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Passive Reactor Compensated Cascaded H-Bridge Multilevel LC-StatCom

Glen Farivar, *Student Member, IEEE*, Christopher D. Townsend, *Member, IEEE*, Branislav Hredzak, *Senior Member, IEEE*, Josep Pou, *Fellow, IEEE*, Vassilios G. Agelidis, *Fellow, IEEE*

Abstract— The cascaded H-bridge (CHB) low-capacitance StatCom (LC-StatCom) has a limited operating area in the inductive region compared to a conventional StatCom's $V-I$ characteristic. This limitation for operation in the inductive region is considered to be the biggest disadvantage of CHB LC-StatCom. In this paper, the effect of adding parallel and series reactors on the LC-StatCom system's $V-I$ characteristic is analyzed. Then, a new configuration, which fully compensates for the lost operating area of the LC-StatCom is introduced. A scaled down single-phase seven-level laboratory prototype is used to confirm practicability of the proposed system.

Index Terms— Cascaded H-bridge, LC-StatCom, reactive power compensation, thin dc capacitor

I. INTRODUCTION

THE cascaded H-bridge multilevel converter (CHB-MC) is a popular choice in many industrial applications due to its modularity, ability to decrease switching loss while maintaining excellent harmonic performance, and the possibility to eliminate the step-up transformer in medium voltage applications [1], [2]. An additional feature which makes this converter suitable for the StatCom application is its linear relationship between level number and component count [2], as opposed to monolithic multilevel converters where this relationship is quadratic.

Compared to monolithic multilevel converters, the requirement for isolated dc power sources is considered to be one of the main disadvantages [1]. However, in StatCom applications the isolated dc sources are floating capacitors and therefore the isolation requirement is easily met. The idea of using a CHB-MC as a StatCom was introduced in [3]. Thereafter, different aspects of this application for CHB-MC

have been studied in the technical literature [4]–[24].

A three-phase CHB converter is constructed from three single-phase converters, which implies that each phase-leg must buffer the per-phase variations in instantaneous power that occur within each fundamental cycle. Typically, the voltage variation on the capacitors due to flow of this instantaneous power is limited to less than 10% of nominal dc voltage [31] by utilizing large dc capacitors. The need for large capacitors increases the cost, weight, and volume of the system. Furthermore, utilizing electrolytic capacitors to achieve the required high capacitance reduces the reliability of the system [25], [26].

Recent studies demonstrated the feasibility of operating CHB StatCom with low capacitor sizes, implying operation with capacitor voltage ripples in excess of the conventional 10%. In [33], a CHB StatCom was developed that was able to operate with approximately 30% voltage ripple on the capacitors. The system was constructed using film capacitors to achieve high reliability [27]–[30]. Reduced capacitor size requires a faster control system to regulate capacitor voltages during transient conditions. Simultaneously, removing the effect of voltage ripple components on the controller becomes more challenging due to the increased size of the ripple. To address these issues, the control system in [33] utilizes an analytic formula to eliminate the ripple component from each measured cluster voltage (sum of capacitor voltages in a phase-leg) without imposing any significant delay into the control loop.

In a conventional CHB StatCom, the minimum cluster voltage is designed to be at all times higher than the sum of peak grid voltage and peak voltage drop across the connection inductor. As a consequence, in conventional CHB StatComs, increasing the ripple on capacitors causes increased peak cluster voltages, which is a major limiting factor for reducing the capacitor energy and size. Larger peak cluster voltages were also the main disadvantage of the system developed in [33].

In [34], the CHB low capacitance StatCom (LC-StatCom) concept was developed. In the CHB LC-StatCom the desire to minimize H-bridge capacitances is achieved by restricting the $V-I$ operating characteristic of the converter. In theory, the LC-StatCom system is able to operate with 100% ripple on the capacitors and facilitate lower peak capacitor/cluster voltages compared to a conventional CHB StatCom. It was shown that when operating in the capacitive region, the synthesized output voltage waveform has the same phase angle as the

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capacitor voltage ripple waveform. This implies there is sufficient cluster voltage to maintain current control even when the cluster voltage reduces to almost zero. Hence, the CHB LC-StatCom is a promising solution for significantly reducing H-bridge capacitance values. Furthermore, better voltage and current quality, lower voltage stress on switches and lower switching losses are additional benefits of the LC-StatCom [34]. However, the limited V - I operating capability is the main disadvantage.

