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Comprehensive Development, Uncertainty and Sensitivity Analysis of a Model for the Hydrolysis of Rapeseed Oil

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Abstract

A model describing the batch hydrolysis of rapeseed oil including kinetics and mass transfer at subcritical conditions is presented in this paper. The primary purpose of this model is to interpret experimental data collected from typical batch tests and to estimate model parameters. The developed model was further investigated using Monte Carlo simulations to statistically quantify the variability in the model outputs due to uncertainties in the parameter estimates. To understand which parameters in the model are responsible for the output uncertainty, a sensitivity analysis method was used (polynomial chaos expansions-based Sobol sensitivity indices). The results from the sensitivity analysis helped to identify what parameters in the model are influential, giving insight into the robustness and predictive capabilities of the model which form the basis for any model-based decision making for detailed process characterization, design, optimization and operation of the hydrolysis of rapeseed oil.

Keywords: Uncertainty Analysis, Sensitivity Analysis, Vegetable Oils, Kinetic modeling

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1. Introduction

While production of oilseed and vegetable oils, with an estimated production of 769 million metric tons per year (2017/2018 forecast), are small compared to primary petrochemicals, they are an important component in today's commodities market [1]. To a large extent, this is due to the high technological standard of this mature industry [2]. Generally speaking, vegetable oils are extracted from soybeans, palm fruit, sunflower, coconuts, rapeseed, cottonseed, olives, flax, castor seed and groundnuts, making them the most important renewable raw materials for the chemical industry [3].

Vegetable oils are primarily triglycerides, i.e., triesters of long-chain saturated and unsaturated fatty acids with glycerol. Basic oleochemicals (chemicals derived from vegetable oil and animal fats) are free fatty acids, methyl esters, fatty alcohols, and fatty amides as well as glycerol as by product [4]. Fatty acids of different chain length, saturated and unsaturated, have been produced through hydrolysis on an industrial scale for more than 130 years (Lemmens Fryer's Process, Budde and Robertson's Process, Ittner's Process, Twitchell Process, etc.) [5]. The hydrolysis of fats and oils also produces several important industrial chemicals including monoglycerides, diglycerides, and glycerol as side-products [6]. The existing industrial and commercial process hydrolyzes oils to fatty acids and glycerol at temperature and pressure of about 250°C and 50 bar within a few hours to achieve conversions between 96% and 99% [7, 8].

The main products of the oleochemical industry are for human consumption (ca. 80%) and nonfood applications (ca. 20%) such as detergents, cosmetics, plastics, or biofuels. Because of their importance in the preparations of further derivatives and with a fast-growing market for bio-based products, demand for these products is expected to grow around the world [9]. For example, the global market for natural fatty acids reached US\$17.1 billion and US\$18.3 billion in 2014 and 2015, respectively. This market is expected to grow at an annual growth rate of 7.1% to US\$25.7 billion for the period 2014-2019 [10]. Hence, it has become more imperative for industry to better respond to consumer needs

by understanding the chemical transformations involved in the processing of vegetable oils.

1.1. Previous modeling efforts

The hydrolysis of oils and fats is an important processing route for the chemical industry. In this regard, several authors have developed kinetic models for the hydrolysis reaction of triglycerides [11, 12, 13, 14, 15]. The process for hydrolyzing oil by using water is influenced by both mass transfer between the phases and by the kinetics of the reactions. Processes at subcritical conditions are conducted with water in a temperature range of 100 to 374°C under sufficient pressure (below the critical point) to keep the water in the liquid state. Conventional industrial hydrolysis of oils and fats is generally conducted under subcritical pressures close to 45 bar and temperatures around 250°C for a maximum period of 2 hours with high yields (96-99%). The resulting products are extremely dark fatty acids and an aqueous solution rich in glycerol, which need to be re-distilled for color removal and purification [?]. The hydrolysis of triglycerides can be carried out batchwise (Twitchell process) or continuously (Colgate Emery process) [16].

Currently, the continuous hydrolysis of triglycerides allows the industrial production of fatty acids by the action of water vapor in a spray column at high pressures [17]. The reaction is non-catalyzed with conversions of triglycerides up to 99% after 1 to 3 hours in the reactor [18]. The glycerol formed during the hydrolysis is continuously extracted from the reaction medium.

[19, 20] found that the conversion of this reaction is dependent of the temperature. [6] described the autocatalytic behavior of the reaction in a batch reactor, with the assumption that the reaction occurs in the bulk of the oil phase. Such behavior had been attributed to the elevated ion product of water at high temperature [6]. [13, 14, 15] proposed a model to describe the biphasic hydrolysis by using a combined mass transfer and kinetic approach. The authors also investigated the reaction in both batch and continuous mode and proposed a three-step reversible reaction mechanism for the hydrolysis of tri-,

di- and monoglycerides [13, 14, 15]. [12] developed a second-order chemical reaction model and suggested an autocatalytic mechanism due to the action of generated fatty acids in the aqueous phase that subsequently act as acid catalyst in subcritical water [12]. More recently, [21] presented a kinetic study for the hydrolysis of sunflower oil under subcritical conditions in a PFR, where information on the different kinetic regimes the reaction exhibits as well as on the rate parameters was also provided. Additionally, the hydrolysis at low/middle temperatures over solid acid catalysts was discussed by [22]. In their study, the rates of hydrolysis were increased by the action of solvents and phase transfer agents.

Nevertheless, after a revision of the technical process development of hydrolysis of triglycerides one finds that some basic facts related to the thermodynamics, mass transfer, and kinetics inherent to the biphasic nature of the process have only been partially recognized due to the rather harsh physical conditions at which tri-, di-, and monoglycerides are exposed to during their hydrolysis. In the literature, the experimental data available which concerns the reactions needed for the design and analysis of processes which involves lipid technology are, in the best case scenario, scarce and not conclusive such as, solution and reaction properties of the species involved, extent of miscibility, phases where reactions occur and the reaction and mass transfer mechanisms. Moreover, the mathematical models used to correlate the behavior of reactions with phenomena are not accurate enough and are not used for validation. Hence, these models are not predictive in nature, which limit their scientific and industrial applicability. Hence, only limited information is available [23]. Besides, another disadvantage of the available models in the open literature is, to the best of our knowledge, that none of the recent studies has been analyzed and thoroughly validated.

Kinetic modeling and validation of biphasic reactions, specifically the hydrolysis of vegetable oils at subcritical conditions, is complicated due to the heterogeneous nature of the system and the lack of experimental information. Moreover, these task depends strongly upon selecting accurate estimation and

simulation methods. Missing or insufficient physical properties and operating parameters can weaken the accuracy of a model or even prevent one from simulating it [24]. Hence, it is very important to find and use good values for
95 models, parameters and properties. In this way, integrating experimentation and modeling of chemical processes is a relevant validation strategy for improving property and process modeling as well as designing and optimizing the reaction and recovery of high value added products.

In this work, a problem-specific model was proposed to evaluate its applica-
100 bility and predictive capabilities. In the modeling of biphasic reaction systems, a model can be used for studying the behavior of the different species within one phase, defining the distribution of species between two phases, or predicting the effect of process conditions on reacting species or reaction rates. The challenges presented by the absence of accurate models for this reaction and process
105 can be overcome by collecting data through experiments, rigorous mathematical modeling, uncertainty and sensitivity quantification, thermodynamic analysis of reactions and mixtures, simulation of technologies and scenarios, and analysis of fluid flow behavior in industrial settings. By applying these methodologies, it is possible to represent accurately a studied system. In this way, the production
110 of fatty acids can be analyzed in terms of its phenomena, design variables and process parameters as a whole. Furthermore, the results can be used to validate and improve property and process modeling.

This model describes batch runs with a reasonable number of parameters and degree of accuracy. Monte Carlo simulations were run to identify the work-
115 ing bounds and the cases where the model is most accurate under uncertainty in the parameter estimates and model outputs. Furthermore, a sensitivity analysis method based on variance was used in order to quantify how much of the variance in the model output each uncertain parameter is responsible for.

2. Model development

2.1. System phenomena relevant for modeling

The hydrolysis of triglycerides is generally considered a three-step set of consecutive, reversible reactions in which one mole of glyceride is generated and consumed as seen in (Reaction 1) - (Reaction 3). In water at high temperature, this hydrolysis reaction with its backward reaction occurs without any catalyst. In this system of reversible reactions, a molecule of Triglyceride (TG) is hydrolyzed to one molecule of Diglyceride (DG) and one molecule of Fatty Acid (FA). DG is subsequently hydrolyzed to Monoglyceride (MG) which is further hydrolyzed to Glycerol (Gly), producing three molecules of FA in total [14, 25].

The following reactions present the three-step vegetable oil hydrolysis reaction:

130

However, as presented by Nouredini et al, the reaction described by (Reaction 4) can take place at high temperatures (180°C-280°C) [26].

As a result of its heterogeneous nature, the hydrolysis reaction is affected not only by the chemical kinetics but also by the rate of mass transfer between the oil and water phase. Other important variables which are affecting the process are temperature, pressure, density, viscosity, and geometry of reactor. Since the polar water and non-polar TG form two immiscible phases, one component

135

must diffuse into the other before the reaction between them can happen. Thus,
140 both a mass transfer of water from the bulk of the aqueous phase to the organic
phase and a chemical reaction take place in the process. An increase in the
solubility of water in the oil-rich phase with high temperature as well as the
action of high agitation could overcome the interface mass-transfer resistance
due to the dissimilarity in size and polarity between triglycerides and water,
145 and consequently boost the reaction rate of hydrolysis. At subcritical condi-
tions the dielectric constant of water declines significantly as water is heated at
constant pressure. At such conditions, water behaves closely as organic solvent.
This means that its solvation properties are enhanced because the hydrogen
bonding between molecules of water is weaker allowing greater miscibility and
150 consequently diffusion of. Additionally, different levels of agitation can result in
the change of dimension and nature of the interfacial area between organic and
aqueous phase.

[19] observed that in the beginning of the reaction, a water in oil emulsion
is formed and the reaction proceeds slowly due to mass transfer limitations. As
155 the reaction continues, the emulsion breaks down and the reaction rate increases
significantly. This is because the fatty acid content in the oil increases due to the
reaction, which then acts as an acid catalyst. Consequently, the overall reaction
rate expression should consist of the mass transfer rate, the chemical reaction
rate and include explicitly the solubility of water in the oil phase depending on
160 its composition.

