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Robust model for estimating pumping station characteristics and sewer flows from standard pumping station data

Martin FENCL^{1,2*}, Morten GRUM³, Morten BORUP¹, AND Peter Steen MIKKELSEN¹

¹*Technical University of Denmark, Department of Environmental Engineering (DTU Environment), Urban Water Systems Section, 2800 Kgs. Lyngby, Denmark*

²*Czech Technical University in Prague, Department of Hydraulics and Hydrology, 166 29 Prague 6, Czech Republic*

³*WaterZerv, Copenhagen, Denmark*

**Corresponding author*

E-mail: martin.fencl@cvut.cz

ABSTRACT

Flow data represent crucial input for reliable diagnostics of sewer functions and identification of potential problems such as unwanted inflow and infiltration. Flow estimates from pumping stations, which are an integral part of most separate sewer systems, might help in this regard. A robust model and an associated optimization procedure is proposed for estimating inflow to a pumping station using only registered water levels in the pump sump and power consumption. The model was successfully tested on one month of data from a single upstream station. The model is suitable for identification of pump capacity and volume thresholds for switching the pump on and off. These are parameters which are required for flow estimation during periods with high inflows or during periods with flow conditions triggering pump switching on and off at frequencies close to the temporal resolution of monitored data. The model is, however, sensitive within the transition states between emptying and filling to observation errors in volume and on inflow/outflow variability.

KEYWORDS

Flow estimation, pumping station, level data, power consumption, urban hydrology.

INTRODUCTION

An efficient planning and evaluation of rehabilitation/replacement actions in sewer systems requires long-term flow data (Staufer et al., 2012), however, such data is often not available as flow monitoring is challenging and often costly in the harsh conditions occurring in sewers. Level sensors are more wide-spread in the systems, since they are cheaper and require less maintenance. For this reason, flow is often computed indirectly from level observations at e.g. overflow structures where the local hydraulic properties of the system allow for it (Ahm et al., 2016; Borup et al., 2016; Isel et al., 2014). Level sensors are also usually installed in pumping stations, and using data from these to compute reliable flow estimates will potentially facilitate better analysis and control of sewer systems (Carstensen et al., 1996; Löwe et al., 2016). Pumping stations consist of a pump sump (wet well) that collects wastewater inflow and a pump. The pumping is especially by smaller systems controlled by simple control rules. The pump switches on when the pump sump is filled to some predefined level and then switches off again when the pump sump has been emptied. Pumping stations are often equipped with two (or more) pumps. This enables to increase the pump capacity during higher

50 inflow rates and it increases the life span of the system as pumps usually alternate after each
51 pumping cycle during low-flow conditions. The pump redundancy also enables maintaining
52 one pump while operating the pumping station with a second pump and increases the
53 resilience of the whole system against complete failure.

54

55 Pump sumps are usually equipped with level gauges which measure water level in the pump
56 sump. Furthermore, the electrical power consumption of the pump is measured. These data
57 are primarily intended for pumping control and diagnostics and can be accessed through a
58 SCADA system (Olsson et al., 2005). They also represent valuable sources of proxy flow
59 data, as the average inflow into the pump sump within the time step Δt can be estimated as:

