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ALES+: Adapting a homogenous ocean retracker for satellite altimetry to sea ice leads, coastal and inland waters.

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Abstract

Water level from sea ice-covered oceans is particularly challenging to retrieve with satellite radar altimeters due to the different shapes assumed by the returned signal compared with the standard open ocean waveforms. Valid measurements are scarce in large areas of the Arctic and Antarctic Oceans, because sea level can only be estimated in the openings in the sea ice (leads and polynyas). Similar signal-related problems affect also measurements in coastal and inland waters.

This study presents a fitting (also called retracking) strategy (ALES+) based on a subwaveform retracker that is able to adapt the fitting of the signal depending on the sea state and on the slope of its trailing edge. The algorithm modifies the existing Adaptive Leading Edge Subwaveform retracker originally designed for coastal waters, and is applied to Envisat and ERS-2 missions.

The validation in a test area of the Arctic Ocean demonstrates that the presented strategy is more precise than the dedicated ocean and sea ice retrackers available in the mission products. It decreases the retracking open ocean noise by over 1 cm with respect to the standard ocean retracker and is more precise by over 1 cm with respect to the standard sea ice retracker used for fitting specular echoes. Compared to an existing open ocean altimetry dataset, the presented strategy increases the number of sea level retrievals in the sea ice-covered area and the correlation with a local tide gauge. Further tests against in-situ data show that also the quality of coastal retrievals increases compared to

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the standard ocean product in the last 6 km within the coast.

ALES+ improves the sea level determination at high latitudes and is adapted to fit reflections from any water surface. If used in the open ocean and in the coastal zone, it improves the current official products based on ocean retracers. First results in the inland waters show that the correlation between water heights from ALES+ and from in-situ measurement is always over 0.95.

Keywords: Satellite Altimetry, retracking, subwaveform retracker, validation, tide gauge, Leads, Arctic Ocean, ALES;

1. Introduction

1 Sea level is an Essential Climate Variable (ECV) regarded as one of the main indi-
2 cators of climate variability (Cazenave et al., 2014). For more than 25 years, traditional
3 measurements obtained by means of in-situ pressure gauges have been supported by the
4 repeated global remotely sensed estimations from the radar signals registered onboard
5 satellite altimeters. This has led to significant advancements in our knowledge of the
6 seasonal and interannual sea level fluctuations (Vinogradov & Ponte, 2010; Ablain et al.,
7 2016), of the regional distribution of trends in a changing climate (Palanisamy et al.,
8 2015) and of the mid to large scales of geostrophic circulation (Pascual et al., 2006).

9 The basic concept of this remote sensing technique considers the sea surface height
10 (SSH) as the difference between the height of the satellite referenced to the earth ellipsoid
11 and the distance (range) between the satellite centre of mass and the mean reflecting
12 surface. The SSH has then to be corrected for instrumental, atmospheric and geophysical
13 effects. For a full description of the corrections the reader is referred to Fu & Cazenave
14 (2001). The progress of satellite altimetry has been fostered by the developments in orbit
15 determination (Rudenko et al., 2014), in the corrections (Handoko et al., 2017) and in
16 the range retrieval, based on the fitting of a functional form to the received signal in a
17 procedure called retracking (Cipollini et al., 2017).

18 The processing of the echoes sent by pulse-limited radar altimeters (i.e. every radar
19 altimeter before the launch of CryoSat-2 in April 2010 and, more recently, Sentinel-3A) is
20 well known in the open ocean, where the shape of the received signal resembles the Brown-
21 Hayne (BH) model (Brown, 1977; Hayne, 1980) perturbed by Rayleigh noise (Quarty
22 et al., 2001), characterised by a steep leading edge and a slowly decaying trailing edge.

23 Departures of the received signal (also called 'waveform', a sampled time series whose
24 resolution cell is called 'gate') from the BH shape are instead found in the presence of
25 sea ice and in the proximity of land (i.e. both in coastal and inland waters) (Boergens
26 et al., 2016; Laxon, 1994b). The common feature is the presence of the so-called 'bright
27 targets' or 'hyperbolic targets': points with a higher backscatter coefficient that perturb
28 the expected shape travelling along the trailing edge as they appear in the illuminated
29 area, eventually constituting the main leading edge.

30 These retracking issues, together with the degradation of some corrections in the same
31 areas, have been a major impediment in expanding our knowledge of sea level variability
32 in the coastal ocean and in the Arctic Ocean. These are regions of primary importance,
33 since a growing number of people and infrastructures are located at the coast (Neumann
34 et al., 2015) and since changes in the Arctic Ocean dynamics significantly affect the global
35 climate (Marshall et al., 2014).

36 This study is motivated by the need of increasing the quality and the quantity of sea
37 level retrievals in the Arctic Ocean. It focuses on a retracking procedure that is able
38 to retrieve the ranges of pulse-limited radar altimeters reflected from the leads (water
39 apertures in sea ice) while improving the retracking in open and coastal ocean as well.
40 Given the similarities of the problem, we aim also at demonstrating the validity of this
41 strategy for the retrieval of water level in inland waters. The result is the definition of a
42 single algorithm that is able to adapt the estimation to any kind of water returns.

43 Here, our efforts are aimed at improving the times series for 1995-2010 by fitting the
44 signals from the altimeters on two European Space Agency (ESA) missions: ERS-2 and
45 Envisat, which have occupied the same ground tracks of a 35-day repeat cycle between
46 latitudes 82° S and 82° N.

47 Previous and on-going studies share the objective of improving the quality of satellite
48 altimetry at high latitudes. Giles et al. (2007) applied a dedicated empirical functional
49 form to lead waveforms, separating the typical peaky shape into a Gaussian and an
50 exponential function. For the open water points though, they used the standard product,
51 which adopts the BH fitting. The use of heterogenous retrackers leads to a significant
52 bias, which was quantified in 15 ± 11 cm. Two different retrackers for ocean and leads
53 and a consequent bias adjustment were also the choice of Peacock & Laxon (2004).
54 More recently, Cheng et al. (2015) edited the Envisat data from the Radar Altimetry

55 Database System (RADS) without applying a specific retracker, while Poisson et al.
56 (2017) (personal communication) are also aiming at a homogenous retracking strategy,
57 as this paper, by using the modified BH proposed by Jackson et al. (1992), in which the
58 peakiness of the waveform is modelled by a surface roughness parameter.

59 Our starting point is the Adaptive Leading Edge Subwaveform (ALES) retracker by
60 Passaro et al. (2014), which is based on a BH fitting of a portion of the echo in order
61 to avoid bright targets on the trailing edge of the waveforms. The ALES-reprocessed
62 altimetry data have already been validated against in-situ measurements from tide gauges
63 (TGs) and used for coastal sea level variability studies (Passaro et al., 2015a, 2016). The
64 potential for the application to peaky echoes was already identified in a paper by Passaro
65 et al. (2015b), where ALES was applied on the tidal flats in the German Bight, whose
66 still waters produce returns analogous to lead echoes. Here, we develop a new version
67 of the algorithm (ALES+) to improve the fitting of the peaky waveforms and abate the
68 noise in the open ocean compared to the standard processing.

69 In the framework of the ESA Sea Level Climate Change Initiative (SL CCI), ALES+
70 will be the retracker of choice for Envisat and ERS-2 missions in the DTU/TUM high
71 latitude sea level product (Rose et al., in preparation). Therefore, the main part of this
72 paper is dedicated to the description and validation of the ALES+ solution in a test zone
73 of the Arctic Ocean. We also evaluate the performances at the coast and in the inland
74 waters, in order to exploit ALES+ as a homogenous retracker solution for any kind of
75 water surfaces.

76 The dataset and the areas of study are defined in Section 2; The ALES+ procedure
77 and the methodologies followed to identify leads among the sea ice are described in Section
78 3; validation and discussion follow in Section 4, while Section 5 derives the conclusions.

79 **2. Areas of Study and Datasets**

80 *2.1. Areas of Study*

81 As a main area of study the surroundings of the Svalbard Islands (the Svalbard test
82 area, latitude limits: $78 - 82^{\circ}N$, longitude limits: $0 - 20^{\circ}E$) are chosen, in order to
83 validate ALES+ in the sea ice and in the open ocean. This geographical box presents
84 both constant open water and sea ice. The presence of a TG, which is very rare at such
85 latitudes, also allows a validation in areas that are seasonally covered by sea ice. Figure

86 1 (a) shows the minimum (September 2007) and maximum (February 1998) extent of the
87 sea ice during the period considered in this study, provided by the Sea Ice Index Data
88 and Image Archive at NSIDC (Fetterer et al., 2016) and is given as a monthly sea ice
89 extent polygon. Also the TG Ny Ålesund used in the validation is shown in Figure 1 (a).

90 To validate ALES+ as a coastal retracker, the coastal waters of a region in the North-
91 East Atlantic Ocean within 70 km of the coast are considered, due to the availability of
92 local TG data with high temporal resolution. Figure 1 (b) displays the TGs used in the
93 study and highlights in red the analysed segments of the altimetry tracks.

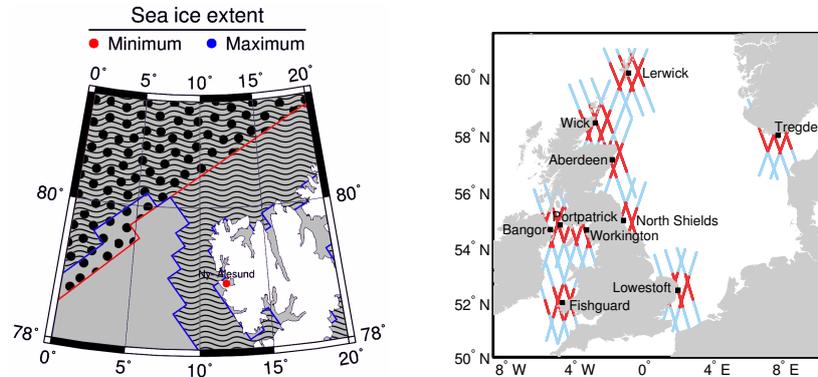
94 Finally, the Mekong River is taken as example of an inland water application in order
95 to allow the comparison with previous studies that exploit the synergy between altimetry
96 and in-situ stations, which are shown in Figure 1 (c).

97 *2.2. Satellite Altimetry Data*

98 The waveforms and all the additional information needed to apply the ALES+ al-
99 gorithm are taken from the ESA Sensor Geophysical Data Records (SGDR) of ERS-2
100 REAPER (Femenias et al., 2014) and Envisat version 2.1. For Envisat the entire dura-
101 tion of the phase 2 (May 2002 - October 2010) is considered; for ERS-2 the REAPER
102 data cover the period from September 1995 to July 2003. The RADS altimetry database
103 (<http://rads.tudelft.nl/>) with its default settings is used to provide an alternative sea
104 level anomaly (SLA, see Section 3.3) product for comparisons..

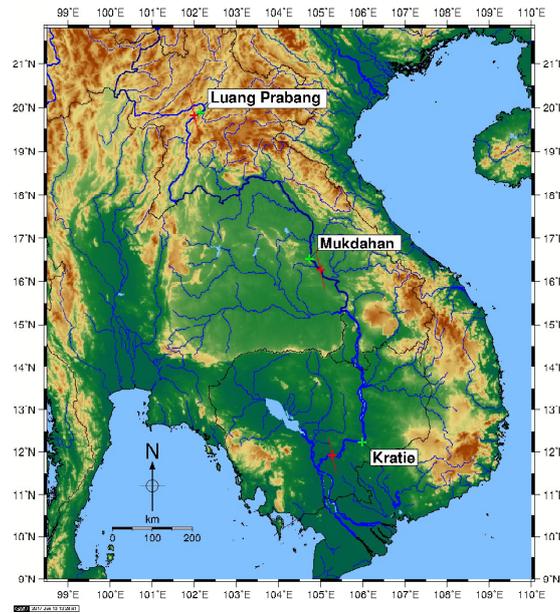
105 *2.3. In-situ Data*

106 In the sea ice region Revised Local Reference (RLR) TG data of the Ny Ålesund sta-
107 tion are downloaded as monthly averages from the Permanent Service for Mean Sea Level
108 (PSMSL) at <http://www.psmsl.org/data/obtaining/stations/1421.php>. In the coastal re-
109 gion TG records were obtained from the UK National Tide Gauge Network archives at
110 the British Oceanographic Data Centre (BODC) and the University of Hawaii Sea Level
111 Center (UHSLC). The temporal resolution of the sea level data is 15 minutes for records
112 stored at the BODC and 1 hour for those stored at the UHSLC. Here, we use a set of 10
113 TGs with nearly continuous records of sea level over the period 1995-2010, which have
114 been visually inspected for shifts and outliers. In the Mekong river, telemetric gauge data
115 is provided by the Mekong River Commission (MRC, <http://ffw.mrcmekong.org/>). The
116 latter has a daily resolution, but no absolute height reference.



