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Dark energy from Higgs potential

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PACS 98.80.Cq - Particle-theory and field-theory models of the early Universe (including cosmic pancakes, cosmic strings, chaotic phenomena, inflationary universe, etc.)

Abstract - We derive the ratio of dark energy to baryon matter content in the universe from a Higgs potential matching a description of baryon matter on an intrinsic configuration space. The match determines the Higgs mass and self-coupling parameters and introduces a constant term in the Higgs potential. The constant term is taken to give dark energy contributions from detained neutrons, both primordial and piled-up neutrons from nuclear processes in stars. This corresponds to the dark energy content increasing with time. The two contributions possibly give rise to the primordial inflation and the later accelerated recession, respectively. The ensuing inflation during nucleosynthesis may explain the primordial lithium-seven deficit relative to the standard Big Bang nucleosynthesis model predictions. From the observed helium and stellar metallicity contents, we get a dark energy to baryon matter ratio of 14.5(0.7) to compare with the observed value of 13.9(0.2).

Introduction. – Observation of accelerated recession of supernovae in low and high red-shift galaxies [1] led to the acceptance of a major dark energy content in the universe [2,3]. The present, observed ratio \( \Omega_\Lambda / \Omega_b = 13.9(0.2) \) [4] between the dark energy content and the baryonic content remains unexplained. We suggest that the dark energy content of the universe is a manifestation of detained neutron decay, expressed as a constant term in the Higgs potential. We derive the ratio \( \Omega_\Lambda / \Omega_b = 14.5(0.7) \) from an intrinsic conception of the structural changes taking place during transformations between protons and neutrons in the nuclear fusion processes inside stars. The present work is developed from [5]. We leave the question unanswered as to how the underlying coupling to accelerated expansion should be described. Suggestions already exist concerning the relation between Higgs physics, inflation and dark energy, mediated by a coupling between the Higgs field and the Ricci curvature of spacetime [6–10]. The problem in these models is to find a “natural” coupling level. Also models with add-on inflaton fields have been considered [11]. The accelerated supernovae recession has been called into question [12] as dependent on bias removal from observational samples. The biases concern the choice of coordinate system, removal of peculiar velocities with respect to the cosmic microwave background and possible red-shift and light curve bias for the supernovae analyzed. The debate [13,14] has made it clearer than ever that determinations of cosmological parameters is a combination of observations and models. Fluctuations in radiation and matter distributions as inferred from fluctuations in the cosmic microwave radiation (CMB) and from baryon acoustic oscillations (BAO) inferred from galaxy clustering can be modelled by a cosmological model \( \Lambda \text{CDM} \) with a cosmological constant and a cold dark matter component to add up to a more or less flat universe [4].

Our purpose here is only to give a derivation from theoretical considerations of the present value of the dark energy to baryon matter content. If our derivation is causally correct, it means that the dark energy content increases with time from its primordial value after nucleosynthesis, followed by the pile-up of neutrons in stellar burning of nuclear fuel, e.g., neutrons in helium nuclei in the \( p-p \) cycle in main sequence stars. That is, burning hydrogen to helium with the gross result

\[
4^1H \rightarrow ^4He + 2e^+ + 2\nu_e, \tag{1}
\]

where new neutrons are detained in the helium nuclei.
Dark energy and Higgs potential. – We repeat the Higgs potential [15] from [16], also used in [17] for Higgs couplings to gauge bosons

\[ V_H(\phi) = \frac{1}{2} \delta^2 \phi_0^2 - \frac{1}{2} \mu^2 (\phi^0, \phi) + \frac{1}{4} \lambda^2 (\phi^0, \phi)^2, \]  

with Higgs field \( \phi \) [18–21] and coefficients

\[ \delta^2 = \frac{1}{4} V_0, \quad \mu^2 = \frac{1}{2} V_0, \quad \lambda^2 = \frac{1}{2}. \]  

expressed in the electroweak energy scale (\( v = \phi_0 \sqrt{2} \))

\[ \frac{v}{\sqrt{2}} \equiv \phi_0 = \frac{2\pi}{\alpha} \Lambda_b = \frac{2\pi}{\alpha(m_W)} \alpha_e m_e c^2. \]  

Here \( \Lambda_b \) is a baryonic energy scale [16,22] not to be confused with the cosmological constant. Further, \( \alpha(m_W) \) and \( \alpha_e \) are the fine structure couplings at the W boson and electron energy scales respectively.1

