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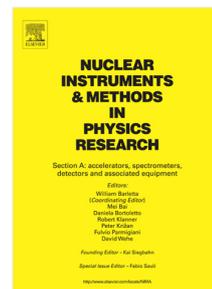
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Design of the cold and thermal neutron moderators for the European Spallation Source

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Abstract

At the European Spallation Source (ESS), neutrons will be generated by spallation induced by a 2-GeV proton beam on a tungsten target. ESS will have a grid of 42 beamports available for a variety of neutron scattering experiments. Neutron moderators will provide thermal and cold neutrons to the instruments, allowing bispectral beam extraction wherever needed.

The moderators were designed by adopting a holistic design approach that has considered brightness, brightness transfer and beam extraction constraints, resulting in a system with the following main features: low-dimensional moderators for enhanced brightness and maximum flux to the sample; a single moderator system placed above the spallation target; lateral shape of the moderators optimized for bispectral extraction. A moderator with a vertical extraction surface of 3 cm was chosen as a result of the optimization process.

With all initial instruments pointing to the top moderator, and a beamport system that allows the possibility to extract neutrons from above and below the target, the adopted configuration opens the possibility to have different types of moderators below the target, so that other neutron beams of different intensity, or spectral shape, with respect to the ones delivered by the top moderator, could be envisaged, adding additional scientific opportunities to the facility without having the need to build a second target station.

Keywords: low-dimensional moderators, source brightness, parahydrogen, water, neutron beam extraction, long pulse sources

1. Introduction

The European Spallation Source (ESS), presently in construction in Lund, Sweden, aims at starting the user program in 2023 [1]. At 5 MW time-average power, and 125 MW peak power, ESS will be the most powerful neutron source in the world for neutron scattering studies of condensed matter. Neutrons will be produced by a 2-GeV proton beam impinging on a target made of tungsten. ESS will be the first high-power accelerator driven long pulse source [2], the pulse length of the beam will be of 2.86 ms, with 14 Hz repetition rate.

Neutron moderators, placed next to the spallation target and designed to slow down neutrons from MeV to the sub-eV range, are a key component of the neutron source. While the accelerated power is a key parameter to indicate the performance of the facility, the brightness of the neutron source, for cold and thermal neutrons, is more relevant for the neutron scattering experiments, because it is a quantity directly related to the number of neutrons at the sample.

The first complete moderator design was presented in the Technical Design Report (TDR) [1] and in Ref. [3]. The TDR cold moderators were pure parahydrogen cylindrical moderators of 16 cm diameter and 13 cm height, and their calculated brightness exceeded the design goal of ESS, to deliver a cold peak brightness a factor of 30 higher than the official ILL cold brightness [4]. After the work for the TDR, the ESS neutronic team led a research effort aimed at designing moderators with further increased brightness. The design of the moderators was redefined based on the concept of low-dimensional moderators [5, 6]. As low-dimensional moderators represent a new idea for enhanced moderator brightness, we discuss in detail their physics properties in Section 2.

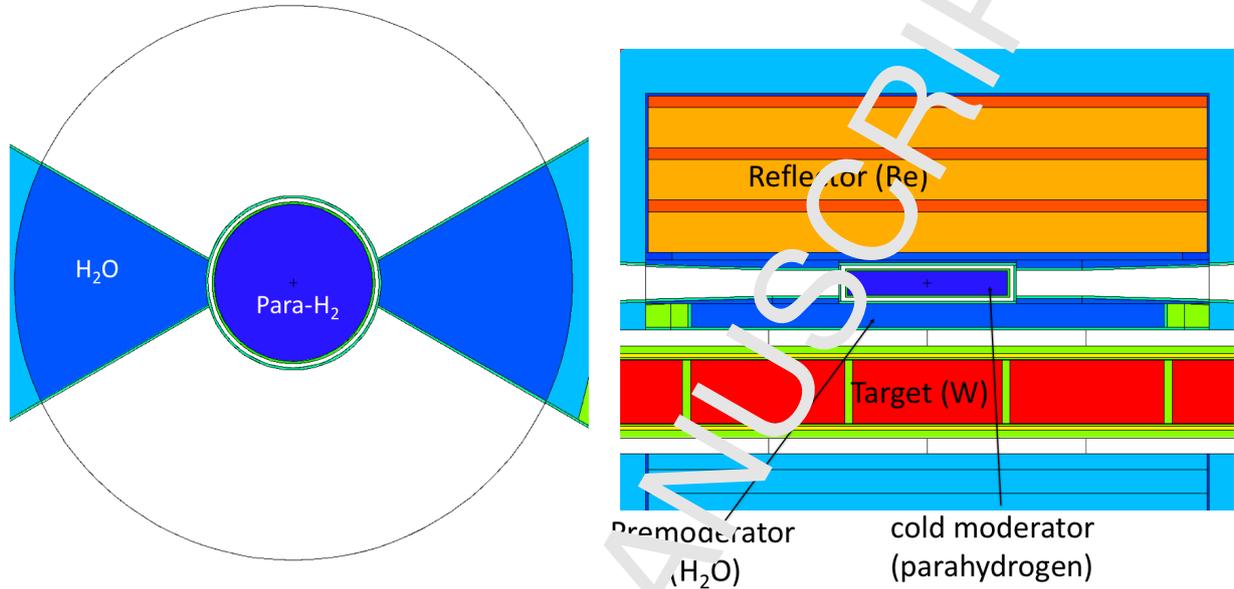
In this discussion we concentrate on *flat*, quasi-two-dimensional moderators, because it is the design basis for the ESS moderators. (quasi-one dimensional moderators are discussed in AppendixB). In Section 3 the different moderator concepts that were considered for ESS are discussed. In Section 4 the beam extraction aspects and their role on the moderator design are discussed. The performances of the moderators are compared in Section 5. In Section 6 the *butterfly*-shape moderator, the selected moderator shape, is described and characterized in detail. Conclusions and some initial suggestions for future upgrade possibilities are given in Section 7. The method of brightness calculation, and the tube moderators (one of the options for future upgrades at ESS) are discussed in the appendices.

All calculations have been performed with MCNPX 2.7.0 [7–9] using the default Bertini/Dresner spallation/evaporation models and ENDF/B-VII nuclear data libraries.

2. Properties of low-dimensional moderators

Low-dimensional moderators have been proposed in recent years to increase the brightness of neutron sources. Studies on moderators of reduced dimensions were carried out from first principles to conceptual design for two high-power spallation sources under design: ESS [5, 6, 10] and the SNS second target station [11]. In these facilities a large number of beam lines covering beam extraction sectors 60°-wide or more is foreseen. For this purpose, two-dimensional moderators are considered. Following the more radical concept of quasi-one-dimensional moderators [6], ideas to use *tube* moderators in reactors [6] and compact sources [12] have been brought up, exploiting the strong brightness and directionality of such moderators, which gives an extra advantage in specific situations where the moderator is feeding only a few beam lines covering a narrow angular span of about 10-20°. While possible future applications of tube moderators for

Figure 1. Basic physics model of a pancake moderator. *Left*: horizontal cut. *Right*: vertical cut of the target-moderator-reflector configuration. The 2-GeV proton beam is hitting the target perpendicular to the plane of the figure.



59 ESS are discussed in the appendix, in this section we examine the properties of two-dimensional moderators,
 60 which are the basis for the ESS design.

61 2.1. Quantification of the brightness gain

62 The fundamental properties of the low-dimensional moderators can be understood by the study of a
 63 simple quasi-two-dimensional moderator of cylindrical shape, which we called *pancake*: a cylindrical alu-
 64 minium vessel filled with pure parahydrogen, placed above a spallation target, with a beryllium reflector on
 65 top, and a water premoderator between target and moderator (Figure 1). The premoderator shapes the
 66 energy spectrum of the neutrons, which, coming from the spallation target, have high energies in the range
 67 of 1-2 MeV. We consider the case of neutron beam extraction over a large angular range, with two sectors
 68 covering 120° each because this applies directly to ESS (a wider opening area is in practice not possible
 69 for a configuration where the proton beam hits the target horizontally). However, the discussion can be
 70 generalized to different beam extraction configurations.

71 We define the brightness B in Appendix A. Although the brightness is time-dependent, we describe it in
 72 terms of a peak and a time-average brightness, since it is largely constant during the duration of the proton
 73 pulse (apart from the rise and fall-off tails). For the peak brightness, we assume that B is equal to the
 74 plateau value reached during a 2.86 ms long pulse. For the time-average brightness, the pulse structure of

Figure 2. Cold peak brightness wavelength spectra for moderators of different heights, calculated from the geometry of Figure 1. Neutrons are extracted in an exit direction perpendicular to the incoming proton beam, at the center of the 120° sector of Figure 1 (left).

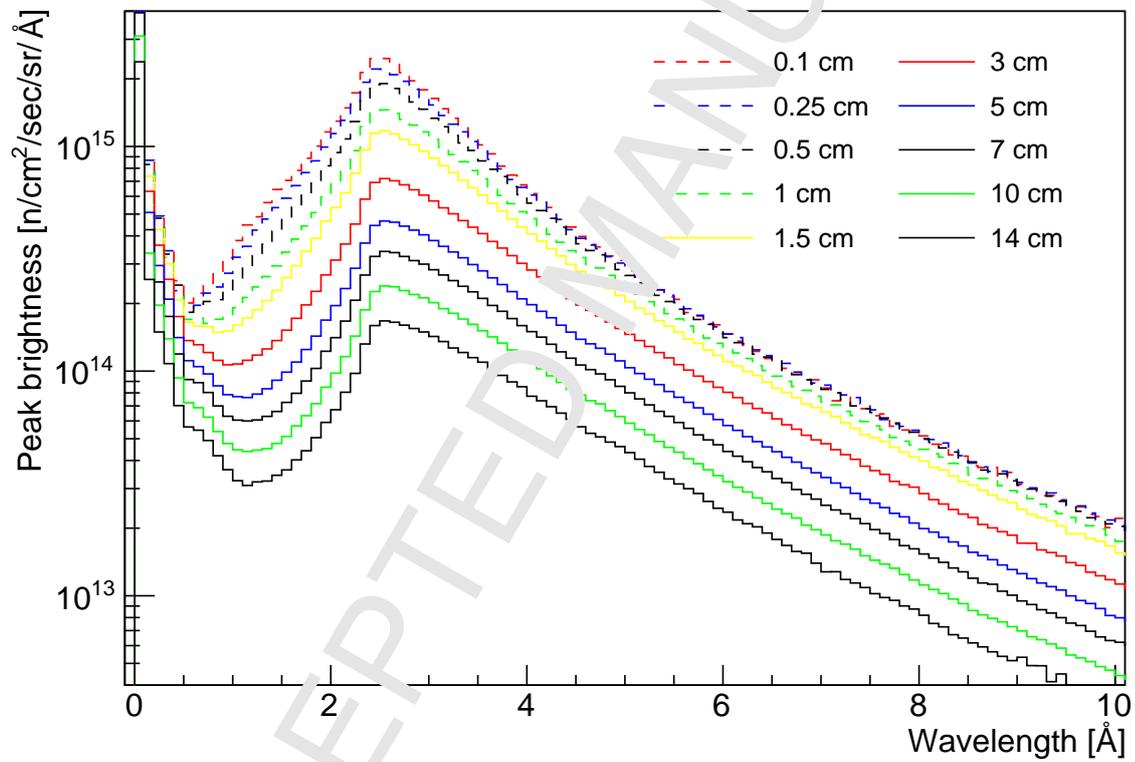


Figure 3. Same as Figure 2, for thermal neutrons, extracted from water wings.

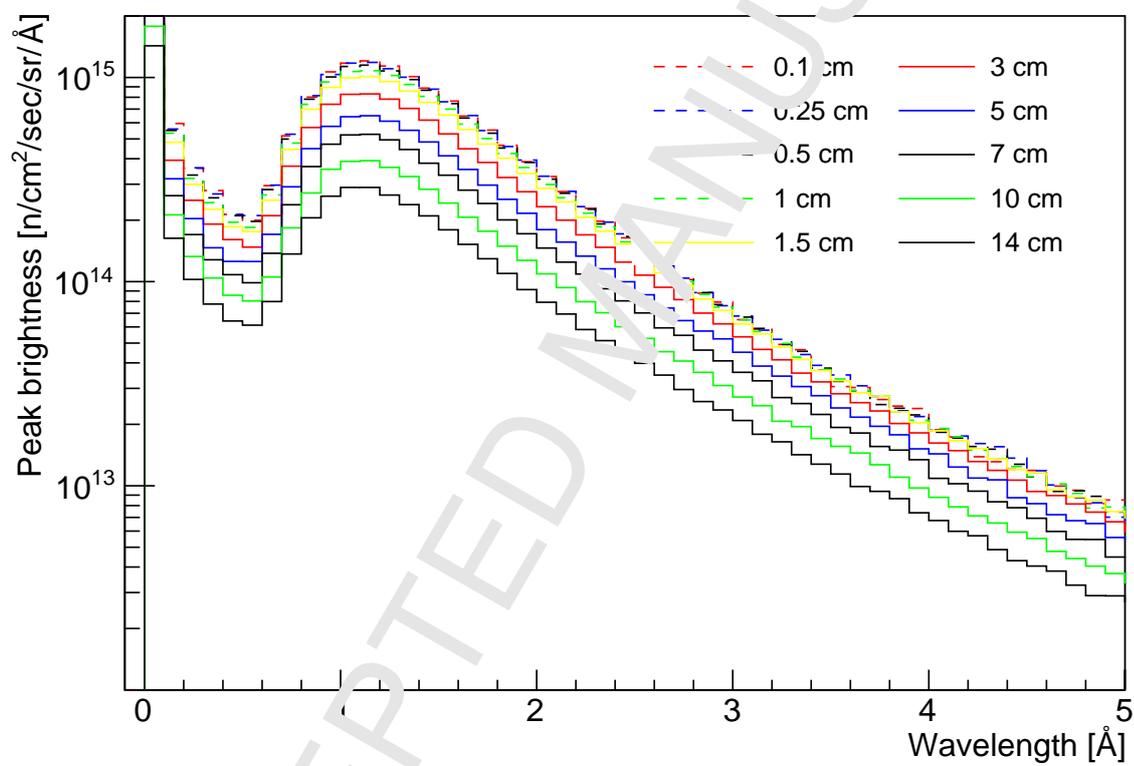
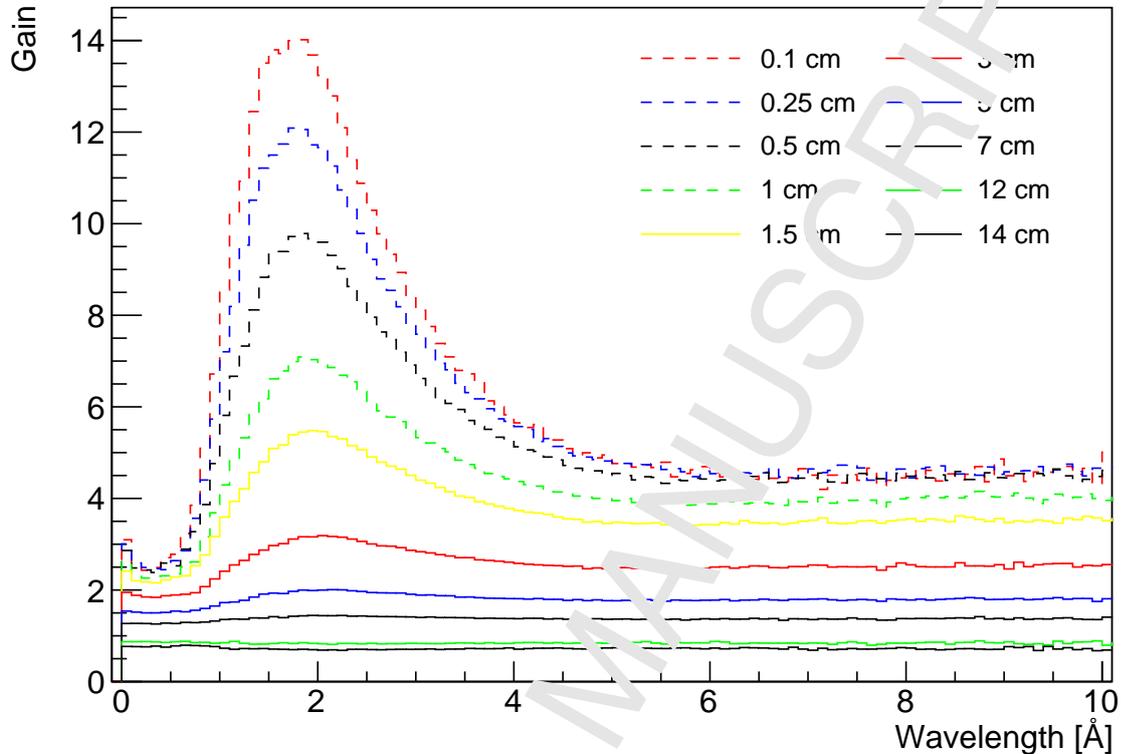


Figure 4. Cold brightness gains with respect to 10 cm tall moderator, from the spectra shown in Figure 2.



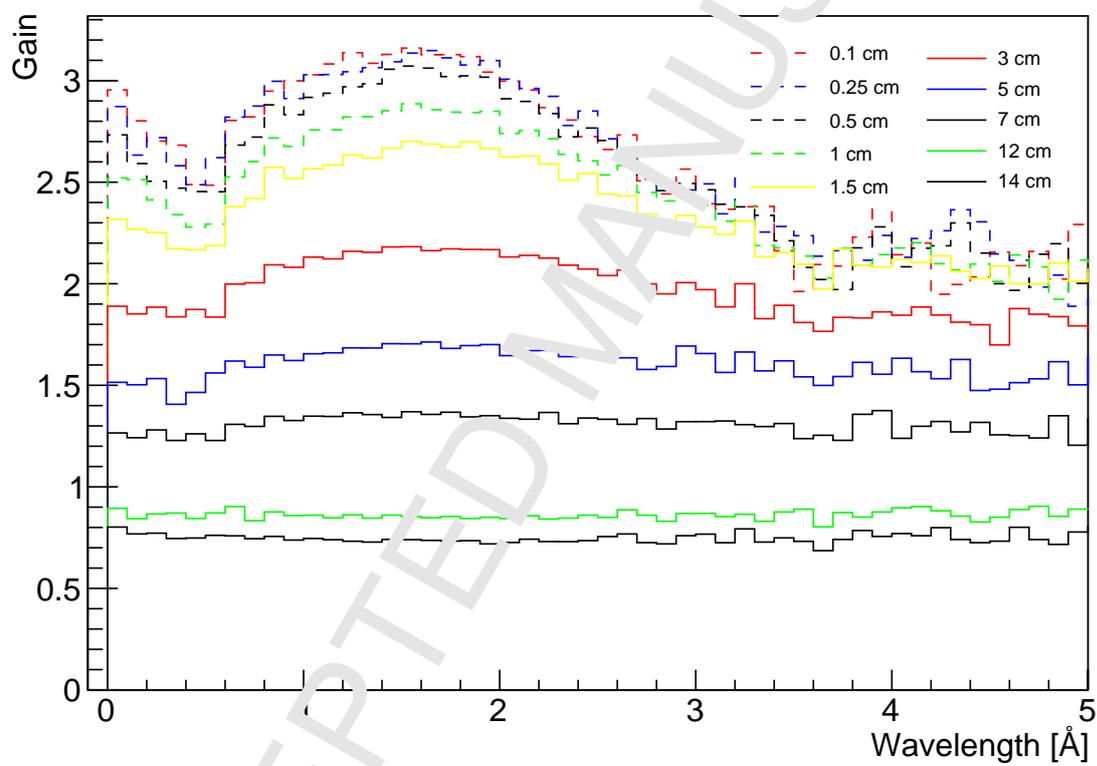
75 the beam is not considered and the ratio between peak and time-average brightness is $T/\tau=25$, where the
 76 repetition period $T = 1/14$ Hz and the pulse length $\tau \approx 2.86$ ms.

77 In Figure 2 and Figure 3 the spectral brightness from the cold and thermal parts of the moderators are
 78 shown, respectively. Cold neutrons are extracted from the center of the cold moderator, from an area of
 79 fixed width of 6 cm, with height equal to the height of the moderator. The brightness is averaged over the
 80 extraction surface. In the case of the thermal moderator, neutrons are extracted from a window of the same
 81 area, from the water moderator placed at the side of the cold moderator of Figure 1.

82 The wavelength spectra, divided by the brightness of the 10-cm-tall moderator, thus representing the
 83 brightness gain as a function of the wavelength relative to the 10 cm moderator, are shown in Figures 4
 84 and 5. There is a qualitative difference between the gain from the thermal moderators and parahydrogen, as
 85 a function of the wavelength: while for thermal neutrons the gain does not vary much within the wavelength
 86 span shown in Figure 5, a strong variation is observed for cold neutrons.

87 For the determination of the optimal height of the moderator, and in general for its neutronic design, we
 88 considered integrated cold and thermal brightness in different energy ranges of interest for most common

Figure 5. Same as Figure 4, for thermal neutro.



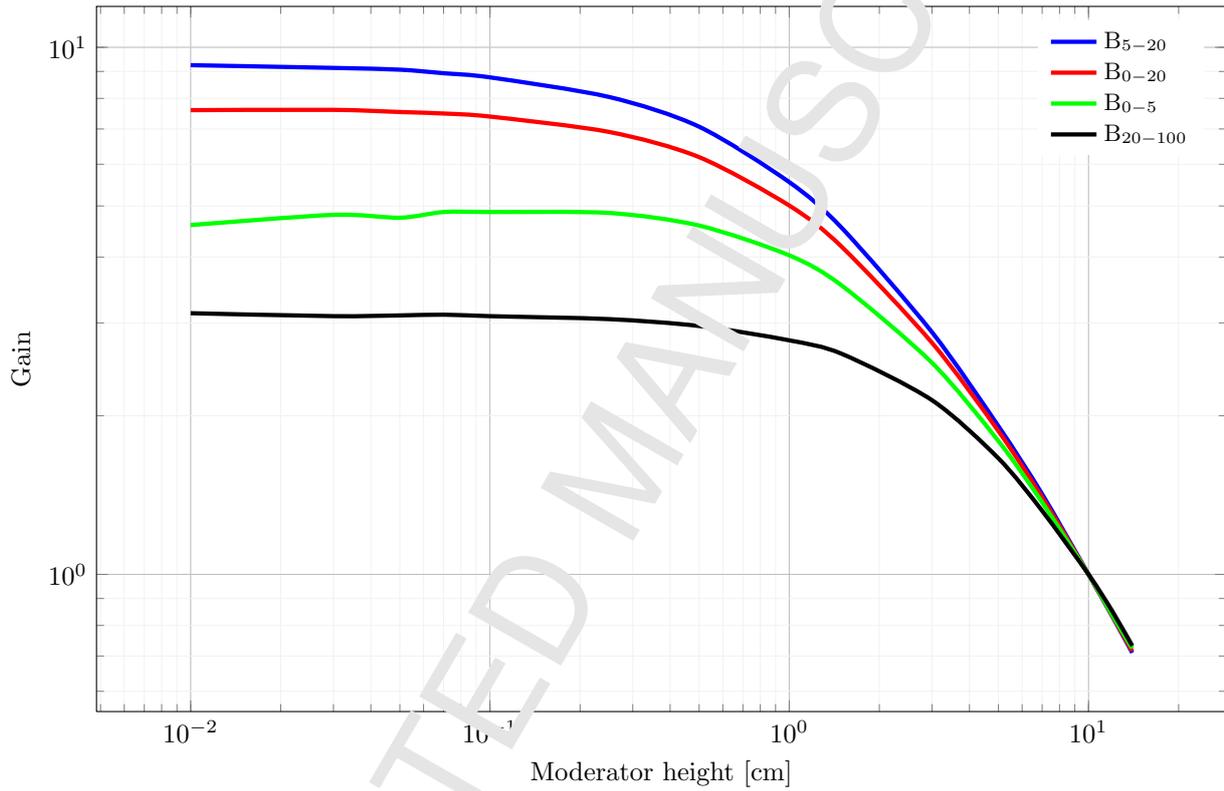


Figure 6. Cold and thermal integrated brightness as a function of moderator height, calculated from the geometry of Figure 1. Neutrons are extracted in an exit direction perpendicular to the incoming proton beam, at the center of the 120° sector of Figure 1. The brightness is calculated for a 6-cm wide horizontal width, the vertical range being equal to the parahydrogen height. Integral brightnesses are relative to the brightnesses for the 10 cm high moderator.

89 applications in neutron scattering (see AppendixA): for cold neutrons, B_{0-5} below 5 meV (4 Å), B_{5-20}
 90 between 5 meV and 20 meV (2 Å), averaged over the cold moderator surface. For thermal neutrons,
 91 B_{20-100} , between 20 meV and 100 meV (0.9 Å), averaged over the thermal moderator surface, was used.

