Unexpected Stretching of Entangled Ring Macromolecules

Huang, Q.; Ahn, J.; Parisi, D.; Chang, T.; Hassager, O.; Panyukov, S.; Rubinstein, M.; Vlassopoulos, D.

Published in:
Physical Review Letters

Link to article, DOI:
10.1103/PhysRevLett.122.208001

Publication date:
2019

Document Version
Publisher's PDF, also known as Version of record

Link back to DTU Orbit

Citation (APA):
Unexpected Stretching of Entangled Ring Macromolecules

Q. Huang, J. Ahn, D. Parisi, T. Chang, O. Hassager, S. Panyukov, M. Rubinstein, and D. Vlassopoulos

Department of Chemical and Biochemical Engineering, Technical University of Denmark, 2800 Kongens Lyngby, Denmark
Division of Advanced Materials Science and Department of Chemistry, Pohang University of Science and Technology, Pohang 790784, Korea
Institute of Electronic Structure and Laser, Foundation for Research and Technology Hellas (FORTH), Heraklion, Crete 70013, Greece
Department of Materials Science and Technology, University of Crete, Heraklion, Crete 71003, Greece
P. N. Lebedev Physics Institute, Russian Academy of Sciences, Moscow 117924, Russia
Departments of Mechanical Engineering and Materials Science, Biomedical Engineering, Chemistry, and Physics, Duke University, Durham, North Carolina 27708, USA

(Received 28 December 2018; published 22 May 2019)

In the melt state at equilibrium, entangled nonconcatenated ring macromolecules adapt more compact conformations compared to their linear analogs and do not form an entanglement network. We show here that, when subjected to uniaxial stretching, they exhibit a unique response, which sets them apart from any other polymer. Remarkably, whereas both linear and ring polymers strain-harden, the viscosity of the rings increases dramatically (the melt thickens) at very low stretch rates due to the unraveling of their conformations along the stretching direction. At high rates, stretching leads to viscosity thinning similar to that of entangled linear polymers, albeit with subtle differences.

DOI: 10.1103/PhysRevLett.122.208001

The state-of-the-art understanding of entangled flexible polymer chains is based on the concept of entanglement network formation (characterized by a plateau modulus). Their motion, called reptation for linear polymers, reflects their ability to make conformational adjustments mediated by their free ends [1]. Incorporated into the tube model [2], the reptation concept has proven remarkably successful in predicting the linear and (in part) nonlinear rheology of linear polymers [1,2]. Linking the two free ends of a linear polymer has dramatic consequences, which have been explored in the last decade [3,4]. In brief, linked linear polymers, hereafter called rings, have compact conformation in the melt and reduced size compared to unlinked chains, as shown by neutron scattering [5,6] and molecular dynamics simulations [7,8]. In fact, very large nonconcatenated ring polymers in the entangled state approach an asymptotic state of compact conformations, where each polymer is compressed by surrounding rings because they cannot heavily overlap [7,8]. The resulting long-lived topological constraints between entangled nonconcatenated rings do not form an entanglement network as linear chains do (hence their stress relaxation modulus does not exhibit an entanglement plateau even at very large molar masses) and their zero-shear-rate viscosity is much lower compared to that of their linear entangled counterparts [3,9]. This sets rings apart from any other macromolecule, with several implications in diverse disciplines. For example, DNA forms highly compact loopy conformations in constrained environments (chromosome territories) [10,11] and becomes knotted in the presence of appropriate enzymes [12].

In view of this background, an outstanding challenge is to unravel the nonlinear rheology of rings as it pertains to their processing conditions relevant to the macromolecular engineering applications [13,14] as well as to the fundamental understanding of polymer dynamics with respect to the relation between molecular details and macroscopic properties. In fact, the field of nonlinear ring rheology is virtually virgin [15,16]. Recent fragmental evidence from experiments and simulations with marginally entangled rings under moderate nonlinear shear deformation indicates a much weaker thinning response compared to their linear counterparts, reminiscent of that of unentangled linear chains [16,17]. Yet, the most relevant flow in processing involves strong extensional components, which imparts substantial conformational changes on the macromolecules [13,18,19]. To date, entangled rings have never been subjected to extensional flows. Here, we present new experiments where we stretch well-characterized rings uniaxially under controlled conditions, using unique instrumentation, a filament stretching device [20]. We show that stretched entangled rings exhibit a hybrid response: at low rates, they depart from linear viscoelasticity with substantial viscosity thickening (exceeding one order of magnitude), whereas at higher rates, they behave similarly to their entangled linear counterparts (with the same molar mass) with thinning viscosity exhibiting a power-law dependence on stretch rate with an exponent of about $-1/2$.

