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Added-value of ensemble prediction system on the quality of solar irradiance probabilistic forecasts

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Added-value of Ensemble Prediction System on the quality of solar irradiance probabilistic forecasts

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Abstract

Accurate solar forecasts is one of the most effective solution to enhance grid operations. As the solar resource is intrinsically uncertain, a growing interest for solar probabilistic forecasts is observed in the solar research community. In this work, we compare two approaches for the generation of day-ahead solar irradiance probabilistic forecasts. The first class of models termed as deterministic-based models generates probabilistic forecasts from a deterministic value of the irradiance predicted by a Numerical Weather Prediction (NWP) model. The second type of models denoted by ensemble-based models issues probabilistic forecasts through the calibration of an Ensemble Prediction System (EPS) or from information (such as mean and variance) derived from the ensemble. The verification of the probabilistic forecasts is made using a sound framework. A numerical score, the Continuous Ranked Probability Score (CRPS), is used to assess the overall performance of the different models. The decomposition of the CRPS into reliability and resolution provides a further detailed insight into the quality of the probabilistic forecasts. In addition, a new diagnostic tool which evaluates the contribution of the statistical moments of the forecast distributions to the CRPS is proposed. This tool denoted by MC-CRPS allows identifying the characteristics of an ensemble that have an impact on the quality of the probabilistic forecasts. The assessment of the different models is done on several sites experiencing very different climatic conditions. Results show a general superior performance of ensemble-based models as the gain in forecast quality measured by the CRPS ranges from 4% to 16% depending on the site.

Keywords: Day-ahead solar irradiance probabilistic forecast, Ensemble prediction system, Non parametric methods, Ensemble calibration, CRPS

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39 1. Introduction

Operations of electrical power systems are becoming more challenging as the share of solar energy increases. In particular, due to the intrinsic variability of the solar resource, high penetration of solar power generation into the electrical grid may put in danger the grid supply-demand balance. Energy storage systems (EES) are one of the means used to ensure the grid stability. Notwithstanding, accurate PV power forecasting is a cost-effective way to size and operate ESS optimally. Consequently, PV power forecasts facilitate the large-scale integration of solar energy into the grid. In addition, for energy trading, accurate PV power forecasts are also required because penalties in proportion with the forecast errors are applied.

In this study, however, we focus on the global horizontal solar irradiance (GHI) forecasts instead of PV power forecasts. The present work constitutes thus a first step in assessing the contribution of the proposed methodologies for improving the quality of the PV power forecasts and of their potential gain for improved grid operations. Day-ahead GHI forecasts are treated here as they have been considered essential to secure the power grid [1]. Moreover, we propose to work on probabilistic forecasting in order to estimate the uncertainty associated to day-ahead GHI forecasts. This additional knowledge permits for instance grid operators to improve their decisions regarding the grid operations. The interested reader can refer to [2] or [3] to understand the benefits of a probabilistic forecast against a deterministic one.

Day-ahead GHI forecasts are classically generated by Numerical Weather Predictions models (NWPs). For instance, The Integrated Forecasting System (IFS) model of the European Centre of Medium-Range Weather Forecasts (ECMWF) provides day-ahead GHI forecasts [4]. The forecasts can take either the form of a deterministic forecast or an ensemble forecast denoted by the term Ensemble Prediction System (EPS). EPS consists in a set of several perturbed forecasts of irradiance, each representing a possible future state of the atmosphere. If an EPS gives an important information about the uncertainty associated to a forecast, it requires a high computational cost. Thus, the added value of EPS for probabilistic forecasting needs to be determined to justify their computation.

We propose below to conduct a bibliographic survey related to day-ahead solar forecasts with a special emphasis on the use of NWP outputs to generate probabilistic forecasts. One of the first approach used to generate day-ahead probabilistic irradiance forecasts was proposed by Lorenz et al. [5]. In this work, a Gaussian distribution of the error of the ECMWF-IFS deterministic irradiance forecast was used to generate prediction intervals. Alessandrini et al. [6] developed an analog statistical method approach applied to a set of explanatory weather variables (GHI, cloud cover, air temperature, etc.) provided by the NWP Regional Atmospheric Modeling System (RAMS) to generate probabilistic PV power forecasts for three solar farms located in Italy. Zamo et al. [7] proposed two statistical approaches to generating probabilistic forecasts of daily PV production from information provided by Météo France's EPS, PEARP. The first approach makes use of the PEARP control member as unique input to quantile regression methods while the second one averages the set of quantiles calculated from each of the 35 members of the PEARP ensemble. Bacher

et al. [8] used a weighted quantile regression (WQR) technique to compute up to 24h ahead probabilistic PV forecasts. In addition to lagged PV measurements, the WQR model used also a NWP-based GHI deterministic forecast. Lauret et al. [9] used the IFS model to produce quantile forecasts of solar irradiance and Iversen et al. [10] introduces the idea of modeling uncertainty by stochastic differential equations from a NWP-based deterministic forecast provided by the Danish Meteorological Institute. Bakker et al. [11] proposed a comparison of seven statistical regression models to issue GHI probabilistic forecasts from the deterministic numerical weather prediction (NWP) model HARMONIE-AROME (HA) and the atmospheric composition model CAMS.

It must be noted that the above cited works make use of deterministic information extracted from NWP models to generate probabilistic forecasts with the help of statistical techniques like quantile regression or analog ensemble. Others authors like Sperati et al. [12] proceeded differently. In their work, Sperati et al. [12] generated up to 72h probabilistic forecasts from the raw EPS provided by the ECMWF. In this study, two post-processing methods (also called calibration techniques) applied to the initial raw ensemble were used to further improve the quality of the probabilistic forecasts. Massidda and Marrocu [13] went a little bit further and proposed a methodology to combine ECMWF ensemble and the high-resolution IFS deterministic forecast.

If we extend our bibliographic survey to the probabilistic predictions of other weather variables such as wind, temperature or precipitation, more publications can be found on how to use information from NWP models to generate probabilistic forecasts. For example, Pinson [14] and Pinson and Madsen [15] suggested a framework for the calibration of wind ensemble forecasts. Junk et al. [16] proposed an original calibration model for wind-speed forecasting applied to ECMWF-EPS based on the combination between Nonhomogeneous Gaussian Regression and Analog Ensemble Models. Likewise, Hamill and Whitaker [17] suggested an adaptation of the analog ensemble technique for the calibration of ensemble precipitation forecast, using the statistical moments of the distribution such as mean and spread of the members as predictors.

