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Modeling of MIMO less Mode Division Multiplexed Systems

Lars Grüner-Nielsen, *Member, IEEE*, Neethu Mariam Mathew, Mads Lillieholm, Michael Galili, and Karsten Rottwitt

Abstract—A transmission model for a mode group division multiplexing system is presented. The model is used to model a two mode group system with either 10 Gbit/s NRZ modulation or 25 Gbit/s PAM4 modulation. Influence of wavelength separation between the channels, detector bandwidth and component crosstalk is examined.

Index Terms—Space division multiplexing, crosstalk, interference

I. INTRODUCTION

MODE division multiplexing (MDM) has been extensively researched for now almost 10 years. Impressive results in both reach and number of channels have been obtained using MIMO-DSP. However, MIMO less systems for shorter distances is of interest too, for example for use in data center communications. For data center applications MDM might pose advantages over CWDM systems such as, use of simpler lasers with no wavelength stabilization, and less impact from dispersion as all channels can be at a wavelength close to the zero dispersion wavelength of the fiber.

For MIMO less MDM, it is required to use special fibers with no degenerate modes (except for the polarization degeneracy) such as fibers supporting orbital angular momentum [1], or elliptical core fibers [2]. The focus of this paper will be MIMO less mode group division multiplexing (MGDM), where each mode group supports a transmission channel. This requires use of demultiplexers, which detects the whole mode group. This has been demonstrated using demultiplexers based on multiplane light converters [3], and couplers [4]. Alternatively, each degenerate mode can be detected and their power added either in the optical domain [5] or in the electrical domain [6].

It is important to understand the requirements for the components of a MIMO less MGDM system, especially, the tolerable amount of crosstalk. This can be difficult to do experimentally due to a lot of variables. Therefore, in this paper, we will use a theoretical model for a system supporting the two mode groups LP₀₁ and LP₁₁. The model will be used to analyze the system and find the crosstalk requirements for the mode multiplexers and splices. Only relative short reach systems with lengths limited to tens of kilometers will be

considered. Therefore crosstalk in the transmission fiber, DGD within the mode group, and all nonlinear effects are neglected.

II. MODEL

The system modeled is shown in Fig. 1a. The back to back case is modeled as shown in Fig. 1b. A linear propagation model of phase and amplitude is used. The field is normalized to the power and characterized by a vector:

$$\vec{E} = \begin{pmatrix} \sqrt{P_{01}} e^{-i\varphi_{01}} \\ \sqrt{P_{11}} e^{-i\varphi_{11}} \end{pmatrix}, \quad (1)$$

where P_{01} and φ_{01} are the power and phase for LP₀₁ and equivalent for LP₁₁. Then, each component: Input multiplexer (mux), propagation in the two mode fiber (TMF), splice and output mux are modeled by a transfer matrix. For example, the splice is modeled as:

$$\vec{E}_{out} = \begin{pmatrix} \sqrt{\frac{1-x_{ts01}}{\alpha_{s01}}} & \sqrt{\frac{x_{ts11}}{\alpha_{s11}}} \\ \sqrt{\frac{x_{ts01}}{\alpha_{s01}}} & \sqrt{\frac{1-x_{ts11}}{\alpha_{s11}}} \end{pmatrix} \vec{E}_{in}, \quad (2)$$

where α_{s01} and α_{s11} is the splice loss for LP₀₁ and LP₁₁ and x_{ts01} and x_{ts11} the crosstalks; all in linear units. Similarly, neglecting distributed crosstalk in the fiber, the propagation in the two mode fiber is modeled as

$$\vec{E}_{out} = \begin{pmatrix} e^{-i\beta_{01}z} \\ e^{-i\beta_{11}z} \end{pmatrix} \vec{E}_{in}, \quad (3)$$

where z is the distance travelled and the propagation constants (β) are found as function of wavelength λ from:

$$\beta_{01} = \beta_{01}(\lambda_0) - \Delta\beta/2 \quad (4)$$

$$\beta_{11} = \beta_{11}(\lambda_0) + \Delta\beta/2 \quad (5)$$

$$\Delta\beta = \frac{2\pi c DGD(\lambda - \lambda_0)}{\lambda_0^2}, \quad (6)$$

where λ_0 is the reference wavelength, c the speed of light in vacuum, and DGD is the length normalized differential group delay between LP₀₁ and LP₁₁. The propagation is the only wavelength dependent element in the model.