60

$$61 \quad Q_{in} = (\Delta V(h) + Q_p * T_p) / \Delta t \quad (1)$$

62

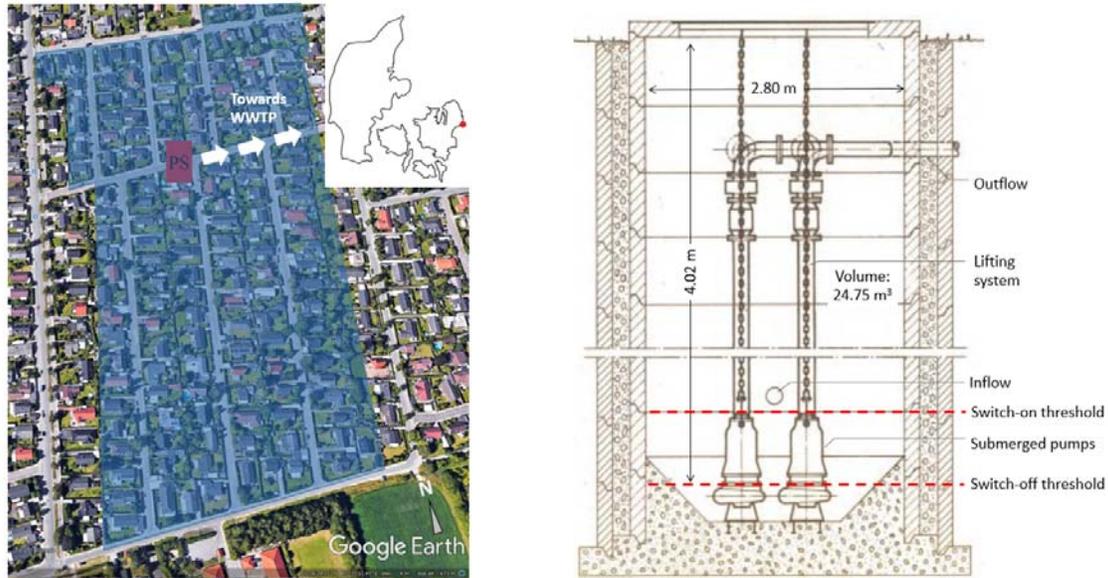
63 where ΔV is the change of water volume in the pump sump, which is a function of measured
64 water level h given by the pump sump geometry, Q_p is the pump capacity and T_p is the
65 duration of pumping (time when the pump is on). However, pumping stations are not
66 primarily optimized for flow monitoring and data is often collected with insufficient temporal
67 resolution. Thus, exact times of pumping are often unknown as well as the exact pump
68 capacity and control rules which govern the switching of the pump on and off. This causes
69 uncertainties in inflow estimation during high flow rates when the pump is constantly running
70 for a long period or during flow conditions triggering pump switching on and off at
71 frequencies close to the temporal resolution of monitored data. Independent flow observations
72 would obviously be beneficial, but such data redundancy is very rare in the water sector, and
73 making use of whatever non-ideal data from pumping stations that is available can be a first
74 step before further investments in data acquisition for flow estimation are made.

75

76 In this article, we suggest a pumping station inflow model with pump capacity and control
77 rules as model parameters (we further refer to these parameters as pumping station
78 characteristics). Furthermore, we propose a procedure to fit the model using pumping station
79 data only. This enables us to estimate the pump capacity as well as the control rules, i.e.
80 parameters needed for reliable pump sump inflow estimation during periods with high flows.
81 The proposed methodology in its current form assumes constant pump capacity and is
82 therefore only suitable for pump sumps where the pump capacity can be regarded as being
83 independent from the water level in the pump sump.

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Figure 1. Subcatchment of the pumping station (left) and layout and geometry of the pumping station (right) with depicted level thresholds for switching the pump on and off.

91 MATERIAL AND METHODS

92 Taarnby catchment – data specification

93 The pumping station used in this study is a part of a combined sewer system in a small urban
94 catchment located in the coastal town Taarnby, Denmark (Fig. 1, left) and characterized by
95 flat terrain with altitudes not exceeding 10 m above sea level. The pumping station serves a
96 subcatchment with approx. 400 inhabitants and a pipe length of about 2 km. The volume of
97 the pump sump is 24 m³, but it is mostly operated within the approximate range 2-5 m³(Fig. 1,
98 right). The pumping station has a duplex pumping system with two pumps each having a
99 nominal pump capacity 9 l/s. The pumps alternate after each pumping cycle during dry
100 weather flows and run simultaneously when the inflow rate into the pump sump exceeds the
101 capacity of a single pump. In this investigation, we concentrate on dry weather flows and do
102 not distinguish between the two pumps, implicitly assuming the pumps have the same
103 characteristics.

104

105 The exact pumping capacity and level resp. volume thresholds for switching the pump on and
106 off are unknown. Level data and electrical power consumption data are sampled at irregular
107 time steps of $\Delta t \approx 5$ min. One month of observations from May to June 2017 is used for this
108 study. This period was characterised by dry weather with only very few light rain events.