(a)

(b)



(c)

Figure 1: (a) The Svalbard test area in the Arctic Ocean. The dotted area with red border is the minimum sea ice cover, while the wavy area with blue border is the maximum. The red dot indicates the location of the Ny Ålesund TG used for validation. (b and c) Location of the TGs used for coastal and inland waters validation and (red) along-track extension of nominal Envisat and ERS-2 tracks used for comparison with in-situ data.

117 This kind of in-situ data are widely used by the Scientific Community as valida-
 118 tion means. All types of TG (acoustic, pressure, float, and radar) can measure sea-
 119 level variations with an accuracy of at least 1 cm (see the IOC Manual on Sea Level at
 120 http://www.psmsl.org/train_and_info/training/manuals), which is significantly bet-
 121 ter than the accuracy achieved by altimeters. Telemetric river monitoring system is con-
 122 sidered to reach a mm accuracy (see [http://www.radio-data-networks.com/products/](http://www.radio-data-networks.com/products/flooding/radar-based-river-level-monitoring-telemetry/)
 123 [flooding/radar-based-river-level-monitoring-telemetry/](http://www.radio-data-networks.com/products/flooding/radar-based-river-level-monitoring-telemetry/))

124 3. Methodology

125 3.1. ALES+ Retracker

126 3.1.1. The Brown-Hayne model

127 ALES+ inherits the functional form used to fit the waveforms from the BH model.
 128 In order to clarify the terminology in use, we report here the corresponding Equations.
 129 The return power V_m is

$$V_m(t) = a_\xi P_u \frac{[1 + \operatorname{erf}(u)]}{2} \exp(-v) + T_n \quad (1)$$

130 where

$$\operatorname{erf}(x) = 2 \frac{1}{\sqrt{\pi}} \int_0^x e^{-t^2} dt \quad a_\xi = \exp\left(\frac{-4 \sin^2 \xi}{\gamma}\right) \quad \gamma = \sin^2(\theta_0) \frac{1}{2 \cdot \ln(2)} \quad (2)$$

$$u = \frac{t - \tau - c_\xi \sigma_c^2}{\sqrt{2} \sigma_c} \quad v = c_\xi \left(t - \tau - \frac{1}{2} c_\xi \sigma_c^2\right) \quad (3)$$

$$\sigma_c^2 = \sigma_p^2 + \sigma_s^2 \quad \sigma_s = \frac{SWH}{2c} \quad (4)$$

$$c_\xi = b_\xi a \quad a = \frac{4c}{\gamma h \left(1 + \frac{h}{R_e}\right)} \quad b_\xi = \cos(2\xi) - \frac{\sin^2(2\xi)}{\gamma} \quad (5)$$

131 where c is the speed of light, h the satellite altitude, R_e the Earth radius, ξ the off-
 132 nadir mispointing angle, θ_0 the antenna beam width, τ the Epoch with respect to the

133 nominal tracking reference point (linked to the range), σ_c the rise time of the leading
134 edge (depending on a term σ_s linked to the Significant Wave Height (SWH) and on the
135 width of the radar point target response σ_p), P_u the amplitude of the signal (linked to
136 the backscatter coefficient σ_0) and T_n the thermal noise level.

137 The variables that can alter the slope of the trailing edge in BH are all contained in
138 the term c_ξ . It is important to note that c_ξ has also a small effect on u via the term $c_\xi\sigma_c^2$.
139 This means that changes in c_ξ also slightly affect the position of the retracking point τ
140 along the leading edge. An approach to fit the trailing edge slope was also attempted in
141 other studies, such as in the empirical 5-parameter model by Deng & Featherstone (2006),
142 in which nevertheless a change in the parameter related to the slope of the trailing edge
143 would not cause any change in the location of the retracking point on the leading edge.

144 In Equations 1-5, the trailing edge slope variability is constrained by the fact that
145 θ_0 is given and the variations of ξ are slow and must be smaller than 0.3° (Dorandeu
146 et al., 2004). While these constraints correctly model a typical open ocean response, they
147 prevent the fitting of peakier waveforms. Therefore, in order to be able to fit waveforms
148 with a steep trailing edge slope, ALES+ preliminary estimates c_ξ . The steps followed by
149 ALES+ are the following:

- 150 1. Detection of the leading edge
- 151 2. Choice of c_ξ
- 152 3. First retracking of a subwaveform restricted to the leading edge, i.e. first estimation
153 of the SWH
- 154 4. Extension of the subwaveform using a linear relationship between width of the
155 subwaveform and first estimation of the SWH
- 156 5. Second retracking of the extended subwaveform, i.e. precise determination of τ ,
157 SWH and P_u

158 Steps 1 and 2 are described respectively in Section 3.1.2 and Section 3.1.3. Steps 3
159 to 5 are unchanged compared to the ALES retracker (Passaro et al., 2014) and they are
160 recalled in Section 3.1.4. A flow diagram of the main steps followed by ALES+ to retrack
161 each waveform is shown in Figure 2.

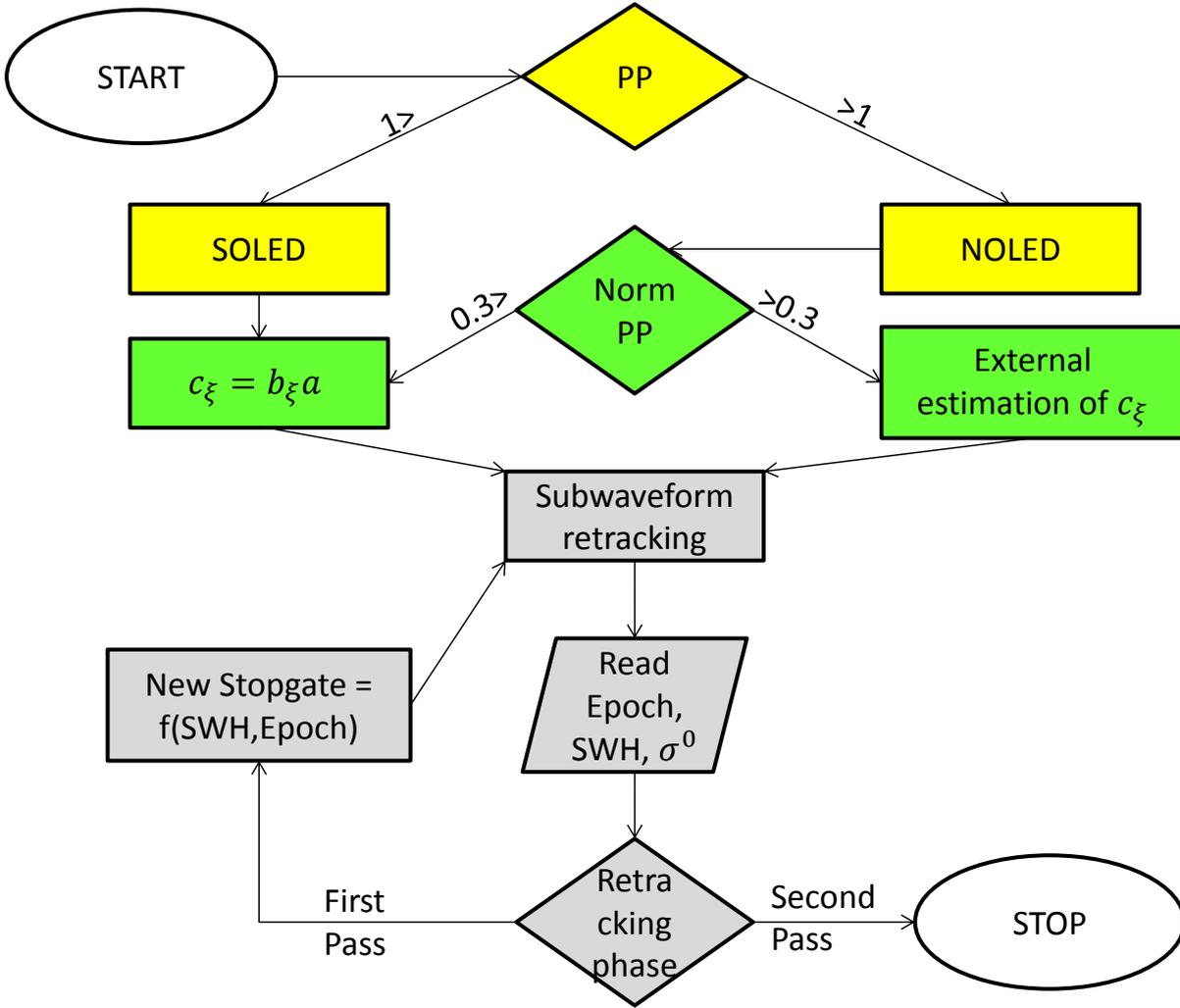


Figure 2: Flow diagram of ALES+ retracking procedure for each waveform. PP stands for Pulse Peakiness, Norm PP for Pulse Peakiness computed on the normalised waveforms. SOLED and NOLED are the leading edge detection procedures for standard and non-standard ocean waveforms described in Section 3.1.2. The steps highlighted in green are described in Section 3.1.3 and the ones in grey, analogous to ALES in Passaro et al. (2014), are recalled in Section 3.1.4.

162 *3.1.2. Leading edge detection*

163 Since ALES+ is based on the selection of a subwaveform, it is essential that the
 164 leading edge, containing the information on the range between satellite and reflecting
 165 surface, is correctly detected in all cases. Lead waveforms and ocean/coastal waveforms
 166 are characterised in this respect in two different ways: in the first case, the lead return
 167 (if at nadir) clearly dominates any other return, but the decay of the trailing edge is
 168 extremely quick; in the latter, the leading edge is better characterised, but spurious
 169 strong returns can precede (if from icebergs, ships, or targets at a higher height than the

170 water level) or follow (if from areas of the footprint characterised by different backscatter
171 characteristics) the main leading edge, whose trailing edge decreases very slowly.

172 To distinguish between the two cases, a Pulse Peakiness (PP) index is computed in
173 ALES+ following the formula in Peacock & Laxon (2004). The order of magnitude of PP
174 ranges from 10^{-1} for waveforms in which the peak power is comparable to the average
175 backscatter in the other waveform gates, to over 10^1 for echoes dominated by a strong
176 specular reflector. Waveforms with $PP < 1$ are sent to the standard ocean leading edge
177 detection (SOLED) procedure, the others are sent to the non-standard ocean leading edge
178 detection procedure (NOLED). This is not a physical classification aimed at detecting
179 leads, but only a way to aid the correct detection of the leading edge; moreover, the
180 retracking (steps 3-5 in Section 3.1.1) remains the same in both cases.

181 Non-standard ocean waveforms are in our case not only the leads (peaky waveforms),
182 but any waveform whose trailing edge decay is more pronounced than in the standard
183 ocean return. We do not exclude the waveforms coming from sea ice, since these are
184 excluded in the post-processing by the classification of Section 3.2. The aim is therefore
185 different from Peacock and Laxon (2004), in which a strict classification is needed in order
186 to send each kind of waveform to a different retracker and to avoid the detection of false
187 leads, which would cause inconsistencies in the sea level retrieval.