92 Figure 6 shows the relative gain in thermal and cold brightness as a function of the moderator height, for
 93 integrated brightness in different energy ranges. We observe for all (thermal and cold) integrated brightnesses
 94 a general increase by reducing the moderator height.

95 We argue in the following that the gains observed are in part due to general properties of hydrogenous
 96 moderators, related to the mean free path of thermal neutrons in such materials. The additional gain in
 97 parahydrogen with respect to water can be attributed to the properties of its total neutron cross section.
 98 The gain is particularly strong for the cold moderator in the wavelength region between about 1 Å and
 99 3 Å (Figure 4).

100 B_{5-20} reaches a constant value for moderator height approaching zero. For colder neutrons, B_{0-5} slightly
 101 decreases after reaching a maximum for about 2 mm height.

102 The total cross section in parahydrogen for neutrons in the thermal region is about $\sigma=20-30$ barn, which
 103 translates to a mean free path (MFP) in parahydrogen of about 1 cm. For water, the MFP of thermal
 104 neutrons is about 0.3 cm. For the moderator height d much lower than the MFP, the number of collisions,
 105 including those leading to neutrons exiting the moderator, is proportional to σd ; as the brightness is averaged
 106 over the emission surface with area $A = Wd$ (the product of width W and height d), one can expect that
 107 for small moderator thicknesses B is independent of d . This explains the near constant value of B observed
 108 in Figure 6 for low moderator heights.

109 We consider in the following subsections different contributions to the observed gains. We discuss first
 110 the role of the reflector.

111 2.2. Reflector response

112 The reflector surrounding the moderator has the function to return neutrons that have not gone through
 113 the moderator, or that have escaped from it, to the moderator itself, giving them another chance to be
 114 moderated and redirected towards the beam extraction channels. For long pulses the time response of the
 115 reflector (of the order of 100 ns) is of no concern. Beryllium is the material of choice for reflectors in pulsed
 116 neutrons sources. The removal of beryllium around the moderator to extract thermal and cold neutrons has
 117 the effect of reducing the brightness with respect to the maximum theoretical *unperturbed* brightness, i.e.,
 118 the configuration where the moderator is fully surrounded by reflector material.

119 The amount of reflector material removed increases with the height of the moderator, if neutrons are ex-
 120 tracted from the entire moderator surface. However, it also varies in the horizontal plane (where instruments
 121 are placed), depending on the beam extraction configuration and in particular on the number of beamlines
 122 that point to the moderator.

123 We therefore consider separately these two aspects: the effect of the removal of reflector material for
124 moderators of different height, and the effect of removal of reflector material in the horizontal plane of beam
125 extraction.

126 In Ref. [5] we examined the unperturbed brightness. Comparing the unperturbed brightness of 10 cm
127 and 3 cm tall moderators, it was found that the 3 cm tall moderator is 1.6 times brighter than the 10 cm tall
128 moderator, for neutrons below 5 meV. It was also found that for a 10-cm tall moderator, the unperturbed
129 brightness is a factor 1.7 higher than the *perturbed* brightness, calculated for a configuration with two 60°
130 beam extraction openings in the reflector.

131 On the other hand, from Figure 6 the cold perturbed brightness difference between two moderators with
132 height of 10 cm and 3 cm is of a factor 2.5, which is close to the product of the two gain factors. Thus it
133 appears that the overall brightness increase effect is due to two main factors, of roughly equal amount; one
134 due to removal of reflector material, the other, observed in the comparison of the unperturbed configuration,
135 due to other physics effects. It is however not possible to fully disentangle the two effects: in the unperturbed
136 configuration, by reducing the height of the moderator the amount of beryllium is also increased; therefore
137 the brightness increase in the unperturbed configuration is due in part to increase of reflector, in part to
138 additional physics effects discussed below.

139 Besides the effect of the reflector on the different heights of the moderator, there is an effect also on the
140 angular size of the opening for beam extraction. Instruments at ESS will be arranged around the moderators
141 covering four angular sectors of 60°, which will be paired forming two large angular sectors of 120°, one
142 consisting of the North and West sectors the other one of the South and East sectors (see Figure 7).

143 In order to further study the effect of the reflector removal, we considered two geometries (Figure 8),
144 with different openings in the reflector, which were both considered for ESS: a configuration with two large
145 opening configuration of 120°, with 21 beamports per opening, and a configuration of two openings of 60°,
146 with 11 beamports per opening.

147 Figure 9 shows the brightness distributions for individual beamports. As a result of the reflector removal,
148 going from 60° to 120° results in an average brightness loss of 6% for the 3 cm moderator, while it is twice
149 as much for the 10 cm moderator. The effect is larger for a taller moderator, because of the larger amount
150 of beryllium removed.

151 In the original design of the TDR two identical volume moderators (placed above and below the target)
152 viewed two face-to-face openings of 60° [1], so that half of the beamports of one 120° sector would point to
153 the top moderator, the other half to the bottom. This had the advantage that each moderator would have
154 two openings of 60°, and not of 120°, thus increasing the amount of reflector surrounding the moderator.
155 It had however the disadvantage that two different moderators had to be operated, as the use of a single
156 moderator for the whole instrument suite would have resulted in a too big loss of brightness. Such loss
157 would be lower in the case of low-dimensional moderators.

158 A goal of ESS is to provide a beamport grid covering an angle of 240° . In practice the choice, by using
159 low-dimensional moderators, is between a single flat moderator with two 120° openings, or two identical flat
160 moderators, placed above and below the spallation target, with two 60° openings each. As shown in Figure 9,
161 the difference in brightness is of about 6 %. This is calculated considering a flat moderator above the target,
162 and a steel reflector at the bottom. In reality, if a flat moderator with two 60° openings is placed at the top,
163 another moderator must be placed at the bottom. Cross-talk effects between top and bottom moderator
164 exist (see Section 2.8), according to which the brightness of a moderator is reduced, if another moderator
165 is placed below the target, by at least 5 %. Therefore, a single low-dimensional moderator with two 120°
166 openings will have in a real situation about the same performance as two low-dimensional moderators with
167 two 60° openings each. The performance of the single moderator can be further increased if a fast neutron
168 reflector on the other side of the target is designed to increase its performance (see Section 2.8), which is
169 not possible if there are two moderators.

170 In summary, we see that the effects related to the reflector play two roles, both in advantage of low-
171 dimensional moderators: first, the brightness increase effected by reducing the moderator height; second, the
172 possibility to use a single moderator, which would not have been acceptable for tall moderators, because of
173 the stronger brightness decrease.

174 The latter finding had a profound influence on the design of the ESS facility, as it was understood at
175 an early stage that only one low-dimensional moderator was needed. By following this path, options on
176 the use of a second moderator from the start of ESS were investigated. After the realization that all of
177 the ESS initial instruments would perform well by pointing at the top moderator, as discussed in [13], the
178 decision was that only one moderator would be installed at the start of ESS, thus adding a wide array of
179 possibilities for future upgrades using the place below the target. Such an approach also reduces costs and
180 risks of malfunction.

181 2.3. Physics effects

182 2.3.1. Parahydrogen

183 Liquid parahydrogen is the chosen material for cold neutron production at ESS, and is used in other
184 facilities including J-PARC. The advantage of using pure parahydrogen, as opposed to a mixture of ortho-
185 and parahydrogen, stems from the peculiarity of its total neutron cross section [14, 15]: below about 80 meV
186 the total cross section starts decreasing, from a value of about 30 barn, until reaching about 1 barn below
187 15 meV. The reason for this drop is due to the spin-dependence of the neutron-proton interaction, and to
188 the spin-dependent interference between the neutron wave functions scattered from the two protons in the
189 hydrogen molecule [16]. At 20 K, 99.8 % of hydrogen is in parahydrogen form at thermal equilibrium [17].
190 As the main reaction for neutrons in the meV energy range is the para- to orthohydrogen spin-flip transition,
191 which requires 14.7 meV, this reaction is not possible below this energy, explaining the drop in the cross

192 section. The inelastic cross section for para- to orthohydrogen, in the range between 14.7 meV to about
193 70 meV, increases from about 1 barn to about 30 barn, which is comparable to the elastic scattering in
194 orthohydrogen at the same energy. The density of liquid hydrogen and the behavior of its cross section
195 are responsible for several effects relevant to moderator neutronics, namely: the thermalization of the
196 neutrons in about 1 cm from the moderator walls; the near-transparency to cold neutrons; the non-complete
197 thermalization of the neutron spectrum.

198 The neutron spectrum entering the moderator has a strong thermal component, due to the presence of
199 the premoderator on one side (between target and moderator), and of the beryllium reflector, which returns
200 partially moderated neutrons to the moderator, on the other side. Figure 10 shows the energy spectra
201 calculated in regions above and below the moderator, namely the water premoderator, and a cooling water
202 layer placed in the bottom part of the reflector. Neutrons from the reflector side are mostly thermalized.

203 In Figure 4 a peak in gain factor is observed for neutrons in the wavelength range between about
204 1 Å and 3 Å, corresponding to an energy range between about 9 meV and 80 meV. These neutrons are not
205 fully thermalized in the moderator, and most of them have probably only one collision before exiting the
206 moderator. Because of the small MFP, such neutrons are concentrated on the edges of the moderator, on
207 both target and reflector sides. Due to the sudden drop of the total neutron cross section in parahydrogen
208 below 70 meV, the MFP of cold neutrons increases to about 10 cm: the medium becomes *quasi-transparent*
209 to cold neutrons which therefore have low probability to be scattered.

210 This effect is most evident in Figure 11, which shows the vertical distribution of the brightness for
211 neutrons in the wavelength range between 1.5 Å and 2.2 Å (i.e., corresponding to B_{17-36} , where the gain
212 observed in Figure 4 is maximum), for moderators of 1.5 cm, 3 cm and 10 cm height. The two peaks get closer
213 to each other for flatter moderators. The fact that, for this energy range, the brightness is enhanced at the
214 edges of the moderator, explains the large gain seen in Figure 6: for the 10 cm tall moderator, the brightness
215 in the central part of the moderator is strongly reduced, leading to a surface-average brightness decrease. The
216 concentration of neutrons towards the edges of the moderators is also evident in the brightness distribution
217 maps of B_{0-20} shown in Figure 12 for moderators of height of 1.5 cm, 3 cm and 10 cm. These maps are pinhole
218 images of the brightness distribution on the moderator surface. For the 10-cm tall moderator there are two
219 areas in the moderator of increased brightness, one on the bottom side of the moderator (the target side),
220 one on the top part (the reflector side). A similar figure was calculated for the coupled parahydrogen volume
221 moderator at J-PARC [18]. This non-uniform brightness distribution has been experimentally confirmed
222 by a brightness map measurement of the J-PARC coupled moderator [19]. Our calculations show that the
223 effect is much less pronounced for the 3 cm moderator, and almost cancelled for the 1.5 cm one. This feature
224 is apparent also from Figure 13 and Figure 14 in which the brightness B_{0-20} and B_{0-5} projection across
225 the moderator height, as a function of the vertical position, for three pancake geometries of 1.5 cm, 3 cm
226 and 10 cm height, is shown. The increase of the brightness at the moderator edges is less pronounced for

227 colder neutrons. We interpret this result as due to the fact that to slow down neutrons from thermal to cold
228 energies below 5 meV on average requires more than one collision, which would extend the volume of the
229 production region of neutrons of this energy.

230 2.3.2. Water

231 The brightness increase is observed also for the water moderator, although less pronounced than for
232 parahydrogen: it is of about a factor of 2 (Figure 6), from a 10 cm moderator to a 3 cm moderator.

233 We can expect the reflector effect to be similar for water and parahydrogen. The MFP of thermal
234 neutrons in water is 3 mm, which contributes to an increase in brightness for low dimensional moderators.
235 However, the edge effects observed for parahydrogen, due to its cross section, cannot be observed in water,
236 and therefore the overall gain is lower. Figure 15 shows the distribution of B_{20-100} across the height of the
237 water moderator. As expected, an overall brightness increase is observed, but without edge effects.

238 2.3.3. Directionality

239 The moderator and reflector response, combined with the properties of the parahydrogen, result in a
240 directional emission of low-dimensional cold moderators: the moderator-shape induced directionality trans-
241 lates into higher flux in the horizontal direction with a roughly triangular angular dependence and a FWHM
242 of about 40° . See Figure 16, as well as Ref. [6]. The physical reason for the directional emission is related
243 to the properties discussed above; the cold neutron density increases near the interface of a parahydrogen
244 moderator with the reflector within a depth of the order of the mean free path of the thermal neutrons
245 in parahydrogen (about 1 cm). The cold neutron emission from a parahydrogen moderator, in contrast,
246 effectively happens from a volume within the 10-times higher mean free path of cold neutrons measured
247 from the neutron emission window of the moderator. Thus the neutron emission probability is higher in
248 directions where a larger volume of the moderator material is seen.

249 In contrast and comparison the angular distribution in the vertical direction of the thermal neutron
250 beam from the water moderator (Figure 17), shows a much lower directionality. The directionality of the
251 water moderator in the vertical direction roughly follows the expected cosine dependence [26], displaying a
252 broad peak falling to zero intensity at 90° .

253 2.3.4. Neutron absorption

254 Due to the significant absorption cross-section of thermal neutrons (0.3 barn at 2200 m/s) in hydrogen,
255 a volume moderator tends to function as a parasitic absorber. This absorption term is reduced in a flat
256 moderator, due to the lower content of hydrogenous material. We calculated that about 10% of the neutrons
257 entering a 10 cm tall cylindrical moderator are captured in hydrogen, while about 3% are captured in a
258 3 cm tall moderator. Therefore the relative gain in using a flatter moderator is at the per cent level. Similar
259 gains are found for water.

260 2.4. Total neutron emission and heat load

261 Figure 18 illustrates two additional aspects of low-dimensional moderators, by comparing total neutron
262 emission and heat load in the cold moderator as a function of the moderator height. The total neutron
263 emission or *intensity* is proportional to the product of the brightness and the area of the emission surface of
264 the moderator.

265 The total intensity approaches a maximum for moderator heights larger than about 3 cm: a 3-cm
266 tall moderator, while it is about 2.5 times brighter than a 10 cm one, delivers roughly 80% of its neutron
267 intensity. The higher brightness almost compensates the smaller emission surface by providing a total number
268 of emitted neutrons almost as high. Above 10 cm height, the total number of neutrons emitted approaches
269 a constant value. The implication of this result is that to increase the intensity of neutron emission one
270 should not increase the height of a parahydrogen moderator. Rather other types of moderators should be
271 considered, such as large-volume D_2 moderators.

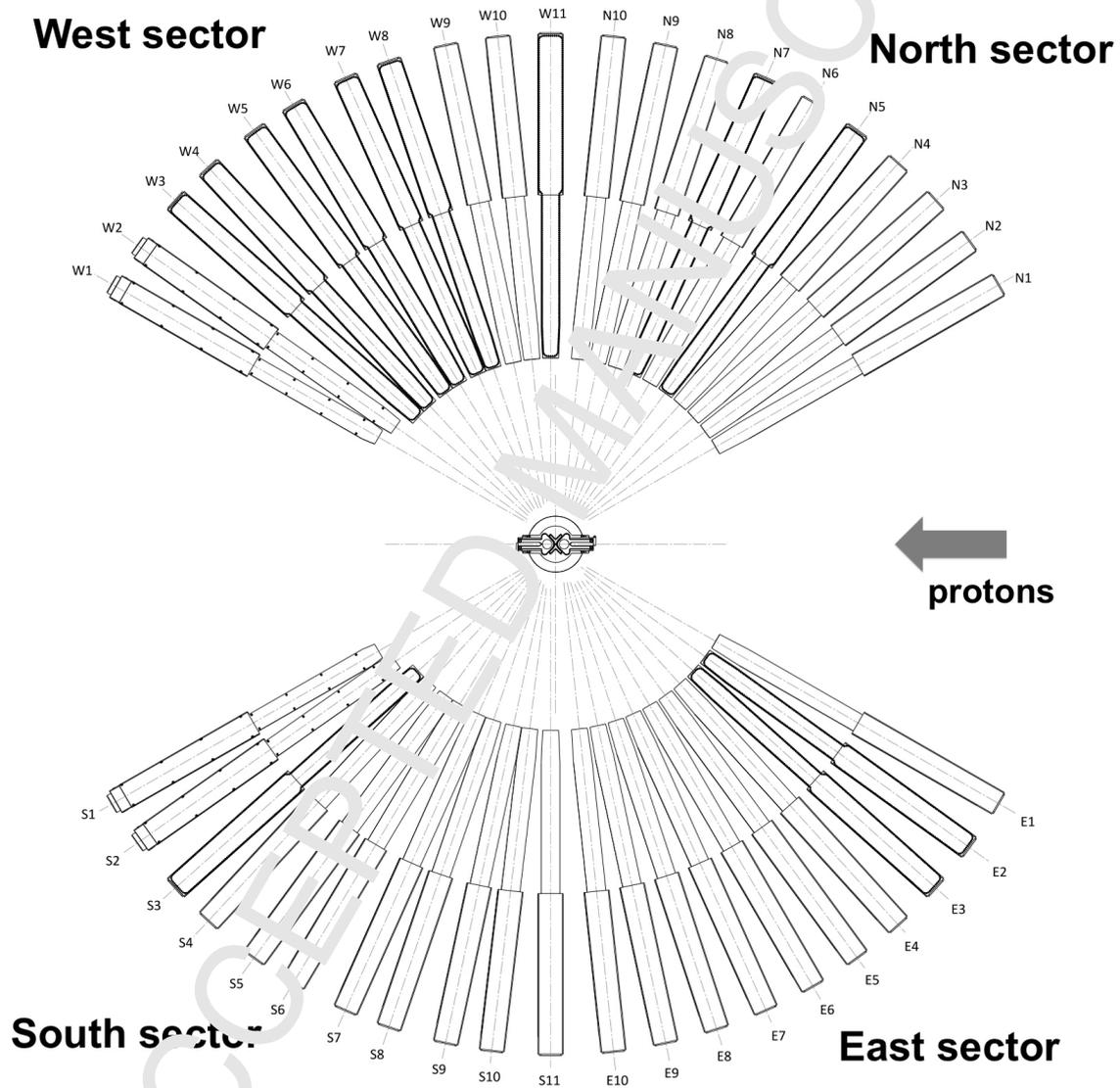
272 The heat load in the moderator (parahydrogen and aluminum cryogenic parts) increases with the mod-
273 erator volume (black curve in Figure 18). Thus, flat moderators have an advantage in terms of requirements
274 on the total capacity of the cryogenic systems. It must be noted however that there are other challenges in
275 the design of the cooling of cold moderators, related to the peak heat deposition in the system, and to the
276 flow rate of the hydrogen, that must be addressed in the engineering design.

277 2.5. Premoderator

278 The premoderator changes the shape of the neutron spectrum from the spallation target, bringing neutron
279 energies down from the MeV to the thermal range. Usually the premoderator is a layer of water between
280 cold moderator and target. Its thickness is determined by a balance of optimal spectral shaping, by the
281 need to minimize the distance target-moderator, and to minimize neutron absorption.

282 A thickness of 3 cm was found as optimal; concerning the lateral dimensions, we found that a disk-
283 shaped, extended premoderator, with radius practically equal to the Be reflector, gives a substantial gain
284 in both thermal and cold brightness. Figure 19 shows the relative variation of cold and thermal moderator
285 brightness with the radius of a disk-shaped premoderator. In this sensitivity study, the gain is different
286 depending on the material placed outside the premoderator, i.e., in the ring with inner radius equal to the
287 radius of the premoderator, and outer radius equal to the radius of the beryllium reflector. If there is void,
288 there is a steady increase of both thermal and cold brightness, reaching the maximum for a 30 cm radius
289 disk. By placing a reflector material (in this case, beryllium with 30% water cooling), there is a maximum
290 cold brightness for a premoderator of about 15 cm radius. This could be an option for future upgrades. The
291 present configuration has a steel ring with inner radius of 30 cm.

Figure 7. View of the 42 ESS beamport inserts each of 3.5 m length, located in four beam extraction sectors of 60° . The proton beam comes from the right in the figure. The tips of the beamports are at 2 m from the center of the moderator. The beamports are labeled according to the name of the sectors (North, South, East, West). The angular spacing between beamports in the North and East sectors is of 6° . In the West and South sectors alternating angular spacing of 5.7° and 6.3° between the beamports is used.



2.6. Orthohydrogen contamination

Figure 20 shows the variation of the cold brightness from a 3-cm tall moderator (in this case of butterfly-2 type, see Section 3.3) as a function of the parahydrogen fraction in the moderator. Maximum performance of low-dimensional moderators requires pure parahydrogen and ideally 100 % parahydrogen should be used. The aim during ESS operation is to achieve a parahydrogen fraction of at least 99.5 % by using catalyzers. Thus small fractions of orthohydrogen are expected, which may slightly affect the neutronic performance of the moderator. In our calculations we assumed 99.5 % parahydrogen, but we had to specify it as 100 % in the model; the reason is because recent experimental results [15] indicate that the ENDF/B-VII measured cross section did not account for an impurity of orthohydrogen of 0.5% in the hydrogen samples.

In the following two subsections we discuss two properties which are not specific to low-dimensional moderators, but are linked to the design of the moderator systems. The information on the size and location of hotspot of neutron production indirectly dictates the dimension of the moderators, as well as the ideal location of the cold and thermal neutron moderators. The cross-talk between the areas above and below the target is also of interest and can be possibly exploited to increase the moderator brightness.

2.7. Hotspot

Figure 21 shows the map of high-energy ($E > 0.1$ MeV) neutrons from the spallation-evaporation process in the tungsten, assuming 2 GeV protons. The plane of the color map is at the vertical coordinate $Z=8$ cm, just above the tungsten target and below the water premoderator. To give an idea of the relative dimensions of the moderators and of the neutron hot spot, the geometries of the butterfly (discussed in detail in Section 6) and pancake moderators are superimposed to the neutron flux map, even though the moderators are placed above the plane where this fast neutron map is calculated. The dimensions and lateral positions of both moderators in this figure are optimized for maximum cold brightness across the 120° sectors. This figure confirms that the dimension of the moderators should be comparable to the source of spallation-evaporation neutrons, as expected. This figure also suggests that it is convenient, if possible, to place both thermal and cold sources above the hot spot. This is one of the arguments in favor of the butterfly moderator (see Section 5) and the thermal moderator brightness is higher if the water moderator is placed closer to the center of the hot spot.

2.8. Cross talk between moderators and fast neutron reflectors

The beam extraction system at ESS is designed such that neutrons can be extracted from two angular sectors of 120° each, from above and below the target. The two beam extraction areas above and below the target are not completely independent of each other as neutrons generated or reflected in one region of the target can travel to the other side if their energy is high enough to cross the target wheel. The size of this effect might be increased by the lack of moderating material in the target, which would increase the

325 absorption of neutrons in the target itself. Thus, the brightness of the moderator placed above the spallation
326 target may depend to some extent on what is placed on the other side.

327 At ESS this opportunity can be exploited, considering also that ESS is a long pulse facility, and therefore
328 an increase of the width of the time distribution of the neutrons within the long pulse is not of primary
329 concern. If only one moderator system on the top side of the target is present, it is worthwhile considering
330 different options to design a fast neutron reflector placed below the target to increase the brightness of the
331 top moderator. Such study can be of interest also if two moderator systems are implemented, at least in
332 some cases, for instance if the second moderator system requires a significant neutron and gamma shielding
333 to allow reaching very low temperature (this is the case for some moderators for Ultra Cold Neutrons or Very
334 Cold Neutrons) [20–22]. In that case, the presence of these shields, which are typically heavy metals (such
335 as Bi or Pb) with good properties of fast neutron reflection, could be exploited to increase the brightness of
336 the top moderator.

337 We considered a few cases using some typical fast neutron reflector materials. Table 1 indicates the
338 gain factors relative to the two-moderator configuration, i.e., a configuration where a moderator/reflector
339 system similar to the top one is placed at the bottom. This is the configuration that results in the lowest
340 brightness, due to the presence of the extended pre-moderator, as well as the water moderator and coolant,
341 which thermalize the fast neutrons preventing them from crossing the spallation target and reaching the top
342 moderator. On the other hand, if materials that can reflect fast neutrons, such as copper, lead, tungsten, or
343 steel, are used, a significant brightness increase is obtained on the moderators placed at the top. If beryllium
344 is used at the bottom, the brightness increase is not as large as for heavier metals. This is due to the fact
345 that in beryllium neutrons are reflected but also partially slowed down, and a significant part of the neutrons
346 reflected will be absorbed by the tungsten target.

347 The effect depends on the material used, but also on the amount of water coolant used. The calculations
348 with a tungsten reflector are performed using the same effective density of the tungsten in the spallation
349 target, and assuming helium cooling. It is worth noting that the reflectors absorb a heat load of the order
350 of 500 kW (calculated for steel reflector). Their cooling is therefore quite demanding.

