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Electron Inelastic Mean Free Path in Water †

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Liquid phase transmission electron microscopy (LPTEM) is rapidly developing as a powerful tool for probing processes in liquid environments with close to atomic resolution. Knowledge of the water thickness is needed for reliable interpretation and modelling of analytical studies in LPTEM, and in particular a quite essential role for choosing using their liquid layers, required for achieving the highest spatial resolutions. The log-ratio method in electron energy-loss spectroscopy (EELS) is often applied in TEM to quantify the sample thickness, which is measured relative to the inelastic mean free path ($\lambda_{IMFP}$). However, $\lambda_{IMFP}$ itself is dependent on sample material, the electron energy, and the convergence and divergence angles of the microscope electron optics. Here, we present a detailed quantitative analysis of the $\lambda_{IMFP}$ of water as functions of the EELS collection angle ($\beta$) at 120 keV and 300 keV in a novel nanochannel liquid cell. We observe good agreement with earlier studies conducted on ice, but find that the most widely used theoretical models significantly underestimate $\lambda_{IMFP}$ of water. We determine an adjusted average energy-loss term $E_{m,\text{water}}$, and characteristic scattering angle $\theta_{E,\text{water}}$ that improve the accuracy. The results provide a comprehensive knowledge of the $\lambda_{IMFP}$ of water (or ice) for reliable interpretation and quantification of observations in LPTEM and cryo-TEM studies.

1 Liquid phase transmission electron microscopy (LPTEM) is emerging as a powerful method to investigate the evolution of materials’ morphology and chemistry in-situ in their native liquid environment down to atomic resolution.18 Advanced detector3 and low dose2 imaging techniques have been used to reduce beam damage5 and artefacts16, and have resulted in improved spatial and temporal resolutions.7,8

Liquid sample thickness is a crucial factor for interpreting physical and chemical processes observed in LPTEM, for instance mass transfer, sample-beam interactions,5,26 nanoparticle/bubble growth and diffusion dynamics,8,17 and electrochemical potential driven growth.12,13 Additionally, reducing sample thickness is a significant factor for achieving higher spatial resolution in the LPTEM,14 and phase contrast imaging is only possible at ultra-thin liquid layer less than $\lambda_{IMFP}/2$. The $\lambda_{IMFP}$ will also aid quantitative analysis of High-Angle Annular Dark Field (HAADF) scanning TEM (STEM) imaging18 and chemical analysis with electron energy-loss spectroscopy (EELS).12 Reducing liquid thickness is at times facilitated by means of creating radiolytic bubbles in the liquid cells18–19, or by reducing the encapsulating membrane thickness and bulging using different liquid cell architectures.20–24 However, such thin liquid layers can have vastly different mass transport mechanisms, which can potentially modify the kinetics and fluid dynamics in different liquid processes, and can lead to misinterpretation of the results without knowing the liquid thickness. For example, in graphene trapped liquid blister cells24 one needs to knot liquid thickness to estimate pressure in to better understand the reaction mechanism25–26, or understand the degree of wall confinement in nanoparticle diffusion studies.27–29 Therefore, the actual liquid thickness present in liquid cell is a crucial factor for correctly interpreting many experiment results and modelling of analytical studies in LPTEM.

One can estimate liquid thickness by comparing electron beam currents with and without samples in TEM, at best with some 30% accuracy.29,30 However, electron energy loss spectroscopy (EELS) is the most frequently used method to calculate liquid sample thickness in TEM based on the log-ratio model that measures thickness relative to the inelastic mean free path ($\lambda_{IMFP}$)31.