The main message from the analysis of the linear viscoelastic (LVE) response is that ring purity is of utmost
of 1.01. This corresponds to \( \tau \) below (\( \tau \) of extensional rate of purified ring sample [3,21,27,28]). The explored range of extensional rates (see Figs. S2–S4 of the Supplemental Material) was determined by experimental measurements and the stress growth coefficient is then defined as \( \eta_\varepsilon(\dot{\varepsilon}, t) = \Delta \sigma / \dot{\varepsilon} \). At steady state, \( \Delta \sigma \) becomes independent of time and we define the extensional viscosity function by \( \eta_\varepsilon(\dot{\varepsilon}) = \Delta \sigma / \dot{\varepsilon} \). Further experimental details are presented in the Supplemental Material [24].

Figure 2(a) depicts the stress growth coefficient of the ring polymer and its linear precursor as functions of time for different values of \( \dot{\varepsilon} \). Based on knowledge from linear polymers [2], this range corresponds to orientation and stretching [Figs. 1(b) and 1(c)]. We observe that, in the investigated range of extensional rates, the polymers exhibit initial extension hardening. It appears, however, that this effect is significantly more pronounced in the ring polymer and this will be further discussed below. The same data are plotted in the form of stress versus strain in Fig. 2(b). This log-linear representation emphasized that steady-state values are reached; hence we assess the steady extensional viscosity as a function of rate below.

A closer look at the data of Fig. 2 reveals more features distinguishing rings from their linear counterparts. At the same extensional rate, the onset of stretching occurs earlier in linear polymers [Fig. 2(a)], which have longer relaxation times [24]. Moreover, steady state is reached earlier in linear polymers [see arrows in Fig. 2(b)]. Note that, in the absence of an entanglement network, it is difficult to transmit stress between different rings; hence the distribution of extensions may be broader and stretching delayed.

![FIG. 1. (a) Photo of stretched polystyrene in the perpendicular direction. (b) Illustration of equilibrated specimens before stretching with different conformations of entangled linear (top) and ring (bottom) polymers. (c) Illustration of stretched specimens with different conformations of the same [as in (b)] linear (top) and ring (bottom) polymers, showing the dramatic change in conformation due to stretching [18]. For clarity, we color one macromolecule with blue in each case, to emphasize its conformation in the melt.](image-url)
Certainly, the strong extensional flow is imposed on two systems with markedly different equilibrium conformations, rings being more compact. This is documented in a recent single-molecule study of DNA ring and linear polymers, which have been visualized when stretched in a cross-slot device\[29\].

The extracted steady-state extensional viscosities are plotted against $\varepsilon$ in Fig. 3 together with the inverse relaxation time for the molar mass of 185 000 g/mol linear and ring molecules, respectively. We note that the linear chains exhibit a transition from constant viscosity to a power-law behavior at about the inverse reptation time ($\tau_{\text{d}}^{-1}$) with no apparent change in behavior at the inverse Rouse time, as previously observed\[30\]. By contrast, at low rates, the extensional viscosity of the ring is smaller than its linear counterpart by about a factor of 50, corresponding to the absence of entanglement network and much more collapsed nature of the equilibrium ring configurations compared to linear molecules\[27\]. At intermediate rates, there is a dramatic transition with an increase in extensional viscosity of the rings by about a factor of 10 over one to two decades of extensional rate. We interpret this increase as being due to the unraveling and elongation of the rings by the extensional flow. Because of the collapsed state of the rings, this transition becomes more dramatic for the rings than for the linear molecules. Finally, at high rates, the extensional viscosity of the rings and the linear molecules are identical within experimental accuracy, both reaching a power-law behavior $\eta_E \sim \dot{\varepsilon}^{-1/2}$.

The $-1/2$ exponent at high extensional rates has been observed with a range of polymer melts, albeit all with free ends, including model linear\[30\] and star\[31\] polystyrene, long-chain branched polyethylene\[32,33\], and unentangled linear chains\[34\]. However, even for the simplest monodisperse linear polymer melts this exponent is still debatable. Recent molecular dynamics simulations indicate that the confining tube elongates and thins with $\dot{\varepsilon}$\[35\]. The original tube theory predicts orientation and stress saturation at rates exceeding the inverse reptation time, as discussed above, corresponding to a slope of $-1$\[36\] and then a strong increase in stress as the rate overcomes the inverse Rouse time. Indeed, such a qualitative behavior is

![FIG. 2.](image1)

FIG. 2. (a) Stress growth coefficient of linear (185 000 g/mol) and ring (185 000 g/mol) polymers at 130 °C and different extensional rates in the range $3 \times 10^{-3} - 1$ s$^{-1}$. The linear viscoelastic envelopes (from Fig. S1) are depicted by solid lines. (b) The same data plotted as stress against Hencky strain in linear scale, showing that a steady state has been reached. The arrows indicate the start of steady state for the highest extensional rate.