351 2.9. Background from high energy neutrons

352 Neutron scattering research mainly uses slow neutron beams with energies below a few eV. Fast neutrons
353 can preferentially escape the target shielding through the slow neutron beamports. They are also emitted by
354 scattering on the structures around the moderators also viewed by the beam lines. High-energy neutrons can
355 be thermalized by scattering on structures and materials in the experimental halls and ultimately contribute
356 to the background of the slow neutron detectors in the neutron scattering instruments. This is an issue
357 for all neutron sources; we want to investigate if in the *low-dimensional* moderator concept adopted for ESS
358 the slow neutron signal to fast neutron background emission ratio will be more or less favorable than for

359 existing spallation sources.

360 2.9.1. Figure of merit

361 The figure of merit (FOM) in neutron data collection can be conveniently defined as the square of the
362 signal-to-noise ratio (where by definition both signal and noise are expressed in units of counting time). This
363 corresponds to the data collection rate, i.e. the inverse of the time needed to achieve a given signal-to-noise
364 ratio. The *noise* must be defined as the uncertainty of the measured value of the signal S .

365 There are two main sources of uncertainties: the statistical precision of the counts measured and the
366 systematic uncertainties and instabilities, which are independent of counting statistics. Considering the
367 issues we are concerned with here, we can restrict the analysis to the statistical precision of the data
368 (assumed to be stable and understood concerning their origin). Other systematic errors are independent
369 of the neutron beam intensities, but of course they become more and more dominant, as the statistical
370 accuracy of the data improves, e.g. by the new level of neutron intensities ESS will offer.

371 The statistical noise of the signal S will be proportional to $\sqrt{S+B}$, where B is the background. The
372 measured raw neutron counts for both S and B are proportional to the data collection time t , thus the
373 data collection rate is the inverse of the time needed to achieve a given statistical signal-to-noise ratio. The
374 background B has two main components: B_S coming from the slow neutrons delivered to the sample and
375 its environment for the intended observations (usually the main part of B) and B_F due to fast neutrons
376 coming through the beamline or through the shielding of other beamlines, etc. Thus

$$\text{FOM} = \frac{S^2}{S + B_S + B_F} \quad (1)$$

377 In the denominator the first two terms are proportional to the slow neutron beam intensity, the last to
378 the fast neutron production.

379 Shielding measures that reduce B_F without any effect on S are always useful, to varying degrees. If such
380 a measure impacts both S and B the balance is what matters. For example, if both the slow neutron and
381 the fast neutron production change by the same factor n , the change of FOM will be proportional to n . So
382 the data collection gains of ESS compared to other facilities will be proportional to the delivered neutron
383 beam intensities (i.e. some 10–100 times higher than the other sources) under the assumption that the fast
384 neutron background also increases in the same proportions. If the fast neutron background increases less
385 than proportionally to the slow neutron production rate, the FOM will be for some experiments higher than
386 proportional to the beam intensity gain, primarily in cases where B_F is comparable to or larger than S .

387 2.9.2. Fast neutron background at ESS.

388 The total number of fast neutrons emitted is, as for all neutron sources, about the same as that of the
389 moderated neutrons, and it is the beam extraction and shielding equipment that ensures that only a very

390 small fraction of these neutrons turn up as counts in the detectors (which have in addition low detection
391 efficiencies for fast neutrons).

392 Figure 22 shows the simulated vertical distribution of the points of emission of neutrons with $E > 1$ eV
393 from the moderator area, for three different pancake moderator heights.

394 These “emission points” are defined by the backward extrapolation of the neutron trajectories entering
395 the beam line openings to their crossing of the nominal neutron emitting surface of the cold moderator or
396 to its vertical continuation. In reality, these neutrons are directly generated either by collision with atoms
397 in the volume of the moderating material or by collision with atoms in the structures around the moderator
398 such as the moderator vessel, its insulating housing, the reflector and the collimators.

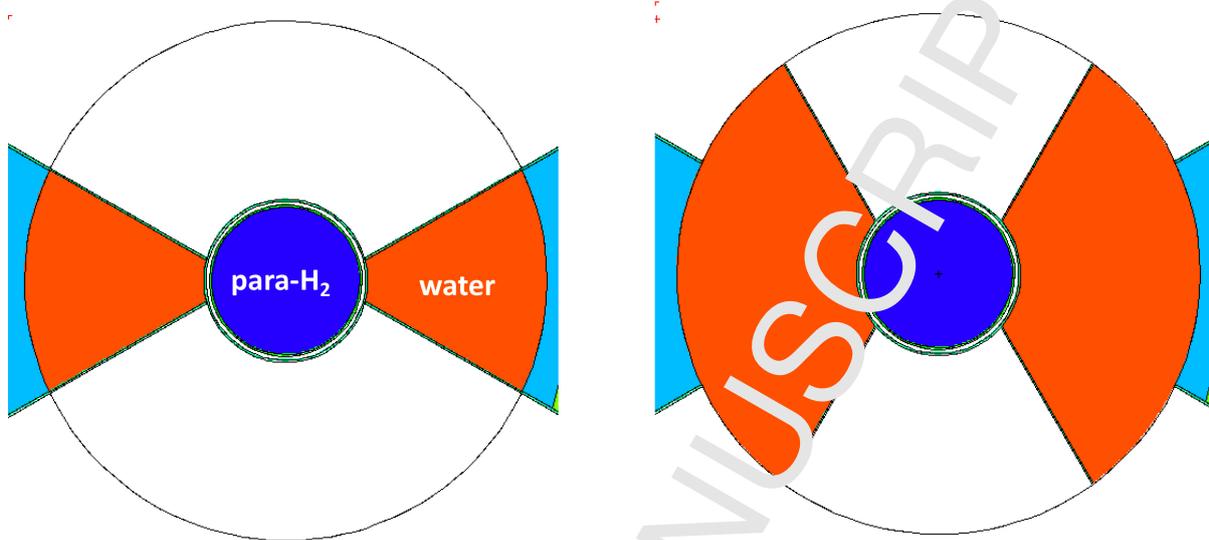
399 Since the back trajectory simply follows the direction of the neutron as determined at radius 2 m, the
400 method implicitly assumes that no scattering along the trajectory occurs. For neutrons originating elsewhere
401 than from the moderators, this assumption is not strictly valid, causing a “blur” to the apparent emission
402 point of these neutrons.

403 The main conclusions from the figure, and considering also Figure 14, can be summarized as follows:

- 404 - The total fast neutron emission by flat moderators is less than for the tall one (about 50 % for 1.5 cm
405 moderator height and about 67 % for 3 cm moderator height).
- 406 - There is some fast neutron emission outside the moderator window, which amounts to about 36 % of
407 the total fast neutron emission for the 10 cm moderator, 45 % of the total for the 3 cm high moderator,
408 and 51 % of the total for the 1.5 cm high moderator.
- 409 - The ratio of the deliverable cold neutron intensity (which scales with the brightness) to the total fast
410 neutron emission is about 3 times more favorable for the 1.5 cm moderator than for the 10 cm one.

411 Based on the results in Figure 22, Figure 23 shows the relative evolution of the ratio S/B_F of the signal
412 (which is proportional to the cold neutron brightness B_{0-5} , cf. Figure 14) to the emission of > 1 eV fast
413 background neutrons that are coming from the central 8 cm high effective neutron emission area around the
414 middle of the moderator. This means that the assumed background emission conservatively also includes
415 fast neutrons coming from outside the nominal moderator emission surface for moderators of < 8 cm height,
416 while fully excluding these neutrons for taller moderators.

417 Our MCNPX simulations of detailed models of the ESS target monolith system have shown that the
418 neutron moderators and their immediate vicinity emit towards the beam-line openings in the monolith
419 shielding about as many > 1 eV energy “fast” neutrons (which are assumed to contribute to the background
420 detected at the instruments) as slow neutrons for use in neutron scattering experiments on the instruments
421 (cfr Figure 14 and Figure 22). The emission of fast neutrons geometrically peaks at the edges of the
422 moderators, including areas around and outside the viewed nominal face of the moderator. The ratio of

Figure 8. Pancake geometry, with openings in the reflector of 120° (left), and 60° (right).

423 slow to fast neutron emission is significantly more favorable for the low dimensional, flat ESS moderators
 424 than for the conventional larger beam cross section moderators at existing spallation sources.

425 3. Moderator concepts

426 In this section we describe the moderator concepts that were considered for ESS. We start from the
 427 volume-moderator configuration of the TDR, then two low-dimensional moderator concepts which were
 428 seriously considered for the facility are described.

429 3.1. Volume moderator: TDR

430 The TDR design was based on the J-PARC coupled volume parahydrogen moderator [18]. In the TDR
 431 baseline configuration, there are two volume moderators filled with pure parahydrogen. The MCNPX model
 432 shown in Figure 24 reproduces the engineering design developed during the target station design update
 433 phase [1]. The moderators have a diameter of 16 cm and a height of 13 cm. The moderators are surrounded
 434 by light water pre-moderators (except for the cold neutron extraction window), of which the most important
 435 part, from the neutron's point of view, is the layer between target and moderator, which is 2 cm thick. The
 436 window surface of the cold moderators for beam extraction is of $12 \times 12 \text{ cm}^2$. A variation from the J-PARC
 437 design is the presence, on the sides of the cold moderators, of thermal moderators for thermal or bispectral
 438 extraction. They consist of 4 cm thick water slabs with a surface area for neutron extraction of 12×11

Figure 9. B_{0-20} angular distribution for a 3 cm and 10 cm tall pancakes, with 60° and 120° openings in the reflector allowing for 21 and 11 beamports with 6° separation, respectively. The brightness is averaged over the extraction surface, with fixed width of 6 cm, and height equal to the height of the moderator. Beamport angles are defined with respect to the direction of the proton beam, from left to right in Figure 8.

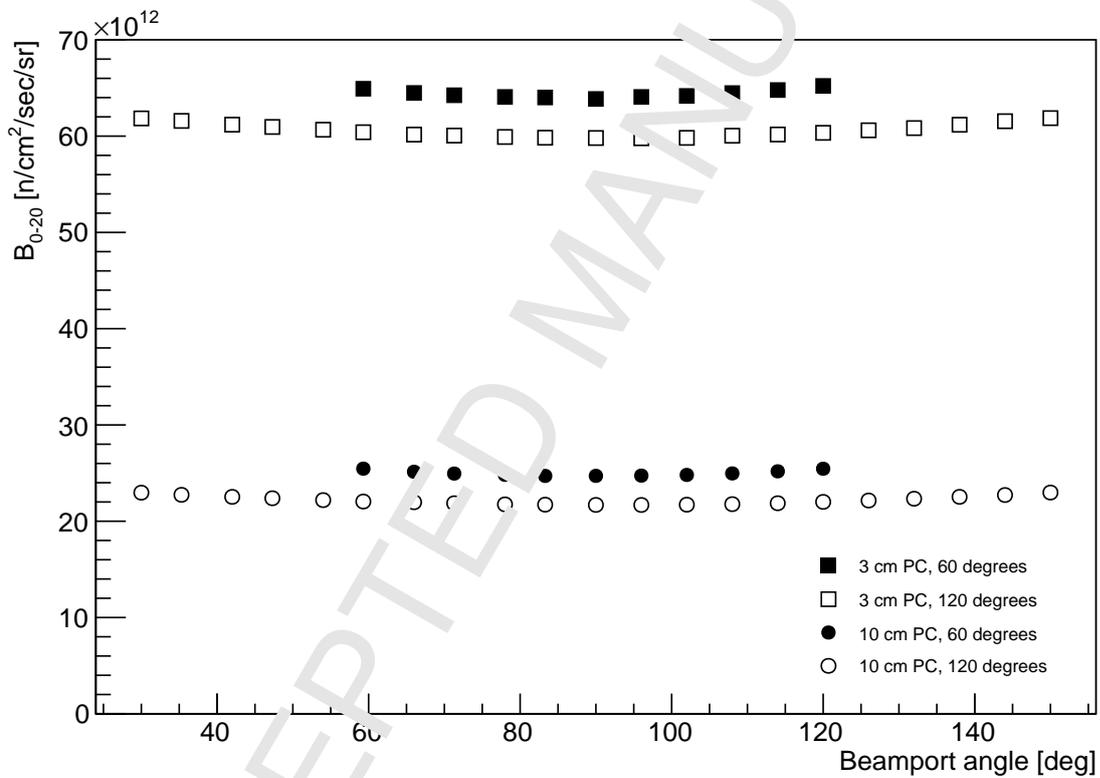
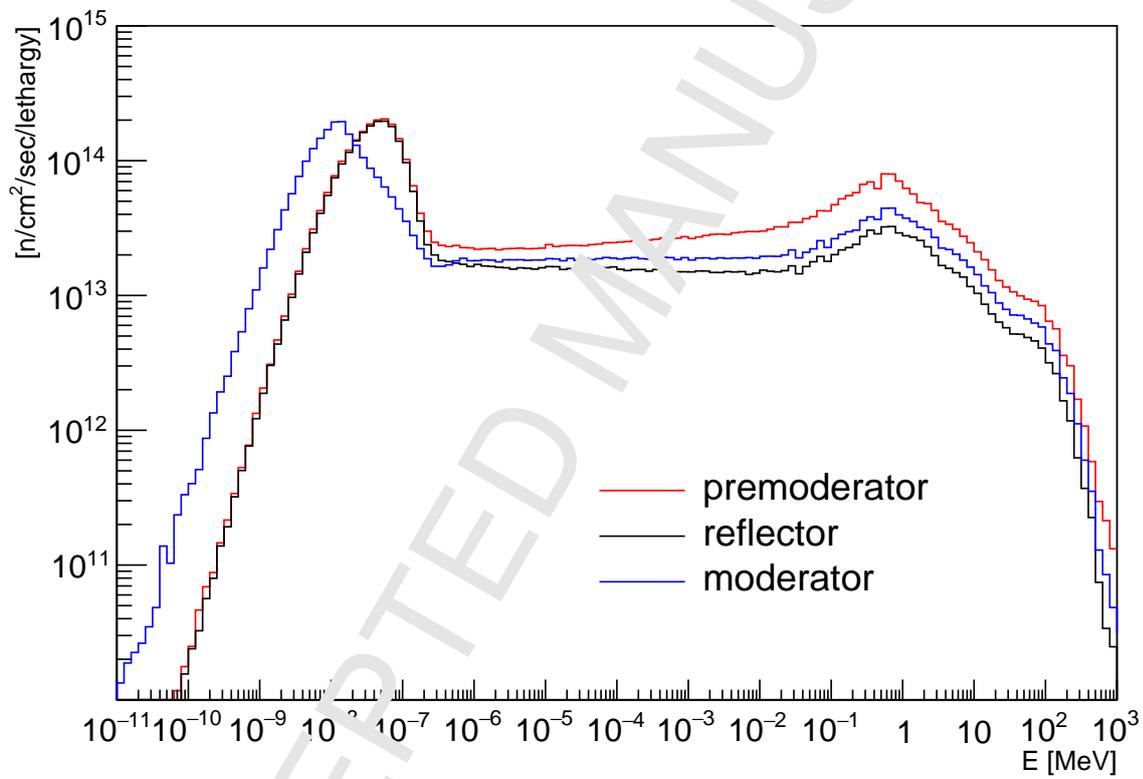


Figure 10. Average flux per unit lethargy inside the cold moderator, the water pre-moderator, and in the bottom part of the reflector, above the moderator. The flux is calculated using the f4 track-length estimator.



439 cm². The openings in the reflector for beam extraction are of 60°, with two openings per moderator, as
440 shown in the figure. There are two identical thermal-cold moderators, one above and one below the target.
441 The openings in the reflector are arranged so that, of the four 60° sectors, each two 60° sectors, above and
442 below the target, form a 120° sector available for the beamports. More information is available in [1, 3].

443 3.2. Pancake low-dimensional moderators

444 The first low-dimensional design considered was the pancake moderator [10], which has been extensively
445 discussed in the previous section, as it forms a convenient basis to determine the properties of low-dimensional
446 moderators. The pancake consists of a disk-shaped (3 cm height, 20 cm diameter) cold moderator (see
447 Figure 1). The basic cylindrical shape comes from the need to serve cold neutron instruments in a 2 × 120°
448 suite. Thermal neutrons are extracted from the sides of the cold moderator which contain water. The need
449 of bispectral extraction implies that a design solution must be found to allow for bispectral extraction. For
450 the pancake, two options are possible, and are discussed in the next section.

451 3.3. Butterfly low-dimensional moderators

452 *Butterfly*-shaped moderators [23–25] consist of a modified version of the pancake, where the thermal
453 source is moved to the center of the moderator. The goal of this design is to adapt to the beam extraction
454 configuration of ESS and provide bright bispectral neutron beams for the whole instrument suite. The first
455 idea behind this concept is to have both thermal and cold sources close to the hot spot of neutron production
456 (see Section 2.7 and Figure 21, left), thus reaching high thermal and cold brightness, and having a design
457 capable of delivering a good bispectral beam over the full 2 × 120° beam extraction sector. Two variants
458 of this design were considered. The first moderator, that will be used at the start of operation, is the
459 so-called *butterfly 2* (Figure 25, bottom). It consists of two distinct cold moderators separated by a thermal
460 cross-shaped moderator and will be operated until the start of the user program. The second variant is the
461 *butterfly 1* (Figure 25, top).

462 The drivers for the butterfly design were the following:

- 463 - place cold and thermal moderators on the hot spot, in order to provide high thermal and cold bright-
464 ness for a required extraction area of at least 3 (height) × 6 (width) cm² for both thermal and cold
465 moderators.
- 466 - exploit to some extent, also the concept of tube moderators (discussed in [6] and in the appendix),
467 thanks to the geometry of the cold moderator.
- 468 - keep a relatively compact shape to ease the beam extraction: for all the 42 beamports, the thermal
469 and cold extraction surfaces lie next to each other, being placed on the two sides of the focal points
470 (see Section 4.4), allowing instruments to see the brightest part of thermal and cold moderators. Such

471 moderators fit well for a beam extraction in the two 120° sectors; the brightness variation across the
472 sectors is within 15%.

473 Before comparing the neutronic performance of the different moderator concepts we describe in detail
474 the beam extraction principles and implementation for ESS, to better understand their role in the design of
475 the moderators.

476 4. Beam extraction

477 4.1. Design features for instrument performance

478 For a high-performance instrument suite, the moderator assembly of any facility for neutron beam
479 instruments needs to be designed with three key performance indicators in mind:

- 480 1. high source brightness;
- 481 2. ability to extract the right amount of phase space for each beamline;
- 482 3. ability to install the required number of beamlines.

483 At ESS, two additional factors were included in the design considerations:

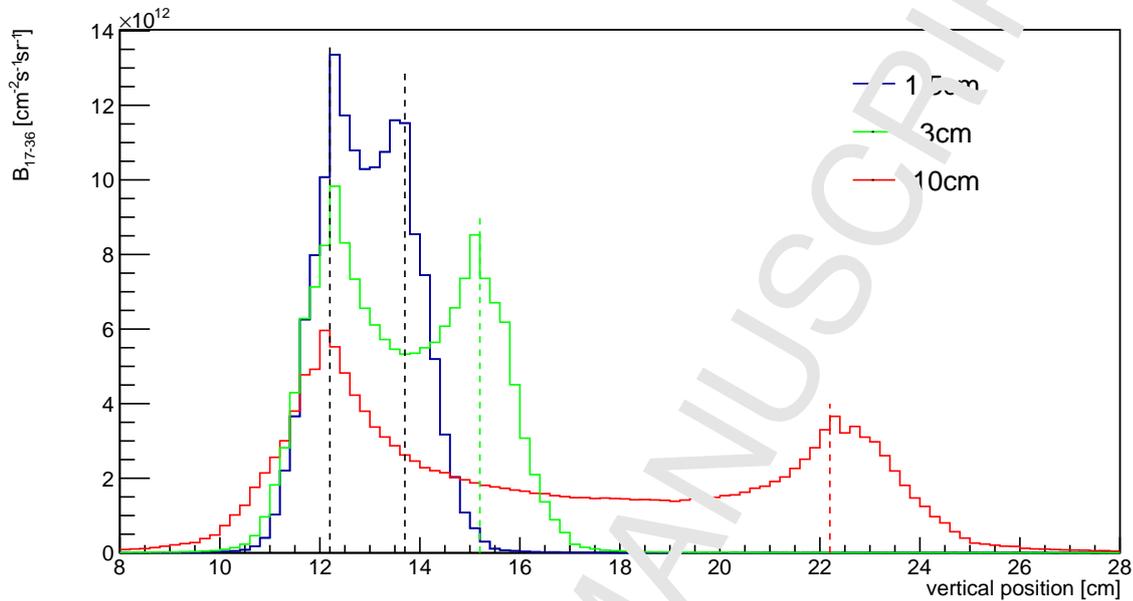
- 484 4. ability of each beamline to freely choose between viewing a cold source, a thermal source, or, using a
485 bispectral mirror assembly, a bispectral source;
- 486 5. upgradeability.

487 Achieving high brightness, the first performance indicator, gave the main figure of merit used in the
488 moderator design and is the main focus of the present paper. However, the other performance indicators
489 were also used in the moderator design. In this section key features of the other performance factors are
490 described, and in particular their link to the design of the ESS moderator assembly. All these performance
491 indicators gave practical constraints and guides on the design of the moderator. This is however only one
492 side of the work, as every proposed design implied an extensive study of the brightness transfer to the
493 instruments, which in turn gave additional inputs to the moderator design, in an iterative process. This
494 iterative work, from the point of view of beam extraction and brightness transfer to the instruments, is
495 described in detail in [13].

496 4.2. Phase space

497 Most neutron beam instruments use the neutron beam to illuminate a sample of a material to be studied.
498 The huge range of types and geometries of samples reflects the diversity of the science which can be addressed
499 with beams of slow neutrons [1]. The main limiting features to the required phase space of the neutron
500 beam are, however, fairly well-known.

Figure 11. B_{17-36} distribution across the moderator height, for cold neutrons, for three cylindrical moderators with 1.5 cm, 3 cm and 10 cm height, for neutrons between 1.5 Å and 2.2 Å. Moderator edges are marked by dashed vertical lines. The vertical position is relative to the center of the spallation target.



501 4.2.1. Beam size

502 The beam size typically needs to be adapted to the sample size. In a few cases, samples can be very
 503 large, up to several metres in linear dimension. However, in these cases, the purpose of the neutron beam
 504 investigation is always to measure local properties with a spatial resolution which is much smaller than the
 505 size of the sample, typically of the order of mm's or less. Most neutron scattering experiments are flux-
 506 limited, due to the intrinsically low neutron source brightness compared to, e.g. synchrotron light sources.
 507 For optimal experimental conditions, sample volumes for neutron experiments are therefore usually fairly
 508 large to compensate for the low neutron flux. For materials characterization, the sample size is typically
 509 limited by the amount which can reasonably be synthesized given the available time and funding. This
 510 results in an upper limit on most samples of the order of a few cubic cm's. In many cases, researchers
 511 wish to measure much smaller sample volumes. There can be many reasons for this, ranging from sample
 512 availability and cost to the need to measure local properties in intrinsically inhomogeneous materials. The
 513 lower limit to the sample volume is almost always determined by the available neutron flux. Typical beam
 514 sizes are therefore in the range of a few mms to a few cms.

4.2.2. Beam divergence

Most neutron experiments are aimed at a measurement of the dynamic structure factor $S(\mathbf{Q}, \omega)$ straightforwardly obtainable from the neutron scattering cross-section, or one of its derived quantities such as the static structure factor or reflectivity profile. The dynamic structure factor contains the essential information on the spatial correlations between atoms (as a function of $\hbar\mathbf{Q}$, the momentum transfer) and their time correlations (as a function $\hbar\omega$, the energy transfer). The spatial resolution which can be achieved depends on the precision with which \mathbf{Q} , the wavevector transfer, can be known. Most diffraction measurements will aim to achieve a \mathbf{Q} -resolution of the order of 10^{-3} or better in $\Delta\mathbf{Q}/Q$. This directly results in divergence resolution of $\Delta\theta/\theta$ of 10^{-3} or better, i.e. a beam divergence of the order of 0.1° . Small-angle neutron scattering can generally tolerate a significantly more relaxed \mathbf{Q} -resolution, but the need to measure at very low scattering angles near the incident beam, usually also requires a divergence of the order of 0.1° . Spectroscopic measurements will usually accept a relaxation of the \mathbf{Q} -resolution in order to gain flux. Today's neutron spectrometers (i.e. instruments for spectroscopic measurements) will typically accept a beam divergence of the order of 1° , and some even $4\text{--}5^\circ$, in order to achieve the flux needed to observe the desired inelastic signal.

A typical instrument will thus need a phase space volume of the order of 10 (cm-deg)^2 with a few instruments requiring much less and a few requiring up to 20 times as much. For each instrument, a phase space of beam area and divergence at the sample can be specified which the neutron source should fill as completely as possible, in order to maximize flux. Each instrument needs to be equipped with a neutron optical system designed to transport this phase space from the source to the sample, while minimizing the loss of phase space density, in accordance with Liouville's theorem (see Appendix A). Such an optical system usually consists of neutron guides in which the amount of phase space which can be transported is roughly proportional to the neutron wavelength squared, due to the reflection properties of the inner guide surface. As a result, the phase space volume delivered to the sample is usually strongly wavelength-dependent and often only reaches the desired value for longer wavelengths.