188 The steps followed by NOLED are the following:

- 189 1. The waveform is normalised with normalisation factor N , where $N = 1.3 * \text{me-}$
190 $\text{dian}(\text{waveform})$
- 191 2. The tentative starting point of the leading edge, defined as startgate, is assigned
192 to the first gate higher than 0.01 normalised power units compared to the previous
193 gate
- 194 3. If any of the subsequent 4 gates after the selected startgate have a normalised power
195 below 0.1 units, the algorithm goes back to step 2 and a new startgate is found
- 196 4. The end of the leading edge (stopgate) is fixed at the first gate in which the deriva-
197 tive changes sign (i.e. the signal start decreasing and the trailing edge begins), if
198 the change of sign is kept for the following 3 gates.

199 The steps followed by SOLED are the following:

- 200 1. The waveform is normalised with normalisation factor N , where $N = \text{max}(\text{waveform})$

- 201 2. The stopgate is the maximum value of the normalised waveform
 202 3. Going backwards from stopgate, the startgate is the first gate in which the derivative
 203 is lower than 0.001 units

204 $N=1.3*\text{median}(\text{waveform})$ was chosen empirically as a reference power whose value
 205 is close to the maximum of the leading edge also in case of high trailing edge noise.
 206 Note that for NOLED waveforms the maximum of the leading edge does not necessarily
 207 correspond to the maximum power registered in the waveform, since it may come from
 208 spurious coastal reflections and/or noise in the trailing edge.

209 3.1.3. Choice of c_ξ

210 The non-standard ocean waveforms undergo a further preliminary step: c_ξ is esti-
 211 mated externally. Beforehand, a further check on the PP recomputed on the normalised
 212 waveform (Norm PP >0.3) is computed in order to avoid, where possible, the estimation
 213 of c_ξ in the presence of other peaks in the trailing edge. Norm PP is useful because by
 214 using a normalised waveform it is easier to set up a threshold for all peaky waveforms
 215 regardless of their maximum backscatter power, which greatly differ between specular
 216 reflections (Passaro et al., 2017). The threshold was determined by empirical observation
 217 of waveforms, of which Figure 3 provides an example.

218 In the external estimation, the full waveform is fitted using a simplified BH model up
 219 to Equations 4, having 4 unknowns: $\tau, \sigma_c, P_u, c_\xi$. From this result, only c_ξ is kept and
 220 used as an input in the remaining steps of the ALES+ algorithm.

221 If Norm PP <0.3, c_ξ is computed from Equations 5.

222 c_ξ can be therefore estimated for all the waveforms that successfully pass through
 223 SOLED and if Norm PP >0.3, i.e. all the peaky waveforms in which one clear leading
 224 edge can be identified. Since the estimation of c_ξ is suitable for peaky waveforms, irregular
 225 waveforms where no leading edge is identifiable cannot be correctly fitted by ALES+.
 226 Figure 4 shows the estimations of c_ξ for cycle 35 of Envisat (February-March 2005). The
 227 areas where c_ξ is estimated are all located in the sea-ice-covered region.

228 3.1.4. Subwaveform retracking

229 Steps 3 to 5 are analogous to the ALES retracker. In step 3, a first subwaveform from
 230 startgate to stopgate is fitted with the BH model having τ, σ_c, P_u as unknowns.

231 The SWH derived from σ_c and τ are used in step 4 to compute the new stopgate using
 232 the following linear relationship:

$$\text{Stopgate} = \text{Ceiling}(\text{Tracking point} + 2.4263 + 4.1759 \times \text{SWH}) \quad (6)$$

233 for Envisat and:

$$\text{Stopgate} = \text{Ceiling}(\text{Tracking point} + 3.1684 + 2.3203 \times \text{SWH}) \quad (7)$$

234 for ERS-2. The Tracking point is the gate corresponding to the estimated Epoch τ .
 235 Finally, in step 5 a new fitting is performed using a subwaveform up to the new
 236 stopgate and the final estimations of τ, σ_c and P_u are obtained. Note that in every fitting,
 237 the subwaveform is oversampled by means of the Akima interpolation by Akima (1970) in
 238 order to increase the redundancy of the information across the leading edge as described
 239 in Passaro et al. (2015b); in ALES+, the waveforms are oversampled by a factor of 8 for
 240 both Envisat and ERS-2.

241 Figure 5 shows three examples of ALES+ waveform fitting for three different trailing
 242 edge slope conditions typical of open ocean, coast and leads. A black vertical line high-
 243 lights the location of the retracking point estimated by ALES+. In the lead case (Figure
 244 5c), it is evident how the retracking point (Epoch) is not located at the mid-point of the
 245 visible leading edge, since the retracking point τ and c_ξ are present both in the expo-
 246 nential term v and in the argument of the error function u as described in Section 3.1.1.
 247 This effect is not simply empirical, but is related to the mean square slope (MSS) of the
 248 sea surface, as shown in Jackson et al. (1992). In the latter, the so-called trailing edge
 249 parameter, which has an effect on the retracking point as well, depends explicitly on the
 250 MSS and hence on the surface roughness. Indeed, using the mid-point of the 'visible'
 251 leading edge as the retracking point of any peaky waveform has no physical meaning,
 252 because the waveform, i.e. a discrete time series, is in this case highly undersampled: the
 253 information on the position of the true maximum power and consequently the location
 254 of the true mid-point of the leading edge cannot be retrieved. ALES+ cannot create new
 255 information and solve the problem of the undersampled leading-edge, but it can perform
 256 a consistent guess of τ given c_ξ , using an existing waveform model and adapting it to a
 257 more general case.

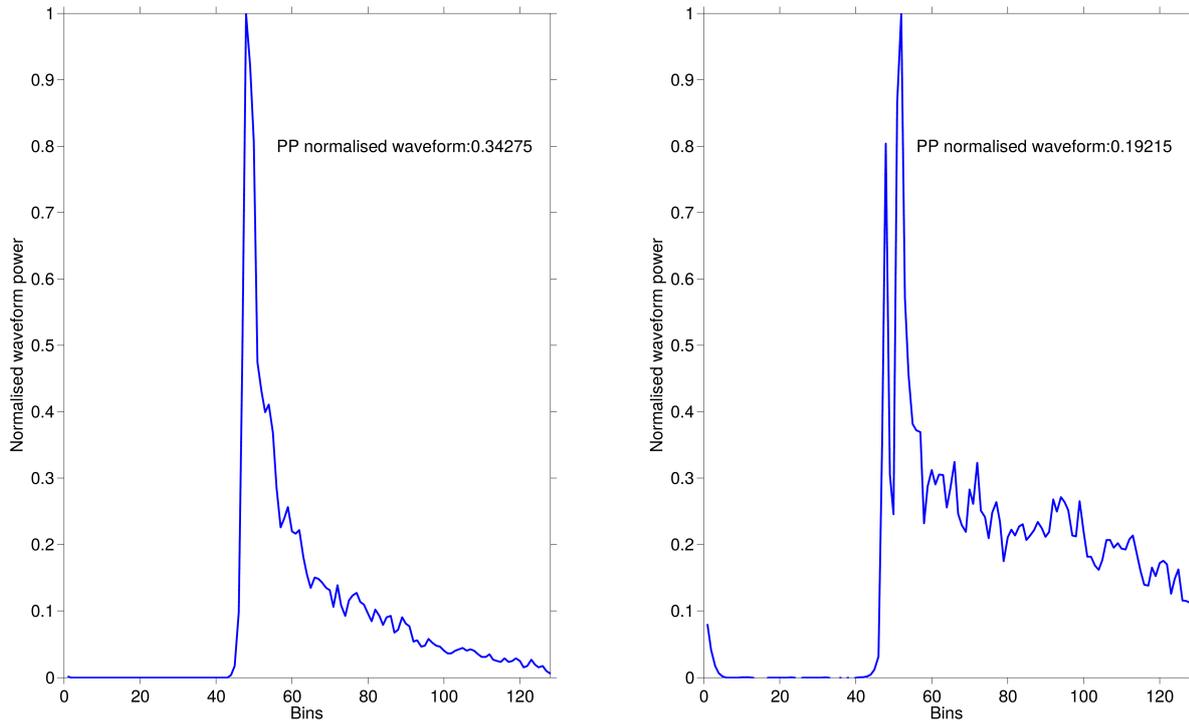


Figure 3: Normalised waveforms and their pulse peakiness (Norm PP). Left: a peaky waveform in which c_{ξ} can be estimated by ALES+; Right: a waveform with a peak following the trailing edge.

258 3.1.5. Sea State Bias recomputation

259 The Sea State Bias (SSB) is among the time-variable corrections that are applied to
 260 SSH estimates from satellite altimetry. SSB is linked with both the signal processing of
 261 the radar echo and the interaction between the latter and the waves. Given the theoretical
 262 complexity and the different sources of SSB, the accepted procedure to derive an SSB
 263 correction is to infer an empirical relationship between the height error due to SSB,
 264 and the SWH and wind speed (derived from σ^0) estimated from the retracking of each
 265 altimetry mission. Sandwell & Smith (2015) have studied the relationship between the
 266 parameters estimated by the retracking algorithms (range, SWH and σ^0) and have found
 267 significant correlated errors. In the same study, they argue that correlated errors in the
 268 retrackers explain a significant part of the SSB. It is therefore fundamental to correct the
 269 ranges for the SSB corresponding to SWH and σ^0 values estimated by the same retracker.

270 The SSB applied to the ALES+ data is obtained by bilinear interpolations from a
 271 look-up table in which this correction is a function of SWH and Wind Speed (Labroue,
 272 2007). The look-up table could be obtained from the SGDR data by tabulating the values

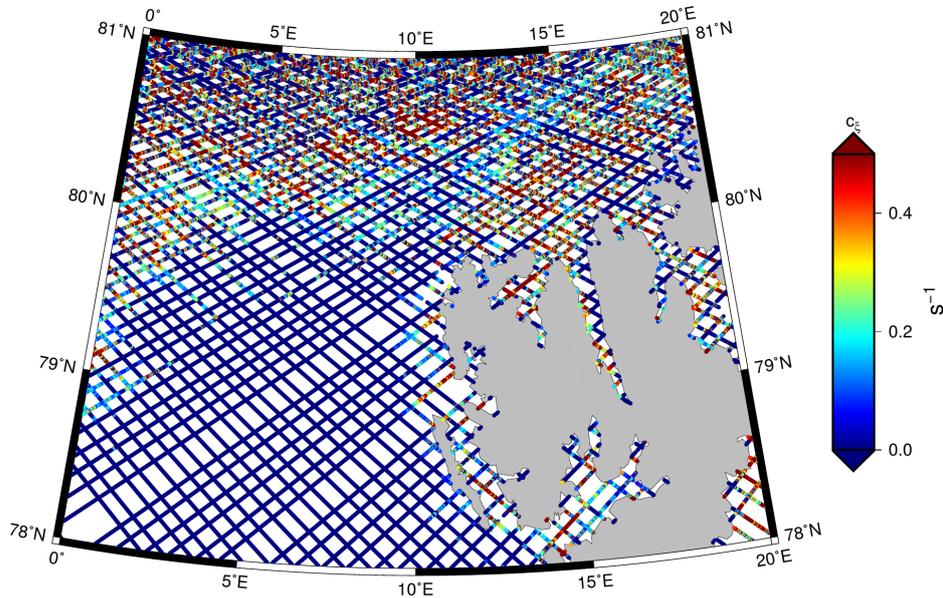


Figure 4: Estimations of c_ξ for cycle 35 of Envisat. In the plot, c_ξ is set to 0 for NOLED waveforms and for waveforms in which Norm PP < 0.3 , because c_ξ is in these cases not estimated.

273 assumed by the given SSB correction for each value of SWH and Wind. In order to be
 274 more accurate, the authors have obtained the look-up table with permission from Collecte
 275 Localisation Satellite (CLS). When performing the bilinear interpolations, SWH and σ^0
 276 obtained from ALES+ were used. σ^0 was converted to wind speed using the algorithm
 277 described in Abdalla (2012). This follows the procedure applied and validated against
 278 in-situ data for ALES Envisat in Gómez-Enri et al. (2016). For ERS-2, we use the same
 279 look-up Table as for Envisat mission, since the one used in the REAPER product has
 280 not been published (Gilbert et al., 2014).