In this paper, a passive reactive compensated LC-StatCom system, which integrates the concept of a thyristor bypassed reactor (TBR), is proposed to overcome the abovementioned shortcoming of the LC-StatCom. In a TBR device, thyristor switches are connected in parallel to the inductor. Therefore, this concept differs from the conventional thyristor controlled reactors (TCR) where the switches are placed in series with the inductor. The proposed compensated LC-StatCom system maintains the benefits of the LC-StatCom while reshaping its V - I characteristics to match a conventional StatCom.

The rest of this paper is organized as follows. Section II provides the background on the CHB LC-StatCom system. The effect of series and parallel reactors on the V - I characteristics of the LC-StatCom system is analyzed in Section III. The proposed compensated LC-StatCom system is introduced in Section IV. Experimental results are provided in Section V. Finally, conclusions from the work are summarized in Section VI.

II. CHB LC-STATCOM SYSTEM

A. CHB LC-StatCom Model

Fig. 1 shows a single-phase CHB LC-StatCom. A three-phase configuration is composed of three identical single-phase converters. Therefore, for the rest of this paper, without loss of generality, a single-phase system is considered.

Using Kirchhoff's voltage law on the ac side yields,

$$\sum_{j=1}^N v_j - v_g - Ri_g - L \frac{di_g}{dt} = 0 \quad (1)$$

where, v_j is the ac voltage generated by the j^{th} H-bridge ($j \in \{1, \dots, N\}$), L represents the filter inductor and R is its parasitic series resistance. v_g and i_g are the grid voltage and converter current, respectively.

On the other hand, on the dc side of each H-bridge,

$$i_{c-j} + C \frac{dv_{c-j}}{dt} = 0, \quad (2)$$

where C represents the capacitance of the capacitors ($C=C_1=C_2=\dots=C_N$) and v_{c-j} is the voltage across the individual capacitors. i_{c-j} represents the current flowing into the j^{th} capacitor. Assuming that the losses are negligible, the input power on the ac side is equal to the output power on the dc side; hence,

Fig. 1. A general single-phase, $(2N+1)$ -level CHB converter StatCom

$$i_{c-j} = \frac{v_j}{v_{c-j}} i_g. \quad (3)$$

Replacing i_{c-j} from (3) in (2) yields,

$$\frac{v_j}{v_{c-j}} i_g + C \frac{dv_{c-j}}{dt} = 0. \quad (4)$$

(1) and (4) are the core equations that model the behavior of the CHB converter.

B. Control System

From a hardware perspective, except for facilitating smaller H-bridge capacitance values, the CHB LC-StatCom is similar to a conventional CHB StatCom, as can be seen from Fig. 1. However, the control system must operate differently due to the low capacitances and large voltage ripples on the capacitors. The overall view of the utilized control system is shown in Fig. 2 [34].

The individual capacitor voltage loops use separate PI controllers to balance the voltage on each capacitor [35]. The current is controlled by a dead-beat controller to achieve fast dynamic performance. The cluster voltage controller uses the square of the voltage to linearize the control system, which is important as the voltage reference varies throughout a wide range, implying the nonlinear relationship between voltage and capacitor energy would otherwise cause significant control interaction between loops [35]. The feedforward ripple

Fig. 2. LC-StatCom control system composed of three sub-sections: (i) cluster voltage controller, (ii) current controller, and (iii) voltage balancing (individual capacitors' voltage controller).

compensator subtracts the second order ripple component from the measured capacitor voltages. The ripple compensator replaces the low pass filter typically utilized in conventional controllers [10], and allows an increase in the bandwidth of the cluster voltage controller.

