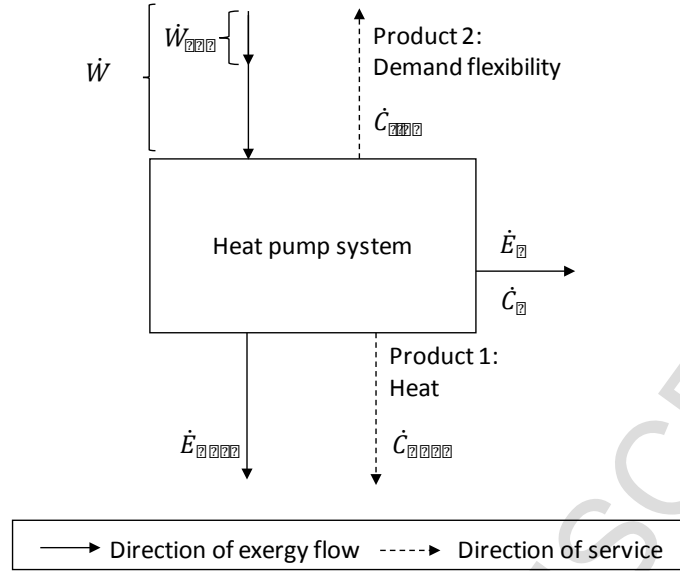


Figure 5 Direction of energy flow and product delivery for a conversion unit in an integrated energy system

292 As the flexibility provided to the electricity sector was not directly connected to an exergy product  
 293 stream, the cost was allocated according to the increased exergy destruction due to flexible operation,  
 294 which was given as the difference between the overall exergy destruction in the flexible and the non-  
 295 flexible case. The specific cost per unit of exergy was calculated as:

$$c_{\text{ex}} = \frac{(C_{\text{heat}} + C_L)}{E_{\text{heat}} + (E_{D,\text{flex}} - E_{D,\text{nonflex}})} \quad (18)$$

296 The overall cost exiting the system is the sum of the integrated cost of heat  $C_{\text{heat}}$  and of the exergy loss  
 297  $C_L$ .  $E_{\text{heat}}$  is the integrated amount of exergy supplied as heat to the DH grid and  $E_{D,\text{flex}}$ ,  $E_{D,\text{nonflex}}$  is the  
 298 overall exergy destruction caused during flexible operation and non-flexible operation, respectively. All  
 299 values were calculated by integrating the respective cost and exergy flow rates over one year.

300 Knowing the overall cost related to flexible operation per year, the specific cost per unit of regulating  
 301 energy  $W_{\text{reg}}$  provided can be determined.

$$c_{\text{flex}} = \frac{c_{\text{ex}} \cdot (E_{D,\text{flex}} - E_{D,\text{nonflex}})}{W_{\text{reg}}} \quad (19)$$

302 In order to be able to compare different units, we also calculate the annual specific cost of flexible  
 303 operation per kW installed electric capacity  $\dot{W}_{\text{installed}}$ .

$$c_{\text{flex, capacity}} = \frac{c_{\text{ex}} \cdot (E_{D,\text{flex}} - E_{D,\text{nonflex}})}{\dot{W}_{\text{installed}} \cdot 8760 \cdot 3600 \text{ s/a}} \quad (20)$$

304 The heat generation cost is calculated from the overall cost delivered into the DH grid over the overall  
 305 amount of heat.

$$c_{\text{heat}} = \frac{c_{\text{ex}} \cdot E_{\text{heat}}}{Q_{\text{heat}}} \quad (21)$$

### 306 3 Results

307 To calculate the performance of the system when operated flexibly the system was simulated and the  
 308 exergoeconomic analysis was carried out for two different cases:

- 309 A. Non-flexible operation– the heat pump is not operated according to regulation requests from  
 310 the grid, but only according to heat demand. This means the heat pump is mostly operating in  
 311 part load.
- 312 B. Flexible operation according to regulatory signal – the heat pump is controlled according to the  
 313 heat demand, the state of storage and a regulatory signal to provide flexibility. This control  
 314 strategy was presented previously in chapter 2.2, Figure 3.

315 Figure 6 shows the heat load at the heat pump condenser for the non-flexible and flexible operation.  
 316 The non-flexible operation followed the heat demand apart from the periods, where the heat demand  
 317 was lower than the lowest allowable part load of the heat pump (150 kW). In that case, the heat pump



318 was operated at minimum part-load until the storage was filled to the maximum, then the heat demand  
 319 was supplied from the storage and the heat pump was switched off until the storage was emptied.  
 320 In the case of flexible operation the heat pump load changed frequently. When down- or up-regulation  
 321 was requested, the system ramped up to full load or shut down, if possible. When there was no  
 322 regulation signal, the heat load at the condenser followed the heat demand.