The EELS log-ratio model is based on Equation (1):

$$\frac{t}{\lambda_{IMFP}} = \ln\left(\frac{I_t}{I_0}\right), \quad (1)$$

where $t$ is the sample thickness, $\lambda_{IMFP}$ is the inelastic mean free

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This relies on the $\lambda_{\text{IMFP}}$, whose value is, in general, estimated as in Equation (2):

$$\lambda_{\text{IMFP}} \approx \frac{106F_0}{E_m \ln(2\beta E_0/E_m)} \cdot F = \frac{1 + E_0/1022}{(1 + E_0/511)^2}$$

where $E_0$ [keV] is the electron energy, $\beta$ [mrad] is the collection angle of the EELS spectrometer, $F$ is the relativistic factor, and $E_m$ [eV] is the average energy loss for the examined material. $E_m$ is in general dependent on the material refractive index and composition. However, $E_m$ is often calculated from Equation (3):

$$E_m = 7.6Z_{\text{eff}}^{0.36}$$

which is an experimentally determined fit to results sourced from several solid materials, with $Z_{\text{eff}}$ as the effective atomic number.

Little has been reported on $\lambda_{\text{IMFP}}$ in liquid water despite EELS having been applied on LPTEM. Holtz et al. found $\lambda_{\text{IMFP}} \approx 106$ nm at 200 keV and $\beta > 20$ mrad, not matching expectations from Equation (2), in which they used a simple single-pole plasmon model assuming that the electrons in the fluid behave as free electrons. Tanase et al. have reported a single measurement $\lambda_{\text{IMFP}} \approx 330$ nm for an unknown mixing ratio of water and ethanol at 300 keV and $\beta = 9.6$ mrad, almost 1.5 times that from Equation (2), maybe due to the addition of ethanol. However, without verifying Equation (2) and other $E_m$ models for liquids, relying on these models for calculating $\lambda_{\text{IMFP}}$ can lead to errors in estimating liquid thicknesses and subsequently, the interpretation of observations.

In this study, we have used a novel nanochannel liquid cell (Fig. 1) that holds liquid layers with well-defined thicknesses, in order to carry out a detailed quantitative evaluation of the log-ratio EELS measurement of the $\lambda_{\text{IMFP}}$ of water and the encapsulating silicon nitride (Si$_3$N$_4$, and low stress silicon-rich SiN$_x$) membranes. The results are compared to two different models: the effective nuclear charge $\lambda_{\text{IMFP}}$ by Malis et al. presented in Equation (2) and $\lambda_{\text{IMFP}}$ defined by Iakoubovskii et al. as in Equation (4) and (5):

$$\lambda_{\text{IMFP}} \approx \frac{200F_0}{11\rho^{0.3}} \left(\frac{1 + \beta^2}{1 + \beta^2/\theta_E^2}\right)$$

$$\theta_E = 5.5 \rho^{0.3} / F_0$$

in which $\rho$ is sample density [g cm$^{-3}$], $\theta_E$ is the characteristic scattering angle, and $\theta_E$ is a saturation factor, and normally is set to $\theta_E = 20$ [mrad].

These two models are both used in the literature, but only occasionally compared, and there is no clear guideline for which one best describes the $\lambda_{\text{IMFP}}$ of water nor silicon nitride, which is the typical liquid encapsulation material in LPTEM. Our detailed study provides a fundamental reference methodology for future EELS and $\lambda_{\text{IMFP}}$ based studies in liquid samples. Additionally, the results are also highly relevant for cryo-TEM studies, in which vitrified ice thickness is a critical factor for obtaining better images as the results match to earlier ice measurements makes it reasonable to assume that these more extensive measurements on water can be transferred to apply to vitrified ice.