The LC-StatCom is well suited to operate in capacitive region as the ripple on the capacitor voltages is in phase with the grid voltage, which allows the control system to lower the cluster reference voltage well below the peak grid voltage. Fig. 3 shows the operational principal of the LC-StatCom compared to a conventional CHB StatCom. The LC-StatCom's ability to operate with capacitor voltages lower than the grid voltage peak, provides the control system with a degree of freedom to maintain a fixed maximum voltage on the capacitors, V_{dc-max} , when the ripple is large (as high as 90% of the nominal dc capacitor voltage). The LC-StatCom control system uses a capacitor voltage limiter (CVL) module to generate a reference signal for the cluster voltage controller [34]. The operation principal of the CVL is provided in the Appendix.

III. PASSIVE REACTIVE COMPENSATION

It was shown in [34] that the operational limits of an ideal LC-StatCom are as follows

Capacitive:

$$(0 \leq I_{q(p.u)} \leq 1) \quad , \quad (0 \leq V_{g(p.u)} \leq 1). \quad (5)$$

Inductive:

$$0 < I_{q(p.u)} \leq \frac{1}{V_{g(p.u)}} - V_{g(p.u)} \quad , \quad (0.62 \leq V_{g(p.u)} \leq 1) \quad (6)$$

$$0 < I_{q(p.u)} \leq 1 \quad , \quad (0 \leq V_{g(p.u)} < 0.62)$$

The details and the assumptions to derive these limits are provided in the Appendix. It is worthwhile mentioning that to simplify the comparison between compensation options; the rest of this section considers an ideal case. That is, the effect of series filtering inductor (L_f), included in any StatCom voltage source converter to facilitate current control, is

Fig. 3. Comparison between operation of (a) LC-StatCom system and (b) conventional StatCom system.

Fig. 4. V-I characteristics of an LC-StatCom.

neglected. The effect of this inductor on the I-V characteristic will be addressed in Section V. The operational limits defined in (5) and (6) are shown graphically in Fig. 4 by the solid black lines. Therefore, the dashed area shown in Fig. 4 needs to be added to the V-I characteristic of the LC-StatCom, in order to compensate for its shortcoming compared to a conventional StatCom.

To expand the inductive operating region, a compensating inductor can be added to the LC-StatCom in either parallel or series configurations as shown in Fig. 5. If utilizing a parallel compensation inductor, the disconnecting switch, S_p , needs to be closed when the LC-StatCom operates in the inductive region. Alternatively, if utilizing a series compensation

Fig. 5. Integrating a compensating inductor into an LC-StatCom system. (a) Parallel and (b) series configuration.

inductor, the bypass switch, S_s , needs to be open when the LC-StatCom operates in the inductive region. In the following analysis, both series and parallel compensation strategies are explored in detail.

A. Parallel Compensation

Parallel compensation is achieved by installing a thyristor switched reactor (TSR) [36]. Once switched into the circuit, a TSR provides a constant inductive current (proportional to voltage) with no explicit control on the magnitude or phase of the current. In the parallel system, the total reactive current when operating in the inductive region can be controlled by varying the capacitive current injected by the LC-StatCom. Therefore, there is no need for utilizing a thyristor controlled reactor (TCR) to achieve variable inductive current [36]-[38]. Whereas the current in a TCR is varied by modifying the applied firing angle, a TSR produces no switching harmonics and has a simpler control system. Furthermore, the LC-StatCom provides a faster dynamic response compared to a TCR [39].