Wilks [18], followed in his methodology by Williams et al. [19], compared several post-processing techniques of weather EPS forecasts, such as ensemble dressing, Logistic Regression, Nonhomogeneous Gaussian Regression (NGR) and Rank-Histogram recalibration. The reader can refer to [20] and [21] for more details regarding the parametric calibration of ensemble forecasts with techniques like NGR with a special emphasis on the choice of the type of the parametric distribution used by the regression technique. Finally, the interested reader should consult the reference book [24], which proposes a summary of the common probabilistic forecasting ensemble-based models with their respective pros and cons.

Based on this bibliographic survey, two different approaches for day-ahead GHI probabilistic forecasting with the help of NWP models can be identified, which we denoted here by approaches 1 and 2:

1. Approach 1 referred herein as deterministic-based models: the probabilistic forecast is computed from deterministic NWP predictors with the help of statistical methods. Linear Quantile Regression and Analog Ensemble techniques are particularly attractive

to implement this methodology.

2. Approach 2 referred herein as ensemble-based models: the estimation of the forecast is made through the calibration of an EPS or from information (for example mean or spread) inferred from the ensemble. For instance, calibration techniques like Nonhomogeneous Regression can be used to improve the raw ensemble EPS. Also, methods based on Linear Quantile Regression and Analog methods can be used to produce probabilistic forecasts from the mean and spread of the ensemble.

It must be stressed however that, to the best of our knowledge, no previous works have been dedicated to the comparison of the two approaches and particularly in the realm of solar probabilistic forecasts. In this work, our main goal is therefore to assess the relative merits of each approach for day-ahead GHI probabilistic forecasts. Besides, we would like to highlight the possible added-value brought by EPS for probabilistic forecasting. Indeed, it is well known that the generation of such ensemble necessitates high computing capacities compared to a single deterministic forecast that is fed into a statistical method to produce the probabilistic forecasts. More precisely, it should be noted that the calculation cost is not the same to produce only the control member of EPS or the whole set of members.

To understand the benefits associated with the usage of EPS, we propose in this paper a a sound and consistent methodology to evaluate the respective contribution of each approach. First, the quality appraisal of the different models will be made according the verification framework proposed by Lauret et al. [25]. This framework (which is not consistently proposed in the literature) is based on visual diagnostic tools and numerical scores like the Continuous ranked Probability Score (CRPS) which permits to objectively rank the competing forecasting methods. However, this classical verification framework is not sufficient to completely explain the contribution of the statistical moments of the forecast distributions to the forecast quality. That is why we propose in a second step a new tool that evaluates the accuracy of all moments of the forecast distribution and its contribution to the CRPS score. We hope that this new diagnostic tool will provide a more in-depth understanding of the performance of each approach. To this end, we evaluate models that generate day-ahead GHI probabilistic forecasts on 6 sites that experience different sky conditions. The probabilistic models are built:

- 1. With only the control member of the EPS as a deterministic predictor (deterministic-based approach),
- 2. With a deterministic predictor inferred from the whole set of EPS's members. The first statistical moment (mean of the members) can be such a deterministic predictor (ensemble-based approach),
- 3. With several predictors inferred from the ensemble like the mean and the variance of the ensemble (ensemble-based approach).

We propose the following structure for the paper. Section 2 introduces the different forecasting models while section 3 briefly presents the diagnostic tools used for the verification of probabilistic forecasts. Section 4 presents the case studies and details the data used to evaluate the different probabilistic models. Section 5 provides a detailed assessment of

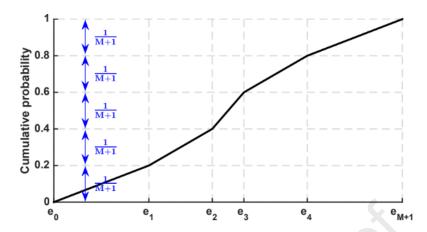


Figure 1: Illustration of an uniform construction of a CDF from an ensemble of M=4 members (e_1,e_2,e_3,e_4) . The tails of the CDF are bounded by e_0 and e_{M+1} which correspond to the minimum and the maximum of the climatology.

the performance of the different methods. Finally, a discussion will be conducted in section 6, trying to understand the pros and cons of each forecasting methods and the factors impacting the forecast quality.

2. Building probabilistic forecasts

Regarding probabilistic forecasts of continuous predict and like GHI, a probability statement i.e. either a Probability Distribution Function (PDF) f or a Cumulative Distribution Function (CDF) F encodes the uncertainty of the forecast. In this work, three ways to estimate this CDF or PDF are considered: parametric PDFs, discrete quantile estimates of a CDF via a non-parametric method and CDF derived from EPS.

In this study, the EPS is provided by the European Centre of Medium-Range Weather Forecasts (ECMWF). It corresponds to 50 perturbed members and a control run (unperturbed member) [4] that give the cumul of the GHI with a 3 hours time step. This leads to a total of M=51 members. An EPS can be seen as discrete estimates of a CDF when they are sorted in ascending order. Lauret et al. [25] discussed three ways to associate these sorted members to cumulative probabilities. In this work, we chose the uniform distribution which consists in a uniform spacing of the members and a linear interpolation between the members. More precisely, this choice assigns a probability mass of 1/(M+1) between two members and for events that fall outside of the ensemble. Using this definition, the i^{th} ensemble member can be interpreted as a quantile forecast with a probability level equal to $\tau = \frac{i}{M+1}$. Put differently, the ECMWF ensemble forecasts are in the form of 51 equally spaced quantiles with probability levels $\tau = \frac{1}{52}, \frac{2}{52}, \cdots, \frac{51}{52}$. This construction is illustrated in Figure 1, for an EPS with 4 members. In the following, we present first the different statistical techniques used to estimate the uncertainty of the forecasts. Secondly, we detail the two approaches introduced in section 1.

88 2.1. Statistical techniques used to generate probabilistic forecasts

2.1.1. The linear quantile regession (LQR) technique

This method estimates the quantiles of the cumulative distribution function F of some response variable Y (also called predictand) by assuming a linear relationship between the quantiles of Y, namely q_{τ} and a set of explanatory variables X (called predictors):

$$q_{\tau} = \beta_{\tau} X + \epsilon, \tag{1}$$

where β_{τ} is a vector of parameters to optimize for each probability level τ and ϵ represents a random error term.

