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Fundamental Limitation of Electrocatalytic Methane Conversion to Methanol

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The electrochemical oxidation of methane to methanol at remote oil fields where methane is flared is the ultimate solution to harness this valuable energy resource. In this study we identify a fundamental surface catalytic limitation of this process in terms of a compromise between selectivity and activity, as oxygen evolution is a competing reaction. By investigating two classes of materials, rutile oxides and two-dimensional transition metal nitrides and carbides (MXenes), we find a linear relationship between the energy needed to activate methane, i.e. to break the first C-H bond, and oxygen binding energies on the surface. Based on a simple kinetic model we can conclude that in order to obtain sufficient activity oxygen has to bind weakly to the surface but there is an upper limit to retain selectivity. Few potentially interesting candidates are found but this relatively simple description enables future large scale screening studies for more optimal candidates.

1 Introduction

At oil fields around the globe, an estimated 150 billion cubic meters of methane (CH\textsubscript{4}, natural gas) are burned as waste, every day, corresponding to 20% of the U.S. gas consumption\textsuperscript{2}. Consequently, CO\textsubscript{2} is released into the atmosphere contributing with 3% of the global CO\textsubscript{2} emissions\textsuperscript{3} and an enormous amount of energy (30 EJ\textsuperscript{2}) is lost annually. Methane has 25 times the global warming potential of carbon dioxide, which is why it is usually burned instead of released directly\textsuperscript{2}. This happens at remotely located oil fields where there is insufficient infrastructure to store and transport the gaseous methane. One attractive solution to this problem would be to develop a remote-deployable technology which can oxidise methane into a liquid fuel, such as methanol, that would fit better into the existing infrastructure. This has been a major challenge within the field of heterogeneous catalysis for decades\textsuperscript{2,4–9}. However, the direct routes to produce methanol from methane are inefficient, require high pressures, are unselective or require oxidants such as H\textsubscript{2}O\textsubscript{2}, for which transportation to remote locations is extremely challenging. To yield higher efficiencies, more complex, indirect multistage processes can be utilized but has drawbacks in form of requiring higher temperatures and pressures and consequently extended infrastructure. In contrast, the electrochemical oxidation of methane to methanol could be far more attractive. A schematic of an electrochemical fuel cell producing methanol is shown in Fig. 1 requiring only methane, water and oxygen. The overall reaction is

$$\text{CH}_4(g) + \frac{1}{2}\text{O}_2(g) \rightarrow \text{CH}_3\text{OH}(l) \quad (1)$$

$$\Delta G^0 \approx -116.0 \text{kJ/mol}$$

At the anode, CH\textsubscript{4} is oxidised to methanol according to:

$$\text{CH}_4 + \text{H}_2\text{O} \rightarrow \text{CH}_3\text{OH} + 2(\text{H}^+ + e^-) \quad (2)$$

$$\Delta G^0 \approx 121.2 \text{kJ/mol}$$

$$E_{\text{cell}}^0 \approx -0.63 \text{ V (RHE)}$$

whereas at the cathode, O\textsubscript{2} is reduced to H\textsubscript{2}O:

$$\frac{1}{2}\text{O}_2 + 2(\text{H}^+ + e^-) \rightarrow \text{H}_2\text{O} \quad (3)$$

$$\Delta G^0 \approx -228.6 \text{kJ/mol}$$

$$E_{\text{cell}}^0 \approx 1.18 \text{ V (RHE)}$$

Rather than consuming energy, such a device could in principle produce energy to harness in the form of electricity, in addition to the liquid fuel methanol. This is the ultimate solution for tapping into the wasted methane. The device would be portable with easy scale up and the produced liquid methanol could be easily stored.

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in tanks in areas without sufficient pipelines. In this study we identify the fundamental surface catalytic limitations for methane oxidation to methanol. The challenge is to produce methanol at high rates and selectivity requiring at least three criteria to be fulfilled: 1) Activate CH$_4$ and form CH$_3$OH, 2) Avoid O$_2$ evolution and 3) Avoid CH$_3$OH oxidation to the more thermodynamically favourable product, CO$_2$.