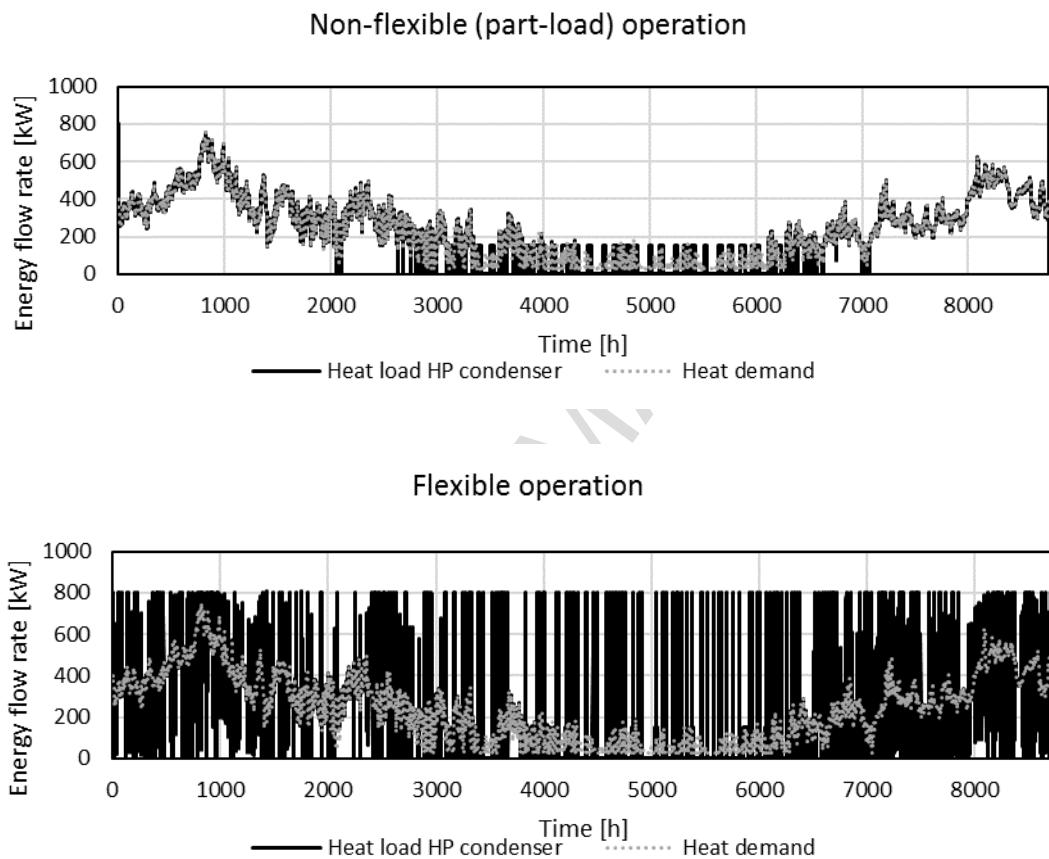


Figure 6 Heat load at heat pump condenser and heat demand for non-flexible operation and flexible operation for one year (2012)

323 The overall power uptake was higher for flexible operation (Table 4). This was mainly due to reheating  
 324 the water from the storage in the electric heater. The electric heater consumption increased from 37  
 325 MWh/year to 85 MWh/year. The power uptake of the heat pump was slightly lower during flexible

326 operation. The seasonal heat pump COP was the same for both operation modes, whereas the seasonal  
 327 SCOP was lower for the flexible case.

328 The overall exergy input into the system is given as the sum of all electric energy inputs into the system.  
 329 The exergy provided to the heat pump accounts for 84.5 % and 79.4 % of the overall exergy input in the  
 330 non-flexible and flexible case, respectively.

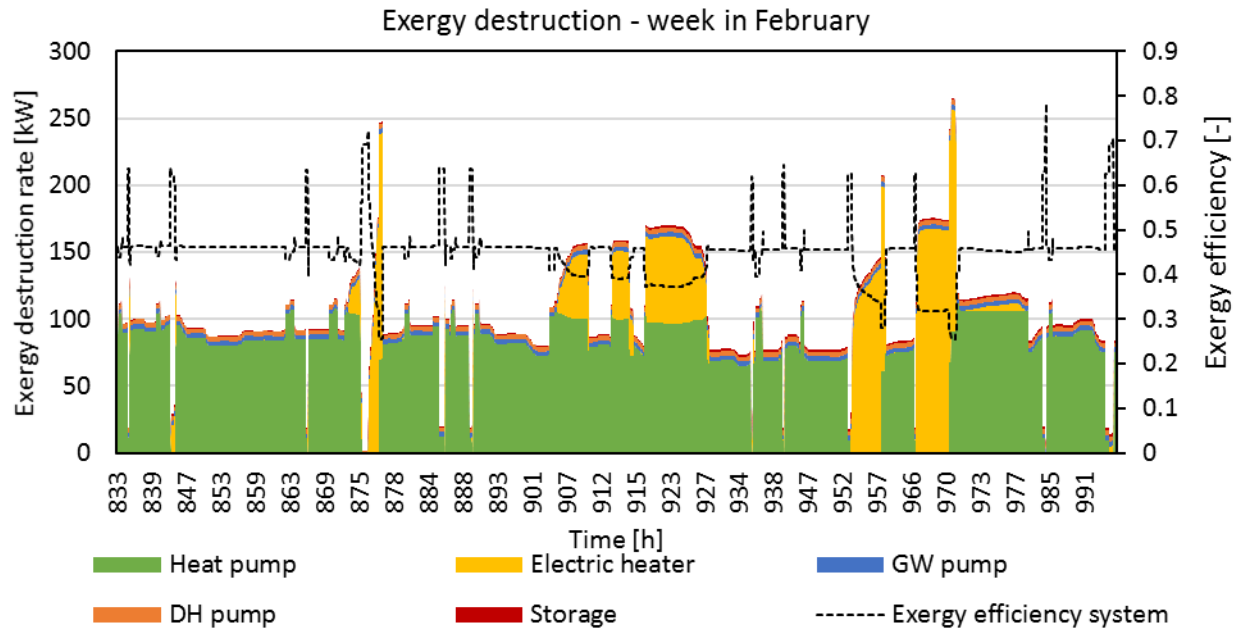
Table 4 Energetic performance indicators

		Non- Flexible operation	Flexible operation
Heat pump electric energy consumption	[MWh/a]	582	577
Electric heater electric energy consumption	[MWh/a]	37	85
GW pump electric energy consumption	[MWh/a]	40	35
DH pump electric energy consumption	[MWh/a]	30	30
Total electric energy consumption	[MWh/a]	689	728
Heat supplied to DH system	[MWh/a]	2125	2125
Overall heat loss within the conversion system	[MWh/a]	5.9	41.2
Seasonal heat pump COP	[-]	3.60	3.60
Seasonal system COP (SCOP)	[-]	3.09	2.92
Exergy of heat	[MWh/a]	293	293
Total exergy destruction	[MWh/a]	360	399
Overall exergy loss	[MWh/a]	43.6	43.4
Overall exergy efficiency	[%]	42.6%	40.3%