The fields out of the lasers after modulation is modeled as:

$$\vec{E}_{in} = \begin{pmatrix} \sqrt{P_{01}(t)} e^{-i(\frac{\omega_B t}{2} + \varphi_{01}(t))} \\ \sqrt{P_{11}(t)} e^{-i(-\frac{\omega_B t}{2} + \varphi_{11}(t))} \end{pmatrix}, \quad (7)$$

where t is the time, $P_{01}(t)$ and $P_{11}(t)$ are the powers after modulation, and ω_B is the beat frequency between the two lasers:

$$\omega_B = \frac{2\pi c(\lambda_{LP11} - \lambda_{LP01})}{\lambda_{LP11} \lambda_{LP01}}, \quad (8)$$

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L. Grüner-Nielsen, N. M. Mathew, M. Lillieholm, Michael Galili, and K. Rottwitt are with DTU Fotonik, Technical University of Denmark, Ørsted Plads, Building 343, 2800 Kgs. Lyngby, Denmark

L. Grüner-Nielsen is also with Danish Optical Fiber Innovation, Åvenningen 22A, 2700 Brønshøj, Denmark e-mail: lars@dofi.dk.

Fig. 1. (a) Layout of the modeled system. (b) Model for the back to back case.

where λ_{LP01} and λ_{LP11} are the wavelength of the LP₀₁ and LP₁₁ channels. The phase noise of the two lasers is modeled as a Wiener process [7]:

$$\varphi_i = \varphi_{i-1} + \Delta\varphi w_i \quad (9)$$

$$\Delta\varphi = \sqrt{2\pi f_{FWHM,laser} T_s} \quad (10)$$

Here, i is the sample number in the simulation, w_i is a series of independent random numbers with Gaussian distribution with zero mean and a variance of one, $f_{FWHM,laser}$ is the full width half maximum linewidth of the laser, and T_s is the time between two samples in the simulation. The amplitude noise is modeled by for each sample in the simulation adding a random number with Gaussian distribution and zero mean. The variance is adjusted to get a reasonable back to back Q .

The Gaussian filters used to emulate the modulation bandwidth and the detector bandwidth are both first order Gaussian filters. Typical parameters used for the simulations are summarized in Tab. I. The mux parameters are typical for photonic lantern mode multiplexers developed in our group [6], [8].

The model has been validated by comparing modeled loss versus wavelength with measurements of connected photonic lanterns and a good agreement was found.

TABLE I
PARAMETERS USED FOR SIMULATION.

No of bits in simulation		500
No of samples per bit		100
Modulation frequency	Gbit/s	10
Modulation extinction ratio	dB	7
Modulator 3 dB bandwidth	GHz	20
Laser linewidth	MHz	1
Wavelength LP ₀₁ channel	nm	1551
Wavelength LP ₁₁ channel	nm	1551.5
Power LP ₀₁ channel	dBm	0
Power LP ₁₁ channel	dBm	2
Detector 3 dB bandwidth	GHz	10
Input mux loss LP ₀₁ channel	dB	1
Input mux loss LP ₁₁ channel	dB	3
Input mux crosstalk LP ₀₁ channel	dB	-15
Input mux crosstalk LP ₁₁ channel	dB	-15
Length 1 (L_1)	m	6
Length 2 (L_2)	m	4
DGD two mode fiber (1550 nm)	ps/m	2.1
β_{01} (1550 nm)	μm^{-1}	5.870
β_{11} (1550 nm)	μm^{-1}	5.864
Splice loss LP ₀₁	dB	0.04
Splice loss LP ₁₁	dB	0.04
Splice crosstalk LP ₀₁	dB	-25
Splice crosstalk LP ₁₁	dB	-25
Output mux loss LP ₀₁ channel	dB	3
Output mux loss LP ₁₁ channel	dB	4
Output mux crosstalk LP ₀₁ channel	dB	-10
Output mux crosstalk LP ₁₁ channel	dB	-10