As for CO$_2$ reduction, the key component in controlling the performance of electrochemical devices is the interface between the electrolyte and electrode. Typically, metal electrocatalysts produce CO$_2$ by oxidising methane. A number of reports in the literature have been devoted to the oxidation of methane to methanol at low temperatures (i.e. 100°C or below), via (i) an indirect method or (ii) a direct method. In the indirect method, the same electrode acts as cathode and anode, reducing O$_2$ and at the same time oxidising methane. Earlier studies suggest that this proceeds by the formation of the superoxide anion via an “outer-sphere” solution phase step. This highly reactive species would abstract a proton from methane, allowing it to be oxidised. However, it would be far more attractive to oxidise methane directly, avoiding its potentially explosive mixture with O$_2$.

Upon oxidising methane, reactive metals such as Pt produce close to 100% CO$_2$. On the other hand, oxides seem to be able to produce methanol; for instance V$_2$O$_5$ on SnO$_2$ produces 60% methanol at a current density of 4 mA cm$^{-2}$ at 100°C. Methanol production peaked at a cell potential of 0.9 V, i.e. equivalent to an energy input of ~170 kJ/mol; however, this input is only 25% of the Gibbs free energy released upon the complete oxidation of methanol to CO$_2$. In order for this to be industrially viable, the current density has to be increased, selectivity improved and the overpotential minimized.

The catalyst material needs to bind oxygen weakly or as a radical, to have the driving force for oxidizing methane. The consequence is that the potential needed to run the reaction: H$_2$O + star o + 2(H$^+$ + e$^-$) is high, but at the same time below the potential necessary to catalyse the oxygen evolution. The activity of the methanol production therefore depends on having available +O species to react with methane but in order to ensure selectivity towards the methanol reaction pathway the coverage of these +O species should be kept low and the catalyst should have a high oxygen vacancy formation energy to avoid O$_2$ formation. Consequently, it is not a precondition that the bare surface has to be an effective catalyst for thermal methane activation since the reactivity is determined by the adsorption energy of +O, which is obtained via electrochemical water splitting.

Furthermore it poses a challenge to selectively form methanol versus the more thermodynamically favoured products, in particular CO$_2$ according to:

$$\text{CH}_4(g) + 2\text{O}_2(g) \rightarrow \text{CO}_2(g) + \text{H}_2\text{O}(g) \quad (4)$$

ΔG ≈ −801 kJ/mol.

However, based on the work of Behm and co-workers on similar reactions, we propose that accelerated mass transport of methanol away from the surface could prevent its oxidation. This could be controlled by judicious electrode structuring and mass transport as we do not expect that the further oxidation of methanol can be avoided by controlling the catalyst material. In this study we therefore focus on how to obtain methanol and further oxidation reactions will be considered in future work.

![Fig. 1 Schematic figure of an electrochemical fuel cell converting CH$_4$ and O$_2$ into CH$_3$OH and H$_2$O](Image)

![Fig. 2 Top and side view of the a) (110) rutile transition metal oxides and b) MXenes. Oxygen atoms are red, metal atoms light grey and green and carbon atoms are brown.](Image)

In this study we investigate two different classes of surfaces for methanol production. The (110) surface of rutile transition metal oxides, MeO$_2$ (Me; a transition metal atom), and monolayer MXenes of the AB$_2$C$_2$O$_2$ type (A, B: two transition metal atoms). MXenes is a new class of two-dimensional materials comprising carbides and nitrides of transition metals. MXenes have shown
promise for various applications in lithium/sodium ion batteries and as HER catalysts. MXenes come in various types; M₃X₂, MₓX₂A₂, MₓX₂A₃, MₓX₂A₄ etc., where M refers to the transition metal, X refers to carbon or nitrogen and A refers to the functional group present on the surface (O, OH or F). Additionally, all the MXenes considered here are metallic resulting in better electron transport properties under operating conditions compared to the mostly semiconducting rutile oxides. In this study, we limit ourselves to seven candidates. In this class of materials, this is vast. In this study, we limit ourselves to seven candidates.