### 331 3.1 Exergy analysis

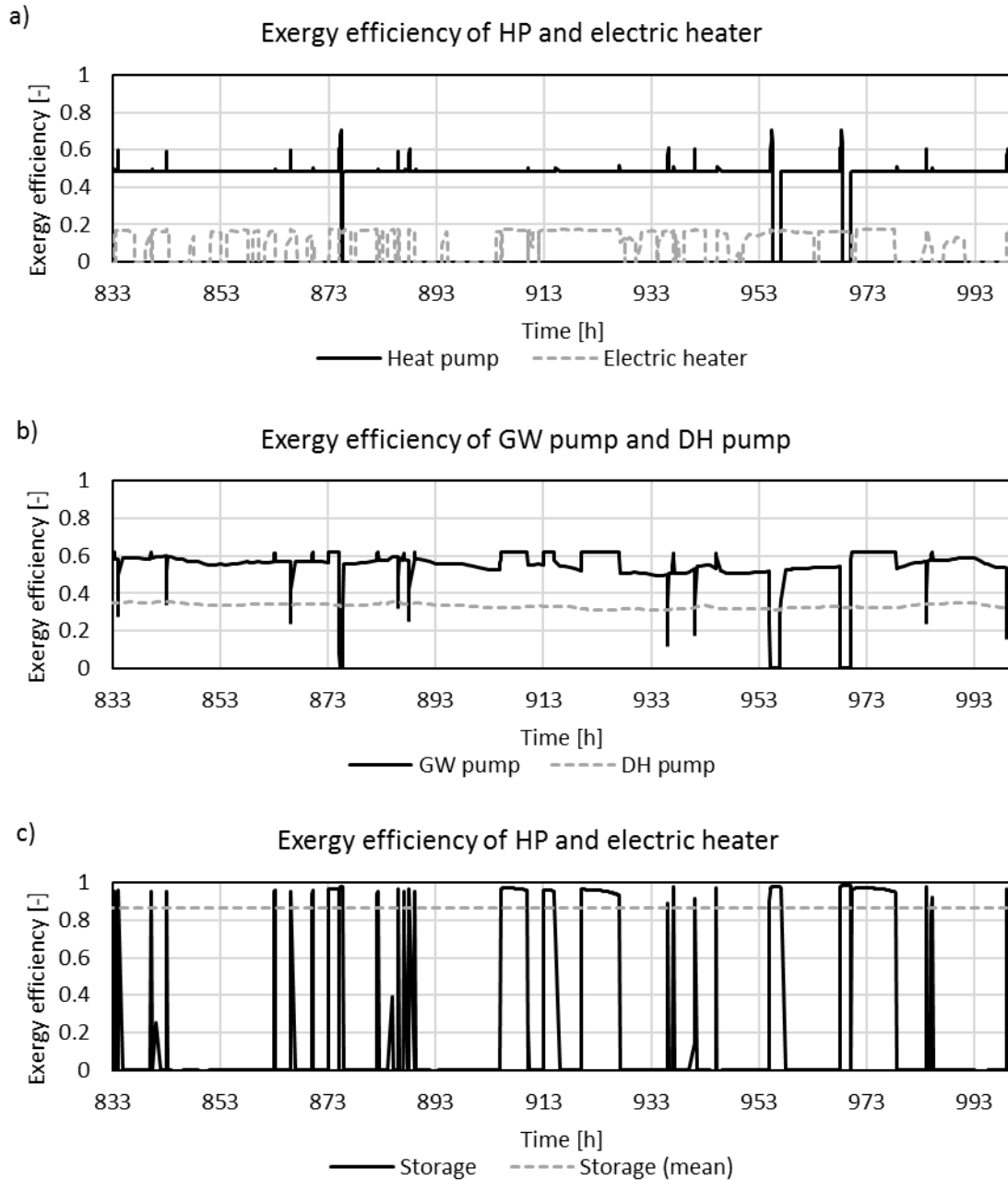
332 **Error! Reference source not found.** shows the exergy destruction within the major components for a  
 333 week in February. When the heat pump turned on, the exergy destruction in the heat pump increased  
 334 rapidly and leveled out to a steady state value. The exergy destruction of the heat pump increased with  
 335 the overall power input. When the heat pump turned off, the exergy destruction in the heat pump  
 336 decreased to zero. The exergy efficiency peaked at these times because the heat supplied from the  
 337 upper layers of the storage had a high enough temperature to supply the DH grid directly. When the

338 temperature from the storage dropped, the electric heater was turned on to heat the supply flow to the  
 339 desired temperature. The exergy efficiency decreased accordingly.



340 *Figure 7 Exergy destruction (ED) rates during flexible operation for major components*

341 The component exergy efficiencies are presented in Figure 8 for the same week. The heat pump exergy  
 342 efficiency was constant during operation (Figure 8 (a)). Peaks only occurred during ramping and shut-off.  
 343 This is due to the heat stored in the heat pump components, which is still available during shut-down..  
 344 The exergy efficiency of the electric heater is lower than the HP efficiency with approx. 17 %.  
 345 The exergy efficiency of the groundwater pump was highest when the heat pump was operated at full  
 346 load, i.e. at nominal conditions. Accordingly, the exergy efficiency decreased with decreasing mass flow.  
 347 The exergy efficiency of the storage was above 90 % when the storage was charged or discharged  
 348 (Figure 8 (c)). Losses from the storage also occurred when the storage was not operated. Thus, the mean  
 349 exergy efficiency of the storage was calculated as approx. 86.3 %.



350

Figure 8 Exergy efficiency of major components for flexible operation

351 Figure 9 shows the exergy content of the storage for the first thousand hours of the year for flexible  
 352 operation. The amount of exergy stored as hot water increased during charging and the exergy content  
 353 of the cold water decreased accordingly. When the storage was not charged or discharged over a longer  
 354 period, the exergy content decreased slowly due to heat losses.

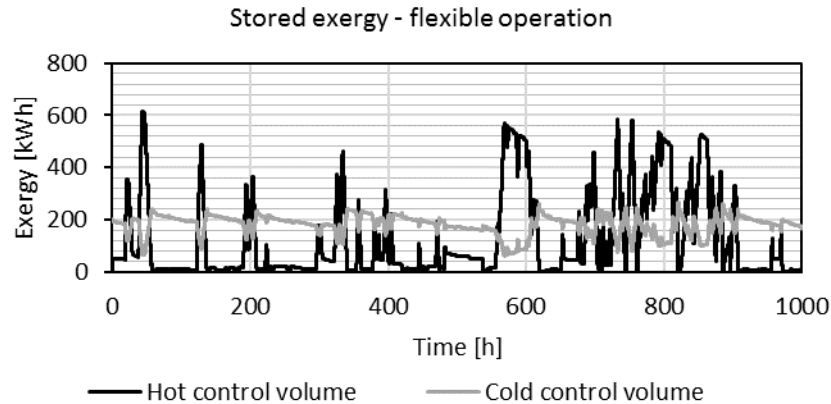


Figure 9 Exergy content of hot and cold control volume of the stratified storage tank for the first 1000 hours of the year 2012

### 355 3.2 Exergoeconomic analysis

356 Figure 10 shows the condenser load of the heat pump and the overall specific cost per unit of exergy  
 357 that was delivered into the DH system. Further, the cost of electricity is shown. The yearly average for  
 358 eastern Denmark for the year 2012 was 0.3757 DKK/kWh including the tariffs given in section 2.4.