Following Koenker [26], the

vector $\hat{\boldsymbol{\beta}}_{\tau}$ that defines each quantile is obtained as the solution of the following minimization problem:

$$\hat{\beta}_{\tau} = \underset{\beta}{\operatorname{arg\,min}} \sum_{i=1}^{N} \Psi_{\tau} (Y_i - \beta X_i). \tag{2}$$

where N is the number of pairs of observed predictand Y_i , set of predictors X_i taken from the training set. $\Psi_{\tau}(u)$ is the quantile loss function defined as:

$$\Psi_{\tau}(u) = \begin{cases} u\tau & \text{if } u \ge 0, \\ u(\tau - 1) & \text{if } u < 0, \end{cases}$$
 (3)

with τ representing the quantile probability level. Hence, in quantile regression, the quantiles are estimated by applying asymmetric weights to the mean absolute error.

Thus, the quantity $\hat{q}_{\tau} = \hat{\beta}_{\tau} X$ is the estimation of the τ^{th} quantile obtained by the LQR method.

It must be noted that the quantile regression method estimates each quantile separately (i.e. the minimization of the quantile loss function is made for each τ separately). As a consequence, one can obtain quantile regression curves that may intersect, i.e $\hat{q}_{\tau 1} > \hat{q}_{\tau 2}$ when $\tau_1 < \tau_2$. To avoid this issue during the model fitting, we used the rearrangement method described by Chernozhukov et al. [27].

Figure 2 shows some quantiles estimates of the CDF of the predictand Y (here GHI) as a function of the day-ahead forecasted GHI. Hence, in this case, the predictor X is the predicted irradiance which will be represented in this work either by the ECMWF control member or the mean of the ECMWF ensemble (see Table 2 below). This example shows that the forecast uncertainty depends on the level of the predicted irradiance. More precisely, and as shown by Figure 2, the dispersion of points is lower for values of predicted irradiance close to $0 \ W/m^2$ and greater for values between 40 and 100 W/m^2 .

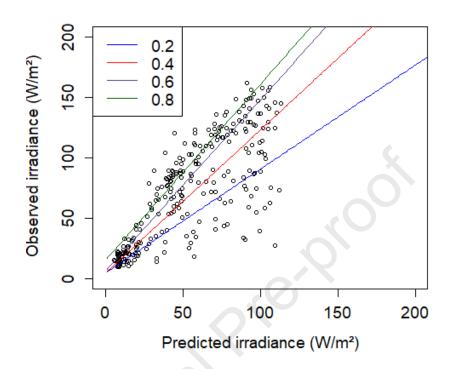


Figure 2: Observed GHI vs. the predicted day-ahead GHI. The lines are the estimates of the quantiles with probability levels of 0.2, 0.4, 0.6 and 0.8. Data are from the training period of Hawaii. Observed and predicted GHI are averaged on the 3-hour window [17h-20h] local time.

2.1.2. The Analog Ensemble (AnEn) technique

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The analog ensemble technique is now quite a standard in the energy meteorology forecasting community [29, 17]. Similarly to the LQR method, the analog technique is a nonparametric method that can be used to estimate the predictive CDF of the predictand.

Considering a training set of N ordered (sorted by forecasts) pairs of GHI observations/GHI forecasts $(Y_i, \hat{Y}_i)_{i=1,\dots,N}$, the procedure for determining the forecast CDF is as follows:

- 1. For a new forecast taken from a testing set, calculate its distance from every past forecast order and find the rank R of the past forecast that is the closest to the new forecast.
- 2. Form an ensemble by selecting the $2\alpha + 1$ past training observations Y_k having their ranks k inside the interval $[R \alpha, R + \alpha]$.
- 3. Compute the predictive CDF at a specific value y of the predictand using the following equation:

$$\hat{F}(y) = P(Y \le y) = \frac{1}{2\alpha + 1} \sum_{k=1}^{2\alpha + 1} H(y - Y_k),\tag{4}$$

where Y is the random value related to the predictand (here GHI) and H is the Heaviside or step function. The effectiveness of the method is strongly dependent on the value of α . It is proposed here to take $\alpha = 0.02N$. This choice has been motivated by a preliminary study made on the training period. Appendix C details the selection of the optimal value of α . Finally, as for the linear quantile regression, note that the GHI forecasts used in the AnEn technique will be given either by the ECMWF control member or the mean of the ensemble (see Table 2 below).

2.1.3. The Nonhomogeneous truncated Gaussian Regression technique (t_NGR)

The NGR technique also called in some studies "Ensemble Model Output Statistics" (EMOS) has been introduced by Gneiting et al. [20] for probabilistic forecasting of weather variables. This technique is dedicated to the post-processing of ensemble forecasts produced by an EPS. The NGR technique builds the predictive PDF of the predictand Y from a normal PDF. As such, this kind of model can be termed as a parametric model. The predictive pdf \hat{f} estimated by the NGR method is given by:

$$\hat{f} \sim \mathcal{N}(a + \sum_{k=1}^{M} (b_k m_k), c + dS^2), \tag{5}$$

where M is the number of members, m_k is the k^{th} member and S^2 is the variance of the ensemble members distribution. The free parameters a, b_1, \dots, b_M, c and d are determined with the help of an optimization procedure. In this work, and following Gneiting et al. [20], these parameters are calculated by minimizing (over a training period) an evaluation metric for probabilistic forecasts called CRPS (see section 3.2 for details regarding CRPS). Furthermore, as GHI is a necessarily positive quantity, we propose, in this work, a variant of the NGR technique namely a truncated version (at 0) of the nonhomogeneous gaussian regression. In the following, the corresponding model is denoted as t NGR.

2.1.4. The Nonhomogeneous Regression of Generalized Extreme Value technique (NR_GEV) One can question the choice of a Gaussian distribution in the t_NGR technique. Indeed, the distributions of observations for a fixed forecasting level are actually non-Gaussian. Two examples for the studied sites are presented in Figure 3.