The second part of the overall reaction in Eq. (1) is a reaction between atomic oxygen on the metal oxide surface and methane, which is a purely thermal catalytic step. The reaction pathway consists of the following elementary reactions:

- $\text{O} + \text{CH}_4(g) \rightarrow \text{O} \cdots \text{CH}_4$ (13)
- $\rightarrow \text{O} \cdots \text{CH}_3$ (14)
- $\rightarrow \text{CH}_2\text{OH}$ (15)
- $\rightarrow \text{H}_2\text{O}$ (16)

where $\text{O}$ in Eq. (13) is the same site as $\text{O}$ introduced in Eq. (6). The product of the reaction in Eq. (13) is an oxygen atom bonded to the active site and $\text{CH}_4$ in the vicinity to it. Eq. (14) denotes the transition state and Eq. (15) is $\text{CH}_2\text{OH}$ bonded to the surface. Eq. (16) is the final state, which is the clean surface and gas phase methanol. The reaction is therefore found to proceed via the coupling of $\text{CH}_3$ and a OH on the surface. This reaction
pathway was established by carrying out Climbing Image Nudged Elastic Band (CI-NEB) calculations for RhO$_2$ (see Fig. 5), VO$_2$ and a few of the MXenes. In Fig. 5, images are shown along the pathway. The first image in Fig. 5 corresponds to $\ast$O···CH$_4$ in Eq. (13) and the last to $\ast$CH$_3$OH in Eq. (15). Image 3 in Fig. 5 is the transition state where the methane has delivered a single H atom to the $\ast$O site and CH$_3$ is in the vicinity. This transition state is in consensus with what has been named the radical pathway, but for a different reaction, in a recent publication from Latimer et. al.\textsuperscript{23}

Analysis of the structure of the adsorbate in the transition state shows that the CH$_3$ molecule exhibits planar geometry with all H-C-H bonding angles $\sim$120°. However, the geometry of the CH$_4$ molecule is tetrahedral with all H-C-H bonding angles of $\sim$109.5°. This suggests that the energy required to break the first C-H bond, i.e. to activate methane, equals the energy needed to deliver a single H atom to the surface and form CH$_3$ from CH$_4$, i.e.:

$$E_{\text{act}} = (E_{\text{CH}_3(g)} - E_{\text{CH}_4(g)}) + (E_{\ast\text{OH}} - E_{\ast\text{O}}) \quad (17)$$

relating the activation energy to $\Delta G_3$ in Eq. (11). This corresponds to converting the sp$^3$ hybridisation in CH$_4$ to sp$^2$ hybridisation in CH$_3$ and the double bonded oxygen to the metal atom to a single bonded OH group on the surface. In Fig. 5, the activation energy of Eq. (17) is plotted with circles against the descriptor $E_{\ast\text{OH}} - E_{\ast\text{O}}$. With this model, all materials lie on a straight line. The activation energy calculated with the CI-NEB method according to

$$E_{\text{act}} = E_{\ast(\text{OH} \cdots \text{CH}_3)} - E_{\ast\text{O} \cdots \text{CH}_4} \quad (18)$$

is marked with squares in Fig. 5. Marked with triangles is an approximated calculated activation energy using the already found CI-NEB path and unit cell of RhO$_2$ for all the other materials of the MeO$_2$ type (except VO$_2$). The approximated and calculated
The calculated activation energy is found to be very low or 0 eV in agreement with that. The data in Fig. 5 can also be interpreted as the potential vs. rate i.e. the applied potential needed to run the reaction vs. rate of methanol production. As higher potential is applied (more negative $E_{OH} - E_O$ values) the activation energy increases, lowering the rate for methanol production at a given temperature.