Results and Discussion

The nanochannel Liquid Cell

A conventional LPTEM cell uses two manually clamped microchips in which the liquid is enclosed between two thin (~50 nm) electron-transparent silicon nitride membranes typically at least 50 nm wide. Inside the TEM, the membranes bulge outwards, due to the ambient sample pressure difference with respect to the TEM vacuum chamber, resulting in liquid layer thickness variation over the field-of-view (FOV). In this case, the liquid layer thickness can reach up to a few micrometers in the middle of the membranes, which significantly deteriorates the spatial resolution achievable in these regions of the membrane. In some cases, gaseous bubbles are generated during illumination with the electron beam, displacing the liquid to the bubbles periphery, and leaving a thin residual layer of liquid on the top and/or bottom membranes. This improves the spatial resolution, but similar to the membrane bulging, adds to the ambiguity about the true thickness of the liquid layer. Besides the poor spatial resolution in imaging of thick conventional liquid cells, the EELS signal in thicker liquids can also degrade, due to multiple scattering. Although EELS quantification in thick samples ($\lambda_{\text{IMFP}} > 1$) is possible in some cases, and typically multiple plasmons dominate the spectra and can obscure information from other valence and core-loss signals. Because of this, systems that allow control of the liquid thickness and quantification of the liquid thickness are needed to enable higher spatial resolution imaging, spectroscopic measurements, and complementary analytical studies.

![Fig. 1 The nanochannel liquid cell. a) A CAD drawing of the nanochannel liquid cell; it has one inlet and outlet connected with nanochannels in-between as passing over a window region for imaging. b) A bright field optical microscopy (BFOM) image of the nanochannels in the window region. Due to light interference, the suspended nanochannel (brown) and the nanochannel on silicon (white) show different colours. c) A STEM HAADF image of a single nanochannel. The nanochannel is filled with liquid water, and bulges inward. d) A 2D COMSOL simulation shows the stress that a nanochannel experienced during the capillary filling.](image-url)
In liquid cell holders that employ manual clamping of the silicon nitride windows, reducing the bulging via shrinking the total size of the encapsulating membranes to a few μm is not practical, due to the stringent alignment tolerance of small windows. In this work, we have fabricated a nanochannel liquid cell (Fig.1a-c) by bonding two Si₃N₄ coated silicon wafers to encapsulate a channel system (see experimental section, and Figure S1). The resulting bonded wafer architecture creates periodic connections between the top and bottom membranes (Fig.1d), creating a large (200μm × 200μm) window but with embedded 2.5-3.5 μm wide Si₃N₄ nanochannels. This, in turn, results in the local top-to-bottom bulge of the nanochannel being limited to a few nanometers. The liquid layer thickness is then defined by the channel trench depth, which is formed during fabrication. The nanochannel system is hermetically sealed, until punctured for filling. This seals against external contamination making cleaning of the hydrophilic channels before use unnecessary.

The nanochannel liquid filling processes are described in Experimental section. The strong capillary force pulls the liquid into the nanochannels. The measured nanochannel height is 85 ± 5 nm, as shown in the scanning electron microscopy (SEM) cross-section images in Figure S2. We estimated the capillary filling pressure Δp of the nanochannel with thickness t ∼ 85 nm from the Young-Laplace equation \[ \Delta p = 2\gamma \cos \theta / d \] where γ = 0.073 Jm⁻² is the surface tension of water and assuming the contact angle θ = 0°. The nanochannels become deformed due to the very high negative pressure developed behind the moving meniscus. Using the COMSOL Multiphysics simulation program (details can be found in Experimental section), we estimated the overall stress that the nanochannel experienced during filling by assuming a static pressure load (15 bar) on both inner sides of the suspended membranes. As shown in Fig.1, the largest stress is concentrated near the outer corner of the nanochannel side wall (red arrow in Fig.1d), reaching a value of 3.3 × 10⁴ Nm⁻² which is still below yield stress of Si₃N₄, which if exceeded, would lead to formation of permanent cracks in the liquid cell. Using the COMSOL simulation program (details can be found in Experimental section), we estimated the overall stress that the nanochannel experienced during filling by assuming a static pressure load (15 bar) on both inner sides of the suspended membranes. As shown in Fig.1, the largest stress is concentrated near the outer corner of the nanochannel side wall (red arrow in Fig.1d), reaching a value of 3.3 × 10⁴ Nm⁻² which is still below yield stress of Si₃N₄, which if exceeded, would lead to formation of permanent cracks in the liquid cell. This stress is accommodated by plastic deformation of the nitride structure, which develops an inwards bow even under vacuum.