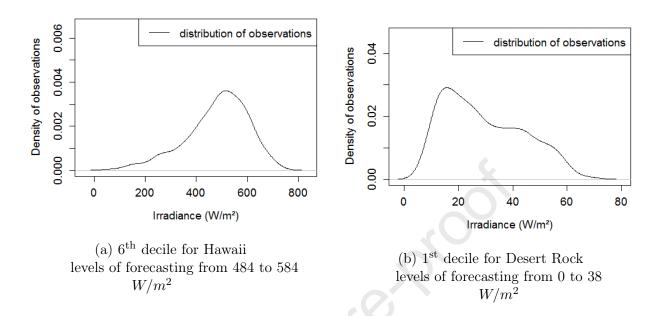


Figure 3: Example of distributions of observations for a fixed forecasting level.

GHI is defined as:

On these specific examples, the distributions of observations are clearly non-Gaussian

and the consideration of other types of distributions may improve the skills of the forecast. As pointed out in [21] and [22], other types of parametric distributions can be used to deal with this issue. Here, a Non homogeneous Regression approach with Generalized Extreme Value distributions is proposed to estimate the PDF of the predictand Y. The PDF of a generalized Extreme value distribution for a specific value y of the predictand

$$\hat{f}(y) = \begin{cases} \frac{1}{\sigma} \left[1 + \xi \left(\frac{y - \mu}{\sigma} \right) \right]^{\left(-\frac{1}{\xi} \right) - 1} \exp \left(-\left[1 + \xi \left(\frac{y - \mu}{\sigma} \right) \right]^{-\frac{1}{\xi}} \right) & \xi \neq 0, \\ \frac{1}{\sigma} \exp\left(-\frac{y - \mu}{\sigma} \right) \exp \left[-\exp\left(-\frac{y - \mu}{\sigma} \right) \right] & \xi = 0. \end{cases}$$

$$(6)$$

The parameters μ , σ and ξ are to be determined by optimizing the CRPS over the training period. We followed the framework of [31] and [32] to set these coefficients. Following this procedure, the mean μ and the scale parameter σ of the final distributions are determined by linear regression, and depends only on variables inferred from the EPS. The mean is a linear combination of the mean of the members and the fraction of members which predict exactly zero. The scale parameter σ depends on the "Gini's mean difference" (a measure of the variability closely related to the spread of the members, see [33] for details). Note that the shape parameter is taken as a constant. Thus, the minimization of the CRPS yields the linear coefficients for the mean μ and the scale parameter σ as well as the value of the shape parameter ξ . Note that the two techniques namely t_NGR discussed

Site	HAW	DR	SP	PAL	TIR	LAN
Any perturbed member	138	75.3	126.5	97.7	110.7	98.8
Control member	135	72.8	91.9	102.9	100.8	93.2
Mean of the members	129.7	67.9	113.8	81.8	92.6	84.3
Median of the members	133.9	69.4	115.5	84.1	94.7	85.6

Table 1: RMSE (W/m^2) of 4 deterministic forecasts that can be inferred from an EPS: any of the 50 perturbed members of ECMWF ensemble forecast, the control member (unperturbed), the mean of the members and the median of the members. See Table 3 for the signification of the acronyms of the different sites.

above and NR_GEV discussed here are part of a family of parametric methods named Nonhomogeneous Regression (NR).

2.2. Obtaining probabilistic forecasts from deterministic forecasts (Deterministic-based approach)

Some of the techniques presented in section 2.1, namely the Linear Quantile Regression (LQR) and the Analog Ensemble(AnEn) techniques, are capable of generating a probabilistic forecast from a deterministic predictor.

In our study, and regarding the deterministic-based approach, the control member of ECMWF-EPS is the predictor variable X of the LQR technique and it will be the forecast used in the AnEn procedure. The corresponding probabilistic models are denoted respectively as LQR_c and $AnEn_c$ in the following.

2.3. Obtaining probabilistic forecasts from ensemble forecasts (Ensemble-based approach)

2.3.1. From the raw output of ECMWF-EPS

Given a raw ensemble forecast of M members $\{m_i\}_{i=1,\dots,M}$, it seems natural to define directly a forecast CDF from this EPS as illustrated in Figure 1. Note that this definition corresponds to the "uniform" definition of a CDF derived from an ensemble" discussed in Lauret et al. [25].

2.3.2. From information extracted from an EPS

An EPS differs from a deterministic forecast by the multiplicity of predictors. In this work, we propose to assess the quality of two variants of probabilistic models built with information extracted from an EPS.

The first variant will make use of the mean of the ensemble members of the EPS. The use of the mean of members as a deterministic predictor is justified by Table 1. For all the considered sites depicted in Table 3, Table 1 lists the Root Mean Square Error (RMSE)¹ of different deterministic predictors extracted from an EPS.

As shown by Table 1, the mean of all the members turns out to be the best predictor for deterministic forecasting. Hence, to quantify the improvement brought by the first moment

¹RMSE is a common metric used to assess the accuracy of deterministic forecasts [34]

Approach	Determin	nistic-based	Ensemble-based					
Predictors	Control member		Mean of members		Mean and spread of members			
Technique	AnEn LQR		AnEn	LQR	LQR	NR		
Model Abbreviation	$AnEn_c$	LQR_c	$AnEn_m$	LQR_m	LQR_s	t_NGR	NR_{-}	GEV

Table 2: Summary of all considered forecasting models with AnEn: Analog Ensemble, LQR: Linear Quantile Regression, NR: Nonhomogeneous Regression

estimation (i.e. the mean), two models denoted by LQR_m and $AnEn_m$ based respectively on the LQR and AnEn techniques will be evaluated.

The second variant will include, in addition to the mean of the members, the spread (i.e. the variance) of the members of the EPS. The t_NGR and the NR_GEV models described in sections 2.1.3 and 2.1.4 use the first and second moment of the EPS distribution to build the predictive distributions. Furthermore, we also propose to use the LQR technique with a vector X of predictors given by

$$X = [\mu, S^2], \tag{7}$$

where μ represents the mean of members and S^2 the variance of the ensemble. This method will be referred in this study as LQR_s . Finally, Table 2 summarizes the different probabilistic models that will be evaluated in this study.

3. Verification of the probabilistic forecasts

In this section, we detail some of the verification tools proposed by Lauret et al. [25] that will be applied to assess the quality of GHI probabilistic forecasts. Following this work, we will rely on a quantitative score namely the continuous ranked probability score (CRPS) and its related skill score (CRPSS) to rank objectively the different methods. Moreover, and based on the recommendations of [25], we will provide the decomposition of the CRPS into the main attributes that affect the quality of the forecasts. In addition to this decomposition, it is worth noting that we will propose in this work a new way to have detailed insight into the performance of the methods. This new methodology is based on the contribution of the moments (mean, variance, etc.) of the forecast distribution to the CRPS (see section 3.3 below).