For RhO$_2$, RuO$_2$, CrO$_2$, ReO$_2$, and TaHf$_2$C$_2$O$_2$ the estimation is excellent with a deviation below 0.1 eV from the calculated value. For ReO$_2$, NbO$_2$ and NbTa$_2$C$_2$O$_2$, the deviation is below 0.2 eV and for MnO$_2$, VO$_2$ and MoO$_2$ the deviation is above 0.3 eV. For SnO$_2$, PtO$_2$ and TiO$_2$ the estimation for the activation energy is below 0.0 eV i.e., indicating formation of has no kinetic barrier. The calculated activation energy is found to be very low or 0.0 eV in agreement with that. The data in Fig. 6 can also be interpreted as potential vs. rate i.e. the applied potential needed to run the reaction vs. rate of methanol production. As higher potential is applied (more negative $E_{OH} - E_O$ values) the activation energy increases, lowering the rate for methanol production at a given temperature.

IrO$_2$, RuO$_2$, WTi$_2$C$_2$O$_2$ and TaHf$_2$C$_2$O$_2$ were found to have $\Delta G_2$ as the potential limiting step and relatively low overpotential. Consequently, they are found to have an activation energy of reasonable magnitude, in order for the methanol production reaction to run at a sufficient rate at a given temperature. The more oxidized structure, V$_2$O$_5$, appears on the left side of the volcano in Fig. 5 but $E_O - E_{OH}$ is not a good descriptor for it as OH very weakly bonded (Fig. 3). Therefore, it is the first step, $\Delta G_3 = G_{OH}$ which is the potential determining step and consequently O is never present on the surface on V$_2$O$_5$. In ref. [13], 1 wt.% V$_2$O$_5$ on SnO$_2$ was found to have the highest methanol production. Pure SnO$_2$ i.e. 0 wt.% V$_2$O$_5$ no methanol was produced and pure V$_2$O$_5$ i.e. 100 wt.% V$_2$O$_5$ methanol was produced but in much lower quantities than on 1 wt.% V$_2$O$_5$. The results presented here are partially in agreement what we find, SnO$_2$ is found on the right leg on the OER volcano (Fig. 4) with the potential limiting step the formation of oxygen on the surface and consequently negligible methanol production activity. The V$_2$O$_5$ shown here is a V$_2$O$_5$(001) surface which according to our calculations is not an active methanol catalyst but another surface termination or steps/defects on V$_2$O$_5$(001) could potentially have different energetics and consequently activity towards methanol production.

Having established a linear relation between the activation energy for methanol production and the descriptor $E_{OH} - E_O$ it is possible to investigate the rate of methanol production vs. oxygen evolution as function of the oxygen binding energy by a kinetic model. Assuming the scaling relations hold for the OER reaction i.e. $G_O \approx 2G_{OH}$ and $G_{OOH} = G_{OH} + 3.2$ eV the activation energy for the two reactions can be written as

$$E_{\text{act}}^{\text{CH}_3\text{OH}} = -\frac{1}{2}G_O + 2.4$$  \hfill (19)$$

$$E_{\text{act}}^{\text{O}_2} = -\frac{1}{2}G_O + 3.2 - eU$$  \hfill (20)

where the constant 2.4 in Eq. (19) comes from Eq. (17) and activation energy for oxygen evolution is assumed to be energy needed to form "OOH from "O. This corresponds to a lower limit