According to the two-film theory, an interface separates the phases and there
is one film in either phase that adheres to the interface [27, 28]. Mass transfer
and reaction occur through the following consecutive steps as proposed by [29]
for a high-pressure oil-hydrolysis countercurrent spray reactor:

- 165 1. Water in the aqueous bulk diffuses through the aqueous film.
2. Water diffuses through the liquid/liquid interface.
3. Water diffuses through the oil film to the oil phase bulk where the reaction
takes place.

4. Water reacts with the tri-, di-, and monoglycerides forming fatty acids and glycerol.
5. Fatty acids dissolve in the oil phase with the unreacted tri-, di-, and monoglycerides while glycerol diffuses back to the aqueous phase. The aqueous bulk is composed of water, glycerol, and very low amounts of TG , DG , MG , and FA .

The representation of the mass transfer mechanism is shown in Figure 1.

Figure 1: Mass transfer and reaction processes based on the two film theory for the hydrolysis of oils

2.2. Mathematical formulation

The general modeling objective followed in this work is that the model should be sophisticated enough to describe the complexities of the hydrolysis of vegetable oil, but the parameters should be based on measurable phenomena to a possible extent.

1. Two phases are present: aqueous (polar) and oil (non-polar) represented by the subscripts *aq* and *oil* respectively. All the reactions occur in oil phase.
2. Reactions are elementary and consecutive.
- 185 3. As the reactions are reversible, *TG*, *DG*, and *MG* are present at the chemical equilibrium.
4. Partition of water and glycerol among the two phases.
5. Mass transfer phenomena is described by Whitman's two-film theory [30].

Based on the reaction scheme presented in (Reaction 1) to (Reaction 4),
 190 the following kinetic equations are proposed:

Where k_i is the reaction rate constant for component i .

In order to model the batch hydrolysis, the expression for every species involved in the reaction should be determined. The reaction rates can be described by the expressions in Equations (1) - (4). The mole balances for the aqueous
 195 and oil phases become:

- Aqueous phase

$$\frac{dn_{H_2O}^{aq}}{dt} = -J_{H_2O}^{aq} \cdot V_{aq} \quad (5)$$

$$\frac{dn_{Gly}^{aq}}{dt} = J_{Gly}^{aq} \cdot V_{aq} \quad (6)$$

- Oil phase

$$\frac{dn_{TG}^{oil}}{dt} = (-R_1 - R_4) \cdot V_{oil} \quad (7)$$

$$\frac{dn_{DG}^{oil}}{dt} = (R_1 - R_2 - 2 \cdot R_3) \cdot V_{oil} \quad (8)$$

$$\frac{dn_{MG}^{oil}}{dt} = (R_2 - R_3 - R_4) \cdot V_{oil} \quad (9)$$

$$\frac{dn_{FA}^{oil}}{dt} = (R_1 + R_2 + R_3) \cdot V_{oil} \quad (10)$$

$$\frac{dn_{H_2O}^{oil}}{dt} = (-R_1 - R_2 - R_3 + J_{H_2O}^{oil}) \cdot V_{oil} \quad (11)$$

$$\frac{dn_{Gly}^{oil}}{dt} = (R_3 - J_{Gly}^{oil}) \cdot V_{oil} \quad (12)$$

The equations which describe the mass transfer of water and glycerol from and to the two phases are as follows:

$$J_{H_2O}^{aq} = k_{1L,a} \cdot \left(C_{H_2O}^{aq} - m_{H_2O} \cdot C_{H_2O}^{oil,*} \right) \quad (13)$$

$$J_{Gly}^{aq} = k_{2L,a} \cdot \left(C_{Gly}^{aq} - m_{Gly} \cdot C_{Gly}^{oil,*} \right) \quad (14)$$

$$J_{H_2O}^{oil} = k_{1L,a} \cdot \left(C_{H_2O}^{oil,*} - C_{H_2O}^{oil} \right) \quad (15)$$

$$J_{Gly}^{oil} = k_{2L,a} \cdot \left(C_{Gly}^{oil,*} - C_{Gly}^{oil} \right) \quad (16)$$

When one assumes steady-state, the interfacial concentration (C_i^*) can be calculated by solving the following balance for the i th component:

$$J_i^{aq} \cdot V^{aq} = J_i^{oil} \cdot V^{oil} \quad (17)$$

200 By solving Equation (17), it is possible to obtain:

$$C_i^{oil,*} = \frac{V^{aq} \cdot k_{iL,a} \cdot C_i^{aq} + k_{iL,a} \cdot V^{oil} \cdot C_i^{oil}}{k_{iL,a} \cdot V^{oil} + V^{aq} \cdot k_{iL,a} \cdot m_i} \quad (18)$$

In the absence of experimental data for the liquid-liquid equilibrium, Excess Gibbs energy-based activity coefficients are used to predict the partition coefficient m . In this study the modified UNIFAC (Dortmund) model developed by Gmehling et al. is applied for the calculation of the equilibrium compositions of the two liquid phases and partition coefficients [31, 32, 33, 34, 35]. This method
 205 was chosen due to its large range of applicability and the reliable results predicted for properties related to phase equilibria of systems involving vegetable oils [36]. Moreover, thermodynamic models such as NRTL, UNIQUAC, SAFT or CPA require specific binary interaction parameters obtained by regression and extrapolation of experimental phase equilibrium data of systems containing
 210 tri-, di- and monoglycerides which, unfortunately, are not available in the open literature. In order to solve the mass transfer equations, it is also necessary to define the partition coefficient for both water and glycerol. . These calculations are carried out by using the iterative algorithm proposed by [37], and it is
 215 summarized in the Supporting Information section of this work.

Volumes of oil and aqueous phase are calculated by using the following equation:

$$V_{oil} = \sum_{i,oil} \frac{n_{i,oil}}{\rho_i} \quad V_{aq} = \sum_{i,aq} \frac{n_{i,aq}}{\rho_i} \quad (19)$$

Densities of components (ρ_i) are calculated by using polynomial fittings of experimental data of density versus temperature for the desired range. Corre-
 220 lation parameters for these polynomials have been obtained from the *CAPEC*

Lipids Database [38]. In brief, the mathematical model has 8 variables, i.e. moles, and it contains 10 parameters which are estimated from dedicated experiments.

3. Experimental materials and methods

225 3.1. Chemicals

Rapeseed oil purchased from Scandic Food A/S (Nørre Aaby, Denmark) and deionized water (18 Ω) were used for the hydrolysis experiments. n-Heptane [CAS 142-82-5], Acetic acid [CAS 69-19-7], Isopropanol [CAS 67-63-0], and tert-Butyl methyl ether [CAS 1634-04-4] were used for HPLC-Analysis and were
230 purchased from Sigma-Aldrich Denmark ApS (Brøndby, Denmark).

3.2. Batch experiments

Hydrolysis reactions were run in a 300 ml Hastelloy C-276 jacketed reactor with ceramic band heaters (Parker Autoclave Engineers, Model 300 ml HC EZE-Seal). The reactor includes a spiral cooling coil to provide a mean of
235 removing heat from the vessel to control the reaction and for cooling the reactor at the end of every experiment. This coil consists of multiple loops wound in the inside diameter of the vessel around the shaft guide. The autoclave was sealed and flushed 3 times with 5 bar N_2 and 6 bar H_2 to remove any traces of oxygen. The reactor is equipped with a PID controller to monitor and control
240 temperature and agitation speed. A dip tube connected to a valve was used for withdrawal of liquid samples by the action of pressure difference. This procedure was carried out every 30 minutes. Approximately 2 ml of sample were retrieved from the reactor into a 5 ml vial which was put immediately in ice-water for several minutes and analyzed. The collection of samples in multiphase systems
245 at high pressure presents many challenges. The most difficult one is how to get a representative sample from the system. In this work, the only solution to this problem was to collect the sample using the sampling port, separate the two phases, measure each individually in weight and volume to verify mass balances,

and then recombine them for further analysis. A scheme of the set-up used is depicted in Figure 2. 11 experiments were carried out based on a Box-Behnken design for three factors (temperature, oil-to-water ratio, and agitation speed) and an experimental runtime of 6 hours as shown in Table 1 [39].

Table 1: Experimental design (validation sets are highlighted)

Experimental conditions			
Experiment	Temperature ($^{\circ}\text{C}$)	Water-to-oil ratio	Agitation (rpm)
1	180	15	360
2	180	40	360
3	280	15	360
4	280	40	360
5	180	27.5	120
6	180	27.5	600
7	280	27.5	120
8	280	27.5	600
9	230	15	120
10	230	15	600
11	230	40	600

The initial time of each experiment was defined as the point of time when oil and water reached the operating temperature (approximately 18 minutes).

3.3. HPLC Analysis

Collected samples were analyzed by following the procedure developed by [40], and modified by [41]. 40 μL of the sample were injected in the HPLC (Ultimate 3000, Dionex A/S, Hvidovre, Denmark) to analyze TG, DG, MG, and FA. The separation of the compounds was performed in a cyanopropyl column (0.25 x 0.004 m) (Discovery, Cyano, Sigma Aldrich A/S, Brøndby, Denmark), U3000 auto-sampler, TCC-3000SD column oven, U3400A quaternary pump modules, and a Corona Charged Aerosol Detector (Thermo Scientific, MA, United States). A binary gradient program was run with the use of three solvents (99.6% v/v tert-Butyl methyl ether, 0.4% v/v Acetic acid and, Isopropanol). The detection of the compounds was achieved by a Corona Charged Aerosol Detector from Thermo Scientific Dionex (Chelmsford, MA) with pressurized N_2 .

Figure 2: Reactor setup used for the hydrolysis of rapeseed oil

4. Parameter estimation, uncertainty and sensitivity analysis

4.1. Sequential and simultaneous parameter estimation

For the datasets collected in the experiments, kinetic and mass transfer
 270 parameters were estimated by applying the Levenberg-Marquardt algorithm for
 the non-linear global fitting problem. Thus, the Levenberg-Marquardt algorithm
 presents the simultaneously estimated parameters, the value of the residuals and
 the Jacobian matrix by minimizing the objective function in order to get the
 lowest sum of squared residuals for the kinetic and mass transfer parameters:

$$\theta = \arg \min \sum_i \left(y_i^{\text{exp}} - y_i^{\text{pred}} \right)^2 \quad (20)$$

275 In Equation (20) θ are the estimated parameters, y_i^{exp} the measurement, and
 y_i^{pred} the obtained value of parameter i .