3.1. Attributes for a skillful probabilistic model

We recall here briefly the two main attributes that characterize the quality of the probabilistic models namely reliability and resolution [35, 36]. Reliability or calibration evaluates the statistical consistency between the forecasts and the observations. In the case of a continuous variable like GHI, a high reliability is obtained if predictive distributions and distributions of observations agree. Resolution refers to the ability of the probabilistic model to discriminate among different forecast situations. More precisely, the more distinct the observed frequency distributions for various forecast situations are from the full climatological distribution, the more resolution the forecast model has. A high quality probabilistic

model should issue reliable forecasts with high resolution. In other words, high reliability is a necessary but not a sufficient condition for a high quality probabilistic forecast. The forecast should also exhibit high resolution. For instance, climatological forecasts are perfectly reliable but exhibit no resolution.

3.2. CRPS

In the verification framework proposed by Lauret et al. [25], the authors recommend the computation of a score like the Continuous Ranked Probability Score (CRPS) to evaluate the overall quality of the probabilistic models. We recall here the definition of the CRPS.

3.2.1. Definition

The CRPS measures the difference between the predicted and observed cumulative distributions functions (CDF) [38]. The CRPS reads as

$$CRPS = \frac{1}{N} \sum_{i=1}^{N} \int_{-\infty}^{+\infty} \left[\hat{F}_{fcst}^{i}(y) - F_{y_{obs}}^{i} y) \right]^{2} dy, \tag{8}$$

where $\hat{F}_{fcst}(y)$ is the predictive CDF of the predictand Y (here GHI) and $F_{y_{obs}}(y)$ is a cumulative-probability step function that jumps from 0 to 1 at the point where the value of the predictand y equals the observation y_{obs} (i.e. $F_{y_{obs}}(y) = 1_{\{y \ge y_{obs}\}}$). The squared difference between the two CDFs is averaged over the N forecast/observation pairs. The CRPS score rewards concentration of probability around the step function located at the observed value [35]. In other words, the CRPS penalizes lack of resolution of the predictive distributions as well as biased forecasts. Note that the CRPS is negatively oriented (smaller values are better) and it has the same dimension as the forecasted variable. CRPS is a proper score meaning that it obtains the best expected value when the forecast distribution is equal to the true distribution of probability of the observation. Besides, using proper scoring rules allows the decomposition of the score into the two important attributes of the quality of a forecasting probabilistic model namely resolution and reliability. This permits to understand more precisely the characteristics of the quality of the forecast.

3.2.2. CRPS Skill Score

In a similar manner, skill scores are used to assess the forecast skill of deterministic forecasts [39], Pedro et al. [40] used the CRPS Skill Score (CRPSS) to gauge the quality of their probabilistic forecasting models against a reference method. The CRPSS metric (in %) reads as

$$CRPSS = 100 \times \left(1 - \frac{CRPS_m}{CRPS_r}\right), \tag{9}$$

where CRPS_r denotes the CRPS of the reference method and CRPS_m refers to the CRPS of the model under evaluation (see Table 2). A negative value of CRPSS indicates that the probabilistic method fails to outperform the reference model while a positive value of

CRPSS means that the forecasting method improves on the reference model. Further, the higher the CRPSS, the better the improvement.

In this work, and following the recommendations of Doubleday et al. [41], the raw output of the ECMWF-EPS serves as the reference benchmark model.

3.2.3. Decomposition of the CRPS

The decomposition of the CRPS is given by:

$$CRPS = REL - RES + UNC, (10)$$

where REL, RES and UNC are respectively the reliability part, the resolution part and the uncertainty part of the CRPS. The interested reader is referred to [25] for details regarding the computation of the different components of the CRPS.

In addition to reliability and resolution, the uncertainty term accounts for the variability of the observations. It is an indication of the difficulty to forecast the variable of interest and cannot be modified by the forecasting model. It is also worth noting that the uncertainty part UNC corresponds to the score of the climatology. For scores like CRPS that are negatively oriented, the goal of a forecasting model is to minimize (resp. maximize) as much as possible the reliability term (resp. the resolution term). In fact, a forecasting model with a high resolution term means that the model has captured the maximum of the variability present in the data (which variability is measured by the uncertainty term).

3.3. Contributions of the statistical moments of the forecast distribution to the CRPS

In this study, a new methodology for a better understanding of the skills of a probabilistic forecast in relation with the CRPS score is developed. The main idea is to assess separately the contribution of the statistical moments (mean, variance, etc.) of the predictive distributions to the CRPS and consequently to the quality of a probabilistic forecasting model. The principle of the method is to create two virtual forecasts which show the contribution of the statistical moments of the actual forecast to the CRPS. Let us illustrate the methodology with 3 forecast PDFs depicted in Figure 4. f represents the actual forecast PDF and f_{m1} and f_{m2} the associated virtual PDF forecasts.

The first virtual forecast f_{m1} is derived from the first moment (mean) of the actual forecast f. Let m_1 be the first moment of f and δ the Dirac distribution (corresponding to the dotted vertical line in Figure 4), the PDF of f_{m1} is thereby defined by:

$$f_{m1}(y) \equiv \delta(y - m_1). \tag{11}$$

Note that this definition implies that the second, third and further moments of f_{m1} are equal to 0.

The second virtual forecast f_{m2} is given by a Gaussian distribution with first and second moments equal to those of f. Let m_2 be the second moment of f, f_{m2} is defined as:

$$f_{m2} \sim \mathcal{N}(m1, m2). \tag{12}$$

Being a Gaussian distribution, the third, fourth and further moments of f_{m2} are equal to 0.