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**Fig. 6** The activation energy of methane activation plotted as a function of the descriptor $E_{OH} - E_O$. The MXenes are plotted in red and the MeO$_x$ in blue. Squares denote activation energies obtained using the CI-NEB method, triangles activation energies obtained using the optimized reaction path found on the RhO$_2$ structure and circles denote the estimated activation energy according to Eq. (17).
of the activation energy and any additional \( O_2 \) evolution energy barrier will increase the selectivity towards methanol formation. To keep the kinetic model simple but still capturing the important chemistry we consider the following reactions

\[
* + H_2O \xrightarrow{k^{+}_1} *O + 2(H^+ + e^-) \tag{21}
\]
\[
*O + CH_4 \xrightarrow{k^{+}_2} * + CH_3OH \tag{22}
\]
\[
*O + H_2O \xrightarrow{k^{+}_3} * + O_2 + 2(H^+ + e^-) \tag{23}
\]

from where we find that

\[
R_{\text{CH}_3\text{OH}} = p_{\text{CH}_4} k^{+}_2 \theta_{*O} = \frac{p_{\text{CH}_4} p_{\text{H}_2\text{O}} k^{+}_2 K_1(U)}{1 + p_{\text{H}_2\text{O}} K_1(U)} \tag{24}
\]
\[
R_{O_2} = p_{\text{H}_2\text{O}} k^{+}_3 (U) \theta_{*O} = \frac{p_{\text{H}_2\text{O}} k^{+}_3 (U) K_1(U)}{1 + p_{\text{H}_2\text{O}} K_1(U)} \tag{25}
\]

with

\[
K_1 = \frac{k^{+}_1}{k^{-}_1} \quad k^{+}_2 = \frac{k_B T}{h} \exp \left( \frac{E^{\text{act}}_{\text{CH}_3\text{OH}}}{k_B T} \right) \quad k^{+}_3 (U) = \frac{k_B T}{h} \exp \left( \frac{E^{\text{act}}_{O_2}}{k_B T} \right)
\]

The rate constant, \( k^{+}_2 \), in Eq. (22) does not depend on the applied potential as this is a purely thermal heterogeneous catalytic step where as the rate constant for the reaction in Eq. (23), \( k_3 \), depends on the applied potential. In Fig. 7 the rates for methanol production and oxygen evolution are plotted as a function of the binding energy of \( O_e \), \( E_0 \), at for \( p_{\text{H}_2\text{O}} = p_{\text{CH}_4} = 0.5 \) \((p_{\text{H}_2\text{O}} + p_{\text{CH}_4} = 1)\) and two different temperatures, 300 K and 400 K. It is important to note that the coverage of \( +O \) is kept fixed by applying a potential of \( U = 1/2eG_0 \) and thereby assuring that \( G_0(U) = 0 \text{ eV} \). The standard cell potentials for methanol production according to reaction (1) and OER are \(-0.63 \text{ V (RHE)} \) and \(-1.18 \text{ V (RHE)} \) assuming water to react from the gas phase, respectively. Consequently the rate for the two reactions is zero at potentials below 0.63 V (RHE) and 1.18 V (RHE) corresponding to \( G_0 = 1.3 \text{ eV} \) and \( G_0 = 2.36 \text{ eV} \) respectively as \( AG \) for each reaction is positive in this regime and equilibrium is towards the reactants rather than the products. From Fig. 7 it is clear that the rate of methanol production increases as the binding energy of oxygen on the surface decreases i.e. oxygen binds weaker to the surface. At \( U = 1.18 \text{ V} \) (\( G_0 = 2.36 \text{ eV} \)) the oxygen evolution becomes viable (for an ideal OER catalyst having zero overpotential) and runs at higher rate than methanol production as the activation energy is lower for the former. When \( G_0 > 3.2 \text{ eV} \) the activation energy for oxygen evolution is zero which first happens at \( G_0 > 4.75 \text{ eV} \) for the methanol production. For \( G_0 > 3.2 \text{ eV} \) there is no methanol production as \( AG_{3,4} \) becomes the potential limiting step and therefore \( +O \) is not present on the surface to react further with methane. Increasing the temperature by 100 K enhances the methanol production rate by several orders of magnitude depending on the oxygen binding energy where as the effect is much less pronounced for the OER as its activation energy is much lower. By use of geometric effects the difference in binding energy of OOH and \( O \) can be tuned in order to diminish the rate of the oxygen evolution reaction and consequently enhance the selectivity towards the methanol reaction pathway.