This preliminary estimation gives an initial guess for the simultaneous estimation of parameters which is carried out as an ordinary non-linear regression problem.

280 *4.1.1. Covariance-based uncertainty analysis of parameter estimation and out-
put prediction*

The underlying assumption is that the errors are normally distributed. The uncertainty of the parameter estimates is based on the covariance matrix, $COV(\theta)$, which is obtained through first linear approximation as described in the work-
285 flow proposed by [42]. The covariance matrix $COV(\theta)$ is estimated by Equation (21):

$$COV(\theta) = \frac{S(\theta)}{N-p} \left(\left(\frac{d\mathbf{y}}{d\theta} \right)^T Q_m^{-1} \left(\frac{d\mathbf{y}}{d\theta} \right) \right) \quad (21)$$

where $S(\theta)$ represents the minimum error sum of squares calculated from the Levenberg-Marquardt algorithm in the non-linear global fitting problem, $\frac{dy}{d\theta}$ is sensitivity matrix of the outputs obtained in the model ($\mathbf{y}$) with reference to
290 the model parameters (θ). Q_m is the covariance matrix of measurement errors, N is the number of experimental data used for the regression, and p is the total number of estimated parameters. In this way, the correlation between two parameters v and w can be expressed as:

$$COR(\theta_v, \theta_w) = \frac{COV(\theta_v, \theta_w)}{\sqrt{\sigma_{\theta_v}^2 \sigma_{\theta_w}^2}} \quad (22)$$

The histograms of residuals were used to verify that the residuals follow a
295 normal distribution and have a zero mean. This also allows one to evaluate the quality of the fitting by identifying the confidence regions for the parameters through the calculation of normal bivariate distributions.

*4.1.2. Monte Carlo method for uncertainty analysis of parameter estimation
and prediction*

300 In this work, the calculation of the uncertainty in the obtained parameters was carried out by applying the Monte Carlo method. This technique uses randomly sampled parameters so as to evaluate the model outputs and to obtain their distribution. In this way, it is possible to achieve global results in the uncertainty due to the large number of evaluations the model undergoes. Thus,

305 once the input parameter space is defined, the model is evaluated by obtaining the corresponding model outputs $\mathbf{y}$. The procedure for performing uncertainty analysis can be summarized as:

1. **Definition of the input parameter uncertainty:** upper and lower bounds for a model parameter are defined by its confidence intervals $\hat{\theta}$.
- 310 2. **Sampling input uncertainty:** quasi-random sampling of the parameter estimates by means of a Latin Hypercube Sampling to distribute samples evenly over the input parameter space [43].
3. **Use of the sampling matrix to evaluate the model:** simulations are performed by using the sampled input matrix obtained in the previous step. In this way, a cumulative distribution function for each model output
315 is obtained. Consequently, mean values of the model and 5th and 95th percentile calculations are used to represent the uncertainty of the model outputs.

4.2. Variance based sensitivity analysis - Sobol method

320 A variance based sensitivity analysis method uses the variance of the model outputs and decomposes it into fractions that can be related to the model parameters. These partial variances can be obtained by the decomposition of a random vector of input parameters. Then, the partial variances are normalized with the total variance to obtain the so-called Sobol sensitivity indices [44].
325 The Sobol indices are useful to quantify the importance of a parameter X_i on a model output. The Sobol indices can take values between 0 and 1. In this method, a value closer to 1 means that the contribution of the input parameter on the variance is high. The Sobol sensitivity indices also allow one to identify the total and the interaction effect among parameters on the output variance
330 for a specific input parameter [45].

The variance calculates measures on how far a set of random numbers are spread out from their mean value. The variance of a model output y is given

by:

$$V(y) = V(f(X)) = \sigma^2 = \int (f(X) - \mu)^2 - p(X) dX \quad (23)$$

where $V(X)$ is the variance, σ the standard deviation, μ the mean, $p(X)$ is
 335 the probability density function of X , and X is a random parameter.

The variance can be decomposed by using Sobol's higher dimensional model representations as follows [46]:

$$V(y) = \sum_i V_i + \sum_i \sum_{j>i} V_{i,j} \quad (24)$$

where V_i and $V_{i,j}$ are the first-order and second-order variance of the model outputs respectively.

340 Sobol indices can be obtained by normalizing the partial variances with the total variance as:

$$S_i = \frac{V_i}{V(y)} \quad S_{i,j} = \frac{V_{i,j}}{V(y)} \quad (25)$$

where S_i is the first-order sensitivity index which allows one to characterize the influence of parameter X_i on the model output. $S_{i,j}$ is the second-order sensitivity index, which allows the quantification of interactions among parameters
 345 X_i and X_j .

S_{Ti} is the total sensitivity index where the input parameter X_i is present, which can be expressed as [47]:

$$S_{TI} = S_i + \sum_j S_{i,j} \quad (26)$$

These indices can be obtained by using Monte Carlo simulations (e.g. Janssen, Sobol, or Saltelli approximation) [48, 44, 49]. However, recently developed
 350 methodologies make use of metamodels, such as polynomial chaos expansions to overcome the computational costs related to the sampling of the Monte Carlo method.

4.2.1. Polynomial chaos expansions

Polynomial chaos expansion (PCE) is a sampling-based method to determine
 355 the evolution of uncertainty in a model, which can be estimated as a sum of
 orthogonal polynomials. The main advantage of representing the model output
 as a polynomial is that it allows one to simplify and speed-up the calculations
 required.

Different polynomial types can be used to approximate the model output.
 360 This approximation depends on the type of distribution the input variable X
 follows. For example, Legendre polynomials and Hermite polynomials are used
 for rectangular and standard normal distributions respectively. The model out-
 put can be approximated with different polynomial types. The approximated
 function is defined as:

$$y = f(\mathbf{X}) \approx \sum_{a \in \mathbb{R}^M} \hat{y}_a \phi_a(\mathbf{X}) \quad (27)$$

365 where the coefficients $\hat{y}$ can be found by using Gauss-Legendre quadrature
 rules [50]:

$$\hat{y}_a \approx \sum_{k=1}^N f(x_k) \phi_a(x_k) w_k \quad (28)$$

In Equation (28) w_k represent the weights and x_k the nodes, which can
 be calculated by the polynomial distribution function of the independent input
 parameters. Both the weights and nodes can be determined by finding the roots
 370 of the polynomial function [47].

Once this approximation of the model output is obtained, the total and par-
 tial variance of the function can directly be computed due to the orthogonality of
 the polynomials [47, 51]. Once the variances are obtained, the Sobol sensitivity
 indices can be computed.

$$V_t = \sum_{\substack{a \in \mathbb{R}^M \\ a \neq 0}} \hat{y}_a^2 \quad (29)$$

$$V_i = \sum_{\substack{a \in \mathbb{R}^a \\ a \neq 0}} \hat{y}_a^2 \quad (30)$$

375 4.3. Residual analysis

The residual analysis is relevant for model validation because it allows one to verify whether the model estimates explain the variations in a dependent variable. Ideally the residuals should be small and uncorrelated. If the residuals are correlated or have any special aspect that does not seem random, there is a
380 methodical error in the model. The residuals are calculated as:

$$e = \mathbf{y} - \hat{\mathbf{y}} \quad (31)$$

Where e is a vector which contains the residuals, y are the measurements taken in a experiment, and $\hat{y}$ is the output calculated in the model.

5. Implementation and simulation environment

The implementation of the methodologies, simulations, and programming of
385 the statistical methods were coded in Matlab by using the work-flow presented by [52, 53]. [52, 54]. The algebraic differential equations proposed in the model were solved by using the built-in routine *ode23s*, while parameter estimations and regressions were performed with the use of the *fminsearch* and *lsqnonlin* algorithms in Matlab [55, 56, 57, 58]. The UQLab framework provided im-
390 plementations of PCE models and Sobol sensitivity indices, which were used in this study [47, 59]. The implementation of the above presented methods is summarized in Table 2.

6. Results and discussion

6.1. Model fitting, parameter uncertainty and correlation

395 Eight datasets obtained with the above described experimental procedure were used to estimate the model parameters through global fitting, while three

Table 2: Uncertainty and sensitivity analysis method

#	Step	Description	Output
1	Parameter estimation	Parameters to fit the model	θ_0
		Identification of parameter	$\hat{\theta}_R$
		Correlation matrix	R_θ
		Confidence interval for parameters	σ
2	Uncertainty analysis	Prediction uncertainty of the model	5 th and 95 th
3	Sensitivity analysis	Sobol sensitivity indices	S_i and S_{T_i}
		Polynomial chaos expansions	V_i and V_T
4	Residual analysis	Simulations with estimated parameters	
		Probability distribution of residuals	
		Compute the autocorrelation function	

are used for model validation. Model fits for the validation sets as well as the parameter estimation are presented in Figure 3 and Table 3.

The performance of the model fits for the validation sets during the reaction
400 times is shown in Figure 3, where data is provided in terms of moles of species.
It can be seen that the quality of the model fits is high. The quality of the model
fits and the experimental data is important in order to ensure that the model
gives a true measure of the real system. In this regard, the Mean Absolute Error
was quantified to measure the average magnitude of the errors in the predictions
405 provided by the proposed model for the experimental validation sets. For the
studied model outputs n_{TG} , n_{DG} , n_{MG} and n_{FA} the Mean Absolute error was
0.0042 moles, 0.0038 moles, 0.0037 moles and 0.0187 moles respectively, which
can be considered as low. These fits were obtained by estimating 8 kinetic and 2
mass transfer parameters present in the developed mathematical model. Since
410 the estimation error obtained by the standard deviation is low, it is possible to
say that the estimated values are accurate [54].