The Higgs mechanism mediates the electroweak neutron to proton transformation with Higgs field \( \phi = 0 \) for a neutronic state and \( \phi = \phi_0 \) for a protonic state, see fig. 1. Reversing the mechanism, we thus assume, that for each detained neutron there is one zero-mode \( \delta \)-contribution to the dark energy. With \( \delta = \phi_0/2 \) from (3), this gives the following dark energy to baryon matter ratio:

\[ \frac{\Omega_b}{\Omega_{\Lambda}} = \frac{\sum_{\text{neutrons}} \delta}{\sum_{\text{baryons}} m_{\text{baryon}} c^2} \approx \frac{n_n \cdot \phi_0/2}{n_b \cdot m_n c^2}. \]  

Here the \( n \)'s are cosmological number densities of the respective species and the baryons we consider are either neutrons or protons, i.e., \( n_b \approx n_p + n_n \). The ratio \( n_n/(n_p + n_n) \) for use as \( n_n/n_b \) in (5) we get from the helium Y and heavier Z content by the expression (see, e.g., p. 481 in [23])

\[ Y + Z = \frac{2n_n}{n_p + n_n} \rightarrow \frac{n_n}{n_b} = Y + Z^*. \]  

Here \( Z^* \) is weighted with relative neutron content in each nucleus². Then, in standard model language where \[ \upsilon_{\text{SM}} = v \sqrt{|V_{ud}|} \] via the up-down quark mixing matrix element \( V_{ud} \) [17]. In the left eq. (6) we assume a 1:1 amount of neutrons and protons in the nuclei of all elements from helium and up. A simple counting argument then gives \( \frac{n_n}{n_p + n_n} = \frac{4}{14} = 0.29 \). This is most easily seen for \( Z = 0 \), where \( X + Y = 1 \) and all neutrons are detained in helium-4 nuclei. Then by definition of \( Y \) as a ratio of helium mass to the total, we count 2 units of the neutron number density \( n_n \) into the helium mass contribution because helium-4 contains as many protons as it contains neutrons, i.e., \( Y = 2n_n/m_{\text{baryon}} = 2n_n/(n_p + n_n) \). For this counting it is essential that \( X : Y : Z : 2 \) are mass ratios, that nuclear binding energies are small compared to the nuclear masses and that \( n_n \approx m_p \). The fact that, for heavy nuclei \( n_n > m_p \), modifies the implied \( \Omega_b/\Omega_{\Lambda} \). The modification is done by substituting \( Z \) in the left eq. (6) with the weighted value \( Z^* \equiv \sum_{i \geq 3} w_i Z_i \). Here \( Z_i \) is the contribution from element \( i \) to the total metallicity and the weights count the neutron to proton ratio in the nucleus of this element, i.e., \( w_i = \frac{N_i}{A_i - N_i} \), where \( N_i \) is the neutron number and \( A_i \) is the nucleon number of element \( i \). This is implied in the right eq. (6) and used in (7). To be very accurate one should use individual weights for every isotope of element \( i \). We do not take into consideration a possible minute fraction of heavier baryons in very energetic environments. Neither do we count minute fractions of deuterium and helium-3.

\[ \Omega_b \bigg|_{\text{observation}} = 0.0493(6) = 13.9 \pm 0.2. \]  

Note that our \( v \) is related to the standard model value by \( \upsilon_{\text{SM}} = v \sqrt{|V_{ud}|} \) via the up-down quark mixing matrix element \( V_{ud} \) [17].

In the bulk [30] with \( X \) being the hydrogen fraction and \( Z \) is the fraction of elements with atomic number larger than 2 for helium. Further we used \( \upsilon_{\text{SM}} = 246.21965(6) \text{ GeV}, \left| V_{ud} \right| = 0.97420(21) \) and \( m_n c^2 = 939.565413(6) \text{ MeV} \) [4]. The value of the standard model electroweak energy scale \( \upsilon_{\text{SM}} \) is obtained from the Fermi coupling constant \( G_{\mu}/|hc|^3 = 1.1663787(6) \cdot 10^{-5} \text{ GeV}^{-2} \) [4] by \( \upsilon_{\text{SM}} = \sqrt{|V_{ud}|} \). The dark energy to baryonic matter value in (7) agrees with the observed ratio [4], see fig. 2.