λ IMFP of liquid water

Experimental Measurement of λ IMFP

The λ IMFP of liquid water and encapsulating stoichiometric silicon nitride (Si₃N₄) were experimentally measured using EELS with the microscope operated in STEM mode at electron energies 120 keV and 300 keV, for various collection angles β (see experimental section). The experiment data were acquired at convergence semi-angle α = 4.9 mrad, and with all collection angles β > = 5 mrad. The spectra were analysed using Hyperspy and additional post data analysis was conducted using custom python code.

Fig.2 presents an annular dark field (ADF) image of a single nanochannel; the green rectangle indicates the region where the EELS spectra in (b) was recorded from. The black arrow indicates the location of the gas bubble formed during beam irradiation. (c) The EELS spectra of the nanochannel with liquid in between. Each pixel represents a spectrum. Pixel size is ∼ 40 nm and the scale bar is 400 nm. The EELS spectra recorded in regions R1-R4 in Fig.2c are plotted in Fig.2d, where the spectra in each pixel were summed along the direction parallel to the nanochannel side wall, and normalized with respect to the ZLP maximum intensity. Spectrum R3 shown in Fig.2c confirms the inward bulging of the nanochannel, as it is almost identical to the spectrum recorded from region R1. This indicates that there is at most an ultra-thin liquid layer present in region R3 which is at our detection limit. Region R2 is filled with water between two suspended Si₃N₄ membranes, as can be confirmed by the increase in the energy-loss signal compared to regions R1 and R3. The spectrum from region R4 differs from R1 and R3. In region R4, gases released by radiolysis and residual thin liquid layers on top and bottom membranes contribute to the spectrum. The effects of radiolysis products in the water are estimated to be in the mM.
range and neglected here as their concentrations are negligible compared to 56 M water.

The relative thickness $t/\lambda_{IMFP}$ can be estimated from low-loss EELS spectra based on Equation (1). As an example, the $t/\lambda_{IMFP}$ map obtained from the spectrum image in Fig. 2, for $\beta = 22$ mrad at electron energy 300 keV, is shown in Fig. 3a. The $t/\lambda_{IMFP}$ maps of the same channel at different collection angles and electron beam energies are shown in Figure S3 & S4. The $t/\lambda_{IMFP}$ values for different collection angles measured at 300 keV and averaged along the direction of the sidewall of the nanochannel are plotted in Fig. 3b. As expected from Equations (1) and (2), the $t/\lambda_{IMFP}$ increases with increasing $\beta$ in both the bonded Si$_3$N$_4$ region and the water filled nanochannel region.

To calculate $\lambda_{IMFP}$, the nanochannel height is needed and was obtained from the SEM cross section images (Figure S2). The liquid thickness, $t$, is equal to the nanochannel height near the sidewalls in the measurements, even when the suspended nanochannel has inward bulging (Fig. 1, Fig. 3). Considering that both the Si$_3$N$_4$ and water are amorphous materials, the liquid cell is thin ($t/\lambda_{IMFP} < 1$), we can to a first approximation assume a linear relationship between the sample thickness and the HAADF image intensity (Fig. 3c). After subtracting the signal contribution from the Si$_3$N$_4$, the measured channel height of 85 nm was assigned as the thickness of liquid near the sidewall and extrapolated to the rest of the signal profile across the nanochannel to obtain the water thickness profile displayed in Fig. 3d. As shown in Fig. 3e, the liquid layer thickness decreases to below 10 nm in the middle of the nanochannel. This is a reasonable residual layer given the 3 nm RMS roughness of the Si$_3$N$_4$ and possibly the TEM vacuum causing an outwards bulging of the pressurized channel’s top and bottom up to 10 nm. It is worthwhile to note that in the bubble region the thickness of the thin liquid layer on the top or bottom membrane is also about 10 nm (neglecting any scattering in the gas), which might be used as an starting point estimate of cumulative liquid layer thickness in studies where a bubble is present between the membranes.