\[\text{Fig. 7} \text{ The rates for the OER (black) and methanol production (green) plotted according to Eq. (24) and (25) at 300K and 400K. The rates are plotted for a fixed coverage of +O with } G_0(U) = 0 \text{ eV} \text{ by applying a potential of } U = 1/2eG_0 \text{ V. The names of the materials considered here are marked along the bottom x-axis. The upper x-axis does as such denote the minimum required applied potential for oxygen adsorption on a specific surface.}\]

3 Conclusion

The production of methanol via an electrochemical process is found to be viable by considering a range of different rutile \( \text{MeO}_2(110) \) surfaces and \( \text{Ab}_2\text{C}_2\text{O}_2 \) MXenes as electrocatalysts. A fundamental surface catalytic limitation in terms of a compromise between selectivity and activity of the methanol production is identified. By changing the catalytic surface it is possible to tune the reactivity of an adsorbed oxygen atom. This is shown to correlate with the activation energy required to activate methane. A less stable oxygen binding catalyst, i.e. a catalyst providing a more reactive oxygen, results in a lower energy barrier to overcome. Consequently, a higher potential needs to be applied. A kinetic model validates the hypothesis that the rate for methanol production increases with weaker oxygen binding but in order to acquire sufficient selectivity the applied potential should not allow the full OER reaction to proceed. The candidates that fulfill the necessary criteria, i.e. have OOH adsorption as the potential limiting step (\( G_0 - G_0\text{OH} < 1.6 \text{ eV} \)) and \( 1.3 \text{ eV} < G_0 < 3.2 \text{ eV} \), and have reasonable activation energy at suitable temperatures are \( \text{IrO}_2 \), \( \text{RuO}_2 \), \( \text{RhO}_2 \), \( \text{WTi}_2\text{C}_2\text{O}_2 \) and \( \text{TaHf}_2\text{C}_2\text{O}_2 \). Only a small subset of the MXenes have been studied here, but the performance warrants a larger study. By varying the number of layers, the composition of the transition metals and surface terminations, we expect to find candidate materials with a more optimal binding to \( O \) and OH. As such, we anticipate there is ample room for improvement of the catalysis of this important reaction.
4 Computational Details

All calculations were performed using the Grid-based Projector Augmented Wave (GPAW) program with the Atomic Simulation Environment (ASE) interface. For the MeO₂ structures: Exchange and correlations (XC) were modelled on the Generalized Gradient Approximation (GGA) level, using the XC-functional, BEEF-vdW, and grid spacing of \( h = 0.18 \, \text{Å} \). The unit cell of the rutile (110) metal oxide slabs consisted of four tri-layers, in total 24 metal atoms and 48 oxygen atoms corresponding to a \((1 \times 3)\) surface unit cell. A k-point mesh of \((3 \times 3 \times 1)\) was used to sample the Brillouin zone.

For the MXenes: The PBE XC-functional was used and a plane wave cutoff of 800 eV employed. The \(2 \times 2\) unit cell was used, resulting in 28 atoms. A k-point mesh of \((9 \times 9 \times 1)\) was necessary. The unit cell of each material was optimised using the UnitCell-Filter method available in the ASE package. To model the transition state and obtain activation energies the Nudged Elastic Band method with the climbing image (CI-NEB) variation as implemented in ASE was used. The Gibbs free energies of the OER reactions were calculated according to the methods described in ref. The rate in Fig. 7 as a function of temperature we used \( H_2O(g) \) and \( H_2(g) \) as references and the zero-point for \( \pm O \) from ref. To obtain the free energies. All structures along with total energies will be available on Jan Rossmeis' group webpage (http://nano.ku.dk/english/research/theoretical-electrocatalysis/katladb/).

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Conflict of interest

There are no conflicts to declare.

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