359 The specific cost per unit exergy of the non-flexible operation followed the development of the  
 360 electricity cost (Figure 10). In the flexible operation case, the specific cost increased when the heat  
 361 pump was turned off, as the heat had to be delivered from the storage tank and reheated in the electric  
 362 boiler. The flow taken from the storage tank had a higher specific cost than that fed into it due to the  
 363 cost of exergy destruction in the tank and the levelized cost of the tank. The cost was accounted to the  
 364 exergy stored in the warm control volume of the tank. The exergy destruction and levelized cost of the  
 365 electric boiler further increased the specific cost. The specific cost did not differ significantly between  
 366 the flexible and non-flexible operation while the heat pump is running. The mean specific fuel cost (spot  
 367 market prices) during regulation was found to be slightly higher than the yearly average.

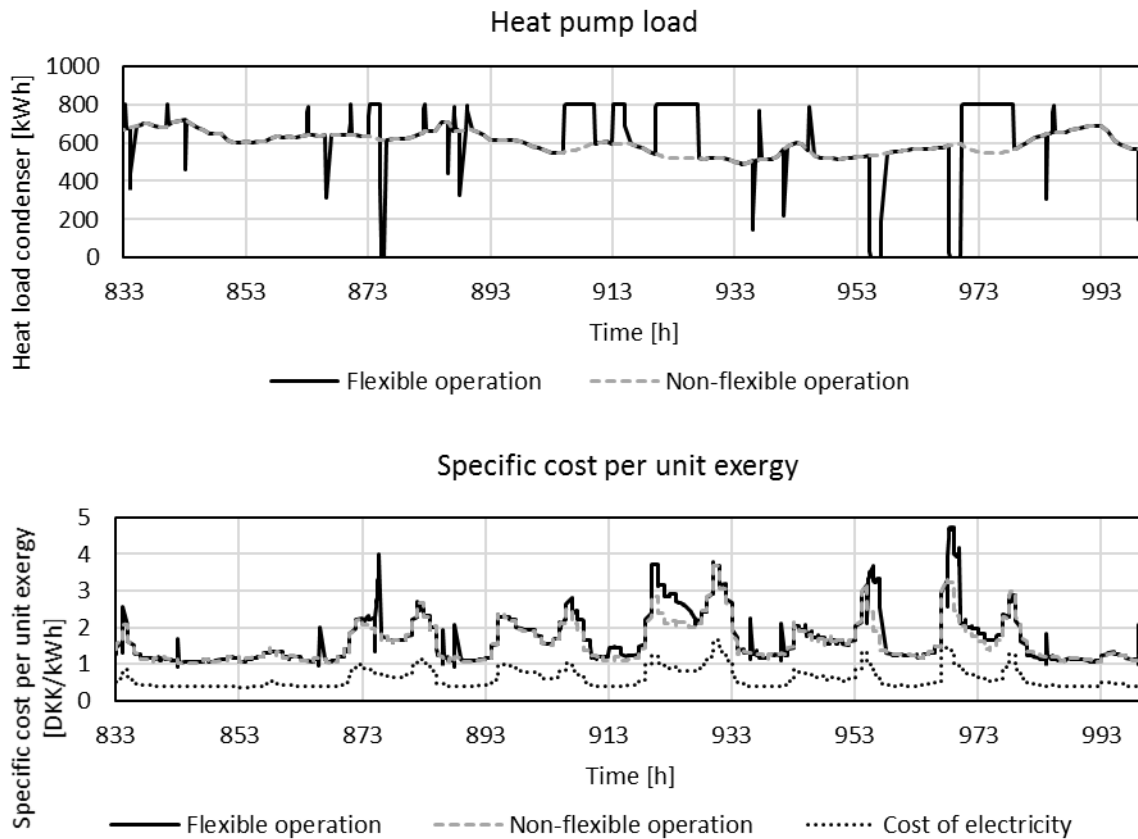


Figure 10 Heat load condenser, overall product cost for non-flexible and flexible operation and cost of electricity for a week in February 2012

368 The regulation energy that was available from the heat pump system is shown in Table 5. The response  
 369 rate given here is the ratio between the time where the system reacted to a regulation signal and the  
 370 time where the system received a regulation signal. The response rate was lower for down-regulation,  
 371 while the overall regulation energy was approx. six times larger than for up-regulation.

372 The specific cost of heat was lower for the flexible operation compared to the non-flexible operation, as  
 373 12 % of the overall product cost were assigned to the provision of flexibility and the overall cost were  
 374 reduced. The specific cost per kWh of regulation energy was 0.660 DKK/kWh. This corresponds to an  
 375 annual cost of flexible operation per kW installed capacity (only heating units) of 65 DKK/kW/a. The  
 376 average difference between the balancing price and the electricity spot price, i.e. the possible benefit by

377 providing balancing services, was 0.133 DKK/kWh for down-regulation and 0.208 DKK/kWh for up-  
 378 regulation for 2012 [28]. The corresponding values for 2017 were found to be even lower with 0.093  
 379 DKK/kWh for down-regulation and 0.153 for up-regulation. During individual hours the benefit of  
 380 performing the service could be higher. For 2012 it was found that in 180 h out of 3101 h where  
 381 balancing power was needed the benefit provided was larger than 0.660 DKK/kWh, this corresponds to  
 382 5.8 % of the hours where balancing services were provided.

Table 5 Amount of regulation energy and heat and specific cost of both products

	Non- flexible operation	Flexible operation	Flexible operation - Winter	Flexible operation - Spring	Flexible operation - Summer	Flexible operation - Autumn
Heat [MWh/a]	2125	2125	965	540	155	464
Up-regulation [MWh/a]	0	67.8	18.5	14.2	15.6	19.5
Down-regulation [MWh/a]	0	11	0.99	0.72	5.49	4.02
Response rate Down-regulation [%]	0	37%	33%	48%	34%	39%
Response rate Up-regulation [%]	0	67%	27%	69%	100%	76%
Specific heat cost [DKK/kWh]	0.219	0.184	0.168	0.181	0.303	0.186
Cost of flexibility [DKK/kWh]	0	0.660	1.079	0.830	0.018	0.695
Overall cost [DKK]	465000	443000	183000	110000	47000	102000
Overall exergy of heat [MWh]	293	293	133	75	21	64
Overall exergy loss [MWh]	44	43	20	11	3	9
Overall exergy destruction [MWh]	360	399	160	103	44	93
Additional exergy destruction [MWh]		39	17	9	0	12

383 The overall cost input into the system is 443000 DKK/a for flexible operation and 464000 DKK/a for non-  
 384 flexible operation. 37 % and 43 % of the overall cost of flexible and non-flexible operation, respectively,  
 385 are the levelized cost of operation. The remaining part is the fuel cost of the system.