The maximum inductive current that the LC-StatCom can generate is lower than 1 p.u for grid voltages higher than 0.62 p.u as described in (6). Therefore, the minimum per-unit current that needs to be supplied by the TSR, $I_{p-min(p.u)}$, in order to achieve full compensation is

$$I_{p-min(p.u)} = 1 - \left(\frac{1}{V_{g(p.u)}} - V_{g(p.u)} \right), \quad (0.62 \leq V_{g(p.u)} \leq 1). \quad (7)$$

The current supplied by the TSR must be larger than $I_{p-min(p.u)}$, as follows:

$$\frac{V_{g(p.u)}}{X_{p(p.u)}} \geq I_{p-min(p.u)}, \quad (0.62 \leq V_{g(p.u)} \leq 1). \quad (8)$$

In (8), $X_{p(p.u)}$ represents the per-unit value of the parallel compensating reactor. The maximum value of $X_{p(p.u)}$ that satisfies (8) is one per-unit. Therefore, a value of one per-unit for the parallel reactor is assumed in the following analysis.

The characteristic of a parallel reactor compensated LC-StatCom in the inductive region is

$$\begin{aligned} 0 < I_{q(p.u)} &\leq \frac{1}{V_{g(p.u)}}, & (0.62 \leq V_{g(p.u)} \leq 1) \\ 0 < I_{q(p.u)} &\leq V_{g(p.u)} + 1, & (0 \leq V_{g(p.u)} < 0.62) \end{aligned} \quad (9)$$

The effect of the TSR in reshaping the LC-StatCom V - I characteristic is depicted in Fig. 6. Fig. 6(a), shows the area that needs to be compensated by a TSR. Fig. 6(b), shows the minimum required current for full compensation and the current provided by the TSR. As can be seen from this figure, the minimum required 1 p.u inductor provides excessive current for voltages lower than 1 p.u. This excessive current extends the operating region of the compensated LC-StatCom system beyond 1 p.u current as shown in Fig 6(c).

B. Series Compensation

In the inductive region, the maximum voltage at which the LC-StatCom is able to operate is lower than 1 p.u as can be seen in Fig. 4. Therefore, from (6), the minimum per-unit voltage that needs to be added by a series compensator, $V_{s-min(p.u)}$, for full compensation is

$$V_{s-min(p.u)} = 1 - \frac{-I_{q(p.u)} + \sqrt{I_{q(p.u)}^2 + 4}}{2}. \quad (10)$$

The voltage drop across the compensating series reactor must be larger than $V_{s-min(p.u)}$,

$$X_{s(p.u)} I_{q(p.u)} \geq V_{s-min(p.u)}. \quad (11)$$

In (11), $X_{s(p.u)}$, represents the per-unit value of the series compensating reactor. The minimum value of $X_{s(p.u)}$ that satisfies (11) is 0.5 per-unit. The characteristic of the series TBR integrated LC-StatCom in the inductive region is

$$0 < V_{g(p.u)} \leq \frac{\sqrt{I_{q(p.u)}^2 + 4}}{2}, \quad (0 < I_{q(p.u)} \leq 1). \quad (12)$$

The effect of the 0.5 p.u series inductor in reshaping the LC-StatCom characteristic is summarized in Fig. 7. Fig. 7(a), shows the area that needs to be compensated by a series inductor. Fig. 7(b), shows the minimum required voltage for full compensation and the voltage provided by the series inductor. As can be seen from this figure, the selected 0.5 p.u inductor provides some excessive voltage for currents higher than 1 p.u. This excessive voltage extends the operating region of compensated LC-StatCom system beyond 1 p.u voltage as shown in Fig. 7(c).

IV. PROPOSED SYSTEM

From the previous section it is clear that both series and parallel inductors require the same current rating. Therefore, the option with lower inductance will have a lower energy storage capacity (e_L), according to $e_L = 0.5Li^2$. Since the series compensation solution has a lower inductance, it is a smaller and cheaper option. Additionally, the series

Fig. 6. Parallel compensation. (a) LC-StatCom characteristic and the current required for full compensation, (b) minimum current required for full compensation and the excessive current added by a 1 p.u. parallel inductor, and (c) V-I characteristics of a parallel inductor compensated LC-StatCom.

Fig. 7. Series compensation. (a) LC-StatCom characteristic and the voltage required for full compensation, (b) minimum voltage required for full compensation and the excessive voltage added by a 0.5 p.u. series inductor, and (c) V-I characteristics of a series inductor compensated LC-StatCom.