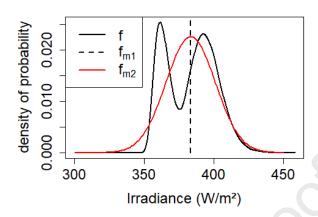


Figure 4: Illustration of the virtual forecasts f_{m1} and f_{m2} related to the forecast PDF f

The contribution of the statistical moments of the distribution to the CRPS is computed as follows. First, the CRPS of each forecast namely $CRPS_f$, $CRPS_{fm1}$ and $CRPS_{fm2}$ are averaged over the N forecast/observation pairs. This leads to the corresponding values CRPS, $CRPS_{m1}$ and $CRPS_{m2}$. Second, the difference $G_2 = CRPS_{m1} - CRPS_{m2}$ and $G_+ = CRPS_{m2} - CRPS$ are calculated. Note that one can therefore rewrite the CRPS as:

$$CRPS = CRPS_{m1} - G_2 - G_+.$$
 (13)

Note that the $CRPS_{m1}$ of the deterministic forecast f_{m1} is actually its Mean Absolute Error (MAE)² (see [38] for details).

 G_2 is the measure of the gain in CRPS or equivalently in forecast quality that results from the additional information brought by the second moment of the distribution. G_+ represents the gain resulting from the other statistical moments. G_2 is assumed to be positive. If it is found negative, then the probabilistic forecast has no added value compared to a deterministic forecast. Indeed, the CRPS of the probabilistic forecast would be higher than the CRPS of the deterministic one $(CRPS_{m_1}, \text{which})$, thus denoting a loss of quality of the probabilistic forecast. On the other hand, G_+ is generally positive. It can be null or negative if the forecast distribution obtains a higher CRPS score than a Gaussian distribution defined by $\mathcal{N}(m_1, m_2)$. This would indicate that the forecast distribution is less suitable than a Gaussian distribution.

In section 5.3 below, we propose to present this diagnostic tool under the form of a barplot, where CRPS, G_+ and G_2 are stacked in this order. G_2 is denoted by the pink part of the bar, G_+ by the green part and CRPS by the blue part. Note that a black line on the top of the blue part is used to better highlight the value of the CRPS and a dotted black line

²Similarly to RMSE, MAE is also a common metric used to assess the accuracy of deterministic forecasts.

indicates $CRPS_{m1}$ (see Figure 6). In the following, we refer to this diagnostic tool based on the contribution of the moments of the forecast distributions to the CRPS as "MC-CRPS".

393 4. Case studies

Six sites are chosen to test the selected models. The first one, Desert Rock, which is part of the SURFRAD network, is located in an arid area. It experiences a high occurrence of clear skies and consequently a very low variability. Two other sites, the airport of Hawaii, where the NREL set up a radiometric network, and Saint-Pierre, which is located on the coastal part of the island La Réunion, are insular sites. Both present a high yearly solar irradiation but also an important variability due to frequent partly cloudy skies. These differences between the two types of sites will permit testing the models under different sky conditions. For an extensive study on the multiple factors that impact the climatology and sky conditions in the specific case of Saint-Pierre and La Réunion, see Badosa et al. [42] or Kalecinski [43].

As the aforementioned sites exhibit a similar level of irradiation, three other BSRN sites namely Palaiseau, Tiruvallur and Langley are also considered to test our methodology. The six chosen sites experience different levels of annual solar irradiation and of sky conditions. Thus, this set of sites is representative of the various climates around the world. The main characteristics of these six sites are given in Table 3. The solar variability, presented in the last line of Table 3, is defined as the standard deviation of the changes in the clear sky index [44].

4.1. Measurements

The measured data used in this work are global horizontal irradiance (GHI) time series recorded at the six considered sites. These datasets have been prepared for previous works related to the development and the benchmarking of probabilistic solar forecasts [45, 46]. They correspond to two years of data divided in a training set (the first year) and test set (the second year). As the ensemble forecasts used here are provided with a 3-hour time step, the recorded time series, initially formatted with a 1-hour granularity, were averaged with a 3-hour time step. A quality check and several test were performed on the recorded GHI time series. The results are given in Appendix A.

	Desert Rock	Hawaii	Saint-Pierre
	(USA)	(USA)	(Reunion)
Acronym	DR	HAW	SP
Provider	SURFRAD	NREL	PIMENT
Position	36.6N, 119.0W	21.3N, 158.1W	21.3S, 55.5E
Elevation (m)	1007	11	75
Climate type	Desert	Insular tropic	Insular tropic
Years of record	2012 - 2013	2010-2011	2012 - 2013
Annual solar irradiation (MWh/m^2)	2.105	1.969	2.053
Solar variability 1-h $(\sigma \Delta k t_{1hour}^*)$	0.146	0.209	0.241
	Palaiseau	Tiruvallur	Langley
	Palaiseau (France)	Tiruvallur (India)	Langley (USA)
Acronym			
	(France)	(India)	(USA)
Acronym	(France) PAL	(India)	(USA) LAN
Acronym Provider	(France) PAL BSRN	(India) TIR BSRN	(USA) LAN BSRN
Acronym Provider Position	(France) PAL BSRN 48.7N, 2.2E	(India) TIR BSRN 13.1N, 80.0E	(USA) LAN BSRN 37.1N, 76.4W.
Acronym Provider Position Elevation (m)	(France) PAL BSRN 48.7N, 2.2E 156	(India) TIR BSRN 13.1N, 80.0E 36	(USA) LAN BSRN 37.1N, 76.4W.
Acronym Provider Position Elevation (m) Climate type	(France) PAL BSRN 48.7N, 2.2E 156 Mild oceanic	(India) TIR BSRN 13.1N, 80.0E 36 Monsoon	(USA) LAN BSRN 37.1N, 76.4W. 3 Humid

Table 3: Main characteristics of time series of recorded global horizontal irradiance (GHI) used to test the models.

420 4.2. Forecasts

As mentioned above, the initial day-ahead ensemble forecasts, covering the same period as the measurements, are provided by the European Centre of Medium-Range Weather Forecasts (ECMWF). The EPS is released by ECMWF at 12:00 for the 72 next hours with a 3-hours timestep which allows it to be used for day-ahead scheduling or trading purposes.

425 5. Results

Based on the verification framework proposed by Lauret et al. [25], the overall performance of the different probabilistic methods is measured by the CRPS and the CRPSS. Detailed insight in the quality of the models is obtained through the decomposition of the CRPS and the new "MC-CRPS" method. Note that this section is dedicated to the presentation of the main results of the study. The next section will be devoted to an in-depth discussion related to the pros and cons of each approach and the added-value brought by the MC-CRPS methodology.