386 The exergy destruction and the related cost are presented in Figure 11 and Figure 12. The exergy  
 387 destruction of the heat pump was very similar for both scenarios. This indicates that the increased  
 388 exergy destruction during load changes did not have a significant influence on the overall exergy

389 destruction of the heat pump. The exergy destruction in the groundwater pump was lower in the case of  
 390 flexible operation, due to part-load operation.

391 The cumulated exergy destruction in the electric boiler was higher during flexible operation compared  
 392 to non-flexible operation. This is due to an increased amount of heat, which was supplied from the  
 393 storage and had to be heated up to fulfill the requirement of 70 °C supply temperature. The exergy  
 394 destruction in the DH pump was similar for both cases, as the heat demand, and thus the mass flow rate  
 395 were the same.

396 The exergy destruction in the storage occurs mainly due to heat losses and is low compared to the other  
 397 components. The cost of exergy destruction in the storage was responsible for 16 % and 7 % of the  
 398 overall cost of exergy destruction in flexible and non-flexible operation mode, respectively. The cost  
 399 related to the exergy destruction in the storage was a larger share of the overall cost. This occurred as  
 400 the fuel of the storage was the warm inlet, which had a high specific cost due to the cost of the  
 401 upstream components assigned to it.

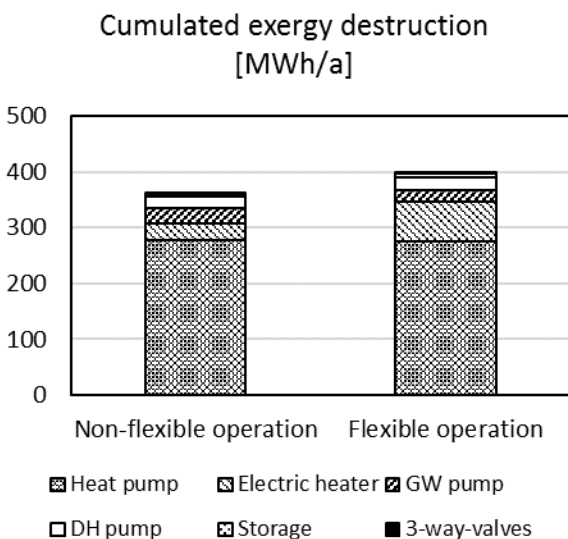


Figure 11 Overall exergy destruction of all components per year for flexible and non-flexible operation

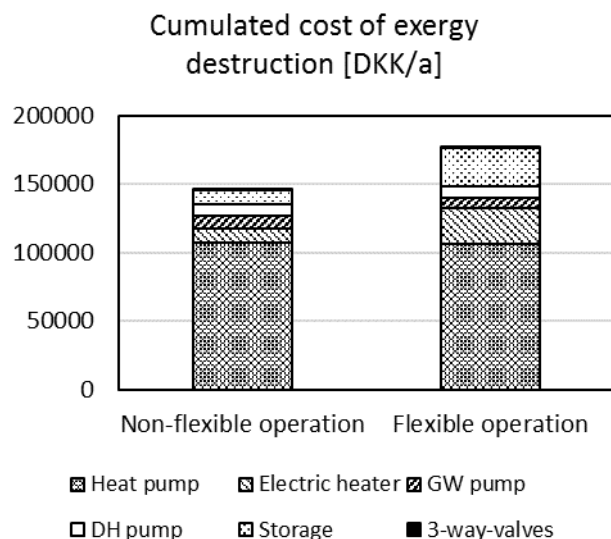


Figure 12 Overall cost of exergy destruction of all components per year for flexible and non-flexible operation



### 402 3.3 Influence of heat pump capacity

403 The system assessed here, was oversized for the given heat demand. This was done with the aim to be  
404 able to operate the system very flexibly. The simulation was repeated for an increase and decrease of  
405 the heat pump capacity of 100 kW each, keeping all other components and the heat demand the same.  
406 The results (Figure 13) indicated that the specific cost of heat is almost constant for all three cases and  
407 the overall cost per year increases slightly with increasing HP capacity. Whereas, the specific cost of  
408 flexibility decreases considerably with increasing HP capacity. This is caused by two effects. Firstly, an  
409 increase in the additional exergy destruction due to flexible operation for larger heat pump capacities  
410 leads to a decrease in the specific cost per unit exergy. Secondly and more importantly, the amount of  
411 regulation energy provided increases with increased heat pump capacity.

412 The results for the overall exergy destruction and the additional exergy destruction due to flexible  
413 operation increased slightly for increased HP capacity. This is due to the lower minimum part-load  
414 capacity of the smaller heat pump and thus a higher share of heat that is directly supplied from the heat  
415 pump, avoiding exergy destruction in the storage and the electric boiler.

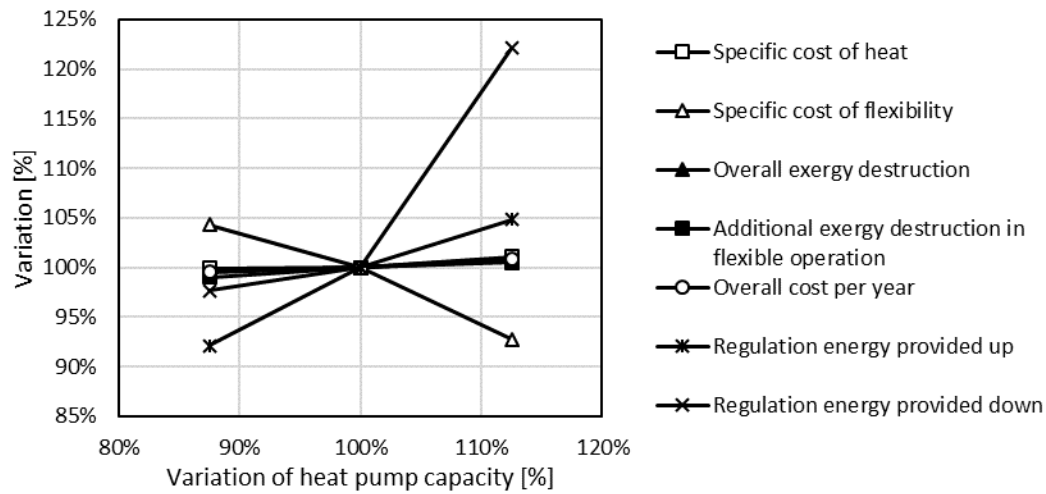


Figure 13 Variation of specific product cost, response rate and exergy destruction in % over the heat pump capacity in %