The Si$_3$N$_4$ contribution (detailed in Figure S5-S10) is first subtracted from the $t/\lambda_{IMFP}$ maps, giving solely the signal from liquid water. The resulting $t/\lambda_{IMFP}$ values are plotted as a function of distance relative to the inner sidewall of the nanochannels for different collection angles and for 300 keV and 120 keV electron beam energies (Fig. 4a,b, respectively). $t/\lambda_{IMFP}$ of water shows a downward trend as a function of distance from the sidewall and towards the centre of the nanochannel. This is expected, as the nanochannel has an inward bow as explained earlier. Fig. 4c,d show the $\lambda_{IMFP}$ of liquid water at different collection angles and electron energies. At each energy they are fairly constant and consistent within error bars but with a slight tendency for increasing $\lambda_{IMFP}$ at thinner liquid thicknesses ($d > 0.5\mu m$). Given that the effect is small compared to the experimental errors, it is considered part of the noise, but if such an effect is present, it could be due to surface excitation and become important for measure-
Fig. 4. $\lambda_{\text{IMFP}}$ of liquid water. a) and b) The $t/\lambda_{\text{IMFP}}$ line plots across the nanochannel after subtracting the Si$_3$N$_4$ contribution for 300 keV and 120 keV beam energies, respectively. c) and d) The $\lambda_{\text{IMFP}}$ of liquid water at different positions across the nanochannel calculated by dividing the thickness profile of water estimated from HAADF images recorded at 300 keV and 120 keV by their corresponding $t/\lambda_{\text{IMFP}}$ profiles. The error bars have contribution from the uncertainty of the nanochannel thickness and the $t/\lambda_{\text{IMFP}}$ signal. a) has the same legend as c), and b) the same legend as d). e) and f) Our experimentally measured $\lambda_{\text{IMFP}}$ of liquid water vs. collection angle plotted alongside the models discussed in the text, and the values reported in the literature for water and ice. The values taken from the literature are: e) $\star$: ice, M. J. Peet et al. (2019), with $\beta$ possibly in the range of 9$< \beta <$27 mrad; X: ice, W. J. Rice et al. (2018), object aperture diameter (100 $\mu$m); $\bullet$: water-ethanol mixture (of unknown mixing ratio), Tanase et al. (2015); f) $\blacklozenge$: ice, B. Feja et al. (1999), $\star$: ice, Egerton (1992), calculated by ref. 50; X: ice, Egerton (1992), at 100 keV; $\bullet$: ice, R. Grimm et al. (1996). $Z_{\text{eff}}$(H$_2$O)=4.38, and $\rho$=1.00 g cm$^{-3}$ were used for the calculations in the two models, and the $\pm$ 20% accuracy (red) in the model Malis et al. and Iabukouvskii et al. models are plotted in Fig. 4e,f. The error bars in experiment data are the standard deviation of the data in distance 0.05 $\mu$m < $d$ < 0.5 $\mu$m shown in c,d. Only the experiment data with $\beta$<20 mrad were used for fitting. The shaded regions in exp. fit curves originate from the standard deviation of $E_m$ and $\theta_E$ as shown in Table 1.

As indicated in equation (1), the $t/\lambda_{\text{IMFP}}$ singles in the nanochannel region, are superimpose of a spatially varying H$_2$O $t/\lambda_{\text{IMFP}}$ signal that varies linearly with HAADF thickness and a constant silicon nitride $t/\lambda_{\text{IMFP}}$ signal. Therefore, a linear regression method was used to separate the two signals, from which the $\lambda_{\text{IMFP}}$ of water and silicon nitride are achieved independently from the approach mentioned above giving results identical within error (Figure S11†).

Both our values and those reported elsewhere (ice and water/ethanol mixture) are significantly larger than those calculated: 60% – 80% larger compared to the Malis model and 30%...
It is important to note that, in the case of both models, $E_{\text{m}}$ (Equation (2)) and $\theta_E$ (Equation (5)) are derived empirically from measurements on a limited group of solids and at specific electron beam energies (100 keV by Malis et al. and 200 keV by Iabukouvskii et al.). The Iabukouvskii model is known to overestimate sample thickness on average by 25%\(^a\), and possibly could be further improved by correction\(^b\). Similarly, different expressions for $E_{\text{m}}$ at higher beam energies have been suggested also\(^c\).