III. RESULTS 10 GBIT/S NRZ MODULATION

Typical simulation results for 10 Gbit/s NRZ modulation, using the values of Tab. I, are shown in Fig. 2. The Q is calculated from the averages and standard deviations of the zeros and ones [9] and the bit error rate (BER) is calculated from the Q , assuming Gaussian distributions of the zeros and ones [9]. This BER should be taken only as an indicative value, since in the presence of crosstalk, the distributions might not be Gaussian as well as the number of bits in the calculations is chosen only to get reliable Q values. The beat noise with frequency given by Eq. (8) is clearly seen on the signals before filtering (Fig. 2b). However, as observed in Fig. 2c, the Gaussian filter, emulating the detector bandwidth, efficiently suppresses this beating. Therefore, an open eye after transmission is obtained as shown in Fig. 2d with a calculated Q of 6.2 at a position in the eye of 48.5 ps and an estimated BER of $4 \cdot 10^{-10}$.

Results for calculated Q versus the wavelength of the LP₀₁ channel for different wavelength separation between the LP₀₁ and LP₁₁ channel are shown in Fig. 3. It should be noted

Fig. 2. Results for 10 Gbit/s NRZ modulation using the parameters of Tab I. (a) Back to back eye for the LP₀₁ channel. The orange line shows the decision threshold. (b) Detector signals before Gauss filtering. (c) Detector signals after Gauss filtering. (d) Output eye for the LP₀₁ channel.

Fig. 3. Q for the LP_{01} and LP_{11} channel vs wavelength of the LP_{01} channel for different wavelength separations between the LP_{01} and LP_{11} channel for 10 Gbit/s NRZ modulation. Besides the wavelengths, all other parameters are as defined in Tab. I.

that for Q below 2, the eyes are totally closed. That is, it is not possible to model Q below 2. As the input powers have been adjusted to compensate for the mode depend loss, similar performance is observed for the LP_{01} and LP_{11} channels. A clear periodic variation in Q with wavelength is observed in Fig. 3. This can be explained by the interference in the connected few mode system, where the crosstalk varies versus wavelength with a wavelength period λ_B [10]:

$$\lambda_B = \frac{\lambda^2}{DGD \cdot L \cdot c}, \quad (11)$$

where λ is the wavelength, L is the length, and c is the speed of light in vacuum. Similar oscillations are seen in modeling and measurements of loss versus wavelength of the system. As the crosstalk in splice is set relatively low compared to the crosstalk of the input and output mux, $L \approx L_1 + L_2$ and thus $\lambda_B \approx 0.38$ nm, which fits well with the period observed in Fig. 3. To properly resolve this periodic behaviour of Q versus wavelength, relatively short fiber lengths have been used in the simulation. For longer lengths λ_B can become comparable to or smaller than the modulation bandwidth of the lasers and Q will become more stable versus wavelength. For example for the considered TMF, λ_B becomes smaller than 0.079 nm corresponding to 10 GHz for a length larger than 48 m. Still, in practical systems there can easily be relative short lengths between the mode coupling points. For this reason, it is most safe for each trace of Fig. 3 to consider the lowest Q when judging the quality of transmission. It is clearly seen in Fig. 3 that for a wavelength separation between the LP_{01} and the LP_{11} channel of 0.1 nm (12.5 GHz) and below, the performance degrades rapidly. This has also been shown experimentally [6]. When the beat frequency between the two channels get comparable to the detector bandwidth or below, the performance is not only degraded by the crosstalk but also the interference noise from the beating.

To examine the requirements for the crosstalk, simulations are done with the wavelength of the two lasers well separated and with the wavelengths almost equal. The results are shown in Fig. 4. Here, calculated Q is shown as function of the wavelength of the LP_{01} channel for different crosstalk levels of the components for a wavelength separation of 0.5 nm in Fig. 4a and 0.02 nm in Fig. 4b. In these simulations

Fig. 4. Q for the LP_{01} and LP_{11} channel vs wavelength of the LP_{01} channel for different crosstalk levels. The wavelength separations between the LP_{01} and LP_{11} channel are (a) 0.5 nm (b) 0.02 nm.

the crosstalk for all components: input and output mux and splice are assumed to be the same. Apart from crosstalk and channel wavelengths, all other parameters are still as defined in Tab. I. It is observed that for a channel separation of 0.5 nm a crosstalk level below -20 dB is enough to ensure a $Q > 8$ corresponding to $BER < 6 \cdot 10^{-16}$, while for the small wavelength separation of 0.02 nm a crosstalk below -30 dB is required to obtain just $Q > 4$ corresponding to $BER < 3 \cdot 10^{-5}$. For a wavelength separation of 0.5 nm a $Q > 4$ can be obtained with a crosstalk values below -15 dB for all components or as observed in Fig. 3 with the experimentally demonstrated values of Tab. I.