Fig. 8. Proposed series reactor compensated LC-StatCom.

compensation helps to improve current quality because the extra inductance is added in series in this configuration, meaning it helps to filter harmonics produced by the LC-StatCom. Therefore, the series configuration is a superior choice.

The proposed compensated LC-StatCom system is shown in Fig. 8. In this figure, L_f represents the existing filter inductor in the original LC-StatCom system. As the filter inductor is also placed in series with the LC-StatCom, it helps to reduce the required inductance value of the compensating inductor L_s .

Fig. 9, shows the effect of the filter inductor on the V-I characteristic of the system. Due to presence of the filter inductor, the LC-StatCom rated voltage needs to be over-designed to provide nominal capacitive current (1 p.u.) at 1 p.u. voltage. The same over-rating is also required for the conventional CHB StatCom. The voltage over-rating reduces the area that needs to be compensated in the inductive region of the LC-StatCom system, as shown in Fig. 9(a). Fig 9(b), shows the minimum required voltage for full compensation and the voltage provided by the compensating inductor L_s . The compensating inductor's value can be calculated from

$$X_{s(p.u)} = 1 - 0.62 - 2X_{f(p.u)}. \quad (13)$$

Fig. 9(c), shows the series inductor compensated LC-StatCom characteristic, which includes the effect of the filter inductor.

Fig. 9. Proposed series compensation. (a) Effect of the filter inductor on LC-StatCom characteristic and the voltage required for full compensation, (b) minimum voltage required for full compensation and the excessive voltage added by a series inductor, and (c) V-I characteristics of an LC-StatCom with filter inductor and a series TBR compensator.

The effect of L_f in reducing the size of L_s is multiplied by two as can be seen from (13). The reason is that L_f reduces the operating area on the capacitive side but increases the area on the inductive side. Therefore, selecting a larger L_f reduces the size of the total reactance ($L_f + L_s$) required in the system. For instance, in the worst case where X_f is zero, $X_{s(p,u)}$ is 0.38, whereas, when $X_{f(p,u)} = 0.19$, X_s is zero. Therefore, when $X_{f(p,u)} = 0.19$, the total required inductance is the smallest one and there is no need for any additional compensating inductor, which prevents any additional hardware complexity being added to the system. However, the voltage drop on the filter inductor becomes larger with an increasing $X_{f(p,u)}$, which increases the converter's voltage rating to allow operation in the capacitive region. This implies that there is a design trade-off between the size of the filter inductor (and subsequent size of the compensating inductor) and the converter voltage over-

rating. To keep the voltage over-rating in the same range as that required in a conventional CHB StatCom, this paper uses a filter inductance of 0.127 p.u. From (13), this implies use of a series compensating inductor rated at, 0.127 p.u to achieve full compensation.

The bidirectional switch used to connect the series compensating inductor into the circuit can be turned off when the current reaches zero to change the operating mode from capacitive to inductive. Utilization of naturally commutated switches, such as thyristors as shown in Fig. 8, ensures the transition will happen at close to zero current where there is approximately zero energy stored in the magnetic field of the filter inductor, which would otherwise produce destructive over-voltages. Thyristors are also relatively cheap, robust, have very low conduction losses, and can be series connected to increase the overall blocking voltage of the switch [40]. Similar to TCRs, a snubber circuit to control the voltage transients during thyristor turn off may be necessary [41], [42]. The current rating of these bypass thyristors is equal to the rating of the semiconductors used within the LC-StatCom. However, their required voltage rating is equal to the maximum voltage drop across the series compensating inductor, which expressed in per unit value is equal to $X_{s(p,u)}$. Therefore, these bypass switches have only a fractional voltage rating compared to the LC-StatCom. Both thyristors share the same gate signal. When the gate signal is activated, the switches start conducting (regardless of current magnitude or direction) to bypass the compensating inductor. On the other hand, when the gate signal is deactivated, the conducting thyristor will remain conducting until the current goes below a certain value (ideally zero), after which the thyristor turns off.