It is worth noting that both the Malis and Iabukouvskii models make use of the Kramers-Kronig (K-K) model estimation of the IMFP, which has been criticized\(^d\) for introducing unknown systematic errors. However, including a refractive index correction (Figure S12\(^f\)) as also discussed in an ice thickness study\(^g\), we do not find improved match to data, rather all predictions significantly deviated from the observations for both models.

No single model fits the measured values. Based on our measurements of $\lambda_{\text{IMFP}}$ in the range $\beta<$20 mrad, we find that a simple fitted value of $E_{\text{m}}$ in the Malis model Equation (3) gives a reasonable fit as $E_{\text{m,water}} = 6.84 \pm 0.25$ eV at 120 keV, and $E_{\text{m,ice}} = 7.48 \pm 0.22$ eV at 300 keV. Our $E_{\text{m,water}}$ matches the $E_{100keV}\text{water} = 6.8$ eV value reported by Egerton for crystalline ice\(^h\). This is not surprising, given the small density and refractive index difference between water and ice, as vitreous ice has a volume density of 0.94 g cm\(^{-3}\) at 84K\(^i\) and refractive index of $n=1.31$ close to water’s 1.33\(^j\). Therefore, our results are also relevant for cryo-STEM investigations, which employ vitreous ice.

For the Iabukouvskii model, we find $\theta_E(120keV,\text{water}) = 0.26 \pm 0.04$ mrad and $\theta_E(300keV,\text{water}) = 0.12 \pm 0.01$ mrad. These results are summarized in Table 1.

<table>
<thead>
<tr>
<th>Material</th>
<th>Reference</th>
<th>Electron beam energy (keV)</th>
<th>$E_{\text{m}}$ (eV)</th>
<th>$\theta_E$ (mrad)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Liquid water</td>
<td>Malis et al(^2)</td>
<td>120</td>
<td>12.93</td>
<td>0.12</td>
</tr>
<tr>
<td></td>
<td>Equation (2)(^f)</td>
<td>300</td>
<td>12.93</td>
<td>0.12</td>
</tr>
<tr>
<td></td>
<td>Iabukouvskii et al(^3)</td>
<td>120</td>
<td></td>
<td>0.06</td>
</tr>
<tr>
<td></td>
<td>Equation (4)(^g)</td>
<td>300</td>
<td></td>
<td>0.04</td>
</tr>
<tr>
<td>Crystalline ice</td>
<td>Experiment Egerton et al(^4)</td>
<td>100</td>
<td>6.8</td>
<td></td>
</tr>
<tr>
<td>Liquid water</td>
<td>Experiment in this work</td>
<td>120</td>
<td>6.84±0.25</td>
<td>0.26±0.04</td>
</tr>
<tr>
<td></td>
<td></td>
<td>300</td>
<td>7.48±0.22</td>
<td>0.12±0.01</td>
</tr>
</tbody>
</table>

In EELS and $t/\lambda_{\text{IMFP}}$ measurements, the specimen should be very thin, as deconvolution of multiple scattering signals become challenging in thick samples, but how thin is not unanimously defined. However, in practice, the plasmon peak should be no more than one-fifth the height of the zero-loss peak to accurately interpret the sample thickness\(^k\) and preferably $t/\lambda_{\text{IMFP}} < 0.5-0.6$\(^l\) or up to a linearity until $t/\lambda_{\text{IMFP}} = 2.5$ for ice\(^m\). Within uncertainty the $\lambda_{\text{IMFP}}$ is independent of thickness in this study in a range of 0.1 < $t/\lambda_{\text{IMFP,water}} <$ 0.5 for water(Fig\(^n\) d), and 0.3 < $t/\lambda_{\text{IMFP,SnN}} <$ 1.0 for silicon nitride (Figure S7 & S10\(^o\)), and up to $t/\lambda_{\text{IMFP,water+SnN}} <$ 1.5 (Figure S4b\(^p\)). Hence we recommend values from this work, $E_{\text{m}}$, $\theta_E$ and $\lambda_{\text{IMFP}}$ can be used directly to calculate the liquid thickness up to $t/\lambda_{\text{IMFP}} = 1.5$, and possibly can be extended to $t/\lambda_{\text{IMFP}} = 2.5$\(^q\) which corresponds to roughly 1 $\mu$m liquid thickness (at $\beta = 5$ mrad and 300 keV).