In terms of the moderator design, these considerations result in a requirement for the minimum viewable surface area of the moderator. However, the amount of phase which can be extracted from the moderator and the heat load and radiation damage incident on the beam optics decrease with the inverse square of the distance from the moderator face to the entrance window of the neutron optical system. The compromise made at the ESS is to start the guide optics at a distance of 2 m from the moderator center. In order to optimally deliver the typically needed phase space volume of 10 (cm-deg)^2 at this distance, the needed viewable moderator surface can be calculated from simple geometrical considerations to be about 20 cm^2 in area, slightly less for thermal neutrons, slightly more for cold neutrons. More information can be found in [13].

549 Of the various moderator geometries described here, the TDR geometry provides the largest viewable
550 surface, of the order of 200 cm^2 , which is more than adequate for the needs of all the instruments. Optimising
551 the height of the pancake geometry presented a challenge, as the brightness increase obtained by reducing the
552 moderator height is to some extent offset by the reduction in viewable area. A trade-off study was performed
553 between these two effects which is described in more detail in [13], evaluating the impact on the flux at the
554 sample for a full suite of instruments, resulting from the compromise between the increasing brightness of
555 the source and the decreasing brightness transfer of the neutron optical system as the moderator height
556 is reduced. The optimal source height was found to be 3 cm, representing the global optimum for the full
557 instrument suite. Once the optimum moderator height was determined for the pancake moderator, it was
558 straightforward to make the same comparison for the butterfly moderator, which display the same height-
559 dependent brightness. The viewable width of the cold moderator in the butterfly geometry is significantly
560 less than that of the pancake moderator, but this turns out not to be a problem, since the width of the
561 cold pancake is much greater than can be usefully accepted by the instruments guide system anyway. The
562 viewable cold surface area of the 3 cm tall butterfly moderator is approximately 25 cm^2 , with some variation
563 with beamport angle. This is sufficient for most instruments. In the case of instruments where a larger area
564 would have been beneficial, the increase in source brightness, compared to the alternative moderators with
565 the larger area, generally more than compensates for the reduced brightness transfer of the system.

566 The feedback of these phase-space requirements into the moderator design was that the extraction
567 surfaces for both thermal and cold moderators should be at least 6 cm wide. As discussed below, the
568 requirement of bispectral extraction and of the number of beam lines, forced the cold and thermal extraction
569 areas to be adjacent.

570 4.3. Number of beamlines

571 The ESS moderators need to permit the extraction of beams for 22 instruments [1]. The instruments are
572 arranged next to each other in experimental halls, such that the beamlines need to be arranged in one or
573 more horizontal fans illuminating the space made available in the halls. Existing facilities typically hardwire
574 the number of instruments into the design of the monolith, by having exactly the number of beamports
575 built into the target monolith corresponding to the number of instruments to be served by the moderators.
576 Given the typical lateral size of neutron instruments and their distance from the target, this has generally
577 resulted in approximately 22 beamports being designed into the monolith, separated by about 12° .

578 ESS has taken a very different approach, in designing 42 beamports into the target monolith with an
579 average angular spacing of 6° . This creates a grid of beamports, from which the 22 beams needed for the
580 currently foreseen scope of the ESS can be extracted, while the remaining 20 beamports will be sealed with
581 temporary dummy plugs. This has the advantage that the facility layout does not need to be determined for
582 its lifetime by the choice of the initial instrument suite. The monolith design with the 42 beamport inserts

583 is shown in Figure 7.

584 The experimental halls of ESS are divided into 4 sectors, of which two (North and East) are similarly
585 sized to existing facilities and will accommodate instruments up to about 60 m in length. The beamports
586 in these sectors have an angular separation of 6° between each. Given the amount of space needed for the
587 instrument components, notably the shielding around the secondary spectrometer, instruments of less than
588 this length will typically need to be separated by about 12° , which will be achieved by activating, on average,
589 every other beamport.

590 The two other sectors (South and West) can accommodate instruments up to 170 m in length. Even
591 instruments with large secondary spectrometers and shielding can easily accommodate instruments on neigh-
592 bouring beamports with 6° of angular separation. Integration of components such as choppers in the area
593 close to the monolith on such closely separated neighbouring beamlines does, however, present a significant
594 challenge. In order to keep this difficulty at a tractable level, the beamport separation in the South and
595 West sectors has been staggered to be alternately 5.7° and 6.5° . In this way, each instrument can primarily
596 concentrate on its integration with the neighbouring instrument on the closer beamline.

597 The ESS design is thus more than sufficient for the 22 instruments foreseen within the current scope of
598 the ESS, and leaves a lot of room for future possibilities.

599 4.4. Spectral freedom

600 The source frequency is one of the most fundamental parameters around which all instruments at a pulsed
601 source need to be designed. The choice of 14 Hz as the repetition rate at ESS was made so as to allow each
602 instrument to benefit from a large bandwidth of neutron wavelengths without suffering from frame-overlap,
603 or needing to suppress pulses, as is commonly done on higher rep-rate sources such as SNS or ISIS-TS1. In
604 order to make the most of this available bandwidth, most of the thermal instruments at ESS choose to use
605 cold neutrons as well. This is typically done using a bispectral switch, a device incorporating one or more
606 neutron mirrors at the front end of the instrument's neutron optical system, inclined so as to reflect in cold
607 neutrons from a source to the side of the guide axis. The device acts as a switch because the reflectivity
608 of neutron mirrors is intrinsically wavelength-dependent, so that short wavelengths are transmitted while
609 longer wavelengths are reflected. Without needing to move, it thus switches as a function of wavelength
610 from allowing short-wavelength neutrons to be transmitted until the reflectivity cut-off is reached, above
611 which longer-wavelength neutrons are reflected into the guide from the side. Together with the choice of
612 the rather low repetition rate of the ESS, a decision was made early on in the project that all beamports
613 should be able to benefit from the resultant large bandwidth by using bispectral switches. This has far-
614 reaching implications on the design of the facility. Because every beamport can now be populated with
615 a cold, bispectral, or purely thermal instrument, every beamport becomes essentially equivalent, and an
616 instruments choice of beamport is no longer based on its spectral needs, as is done at existing facilities

617 but on other factors, such as the size of the experimental hall behind that beamport, the space allowed by
618 components such as choppers on the neighbouring instruments, or proximity to labs and other important
619 infrastructure.

620 Currently existing pulsed spallation sources hardwire the spectral characteristics of each beamport into
621 the monolith design by orienting the beamport axis to point at one moderator or another. Adding this new
622 requirement of spectral freedom to all beamports requires a very different approach. Each beamport now
623 needs to be able to view both a cold and a thermal neutron source, which should be placed side by side with
624 the beamport axis oriented at their junction. In this way, the instrument can choose to shift and/or tilt its
625 beam axis with respect to the beamport axis within the envelope given by the beamport insert, so that it
626 points at the cold or thermal moderator. The design of the beamport inserts shown in Figure 7, typically
627 allows the beam to be tilted by about 1° to one side or the other, with respect to the beamport axis.

628 For the TDR moderator, this works fine. All beamports in one 60° opening should be oriented to point
629 at the junction between the cold and thermal moderators, and the instruments can choose cold, bispectral
630 or thermal beams by tilting one way or the other.

631 For the pancake moderator, there are two options for achieving this spectral freedom. Each beamport
632 can either be oriented so as to point at the cold-thermal junction nearest to its entrance window or the cold-
633 thermal junction on the other side of the cold moderator. These are known as *near-corner* and *far-corner*
634 extraction, respectively and are illustrated in Figure 25.

635 Near-corner extraction works well for beamlines near the perpendicular to the proton beam, but results
636 in very low thermal brightness at angles close to the edges of the fan, as the beamport angle approaches
637 the parallel to the thermal-moderator face (see Section 5.1). This is consistent with the known angular
638 dependence of neutron emission from the thermal moderators [26]. Far-corner extraction works acceptably well
639 for all beamports, but generally results in lower cold brightness, as the viewing angle of the cold moderator
640 for most beamports results in a reduced depth of parahydrogen being seen. The other problem with the
641 far-corner extraction is that it results in fewer beamports overall, as the beamports near the perpendicular
642 to the proton beam would otherwise clash [13].

643 The butterfly geometry solves this problem by orienting all beamports towards the nearest cold-thermal
644 junction. For each instrument sector (North, West, South, East), this junction acts as the *focal point* for
645 the beamports, as indicated by the red spots in Figure 25. All beamports can view either the adjacent cold
646 lobe or the thermal moderator on the other side of the focal point, as indicated by the arrows in Figure 26.
647 The butterfly-1 geometry has an advantage over the butterfly-2 geometry for thermal beam extraction, as
648 the central, most intense part of the thermal moderator near the inside of the V-shape is closer to the focal
649 point, making it more readily viewable from most beamports.

4.5. Upgradeability

All three of the studied low-dimensional moderator concepts incorporate a high degree of upgradeability, as two upgradeability aspects were included as design criteria from the outset: firstly the beam extraction geometry has been designed to allow the extraction of many more beamports than needed for the 22 instruments foreseen in the day-one configuration of the ESS. The primary upgrade path of the ESS is to add more instruments to the initial target station, rather than needing to build a second target station, when the 22 instrument slots have been filled, as is the strategy at existing pulsed spallation sources. This is a far more cost-effective upgrade path, capitalizing on the high performance of the existing accelerator and target station, without the large added expense of a second target station and the dilution in proton beam power associated with the need to supply beam to two target stations with the same accelerator. In order to facilitate such an upgrade, the angular separation of the beamports at ESS has been set to about half that of existing pulsed spallation sources, resulting in up to 42 possible beamports, see Figure 7.

Secondly, the design requirement that all beamports can freely choose between viewing the cold and thermal moderators provides a significant additional freedom of choice when placing future instruments. In addition, contrary to current pulsed spallation sources which use a combination of coupled, decoupled and poisoned moderators to provide the range of pulse-width characteristics needed by the instrument suite, the ESS as a long-pulse source, provides a much greater range of pulse widths by tailoring the source pulse on an instrument-by-instrument basis using pulse-shaping choppers on all the beamlines which need them. This range is available to all instruments, both for day-one instruments, and for instruments which are part of a future upgrade. Finally, by allowing all the instruments to be served by the same moderator assembly above the target, the space for moderators below the target is kept free to be used for future developments. Some ideas are briefly discussed in the conclusion section, as well as in Ref. [13].

One aspect of the target station design which does impose limitations on future moderator designs is the location of the four focal points. The focal points are intended to be fixed for the lifetime of the facility, as the beamport inserts are integrated into the whole target-monolith system. The height of the beamport inserts is set so as to allow a neutron beam to be extracted from either the top or the bottom moderator, or even both. The horizontal coordinates of the focal points thus apply equally to both the top and bottom moderators and are fixed for the lifetime of the facility.

4.6. Iterative procedure for moderator optimization

The considerations outlined above for optimal beam extraction need to be incorporated into the design of the moderators. At ESS, this was approached in an iterative fashion. The requirement on the viewed surface at the moderator, for the ESS beam extraction configuration, was that a width of at least 6 cm was needed, for both thermal and cold extraction surfaces [13]. Such a width should be seen from each of the beamports, and was therefore treated as a requirement for the moderator design.

Figure 12. Calculated brightness B_{0-20} map on the emission surface of cylindrical moderators of different heights: 1.5 cm (top), 3 cm (center), and 10 cm (bottom).

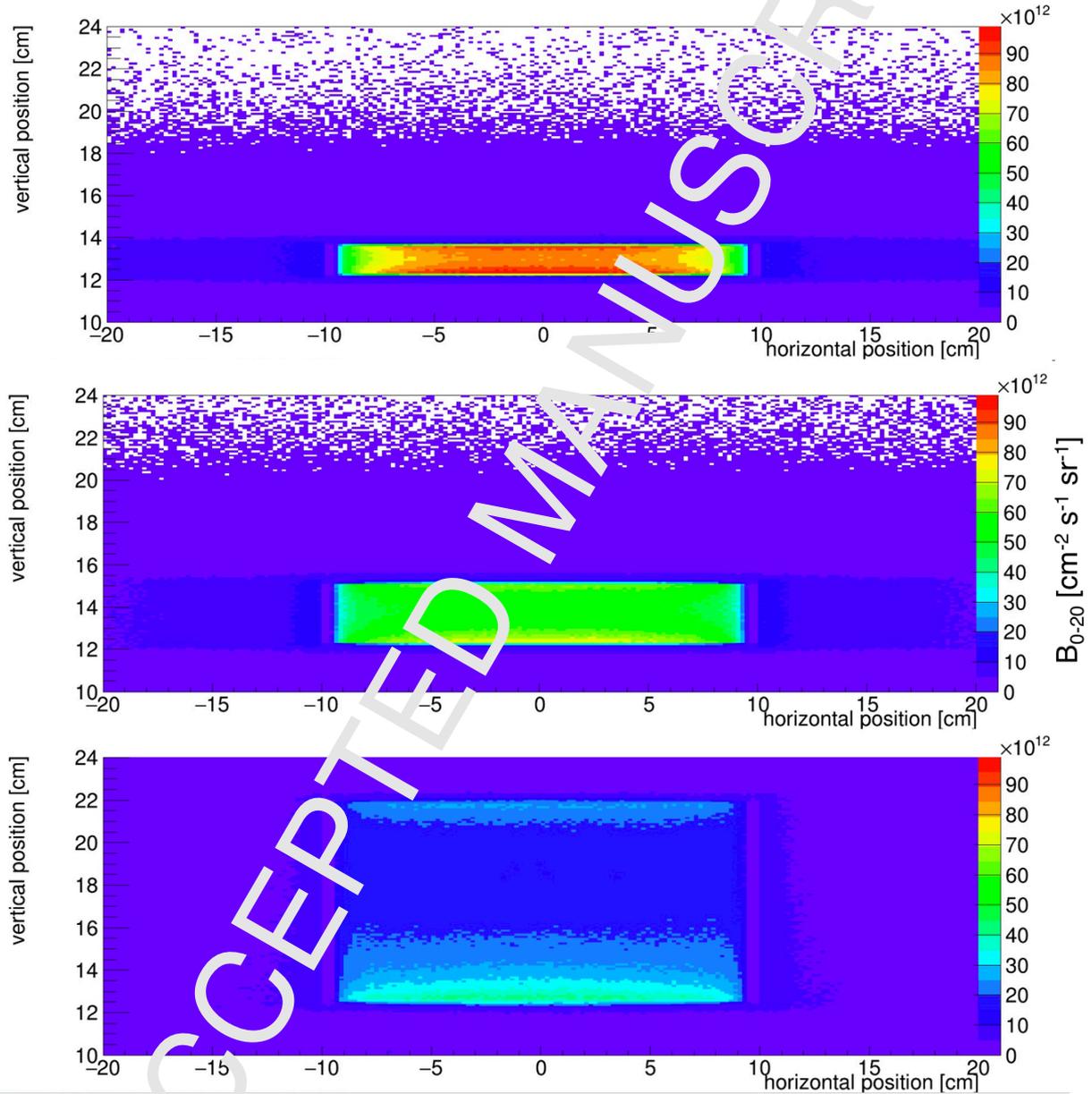
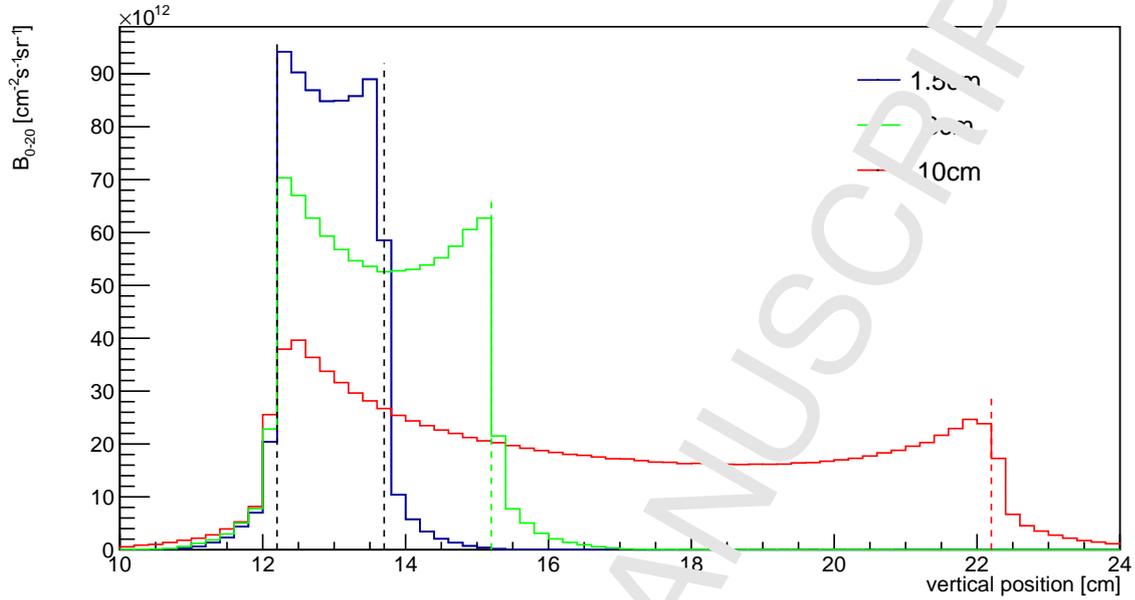
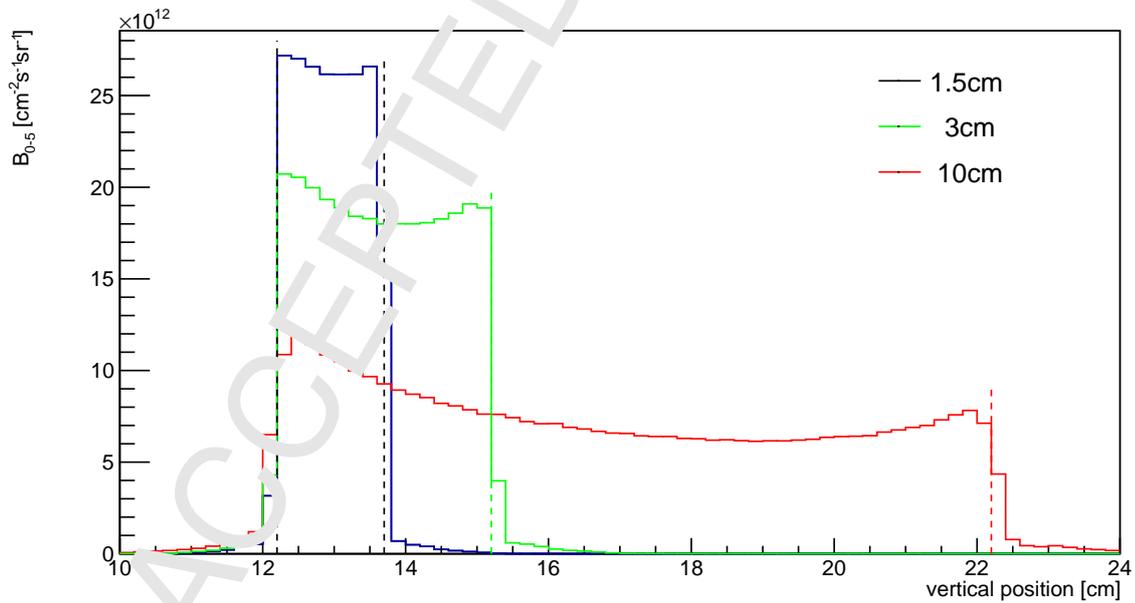


Figure 13. Same as Figure 11 for B_{0-20} .Figure 14. Same as Figure 11 for B_{0-5} .

Each moderator design as it was proposed to the instruments was evaluated for performance impact on each instrument, and the result was fed back to the moderator design team. At each iteration, the strengths and weaknesses of each particular moderator design for instrument performance were highlighted, allowing an informed adaptation of the design to the instrument needs. This allowed the optimal moderator height to be calculated, so as to maximize the global performance of the instrument suite. The issues related to beam extraction were also evaluated at each iteration, culminating in the butterfly moderator geometry which takes all the relevant performance parameters into account.

According to these criteria, the chosen moderator height was 3 cm for both thermal and cold moderators.

5. Moderator Design Choice

5.1. Relative performance of the different concepts

In this section we compare the performance of the three concepts considered for low-dimensional moderators. The brightness was calculated from a viewed surface of the moderator 6 cm wide, 3 cm high. This was done for both thermal and cold moderators and the requirements in the calculations were that each viewed surface would be at a distance of at most 1 cm from the focal point.

For the pancake, the dimensions of the cold hydrogen disk that gave the highest cold brightness was chosen, for both near and far corner extraction.

For the butterfly-1 and butterfly-2 moderators, the total length of the moderator system (along the proton beam axis), after optimization, is of 24 cm and 28 cm, respectively. For the pancake, the optimal diameter of the cold moderator disk is 20 cm, for both near- and far-corner extraction. The overall pancake moderator is, however, wider than both butterfly-1 and butterfly-2, as the 6 cm wide thermal extraction areas must be considered, on both sides of the cold moderator, making the full pancake moderator system about 32 cm wide.

The Monte Carlo models do not have full engineering details, as they were not available at the time of performing the optimization study. However, in an attempt to estimate absolute values of the brightness expected, several details are included such as pipes, correct material thicknesses, and gaps, while some materials are mixtures in order to take into account water loops for cooling, or flow guides in hydrogen or water moderators.

The three low-dimensional designs (one pancake and two butterflies) had exactly the same level of engineering details, allowing a proper comparison of the different concepts. The target, reflector, and all the surrounding of the moderators were identical, and the only difference between the models were the thermal and cold moderators inserted. The flow channels inside the moderators were not modelled, instead the material inside was a mixture of parahydrogen with 5% of aluminum to take into account the reduction in performance due to the presence of aluminum flow guides inside the moderator vessel.

717 In the case of the TDR volume moderator, in order to perform as fair a comparison as possible to the
718 other models, we took the model used for the TDR work, and added some engineering details (e.g. same
719 structure and amount of cooling water in the reflector) to make it similar, from the engineering point of
720 view, to the latest low-dimensional models. We also considered the same type of beam extraction, i.e.,
721 within 7 cm from the focal points, placed at the intersection between thermal and cold sources, as for the
722 latest models.

723 Despite the addition of engineering details, this updated TDR model is probably still favored with respect
724 to the other concepts. Since the publication of the TDR, the spallation target has been redesigned in favour
725 increasing the volume for the flow of the helium coolant, and the moderators have been moved further away
726 from the target to increase the safety margins. These changes result in a reduced neutronic performance
727 close to 10 %. They have not been incorporated in the updated TDR model presented here.

728 Figure 27 shows the resulting brightness angular distributions within one 120° sector of ESS for the low-
729 dimensional moderators considered. Due to symmetry, the results are identical in the other sector. Integral
730 thermal B_{20-100} and cold B_{0-20} brightnesses are shown for the pancake geometry (with near-corner and
731 far-corner extraction) and for the two butterfly configurations.

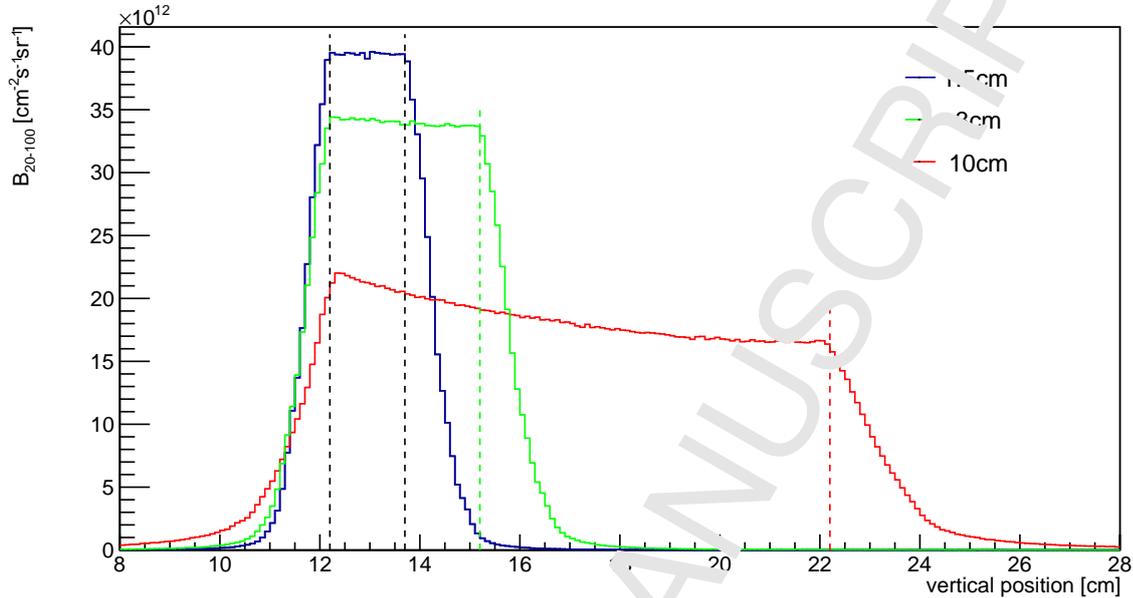
732 Table 2 lists the average integrated thermal and cold brightness for the designs considered. From Table 2,
733 it is apparent that all the low-dimensional models have a much higher brightness than the TDR, thus
734 justifying the transition from TDR to low-dimensional moderators.