The proposed model captures the behaviour for the four analyzed compo-
nent, although the prediction for DG and MG mismatches the experimental
data. However in Figure 3, the experimental amount of moles of validation set
415 1 (180°C - 1:15 oil-to-water molar ratio) shows significant mismatches, when it

comes to the prediction of MG which is much higher than the amount predicted by the model. The model mismatches observed can be related to changes in the phenomena which were not modeled such as viscosity and due to the large generation of emulsifying agents such as DG and MG , which in addition to forming

420 hydrogen bonds, can be combined in the mixture with small amounts of water and glycerol changing then the distribution of phases as reported by Wang et al [60]. At 180°C - 1:40 oil-to-water molar ratio - 360 rpm, there is a higher amount of FA produced which is in agreement with previous research, since it is known that high amounts of water lead to higher conversion rates [60, 12, 13].

425 The mean of the estimated parameters, their standard deviation σ , and correlation coefficients are shown in Table 3. Once parameter estimates are obtained, it is necessary to determine how specific they are in relation to the experimental data used. When two parameters are highly correlated, a change in the model output can be mitigated by a change in the value of the other

430 parameter. As seen in Table 3, some of the parameters are highly correlated, which prevents to find a unique estimate of the parameter value.

Figure 3: Global fitting and experimental data for the hydrolysis at (—) 180°C - 1:15 oil-to-water molar ratio - 360 rpm, (—) 180°C - 1:27.5 oil-to-water molar ratio - 600 rpm and (—) 180 °C-1:40 oil-to-water molar ratio-360 rpm.

Table 3: Mean, standard deviation and correlation matrix for the parameter estimation.

θ	Mean		Correlation matrix									
			k_1	k_{-1}	k_2	k_{-2}	k_3	k_{-3}	k_4	k_{-4}	$k_{1L,a}$	$k_{2L,a}$
k_1	2.029	0.101	1.000									
k_{-1}	1.919	0.208	0.655	1.000								
k_2	2.251	0.203	0.112	0.013	1.000							
k_{-2}	4.236	0.528	0.123	-0.137	0.931	1.000						
k_3	1.173	0.057	0.059	0.168	-0.079	-0.059	1.000					
k_{-3}	0.395	0.031	-0.103	-0.292	-0.092	-0.029	0.603	1.000				
k_4	2.464	0.128	-0.138	0.096	-0.111	-0.185	-0.001	-0.155	1.000			
k_{-4}	1.75	0.102	-0.268	-0.431	-0.302	-0.262	-0.111	0.063	0.068	1.000		
$k_{1L,a}$	0.319	0.025	-0.773	-0.424	-0.524	-0.499	-0.063	0.061	0.191	0.292	1.000	
$k_{2L,a}$	0.772	0.13	-0.273	-0.222	0.063	0.182	-0.426	-0.242	-0.336	0.054	0.255	1.000

For example, k_1 has a high negative correlation with $k_{1L,a}$, which means that the kinetic constant related to the consumption of triglycerides has a negative effect on the mass transfer coefficient of water. Our study also shows that if the value of k_1 increases, $k_{1L,a}$ decreases to obtain a good fit. Similar analyses can be done for k_1 and k_{-1} (consumption and generation of TG in (Reaction 1)), k_{-1} and k_{-4} (consumption and generation of DG in (Reaction 1) and (Reaction 4)), k_2 and k_{-2} (generation and consumption of MG in (Reaction 2)), k_{-2} and $k_{1L,a}$ (consumption of MG in (Reaction 2) and mass transfer of water respectively), k_3 and k_{-3} (generation and consumption of MG). This correlation is expected, since the hydrolysis proceeds as a set of parallel and sequential reactions, which implies poor identifiability. In this regard, more measurements should be performed so as to be included in the parameter estimation. These measurements can be moles of glycerol and water as well as separate measurements of mass transfer rates between phases without the complexity of ongoing reaction.

It is worth mentioning that the uncertainty results presented in this work are conditional to the range defined by the parameter uncertainty alongside their correlation coefficients. Therefore, the results need to be handled accordingly within those conditions [52]. In this context, the results provided by the uncertainty analysis and parameter estimation are of local nature and are valid in the neighborhood at which the minimization was performed in the parameter estimation. To overcome the identifiability issues, it is then necessary to

find a unique combination of estimated parameters which provide low correlation and low confidence intervals. However, the major disadvantage of this approach is that those parameters that are found unidentifiable need to be estimated from independent experiments, which can be expensive. In order to generalize the results obtained, it is required to perform a sensitivity analysis based-identifiability analysis iteratively at different conditions or alternatively one could perform a global sensitivity analysis as the one carried out in this work for model improvement [61, 52]. Another valid option is to accept the model with its parameter uncertainty and use it to evaluate whether it can be applied in process engineering tasks as well as process design and optimization.

6.2. Uncertainty analysis of model predictions

The uncertainty of the calculated model outputs (n_{TG} , n_{DG} , n_{MG} , and n_{FA}) during the hydrolysis reaction can be seen in Figure 4 and Figure 5. In these figures, synthetic data generated by the evaluation of the model by using Latin Hypercube Samples is shown for the validation set (hydrolysis at 180°C - 1:27.5 oil-to-water molar ratio - 600 rpm). It is possible to observe that almost all the experimental values lay inside the working boundaries of the simulations. The tight predictions for n_{TG} and n_{FA} give an overview of the robustness of the model and quality of the fit, while the large predictions calculated for n_{DG} and n_{MG} indicate that either the model which contains deficiencies or the variables were not properly measured. In this case, a better estimation of the parameters and more experiments are necessary to get more accurate predictions for these species.

6.3. Sensitivity analysis of model outputs

For the sensitivity analysis with Sobol indices an output was needed, given our interest in determining which parameters contribute to the uncertainty of the model outputs during the time course of the reaction (0.5 - 6 hours), where there are significant variations in the model outputs of the Monte Carlo simulations (Figure 4). Global calculations were also made by using the mean values of

Figure 4: Uncertainty propagation generated from the simulations based on Monte Carlo method for the selected dataset (hydrolysis at 180°C - 1:27.5 oil-to-water molar ratio - 600 rpm) (—)

Figure 5: Uncertainty propagation represented by the mean (—) and the 5th and 95th percentiles (—) of the Monte Carlo simulations for the selected dataset (hydrolysis at 180°C - 1:27.5 oil-to-water molar ratio - 600 rpm)

the outputs. This was done to rank the significance of the parameters obtained at the different conditions used in the validation sets. It should be noted that the analysis can be performed at different time points and different process
485 conditions at which case the parameter ranking can vary. In this case, the selected set of conditions was the hydrolysis at 180°C - 1:27.5 oil-to-water ratio - 600 rpm.

Results for the variance-based sensitivity analysis are expressed by two sensitivity indices: the Sobol first order sensitivity indices S_i indicate the importance
490 of each parameter considered individually, while the total sensitivity indices S_{Ti} account for both the importance of individual parameters and interactions between parameter pairs. In this study, the values of S_{Ti} are similar to S_i .

The highest sum of S_{Ti} obtained for the input parameters of n_{MG} (1.0059), as seen in Table 4, shows that the variations in outputs are motivated by first-
495 order effects of the parameters, while the second-order interaction terms contribute to only 0.59% of the variance of the model output [62] (See also Supporting Information).

Through the analysis of the sensitivity analysis for the mean values of the validation set, it can be noticed that the consumption of n_{TG} is most influenced
500 by kinetic parameters k_1 and k_{-1} in (Reaction 1) along with the mass transfer coefficient of water $k_{1L,a}$. It is explained by the fact that the mass transfer of water is bound to the reaction with n_{TG} . Hence, the resulting decrease or increase in mass transfer should then affect all the model outputs. For the parameters in the reactions related to the formation and consumption of n_{DG} , the
505 most influential parameters are k_2 and k_{-2} in (Reaction 2), while the remaining parameters are deemed irrelevant. In the case of n_{MG} , kinetic parameters k_3 and k_{-3} in (Reaction 3) have the higher impact. Consequently, the most important parameters related to generation of the product n_{FA} are the rate constants for forward reactions alongside the rate constants for reverse reactions (Reaction 1)
510 - (Reaction 3). As seen in Table 4, the parameters k_4 , k_{-4} , and $k_{2L,a}$ are little or non-influential for the model outputs coupled with the experimental data. Parameters k_4 , k_{-4} which are related to the fourth reaction step were included

in the model to account for additional reactions which occur in the system with unreacted triglycerides and generated diglycerides. In this case, its low contribu-
515 tion to the output variance could indicate that such reaction is not taken place in the reactors. In the same way, low values for the mass transfer coefficient of glycerol $k_{2L,a}$ could be related to a low generation of glycerol which therefore is not relevant in the mass transfer process. Therefore, values for these parameters can be fixed to any value within their confidence intervals without influencing
520 the model outputs. Non-influential parameters contribute to a small percentage of the total variance, which then provide criteria for model simplification.

Table 4: Sensitivity analysis with first order Sobol' indices for each model parameter for the hydrolysis at 180°C - 1:27.5 oil-to-water molar ratio - 600 rpm

Rank	Triglycerides		Diglycerides		Monoglycerides		Fatty acids	
1	k_1	0.5476	k_2	0.7355	k_3	0.6547	k_2	0.3735
2	k_{-1}	0.2339	k_{-2}	0.2149	k_{-3}	0.2185	k_3	0.1778
3	$k_{1L,a}$	0.1181	k_3	0.0234	$k_{2L,a}$	0.0591	k_1	0.1521
4	k_2	0.0671	k_{-3}	0.0073	k_2	0.0344	k_{-2}	0.1096
5	k_{-2}	0.0327	$k_{1L,a}$	0.0068	k_{-2}	0.0257	k_{-3}	0.0622
6	k_{-4}	0.0009	k_1	0.0051	$k_{1L,a}$	0.0049	$k_{1L,a}$	0.0553
7	k_3	0.0006	k_{-1}	0.0045	k_1	0.0043	k_{-1}	0.055
8	k_{-3}	0.0004	$k_{2L,a}$	0.0019	k_{-1}	0.0043	$k_{2L,a}$	0.0167
9	k_4	0.0002	k_{-4}	0.0018	k_4	0	k_4	0
10	$k_{2L,a}$	0.0001	k_4	0.0004	k_{-4}	0	k_{-4}	0
		$\sum S_i = 0.9984$			$\sum S_i = 0.9984$			$\sum S_i = 0.9978$
		$\sum S_{Ti} = 1.0016$			$\sum S_{Ti} = 1.0016$			$\sum S_{Ti} = 1.0022$

In Figure 6 and Figure 7, we show graphically the first order indices S_i obtained by Sobol's method of the mass transfer phenomena ($k_{1L,a}$ and $k_{2L,a}$) and the different reaction pathways (k_1 and k_{-1} , k_2 and k_{-2} , k_3 and k_{-3} , and
525 k_4 and k_{-4}) to the measured outputs n_{TG} and n_{FA} at different time steps. Detailed data concerning the sensitivity analysis of model outputs n_{MG} and n_{DG} is available in the Supporting Information. These indices give information about the significance of each parameter, where high values indicate higher significance and *vice versa* smaller values indicate negligible or no significance.
530 Nonetheless, total sensitivity indices S_{Ti} give information related to the first-

order effects of the parameters in the the model and the mutual interactions among parameters.