281 3.2. Waveform classification

282 To allow the validation of the retracking strategy in the sea ice region, lead and
 283 open ocean waveforms need to be isolated by means of a classification algorithm. For
 284 our purposes, given that sea ice waveforms can be hard to distinguish from open ocean
 285 returns (Drinkwater, 1991; Laxon, 1994a), we first separate the ice-covered region from the
 286 open ocean using the daily ice concentration grids from the Global Sea Ice Concentration

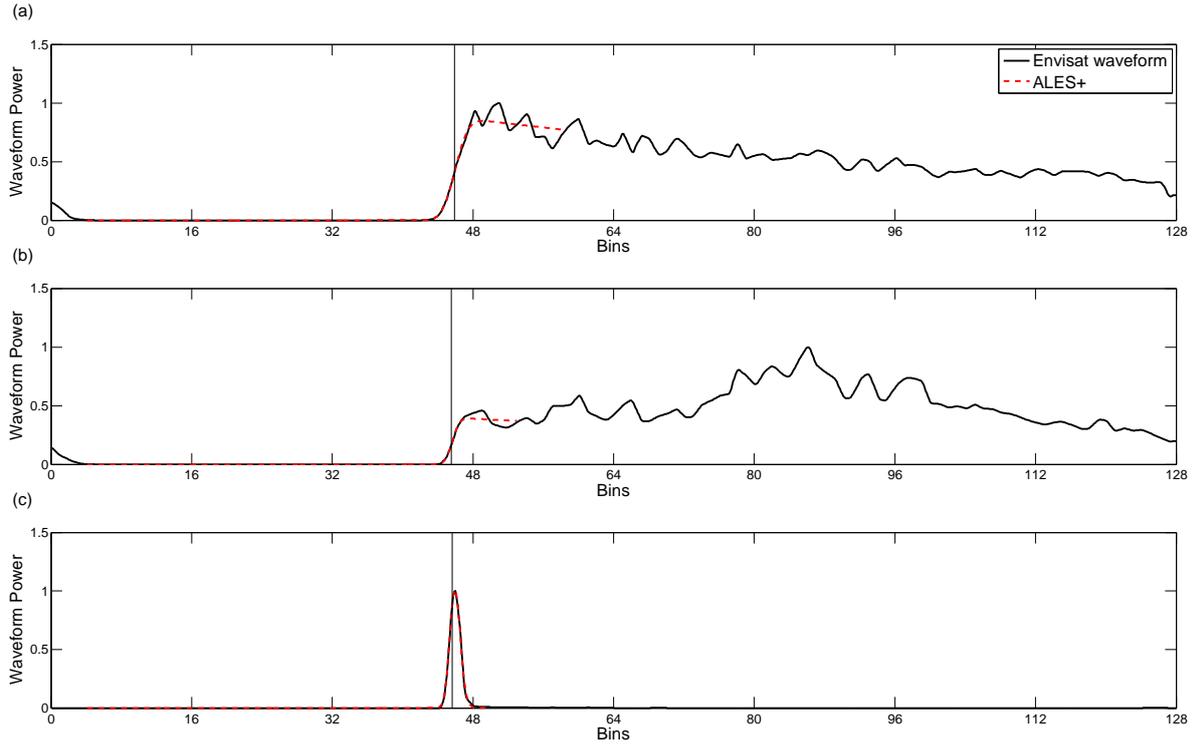


Figure 5: Examples of ALES+ waveform fitting for three different trailing edge slope conditions typical of open ocean (a), coast (b) and leads (c). A black vertical line highlights the location of the retracking point estimated by ALES+.

287 Climate Data Records 1978-2015 (v1.2, 2015) of the Norwegian and Danish Meteorological
 288 Institutes (available online from EUMETSAT Ocean and Sea Ice Satellite Application
 289 Facility <http://osisaf.met.no>). The sea ice area is defined by all the points in the grid
 290 with a sea ice concentration over 15% (Fetterer et al., 2016).

291 In this study, the following classification criteria are used for both Envisat and ERS-2:

- 292 • The samples within the sea ice area characterised by $PP > 20$ and $\sigma_c < 3$ ns are
 293 classified as leads;
- 294 • The samples outside the sea ice area characterised by $PP < 1.5$ and $\sigma^0 < 15$ dB are
 295 classified as open water

296 Any other point is either classified as unknown or as sea ice and is therefore not
 297 considered in our analysis. The criterion on σ^0 is applied to remove spurious data near
 298 the ice edge and in the ice pack (Chelton & McCabe, 1985). Additional discussion and
 299 validation of the classification method will be provided in Rose et al. (in preparation).

300 3.3. Corrections applied to the range

301 While the retracking technique at the centre of this investigation influence the range
302 and the SSB, as mentioned in the introduction other corrections are needed in order to
303 obtain a sea level that is comparable to external sources for validation. In particular, we
304 define the SSH as follows:

$$\text{SSH} = \text{Orbit altitude} - \text{Corrected Range} - (\text{Solid Earth Tide} + \text{Load Tide} + \text{Ocean Tide}) \quad (8)$$

305 where

$$\begin{aligned} \text{Corrected Range} = & \text{Range} + \text{Dry tropospheric correction} + \text{Wet Tropospheric Correction} + \\ & + \text{Sea State Bias} + \text{Ionospheric correction} \end{aligned} \quad (9)$$

306 Note that the correction that eliminates the static and dynamic response of the sea
307 level to the atmospheric wind and pressure forcing (often called Dynamic Atmosphere
308 Correction) is not applied, since the water level measured by pressure gauges used for
309 validation is also subjected to these factors.

310 We use the corrections for the wet and dry troposphere and for the ionosphere from
311 the models available in the SGDR. The SSB is recomputed for ALES+ as previously
312 described. The sea level is also corrected for tides: the FES2014 model is used in the
313 Svalbard test area, given the improvements brought by the model in the Arctic region
314 (Carrere et al., 2015); the Empirical Ocean Tidal model EOT2011a (Savcenko & Bosch,
315 2012) is used in the coastal validation, since it has scored best in a recent validation effort
316 against coastal TGs (Stammer et al., 2014). Finally, the Sea Level Anomaly (SLA), i.e.
317 the variation of the SSH with respect to a local mean, is obtained by subtracting the
318 Mean Sea Surface model DTU15 to the SSH (Andersen et al., 2016).

319 4. Validation and discussion

320 4.1. Svalbard test area

321 4.1.1. Comparison among retrackers

322 The first index that proves the quality of the retracking is the fitting error on the
323 leading edge. The fitting error is a measure of how close the fitted waveform is to the

324 real signal and corresponds to the normalised square root of the difference between the
325 modelled waveform and the real signal along the leading edge. It has already been used
326 in Passaro et al. (2015a) for outliers detection. In Figure 6, the histogram of the fitting
327 error for the waveforms classified as leads is compared to the one for the open ocean
328 waveforms with low SWH, whose leading edge is therefore more similar to the peaky
329 case. The fitting error of lead waveforms is in the vast majority of instances lower than
330 for the low-SWH ocean case, which proves the capability of ALES+ to fit the leading
331 edge of all the peaky waveforms. The statistics for ERS-2 are slightly worse than for
332 Envisat: this can be attributed to the fact that the original ERS-2 data are defined on
333 half the number of gates (64) compared to Envisat (128).

334 Firstly, we compare our retracked data with the SGDR output in the sea ice domain.
335 In particular, concerning SGDR we consider both the ocean retracker and the sea ice
336 retracker, which was specifically designed for the fitting of specular waveforms by Laxon
337 (1994a) and included in the official ESA products from Envisat and ERS-2. This retracker
338 was used to estimate sea level from leads by Peacock & Laxon (2004). Given the absence
339 of network of high-resolution in-situ data at such latitudes, we validate the retracker
340 following the procedure of Deng & Featherstone (2006) by means of an independently
341 surveyed reference . We use GOCO5s, the latest release of the GOCOs geoid model,
342 which is independent from altimetry, being based exclusively on satellite gravimetry data
343 (Pail et al., 2010), although as such it is not able to observe the shorter wavelengths
344 (below 100 km) detected by the altimeter. The GOCO5s geoid height are interpolated to
345 the altimetry tracks in the whole area and the differences between SSH and geoid height
346 are computed. These differences of course include the mean dynamic topography and
347 the uncertainties in the corrections to the altimetry data. Nevertheless what matters
348 for our analysis are the differences among the retracker and the corrections do not
349 have an influence, since exactly the same corrections are applied to every dataset. In
350 order to make our results independent of the performances of the waveform classification,
351 we compute the differences for any point with $PP > 1$ and we only keep the additional
352 criteria of $\sigma_c < 3$ ns, to be sure that we are dealing with peaky echoes. After removing
353 outliers (absolute value of SLA above 2 m), the Median Absolute Deviation (MAD) of
354 the differences is computed for every cycle and the average values are shown in Table
355 1. For both missions ALES+ is the best performing dataset, improving not only the

Table 1: Median Absolute Deviation between GOCO5s geoid heights and SSH data retracked with ALES+, SGDR-Ocean and SGDR-Seaice retracker for peaky waveforms in the Svalbard test area.

	ALES+	SGDR-Ocean	SGDR-Seaice
ERS-2	0.2620 m	0.3659 m	0.2901 m
Envisat	0.2142 m	0.2961 m	0.2364 m

356 results of the ocean retracker (more than 7 cm improvement for Envisat, more than 10
 357 cm improvement for ERS-2), which is not able to fit peaky waveforms properly, but also
 358 of a dedicated solution (more than 2 cm improvement for Envisat against the sea ice
 359 retracker, 2.8 cm for ERS-2).

360 To further investigate the noise performances of ALES+ compared to a standard ocean
 361 retracker, the analysis of repetitive tracks in the open sea is needed. For this purpose, we
 362 limit our area of study using only the track segments that are out of the maximum extent
 363 of the sea ice, as shown in Figure 7. As a noise index we use the standard deviation
 364 of the high frequency data within a 1-Hz block. For comparison, the same analysis is
 365 performed using the SGDR ranges (from the ocean retracker) corrected and processed
 366 in the same way as ALES+ ranges. In the figure, the maps in (a) and (b) show for
 367 each 1-Hz point in ERS-2 and Envisat the median of the difference between the noise of
 368 the ocean retracker (SGDR) and the noise of the ALES+ retracker (ALES+). Positive
 369 numbers therefore mean that SGDR is noisier than ALES+. The histograms considering
 370 each 1-Hz point are shown in (c) and (d). In both missions, ALES+ is less noisy than
 371 SGDR in over 70% of the domain and in 20% of the domain it improves by over 3 cm.
 372 The maps show that, although the best improvements are reached at the border with
 373 the maximum sea ice extent, ALES+ is superior to the standard ocean retracking also
 374 in the open ocean. Overall, the median SGDR noise is 6.23 cm in Envisat and 9.18 cm
 375 in ERS-2, while the ALES+ noise is 5.08 cm in Envisat and 7.95 cm in ERS-2, meaning
 376 over 1.1 cm of improvement.

377 This demonstrates that the ALES+ compromise between a sufficient width of the
 378 subwaveform to characterise the signal. A limited influence of the noise in the trailing edge
 379 in the fitting allows a more precise estimation of the open ocean sea level, if compared with
 380 a full-waveform retracker. This clear improvement in the open ocean was not evident in
 381 Passaro et al. (2014) for ALES. The reason lies in the recomputation of the SSB correction

382 using the ALES+ SWH and backscatter coefficient. We demonstrate this in Figure 9,
 383 where the standard deviation of the 1-Hz points is plotted against the SWH for ALES+
 384 corrected by the standard SSB and by the recomputed SSB. For comparison, the SGDR
 385 statistics are also shown. From the linear fit it is evident that without a recomputed
 386 SSB correction ALES+ is slightly noisier than SGDR, while the new correction brings a
 387 strong improvement.

388 *4.1.2. Comparison of sea level products*

389 The main application of ALES+ is the provision of improved ranges that will be used
 390 to compute SLA in the SL CCI DTU/TUM high latitude sea level product. We evaluate
 391 the improvements in this section. We take RADS as an open ocean sea level reference
 392 that flags coastal and sea ice data, with the objective to show what improvements a
 393 dataset including these areas can bring to the sea level records.