735 Of the two beam extraction concepts for the pancake geometry, the far-corner option is preferable, as it
736 offers a larger gain in thermal brightness, though it results in the loss of a number of beamports. Reduction
737 of each pair of beamports can be seen as a loss of available neutrons to the facility, considered as whole, of
738 about 5%. The near-corner extraction option for the pancake provides a higher cold brightness and does not
739 result in a reduction in the number of beamports. The thermal brightness, however, falls to unacceptably
740 low levels for the edge beamports.

741 The two butterfly concepts were designed with the goal of increasing the thermal brightness, maintaining
742 (or increasing) the high cold brightness, and easing the beam extraction. Of the two concepts, the most
743 successful is the butterfly 1, because; *i*) it has the highest cold brightness of all concepts. More than two
744 thirds of the instruments of ESS are cold or bispectral, therefore in the overall figure of merit to choose the
745 best concept, cold brightness must have the priority. *ii*) It has the second best thermal brightness, after the
746 butterfly 2, which however has a significantly lower cold brightness.

747 Compared to the pancake with far-corner extraction, the butterfly 1 gives both higher thermal and cold
748 brightness (factor 1.13 and 1.12, respectively), without the problem of the loss of beamports. The real gain
749 is however higher, considering the higher number of beamports available for the butterfly 1 concept, as
750 discussed. Compared to the pancake with near-corner extraction, it gives a slightly higher cold brightness,
751 and an average thermal brightness higher by a factor of 1.47.

Figure 15. B_{20-100} distribution across the moderator height, for thermal neutrons. Neutrons are extracted from the water-filled sides of three moderators of cylindrical geometry, with 1.5 cm, 3 cm and 10 cm height.



6. Description and performance of the butterfly 1 moderator

The first moderator that will be installed at ESS at the start of the facility will be a butterfly 2 moderator, which was initially chosen mainly because of its higher thermal brightness. At the time of writing, a detailed engineering design has been finished and the moderator is in fabrication for installation in 2021. For a final configuration of the top moderator we decided to adopt a butterfly 1 design, for the reasons outlined in Section 5. The instruments and their beam extraction systems are designed for that moderator. The butterfly 1 system will be installed in the early years of ESS during the power ramp-up. That is why detailed engineering models are not yet available for the butterfly 1 system.

In this section we give a full description of the butterfly-1 moderator chosen for ESS. The geometry of the butterfly moderator is shown in Figure 25. Engineering details have been extrapolated from the existing engineering model of the butterfly 2 [27].

The MCNPX model of the structures surrounding the moderator is shown in Figures 28 to 30. Some important details of the model are the following:

- The tungsten target was modelled according to the engineering drawings. The density of the tungsten used in the model is of 15.1 g/cm^3 , corresponding to the effective density deduced from the engineering design, which consists of tungsten bricks with cooling gaps, for a filling factor of tungsten of 78%. The

Figure 16. Angular distribution of propagation direction with respect to the horizontal plane of cold neutrons ($E < 20$ meV) emitted from the surface of the parahydrogen moderator.

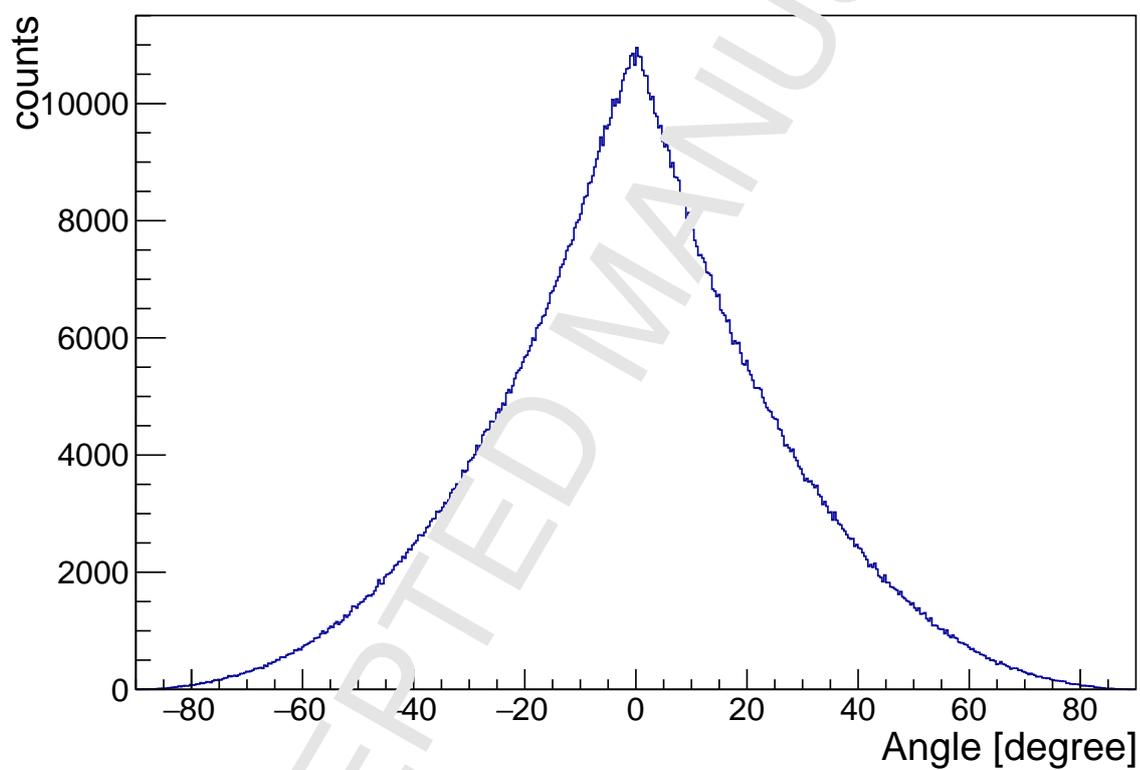
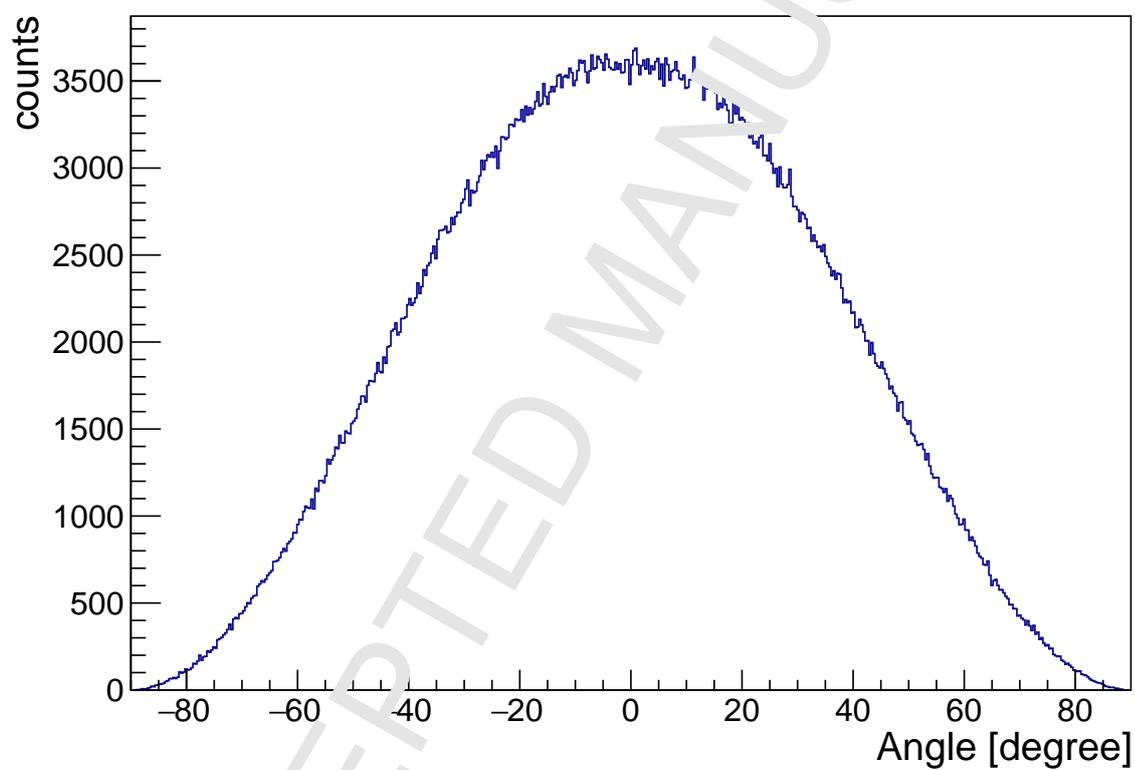


Figure 17. Angular distribution of the propagation direction with respect to the horizontal plane of thermal neutrons ($20 \text{ meV} < E < 100 \text{ meV}$) emitted from the surface of the water moderator.



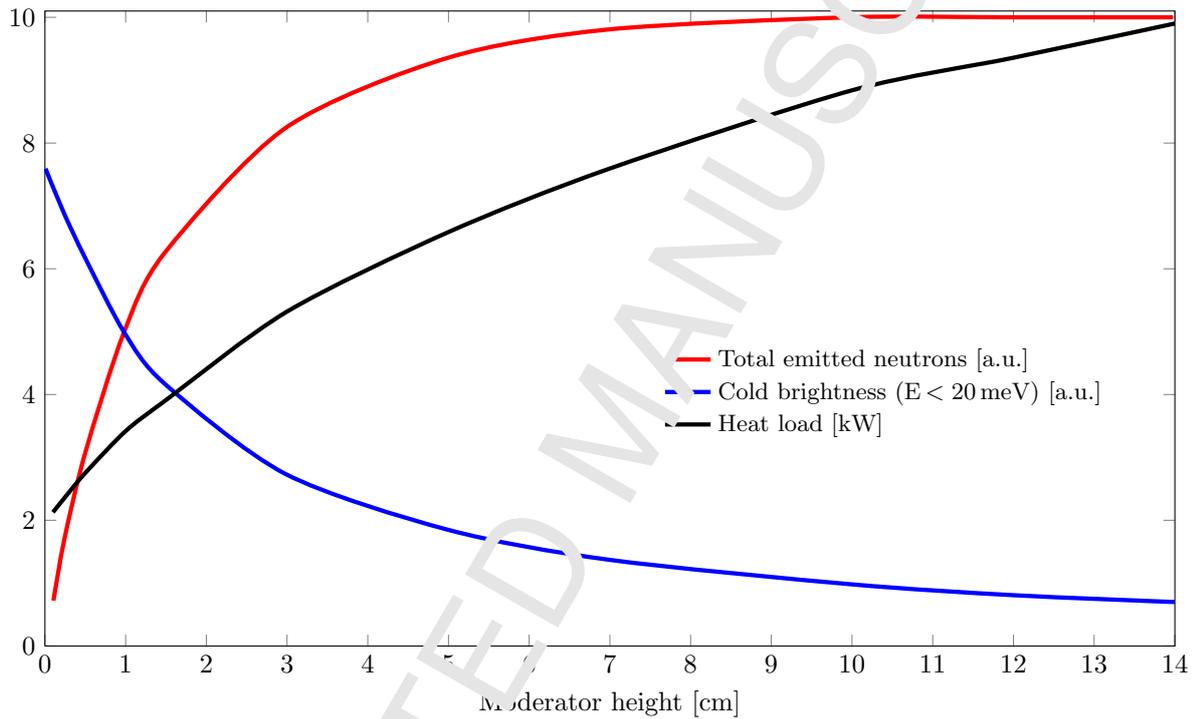
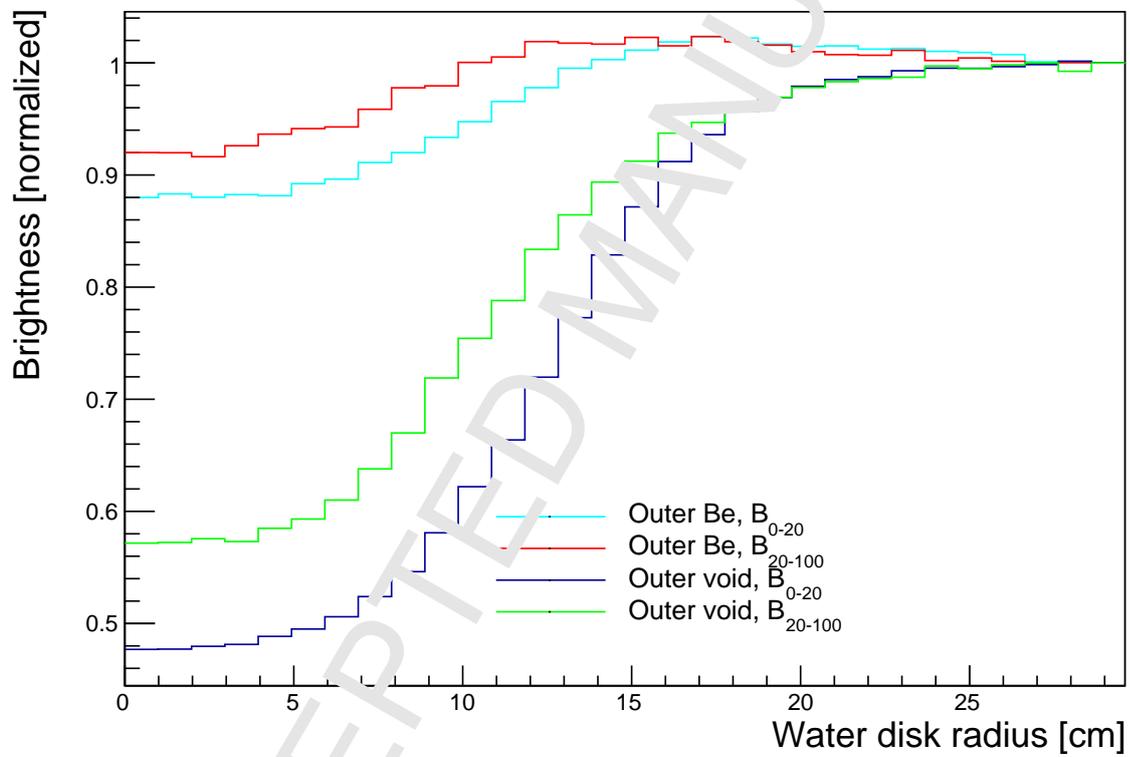


Figure 18. The integral cold brightness \mathcal{B}_{0-20} increases with decreasing height of the moderator. On the other hand, the total number of emitted cold neutrons (\mathcal{N}_{0-20} multiplied by the viewed area of the emitting surface) and the heat load both increase with the moderator height. The heat load is calculated on the cylindrical aluminum vessel and on the pure parahydrogen inside, without piping or other engineering details.

Figure 19. Relative change in thermal and cold brightness as a function of the pre-moderator radius, for two configurations, in which the ring outside the premoderator (with inner radius equal to the premoderator radius, and outer radius of 60 cm) is void, or beryllium with 30 vol% water.



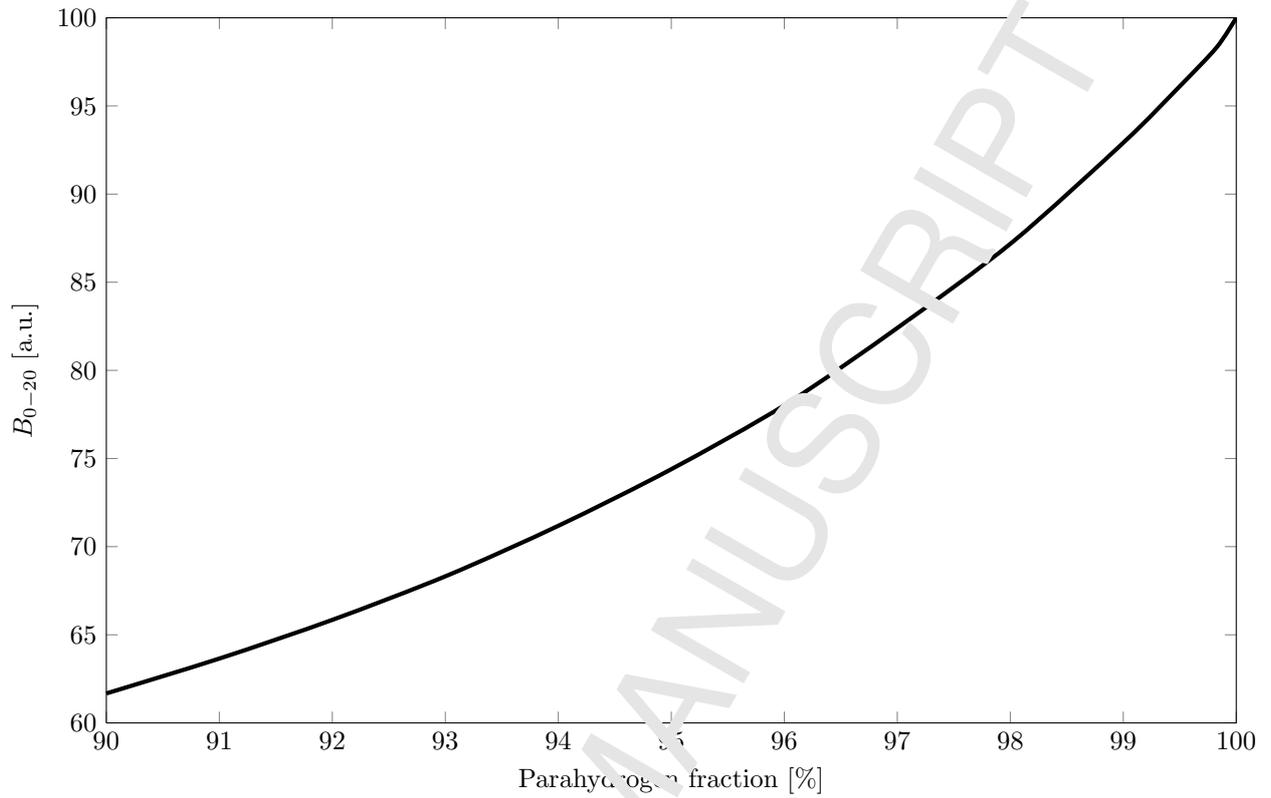


Figure 20. Brightness B_{0-20} relative variation, for the 3-cm high cold moderator, as a function of the parahydrogen fraction, calculated using the ENDF-B/VII cross section at 20 MeV.

Figure 21. Map of high-energy ($E > 0.1$ MeV) neutrons crossing a horizontal plane located between the tungsten target and the premoderator, at $Z=8$ cm. The shape of the butterfly (left) and pancake (right) moderators are superimposed. (The proton beam direction in the figure is upward.)

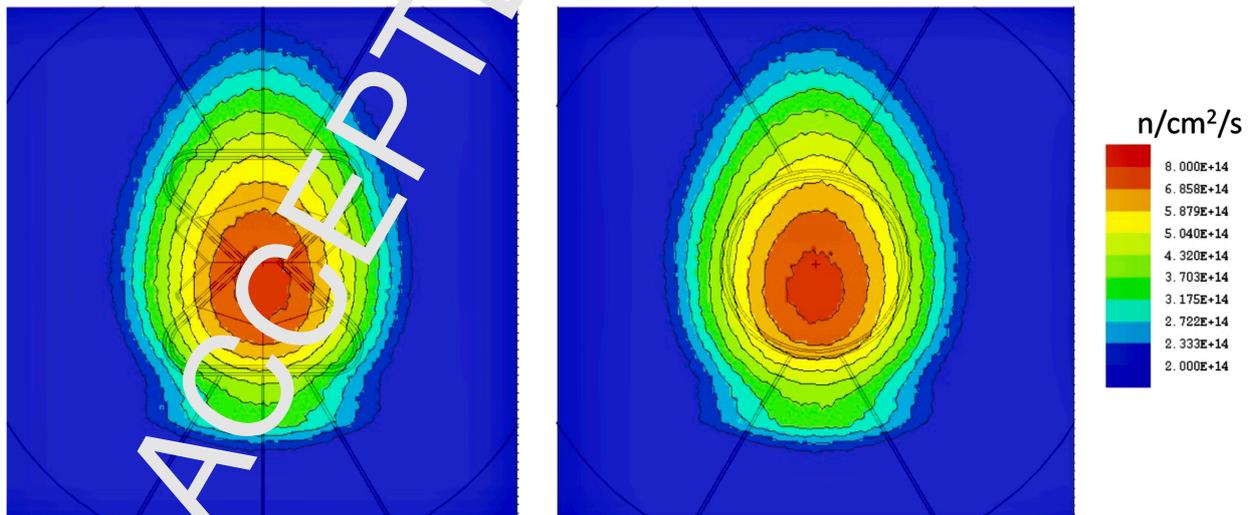


Figure 22. The fast neutron emission distribution for the 1.5, 3 and 10 cm tall pancake moderators. The results have been obtained by a point detector tally (f5) with the emission position (horizontal axis, 0=center of target) calculated by extrapolating the trajectories back to the center of the moderator. Neutrons shown as starting outside the window defined by the moderator edges (dashed vertical lines) traverse through the structure around the moderator that is aligned to the physical edges of the moderator volume.

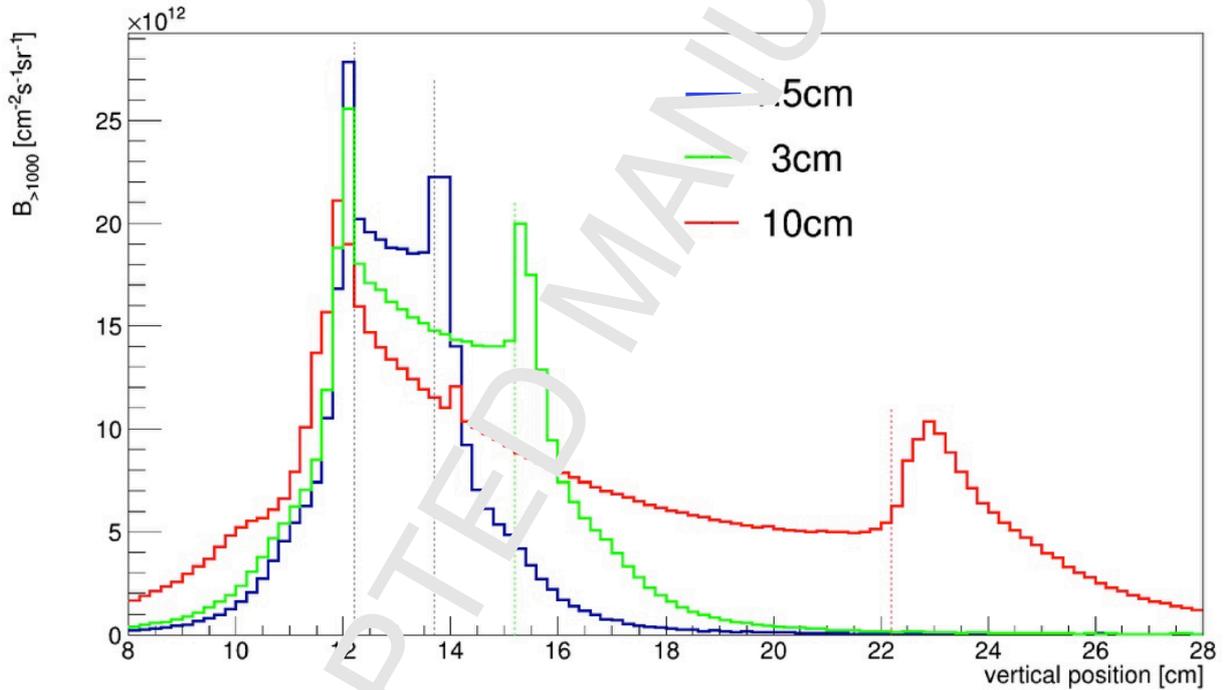
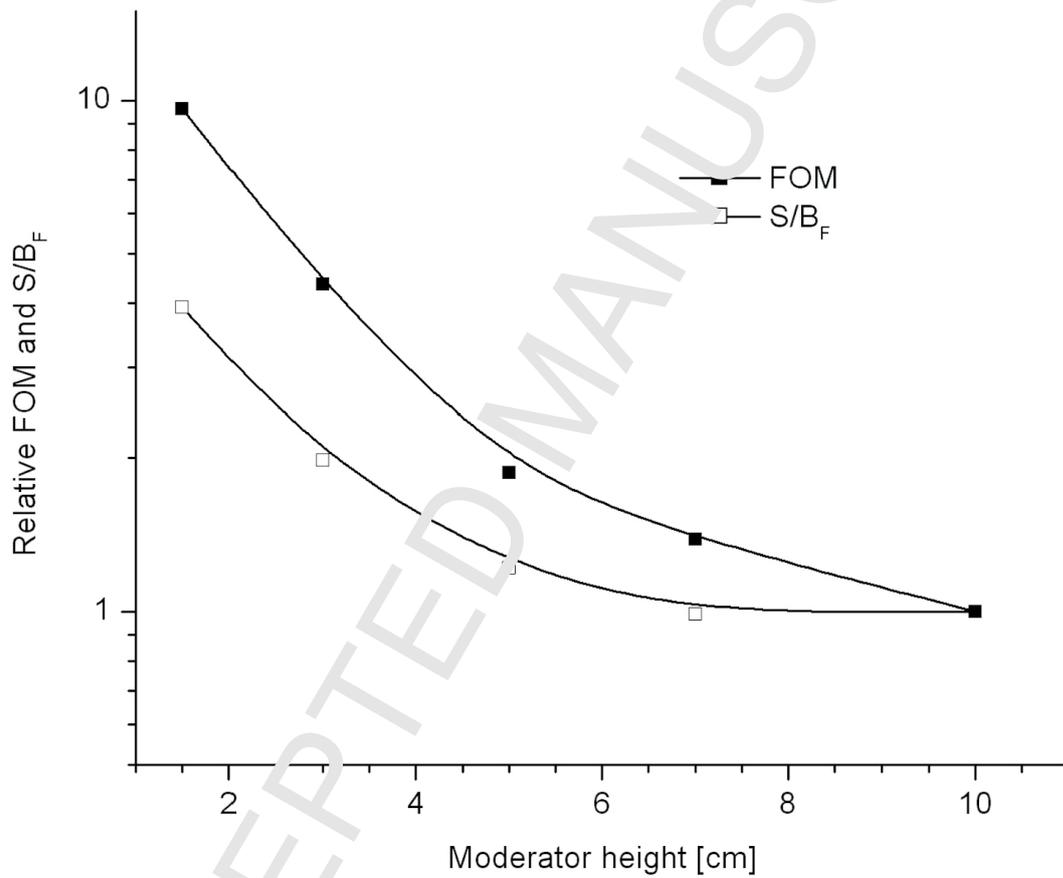


Figure 23. Evolution of the relative signal to fast neutron background ratio (S/I_F) and the data collection figure of merit (FOM) as a function of moderator height. For definitions see the text in Section 2.