In Figure 6 and 7, we present the global sensitivity analysis results conducted as the reaction progresses. The most important insight provided by these results are the relative importance of mass transfer and kinetics parameters changes as reaction progresses. For example, in Figure 6, it is possible to notice that in the early stages of the reaction the consumption of n_{TG} is mainly sensitive to the rate constant for forward (Reaction 1) k_1 and the mass transfer coefficient of water $k_{1L,a}$, which both show a decreasing trend along time. In the beginning of the hydrolysis, the transfer of water from the aqueous phase to the oil phase accelerates the reacting process. As the reaction progresses, the main contributors are the kinetic parameters related to (Reaction 2) and (Reaction 3). In the case of n_{DG} , k_1 , and $k_{1L,a}$, they contribute greatly to the variance at 0.5 h , where they lose their relevance as the reaction progresses. Then, the most influential parameters are the kinetic related to (Reaction 2). Their significance have an appreciable change during the reaction as seen in Figure A.2. In regards to n_{MG} , the parameters associated with the consumption and generation of n_{MG} in (Reaction 2), (Reaction 3), and (Reaction 4) present the largest variations because n_{MG} participates in more reactions of the system than all the other components. As previously mentioned, the reactions are consecutive and reversible. Hence, it is possible that every group of parameters might affect the equations which govern the model differently. When it comes to n_{FA} in Figure 7, the main contributors to the sensitivity, at the beginning, are rate constant for forward (Reaction 1) and the mass transfer coefficient of water. The later is understood by the diffusion of water through the oil film to the oil phase bulk where the reaction takes place. Then, kinetic parameters related to (Reaction 1), (Reaction 2), and (Reaction 3) contribute greatly, which is explained by the fact that the mole balances involving FA do not have a mass transfer component since the generated products are assumed to remain in the oil phase, where they were generated.

A closer look to the 10 estimated parameters shows that the mass trans-

fer phenomena ($k_{1L,a}$ and $k_{2L,a}$) and the three reaction pathways (k_1 and k_{-1} (Reaction 1), k_2 and k_{-2} (Reaction 2), k_3 and k_{-3} (Reaction 3)), are the parameters which have a relatively significant effect on all the four model outputs.

565 The non-influential parameters indicate that at the given experimental conditions, they do not affect the measured outputs. Therefore such information can be used as input to prioritize the research areas, for example, in improving the design of experiments to estimate those parameters or in simplifying the model. This is relevant in particular when reparametrizing and recalibrating the model
570 for different feedstock with different initial composition (e.g. palm fatty acid distillate) or operating conditions (use of catalyst).

The results from the uncertainty analysis showed that the parameter estimates are trustworthy given the narrow working bounds obtained in the model outputs, which is of great interest for predictive purposes. It should be mentioned that the mass transfer coefficients can change during the reaction given
575 the change of the component fractions in the consumed and generated phases. Hence, the values for these are deemed as average. In this regard, uncertainty analysis helped to validate the assumption that the estimated parameters are constant during the reaction. For process development, these analysis are useful
580 when choosing type and finding optimal configurations in reactors. For example the use of batch data to predict reactor configuration residence times and conversions are easy to apply and fast to use. This analysis is therefore of considerable interest to improve the understanding of design and operating variables that increase the feasibility of vegetable oil utilization. It is because they provide
585 information that could be used to compare different modeling approaches under different operating conditions.

6.4. Analysis of residuals

The residuals are calculated based on the validation set (hydrolysis at 180°C, 1:27.5 oil-to-water mol ratio and 600 rpm) and are presented in Figure 8. The
590 errors for n_{TG} , n_{DG} , n_{MG} , and n_{FA} stay within -0.02 and 0.02 moles. If the residuals follow a standard normal distribution and are uncorrelated, the use of

the model does not yield to errors in the evaluations. The Gaussian probability plots in Figure 8 shows the distance of the residuals to a standard distribution. The third plot in Figure 8 determines if there is any information in the residuals that is not obtained when the model is evaluated. It can be seen that there are spikes in almost all plots, however, they are not significant because they do not exceed the limit set by the confidence intervals.

Figure 8: Residual analysis for the validation set (hydrolysis at 180°C, 1:27.5 oil-to-water mol ratio and 600 rpm)

7. Conclusions

In this work a model for the hydrolysis of vegetable oils in a batch reactor under subcritical conditions was developed and the parameters in the model were estimated from experimental data. The model includes mass transfer between oil and water phase and kinetics of the reversible hydrolysis reactions. The parameter estimation results showed that, while the parameter estimates were accurate, the pairwise correlation between estimates were significant for some parameters. This indicates that the available experimental data is not sufficient

to uniquely identify the mass and kinetic parameters and thus requires further and improved experiment design. A Monte Carlo based uncertainty analysis was performed to find the accuracy of estimated parameters, the mean and standard deviations of the model outputs from experimental data. This method was then
610 successfully applied to calculate the accuracy of the estimated parameters as well as their confidence intervals. We recommend this procedure for the estimation of the variance of parameters in chemical kinetics modeling. The results showed that the presented model was able to predict accurately the experimental data with a narrow confidence interval. The performed sensitivity analysis
615 detected the influential and non-influential parameters to the model outputs, which allows to validate the model and assumptions proposed. This analysis provided insights on the relative importance of parameters and their changes as the reaction progresses, being the parameters related to the mass transfer ($k_{1L,a}$ and $k_{2L,a}$) and first steps of the reacting system linked to the consumption of
620 triglycerides the most important (k_1 and k_{-1} (Reaction 1)). Since the lack of experimental data is a crucial issue in the hydrolysis of vegetable oils, this model-based analysis of data is of substantial value to provide necessary information for detailed modeling and characterization of the subcritical hydrolysis process.

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Nomenclature

630 Symbols

C_i Concentration of component i [$mol\ L^{-1}$]

DG Diglycerides

	<i>FA</i>	Fatty acids
	<i>Gly</i>	Glycerol
635	<i>H₂O</i>	Water
	J_i^j	Mass transfer rate of component i in phase j [$mol\ L^{-1}\ hr^{-1}$]
	k_i	Rate constant for forward reaction i [$L\ mol^{-1}\ hr^{-1}$]
	k_{-i}	Rate constant for reverse reaction i [$L\ mol^{-1}\ hr^{-1}$]
	$k_{1L,a}$	Volumetric mass transfer coefficient of water [hr^{-1}]
640	$k_{2L,a}$	Volumetric mass transfer coefficient of glycerol [hr^{-1}]
	m_i	Partition coefficient of component i
	<i>MG</i>	Monoglycerides
	n_i^j	Moles of component i in phase j [mol]
	R_i	Reaction rate [$mol\ L^{-1}\ hr^{-1}$]
645	t	Time [hr]
	<i>TG</i>	Triglycerides
	V_j	Volume of phase j [L]

Greek letters

	ρ_i	Molar volume of component i [$mol\ L^{-1}$]
650	θ	Estimated parameter

Subscripts and superscripts

*	Interface
<i>aq</i>	Aqueous phase
i	Component 1, 2, 3, ..., n

655 *j* Phase
oil Oil phase

References

References

- [1] G. R. List, Forecasts of oilseed and vegetable oil production, *Lipid Technology* 29 (9-10) (2017) 107. doi:10.1002/lite.201700028.
 660
- [2] J. O. Metzger, Fats and oils as renewable feedstock for chemistry, *European Journal of Lipid Science and Technology* 111 (9) (2009) 865–876. doi:10.1002/ejlt.200900130.
- [3] R. Höfer, J. Bigorra, Biomass-based green chemistry: sustainable solutions
 665 for modern economies doi:10.1080/17518250802342519.
- [4] W. Hamm, R. J. Hamilton, G. Calliauw, *Edible oil processing*, Wiley, 2013.
- [5] The Soap and Detergent Association - Glycerine & Oleochemical Division, Glycerine: an overview of terms, technical data, properties and performance, Tech. rep. (1990).
 670 URL <https://goo.gl/YaYzyX>
- [6] A. Sturzenegger, H. Sturm, Hydrolysis of Fats at High Temperatures, *Industrial & Engineering Chemistry* 43 (2) (1951) 510–515. doi:10.1021/ie50494a054.
- [7] I. M. Noor, M. Hasan, K. B. Ramachandran, Effect of operating variables
 675 on the hydrolysis rate of palm oil by lipase, Tech. Rep. 1 (2003). doi:10.1016/S0032-9592(02)00263-7.
- [8] G. Pugazhenth, A. Kumar, Enzyme membrane reactor for hydrolysis of olive oil using lipase immobilized on modified PMMA composite membrane, *Journal of Membrane Science* 228 (2004) 187–197. doi:10.1016/j.memsci.2003.10.007.
 680

- [9] A. E. Bailey, F. Shahidi, Bailey's industrial oil and fat products, John Wiley & Sons, 2005.
- [10] BCC Research, Global Markets for Oleochemical Fatty Acids Use, Tech. rep., BCC Research (2013).
 685 URL <http://bit.ly/2Imxc2p>
- [11] L. Hartman, Kinetics of the Twitchell Hydrolysis, *Nature* 167 (4240) (1951) 199–199. doi:10.1038/167199a0.
- [12] E. Minami, S. Saka, Kinetics of hydrolysis and methyl esterification for biodiesel production in two-step supercritical methanol process, *Fuel*
 690 85 (17-18) (2006) 2479–2483. doi:10.1016/j.fuel.2006.04.017.
- [13] T. A. Patil, T. S. Raghunathan, H. S. Shankar, Thermal hydrolysis of vegetable oils and fats. 2. Hydrolysis in continuous stirred tank reactor, *Industrial and Engineering Chemistry Research* 27 (5) (1988) 735–739. doi: 10.1021/ie00077a002.
- 695 [14] T. A. Patil, T. S. Raghunathan, H. S. Shankar, Thermal hydrolysis of vegetable oils and fats. 2. Hydrolysis in continuous stirred tank reactor, *Industrial and Engineering Chemistry Research* 27 (5) (1988) 735–739. doi: 10.1021/ie00077a002.
- [15] P. D. Namdev, T. A. Patil, T. S. Raghunathan, H. S. Shankar, Thermal
 700 hydrolysis of vegetable oils and fats. 3. An analysis of design alternatives, *Industrial & Engineering Chemistry Research* 27 (5) (1988) 739–743. doi: 10.1021/ie00077a003.
- [16] N. Sonntag, Fat splitting, *Journal of the American Oil Chemists' Society* 56 (11Part1) (1979) 729A–732A.
- 705 [17] I. M. Hill, Countercurrent hydrolysis of fat, uS Patent 2,480,471 (Aug. 30 1949).