394 We apply a gridding procedure to the dataset. First of all, outliers are treated by a
 395 MAD filter. The RADS data are per default already post-processed so no further outlier
 396 detection to this dataset is applied. Subsequently, for each week the SLA values are
 397 gridded using a least squares collocation (kriging) method with a second order Markov
 398 covariance function (Andersen, 1999):

$$c(r) = C_0 \left(1 + \frac{r}{\alpha}\right) e^{-r/\alpha} \quad (10)$$

399 where C_0 is the signal variance, r is the spatial distance, and α is the correlation
 400 length. The covariance scale is derived from the data variance, the correlation length is
 401 set to 500 km. Each grid cell measures 0.1° latitude \times 0.5° longitude. For reference, we
 402 process RADS data in the same way. The collocation error is displayed in Figure 8 (a)-
 403 (b), while (c)-(f) show the number of valid measurements used for each grid point. The
 404 much higher number of measurements used by ALES+ is simply explained by the fact
 405 that it uses high-frequency measurements (18 Hz for Envisat, 20 Hz for ERS-2), while
 406 RADS is based on 1-Hz averages. This allows ALES+ to retrieve much more points in
 407 the sea ice-covered regions. Even if the number of measurements is much lower than in
 408 the open ocean, the error is kept below 2 cm also in most of the northern and coastal
 409 areas of the domain. Overall, the mean error for ALES+ in the sea ice covered zone is
 410 2.1 cm (2.7 cm for RADS) while in the open ocean domain the mean error is 0.9 cm (1.3
 411 cm for RADS).

412 Finally, we verify the accuracy of our sea level estimations by comparison with the Ny
413 Ålesund TG. The location of the TG is visible in Figure 1(a). SLA from ALES+, gener-
414 ated from the range using the corrections in Section 3.3 is averaged in space in a radius
415 of 350 km around the TG and in time to generate a monthly time series. The radius of
416 350 km is needed to perform a regional average that includes both sea ice cover and open
417 ocean areas and the choice was already justified in the same area by Cheng et al. (2015).
418 The agreement of the time series (Figure 10) is proved by a correlation of 0.85. For
419 comparison, we also build a time series using RADS. Indeed, the better correlation using
420 ALES+ is expected, given that RADS is not optimised for the Arctic Ocean: the benefit of
421 the ALES+ retracking is particularly evident in the winter months of 1996 and 1998. As
422 mentioned in Section 4.1, the winter of 1998 had the maximum sea ice extent; a significant
423 part of the area considered for the comparison (the coast west of the Svalbard islands) was
424 covered by sea ice and therefore the use of a standard altimetry product is more problem-
425 atic. In the last decade, most of the area was ice-free during winter as well (not shown,
426 see for example https://nsidc.org/data/seaice_index/archives/image_select.html) and
427 therefore the RADS and ALES+ time series are more similar.

428 4.2. Coast

429 In this Section, the performances of ALES+ in the coastal ocean are tested by com-
430 parison with the set of TGs in Figure 1 (b). The comparison is performed for detided
431 time series of sea level. The amplitudes and phases of the tidal constituents in the tide
432 gauge records were estimated on a year-by-year basis by harmonic analysis using the
433 program t-tide (Pawlowicz et al., 2002). Harmonic analysis produces non-tidal residuals
434 that are more representative of the true variability that can then be used as our ground
435 truth against which we assess the altimetry data. Only constituents with a signal-to-noise
436 ratio equal or larger than three were used to reconstruct the tidal signal. This guarantees
437 the estimation of the most important constituents, while less energetic tidal constituents
438 are not well resolved given the observations and their noise level and thus it is better to
439 remove them.

440 At each tide gauge station, the performance of the altimetry data is assessed as a
441 function of distance from the coast by assigning such data to distance bands of 1 km
442 width starting from the 0-1 km band. As shown in Figure 1 (b), only data that fall within
443 70 km of the TG are used. For each altimetry pass we obtain one altimetry value by

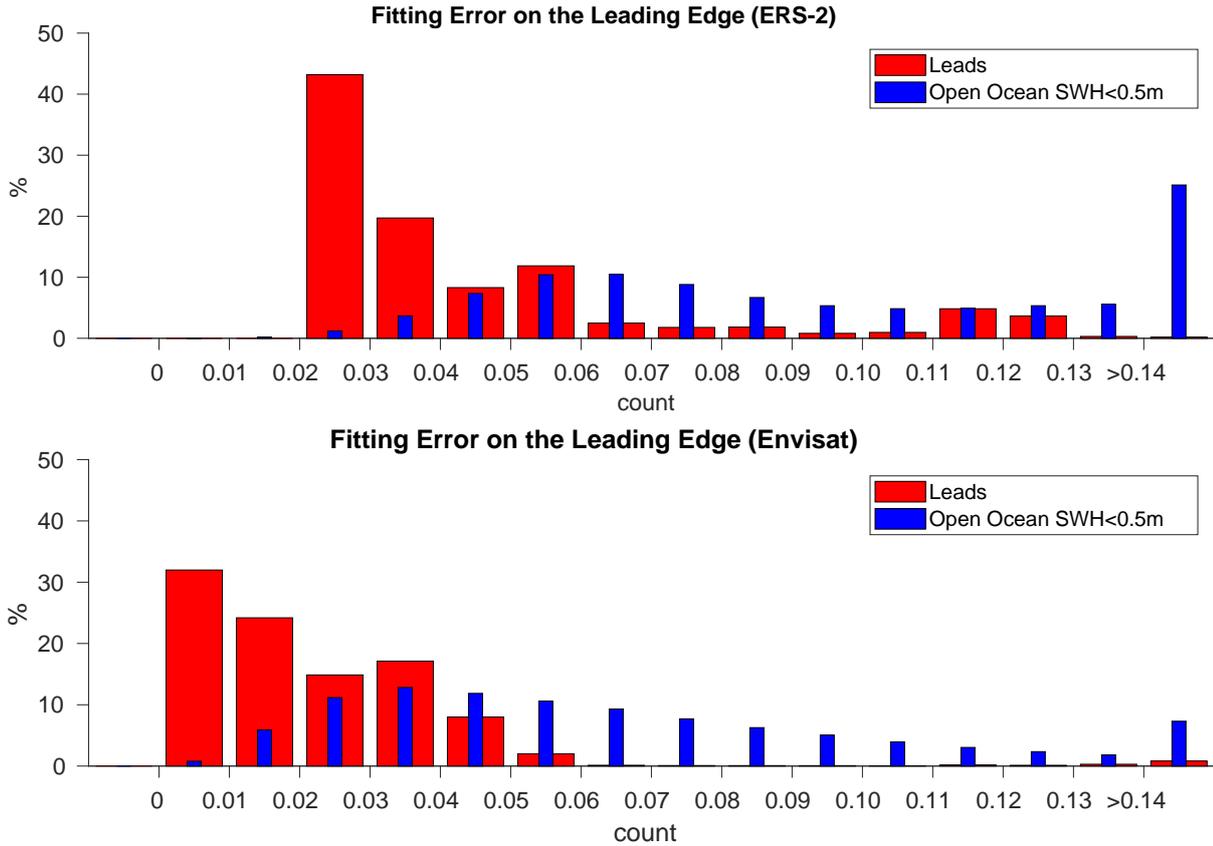


Figure 6: Error of the leading edge fit computed w.r.t. the normalised waveform for echoes classified as leads (red) and as open water with SWH<0.5 m (blue) in ERS-2 (upper plot) and Envisat (lower plot).

444 averaging all the high frequency records falling within the selected distance band. Records
 445 with an absolute SLA larger than 2 m or three standard deviations above the mean were
 446 rejected prior to computing the average. The corresponding tide gauge matching value is
 447 obtained by linearly interpolating the tide gauge observations to the time of the altimetry
 448 pass. The corresponding time series for each km-band are then evaluated according to the
 449 Percentage of Cycles for High Correlation (PCHC): the maximum percentage of cycles
 450 of data that could be retained while guaranteeing a correlation with the TG time series
 451 of at least 0.8 (Passaro et al., 2015b). The same procedure is applied to the SGDR ocean
 452 retracker and to the ALES retracker as described in Passaro et al. (2014), but with the
 453 addition of the recomputed SSB.

454 Firstly, the results are displayed in Figure 11 considering each TG-altimetry track
 455 couple. The values shown in the figures are the median PCHC in the last 10 km from
 456 the coast. Statistics vary considerably depending on the TG and satellite tracks. For

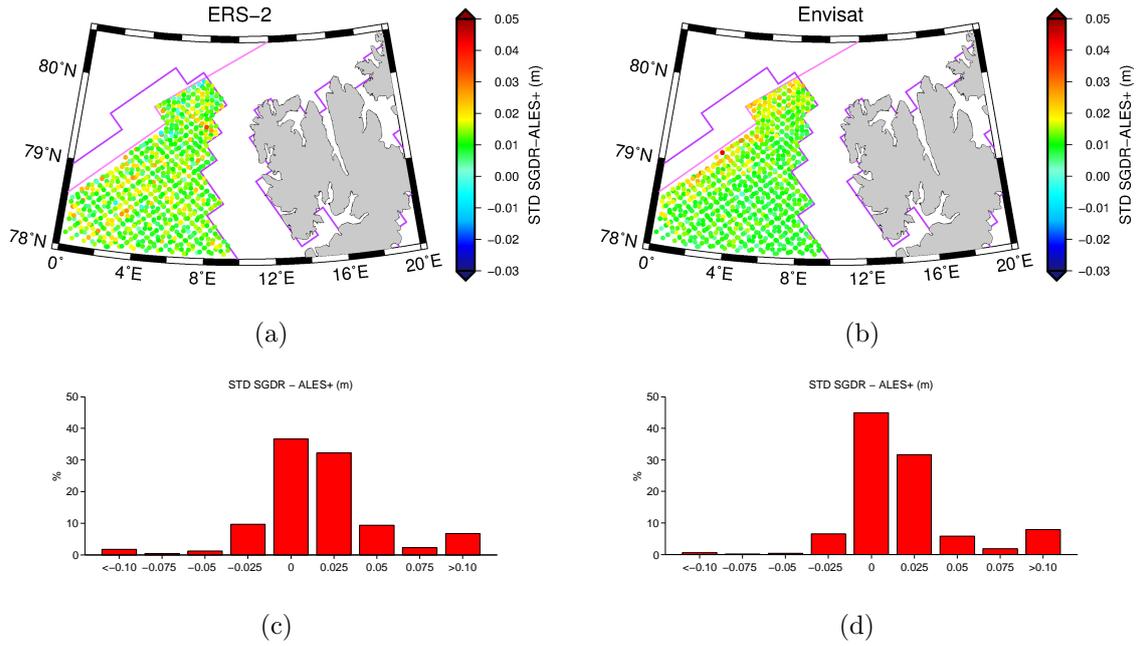


Figure 7: Difference of high-frequency noise in SGDR and ALES+ for ERS-2 (a,c) and Envisat (b,d). The noise is computed as standard deviation of the 1-Hz averages. The maps in (a) and (b) show the median of the noise difference for each 1-Hz point along the satellite tracks considering the entire period of study. Areas characterised by seasonal or multi-year sea ice are masked out.

457 example PCHC is below 20% in 2 cases for Envisat and 4 cases for ERS-2. This is
 458 partly related to the general worse performances and loss of altimetry data in land to
 459 sea transitions (see for example Gómez-Enri et al. (2016)). This is not a problem for our
 460 analysis, in which the objective is the comparison between the retracker. In many cases,
 461 the three retracker have very similar performances. This is well known from previous
 462 studies such as Passaro et al. (2014): a different retracking method is not always needed.
 463 Nevertheless, SGDR has a better PCHC than ALES+ in only 2 cases out of 33 in Envisat
 464 (Fishguard-401 and Workington-704) and ERS-2 (Fishguard-160 and Lowenstoff-57). In
 465 several cases ALES+ and ALES are substantially better than SGDR (for example Tregde-
 466 543 in ERS-2 and Wick-143 in Envisat). Nevertheless there are 3 cases in Envisat and
 467 5 cases in ERS-2 in which ALES scores better than ALES+ by over 5%. To produce a
 468 final rating of the coastal performances with respect to the tide gauges, we looked at the
 469 median value of the PCHC considering all the tracks.