109

110 Pumping station inflow model

111 The pumping station inflow model should be capable of estimating flow from pump sump
112 data during both filling (no pumping) and emptying periods (pumping). Fig. 2 (left) shows a
113 time series of volume and electrical power consumption observations during dry weather. The
114 pump sump is being filled for about 5 time steps (≈ 25 min) and emptied within one or two
115 time steps (5-7 min). A positive electrical power consumption I indicates times when the
116 pump is on. The state of the pump between these records is however not known and the exact
117 time of pumping is thus unknown as well. For example, the first pumping on the figure could
118 last only five minutes from 18:30 to 18:35, but also almost 15 minutes from any time after
119 18:25 (last record with no pumping) to any time before 18:40 (first record with no pumping).

120 We combine the electric power consumption data (I) and volume data (V) from consecutive
 121 time steps k and $k-1$ to estimate the exact pumping times. For this, four pump states (A-D) are
 122 defined (Fig. 2):

123

124 A: pump sump filling: $I_{k-1} = I_k = 0$

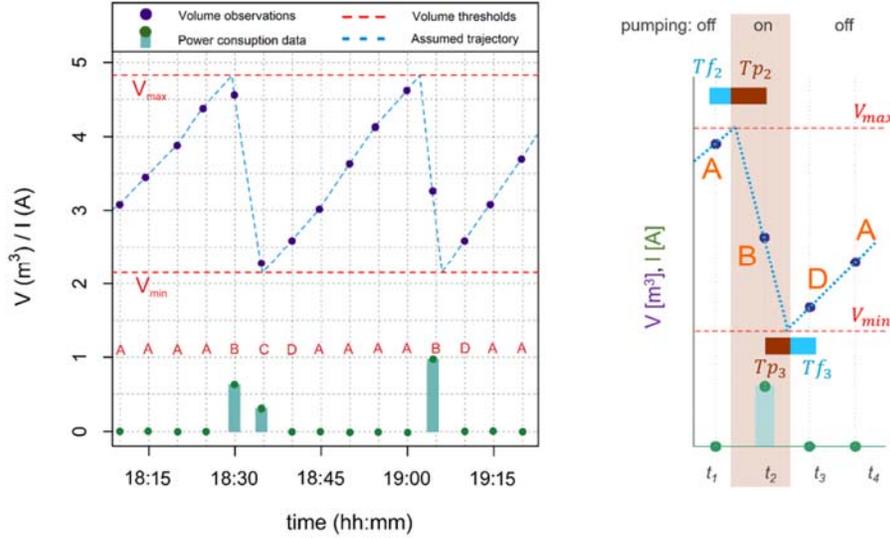
125 B: transition between filling and emptying period: $I_{k-1} = 0 \wedge I_k > 0$

126 C: pump sump emptying: $I_{k-1} > 0 \wedge I_k > 0$

127 D: transition between emptying and filling period: $I_{k-1} > 0 \wedge I_k = 0$

128

129



130

131 **Figure 2.** Left: Volume and power consumption data obtained from the most upstream
 132 pumping station in the Taarnby catchment. Red labels above power consumption records
 133 denote pump states A-D. Blue, dashed lines were added manually to the figure to indicate
 134 differences between continuous and discrete volume time series sampled at raw resolution.
 135 Right: Theoretical model for estimating exact pumping times as described by equations (2-5).

136

137

138 The pumping times (Tp) within state A equal zero and within state C equal the time step size
 139 Δt . The pumping times within state B are estimated from volume data assuming constant
 140 inflow Q_{in_k} during the time step Δt_k (Fig. 2, right). The period before the threshold V_{max} is
 141 reached (Tf_k) and the period the pump is on (Tp_k) can then be expressed as follows:

142

$$143 \quad Tf_k = (V_{max} - V_{k-1})/Q_{in_k} \quad (2)$$

$$144 \quad Tp_k = (V_{max} - V_k)/(Qp - Q_{in_k}) \quad (3)$$

145

146 where V_{k-1} is the last volume record when the pump was off, V_k the first record with pump
 147 being on and thus labelled as B, and Qp is the pump capacity.