In addition to the abovementioned hardware changes, two sets of different parameters for the current controller need to be used for operation in capacitive and inductive modes as the total inductance value changes. In this paper, the dead-beat current controller uses a discretized version of (1) to produce the ac reference voltages [34]. Therefore, L and R need to be updated when the extra inductor switches in or out. Operation around the boundary of inductive and capacitive regions (zero reactive current) could cause rapid switching of the bypassing thyristors. This unwanted switching can easily be circumvented by introducing a hysteresis band in between the changeover of modes.

V. EXPERIMENTAL RESULTS

To experimentally verify the compensated LC-StatCom system, a single-phase seven-level CHB converter was constructed. A photograph and a block diagram of the experimental setup are shown in Fig. 10, and its parameters are given in Table I. The 240V grid voltage was reduced to 110V and isolated from the grid using a step-down transformer. Three POWEREX PP75B060 single-phase H-bridge converters were connected in series to form the seven-level LC-StatCom converter. Phase-shifted PWM was implemented using a DS5203 FPGA module. The PWM signals are transferred to the converter driver board by optical link for galvanic isolation. The feedback signals are

Fig. 10. (a) Photograph and (b) block diagram of the single-phase, seven-level CHB converter LC-StatCom experimental setup.

TABLE I
PARAMETERS OF THE EXPERIMENTAL LC-STATCOM

Symbol	Quantity	Values
V_{gn-rms}	Grid voltage <i>rms</i> value	110 V
C	Capacitance - H-bridge capacitors	260 μ F
L_f	Filter inductor	14 mH (0.127 p.u)
L_s	Series compensating filter inductor	14 mH
f_s	Switching frequency (per H-bridge)	2 kHz
V_{dc-max}	Maximum voltage on capacitors	180 V
V_{dc-min}	Minimum voltage on capacitors	60 V
f_g	Grid frequency	50 Hz
S	Converter nominal power	350 VA
R	Filter inductor series resistance	0.5 Ω
w_v	Bandwidth of the voltage controller	300 rad/s
N	Number of H-bridges	3

routed back to the processor using a DS2004 ADC module. All other control systems were implemented using a dSPACE DS1006 processor board.

In this section, several case studies are performed to demonstrate operation of the compensated LC-StatCom system. In the first case study, response of the system to step changes in reactive current command is investigated. In Fig.

Fig. 11. Operation of compensated LC-StatCom system when the reactive current reference changes from 4 A inductive to 2 A inductive at t_0 .

Fig. 12. Operation of the LC-StatCom system when the reactive current reference changes from full inductive to full capacitive at t_0 .

11 operation in the inductive region is shown (the series compensating inductor L_s is conducting). In this case, initially the system is providing 4 A inductive current. At t_0 the reactive current command changes to 2 A inductive. Prior to t_0 , a standalone LC-StatCom would not be able to operate in this part of the inductive region because the grid voltage waveform overlaps the cluster voltage waveform. However, by adding the compensating inductor, the converter was able to maintain control over the capacitor voltages and provide the requested inductive current.

In Figs. 12 and 13 more dramatic step changes are investigated, in which the reactive current reference changes from full inductive to full capacitive and vice versa, respectively. The transitions occur at zero current to allow for safe disconnection and connection of the compensating inductor. The voltage across the bypass switch when changing state from on to off is shown in Fig. 14. As can be seen, a transient voltage is generated during the change of modes. This is due to a small nonzero inductor current at the time of switching. It is worthwhile mentioning that in this setup no turn-off snubber was utilized. However, for higher voltage and

Fig. 13. Operation of the LC-StatCom system when the reactive current reference changes from full capacitive to full inductive at t_0 .

Fig. 14. Voltage across the bypassing semiconductors turning off at t_0 .

current systems a turn-off snubber would be necessary to safeguard the switches from excessive transient voltages.