![FIG. 3.](image2)

FIG. 3. Steady-state uniaxial extensional viscosity extracted from Fig. 2 at 130°C, as a function of the imposed extensional rate for the linear precursor (filled black squares), ring (open blue circles), and a linear polymer with molar mass 100 000 g/mol (gray stars) with about half molar mass (actually 54%). The respective zero-rate limiting viscosities extracted from the dynamic shear data (accounting for the Trouton ratio of 3\[14\]) are indicated by the horizontal lines. The inverse relaxation times are shown for molar mass of 185 000 g/mol linear at the top (black) and for the respective ring polymers at the bottom (blue). The high-rate data of molar mass of 185 000 g/mol (linear and ring) polymers collapse within experimental uncertainty. The dashed line through the linear polymer data has a slope of $-0.5$ (see text). The dashed line through the ring data represents predictions of the phenomenological model (see text and the Supplemental Material). (Inset) Illustration of the stretched ring comprising a globular head with $N - n$ monomers and two double-folded tails with $n$ monomers (see also Supplemental Material\[24\]). The vertical arrows represent different characteristic times\[24\].
observed for polymer solutions [37] and can be explained by several modified tube models [37]. The monotonic behavior of the extensional viscosity function prompted initially the incorporation of the so-called interchain pressure effect into tube theories [36]. Also, Nielsen et al. [38] have shown that the combination of anisotropic friction with finite chain extensibility leads to \( \dot{\varepsilon}^{-1/2} \) scaling. Lately, the idea of friction reduction in extensional flow was formulated [39,40], a concept that accommodates the difference between entangled melts and solutions [41,42] and describes unentangled linear chain behavior [34]. Ianniruberto and Marrucci [43] considered the balance between frictional and thermal equilibration forces at the onset of stretching and showed that comb polymers exhibit identical behavior with linear polymers in fast extensional flows, provided they have the same equivalent molar mass (i.e., the same Rouse time). To test whether this prediction carries over to rings, we consider a folded ring with half molar mass as the equivalent linear chain. We show in Fig. 3 the extensional viscosity of a linear chain with molar mass 100,000 g/mol along with the ring with molar mass of 185,000 g/mol. It does exhibit thickening, which, however, is much less pronounced (less than a factor of 2 increase with respect to zero-rate viscosity) compared to the ring (factor of 10). The high-rate extensional viscosities of this polymer are clearly below the respective data of the molar mass of 185,000 g/mol polymers, suggesting that this idea may not hold for rings (Figs. 3 and Supplemental Material Fig. S5).

In view of the intriguing overlap of the asymptotic behavior of the ring and linear molar mass of 185,000 g/mol polymers, we rationalize the ring behavior by a simple model where the asymptotic viscosity of the ring and the linear molecule is the same function of the number of monomers. Specifically, we assume that the ring polymer (with \( N \) Kuhn monomers [4]) in extensional flow has the shape of a spherical globule with \( N - n \) monomers and two double-folded tails containing \( n \) Kuhn monomers, as illustrated in Fig. 3. The number of monomers in the undistorted globule is determined by the condition that the reciprocal extensional rate is the relaxation time of this globular part of the ring (head): \( \dot{\varepsilon}^{-1} \approx \tau_{\text{ring}}(N-n) \). The latter is estimated from the fractal loopy globule (FLG) model [4] with \( \tau_{\text{ring}}(N) = \frac{c_0 \tau_m}{(N^{7/3}/N_e^{1/3})} \), where \( c_0 \) is a constant of order unity, \( \tau_m \) corresponds to the monomer relaxation time, and \( N_e \) is the degree of polymerization of the entanglement segment. The total number of Kuhn monomers in the tails is \( n = 0 \) for low extensional rates and \( n = N - N_e^{1/7}(c_0 \tau_m \dot{\varepsilon})^{-3/7} \) for \( \dot{\varepsilon} > \tau_{\text{ring}}(N)/c_0 \).