148

149 Similarly, the pumping time during state D is estimated by expressing the period during
 150 pumping (Tp_k) and after it has stopped (Tf_k) using the volume threshold V_{min} :

151

$$152 \quad Tp_k = (V_{k-1} - V_{min})/(Qp - Q_{in_k}) \quad (4)$$

$$153 \quad Tf_k = (V_k - V_{min})/Q_{in_k} \quad (5)$$

154

155

Parameter estimation

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163

The pump capacity Q_p and volume thresholds V_{max} and V_{min} are regarded as model parameters and are considered constant. The model assumption of constant pump capacity is a simplification which is further discussed in the discussion section. The model is fitted to the inflow Q_{inA} estimated during state A using eq. (1) and considered constant during subsequent states B-D. The assumption of constant inflow is discussed in the Discussion section. The three parameters are optimized separately. The pump capacity Q_p is optimized by minimizing the cost function L_{Qp} :

164

$$L_{Qp} = \sum_{k \in C} |Q_{inA_k} - Q_{inC_k}| \quad (6)$$

165

166

167

168

where Q_{inC} is the inflow estimated from eq. (1) during the state C. The V_{max} threshold is optimized for state B by minimizing the cost function L_{Vmax} :

169

$$L_{Vmax} = \sum_{k \in B} |\widehat{\Delta t}_k - \widetilde{\Delta t}_k| \quad (7)$$

170

171

172

173

where $\widehat{\Delta t}_k$ is the observed duration of time step k , i.e. the time difference between two consecutive records, and $\widetilde{\Delta t}_k$ is the duration of time step k estimated as:

174

$$\widehat{\Delta t}_k = Tp_k + Tf_k \quad (8)$$

175

176

177

178

where Tp_k and Tf_k are obtained from eqs. (2) and (3). The V_{min} threshold is optimized similarly as for V_{max} by minimizing the cost function L_{Vmin} defined for state D:

179

$$L_{Vmin} = \sum_{k \in D} |\widehat{\Delta t}_k - \widetilde{\Delta t}_k| \quad (9)$$

180

181

182

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184

185

where $\widehat{\Delta t}_k$ is calculated according to eq. (8) using Tp_k and Tf_k obtained from (4) and (5). The optimization is performed by a combination of *golden section search* and *successive parabolic interpolation* (Brent, 1973) implemented in the `optimize()` function available within the statistical computing language R (R Core Team, 2017).

186

Performance evaluation

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The exact values of pump capacity and volume thresholds are unknown and we, unfortunately, do not have independent observations of water levels and in-/out-flows to check these values. This is however a common situation for many pumping stations, and the developed estimation procedure thus has great practical value. The correctness of the suggested procedure is therefore checked indirectly. First, the proposed model is fitted to the whole dataset and the parameter space of the model is inspected to verify if it converges to well-defined minima. Second, the estimated pump capacity is compared to its nominal value and the V_{max} and V_{min} thresholds, which are completely unknown, are compared to all observed water volumes at the beginning of the transition states B and D, respectively. If the volume thresholds are identified reliably, most of the observed volumes should fall into the range bounded by V_{min} and V_{max} . Third, the total volume of inflow during the whole observation period is compared to the total outflow (pumped) volume. The inflow volume (V_{in}) is calculated as:

201

$$V_{in} = \sum_{k \in \{A,B,C,D\}} (Q_{inA_k} * \widehat{\Delta t}_k) \quad (10)$$

202

203 where Q_{inA} is calculated directly according to eq. (1) for time steps without pumping (A), and
 204 during pumping (B, C, D) is considered the same as the last value of Q_{inA} before pumping.
 205 The outflow (pumped) volume (V_p) is calculated from the estimated pump capacity Q_p and
 206 pumping times T_p :

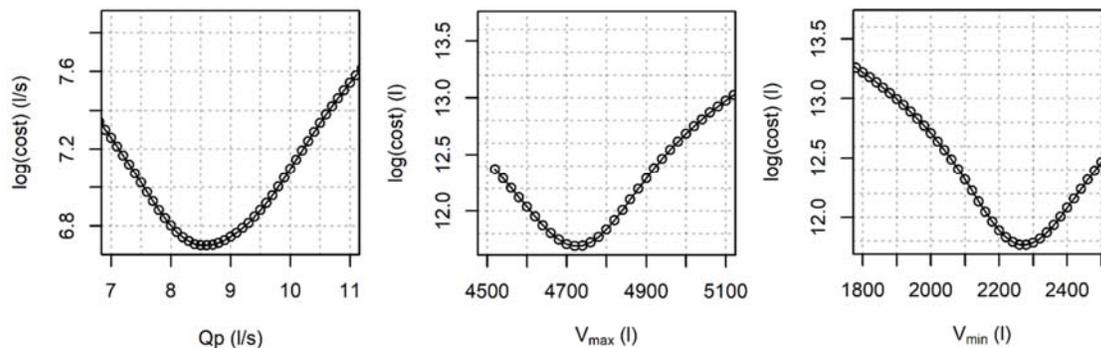
$$207$$

$$208 \quad V_p = \sum_{k \in \{B, C, D\}} (Q_p * T_{p_k}) \quad (11)$$

209
 210 Finally, the pumping model is fitted separately for daily subsets of data ($n = 31$) to investigate
 211 the robustness and stationarity of the model parameters when optimized under different flow
 212 conditions.
 213