- [18] J. A. Kent, et al., Kent and Riegel's handbook of industrial chemistry and biotechnology, Vol. 1665, Springer, 2007.
- [19] L. Lascaray, Industrial fat splitting, Journal of the American Oil Chemist' Society 29 (9) (1952) 362–366. doi:10.1007/BF02631459.
710
- [20] L. Lascaray, Mechanism of Fat Splitting, Industrial & Engineering Chemistry 41 (4) (1949) 786–790. doi:10.1021/ie50472a025.
- [21] R. Alenezi, G. Leeke, R. Santos, A. Khan, Hydrolysis kinetics of sunflower oil under subcritical water conditions, Chemical Engineering Research and Design 87 (6) (2009) 867–873. doi:10.1016/j.cherd.2008.12.009.
715
- [22] J. K. Satyarthi, D. Srinivas, P. Ratnasamy, Hydrolysis of vegetable oils and fats to fatty acids over solid acid catalysts, Applied Catalysis A: General 391 (1-2) (2011) 427–435. doi:10.1016/j.apcata.2010.03.047.
- [23] J. O. Metzger, U. Bornscheuer, Lipids as renewable resources: current state of chemical and biotechnological conversion and diversification, Appl Microbiol Biotechnol 71 (2006) 13–22. doi:10.1007/s00253-006-0335-4.
720
- [24] J. Frutiger, M. Jones, N. G. Ince, G. Sin, From property uncertainties to process simulation uncertainties—monte carlo methods in simsci pro/ii process simulator, in: Computer Aided Chemical Engineering, Vol. 44, Elsevier, 2018, pp. 1489–1494.
725
- [25] C. E. Goering, A. W. Schwab, M. J. Daugherty, E. H. Pryde, A. J. Heakin, Fuel properties of eleven vegetable oils, Transactions of the ASAE 25 (6) (1982) 1472–1477. doi:10.13031/2013.33748.
- [26] H. Nouredдини, D. W. Harkey, M. R. Gutsman, A continuous process for the glycerolysis of soybean oil, Journal of the American Oil Chemists' Society 81 (2) (2004) 203–207. doi:10.1007/s11746-004-0882-y.
730
- [27] G. Astarita, Mass transfer with chemical reaction, 1967.

- [28] P. Trambouze, H. Van Landeghem, J. P. Wauquier, Chemical Reactors: Design, Engineering, Operation, Chemical Engineering Science 44 (7) (1989) 1599. doi:10.1016/0009-2509(89)80040-5.
- [29] M. Attarakih, T. Albaraghtih, M. Abu-Khader, Z. Al-Hamamre, H.-J. Bart, Mathematical modeling of high-pressure oil-splitting reactor using a reduced population balance model, Chemical Engineering Science 84 (2012) 276–291. doi:10.1016/j.ces.2012.08.046.
- [30] W. G. Whitman, The two film theory of gas absorption, International Journal of Heat and Mass Transfer 5 (5) (1962) 429–433. doi:10.1016/0017-9310(62)90032-7.
- [31] J. Lohmann, J. Gmehling, Modified UNIFAC (Dortmund). Reliable Model for the Development of Thermal Separation Processes., Journal of Chemical Engineering of Japan 34 (1) (2001) 43–54. doi:10.1252/jcej.34.43.
- [32] J. Gmehling, J. Li, M. Schiller, A modified UNIFAC model. 2. Present parameter matrix and results for different thermodynamic properties, Industrial & Engineering Chemistry Research 32 (1) (1993) 178–193. doi:10.1021/ie00013a024.
- [33] J. Gmehling, J. Lohmann, A. Jakob, J. Li, R. Joh, A Modified UNIFAC (Dortmund) Model. 3. Revision and Extension, Industrial & Engineering Chemistry Research 37 (12) (1998) 4876–4882. doi:10.1021/ie980347z.
- [34] J. Gmehling, R. Wittig, J. Lohmann, R. Joh, A Modified UNIFAC (Dortmund) Model. 4. Revision and Extension, Industrial & Engineering Chemistry Research 41 (6) (2002) 1678–1688. doi:10.1021/ie0108043.
- [35] A. Jakob, H. Grensemann, J. Lohmann, J. Gmehling, Further Development of Modified UNIFAC (Dortmund): Revision and Extension 5, Industrial & Engineering Chemistry Research 45 (23) (2006) 7924–7933. doi:10.1021/ie060355c.

- 760 [36] L. P. Cunico, A. S. Hukkerikar, R. Ceriani, B. Sarup, R. Gani, Molecular structure-based methods of property prediction in application to lipids: A review and refinement, *Fluid Phase Equilibria* 357 (2013) 2–18.
- [37] H. Rachford, J. Rice, Procedure for Use of Electronic Digital Computers in Calculating Flash Vaporization Hydrocarbon Equilibrium, *Journal of*
765 *Petroleum Technology* 4 (10) (1952) 19–3. doi:10.2118/952327-G.
- [38] C. A. Diaz-Tovar, R. Gani, B. Sarup, Computer-Aided Modeling of Lipid Processing Technology, Phd thesis, Technical University of Denmark (2011).
- [39] G. E. P. Box, D. W. Behnken, Some New Three Level Designs for the
770 *Study of Quantitative Variables*, *Technometrics* 2 (4) (1960) 455. doi:10.2307/1266454.
- [40] T. A. Foglia, K. C. Jones, Quantitation of Neutral Lipid Mixtures Using High Performance Liquid Chromatography with Light Scattering Detection†, *Journal of Liquid Chromatography & Related Technologies* 20 (12)
775 (1997) 1829–1838. doi:10.1080/10826079708005545.
- [41] J. Price, B. Hofmann, V. T. L. Silva, M. Nordblad, J. M. Woodley, J. K. Huusom, Mechanistic modeling of biodiesel production using a liquid lipase formulation, *Biotechnology Progress* 30 (6) (2014) 1277–1290. doi:10.1002/btpr.1985.
- 780 [42] G. Sin, A. S. Meyer, K. V. Gernaey, Assessing reliability of cellulose hydrolysis models to support biofuel process design-Identifiability and uncertainty analysis, *Computers and Chemical Engineering* 34 (9) (2010) 1385–1392. doi:10.1016/j.compchemeng.2010.02.012.
- [43] R. L. Iman, W. J. Conover, A distribution-free approach to inducing
785 rank correlation among input variables, *Communications in Statistics - Simulation and Computation* 11 (3) (1982) 311–334. doi:10.1080/03610918208812265.

- [44] I. M. Sobol, Sensitivity estimates for nonlinear mathematical models, *Mathematical modelling and computational experiments* 1 (4) (1993) 407–414.
- 790 [45] J. Klinkert, The characterization of uncertainty for steady state multiphase flow models in pipelines, Master’s thesis, Delft University of Technology (2018).
- [46] R. C. Smith, *Uncertainty quantification: theory, implementation, and applications*, Vol. 12, Siam, 2013.
- 795 [47] S. Marelli, C. Lamas, K. Konakli, C. Mylonas, P. Wiederkehr, B. Sudret, UQLab user manual – Sensitivity analysis, Tech. rep., Chair of Risk, Safety & Uncertainty Quantification, ETH Zürich, report # UQLab-V1.2-106 (2019).
- [48] M. J. Jansen, Analysis of variance designs for model output, *Computer*
800 *Physics Communications* 117 (1-2) (1999) 35–43.
- [49] A. Saltelli, P. Annoni, I. Azzini, F. Campolongo, M. Ratto, S. Tarantola, Variance based sensitivity analysis of model output. design and estimator for the total sensitivity index, *Computer Physics Communications* 181 (2) (2010) 259–270.
- 805 [50] F. B. Hildebrand, *Introduction to numerical analysis*, Courier Corporation, 1987.
- [51] R. Al, C. R. Behera, A. Zubov, K. V. Gernaey, G. Sin, Meta-modeling based efficient global sensitivity analysis for wastewater treatment plants – an application to the bsm2 model, *Computers and Chemical Engineering*
810 127 (2019) 233–246. doi:10.1016/j.compchemeng.2019.05.015.
- [52] G. Sin, K. V. Gernaey, A. E. Lantz, Good modeling practice for PAT applications: Propagation of input uncertainty and sensitivity analysis, *Biotechnology Progress* 25 (4) (2009) 1043–1053. doi:10.1002/btpr.166.