The current THD remains less than 5 % (4% in capacitive and 3.5 % in the inductive region). In capacitive region, the filter inductor value is half of that in the inductive region but the current THD remains low because of better utilization of the available voltage levels within the LC-StatCom [34]. As shown in Fig. 15, the capacitor voltage ripple in capacitive region helps to synthesize a sinusoidal ac voltage and the converter utilizes its full capacity (seven-level voltage) in most of the period which results in better current quality. On the other hand, in inductive region, the quality of synthesized ac voltage is lower and the system relies on a higher filter inductor value to reduce the current THD.

Operation under grid voltage fluctuation is demonstrated in Fig. 16. In this experiment, the converter is supplying its rated inductive current. A grid voltage sag is generated by dropping the grid voltage from 110 V to 75 V in approximately three cycles. As can be seen, the compensated LC-StatCom's operation was not affected by the transient on the grid voltage. The control system was able to supply the rated current and keep the maximum capacitor voltages constant.

Fig. 15. Demonstration of converter's use of available voltage levels in the LC-StatCom.

Fig. 16. Operation of the compensated LC-StatCom during grid voltage variation.

The maximum voltage on each capacitor in the proposed system is 60 V. Therefore, the total energy stored in the capacitors is 1.4 J at peak cluster voltage. In comparison, a conventional CHB StatCom (with maximum 10% voltage ripple on the capacitors) will have a maximum voltage of 66 V on each capacitor and the capacitors' size will be approximately 1 mF, which results in a total capacitor energy storage requirement of 6.5 J. Therefore, the required capacitor energy storage for the proposed system is approximately 79% less than a conventional CHB StatCom. In terms of inductor energy storage requirement, the proposed system requires 0.28 J, which is double the size of a conventional CHB-StatCom system due to presence of the series compensating inductor. Therefore, overall the compensated LC-StatCom system

provides an approximately 75% reduction in stored energy associated with passive components in the system.

VI. CONCLUSION

The effects of adding series and parallel passive compensating reactors on the LC-StatCom's operating regions have been investigated. It is shown that a series compensator requires a much smaller inductor size compared to the parallel option. A series compensating reactor is designed to fully compensate the operating range of the LC-StatCom in the inductive region. Effective operation of the proposed concept is demonstrated through experiments using a single-phase seven-level CHB LC-StatCom system. The compensated LC-StatCom system was able to operate throughout the full range of inductive and capacitive regions and provide a satisfactory response to transients such as step changes in reactive power and grid voltage variation. The proposed compensated LC-StatCom system offers an approximately 75% saving in overall stored energy compared to a conventional CHB StatCom system.

APPENDIX INTRODUCTION TO LC-STATCOM

Neglecting converter current and grid harmonics, the voltage square on the capacitors will have a pure sinusoidal ripple with double the grid frequency [34].

$$\sum_{j=1}^N V_{c-j}^2(t) = V_0^2 \pm \frac{VI_g}{2\omega C} \cos(2\omega t + 2\alpha_v). \quad (14)$$

In (14), V is the peak value of the generated ac voltage by the inverter and α_v is its angle. V_0^2 is the square of the dc component in the cluster voltage, which is controlled by the cluster voltage controller.

In the LC-StatCom control system, the square of the reference cluster voltage (V_{0-ref}^2) is a function of the reactive current reference. The reason for having a variable capacitor voltage reference is to keep the maximum allowed voltage on the capacitors constant. Hence, V_{0-ref}^2 is generated by the CVL block, in Fig.2, to limit the maximum voltage on the capacitors. From (14), the total maximum voltage on the capacitors can be written as

$$V_{dc-max} = N \sqrt{\frac{V_{0-ref}^2}{N} + \frac{(V_g \pm X_L I_{q-ref}) I_{q-ref}}{2\omega NC}}, \quad (15)$$

where X_L is the reactance of L and I_{q-ref} is the reactive current reference of the LC-StatCom. From (15), in order to have a constant V_{dc-max} , the CVL block generates the reference voltage, V_{0-ref}^2 as follows:

$$V_{0-ref}^2 = \frac{(V_{dc-max})^2}{N} - \frac{(V_g \pm X_L I_{q-ref}) I_{q-ref}}{2\omega C}. \quad (16)$$