The result also indicate that careful validation of the $\lambda_{\text{IMFP}}$ should be considered in non-metal materials, as indicated in the original literature but today not always done in practise.

## Conclusions

In summary, we used a novel nanochannel liquid cell that provides well defined liquid layer thickness, and quantified the $\lambda_{\text{IMFP}}$ of liquid water and silicon nitride (Si$_3$N$_4$, and SiN$_x$)\(^t\) over a range of different collection angles and for two electron energies (120 keV and 300 keV) and compared to the two main models in use today. In our evaluation, the $\lambda_{\text{IMFP}}$ of Si$_3$N$_4$ and SiN$_x$ have the same $\lambda_{\text{IMFP}}$, and matches the Malis et al. model within uncertainty in the range $\beta < 20$ mrad at higher electron energy (300 keV), and matches both the Malis et al. and the Iabukouvskii et al. models at 120 keV. However, both models largely underestimate the $\lambda_{\text{IMFP}}$ of water compared to our experimental values, while the values reported in the literature for ice (single data points) are consistent with our results. A refractive index correction does not give a much better fit to data (Figure S12\(^f\)). The basis for discrepancies between our results and the two models are discussed, and the best fitted fixed values of $E_{\text{m}}$ and $\theta_E$ to the Malis and Iabukouvskii models are obtained. Based on these values, the absolute water or ice thickness in LPTEM and cryo-TEM studies can be estimated with high accuracy up to about $t/\lambda_{\text{IMFP}} \sim 2.5$ or about 1 $\mu$m water thickness.

The results hence provide data and insight to the different approaches to $\lambda_{\text{IMFP}}$ calculations that may also be useful for gas cell and other liquid solutions. Given the low $t/\lambda_{\text{IMFP}}$ in the nanochannel architecture, it will be valuable for pursuing elemental characterization/quantification, such as oxygen and other species which are important for biological applications, and even of light elements such as H$_2$ K-edge at 13 eV in carefully designed experiments, which is also a radiolytic product in LPTEM\(^k\).

## Conflicts of interest

There are no conflicts to declare.

## Author Contributions

M.N. Yesibolati, S. Kadkhodazadeh, S. Lagana, T. Kasama and K. Mølhave designed and conducted the experiments; S. Lagana, and E. K. Mikkelsen fabricated the chips; M.N. Yesibolati made the TEM holder; H.Y. Sun helped with chip characterizations in TEM. M.N. Yesibolati, K. Mølhave, S. Kadkhodazadeh carried out data analysis and wrote the manuscript with corrections and revisions from N.J. Zaluzev, O. Hansen and H.Y. Sun. The manuscript was written through contributions of all authors. All authors have...
given approval to the final version of the manuscript.

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Experimental Section

The nanochannel liquid cell microfabrication. The nanochannel devices were fabricated as depicted in Figure S1, by lithographically defining the channels on a double polished silicon wafer followed by transfer of the pattern into Si using a deep reactive ion etching system (DRIE). The channel depth is defined by the etching time. In order to remove any contamination, the wafers were cleaned in an RCA solution prior to Atomic Layer Deposition (ALD). A thin ~3 nm layer of ALD Al₂O₃ was deposited on the channel wafer in order to improve the bonding adhesion. The wafers were annealed at 400 °C for 8 hours to enhance the bonding strength. Backside lithography is then applied to the un-patterned wafer, followed by etching in a KOH/H₂O solution at 80 °C of the fully bonded system in order to open in/outlet and release the middle membrane region.