- [53] N. H. Azim, A. Subki, Z. N. B. Yusof, Abiotic stresses induce total phenolic, total flavonoid and antioxidant properties in Malaysian indigenous microalgae and cyanobacterium (2018). doi:10.1017/CB09781107415324.004.
- [54] G. Sin, K. V. Gernaey, Data Handling and Parameter Estimation, in: Experimental Methods in Wastewater Treatment, IWA Publishing, 2016, pp. 201–234. doi:10.1017/CB09781107415324.004.
- [55] L. F. Shampine, M. W. Reichelt, J. A. Kierzenka, Solving Index-1 DAEs in MATLAB and Simulink, SIAM Review 41 (3) (1999) 538–552. doi:10.1137/S003614459933425X.
- [56] The Mathworks Inc., MATLAB and Statistics Toolbox, version 2016b (2016).
- [57] L. F. Shampine, M. W. Reichelt, The MATLAB ODE Suite, Tech. rep. URL <http://bit.ly/2Uatvzq>
- [58] T. F. Coleman, Y. Li, An Interior Trust Region Approach for Nonlinear Minimization Subject to Bounds. URL <https://ecommons.cornell.edu/handle/1813/6108>
- [59] R. Al, C. R. Behera, A. Zubov, G. Sin, Systematic framework development for the construction of surrogate models for wastewater treatment plants, Computer-aided Chemical Engineering (2018) 1909–1914doi:10.1016/B978-0-444-64241-7.50313-X.
- [60] W. C. Wang, R. H. Natelson, L. F. Stikeleather, W. L. Roberts, Product sampling during transient continuous countercurrent hydrolysis of canola oil and development of a kinetic model, Computers and Chemical Engineering 58 (2013) 144–155. doi:10.1016/j.compchemeng.2013.06.003.
- [61] R. Brun, M. Kühni, H. Siegrist, W. Gujer, P. Reichert, Practical identifiability of ASM2d parameters—systematic selection and tuning of parameter subsets, Water Research 36 (16) (2002) 4113–4127. doi:10.1016/S0043-1354(02)00104-5.

- [62] A. Zubov, G. Sin, Multiscale modeling of poly (lactic acid) production: From reaction conditions to rheology of polymer melt, *Chemical Engineering Journal* 336 (2018) 361–375.
- 845 [63] J. P. O’Connell, J. M. Haile, *Thermodynamics: Fundamentals for applications*, Vol. 9780521582, Cambridge University Press, Cambridge, 2005. doi:10.1017/CB09780511840234.

Supporting Information

Liquid-Liquid Equilibrium Calculations

850 *Modified UNIFAC (Dortmund)*

The modified UNIFAC (Dortmund) model has a combinatorial contribution ($\ln \gamma_i^C$) to the activity coefficient, which is directly related to differences in size and shape of the molecules, and a residual contribution ($\ln \gamma_i^R$) to define the energetic interactions between the molecules as presented by Gmehling et al

855 [31, 32, 33, 34, 35].

$$\ln \gamma_i = \ln \gamma_i^C + \ln \gamma_i^R \quad (\text{A.1})$$

The combinatorial part is given by:

$$\ln \gamma_i' = 1 - V_i' + \ln V_i' - 5q_i \left[1 - \frac{V_i}{F_i} + \ln \left(\frac{V_i}{F_i} \right) \right] \quad (\text{A.2})$$

The pure-component parameters r_i and q_i are respectively, related to molecular van der Waals volume and molecular surface area. They are calculated as the sum of the group volume and group parameters, R_K and Q_K .

860 The mole fraction of component j in the mixture is denoted as z_j . Thus:

$$r_i = \sum_k v_k^{(i)} R_K \quad q_i = \sum_k v_k^{(i)} Q_K \quad (\text{A.3})$$

Where v_k^i , always an integer, is the number of groups of type k in the molecule i . The group parameters R_K and Q_K are normally obtained from van der Waals group volumes and surface areas.

The residual part is given by:

$$\ln \gamma_i^R = \sum_k v_k^{(i)} \left[\ln \Gamma_k - \ln \Gamma_k^{(i)} \right] \quad (\text{A.4})$$

865 Γ_k is the group residual activity coefficient, and $\Gamma_k^{(i)}$ is the residual activity coefficient of group k in a reference solution containing only molecules of type i .

$$\ln \Gamma_k = Q_k \left[1 - \ln \left(\sum_m \theta_m \psi_{mk} \right) - \sum_m \frac{(\theta_m \psi_{mk})}{\sum_n \theta_n \psi_{nk}} \right] \quad (\text{A.5})$$

$$\theta_m = \frac{Q_m X_m}{\sum_n Q_n X_n} \quad X_m = \frac{\sum_i v_m^{(i)} x_i}{\sum_i \sum_m v_k^{(i)} x_i} \quad (\text{A.6})$$

The surface area fraction of group m in the mixture is represented by θ_m and X_m is the mole fraction of group m in the mixture. The group interaction parameter ψ_{nm} characterizes the interaction between groups m and n at
870 temperature T through parameters a , b and c .

$$\Psi_{nm} = \exp \left(- \frac{a_{nm} + b_{nm}T + c_{nm}T^2}{T} \right) \quad (\text{A.7})$$

Liquid-Liquid Equilibrium Algorithm

The equilibrium for a liquid – liquid system is defined by the equation:

$$\gamma_i^\alpha z_i^\alpha = \gamma_i^\beta z_i^\beta \quad i = 1, 2, 3, \dots, \text{Component} \quad (\text{A.8})$$

Where γ_i , the activity coefficient of component i in phase (α or β), is predicted using the modified UNIFAC (Dortmund) model. z_i^α and z_i^β represent the
875 mole fraction of component i in phase α and β respectively.

The algorithm is summarized as a flow diagram in Figure A.1 as proposed and presented by O'Connell and Haile [63]. If the system temperature and pressure are known (as they usually are for liquid-liquid equilibrium situations),
880 then the problem can be posed as an analogy to isothermal flash calculations.

In such an approach, the known quantities are temperature T , pressure P and the set of overall system mole fractions z . The following relation can be defined:

$$z_i = \frac{n_i}{n_{Total}} = \frac{n_i^\alpha + n_i^\beta}{n_{Total}^\alpha + n_{Total}^\beta} \quad (\text{A.9})$$

Then the quantities to be computed would be the mole fractions in each phase, z^α and z^β , and the fraction of total material in one phase, $R = \frac{n_i^\beta}{n_{Total}^\beta}$.

885 Distributions coefficients for each component m_i are defined by $m_i = \frac{z_i^\beta}{z_i^\alpha}$.

In order to calculate the required mole fractions, a gamma-gamma formulation for the phase equilibrium equations needs to be expressed in terms of the distribution coefficients as:

$$m_i = \frac{z_i^\beta}{z_i^\alpha} = \frac{\gamma_i^\alpha}{\gamma_i^\beta} \quad i = 1, 2, \dots, \text{Component} \quad (\text{A.10})$$

For each component i in the liquid-liquid system, a material balance is written as:
890

$$z_i^\alpha (1 - R) + z_i^\beta R = z_i \quad (\text{A.11})$$

Where $R = \frac{n_i^\beta}{n_{Total}^\beta}$. Then, by using Equation (A.10) for the distribution coefficients, it is possible to eliminate z_i^β in favor of z_i^α :

$$z_i^\alpha (1 - R) + z_i^\alpha m_i R = z_i \quad (\text{A.12})$$

Solving for z_i^α and z_i^β :

$$z_i^\alpha = \frac{z_i}{1 + R(m_i - 1)} \quad z_i^\beta = \frac{z_i m_i}{1 + R(m_i - 1)} \quad (\text{A.13})$$

However, the mole fractions in each phase must sum to unity, therefore, a Rachford-Rice type function F must be defined as [37]:

$$F \equiv \sum_i^m z_i^\beta - \sum_i^m z_i^\alpha = \sum_i^m \frac{z_i (m_i - 1)}{1 + R(m_i - 1)} = 0 \quad (\text{A.14})$$

895 This Rachford-Rice type function is one equation in the unknown R , independent of the number of components present, which readily lends itself to a

solution by Newton's method. A flow diagram for solving this problem is shown in Figure A.1.

Figure A.1: Rachford-Rice algorithm applied to the gamma-gamma method for solving multicomponent liquid-liquid equilibrium problems (adapted from O'Connel et al. [63])

Results of the Sobol' sensitivity analysis

900 In this section (Tables A.1 to A.4), we provide original numerical values coming out from the sensitivity analysis. Values from Tables A.1 to A.4 were used to produce plots in Figure 6 and 7 in the main text, and Figure A.2 and A.3; which were also used to discuss the results of the sensitivity analysis.

Table A.1: First order and total Sobol sensitivity indices of the model outputs n_{TG} for the hydrolysis at 180°C - 1:27.5 oil-to-water molar ratio - 600 rpm

First order Sobol' sensitivity indices												
	0.5 h	1 h	1.5 h	2 h	2.5 h	3 h	3.5 h	4 h	4.5 h	5 h	5.5 h	6 h
k_1	0.522	0.584	0.583	0.483	0.379	0.300	0.241	0.193	0.155	0.126	0.102	0.084
k_{-1}	0.001	0.022	0.131	0.306	0.430	0.472	0.463	0.428	0.382	0.334	0.290	0.253
k_2	0.000	0.000	0.004	0.037	0.101	0.165	0.207	0.223	0.221	0.207	0.188	0.168
k_{-2}	0.000	0.000	0.000	0.002	0.013	0.041	0.084	0.130	0.169	0.195	0.208	0.212
k_3	0.000	0.000	0.001	0.002	0.002	0.001	0.000	0.003	0.009	0.018	0.026	0.031
k_{-3}	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.002	0.005	0.011	0.019
k_4	0.000	0.000	0.001	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
k_{-4}	0.000	0.001	0.003	0.003	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000
$k_{1L,a}$	0.477	0.392	0.278	0.166	0.071	0.017	0.001	0.017	0.054	0.104	0.160	0.215
$k_{2L,a}$	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.001	0.003	0.005
$\sum S_i$	1.000	1.000	1.000	0.999	0.998	0.997	0.996	0.994	0.993	0.990	0.987	0.985

Total Sobol' sensitivity indices												
	0.5 h	1 h	1.5 h	2 h	2.5 h	3 h	3.5 h	4 h	4.5 h	5 h	5.5 h	6 h
k_1	0.523	0.584	0.583	0.483	0.380	0.301	0.242	0.195	0.158	0.129	0.105	0.086
k_{-1}	0.001	0.022	0.131	0.307	0.432	0.475	0.466	0.433	0.387	0.341	0.297	0.260
k_2	0.000	0.000	0.005	0.038	0.102	0.167	0.209	0.226	0.224	0.211	0.192	0.172
k_{-2}	0.000	0.000	0.000	0.002	0.013	0.042	0.084	0.131	0.171	0.198	0.213	0.218
k_3	0.000	0.000	0.001	0.002	0.002	0.001	0.000	0.003	0.010	0.018	0.027	0.032
k_{-3}	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.002	0.006	0.012	0.020
k_4	0.000	0.000	0.001	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
k_{-4}	0.000	0.001	0.003	0.003	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000
$k_{1L,a}$	0.477	0.393	0.278	0.166	0.071	0.017	0.002	0.017	0.055	0.107	0.164	0.221
$k_{2L,a}$	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.001	0.003	0.006
$\sum S_{Ti}$	1.000	1.000	1.001	1.001	1.002	1.003	1.004	1.006	1.007	1.010	1.013	1.015