\[ \frac{\Omega_b}{\Omega_{\Lambda}} = \frac{Y + Z^* \upsilon_{\text{SM}} / \sqrt{|V_{ud}|}}{2 m_n c^2} = \frac{14.5 \pm 0.7}{4 \sqrt{2}}. \]  

As an example we here used \( Y = 0.29(2) \) from a globular cluster as a representative of a stellar population and set \( Z^* \equiv Z = 0.0142 \) which is the metallicity for our own Sun. Our Sun has \( X : Y : Z = 0.7154 : 0.2703 : 0.0142 \) in the bulk [30] with \( X \) being the hydrogen fraction and \( Z \) is the fraction of elements with atomic number larger than 2 for helium. Further we used \( \upsilon_{\text{SM}} = 246.21965(6) \text{ GeV}, \left| V_{ud} \right| = 0.97420(21) \) and \( m_n c^2 = 939.565413(6) \text{ MeV} \) [4].

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We are aware that this argument relates to main sequence stars in the Hertzsprung-Russell diagram, see, e.g., p. 181 in [23]. Very heavy stars—and old stars—may be so dense from gravitational contraction that they start burning helium. This of course diminishes the helium content in the stellar interior and ultimately in the star’s atmosphere. One would therefore need to include \( Z^* \) in the calculation based on (7). The same goes for main sequence stars when nearing the end of their lives. Indeed, our own Sun is expected to start burning helium when the hydrogen in its centre has already been transformed.

The primordial helium fraction \( Y_p \) can be extracted in various ways. One can analyse spectra from HII-regions in galactic media containing a mixture of helium and hydrogen that is supposed not yet to have participated in fusion processes in stars—one looks for He emission lines [32]. Or one can look for absorption lines in the spectrum of a distant quasar whose light passes through intergalactic gas clouds [33] likewise thought not to have been involved in fusion in stars. And one can analyse the cosmic microwave background for diminished fluctuations in the damping tail of the power spectrum [34,35]. The latter method is somewhat model-dependent. It takes as granted a relation between \( Y_p \) and the number density of free electrons \( n_e \) and baryons \( n_b \) at the time of hydrogen recombination [35]

\[
n_e = n_b(1 - Y_p).
\]

Here it is assumed that the helium recombination happens much earlier than the hydrogen recombination from which the cosmic microwave background radiation originates. The larger the \( Y_p \), the smaller \( n_e \) and thus the less the photons interact with the not yet recombined primordial plasma. In short: the larger the \( Y_p \), the larger the photon mean-free path and thereby the smaller the damping tail power spectrum fluctuations in the cosmic microwave background [35].

In table 1 we list various determinations of the helium content, both \( Y_p \) and \( Y \) and variations in their determinations. From table 1 we see that the determinations of \( Y_p \) are converging around the value predicted from a standard Big Bang Nucleosynthesis model [36]. Using, e.g., \( Y_p \) from HII in (7) would give \( \Omega_\Lambda/\Omega_b = 12.1 \pm 1.2 \) which is somewhat lower than the observed value 13.9 \( \pm 0.2 \). But we want to determine a present value for \( \Omega_\Lambda/\Omega_b \) from (7). Thus we need some kind of average \( Y + Z^* \) for the star population in the Milky Way and its surroundings within minimal red-shifts \( z \) in stead of the primordial value \( Y_p \). For this, the determinations from globular clusters could serve as representative where Villanova et al. find...
the thing seems to be certain, though, namely the increase of among star populations as seen already from table 1. One is shown in fig. 2. We repeat that there are large variations the observed value $13^{+0.014}_{-0.012}$ as a manifestation of dark energy and we consider $Y$ stat as a free parameter in a Big Bang Nucleosynthesis model.

$$Y = 0.29 \pm 0.01_{\text{stat}} \pm 0.01_{\text{sys}}$$

for the globular cluster Messier 4 shown in fig. 3. This yields $\Omega_\Lambda/\Omega_b = 13.8 \pm 0.7$ and is shown in fig. 2. To get an exemplar $Y + Z^*$ we added the solar $Z$ for the result $14.5 \pm 0.7$ in (7) which agrees with the observed value $13.9 \pm 0.2$ within uncertainties and also is shown in fig. 2. We repeat that there are large variations among star populations as seen already from table 1. One thing seems to be certain, though, namely the increase of the $Y + Z^*$ content with increasing star evolution in general. And that is what is key to our argument that we should expect $\Omega_\Lambda/\Omega_b$ to increase with time from neutron pile-up in accordance with the observed accelerated recession of supernovae interpreted as originating in increasing dark energy content in the universe.