768 final brightness was calculated using a model with the individual bricks, and it was verified that it
769 gives the same brightness as the homogenized model. The SS316L container of the bricks was modelled
770 in detail according to the engineering drawings.

- 771 - The water premoderator between target and moderator consists of an aluminum vessel, containing a
772 mixture of water and aluminum, with a volume fraction of Al of 8 vol% to account for water flow
773 channels, deduced from the engineering drawings of the water premoderator currently in construction.
- 774 - Similarly, parahydrogen in the cold moderator contains 5 vol% of aluminum, corresponding to the ex-
775 pected volume fraction occupied by the flow channels. The final model however contains a preliminary
776 design of the flow channels [28]. The shape and thickness of the aluminum vessel is modelled according
777 to the engineering drawings.
- 778 - Thicknesses of aluminum walls of the cold and thermal moderators, and of the beryllium reflector are
779 in agreement with the engineering drawings. Similarly, the beryllium reflector is modelled according
780 to the present status of the engineering design, with the expected amount of light water cooling.
- 781 - The outer reflector is made of SS316L with 10 vol% of water cooling.
- 782 - Two hydrogen pipes, inlet and outlet, are assumed for the cold moderator, see Figures 25 28 and 30

783 The results provided are with a fast neutron reflector placed at the bottom of the target. For the first
784 moderator-reflector plug, with a butterfly 2 moderator at the top, a steel plug is designed for the bottom,
785 which gives a 4 % brightness increase with respect to having a two-moderator configuration. The result
786 presented here are for a reflector providing a 9 % brightness increase which could be achieved by a water-
787 cooled beryllium or copper reflector, while a better performance could be obtained using other options, such
788 as helium cooled tungsten (cf. Table 1).

789 6.1. Focal points

790 The focal points are different for the four instrument sectors. The focal points are (for the North sector)
791 $X=5.4$ cm, $Y=8.9$ cm, $Z=-3.7$ cm. For the other sectors, the absolute values of the X and Y coordinates
792 are unchanged, but the sign change according to the sector (see Figure 25).

793 6.2. Horizontal viewed width

794 Figure 31 shows the projected widths at the moderator surface, for thermal and cold moderators, for
795 the different beam ports. In general there is a good balance between maximum widths of thermal and cold
796 moderators, as required for effective beam extraction.

797 6.3. Horizontal brightness distributions at moderator

798 In Section 2 the brightness distribution along the height of the 3-cm pancake moderator was shown for
799 several integrated brightnesses. The shapes of these distributions depend mainly on the moderator height
800 and therefore the vertical distributions for the butterfly moderators are similar (while the absolute values
801 depend on the performance of the moderator).

802 Horizontal distributions of the brightness at the moderator surface were also calculated. This work
803 was part of a detailed characterization of the moderator brightness, being used in the ray-tracing code
804 McStas [29], for guide and instrument design.

805 The geometry and brightness data presented here have been implemented in the most recent version
806 of the McStas ESS source component, released as an updated component library for McStas 2.3. The
807 implementation is based on functional fits to the underlying MCNP data. This approach ensures that the
808 simulations run efficiently, but comes with some simplifications and assumptions, which means that the
809 results are only valid to within about 10%. Users which are willing to accept a CPU performance penalty,
810 can instead make use of the MCPL implementation [30], where MCNP neutrons are individually handed to
811 McStas with no loss of accuracy in the transition between codes.

812 Horizontal distributions were calculated with MCNP2, using collimators placed at 3 m distance from the
813 moderator, looking at a surface 2 mm wide, 30 mm high, moving the collimator to obtain a distribution
814 across the thermal and cold moderators. Results are shown in Figures 32 and 33.

815 The brightness distribution across the viewed surface shows variations for different beamports. For
816 example, for the W1/E1 beamports, the cold brightness is low for about two cm from the focal point, then it
817 reaches a plateau about 5 cm wide. This is due to the lower amount of hydrogen viewed at this particular
818 angle, for that 2-cm window (cfr. Figure 32). Figure 33 corresponds to a beamport at 42° with respect to
819 the proton beam axis, which is very close to the 45° angle of of the cold moderator vessel walls adjacent
820 to the thermal moderator. Therefore this beamport sees for a few cm of the extraction window the cold
821 vessel in its entire length across that diagonal, resulting, for about half of the viewed surface, in a brightness
822 about 25 % higher than for the other half; if neutrons are extracted from that 3 cm window only, the cold
823 brightness would be about 15 % higher than from a 6 cm wide window.

824 Thus, for the cold moderator, a significant gain of 10-15 % is observed for 16 out of the 42 beamports.
825 Such effects are not possible for the pancake, nor for the butterfly-2, and if exploited by careful guide optics
826 design it can yield an additional cold brightness increase for several beamports.

827 6.4. Brightness results

828 In Figure 34 the distribution of B_{0-20} and B_{20-100} for the 42 ESS beamports is shown. For 16 beamports
829 we observe a significant increase of the cold brightness. These are the beamports where the quasi-tube

Figure 24. The TDR configuration. *Left:* Vertical cut showing top and bottom moderators. *Right:* Horizontal cut showing top cold moderator and water extensions for bispectral neutron beam extraction.

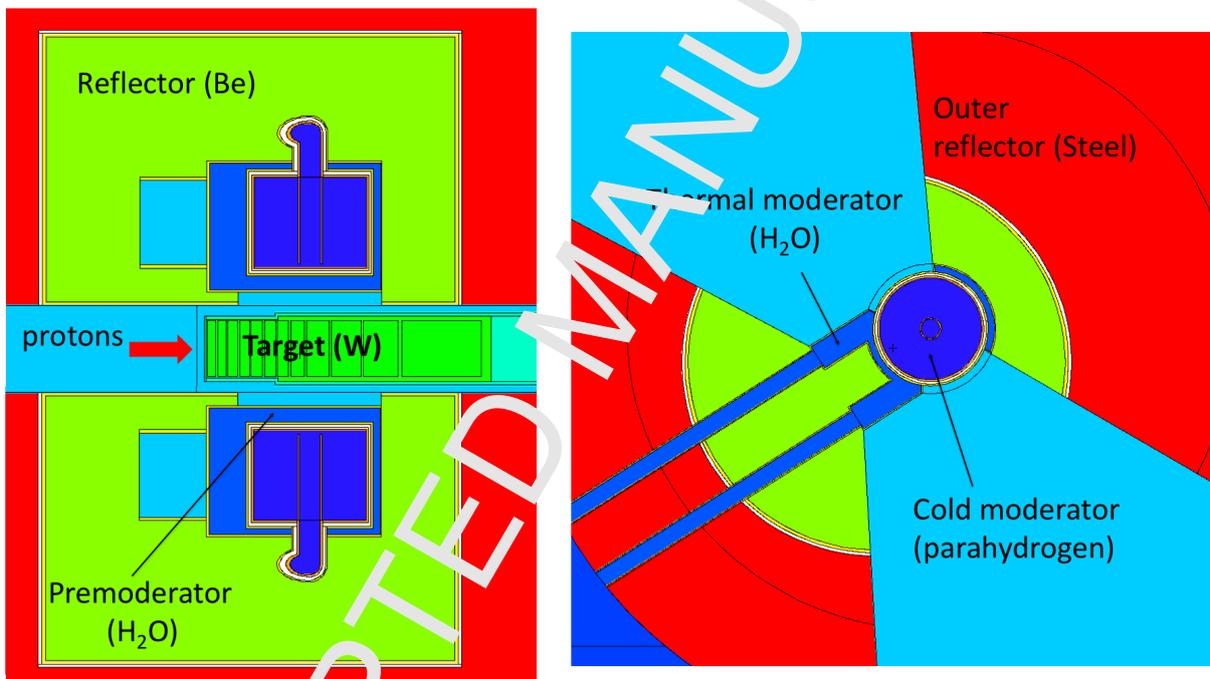


Figure 25. MCNPX models of the two butterfly designs. *Top*: butterfly 1 design, with a single cold moderator vessel and light water moderators, all placed above the neutron production hot spot. *Bottom*: butterfly 2 design, where the cold moderator is split in two parts, and the water moderator occupies a major part of the hot spot. The focal points, the origin of the beamport inserts, are indicated for both designs with red dots.

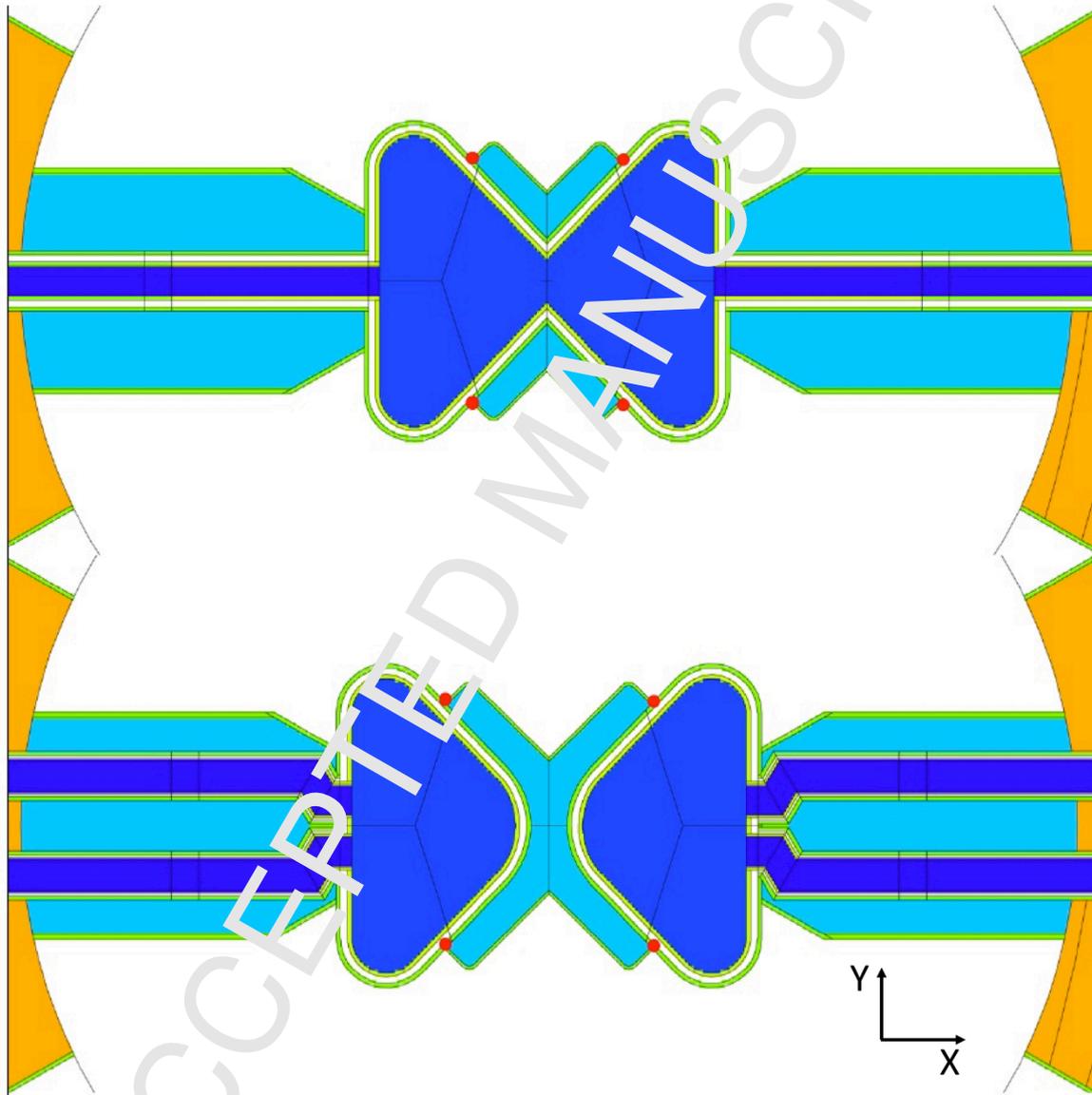


Figure 26. Schematic view of the different beam extraction configurations for thermal (red arrows) and cold (blue arrows) neutrons for the pancake and butterfly moderator. For the pancake, near-corner extraction (top left) and far corner extraction (top right) are possible. For both butterfly concepts, near corner extraction is used (bottom left and right). The red dots show the beamline focal points.

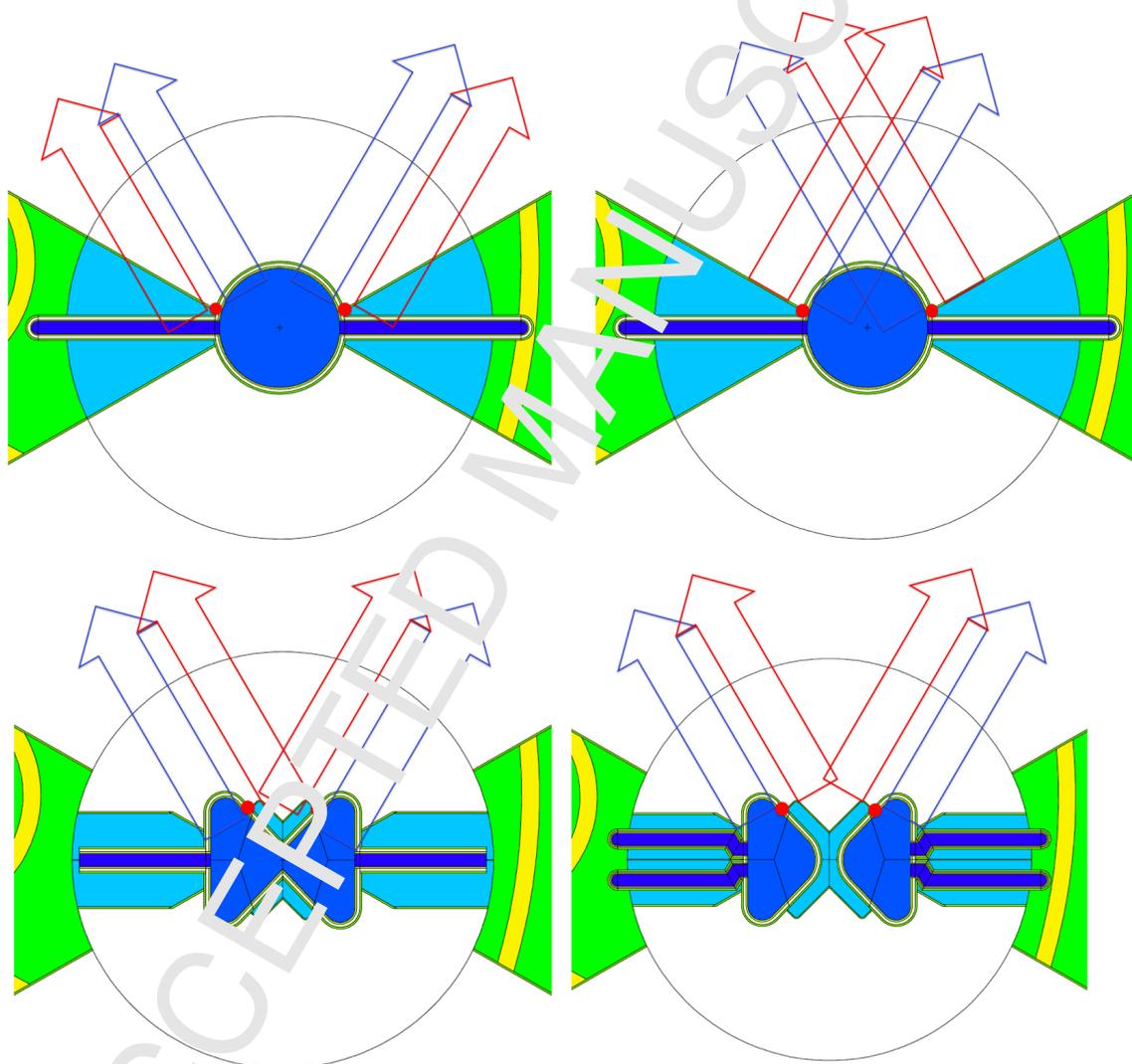


Figure 27. Time-average integrated thermal and cold brightness for the beamports in the South and East sectors. Thermal brightness B_{20-100} integrated between 20 meV and 100 meV. Cold brightness B_{0-20} integrated between 0 and 20 meV. The horizontal viewed width at the moderators is 6 cm.

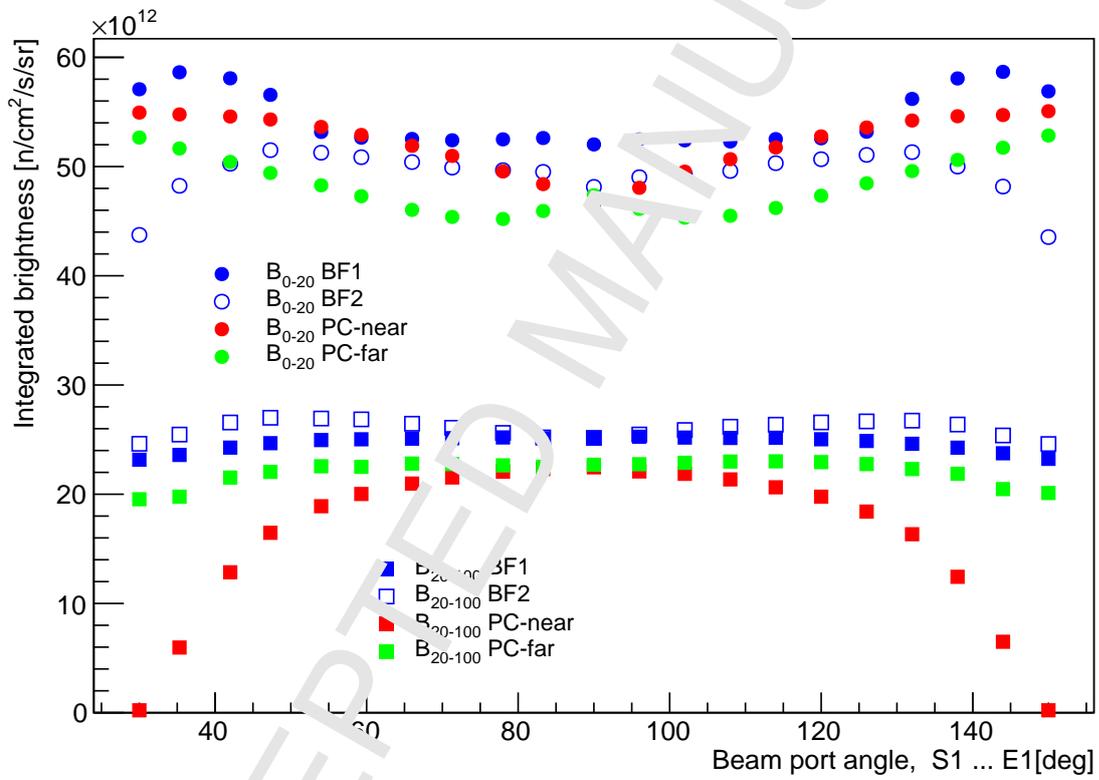


Figure 28. MCNPX geometry used for the brightness calculations of the butterfly 1 model. For side view. Proton beam comes from the left impinging on the tungsten target. The spallation target contains tungsten bricks (green) nominal density of 19.3 g/cm^3 , except for the last two rows which contain stainless steel bricks. However some calculations were performed using a single cell with density of 15.1 g/cm^3 to account for the fraction of helium in the target according to which the filling factor of tungsten is 78 vol%. The water premoderator (light green) between target and moderator has a 8% volume fraction of Al, to account for flow channels, not modelled. The beryllium reflector (light blue) includes water channels (light green) according to engineering drawings. The outer reflector (orange) is made of stainless steel, with 10% volume fraction of water, for cooling.

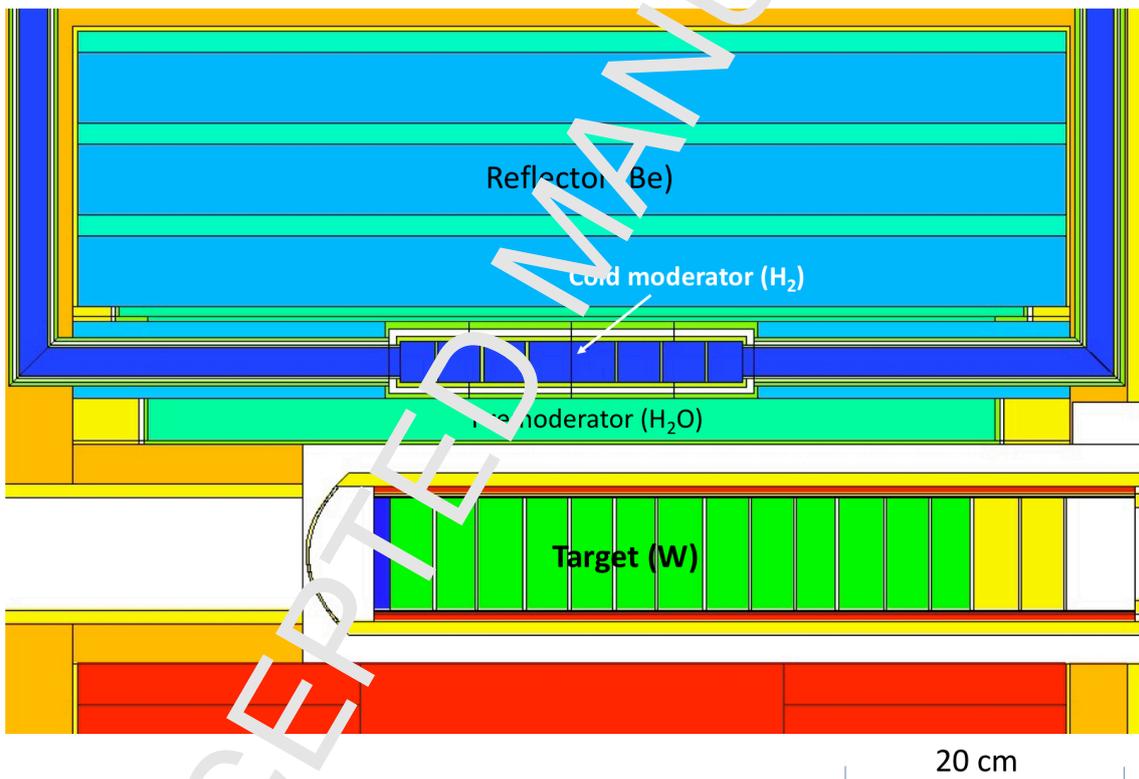


Figure 29. MCNPX geometry used for the brightness calculations of the butterfly moderator, side view showing beam extraction channels. The proton beam is entering the figure in correspondence to the central area of the target.