#### 416 4 Discussion

417 A method was presented to value the two products of a heat pump system using a dynamic  
 418 exergoeconomic analysis. The allocation of cost to the provision of ancillary services was based on the  
 419 additional exergy destruction in the system. We found that this approach is well suited as it resembles  
 420 the common exergy costing method closely, e.g. [30], and at the same time the problem of the different  
 421 directions of exergy flow and service provision (Figure 5) can be handled. Allocating the cost in the  
 422 presented way, a cost could also be assigned to the flexibility when the overall fuel cost is be lower than  
 423 in the reference case. The applied approach is based on exergoeconomic theory. Other approaches  
 424 based on economics or more heuristic assumptions would also be possible and may reach other costs of  
 425 the flexibility.

426 For the case study of a heat pump island system the flexible operation of the system caused higher  
 427 exergy destruction and thus fuel consumption. The overall fuel cost and the specific fuel cost were  
 428 found to be higher during regulation. This is due to the difference between the trends of the electricity  
 429 spot market price and the regulation requests found in the data for Eastern Denmark in 2012. Also, the

430 control algorithm did not consider any kind of optimization, but the system would react to a regulation  
431 request whenever possible. In this case the difference between the overall cost for flexible and non-  
432 flexible operation was approx. 21000 DKK/a.

433 Further, using the spot market price for the calculation implicates that a perfect prediction of the heat  
434 demand can be made. This is of course not possible in reality. The spot market price is also used to  
435 calculate the cost during regulation, thereby the cost difference between the flexible and non-flexible  
436 case is indeed an opportunity cost of providing flexibility. The comparison showed that the obtainable  
437 price at the balancing price was in most cases lower than the additional cost due to losses in the storage  
438 and the electric boiler.

439 The additional exergy destruction was mainly caused by heat losses in the storage, which led to  
440 reheating of the DH forward flow and thus exergy destruction in the electric boiler. This result  
441 reconfirms findings of previous studies on individual HP systems [36,37]. Reducing heat losses in the  
442 storage and the need for reheating, will improve the systems efficiency.

443 No significant difference in the exergy destruction of the heat pump was found. This is related to the  
444 assumption that part load characteristics of the heat pump are not considered. The part load  
445 performance depends on the capacity control type of the compressor [27], as well as the design of the  
446 heat exchangers.

447 The assumption that a largely overdimensioned system can provide more flexibility made when  
448 designing the system correlates with the results of the parameter variation that showed that the  
449 amount of regulation energy provided increased with increased HP capacity. On the contrary, both the  
450 overall cost per year and the exergy destruction in the system increase for larger HPs. Thus, the  
451 examination of the optimal component sizes for systems that are designed to provide flexibility may be  
452 a topic for further analysis.

453 The presented work gave an insight into the effect of providing ancillary services on the conversion unit,  
454 in this case a heat pump system. The advantage of this approach is that the actual thermodynamic and  
455 economic effect of providing flexibility to another sector can be assessed. In this way it is possible to  
456 assess the additional amount of electricity used and the part of the conversion units cost that is caused  
457 by providing another product. This is valuable information for the heat pump operator and it adds a  
458 different perspective to the discussion about how flexibility should be valued. So far the overall system  
459 benefit was mostly discussed (e.g. [4], [15], [38]) and the actual effect on the conversion unit was not  
460 considered.

## 461 5 Conclusion

462 Energy conversion units are an essential part of integrated energy systems. They are able to connect  
463 different sectors and provide services to both of them. In the case of electricity and heating sector, the  
464 conversion units provide heat to the heating system while acting as flexible demand for the electricity  
465 sector. A method to assess the impact of flexible operation of a heat pump system was presented,  
466 where allocation of the cost of both the heating and the flexibility products was based on a dynamic  
467 exergoeconomic analysis.

468 The method was applied to a heat pump island system located in Copenhagen. We found that operation  
469 according to regulation request resulted in higher exergy destruction and higher overall cost of the  
470 system. The additional exergy destruction was mainly caused by heat losses in the storage and reheating  
471 of the forward stream. The cost allocated to the flexible operation was 12 % of the overall cost of the  
472 system.

473 Overall, the method gives important insights into the effect of integrating energy systems on the energy  
474 conversion units and can thus support the decision making process when considering how to design and  
475 operate a conversion unit.

476 **Acknowledgements**

477 This research project is financially funded by EUDP (Energy Technology Development and  
478 Demonstration) under the project "EnergyLab Nordhavn - New Urban Energy Infrastructures" (project  
479 number: 64014-0555).

ACCEPTED MANUSCRIPT

## Nomenclature

### Abbreviations

COP	Coefficient of performance
DH	District heating
El.	Electric
GW	Groundwater
SCOP	Seasonal system COP

### Symbols

$C$	Cost	[DKK]
$c$	Specific cost per unit exergy	[DKK/J]
$\dot{C}$	Cost stream	[DKK/s]
$c_{p,H_2O}$	Heat capacity water	[J/(kg*K)]
$E$	Exergy	[J]
$e$	Specific exergy per unit mass	[J/kg]
$\dot{E}$	Exergy stream	[W]
$k_1, k_2$	Parameters ramp-up function	[-]
$\dot{m}$	Mass flow	[kg/s]
$m$	Mass	[kg]
$N$	Number of discretization layers	[-]
$p$	Pressure	[bar]
$Q$	Heat	[J]
$\dot{Q}$	Heat flow rate	[W]
$T$	Temperature	[K]
$t$	Time	[s]
$T_{m,i}$	Logarithmic mean temperature for stream i	[K]
$V$	Volume	[m <sup>3</sup> ]
$\dot{W}$	Electric power	[W]
$\dot{Z}$	Levelized cost of capital investment, and operation and maintenance	[DKK/s]