Discussion. – We here discuss the cosmological constant as a manifestation of dark energy and we consider the possible contribution to dark matter from the electron neutrinos originating in the build up of neutrons in stars.

The field equations of general relativity with a cosmological constant $\Lambda$ read (cf. p. 155 in [41])

$$\mathcal{R}_{\mu\nu} - \frac{1}{2}g_{\mu\nu}\mathcal{R} - \Lambda g_{\mu\nu} = -\kappa T_{\mu\nu},$$ (10)

where $\mathcal{R}_{\mu\nu}$ is the curvature tensor constructed from derivatives of the spacetime metric $g_{\mu\nu}$, $\mathcal{R}$ is the contraction of $\mathcal{R}_{\mu\nu}$ over the spacetime indices $\mu, \nu$. On the right-hand side we have the total energy-momentum tensor $T_{\mu\nu}$ of matter and energy and $\kappa = 8\pi G_N/c^4$ gives the strength of the influence of matter and energy on the metric on the left hand side. This strength is determined by Newton’s constant of gravity $G_N$ and the speed of light $c$ in empty space. Taking the cosmological term in (10) to the right-hand side

$$\mathcal{R}_{\mu\nu} - \frac{1}{2}g_{\mu\nu}\mathcal{R} = -\kappa T_{\mu\nu} + \Lambda g_{\mu\nu},$$ (11)

it interprets as a contribution to the energy-momentum tensor as first suggested by Gliser and Zeldovich, cf. p. 352 in [4].

Now consider the energy-momentum tensor of a scalar field $\phi$ (cf. p. 357 in [4])

$$T_{\mu\nu} = \partial_\mu \phi \partial_\nu \phi - \frac{1}{2}g_{\mu\nu} \partial_\sigma \phi \partial^\sigma \phi - g_{\mu\nu} V(\phi).$$ (12)

The potential $V(\phi)$ may have extrema where $\partial_\mu \phi = 0$ and where only $V(\phi)$ would survive as a contribution to the energy-momentum tensor. This is the standard way to
derive a cosmological constant from a the potential of a scalar field [42], thus
\[ R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R = -\kappa T_{\mu\nu} + \kappa V g_{\mu\nu}. \] (13)

Comparing with (11), we see that \( \kappa V \) acts as a cosmological constant \( \Lambda \). If we take \( \phi \) to be the Higgs field, the potential \( V(\phi) \) would be taken at its minimum value where \( \phi \) equals its vacuum expectation value \( \phi_0 \). One then expects the value of the potential to be of the order \( \phi_0^{\text{EW}} \sim (\phi_0)^4 \approx (177 \text{ GeV})^4 \) [42]. This would mean a huge value and the idea is only saved if \( V(\phi_0) \) is zero. Actually for our \( V_H \) in (2) we have \( V(\phi_0) = 0 \). Our potential was constructed to fit the intrinsic potential as seen in fig. 1 and therefore it was lifted to match to fourth order in \( \phi \) the minima and curvature of the intrinsic potential. It is from this match we got the coefficients in (3). Now, there is one more stationary value where \( V_H \) could contribute a constant value, namely at zero Higgs field where we get
\[ V_H(0) = \frac{1}{2} \delta^2 \phi_0^2. \] (14)

In (5) we used \( \delta \) and \( \phi_0 \) in units of energy. However, to be strict, we should include \( h \) and \( c \) wherever appropriate to have correct field dimensions (cf. p. 357 in [43]) such that the potential gets the unit of energy per volume. Thus, writing out in full, we have
\[ V_H(\phi) = \frac{1}{2} \left( \frac{\delta}{hc} \right)^2 \left( \frac{\phi_0}{\sqrt{hc}} \right)^2 - \frac{1}{2} \left( \frac{\mu}{hc} \right)^2 \left( \frac{\phi}{\sqrt{hc}} \right)^2 + \frac{1}{4} \left( \frac{\phi}{\sqrt{hc}} \right)^4. \] (15)