The LC-StatCom control system can keep V_{dc-max} fixed for all values of I_{q-ref} within its operational limits. These limits in

capacitive and inductive regions are not symmetrical. At full capacitive load, the minimum instantaneous value of the cluster voltage hits its minimum allowed value, V_{dc-min} . Therefore, from (14) and (16) the nominal reactive power (I_{qn}) is calculated as

$$I_{qn} = \frac{V_{dc-max}^2 - V_{dc-min}^2}{V_{gn} N} \frac{\omega C}{1 + X_{L(p,u)}}, \quad (17)$$

in which, $X_{L(p,u)}$ represents the per-unit value of the filter reactance. In (17), subscript n indicates the nominal value of a quantity. In the following the operational limits of an ideal LC-StatCom are derived.

The LC-StatCom system can work at a given operating point if the instantaneous cluster voltage is higher than the instantaneous grid voltage (absolute value of v_g) for the entire period:

$$NV_c(t) \geq |v_g| \quad (18)$$

In (18), the effect of filter inductor is neglected. Replacing $|v_g| = V_g |\sin(\omega t + \alpha_v)|$ in (18) and squaring each side,

$$NV_c^2(t) \geq \frac{V_g^2}{2N} (1 - \cos(\theta)) \quad (19)$$

where $\theta = 2\omega t + 2\alpha_v$. For the theoretical limit case in the capacitive region where $V_{dc-max} = V_{gn}$, from (14) and (16), (19) can be rewritten as

$$\frac{V_{gn}^2}{N} - \frac{V_g I_q}{2\omega C} (1 + \cos(\theta)) \geq \frac{V_g^2}{2N} (1 - \cos(\theta)) \quad (20)$$

The condition in (20) is valid for any $0 \leq V_g < V_{gn}$ and $0 \leq I_q < I_{qn}$ if it is valid for the worst case (nominal operating condition) where $V_g = V_{gn}$ and $I_q = I_{qn}$. At nominal operating condition, (20) can be rewritten as

$$\left(\frac{V_{gn}}{N} - \frac{I_{qn}}{\omega C}\right)(1 + \cos(\theta)) \geq 0. \quad (21)$$

For the ideal limit case ($V_{dc-max} = V_{gn}$, $V_{dc-min} = 0$, and $X_{L(p,u)} = 0$), from (17) $NI_{qn} = \omega C V_{gn}$. Hence, (21) is valid for the whole period ($0 < \theta \leq 2\pi$). Consequently, the I - V characteristic of the LC-StatCom system is equal to the conventional StatCom system ($0 \leq V_g \leq V_{gn}$, $0 \leq I_q \leq I_{qn}$) for the capacitive region.

In the inductive region on the other hand, the following inequality must be satisfied:

$$\frac{V_{gn}^2}{N} - \frac{V_g I_q}{2\omega C} (1 - \cos(\theta)) \geq \frac{V_g^2}{2N} (1 - \cos(\theta)). \quad (22)$$

The relation between V_g and I_q to define the operating region is determined by replacing $\theta = 3\pi/2$ in (22), resulting in

$$I_q \leq \frac{V_{gn}^2 - V_g^2}{NV_g} \omega C, \quad (0 \leq V_g \leq V_{gn}). \quad (23)$$

By analyzing the inequality in (23), it can be seen that as V_g approaches one, I_q approaches zero, while below $V_g \approx 0.62V_{gn}$ there is no extra limitation on I_q . The inductive operating region can therefore be described by

$$\begin{aligned} 0 < I_q &\leq \frac{V_{gn}^2 - V_g^2}{NV_g} \omega C, & (0.62V_{gn} \leq V_g \leq V_{gn}) \\ 0 < I_q &\leq I_{qn}, & (0 \leq V_g < 0.62V_{gn}) \end{aligned} \quad (24)$$

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