Once the KOH etch is completed the imaging membrane size was 200µm ×200µm. The final bonded chip systems have channels suspended in the middle membrane as depicted in Figure S1e, and inlets are clean and sealed with suspended nitride membranes. After processing, chips are coated in protective resist and diced for further use.

Sample loading and sealing. Protective photoresist on chip was removed by placing chip into acetone and isopropanol baths. Both the in/outlet were protected by Si₃N₄ membranes during cleaning. The membranes covering in/outlets were punctured mechanically before filling liquid. Filling of the nanofluidic chip was done by carefully placing a 1 µL droplet of water solution on top of the inlet, and letting the capillary force draw the liquid into the nanochannels. The nanochannels were completely filled after the droplet was placed over the inlet. The high negative capillary pressure causes inwards bulging of the channel during filling. Plastic deformation of the nanochannel by the capillary pressure may cause some degree of permanent bulging in the channel as mentioned in the paper (Fig.1b and 1c). After filling, the inlet and outlet were sealed with water-insoluble ultra-high vacuum (UHV) compatible epoxy (Epotek 77®). The nanochannel liquid cell was mounted in a custom built TEM holder after the epoxy had cured at room temperature.

COMSOL Multiphysics simulation. In order to assess the stress during liquid filling, Finite element analysis (FEA) was carried out using Comsol Multiphysics® (version 5.4). The model geometry was based on the nanochannel design. The calculus consists of Solid Mechanics module for a linear elastic material. We applied a static pressure load (15 bar) to the inner surfaces of the nanochannel that was needed to make the upper and lower part of the channel reach a collapsed state, and a stationary study was conducted.

STEM-EELS measurement. Before inserting the custom-built TEM holder, the nanochannel liquid cell was plasma cleaned (VAR:VO₂=4:1, at 4mBar and 100 W for 30 minutes) together with the custom-built holder to minimize any carbon contamination to the outer surfaces of the suspended membranes. The data were collected using an FEI Titan 80-300ST TEM operating at 120 keV and 300 keV equipped with a Gatan Imaging Filter 865 Tridium. Pixel step size was around 20-40 nm, and the pixel dwell time was around 0.05 sec. The collection angle β was changed by adjusting the camera length, ranging from 5 mrad<β<34 mrad at 300 keV, and 5 mrad<β<52 mrad at 120 keV. The convergence semi-angle was α = 4.9 mrad. The electron flux was between 40-60 e⁻/Å² s⁻¹.

We have restricted the study to thin samples to avoid complications due to multiple scattering. Moreover, elastic scattering can be an issue when using β < α, or for crystalline samples if strong diffracted intensities occur within or outside the collection aperture. However, in our case, β > α is chosen throughout, and the sample is liquid and amorphous so both these effects can be ruled out.

Thickness measurement. In order to take cross section images and obtain the nanochannel height and Si₃N₄ thickness, we broke the chips used in this study, and immersed them into 15 wt% KOH solution for 15 minutes at room temperature, and cleaned with DI water afterwards. FEI Analytical ESEM 250 was used to take the cross section images. Both the secondary and backscattered detectors were used.

The HAADF inner collection angles are: 99 mrad for 300keV and 125 mrad for 120 keV. The absolute thickness value relies on the known water thickness at the nanochannel sidewall. The HAADF analysis is used to investigate if the λ₁MPF depends on the water thickness, where 100 mrad collection angle ensures there is a linear relation ship between thickness and HAADF signal. Given there is no significant thickness dependence of the measured λ₁MPF compared to the noise level, we allow the most reliable part of the HAADF measurements to be included in the dataset (up to 0.5 µm from the sidewall).

Image analysis. The spectra were analyzed using Hyperspy and additional post data analysis conducted using custom python code including data/figure plots (Fig.3,Fig.4), data fitting (Fig.4).

Notes and references

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