470 The results are displayed in Figure 12, where a median of the PCHC considering all
 471 33 tracks is highlighted with a continuous line for each dataset. In terms of PCHC, the
 472 performances of the three retracker are indistinguishable until 8 km from the coast. From
 473 8 to 2 km from the coast, ALES is the best-performing dataset, followed by ALES+, while

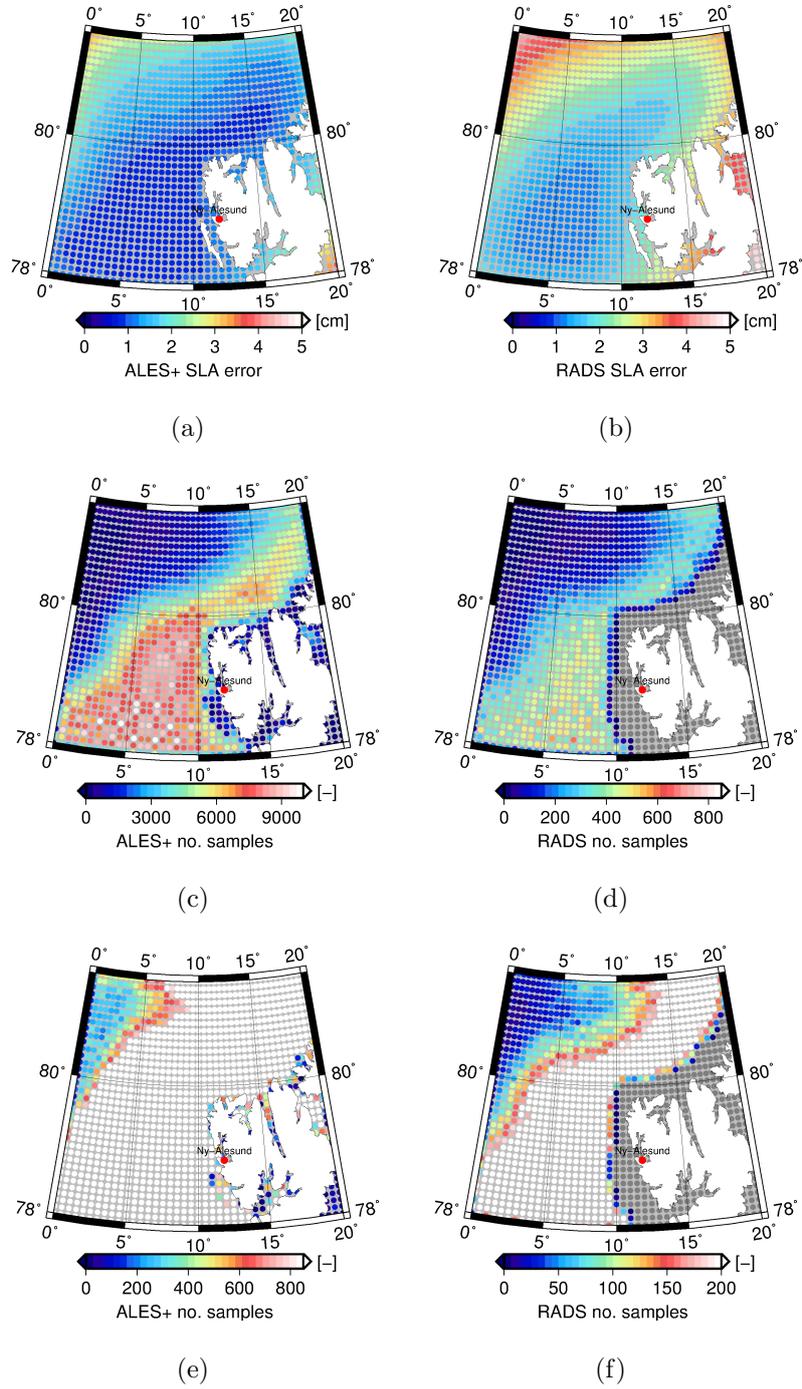


Figure 8: Collocation error estimate for (a) ALES+ and (b) RADS. The error is dependent on the number of samples. Number of samples in each grid cell for (c) ALES+ and (d) RADS. Notice the different color scales. (e) and (f) are the same as (c) and (d), but with saturated color scales in order to highlight points in the sea ice-covered areas.

474 SGDR is the worst-performing. In the last km, where waveforms are extremely irregular,
475 but also where most of the oceanic peaky waveforms are located (Deng & Featherstone,
476 2006), ALES+ is the best performing dataset.

477 This is expected, since ALES+ needs to reach a compromise in the normalisation and
478 leading edge detection, in order to be able to treat peaky waveforms as well, while the
479 objective of ALES is to maximise the number of retracked coastal waveforms, which are
480 normally characterised by strong peaks in the trailing edge.

481 We further validate and compare the retracking solutions by means of the comparison
482 with the geoid model. The GOCO5s geoid height are interpolated to the altimetry tracks
483 in the whole coastal area of the North Sea (Latitude limits: 50-61, Longitude limits: -11
484 15). We divide the domain via 5-km coastal distance bands. For each cycle of Envisat
485 and ERS-2, after excluding unrealistic values of $|SLA| > 2$ m and $SWH > 11$ m, we store
486 the MAD of the differences between SSH and geoid height. Figure 13 show the averages
487 of the results for Envisat and ERS-2. In the last 5 km to the coast, ALES scores better
488 in terms of STD, and ALES+ scores second. Both are much better than the original
489 SGDR data, which scores 2.7 cm worse than ALES+ for Envisat and 1.6 cm worse than
490 ALES+ for ERS-2. ALES and ALES+ are of course equivalent going towards the open
491 ocean and their MAD against the geoid is always lower than in SGDR.

492 We conclude that in the coastal zone ALES is the best choice among the three meth-
493 ods, but ALES+ scores constantly better than the current SGDR standard.

494 *4.3. Inland waters*

495 The possibility of using the same retracker to treat altimetry echoes from leads, open
496 and coastal waters can be extended to retrieve water level in inland water bodies. Indeed,
497 it has been shown that waveforms from rivers and small lakes are mostly quasi-specular
498 or quasi-Brown (Berry et al., 2005).

499 For a first investigation, we have integrated the ALES+ ranges from Envisat for the
500 Mekong river in the Database for Hydrological Time Series over Inland Waters (DAHITI,
501 processed at the DGFI-TUM), in which altimetric ranges are used to produce water levels
502 for river and lakes using a set of corrections, outlier rejection criteria and Kalman filter
503 processing as described in Schwatke et al. (2015). As a comparison, we use the results
504 from the Improved Threshold Retracker (ITR), implemented selecting a threshold of 50%
505 (Hwang et al., 2006), processed through DAHITI in the same way as ALES+. The ITR

506 is of common use in the reprocessing of inland water data (Hossain et al., 2014) and has
507 already been used in the area of study (Boergens et al., 2016). It references a threshold
508 value to the amplitude of the detected leading edge and determines the range by linearly
509 interpolating between adjacent samples (Gommenginger et al., 2011).

510 The comparison of the water level time series is shown in Figure 14 and the results
511 in terms of root mean square (RMS) error and correlation coefficient are reported in
512 Table 2, as well as the number of points in each time series. It is observed that none
513 of the retracers is able to catch the water extremes: this is due to the fact that the
514 temporal resolution of Envisat (one pass every 35 days) is suboptimal compared to an in-
515 situ gauge. The results of the two retracers are comparable in terms of correlation, while
516 ITR has a better RMS in two of the three stations. In Kratie, if one excludes the clear
517 outlier in the time series in 2003, ALES+ RMS scores 1.37 and therefore is inline with
518 the ITR result. Also the number of points in the time series is comparable between both
519 retracers in two of the three stations, while only in Mukdahan ITR has considerably
520 more points. Unfortunately, the comparison with the gauges is only relative, because
521 the in-situ stations lack an absolute reference. Nevertheless, the average bias between
522 ALES+ and ITR changes from 1.8 m in Luang Prabang to slightly more than 0.30 m in
523 Mukdahan and Kratie. The variable bias is due to the fact that, while ITR locates the
524 range using always the same threshold of the waveform amplitude, the location of the
525 retracking point of ALES+ varies depending on the estimated c_ξ , as explained in Section
526 3.1.1. Further validation against absolute water levels are needed to assess whether this
527 improves the accuracy of the altimeter for rivers.

Table 2: Comparison of water level time series in the Mekong river from Envisat retracked by ALES+ and by Improved Threshold Retracker at 50% w.r.t. data from three TGs. In terms of root mean square (RMS), correlation coefficient and number of points in the time series (Num of points).

		RMS (m)	Correlation Coefficient	Num of points
Luang Prabang vs Envisat pass 651	ALES+	0.87	0.97	72
	ITR 50%	0.81	0.97	72
Mukdahan vs Envisat pass 21	ALES+	0.79	0.99	69
	ITR 50%	0.79	0.99	74
Kratie vs Envisat pass 565	ALES+	1.59	0.96	80
	ITR 50%	1.33	0.98	79

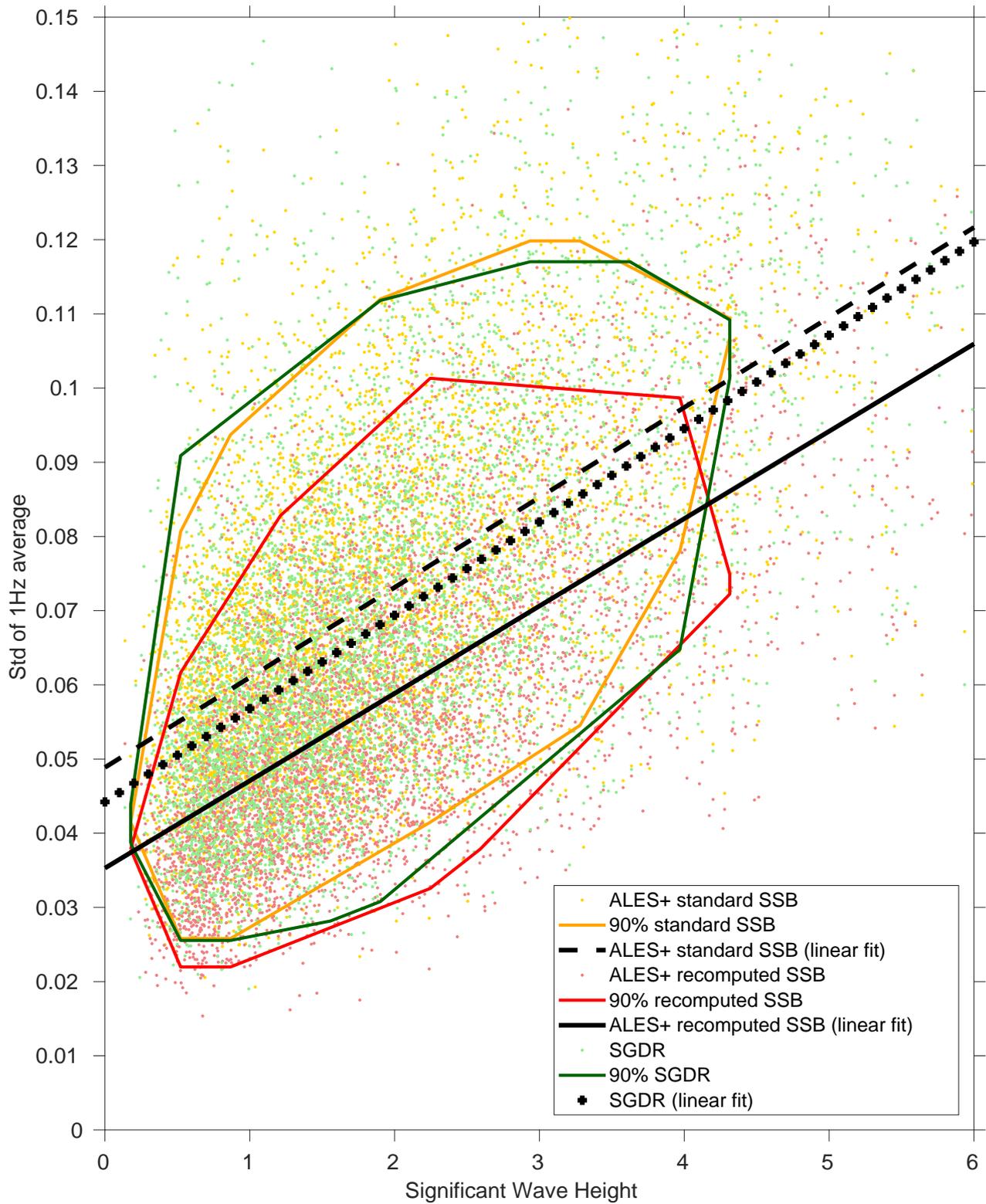


Figure 9: Scatter plot and linear fit of the standard deviations of the 1-Hz points (used as measurement of high-frequency noise) against the SWH, for ALES+ corrected by the standard SSB and by the recomputed SSB. For comparison, the SGDR statistics are also shown. The contours delimit the location of 90% of the data for each dataset.