5.1. Overall performance of the methods

Table 4 lists the CRPS obtained by the different methods. However, in order to better highlight the relative merits of each approach, Figure 5 shows the CRPS skill scores of all

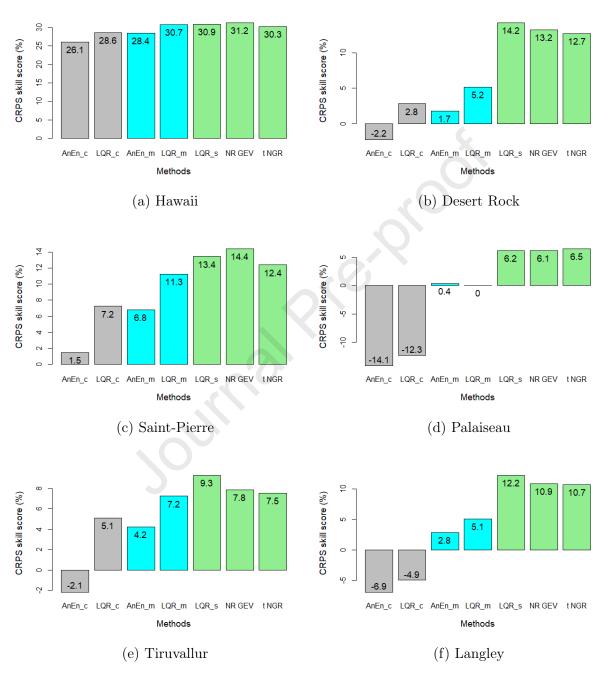


Figure 5: CRPS Skill Score of all models for the six considered sites. Grey: deterministic-based approach, Cyan: ensemble-based approach using the mean of the members, Green: ensemble-based approach using mean and standard deviation of the members.

the forecasting models. Let us recall that positive values of skill scores mean that the model outperforms the reference model (here the raw ECMWF-EPS) while negative values reveal that the quality of the evaluated model is worse than the reference one.

As shown by Figure 5, regardless the site under study, the highest CRPS skill scores are obtained by the ensemble-based approach (represented by the cyan and green bars). Conversely, except the case of Hawaii, the deterministic-based approach (grey bars) yields lower or even negative skill scores. These negative CRPSS values indicate that the deterministic-based models do not always achieve to increase the quality of the raw ensemble forecasts (see for example Palaiseau and Langley).

A deeper look into the performance of the ensemble-based approach shows that models using the mean and the standard deviation of the ensemble members (green bars) exhibit a better forecast skill than models using only the mean of the members (cyan bars) albeit the improvement is less pronounced for Hawaii. Overall, the model with the highest skill score appears to be either LQR_s or NR_GEV . Regarding the latter, it may suggest that a judicious choice of the underlying PDF (see Equation 6) used by a calibration technique like Nonhomogenous Regression (NR) can further improve the quality of the probabilistic forecasts.

Finally, in order to quantify the relative improvement provided by the ensemble-based approach over the deterministic-based approach, we calculate the gain in CRPS based on the CRPS values of the best performer of each approach. It appears that the level of improvement is very dependent on the studied site. It is moderate for Hawaii and Tiruvallur (4%), becomes larger for Saint-Pierre (approximately 8%) and quite significant for Desert Rock (approximately 12%), Langley and Palaiseau (approximately 16%).

5.2. Detailed insight through the decomposition of the CRPS

Table 4 also provides the decomposition of the CRPS into reliability and resolution of the different forecasting methods. As mentioned previously, a forecast should exhibit a small reliability term and a large resolution term. It is worth mentioning first that all models significantly improves the reliability component of the raw EPS forecasts and that the level of improvement strongly depends on the reliability of the initial raw ensemble. Second, it can be noted that the reliability of all calibrated forecasts is fairly comparable. In addition, regardless the site, it appears that, overall, the ensemble-based approach does not significantly improve reliability compared to the deterministic-based approach. Looking in more details, models based on the AnEn technique often appears to generate the most reliable forecasts while the t_NGR model generally provides the less reliable forecasts. Also, in the case of Non homogeneous calibration technique, GEV distributions seem to be more suitable than Gaussian distributions, since NR_GEV is slightly more reliable than the t_NGR model.

Regarding the resolution component, it must be noted first that the deterministic-based approach fails to improve the resolution of the raw Ensemble. Conversely, resolution increases with the ensemble-based approach, and particularly when the spread of EPS members is taken as as input of the models i.e. case of the LQR_s , t_NGR and NR_GEV

	Site	HAW	DR	SP	PAL	TIR	LAN
	raw Ensemble	67.7	29.4	59.4	38.6	46.8	40.0
	$AnEn_c$	50.1	30.1	58.5	44.0	47.8	42.8
	LQR_c	48.4	28.6	55.1	43.3	44.4	42.0
CRPS (W/m^2)	$AnEn_m$	48.5	28.9	55.3	38.4	44.9	38.9
	LQR_m	46.9	27.9	52.7	38.6	43.4	38.0
	LQR_s	46.8	25.2	51.4	36.2	42.5	35.2
	t_NGR	47.2	25.7	52.0	36.2	43.3	35.8
	NR_GEV	46.6	25.5	50.8	36.2	43.2	35.7
	raw Ensemble	23.2	8.4	13.4	7.5	11.5	8.2
	$AnEn_c$	4.2	4.8	6.6	4.9	7.2	4.8
	LQR_c	4.4	5.3	7.1	5.4	6.7	5.3
Reliability (W/m^2)	$AnEn_m$	4.1	4.7	6.2	4.9	7.9	4.5
	LQR_m	4.4	5.7	7.0	5.7	8.2	5.0
	LQR_s	4.5	5.9	7.6	5.3	8.2	5.4
	t_NGR	4.7	6.5	8.4	5.4	8.0	5.7
	NR_GEV	4.1	6.2	7.2	5.4	7.8	5.8
	raw Ensemble	113.3	154.0	126.7	95.4	125.7	122.5
	$AnEn_c$	111.9	149.7	120.8	87.4	120.4	116.4
	LQR_c	113.9	151.7	124.7	88.6	123.3	117.7
Resolution (W/m^2)	$AnEn_m$	113.4	150.8	123.5	93.0	124.0	120.0
	LQR_m	115.3	152.8	127.0	93.6	125.8	121.4
	LQR_s	115.5	155.6	128.9	95.6	126.8	124.7
	t_NGR	115.3	155.7	129.0	95.8	125.8	124.3
	\overline{NR}_GEV	115.3	155.6	129.1	95.6	125.7	124.5
Uncertainty (W/m^2)	All Models	157.8	175.0	172.7	126.5	161.0	154.4