Figure 30. MCNPX model of the butterfly 1 moderator with modelled flow channels [28]



830 behaviour of the moderator is present. On the other hand, the thermal brightness does not show a strong
 831 dependence on the beamport location.

832 Figure 35 shows the thermal and cold peak spectral brightness, averaged over the 42 beamports. The
 833 shapes of the thermal and cold spectra are essentially the same for all the beamports, which justifies taking
 834 the average.

835 The distribution of the time averaged integrated brightness for the butterfly 1 moderator with all the
 836 available engineering details is shown in Figure 27.

837 When optimising the guide design for an individual instrument, a two-stage process is recommended.
 838 Firstly, the instrument's guide should be oriented within the beamport insert to point at the centre of the
 839 relevant source: for a cold instrument, that is the centre of the circle defined by the circular arc defining the
 840 nearest lobe of the hydrogen moderator. For a thermal or bispectral instrument that is the centre of the
 841 V-shape of the outside surface of the thermal moderator.

842 The exact orientation should then be refined using the McStas source component to maximise the in-
 843 strument performance. The effective brightness of the source will vary by up to about 15% depending on
 844 the width and angular acceptance of the guide system.

845 The performance of the ESS source can be compared with the official ILL brightness values from the

846 *Yellow Book* [4]. The original design goal of ESS was to achieve a cold peak brightness 30 times the average
847 ILL brightness [1]. As shown in Figure 36, with the present design using low-dimensional moderators, we
848 are far above this goal. The cold brightness of the butterfly 1 moderator is (at 4 Å) about 150 times higher
849 than the yellow book value. The thermal brightness at 1.5 Å is about 8 times higher than ILL¹. Similar
850 ratios are found for the integral values in the ranges considered in this work (cf. Table 2).

851 The brightness results of Figures 35 and 34, and the numbers in this Section refer to the presented design
852 of the moderator-reflector system. The engineering design is ongoing and changes to the final design will
853 affect the moderator performance. The results are given assuming the presence of a fast neutron reflector
854 below the target giving an increase of 9 % in neutronic performance of the top moderator, compared to
855 having a second moderator assembly below the target (see Table 1). A lower performing reflector, or the
856 presence of a bottom moderator similar to the top one (i.e. with a water premoderator) would reduce the
857 brightness by some %. It will be a strategic decision to be taken at a later stage, whether to focus on
858 the top moderator or to consider different sources at the bottom moderator, which will depend on several
859 factors, including the proposal of novel source concepts. As priority will be given for many years to a high
860 performing top moderator, it will be worth considering an optimized fast neutron reflector which would give
861 a further increase in performance of the top moderator.

862 6.5. Absolute uncertainty

863 A question arose during the design phase, of a possible higher impact of the engineering reality on the
864 neutronic performance of the low-dimensional moderator, with respect to a volume moderator, that would
865 decrease the brightness gain in a real situation. This was studied in detail, also because before deciding on a
866 single butterfly-1 moderator, detailed engineering for a configuration of two butterfly-2 moderators, one 3 cm
867 high, the other 6 cm high, was performed. This allowed to monitor the impact on the brightness of the two
868 moderators, when engineering details were progressively added to the model. It was found that the relative
869 performance of two moderators with significantly different heights (3 cm and 6 cm) does not change in the
870 transition from physics moderator models with added engineering details. This result is consistent with the
871 values from Table 2 that compare the updated TDR model to the low-dimensional moderator engineering
872 models.

873 Although the full engineering design of the butterfly-1 has not yet been performed, an attempt to include
874 all the engineering details (and associated penalties in neutron production) was made in agreement with the

¹According to a recent unpublished compilation of experimental and computational data, the ILL brightness should be corrected, so that on average the thermal brightness is lower by about a factor of 2, and the cold brightness is on average higher, also by about a factor 2, with respect to the official data. However, in this work we stick to the comparison with the official yellow book values.

875 information available from the existing design. A preliminary design of the flow-channels was performed [28]
876 and used for the final brightness calculations.

877 To determine absolute uncertainties on the brightness values one must also consider the uncertainties
878 related to the Monte Carlo calculations. MCNPX calculations are based on spallation/evaporation models,
879 and on nuclear libraries (available mostly up to 150 MeV energy), which includes also the scattering kernels.
880 A detailed study of uncertainties related to these contributions was done during the work for the TDR
881 moderator [1]. On the basis of those results, and considering the more mature level of the present design,
882 we expect an absolute uncertainty of 15% on the brightness calculated from the model.

883 7. Summary and Conclusions

884 The design of the ESS moderators presented here is the result of an extensive work that considered all
885 the relevant aspects to maximize the flux at the sample at the instruments. This approach allowed the
886 selection of an optimal, bright source (the moderators), while ensuring that all the aspects related to beam
887 extraction configuration, bispectral extraction, and phase-space transport were taken into account.

888 The results from the research of the optimal moderator design for ESS has had a profound impact on
889 the configuration of the facility. The main results of this work are summarized below.

890 1) **Brightness increase by using low-dimensional moderators.** The flat moderators adopted for
891 ESS offer a clear brightness increase with respect to the original TDR design based on volume moderators:
892 the cold brightness increases by more than a factor of 2.5 with respect to the original design for ESS.

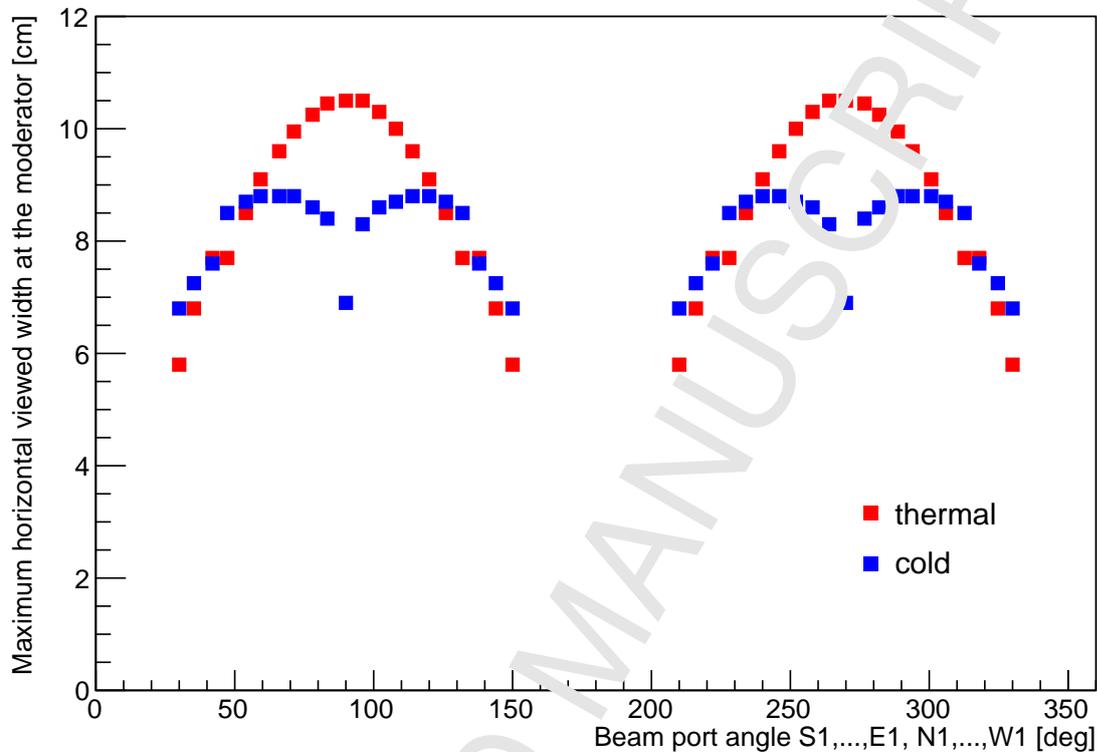
893 2) **Use of a single moderator system.** It was realized at an early stage that a single flat modera-
894 tor would be sufficient, as the difference in performance between a single low-dimensional moderator with
895 ($2 \times 120^\circ$) openings, and two low-dimensional moderators with ($2 \times 60^\circ$) openings each, would be negligible.
896 This finding opened the possibility, eventually adopted, of having an initial instrument suite viewing mod-
897 erators only above the target, with clear advantages in terms of performance, engineering, operation and
898 upgradeability.

899 3) **Moderator shape for optimal beam extraction.** The chosen butterfly moderator is the best
900 solution we could find to deliver high brightness to all instruments since it maximizes both thermal and cold
901 brightness for a large ($2 \times 120^\circ$) opening angle and improves the beam extraction.

902 4) **Upgrade possibilities.** The chosen configuration, where all initial instruments foreseen for ESS
903 point to the top moderator, leaves open several attractive possibilities for future use at ESS. Despite having
904 all the instruments in the initial suite viewing the top moderator, the beam extraction system of ESS is
905 designed so that all of the 42 beamports can view either the top or the bottom moderator, or even both.

906 With a high brightness moderator at the top, the bottom area could be reserved in future for a source
907 of neutrons which should be complementary to the top one. Several possibilities could be explored, such as:

Figure 31. Projected width at the thermal and cold moderator surface for the different beamports, for the butterfly 1 moderator. See explanation in the text.



- 908 - Very Cold Neutron (VCN) source. There is increasing interest in VCNs for neutron scattering and
 909 fundamental physics applications [22]. The production of neutrons with $\lambda > 20 \text{ \AA}$ requires different
 910 materials and temperatures than for cold neutrons. An interesting technique to increase the flux in
 911 this wavelength region might come by the use of diamond nanoparticle reflectors [31].
- 912 - High-intensity moderator, such as a large D_2 moderator, for specific experiments like the nbar beam-
 913 line [32, 33].
- 914 - A high-brightness moderator, even surpassing the brightness of the top moderator, which could be
 915 achieved either by using tube moderators (good for a few beam lines only, due to their strong direc-
 916 tionality), or by further reducing the height with respect to the top moderator. Tube moderators are
 917 discussed in Appendix B.

Figure 32. Brightness distribution along a horizontal X axis perpendicular to the beamport direction, shown for W1 and W11 beamports. Dashed lines pass through the focal points and the 0 of the X axis. At 90° (W11) the cold distributions from the two sides of the cold moderator have the same intensity, as expected.

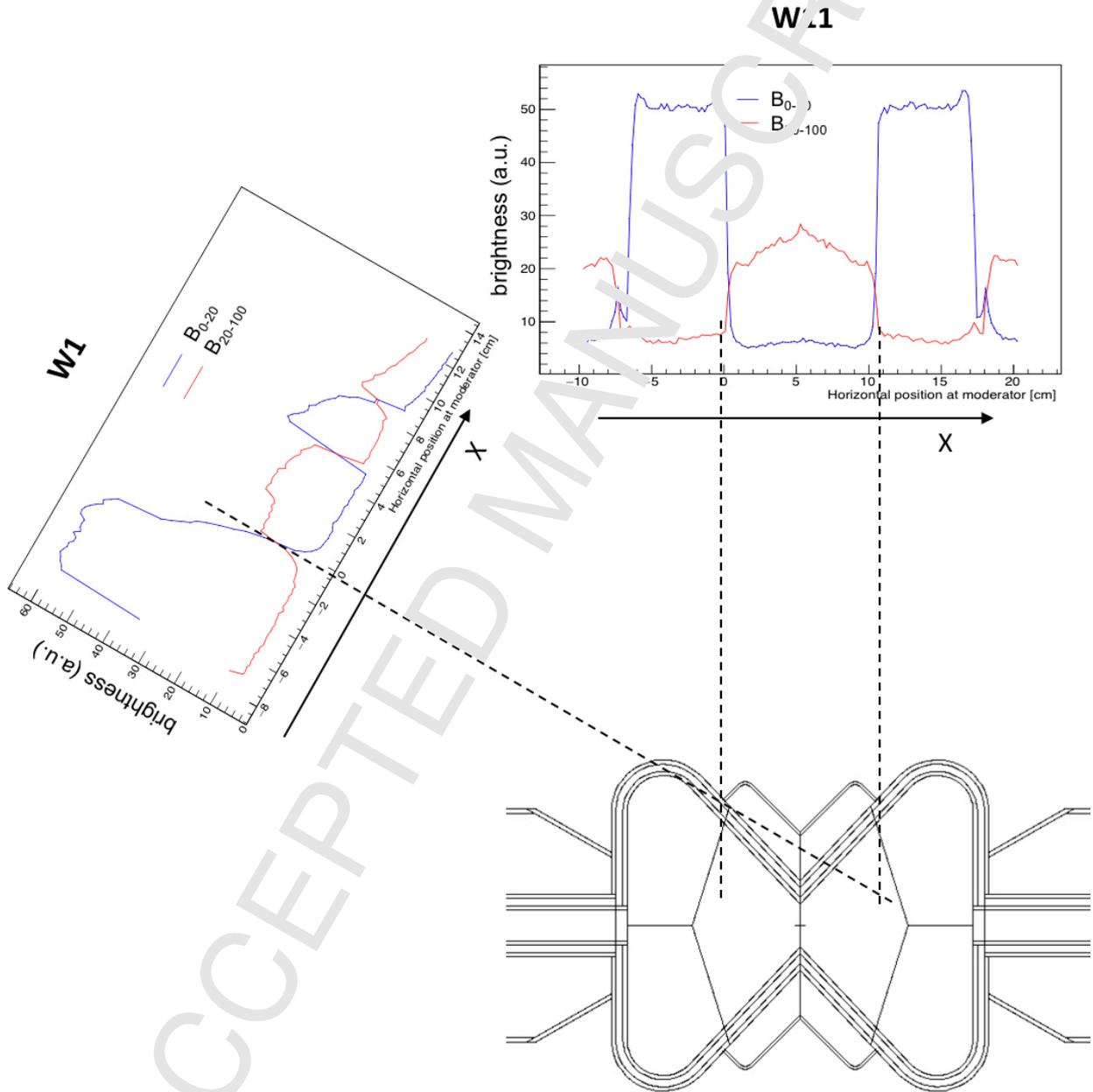


Figure 33. Horizontal brightness B_{0-20} and B_{20-100} distribution for the W3 beamport. The X axis corresponds to a line perpendicular to the beamport axis, with the 0 corresponding to the focal point (see Figure 32). These distributions are also valid for the S3, E3 and N3 beamports.

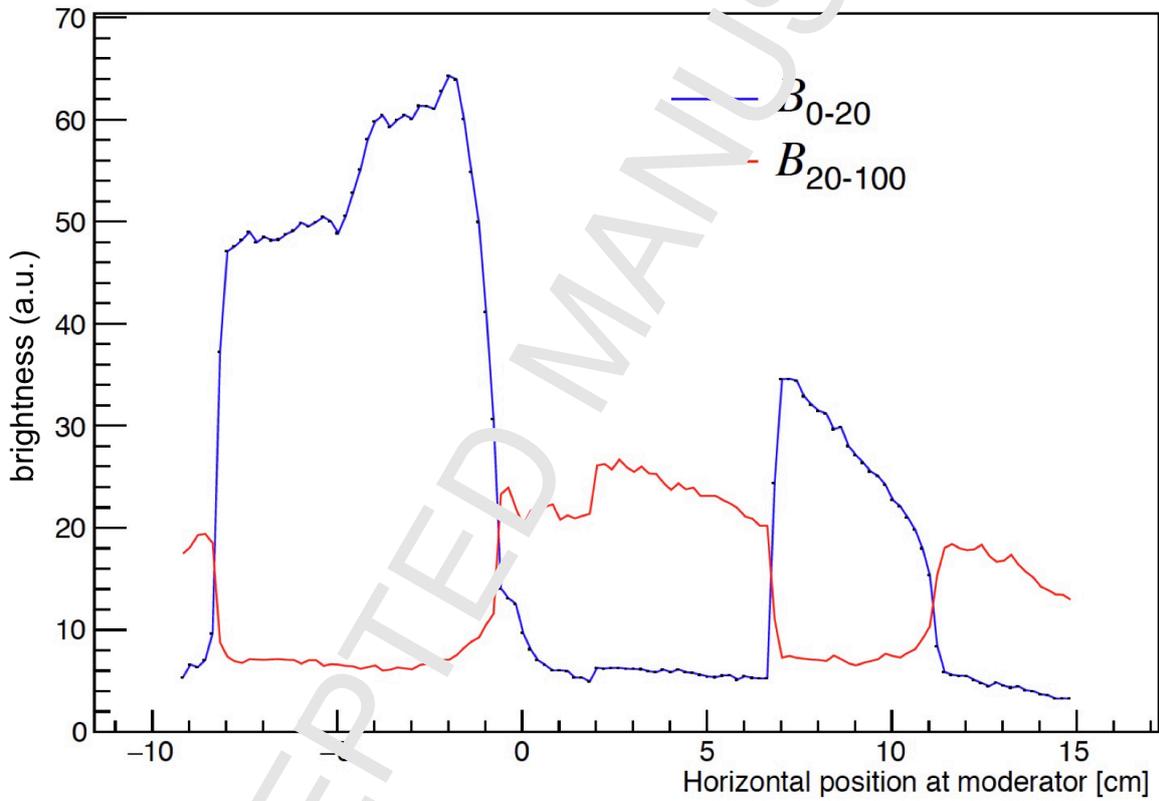


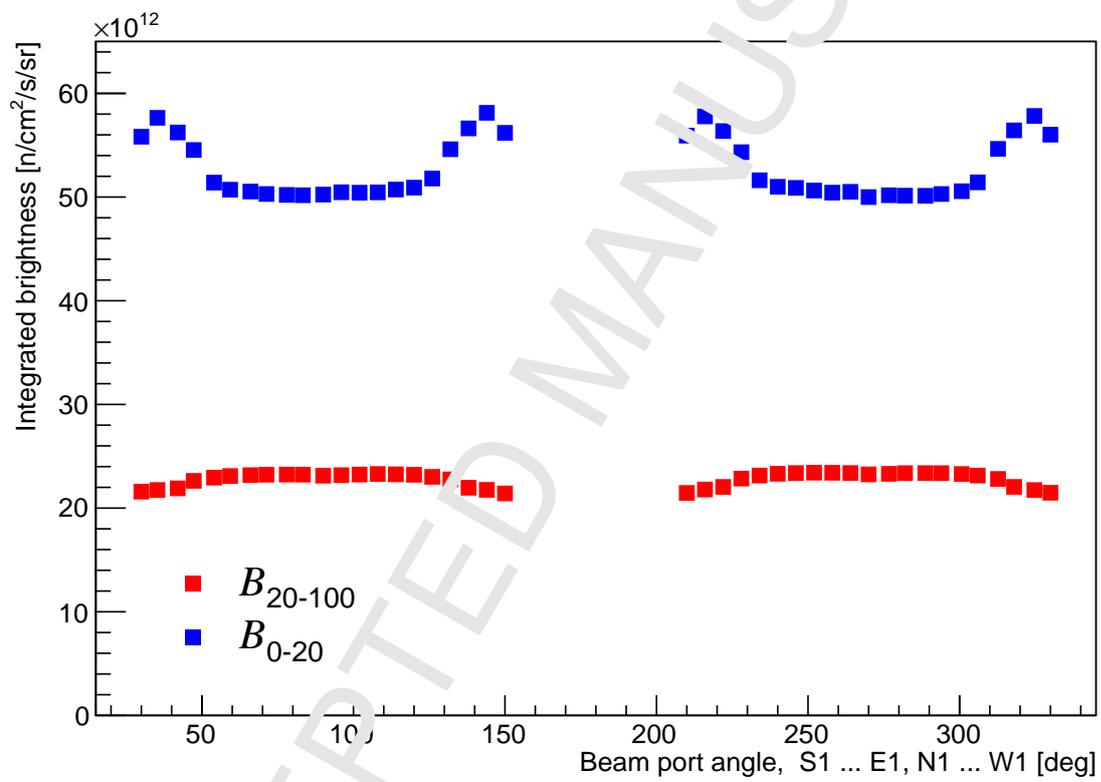
Figure 34. Distribution of B_{0-20} and B_{20-100} for the 42 beamports for the butterfly moderator with full engineering details.

Figure 35. Thermal and cold peak wavelength spectral brightness. Spectra are averaged over the viewed moderator surface area of $3 \times 6 \text{ cm}^2$.

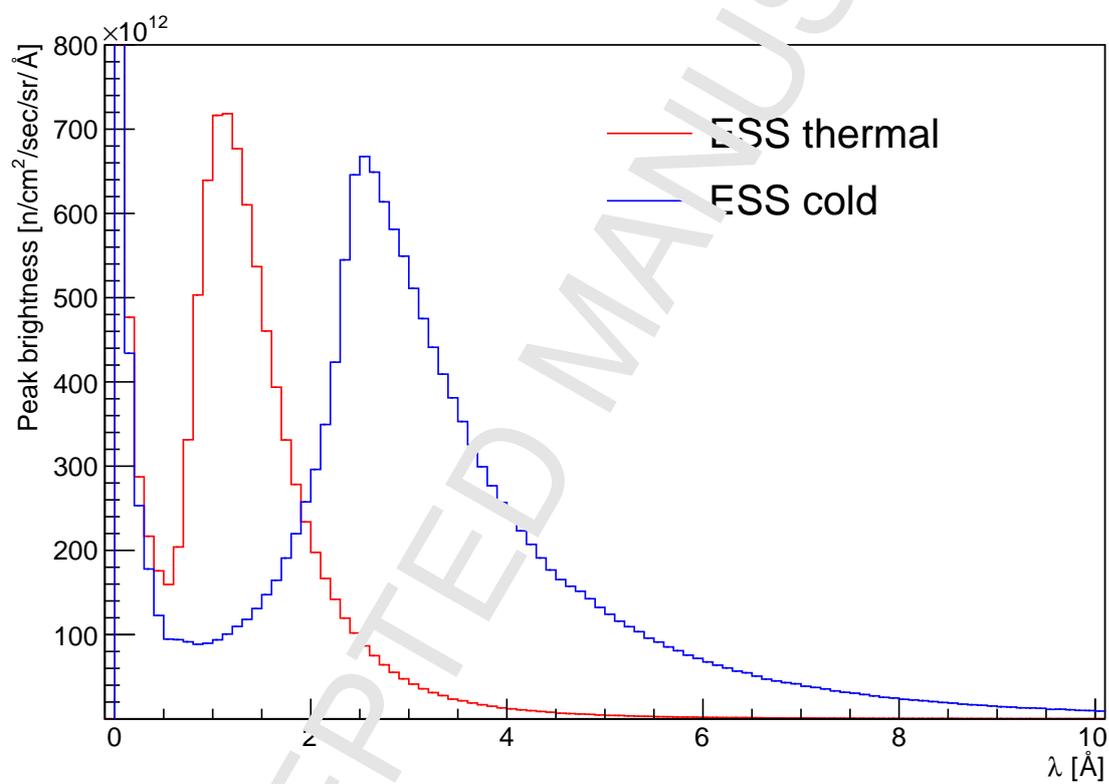


Figure 36. Brightness spectra averaged over 42 beamports for 3 cm high moderator, compared with ILL official curves [4].

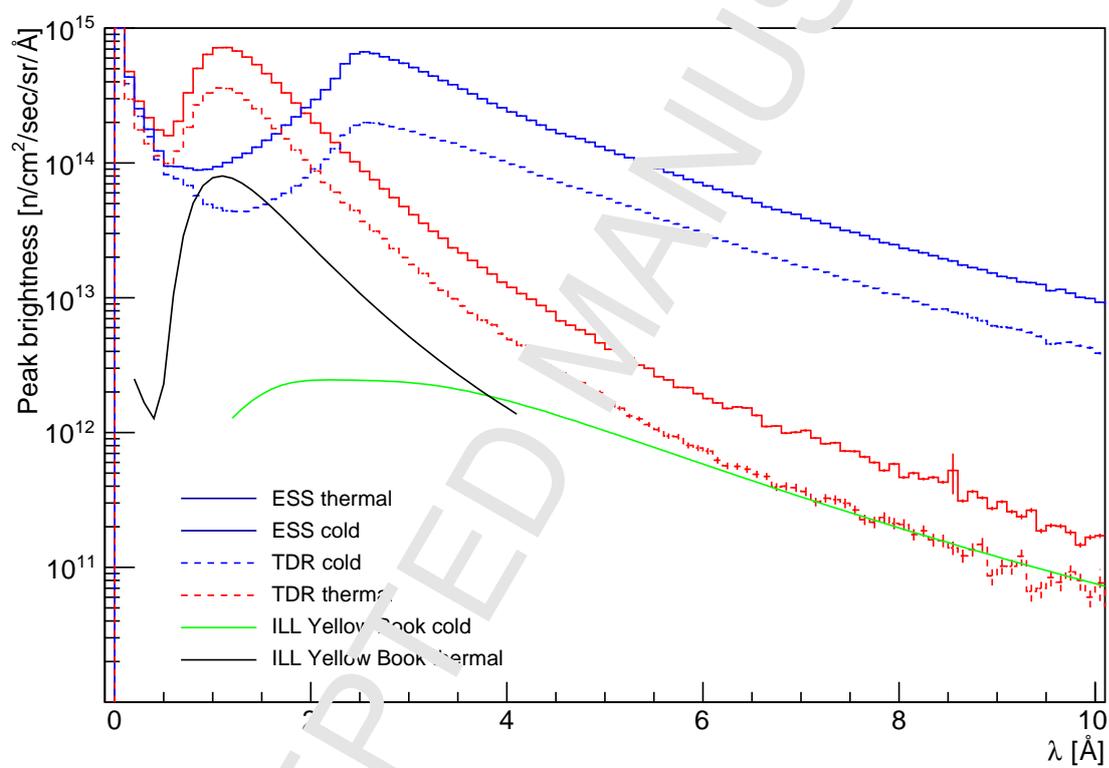


Figure 37. Cold collimators used in the MCNPX model for the brightness calculation. In the figure the collimators for the S1, S5 and S10 beamports are shown. The viewed width at the moderator is of 6 cm, the height is of 3 cm. The collimators intersect the point shown with the yellow dot, which is placed at 1.1 cm from the focal point (red dot), the origin of the axes of the beamports.