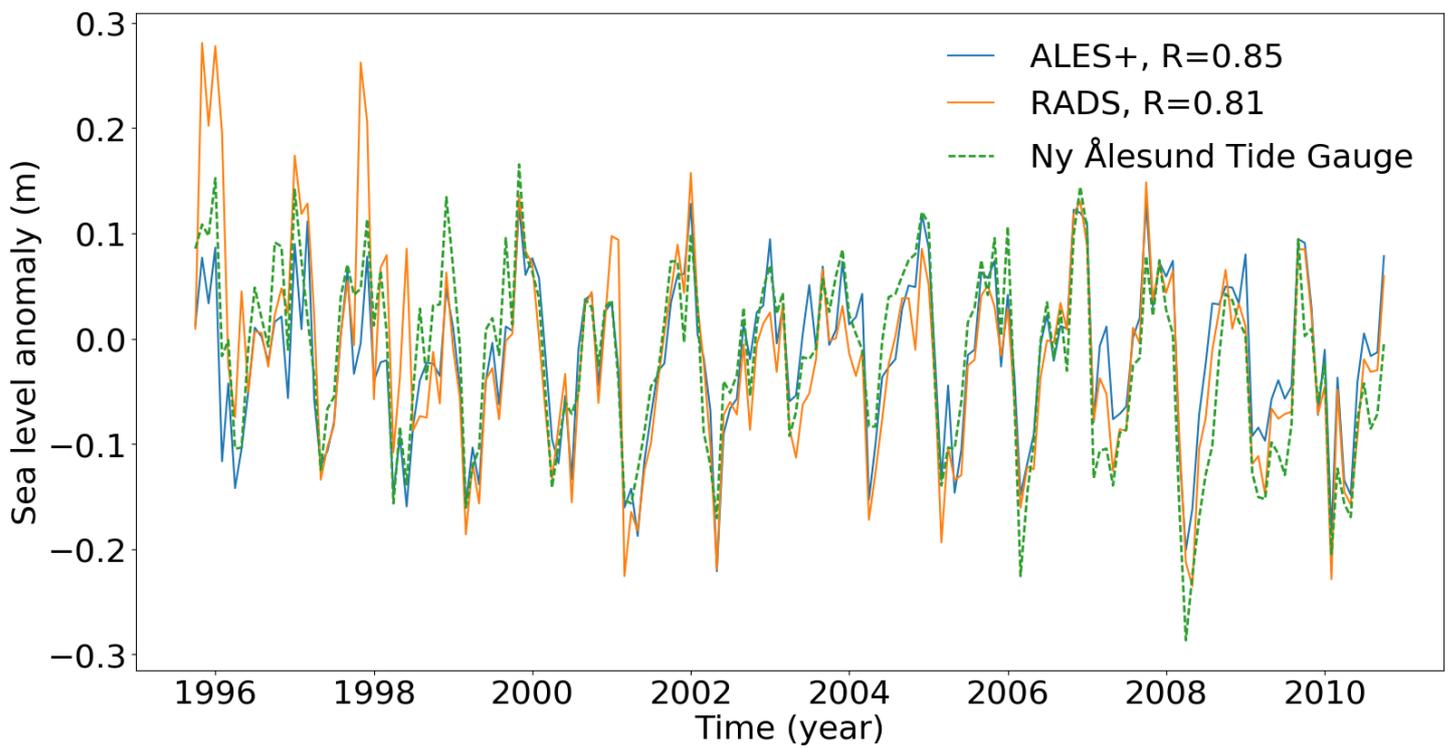


Figure 10: Time series of SLA of ALES+ and RADS data compared to the Ny Alesund TG. The gridded weekly median data are resampled to monthly SLAs. The inverse barometer effect is excluded to be comparable to the TG. R stands for the value of the correlation coefficient between the corresponding altimetry dataset and the TG.

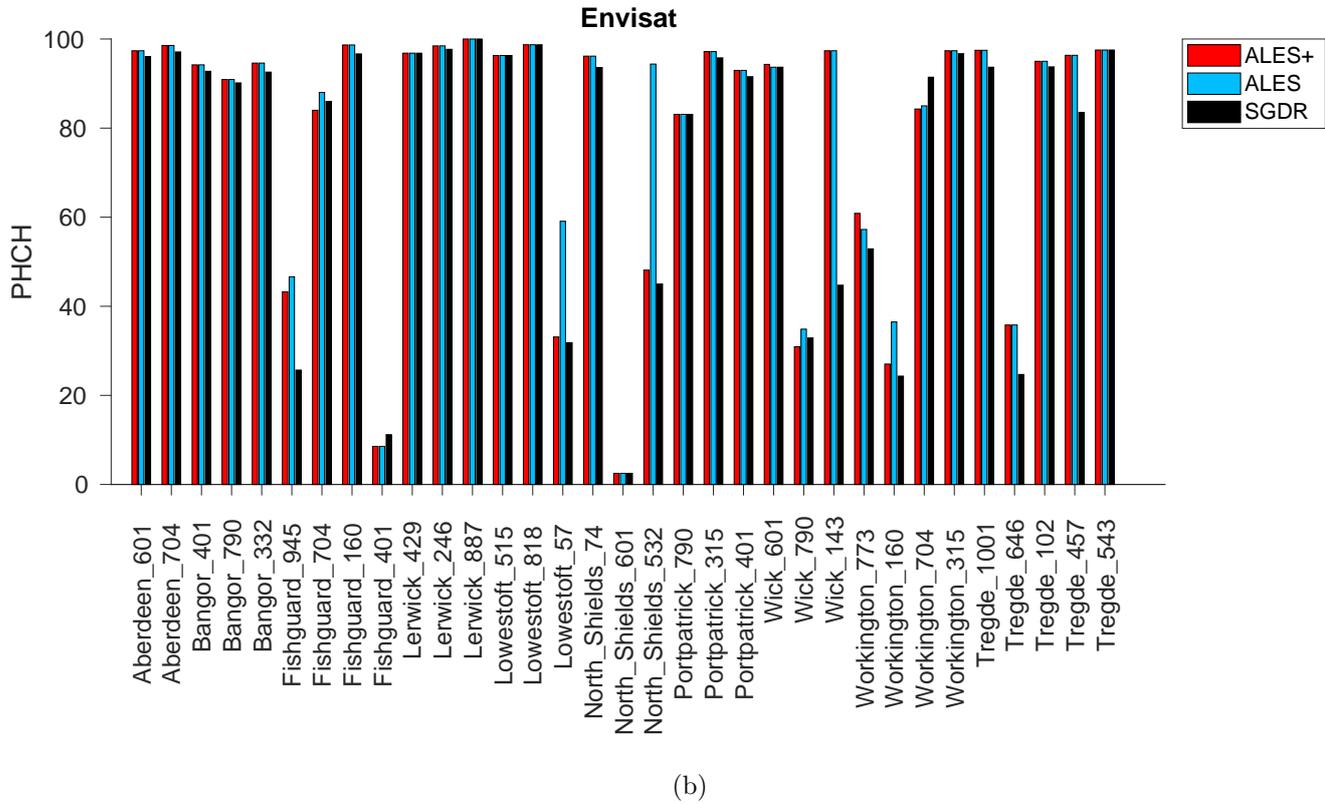
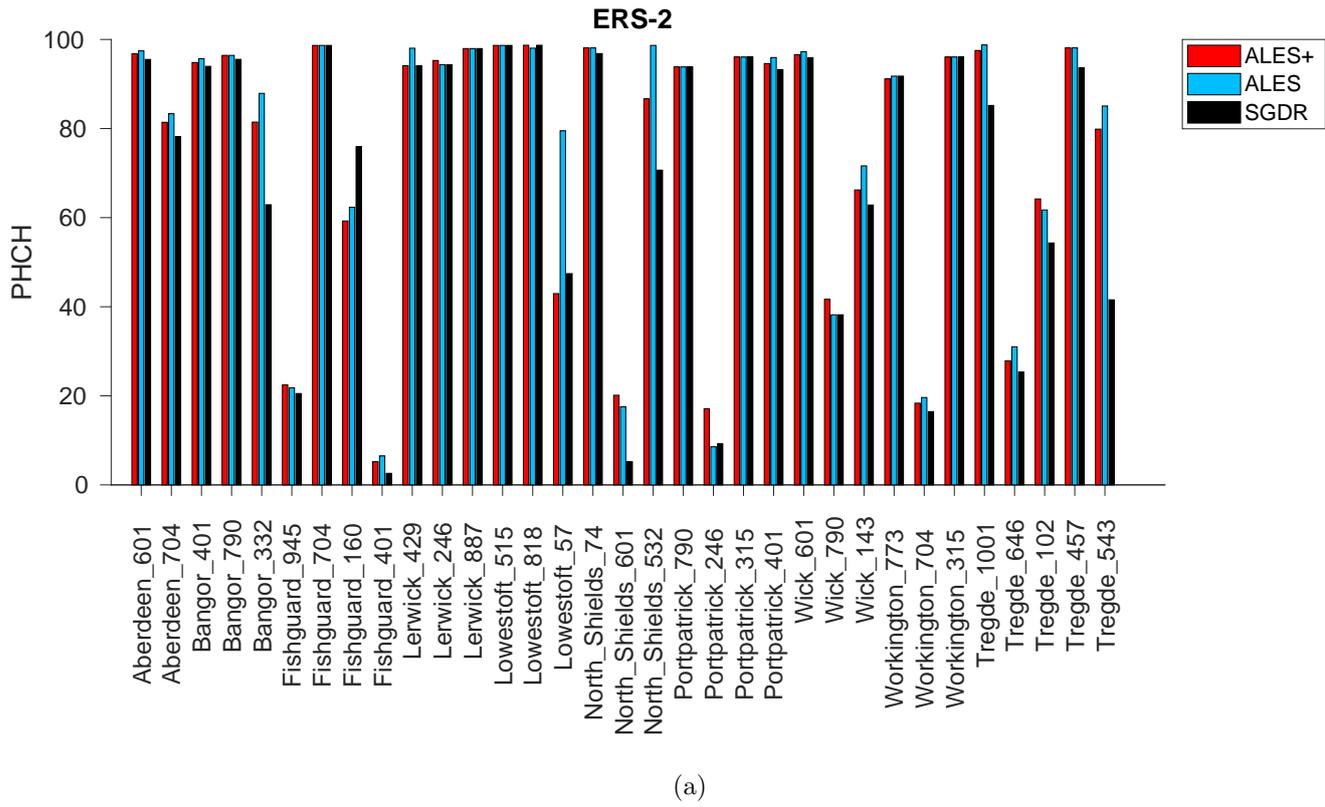
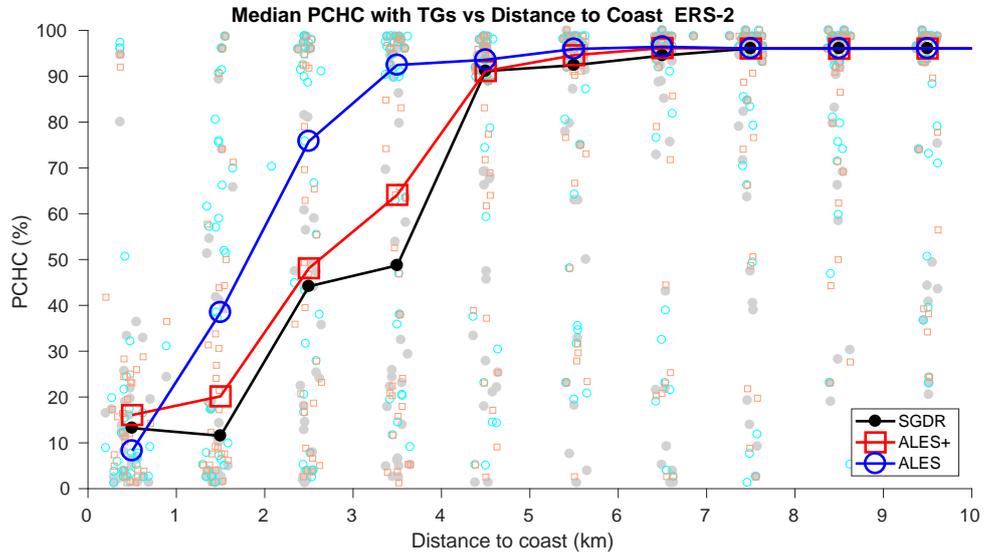
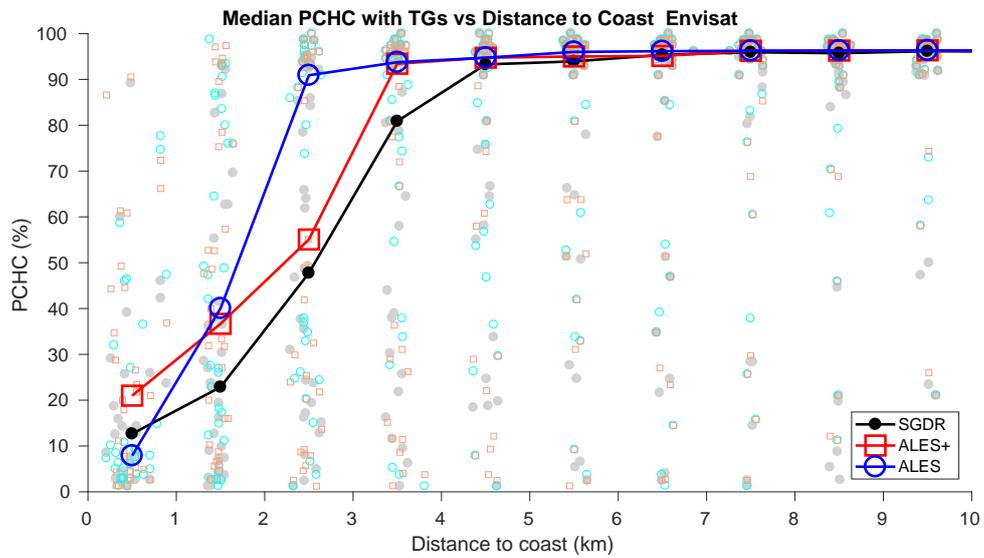