### Greek symbols

$\epsilon$	Exergy efficiency	[-]
$\bar{\rho}$	Mean water density	[kg/m <sup>3</sup> ]

### Subscripts

0	Reference state
capacity	Per installed capacity
cold	Related to cold control volume of the tank
con	Condenser
$D$	Destruction

el	Electricity
eva	Evaporator
ex	Per unit of exergy
<i>F</i>	Fuel
flex	Flexible operation
heat	Heat supply into DH grid
hot	Related to hot control volume of the tank
HP	Heat pump
<i>i</i>	Material stream indicator
in	Inlet
installed	Installed capacity
<i>j</i>	Heat flow indicator
<i>k</i>	Component indicator
<i>L</i>	Loss
<i>l</i>	Electricity flow index
<i>max</i>	Maximum capacity
<i>min</i>	Minimum capacity
<i>n</i>	Discretization layer indicator
nonflex	Non-flexible operation
out	Outlet
<i>P</i>	Product
reg	Regulation energy
season	Seasonal
ss	Steady state
storage	Stratified storage tank
system	Conversion system
tot	Yearly mean value

481 **References**

- 482 [1] Lund H, Mathiesen BV. Energy system analysis of 100% renewable energy systems—The case of  
483 Denmark in years 2030 and 2050. *Energy* 2009;34:524–31. doi:10.1016/j.energy.2008.04.003.
- 484 [2] Mathiesen BV, Lund H, Connolly D, Wenzel H, Østergaard PA, Möller B, et al. Smart Energy  
485 Systems for coherent 100% renewable energy and transport solutions. *Appl Energy*  
486 2015;145:139–54. doi:10.1016/j.apenergy.2015.01.075.
- 487 [3] Lund H, Werner S, Wiltshire R, Svendsen S, Thorsen JE, Hvelplund F, et al. 4th Generation District  
488 Heating (4GDH): Integrating smart thermal grids into future sustainable energy systems. *Energy*  
489 2014;68:1–11. doi:10.1016/j.energy.2014.02.089.
- 490 [4] Mathiesen BV, Lund H. Comparative analyses of seven technologies to facilitate the integration of  
491 fluctuating renewable energy sources. *Renew Power Gener IET* 2008;3:190–204. doi:10.1049/iet-  
492 rpg.
- 493 [5] David A, Mathiesen BV, Averfalk H, Werner S, Lund H. Heat Roadmap Europe: Large-Scale Electric  
494 Heat Pumps in District Heating Systems. *Energies* 2017;10:578. doi:10.3390/en10040578.
- 495 [6] Holttinen H, Cutululis NA, Gubina A, Keane A, Van Hulle F. Ancillary services: technical  
496 specifications, system needs and costs. Deliverable D 2.2. 2012.
- 497 [7] Carmo C, Detlefsen N, Nielsen M. Smart Grid enabled heat pumps: An empirical platform for  
498 investigating how residential heat pumps can support largescale integration of intermittent  
499 renewables. *Energy Procedia* 2014;61:1695–8. doi:10.1016/j.egypro.2014.12.194.
- 500 [8] Stinner S, Schlösser T, Huchtemann K, Müller D, Monti A. Primary energy evaluation of heat  
501 pumps considering dynamic boundary conditions in the energy system. *Energy* 2017;138:60–78.  
502 doi:10.1016/j.energy.2017.07.029.
- 503 [9] Patteeuw D, Reynders G, Bruninx K, Protopapadaki C, Delarue E, D'haeseleer W, et al. CO<sub>2</sub>-  
504 abatement cost of residential heat pumps with active demand response: Demand- and supply-  
505 side effects. *Appl Energy* 2015;156:490–501. doi:10.1016/j.apenergy.2015.07.038.
- 506 [10] Ulbig A, Andersson G. Analyzing operational flexibility of electric power systems. *Int J Electr*  
507 *Power Energy Syst* 2015;72:155–64. doi:10.1016/j.ijepes.2015.02.028.
- 508 [11] Robbi S. LowEx-Fernwärme - Vergleichende Bewertung von Maßnahmen für eine effiziente,  
509 multifunktionale Fernwärmeversorgung (Doctoral thesis). Technische Universität Dresden, 2013.
- 510 [12] Schlachtberger DP, Becker S, Schramm S, Greiner M. Backup flexibility classes in emerging large-  
511 scale renewable electricity systems. *Energy Convers Manag* 2016;125:336–46.  
512 doi:10.1016/j.enconman.2016.04.020.
- 513 [13] Makarov Y V., Loutan C, Ma J, Mello P de. Operational impacts of wind generation on California  
514 power systems. *IEEE Trans POWER Syst* 2009;24, No. 2:1039–50.  
515 doi:10.1109/NOMS.2002.1015622.
- 516 [14] Eid C, Codani P, Perez Y, Reneses J, Hakvoort R. Managing electric flexibility from Distributed  
517 Energy Resources: A review of incentives for market design. *Renew Sustain Energy Rev*  
518 2016;64:237–47. doi:10.1016/j.rser.2016.06.008.