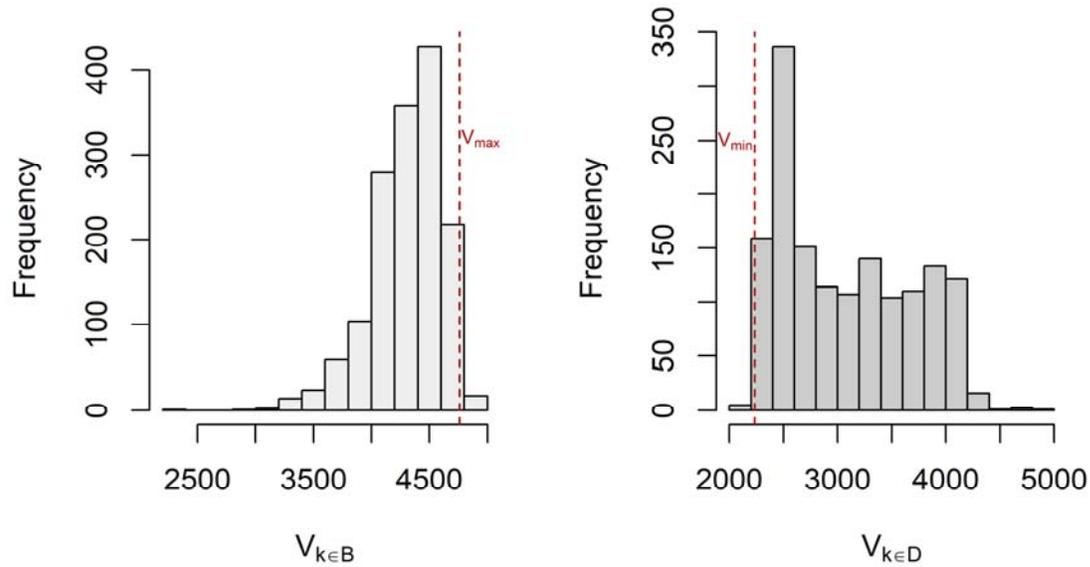
214 RESULTS

215 The model was first optimized for the whole experimental period. Fig. 3 shows the parameter
 216 space of pump capacity Q_p evaluated for states C and volume thresholds V_{max} and V_{min}
 217 evaluated for states B and D. All the parameters converge to well-defined minima.
 218



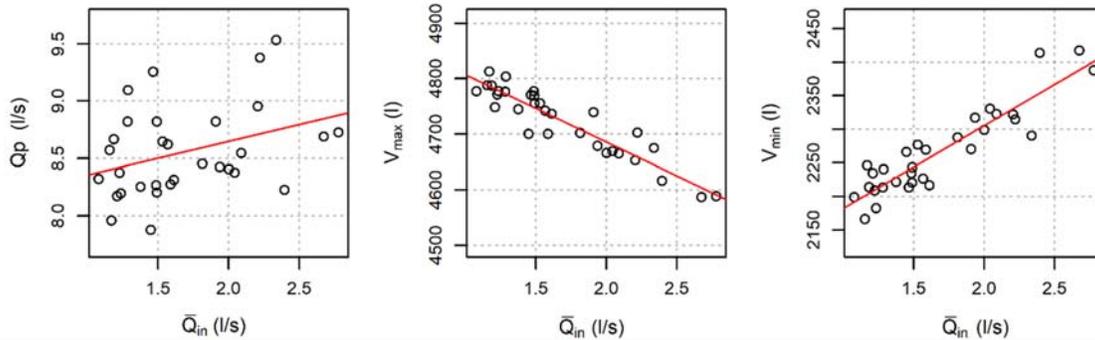
219
 220 **Figure 3.** Cost functions of all three model parameters exhibit clear minima.
 221