Figure 11: Median PCHC for ERS-2 tracks (upper plot) and the Envisat tracks (lower plot) within 10 km of the TG for SGDR, ALES+ and ALES (with recomputed SSB). On the x axis, the name of each TG and the corresponding satellite track numbers are shown.



(a)



(b)

Figure 12: PCHC for ERS-2 tracks (upper plot) and the Envisat tracks (lower plot) within 10 km of the TG w.r.t. the distance to the coast for SGDR, ALES+ and ALES (with recomputed SSB). Single results are shown as grey dots (SGDR), red squares (ALES+) and cyan circles (SGDR). The continuous lines show the median of the statistics.

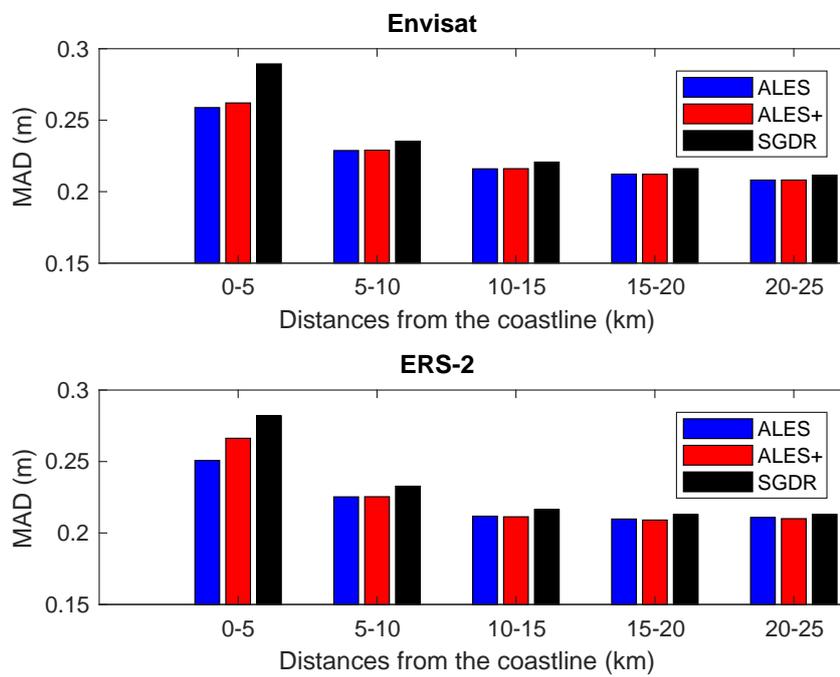
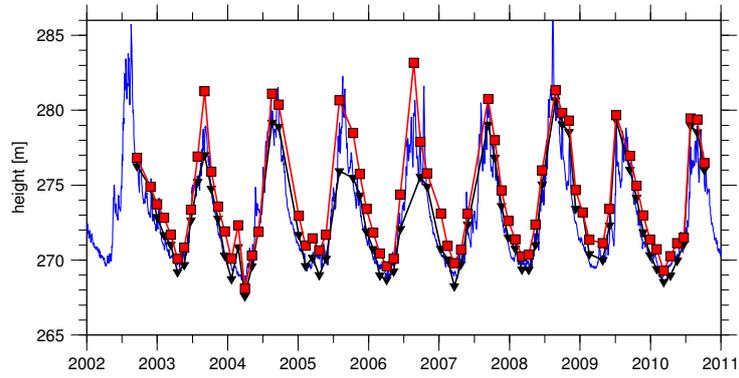
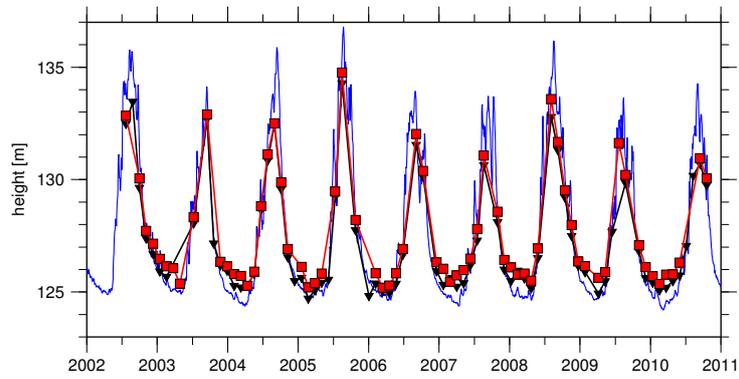


Figure 13: Median Absolute Deviation between GOCO5s geoid heights and SSH data retracked with ALES, ALES+ and SGDR in 5-km wide distance bands.

Luang Prabang



Mukdahan



Kratie

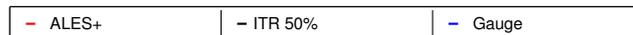
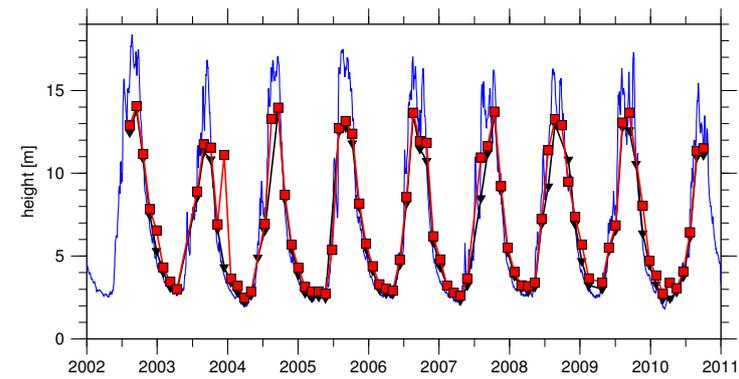


Figure 14: Visual comparison of water level time series in the Mekong river from Envisat retracked by ALES+ (red squares), Envisat retracked by Improved Threshold Retracker at 50% and data from three gauges.

528 5. Conclusion

529 In this study, we have presented a homogenous retracking strategy that uses the same
530 functional form to fit signals reflected back from leads in the sea ice pack and open ocean.
531 The algorithm named ALES+ is applied to ERS-2 and Envisat missions and is based on
532 modifications to the ALES algorithm described in Passaro et al. (2014). Thanks to a
533 preliminary step aimed at estimating the slope of the trailing edge, it is able to adapt
534 the fitting to specular echoes. As a result of a subwaveform strategy aimed at limiting
535 the impact of the noise in the trailing edge and to a recomputed SSB correction, it is
536 able to decrease the high-frequency noise by over 1.1 cm in the open sea unaffected by
537 sea ice. Even considering only peaky waveforms, range retrieval by ALES+ is over 2 cm
538 more precise than the available solution used in previous studies to estimate sea level
539 from leads (the sea ice retracker).

540 The validation against a TG situated on the Svalbard islands demonstrates that
541 ALES+ can improve the quality and the amount of data of the sea level records at
542 high-latitudes. The improvement is brought by the retracking of non-standard ocean
543 waveforms and the use of high-frequency data instead of 1-Hz averages, which are of lim-
544 ited use at high-latitudes given that most of the leads are narrower than 1 km (Lindsay &
545 Rothrock, 1995; Kwok et al., 2009). ALES+ is able to decrease the error on the sea level
546 estimation of the sea ice-covered ocean up to a comparable level with the open ocean and
547 therefore should be used in the next steps of the research to update the sea level record
548 in the Arctic and Antarctic ocean.

549 The lower noise of ALES+ in the open ocean could be used to study mesoscale struc-
550 tures and a spectral analysis should be able to reveal if this can be useful to solve at
551 least partially the noise problems that affect standard altimetry at these scales (Dibar-
552 boure et al., 2014). The improvements obtained by recomputing the SSB using ALES+
553 estimations could be even higher if a new SSB model is recomputed specifically for this
554 retracker.

555 A validation against coastal TGs has demonstrated that ALES+ improves the quality
556 of sea level retrievals in the last 6 km within the coastline compared to the standard open
557 ocean retracking. For coastal studies, ALES still overperforms ALES+. As a possible
558 improvement to ALES+, future studies will seek a better strategy for the leading edge
559 detection in order to avoid that peaks in the trailing edge, typical of coastal waveforms,

560 could be interpreted as peaky leading edges by the algorithm.

561 A preliminary validation has shown that ALES+ time series of water level of the
562 Mekong River are very highly correlated with in-situ data. Nevertheless, the typical
563 retracker used for inland waters (improved threshold) have better statistics, mainly due
564 to outliers still present in ALES+. Future studies should further validate this application
565 and exploit the seamless transition between inland waters and open sea, in order to study
566 the sea level variations across deltas and estuaries.

567 In conclusion, ALES+ offers the chance to fit the echoes from any water surface
568 without the need to change the retracking strategy and therefore avoiding internal bias
569 corrections and calibrations. It provides a more precise and accurate sea level estimation
570 than the available sea ice and ocean retrackers for ERS-2 and Envisat in leads and in
571 open and coastal waters.

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