Table A.2: First order and total Sobol sensitivity indices of the model outputs n_{DG} for the hydrolysis at 180°C - 1:27.5 oil-to-water molar ratio - 600 rpm

First order Sobol' sensitivity indices												
	0.5 h	1 h	1.5 h	2 h	2.5 h	3 h	3.5 h	4 h	4.5 h	5 h	5.5 h	6 h
k_1	0.607	0.249	0.006	0.003	0.012	0.014	0.013	0.012	0.009	0.008	0.006	0.005
k_{-1}	0.001	0.020	0.022	0.015	0.006	0.002	0.000	0.000	0.000	0.001	0.000	0.000
k_2	0.071	0.708	0.788	0.749	0.714	0.657	0.584	0.509	0.439	0.376	0.325	0.274
k_{-2}	0.000	0.003	0.021	0.070	0.157	0.261	0.351	0.409	0.437	0.443	0.433	0.415
k_3	0.000	0.000	0.001	0.002	0.007	0.017	0.033	0.051	0.068	0.082	0.090	0.096
k_{-3}	0.000	0.000	0.000	0.000	0.000	0.002	0.005	0.013	0.026	0.042	0.059	0.081
k_4	0.000	0.001	0.001	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
k_{-4}	0.001	0.008	0.005	0.003	0.001	0.001	0.000	0.000	0.000	0.000	0.000	0.000
$k_{1L,a}$	0.320	0.009	0.155	0.157	0.101	0.045	0.010	0.001	0.011	0.032	0.057	0.086
$k_{2L,a}$	0.000	0.000	0.000	0.000	0.000	0.000	0.001	0.002	0.005	0.011	0.020	0.031
$\sum S_i$	0.999	0.998	0.999	0.999	0.999	0.999	0.998	0.997	0.996	0.994	0.991	0.989

Total Sobol' sensitivity indices												
	0.5 h	1 h	1.5 h	2 h	2.5 h	3 h	3.5 h	4 h	4.5 h	5 h	5.5 h	6 h
k_1	0.608	0.250	0.007	0.004	0.012	0.014	0.013	0.012	0.009	0.008	0.006	0.005
k_{-1}	0.001	0.020	0.022	0.015	0.006	0.002	0.000	0.000	0.001	0.001	0.001	0.001
k_2	0.071	0.709	0.789	0.750	0.715	0.658	0.585	0.510	0.440	0.378	0.327	0.277
k_{-2}	0.000	0.003	0.021	0.070	0.158	0.262	0.353	0.412	0.441	0.448	0.439	0.422
k_3	0.000	0.000	0.001	0.002	0.007	0.018	0.034	0.052	0.070	0.084	0.093	0.099
k_{-3}	0.000	0.000	0.000	0.000	0.000	0.002	0.006	0.014	0.027	0.044	0.062	0.086
k_4	0.000	0.001	0.001	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
k_{-4}	0.001	0.008	0.006	0.003	0.001	0.001	0.000	0.000	0.000	0.000	0.000	0.000
$k_{1L,a}$	0.321	0.010	0.156	0.157	0.101	0.046	0.010	0.001	0.011	0.032	0.059	0.088
$k_{2L,a}$	0.000	0.000	0.000	0.000	0.000	0.000	0.001	0.002	0.006	0.012	0.022	0.034
$\sum S_{Ti}$	1.001	1.002	1.001	1.001	1.001	1.001	1.002	1.003	1.005	1.006	1.009	1.011

Table A.3: First order and total Sobol sensitivity indices of the model outputs n_{MG} for the hydrolysis at 180°C - 1:27.5 oil-to-water molar ratio - 600 rpm

First order Sobol' sensitivity indices												
	0.5 h	1 h	1.5 h	2 h	2.5 h	3 h	3.5 h	4 h	4.5 h	5 h	5.5 h	6 h
k_1	0.138	0.142	0.110	0.034	0.003	0.000	0.002	0.003	0.003	0.003	0.003	0.003
k_{-1}	0.000	0.002	0.010	0.018	0.014	0.008	0.004	0.002	0.001	0.000	0.000	0.000
k_2	0.351	0.455	0.466	0.224	0.056	0.008	0.000	0.002	0.005	0.007	0.007	0.008
k_{-2}	0.000	0.002	0.020	0.047	0.052	0.044	0.032	0.022	0.013	0.009	0.005	0.003
k_3	0.003	0.049	0.290	0.652	0.780	0.768	0.713	0.625	0.535	0.449	0.374	0.317
k_{-3}	0.000	0.000	0.003	0.020	0.060	0.122	0.196	0.281	0.345	0.386	0.410	0.415
k_4	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
k_{-4}	0.001	0.001	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
$k_{1L,a}$	0.504	0.349	0.098	0.002	0.030	0.038	0.022	0.007	0.001	0.003	0.009	0.016
$k_{2L,a}$	0.000	0.000	0.000	0.001	0.003	0.011	0.027	0.052	0.086	0.129	0.175	0.217
$\sum S_i$	0.997	0.999	0.998	0.997	0.999	0.998	0.996	0.993	0.990	0.986	0.982	0.978

Total Sobol' sensitivity indices												
	0.5 h	1 h	1.5 h	2 h	2.5 h	3 h	3.5 h	4 h	4.5 h	5 h	5.5 h	6 h
k_1	0.139	0.142	0.111	0.035	0.004	0.000	0.002	0.003	0.004	0.003	0.003	0.003
k_{-1}	0.000	0.002	0.010	0.018	0.014	0.008	0.005	0.002	0.001	0.000	0.000	0.000
k_2	0.354	0.455	0.467	0.225	0.057	0.008	0.001	0.003	0.006	0.008	0.008	0.008
k_{-2}	0.000	0.002	0.020	0.048	0.052	0.044	0.033	0.023	0.015	0.010	0.006	0.004
k_3	0.003	0.049	0.292	0.654	0.780	0.768	0.713	0.626	0.535	0.450	0.375	0.318
k_{-3}	0.000	0.000	0.003	0.020	0.061	0.123	0.199	0.286	0.355	0.399	0.426	0.436
k_4	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
k_{-4}	0.001	0.001	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
$k_{1L,a}$	0.507	0.349	0.099	0.003	0.031	0.038	0.023	0.007	0.001	0.003	0.009	0.017
$k_{2L,a}$	0.000	0.000	0.000	0.001	0.004	0.012	0.030	0.058	0.095	0.141	0.191	0.237
$\sum S_{Ti}$	1.003	1.001	1.002	1.003	1.001	1.002	1.004	1.007	1.010	1.014	1.018	1.022

Table A.4: First order and total Sobol sensitivity indices of the model outputs n_{FA} for the hydrolysis at 180°C - 1:27.5 oil-to-water molar ratio - 600 rpm

First order Sobol' sensitivity indices												
	0.5 h	1 h	1.5 h	2 h	2.5 h	3 h	3.5 h	4 h	4.5 h	5 h	5.5 h	6 h
k_1	0.421	0.318	0.229	0.171	0.134	0.107	0.084	0.066	0.052	0.040	0.032	0.026
k_{-1}	0.001	0.008	0.024	0.042	0.055	0.062	0.064	0.062	0.056	0.051	0.044	0.039
k_2	0.027	0.142	0.279	0.376	0.421	0.423	0.392	0.341	0.291	0.240	0.201	0.167
k_{-2}	0.000	0.001	0.006	0.024	0.058	0.102	0.144	0.172	0.184	0.189	0.182	0.174
k_3	0.000	0.006	0.032	0.082	0.143	0.198	0.234	0.245	0.240	0.223	0.204	0.185
k_{-3}	0.000	0.000	0.000	0.002	0.010	0.028	0.058	0.093	0.126	0.153	0.177	0.192
k_4	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
k_{-4}	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
$k_{1L,a}$	0.551	0.526	0.429	0.303	0.178	0.075	0.016	0.002	0.017	0.052	0.086	0.121
$k_{2L,a}$	0.000	0.000	0.000	0.000	0.001	0.003	0.007	0.016	0.030	0.047	0.066	0.085
$\sum S_i$	0.999	0.999	1.000	1.000	0.999	0.999	0.999	0.998	0.996	0.995	0.992	0.989

Total Sobol' sensitivity indices												
	0.5 h	1 h	1.5 h	2 h	2.5 h	3 h	3.5 h	4 h	4.5 h	5 h	5.5 h	6 h
k_1	0.422	0.318	0.229	0.171	0.134	0.107	0.084	0.066	0.052	0.040	0.032	0.026
k_{-1}	0.001	0.008	0.024	0.042	0.055	0.063	0.065	0.062	0.056	0.051	0.045	0.040
k_2	0.027	0.143	0.280	0.376	0.421	0.424	0.392	0.341	0.291	0.240	0.201	0.168
k_{-2}	0.000	0.001	0.006	0.024	0.059	0.103	0.144	0.173	0.185	0.190	0.183	0.176
k_3	0.000	0.006	0.032	0.082	0.143	0.198	0.234	0.245	0.241	0.224	0.205	0.185
k_{-3}	0.000	0.000	0.000	0.002	0.010	0.029	0.059	0.095	0.129	0.157	0.184	0.200
k_4	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
k_{-4}	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
$k_{1L,a}$	0.551	0.526	0.429	0.303	0.178	0.076	0.016	0.003	0.018	0.052	0.087	0.123
$k_{2L,a}$	0.000	0.000	0.000	0.000	0.001	0.003	0.008	0.018	0.032	0.051	0.072	0.093
$\sum S_{Ti}$	1.001	1.001	1.000	1.000	1.001	1.001	1.001	1.002	1.004	1.005	1.008	1.011

Figure A.2: Contribution to the variations in the model output n_{DG} over time using Sobol sensitivity indices for the hydrolysis at 180°C - 1:27.5 oil-to-water molar ratio - 600 rpm

Figure A.3: Contribution to the variations in the model output n_{MG} over time using Sobol sensitivity indices for the hydrolysis at 180°C - 1:27.5 oil-to-water molar ratio - 600 rpm