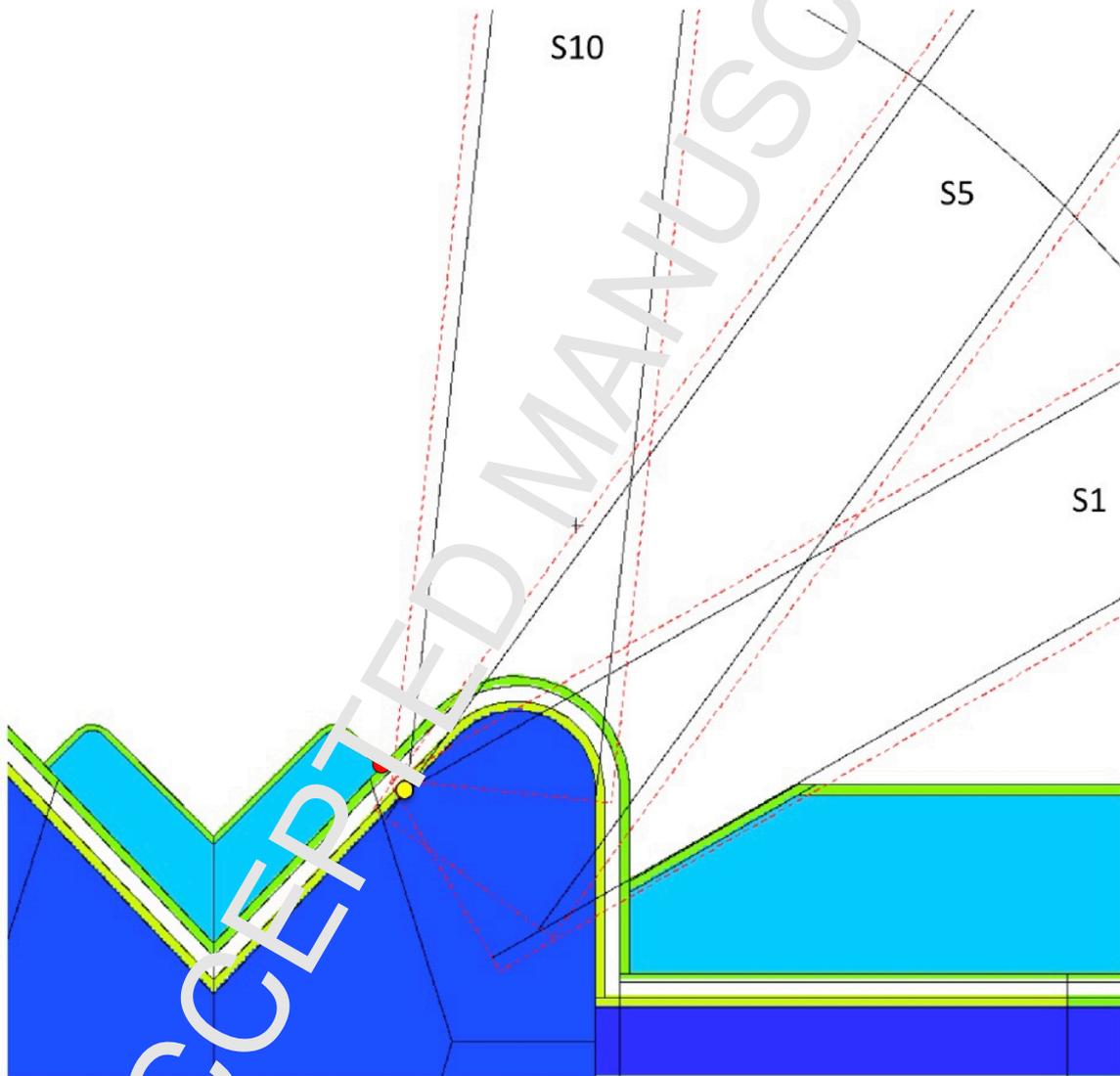


Figure 38. Geometry of box moderator.

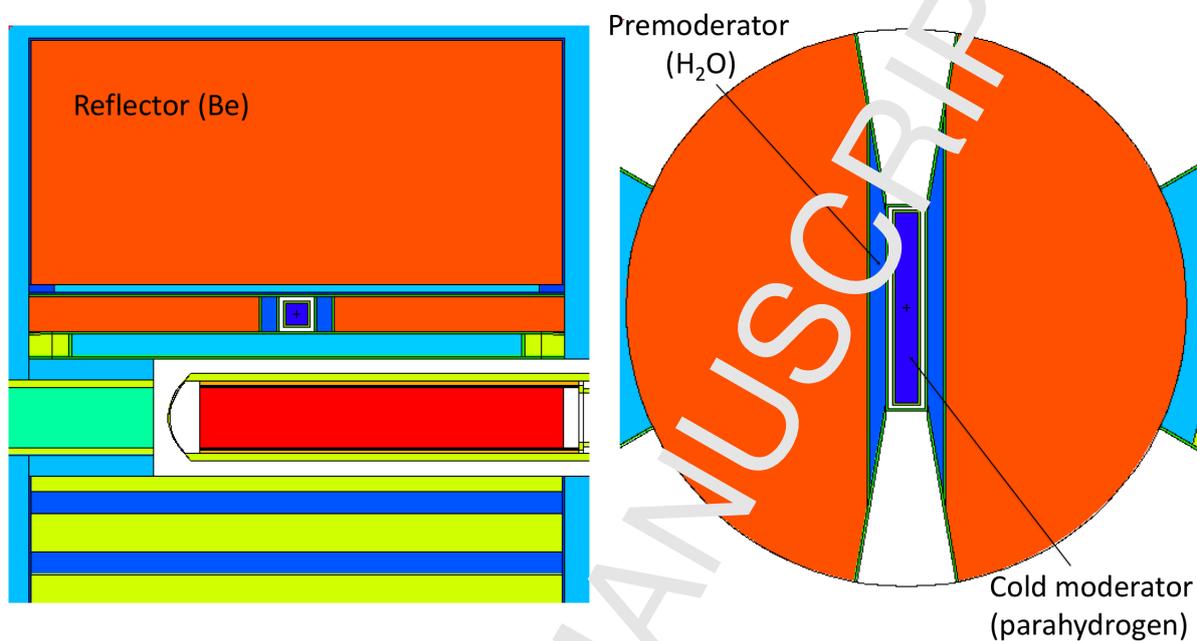
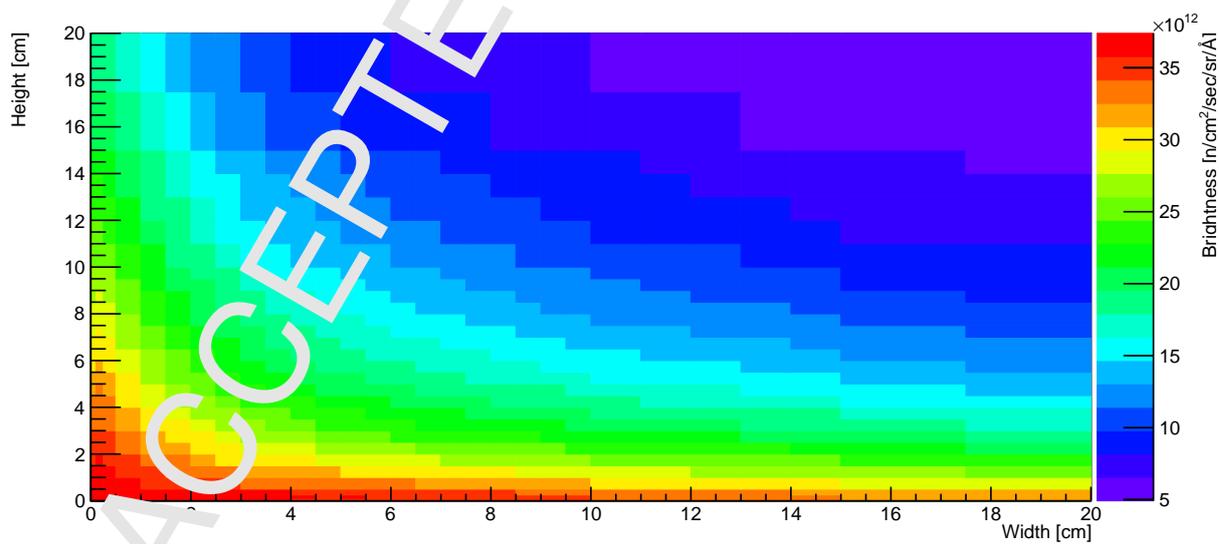


Figure 39. Brightness map as a function of lateral dimensions of a box moderator of 24 cm length.



918 **Appendix A. Brightness and figure of merit**

919 *Appendix A.1. Brightness and Liouville's theorem*

920 We first show the link between the brightness of a source and Liouville's theorem, and, as a consequence,
921 the fact that brightness is a constant of motion.

922 We define as neutron angular density $N(\mathbf{r}, \boldsymbol{\Omega}, E, t)$ the number of neutrons at the position \mathbf{r} with
923 direction $\boldsymbol{\Omega}$ and energy E at time t , per unit volume, per unit solid angle, per unit energy. The vector
924 position \mathbf{r} can be at the surface of a moderator, while $\boldsymbol{\Omega}$ is the direction of neutron emission:

$$N(\mathbf{r}, \boldsymbol{\Omega}, E, t) = \frac{n(\mathbf{r}, \boldsymbol{\Omega}, E, t)}{dV d\Omega dE} \quad (\text{A.1})$$

925 The unit of N is $\text{n/cm}^3/\text{sr/eV}$.

926 The brightness B is the product of the speed v , times the neutron angular density.

$$B(\mathbf{r}, \boldsymbol{\Omega}, E, t) = vN(\mathbf{r}, \boldsymbol{\Omega}, E, t) = v \frac{n(\mathbf{r}, \boldsymbol{\Omega}, E, t)}{dV d\Omega dE} \quad (\text{A.2})$$

927 The units of the brightness is $\text{n/cm}^2/\text{s/sr/eV}$.

928 On the other hand, the phase space density $\rho(\mathbf{q}, \mathbf{p}, t)$ is the number of particles in the phase space volume
929 $d\mathbf{q}d\mathbf{p} = dV p^2 dp d\Omega$ at time t :

$$\rho(\mathbf{q}, \mathbf{p}, t) = \frac{n(\mathbf{r}, \boldsymbol{\Omega}, E, t)}{dV p^2 dp d\Omega} = \frac{v}{p^2} \frac{n(\mathbf{r}, \boldsymbol{\Omega}, E, t)}{dV d\Omega dE} \quad (\text{A.3})$$

930 where we used the relationship between kinetic energy and momentum $E = \frac{p^2}{2m}$.

931 Liouville's theorem states that the phase space density $\rho(\mathbf{q}, \mathbf{p}, t)$, i.e. the number of particles in the phase
932 space volume $d\mathbf{p}d\mathbf{q}$ at a given time t is constant along particle trajectories in phase space, for conservative
933 force fields.

934 From the above two equations it follows that, for constant momentum, the neutron angular density and
935 the brightness B are constant along the direction of motion.

936 These results are also valid if brightness is expressed as a function of the λ , as it is commonly expressed,
937 instead of E .

938 In practical terms, conservation of the phase space density along the neutron trajectory (in phase space)
939 means that knowing the brightness, it is possible to determine the absolute flux at any point of the beam
940 extraction system. In reality, beam losses must also be considered. Neutrons emitted in a volume dV in
941 direction $d\boldsymbol{\Omega}$ around $\boldsymbol{\Omega}$ will be transported in a guide system, assuming only elastic scattering collisions (with
942 no change in neutron speed) and as the phase space density is constant, the divergence of the neutrons at the
943 sample will depend on how focused is the beam (the more focused is the beam, the higher its divergence).

944 *Appendix A.2. Figure of merit*

945 To calculate the brightness with MCNPX we use f5 point detector tallies that calculate the flux at a
946 point [8]:

$$\Phi(\mathbf{r}) = \int dE \int dt \int d\Omega v N(\mathbf{r}, \Omega, E, t) \quad (\text{A.4})$$

947 Thus, the f5 calculation integrates the brightness over 4π sr. If the integration is done in a solid angle
948 $\Delta\Omega$, defined from a point at a distance r much greater than the moderator dimensions, that subtends only
949 the moderator emission surface, so that the solid angle is $\Delta\Omega = \Delta S/r^2$, then the brightness defined by
950 MCNPX is

$$B(\mathbf{r}) = \frac{\Phi(\mathbf{r})}{\Delta\Omega} \quad (\text{A.5})$$

951 In practice, B can be calculated with specified bins in energy and time, so that, for small solid angles,
952 B is a function of $(\mathbf{r}, \Omega, E, t)$.

953 In this work we have often used the time-average, energy-integrated brightness between two energy values
954 E_1 and E_2 defined as

$$B_{E_1-E_2}(r, \Omega) = \int_{E_1}^{E_2} dE \int_0^{\infty} dt B(\mathbf{r}, \Omega, E, t) \quad (\text{A.6})$$

955 *Appendix A.3. Tallies*

956 Brightness is calculated for all the beamports in the two 120° beam extraction openings surrounding the
957 moderators, using point detector tallies placed at 10 m from the moderator surface. The tallies are placed
958 at the 42 angles corresponding to the actual beamport grid.

959 *Appendix A.4. Collimators*

960 The collimators are cells defined in MCNPX so that a point detector tally sees only the desired surface
961 of the moderator (usually 6 cm wide, 3 cm high).

962 Figure 37 shows the viewed horizontal widths at the cold moderator used in the MCNPX model for
963 brightness calculations. The viewed widths are defined by the solid lines, for all the beamports (in the figure
964 as examples the beamports S1, S5 and S10 are shown). In all the calculations the vertical range seen at the
965 moderator surface is always of 3 cm, while the reference horizontal width was of 6 cm. Due to the constraints
966 from the beam extraction system discussed in Section 4, there is limited margin in the positioning of the
967 collimators. A distance of about 1 cm from the focal point is allowed, and in the calculations the collimators
968 were at 1.1 cm from the focal point (see Figure 37).

Appendix B. Tube moderators

Based on fundamental physics properties discussed in Section 2.1, the natural extension of quasi-2-dimensional flat moderators are quasi-1-dimensional "tube-like" moderators. A physics model of a tube moderator adapted to the ESS target-moderator-reflector layout is shown in Figure 38. To study the performance of such moderators we consider for convenience a box shape. This is a basic design which features a box-shaped parahydrogen moderator, surrounded by a premoderator and beryllium reflector. The geometry of the target and reflector is the same as in the other studies, allowing a direct comparison of the brightness. After an optimization of the premoderator thickness, the optimal length of a reference moderator with $3 \times 3 \text{ cm}^2$ cross section was determined to be of 24 cm.

Then, with a fixed length of 24 cm, a two-dimensional brightness map as a function of width and height, size of emission surface given by (height \times width), was calculated (Figure 39). The brightness map indicates a strong increase in brightness with decrease in the moderator height, as it has been already observed for the flat moderators. Increase in brightness with decrease in the moderator width is less pronounced. This is due to the size of the neutron production hotspot (cf. Figure 21). The immediate conclusion is that tube moderators would be particularly suitable for compact neutron sources where the size of neutron production region is comparatively small.

The stand-alone tube moderator of $3 \times 3 \times 24 \text{ cm}^3$ exhibits cold B_{0-5} brightness about 2 times higher than the flat butterfly moderator. However, the tube moderator is highly directional and it can serve narrow extraction angles only. One way to increase the extraction angles would be to combine several tubes in different configurations.

Other examples of tube-like moderators, applied to small sources, are given in [34].

- [1] S. Peggs editor, ESS Technical Design Report, ISBN 978-91-980173-2-8, 2013, <http://europenspallationsource.se/scientific-technical-documentation>
- [2] F. Mezei, *Long pulse spallation sources*, Physica B 234-236 (1997) 1227.
- [3] M. Magán et al., *Neutronic analysis of the bispectral moderator such as that proposed for ESS*, Nucl. Instrum. Methods A729 (2013) 417425.
- [4] Institut Laue-Langevin, 'LL Yellow Book 2008.' <http://www.ill.eu/?id=1379>, 2008.
- [5] K. Batkov, A. Takibayev, J. Zanini and F. Mezei, Unperturbed moderator brightness in pulsed neutron sources, Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment 729 (2013) 500 - 505. doi:<http://dx.doi.org/10.1016/j.nima.2013.07.031>.
- [6] F. Mezei, L. Zanini, A. Takibayev, K. Batkov, E. Klinkby, E. Pitcher, and T. Schönfeldt, *Low dimensional neutron moderators for enhanced source brightness*, Journal of Neutron Research 17 (2014) 101 - 105.
- [7] Waters L. S. et al. 2007 The MCNPX Monte Carlo radiation transport code. *AIP Conf.Proc.* **896**, 81-90.
- [8] MCNP, *A general Monte Carlo N-Particle Transport code*, LA-UR-03-1987, 2003.
- [9] D. Pelowitz editor, *MCNPX Users Manual, Version 2.7.0*, Number LA-CP-11-0438, 2011.
- [10] L. Zanini, K. Batkov, E. Klinkby, F. Mezei, E. Pitcher, T. Schönfeldt, A. Takibayev *Moderator Configuration Options for ESS*, proceedings of the ICANS-XXI conference, JAEA-Conf 20-15-002, 2014.

- 1006 [11] F. X. Gallmeier, W. Lu, B. W. Riemer, J. K. Zhao, K. W. Herwig, and J. L. Robertson, Conceptual moderator studies
1007 for the Spallation Neutron Source short-pulse second target station, *Review of Scientific Instruments* **87**, 063304 (2016).
- 1008 [12] U. Rücker, T. Cronert, J. Voigt *et al.*, *Eur. Phys. J. Plus* (2016) 131: 19. <https://doi.org/10.1140/epjp/i2016-16019-5>.
- 1009 [13] K. H. Andersen, M. Bertelsen, L. Zanini, E. B. Klinkby, T. Schönfeldt, P. M. Bentley and J. Saroun, *Optimisation of*
1010 *moderators and beam extraction at ESS*, *JAC* **51**, 264 (2018).
- 1011 [14] N. Watanabe, *Neutronics of pulsed spallation neutron source*, *Rep. Prog. Phys.* **66** (2003) 35–281, and references therein.
- 1012 [15] K. B. Grammer *et al.*, *Measurement of the Scattering Cross Section of Slow Neutrons on Liquid Parahydrogen from*
1013 *Neutron Transmission* *Phys. Rev.* **B 91**, 180301(R) (2015).
- 1014 [16] J. Schwinger and E. Teller, *The Scattering of Neutrons by Ortho- and Parahydrogen*, *Phys. Rev.* **52**, 286 (1937).
- 1015 [17] P. Rock, *Chemical thermodynamics; principles and applications* (Macmillan 1969). ISBN 1-891389-32-7
- 1016 [18] T. Kai, M. Harada, M. Teshigawara, N. Watanabe, Y. Ikeda, *Coupled hydrogen moderator optimisation with ortho/para*
1017 *hydrogen ratio*, *Nuclear Instrum. Methods in Physics Research A* **523**, 378 (2004).
- 1018 [19] M. Harada, M. Teshigawara, M. Ohi, E. Klinkby, L. Zanini, K. Batkov, K. Okawa, Y. Toh, A. Kimura, Y. Ikeda,
1019 *Experimental validation of the brightness distribution on the surfaces of coupled and decoupled moderators composed of*
1020 *99.8% parahydrogen at the J-PARC pulsed spallation neutron source*, *Volume 903*, p. 38, 2018.
- 1021 [20] R. Golub, K. Bning, and H. Weber, *Ultra-Cold Neutrons at the SNQ Spallation Source*, TUM-E21/SNQ-UCN/81-4, 1981.
- 1022 [21] E. Klinkby, K. Batkov, F. Mezei, E. Pitcher, T. Schönfeldt, A. Takibayev, and L. Zanini, *In-Pile ⁴He Source for UCN*
1023 *Production at the ESS*, *Adv. High Energy Phys.*, 2014, 2014, p. 24–339, doi 10.1155/2014/241639
- 1024 [22] Micklich B.J. and Carpenter J.M (editors), *Proceedings of the workshop on Applications of a Very Cold Neutron Source*,
1025 August 21-24, 2005, Argonne, Illinois, ANL-05/42, Argonne National Laboratory (2005).
- 1026 [23] L. Zanini, K. Batkov, F. Mezei, A. Takibayev, E. Klinkby, T. Schönfeldt, *The neutron moderators at the European*
1027 *Spallation Source*, proceedings of the AccApp'15 conference <http://accapp15.org/wp-content/data/index.html>, 2015.
- 1028 [24] T. Schönfeldt, *Advanced Neutron Moderators*, PhD thesis, Technical University of Denmark, 2017.
- 1029 [25] L. Zanini, K. Batkov, E. Klinkby, F. Mezei, T. Schönfeldt, and A. Takibayev, *The neutron moderators for the European*
1030 *Spallation Source*, *Journal of Physics Conference Series* **1021**(1):012066, DOI: 10.1088/1742-6596/1021/1/012066, 2018.
- 1031 [26] Carpenter, Loong, *Elements of slow neutron scattering*, 2016.
- 1032 [27] R. Garoby *et al.*, *The European Spallation Source Design*, *Physica Scripta*, Vol. 93, N. 1, 2017.
- 1033 [28] Y. Bessler, private communication, 2016.
- 1034 [29] P. Willendrup, E. Farhi and K. Lefmann, *McStas 1.7 a new version of the flexible Monte Carlo neutron scattering package*,
1035 *Physica B*, **350** (2004) E735.
- 1036 [30] T. Kittelmann, E. Klinkby, F. B. Knudsen, P. Willendrup, X. X. Cai, and K. Kanaki, Kalliopi, *Monte Carlo Particle*
1037 *Lists: MCPL*, *Comput. Phys. Commun.*, **218**, 17, 2017, ARXIV:1609.02792.
- 1038 [31] V.V. Nesvizhevsky, E.V. Mochagin, A. Yu. Muzychka, A.V. Strelkov, G. Pignol, K.V. Protasov, *The reflection of very cold*
1039 *neutrons from diamond powder nanoparticles* *Nuclear Instrum. Methods Physics Research A* **595** (2008) 631.
- 1040 [32] E. B. Klinkby, K. Batkov, F. Mezei, T. Schönfeldt, A. Takibayev, L. Zanini, *Voluminous D2 source for intense cold*
1041 *neutron beam production at the ESS*, in: arXiv physics eprints, No. arXiv:1401.6003, 2014.
- 1042 [33] D. Milstead, *A new high sensitivity search for neutron-antineutron oscillations at the ESS*, arXiv:1510.01569v1
- 1043 [34] L. Zanini, F. Mezei, K. Batkov, E. Klinkby and A. Takibayev, *General use of low-dimensional moderators in neutron*
1044 *sources*, *Journal of Physics Conference Series* **1021**(1):012009, DOI: 10.1088/1742-6596/1021/1/012009, 2018

Table 1. Variation of the beamport-averaged brightness B_{0-20} on the top moderator as a function of different moderator or fast neutron reflector configurations below the target.

configuration	gain factor
two moderators	1
Be 10% water	1.09
Pb	1.20
W 22% He	1.18
Steel 10% water	1.10
Steel 20% water	1.07
Cu 20% water	1.09

Table 2. Time-average integral thermal and cold brightness in $[n/cm^2/sr/s]$ for 5 MW average beam power of different moderator concepts. ESS peak brightness are 25 times the indicated numbers. In the last column the ILL Yellow Book brightness is listed [4].

	TDR	PC near	PC far	BF1	BF2	ILL YB
opening	$4 \times 60^\circ$	$2 \times 120^\circ$	$2 \times 120^\circ$	$2 \times 120^\circ$	$2 \times 120^\circ$	
B_{20-100}	1.06×10^{13}	1.6×10^{13}	2.21×10^{13}	2.47×10^{13}	2.60×10^{13}	6.7×10^{13}
B_{0-20}	1.98×10^{13}	5.23×10^{13}	4.83×10^{13}	5.45×10^{13}	4.94×10^{13}	7.5×10^{12}