The influence of detector bandwidth has been examined as well. Q versus the detector bandwidth is shown in Fig. 5 for three different wavelengths of the LP_{11} channel and the back to back case. Apart from the detector bandwidth and the wavelengths of the LP_{11} channel all other parameters are as in Tab. I. For most cases, it is as expected seen that the optimum is a detector bandwidth equal to the modulation rate. Furthermore, it is noticed that for the smaller wavelength spacing Q gets much more degraded if the detector bandwidth get too large. This is because the interference between the channels is not sufficiently suppressed. For the very small wavelength spacing of 0.1 nm (12.5 GHz), it is even noticed that optimum detection bandwidth is lower than the modulation rate.

Fig. 5. Q for the LP_{01} and LP_{11} channel vs detector bandwidth for the back to back case and after transmission for different wavelength separations between the LP_{01} and LP_{11} channel for 10 Gbit/s NRZ modulation.

IV. RESULTS 25 GBIT/S PAM4 MODULATION

So far, 10 Gbit/s NRZ modulation has been examined. However, current data center network use up to 400 Gb Ethernet channels, which typically use 25 Gbit/s PAM4 modulation. This modulation format has therefore been examined too. Example on back to back eye and eye after transmission are shown in Fig. 6. Here compared to Tab. I, the modulation frequency is increased to 25 Gbit/s, the modulator 3 dB bandwidth to 30 GHz, the detector bandwidth to 25 GHz. Furthermore, the input mux crosstalks has been decreased to -20 dB and the output mux crosstalks to -15 dB.

Fig. 6. Calculated eyes for 25 Gbit/s PAM4 modulation. (a) Back to Back. (b) After transmission. The yellow lines are the decision levels used for the Q calculation

The Q is calculated for the three eyes and from these, the symbol error rate (SER) is calculated [9]. As for the 10 Gbit/s NRZ modulation, the average of the three Q 's is calculated as a function of the wavelength of the LP_{01} channel for different wavelength separation between the LP_{01} and LP_{11} channel. The result is shown in Fig. 7a. It is observed that due to the higher detector bandwidth necessary for 25 Gbit/s modulation, a minimum wavelength separation of 0.5 nm is now needed to suppress detrimental effects of the interference between the two channels.

Fig. 7. Q for the LP_{01} and LP_{11} channel vs wavelength of the LP_{01} channel for 25 Gbit/s PAM4 modulation. (a) for different wavelength separations between the LP_{01} and LP_{11} channel. (b) For different crosstalk levels and a wavelength separation of 0.5 nm

Finally, the requirement for component crosstalk is examined. Q versus wavelength of the LP_{01} channel for a wavelength separation of 0.5 nm for different component crosstalk levels is shown in Fig. 7b. As in the similar calculation in Sec. III for the NRZ case, the crosstalk levels are set equal for all

components. It is observed that to get an average Q above 4.3 corresponding to $SER < 2 \cdot 10^{-5}$ a crosstalk level below -20 is needed. Where crosstalk below -15 dB was enough for similar performance in the 10 Gbit/s NRZ case.

V. CONCLUSIONS

Using a linear propagation model, the performance of, a two-mode, mode group division multiplexing system is examined. Due to the interference effect, the transmission performance varies with wavelength. Two effects degrade the system performance namely, crosstalk and interference between the modes (also know as modal noise). The latter effect can be avoided by using a proper wavelength spacing between the channels. The requirements for crosstalk become much more severe when the wavelength of the two channels are close compared to a wider wavelength spacing. For 10 Gbit/s NRZ modulation, the crosstalks of mode mux, de-mux and splices should be lower than -15 dB to secure a bit error rate $BER < 3 \cdot 10^{-5}$, while for 25 Gbit/s PAM4 modulation, the crosstalks should be below -20 dB to get a symbol error rate $SER < 2 \cdot 10^{-5}$. A detector bandwidth equal to the modulation frequency is optimum and are especially important when the wavelength of the two channels are close.

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