- 519 [15] Blarke MB, Lund H. The effectiveness of storage and relocation options in renewable energy  
520 systems. *Renew Energy* 2008;33:1499–507. doi:10.1016/j.renene.2007.09.001.
- 521 [16] Meibom P, Kiviluoma J, Barth R, Brand H, Weber C, Larsen H V. Value of electric heat boilers and  
522 heat pumps for wind power integration. *Wind Energy* 2007;10:321–37. doi:10.1002/we.224.
- 523 [17] Bejan A, Tsatsaronis G, Moran M. Thermal design and optimization. John Wiley & Sons, Inc.;  
524 1996.
- 525 [18] Sayadi S, Tsatsaronis G, Morosuk T. A New Approach for Applying Dynamic Exergy Analysis and  
526 Exergoeconomics to a Building Envelope 2016:1–17.
- 527 [19] Sangi R, Martín PM, Müller D. Thermoeconomic analysis of a building heating system. *Energy*  
528 2016;111:351–63. doi:10.1016/j.energy.2016.05.112.
- 529 [20] Modelica Association. Modelica and the Modelica Standard Library 2017.  
530 <http://www.modelica.org> (accessed October 31, 2017).
- 531 [21] Dassault Systèmes. Dymola Systems Engineering 2017. [https://www.3ds.com/products-](https://www.3ds.com/products-services/catia/products/dymola/)  
532 [services/catia/products/dymola/](https://www.3ds.com/products-services/catia/products/dymola/) (accessed October 31, 2017).
- 533 [22] TLK Thermo GmbH & IfT. TIL 3.4 – Model library for thermal components and systems 2017.
- 534 [23] Grundfos. Product data SP 46-4 2017. [https://product-selection.grundfos.com/product-](https://product-selection.grundfos.com/product-detail.catalogue.product-families.html?from_suid=151022228811006388052718785822&pumpsystemid=280760607&qcid=271031787)  
535 [detail.catalogue.product](https://product-selection.grundfos.com/product-detail.catalogue.product-families.html?from_suid=151022228811006388052718785822&pumpsystemid=280760607&qcid=271031787)  
536 [families.html?from\\_suid=151022228811006388052718785822&pumpsystemid=280760607&qci](https://product-selection.grundfos.com/product-detail.catalogue.product-families.html?from_suid=151022228811006388052718785822&pumpsystemid=280760607&qcid=271031787)  
537 [d=271031787](https://product-selection.grundfos.com/product-detail.catalogue.product-families.html?from_suid=151022228811006388052718785822&pumpsystemid=280760607&qcid=271031787) (accessed July 4, 2017).
- 538 [24] Grundfos. Product data NB 32 - 200/206 2017. [https://product-selection.grundfos.com/product-](https://product-selection.grundfos.com/product-detail.catalogue.product-families.html?from_suid=1510222503906014344929798807637&pumpsystemid=290981485&qcid=293056119)  
539 [detail.catalogue.product](https://product-selection.grundfos.com/product-detail.catalogue.product-families.html?from_suid=1510222503906014344929798807637&pumpsystemid=290981485&qcid=293056119)  
540 [families.html?from\\_suid=1510222503906014344929798807637&pumpsystemid=290981485&q](https://product-selection.grundfos.com/product-detail.catalogue.product-families.html?from_suid=1510222503906014344929798807637&pumpsystemid=290981485&qcid=293056119)  
541 [cid=293056119](https://product-selection.grundfos.com/product-detail.catalogue.product-families.html?from_suid=1510222503906014344929798807637&pumpsystemid=290981485&qcid=293056119) (accessed October 30, 2017).
- 542 [25] HOFOR. Heat demand data for 3 cruise ship terminal buildings and a warehouse. Copenhagen:  
543 2012.
- 544 [26] Jensen JK, Ommen T, Markussen WB, Elmegaard B. Design of serially connected district heating  
545 heat pumps utilising a geothermal heat source. *Energy* 2017. doi:10.1016/j.energy.2017.03.164.
- 546 [27] Pfeil HV. Intelligent Capacity Control Potential for System Efficiency Improvements & Energy  
547 Savings. ICR 2015, Yokohama, Japan: 2015, p. ID:16. doi:10.18462/iir.icr.2015.0016.
- 548 [28] Energinet.dk. Energinet.dk - Markedsdata 2012. <http://www.energinet.dk> (accessed July 10,  
549 2017).
- 550 [29] Rothuizen E, Markussen W, Elmegaard B, Madsen C, Olesen MF, Sølvsten M. High Efficient Heat  
551 Pump System Using Storage Tanks To Increase Cop By Means of the Isec Concept ( Part I ,  
552 Thermal Storage System ). *Proc 24th IIR Int Congr Refrig* 2015:1–8.
- 553 [30] Lazzaretto A, Tsatsaronis G. SPECO: A systematic and general methodology for calculating  
554 efficiencies and costs in thermal systems. *Energy* 2006;31:1257–89.  
555 doi:10.1016/j.energy.2005.03.011.
- 556 [31] Rosen MA, Dincer I. Thermal energy storage systems and applications. 2nd ed. Ontario, Canada:

- 557 John Wiley & Sons, Inc.; 2011.
- 558 [32] Center for Klima og Energiøkonomi. Forudsætninger for samfundsøkonomiske analyser på  
559 energiområdet 2016;Version 3.  
560 [https://ens.dk/sites/ens.dk/files/Analyser/samfundsoekonomiske\\_beregningsforudsætninger\\_2](https://ens.dk/sites/ens.dk/files/Analyser/samfundsoekonomiske_beregningsforudsætninger_2016_v3.pdf)  
561 [016\\_v3.pdf](https://ens.dk/sites/ens.dk/files/Analyser/samfundsoekonomiske_beregningsforudsætninger_2016_v3.pdf).
- 562 [33] Energinet.dk. Marketsdata 2017. [www.energinet.dk](http://www.energinet.dk) (accessed July 10, 2017).
- 563 [34] Energinet.dk. Technology Data for Energy Plants 2016. [www.ens.dk](http://www.ens.dk) (accessed October 12, 2017).
- 564 [35] Energinet.dk. Technology Data for Energy Plants 2012.  
565 [https://ens.dk/sites/ens.dk/files/Analyser/technologydata\\_for\\_energy\\_plants\\_-](https://ens.dk/sites/ens.dk/files/Analyser/technologydata_for_energy_plants_-_may_2012._updated_2015.pdf)  
566 [\\_may\\_2012.\\_updated\\_2015.pdf](https://ens.dk/sites/ens.dk/files/Analyser/technologydata_for_energy_plants_-_may_2012._updated_2015.pdf) (accessed October 12, 2017).
- 567 [36] Baeten B, Rogiers F, Helsen L. Reduction of heat pump induced peak electricity use and required  
568 generation capacity through thermal energy storage and demand response. *Appl Energy*  
569 2017;184–95. doi:10.1016/j.apenergy.2017.03.055.
- 570 [37] Arteconi A, Patteeuw D, Bruninx K, Delarue E, D'haeseleer W, Helsen L. Active demand response  
571 with electric heating systems: Impact of market penetration. *Appl Energy* 2016;177:636–48.  
572 doi:10.1016/j.apenergy.2016.05.146.
- 573 [38] Hedegaard K. Wind power integration with heat pumps, heat storages, and electric vehicles –  
574 Energy systems analysis and modelling (PhD thesis) 2013.

575

Highlights - Dynamic exergoeconomic analysis of a heat pump system used for ancillary services in an integrated energy system

- Dynamic exergoeconomic analysis
- Cost allocation method for regulation power and heat provided by the heat pump
- Large scale heat pump providing manual reserve regulation
- Exergy destruction increase for flexible operation due to storage and reheating