The extensional viscosity of ring melt is assumed to be the sum of the rate-dependent contributions from the globular head and from the double-folded tails: \( \eta(\dot{\varepsilon}) = \eta_{\text{head}}(\dot{\varepsilon}, N-n) + \eta_{\text{tail}}(\dot{\varepsilon}, n) \). The former is the ring viscosity [4] multiplied by \( 3 \) (Trouton ratio), whereas the latter is equivalent to the extensional viscosity of linear polymers containing \( n \) monomers. Details including fitting of model parameters, the analysis of uniaxial extensional data, and the head-tail ring model, which includes Ref. [26], are presented in the Supplemental Material [24]. Whereas this expression fits the experimental data very well (Fig. 3), its main value lies in the description of the ring unraveling process during extension and its relation to viscosity thickening. It is a rather simplified model, but may provide the ingredients for a deeper analysis of globular to double-folded conformation.

Despite this unique stretching behavior of ring polymers, two subtle points merit further discussion. First, the onset of extension thickening (Fig. 3) occurs at a rate of about \( 3 \times 10^{-3} \) s\(^{-1} \), which corresponds to the inverse terminal time of the ring (\( \tau_{\text{terminal}}^{-1} \), i.e., the frequency where the terminal slope of 2 is reached in \( G' \)). However, it is much slower (by a factor of about 25) than the ring relaxation time based on the FLG model fit to the linear viscoelastic data (\( G_{\text{FLG}} \)) or the experimental ring relaxation time (\( \tau_{\text{ring}} \)) based on the fit of low-frequency moduli with lines having slopes 1 and 2 (by a factor of 7) (see also Figs. S2 and S3 and the Supplemental Material [24]). It is also much slower than the inverse Rouse time of the linear precursor, which marks the onset of its stretching [24,30,38]. This suggests the remarkable sensitivity of ring polymers to elongation.

To this end, we note that recent preliminary molecular dynamics simulations with completely pure rings and their linear counterparts in uniaxial extension suggest that the onset of extensional viscosity thickening is observed at stretch rates well below the inverse ring relaxation time, pointing to a completely different mechanism of stretching [44].

Second, the agreement of the model with the asymptotic viscosity at large rates should not be taken as independent support of the data since it comes from fitting. In fact, if one adopts the picture of ring unraveling into a double-folded structure during extension, one could alternatively expect that at high extensional rates it behaves as a linear chain with half molar mass [43]. However, the data of Fig. 3 indicate that this is not the case. To reconcile these two subtle points, the conformational changes of the ring during the unraveling processes should be addressed. It is also worth considering the possible role of linear contaminants on both the onset of thickening and high-rate thinning, something that could be tested with simulations.

Resolving the above delicate issues represents the remaining grand challenge and calls for further investigations using rheo-small-angle neutron scattering, stress relaxation after cessation of uniaxial extension, and molecular dynamics simulations [44]. Nevertheless, it is now established that rings exhibit unique stretching behavior and can serve to tailor the flow of polymeric materials through their extreme sensitivity to extensional flow.
While the behavior of nonconcatenated entangled rings near equilibrium is well documented after extensive studies, their transient strain hardening along with their strong viscosity thickening and linear polymerlike thinning behavior in strong extensional flow at very low and high rates, respectively, are suggestive of processes for polymeric extension and also novel applications. Polymer processing involves extensional deformation; hence the present results shed light on the fascinating flow properties of polymeric loops, while advancing the state of the art in polymer physics. More importantly, a new route opens for using this dual dynamic nature of rings in the design of composites with tunable properties (e.g., elastomers with controlled rolling resistance) or understanding the response of folded proteins and chromosome territories under strong external fields. Finally, uniaxial extensional rheology emerges as a highly sensitive tool in polymer physics for diagnosing effects of macromolecular architecture under nonlinear response.

Support by the Aage og Johanne Louis-Hansen Foundation is gratefully acknowledged. We thank G. Ianniruberto and G. Marrucci for helpful discussions. The photograph of the stretched polymer was taken by Klaus Holsting. M. R. acknowledges financial support from National Science Foundation under Grants No. DMR-1121107 and No. EFMA-1830957, the National Institutes of Health under Grants No. P01-HL108808, No. R01-HL136961, and No. 5UH3HL123645, and the Cystic Fibrosis Foundation.

[24] See Supplemental Material at http://link.aps.org/supplemental/10.1103/PhysRevLett.122.208001 for the various characteristic relaxation times listed in Table S1, which includes Ref. [25], and the analysis of uniaxial extensional data and the head-tail ring model, which includes Ref. [26].