222 The optimal value for pump capacity was found to be 8.6 l/s, which is close to the nominal
 223 pump capacity. The maximal and minimal volume thresholds for switching the pump on and
 224 off were found to be 4.72 m³ and 2.27 m³. The volumes observed at the beginning of
 225 transition time steps classified as B (i.e. during which pumping started) and D (i.e. during
 226 which pumping stopped) are shown on Fig. 4. The V_{max} threshold corresponds to the 95.4%
 227 quantile of observed volumes for state B and the V_{min} threshold to the 1.7% quantile for state
 228 D, i.e. 4.6% of the state B observations are higher than V_{max} and 1.7% of the state D
 229 observations are lower than V_{min} . The records outside of the range given by thresholds are,
 230 however, close to the thresholds and may thus be explained either by inaccuracy of the level
 231 control floats switching the pump on and off, or by observation errors. The maximal volume
 232 observed (4.86 m³) corresponds to a water level 2.2 cm above the estimated V_{max} threshold
 233 and the minimal observed volume (2.16 m³) corresponds to a water level 1.7 cm below the
 234 estimated V_{min} threshold.



235
236 **Figure 4.** Observed volumes at the beginning of the transition time step during which the
237 pump switches on (left, state B) and off (right, state D).
238

239 The total inflow volume V_{in} is 4867 m³, and the pumped volume V_p is 4957 m³, i.e. 1.8%
240 higher. The pumped volume estimated without the pumping model (eqs. 2-5) is 5731 m³, i.e.
241 17.7% larger than V_{in} . The close match of V_{in} and V_p indicates that the suggested model and
242 optimization procedure is conceptually correct and improve the description of the pumping
243 process when pumping data have low temporal resolution.



244
245 **Figure 5.** Pump capacity (left) and volume thresholds (centre, right) found for daily subsets
246 and compared to average daily inflows. Linear trend lines show relations between average
247 daily inflows (\bar{Q}_{in}) and the estimated parameter values.
248

249 The parameter obtained for daily subsets vary noticeably although their mean is almost
250 identical with the parameter values obtained for the whole dataset (difference does not exceed
251 0.1 %). The standard deviation in pump capacity (Q_p) is 0.39 l/s, and in V_{max} as well as in V_{min}
252 it is 0.06 m³. The magnitude of the estimated parameters is clearly dependent on the inflow
253 rates estimated for daily data subsets (Fig. 5). The link between the mean daily inflow and the
254 pump capacity is relatively mild (Pearson's $r = 0.35$), whereas the V_{max} and V_{min} magnitudes
255 are strongly linked to daily inflows having Pearson's correlation coefficients 0.91 and -0.93,
256 respectively. The dependence of the estimated parameters on the average inflows may partly
257 reflect the behaviour of the real system, but it is more likely due to estimation procedure and
258 the assumptions behind it, such as the constant pumping rate.
259

260 DISCUSSION

261 The suggested procedure is suitable for estimating pumping station characteristics, however
262 inflows estimated during states B and D are sensitive to the observation errors in volume, the
263 inflow variability and also the possible outflow (pumping rate) variability. The violation of
264 the assumption of constant inflow and constant pumping rate during emptying periods does
265 however not substantially influence the estimated pumping station characteristics when the
266 variability in inflow/outflow is random.

267
268 The variability of inflows is random in case of upstream pumps, nevertheless our further
269 investigations (not presented here) revealed that this does not always hold for downstream
270 pumps. In the specific case where downstream pumping is triggered by short pulses of high
271 flows from upstream pumps, the inflow rates during the last time step before pumping can be
272 substantially larger than the average inflow rates during pumping. Such systematic deviation
273 then influences the estimated pump capacity and thus makes the estimated flows more
274 uncertain. To take such effects into account the model would have to be extended. A
275 probabilistic formulation of inflow might improve the results as demonstrated e.g. by
276 (Leonhardt et al., 2014) on a combined sewer overflow structure with a storage tank.
277 Reformulating the model into a stochastic grey-box (state space) model (Juhl et al., 2016)
278 may be another feasible approach to describe uncertainties in inflow.