With \( \delta = \varphi_0/2 \) and \( v = \varphi_0 \sqrt{2} \approx 250 \text{ GeV} \) (see footnote 3) from (3) inserted in (15) we get
\[ \kappa V_H(0) = \frac{G_N h}{8c} \left( \frac{v}{hc} \right)^4 \approx 0.05 \text{ cm}^{-2}, \] (16)

to substitute \( \Lambda \) in (11). This would still be at a pathologically large value compared to the observed \( \Lambda = 1.088(30) \cdot 10^{-56} \text{ cm}^{-2} \) [4]. On the other hand, by allowing the Higgs field to stay at the unstable, stationary value \( \phi = 0 \) only when detached neutrons are present, we get a \( \delta \) contribution to dark energy of the right order of magnitude as seen in (7). In the present view, the cosmological constant is not a constant as such but a spatial average over mostly zero values of the Higgs potential and the few locations where neutrons are present and \( \phi \) takes the role of dark energy contributions. These contributions increase slowly with the pile-up of neutrons in stars.

We know from observations towards our own Sun that the neutrinos from the \( p-p \) cycle in (1) escape the stars. It is thus of interest to evaluate such stellar neutrino contributions to the matter content of the universe. We infer
\[ \frac{m_e}{m_n} = \frac{\alpha}{\pi} \frac{1}{E_n}, \] (20)
where \( E_n \equiv \varepsilon_n / \Lambda \) = 4.382(2) from a Rayleigh-Ritz solution [48,49] of (19) with 3078 base functions —at the limit of our computer programme. With the fine structure coupling \( \alpha^{-1}(m_n) = 133.61 \) sliding by radiative corrections [28] from \( \alpha^{-1}(m_e) = 133.476(7) \) [4], eq. (20) yields

\[
\frac{m_e}{m_n} = \frac{1}{1839(1)},
\]

in agreement with the experimental value 1/1838.683661(16) [4].

To sum up, the basic scale and coupling inputs of our model is the electron mass \( m_e \) and the fine structure coupling \( \alpha \). Provided we allow for \( \alpha \) to slide to the relevant energy scales of the phenomena under study, we can condense higher-order field theory corrections into the value of the fine structure coupling as used, e.g., in (4).

**Inflation and nucleosynthesis.** — It is beyond the scope of the present work to give a detailed discussion on primordial cosmology. However, a few notes seem in order. In Standard Big Bang Nucleosynthesis models [36] one starts from more or less equal neutron and proton abundances resulting from equilibrium with the neutrino bath in a radiation-dominated era preceding the nucleosynthesis. One assumes negligible dark energy contributions and in so far as inflation is mentioned this phenomenon is thought to take place prior to the radiation era, see, e.g., [50]. It would be of interest though to consider a model where inflation is directly related to the neutron content. It would mean that inflation prior to the neutron-proton equilibrium would be already into its maximum because here the neutron content is a maximum. It would also mean that inflation would be still ongoing during nucleosynthesis, though at a slowing rate as the free neutrons decay during the cooling. And it would mean that dark energy would have to be included in the underlying spacetime description. One may worry that such a radical change could spoil the success of predicting \( Y_p \) from Standard Big Bang Nucleosynthesis [36]. On the other hand, a continued inflation during synthesis will reduce the particle density and thereby reduce creation rates of nuclei past helium-4. This might solve the persisting Li-7 problem of a factor three too high prediction from Standard Big Bang Nucleosynthesis, see, e.g., [51]. The binding energy of nucleons in the helium-4 nucleus (the alpha particle) is considerable compared to the other light nuclei involved in the synthesis. Thus the alpha particle works already as an attractor in the network of mutual transitions among the primordial nuclei. It is therefore possible that the helium-4 fraction could remain more or less unaltered even in the case of inflation during synthesis.

**Conclusion.** — We have found an expression for the ratio of dark energy to baryon matter content in the universe from a Higgs potential shaped by an intrinsic description of proton to neutron transformation. Our expression contains the cosmological neutron and proton densities and can be condensed into an expression containing the cosmic helium fraction and stellar metallicities as key ingredients. The vast majority of neutrons in the universe are bound in helium nuclei since primordial nucleosynthesis. We suggest the dark energy to represent detained neutrons and found our result by considering the helium and stellar metallicity content of baryon matter as determined in astrophysical observations. Our value 14.5(0.7) for the dark energy to baryon matter ratio compares well with the observed value 13.9(0.2). We look forward to improved determinations of the helium fraction and heavier elements in the baryon matter of the universe and to observations to determine whether the dark energy content is increasing with time as suggested by our interpretation.

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