279
280 The violation of the assumption of constant pump capacity may systematically influence the
281 parameter estimates. The pump capacity in reality depends also on the total hydraulic head,
282 which is lower for higher water levels. The difference in water levels for the V_{min} and V_{max}
283 thresholds is in our case only approx. 40 cm, nevertheless, pressure heads for pumping
284 stations in flat terrains are typically only a few meters and thus even relatively small change
285 in hydraulic head may influence the pump capacity noticeably. The pump capacity is
286 estimated for state C during which the water levels are lower than during state B and on the
287 other hand higher than during state D. The underestimated pump capacity during state B
288 results in an overestimated V_{max} threshold. This overestimation is more pronounced during
289 periods of higher inflow rates where emptying of the pump sump is slower and thus water
290 levels at the end of state B are on average higher than during periods of lower inflow rates. In
291 contrast, overestimation of the pump capacity during state D results in underestimation of V_{min}
292 threshold and this underestimation is more pronounced for lower inflow rates. This could
293 explain the strong link between the estimated V_{min} and V_{max} thresholds and the average daily
294 inflow rates. The extension of the model to consider pump pressure head, as e.g. (Carstensen
295 and Harremoës, 1999) did in their model of a storage tunnel, may further improve the
296 description of pumping and thus also the reliability of the estimated pumping station
297 characteristics and the estimated inflows. Such extension will, however, require data of higher
298 temporal resolution to be able to identify further parameters describing the relation between
299 pump capacity and water level in the pump sump.

300
301 The absence of independent flow measurements does not enable us to draw conclusion on the
302 exact accuracy of the proposed method. The indirect evaluation of the model including the
303 estimated pumping station characteristics using the inflow/outflow balance is here based on
304 estimated pumping times and pump capacity. Total pumping times are often monitored
305 together with the total electrical consumption for the purpose of pump diagnosis and might
306 therefore also be used for indirect evaluation of a model like the one proposed here. We did
307 not, however, have access to such data for the current study.

308

309 Leaky or defect non-return valves is a frequently occurring phenomenon in pump sumps and
310 this can result in a substantial amount of pumped water flowing back into the pump sump
311 after a pumping cycle. This does not affect the proposed methods' ability to estimate pump
312 sump characteristics, since the method does not distinguish between the sources of inflowing
313 water. It does, however, affect the interpretation of the inflow time series obtained using the
314 method since the estimated inflow in that case represents both return flow and water entering
315 the right way into the pump sump.

316

317 Further work on validating the method and extending it to pumping stations in series may
318 benefit from an improved data set including (i) total pumping time and electricity
319 consumption for each of the two pumps in a pumping station, (ii) level and electrical power
320 consumption data recorded at a sufficiently high resolution to identify the pump switching
321 more exactly as well as any systematically increased flows just after pumping that may
322 indicate defect non-return valves, and (iii) direct flow observations allowing the results to be
323 independently confirmed.

324

325 CONCLUSIONS

326 A model for inflows to pumping stations was proposed and an optimization procedure was
327 suggested to estimate the pump capacity and volume thresholds for switching the pump on
328 and off. The model also enables to estimate timing of the pump switching, which is often
329 unknown due to suboptimal sampling frequency of water level and electrical power
330 consumption data. This enables us to identify more exactly duration of the pumping in each
331 pumping cycle. Furthermore, a way of evaluating the performance of the model without
332 independent flow observations was suggested. The model performance was successfully
333 tested on one month of data from a pumping station operated within a small urban catchment
334 with a separate sewer system in Taarnby, Denmark.

335

336 The model is suitable for estimating characteristics of upstream pumping stations which are
337 not systematically influenced by inflow pulses from upstream pumping. Estimation of
338 pumping station characteristics is valuable for pumping diagnostics. Reliable identification of
339 pump sump capacity is also valuable for estimating inflows into pump sumps during periods
340 with high flow rates when the pump is on for a long period. The model is, however, sensitive
341 within the transition states between emptying and filling to observation errors in volume and
342 on inflow/outflow variability. This sensitivity does not substantially influence the estimation
343 of pumping station characteristics when the variability in inflow/outflow is random. The inflow
344 variability can be considered random for upstream pumping stations, however, the model will
345 require explicit consideration of upstream inflow pulses to be applicable also for downstream
346 pumps. Further development will concentrate on considering a variable hydraulic head and a
347 robust quantification of errors affecting the inflow estimation.

348

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355

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