Table 4: CRPS and its components reliability, resolution and uncertainty of all considered models for the 6 sites. Cyan: deterministic-based approach, Green: ensemble-based approach. Red values indicate the worst CRPSs while the black bold ones show the best CRPSs.

models. Finally, one can state that the decomposition of the CRPS given in Table 4 reveals that the difference in quality between the two approaches is mainly explained by the resolution component, whereas reliability is fairly comparable.

o 5.3. Detailed insight through the CRPS Moments-Contributions

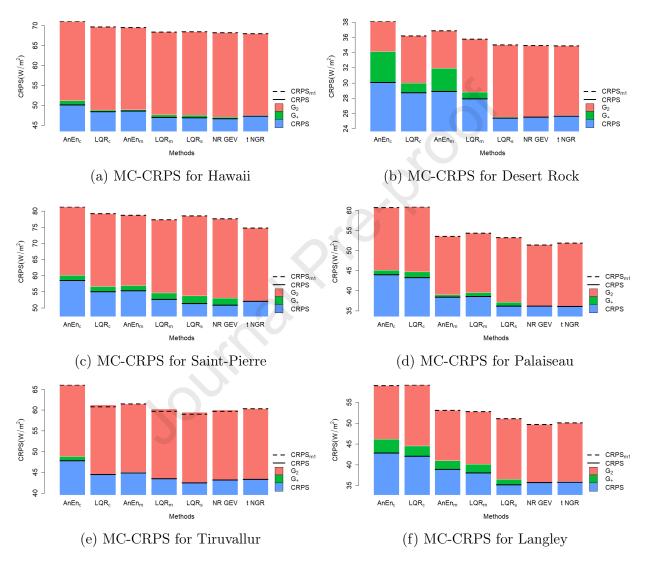


Figure 6: MC-CRPS of the six sites and all forecasting models. A black line is used to better highlight the value of the CRPS and a dotted black line indicates the value of $CRPS_{m1}$.

Figure 6 shows the results of the MC-CRPS introduced in section 3.3. As seen, the final CRPS values, of the forecasting models occur to be dependent on their respective $CRPS_{m1}$ values. In particular, models from the ensemble-based approach appear to have best $CRPS_{m1}$ than models from the deterministic-based approach (see for instance the case of Langley). This means that the aggregation of members improves the estimation of the first

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moment. Among the ensemble-based models, except for the cases of Hawaii and Tiruvallur, the superiority of the LQR_s , NR_GEV and tNGR models using the mean and standard deviation of the ensemble members can be mainly explained by a greater contribution of G_2 . Thus the spread of EPS members is effective and improves more importantly G_2 than $CRPS_{m1}$. Further, the best performer among the three aforementioned models is finally determined by G_+ . This highlights the importance of the choice of the distribution in the non homogenous regression calibration framework.

For example, overall, NR_GEV performs better than the t_NGR model because of G_+ . Let us stress that the choice of strictly truncated Gaussian distributions in the implementation of a NGR technique forces G_+ to be very close to 0 in the MC-CRPS. Hence, the benefits of GEV distributions compared to Gaussian distributions are highlighted by the MC-CRPS method.

498 6. Discussion

In this section, we try to give more clues regarding the merits of each proposed approach.

Also, a discussion related to the advantages brought by the MC-CRPS is proposed.

6.1. Deterministic-based approach versus ensemble-based approach

Let us recall that the deterministic-based approach uses a unique deterministic predictor while the ensemble-based approach makes use of the information conveyed by the ensemble. Therefore, the main weakness of the deterministic-based approach is the lack of information feeding the models. Since the distribution needs to be completely determined from one single deterministic predictor, the spread and the possible skewness and kurtosis of the forecasting distribution need to be only inferred from this single predictor. Conversely, the benefits gained from the multiplicity of predictors provided by the ensemble-based approach need to be significant to justify the computation of the EPS. Two types of benefits can be discussed.

First, the aggregation of predictors leads to a better estimation of the first moment. This is visible in Figure 6 where models issued from the ensemble-based approach get better $CRPS_{m1}$ than models from the deterministic-based approach. It is clear that a gain in the estimation of the first moment can be obtained by the substitution of the control member by the mean of all members.

Second, regarding the determination of the second moment, the uncertainty is already carried by the level of forecasting of the mean of the EPS members. These variables are dependent, as shown in Appendix B (the standard deviations of the observations clearly depends on the level of forecasting). Hence, using the spread of the members of EPS as input of the forecasting models can only be justified if it brings an extra-information on the uncertainty. It is assumed that the spread of the members is higher if the uncertainty is so. Indeed it indicates if slight errors in the initial conditions could lead to great differences in the final state of the atmosphere.

Thus, it appears necessary to investigate on the quantity of information actually provided by the spread of the members. In order to do this, the correlation between the standard deviation of the observations and the spread of the members has been studied. This has been made for a fixed level of forecasting, in order to remove the dependency between uncertainty and level of forecasting. Then an average over all levels of forecasting has been calculated to produce Figure 7. This kind of plot is of great utility to know the added value of the standard deviation of the EPS forecast members. If the dependence between the spread of the members and the uncertainty of the forecast for a fixed level of forecasting is strong, then a large improvement can be expected for calibration models using the spread of the members as an input, compared to simpler models.

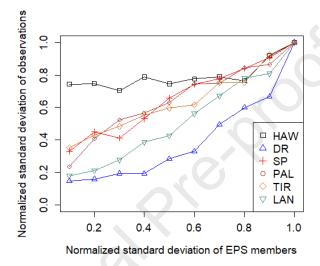


Figure 7: Standard deviation of observations vs. standard deviation of the EPS members (raw ECMWF ensembles). Normalization of the standard deviation has been done by dividing the standard deviations by the maximum of the standard deviation for each site.

As shown by Figure 7, the amount of new information given by the spread of the members is very dependent on the studied site. When for Hawaii, the correlation between the standard deviation of the observations and the spread of the members is almost null, it is quite significant for the other sites and especially for Langley and Desert Rock. A link can be established between this finding and Figure 5 which shows that the success of taking into account the spread of members in the forecasting models depends on the site. It is clearly less valuable in Hawaii than in other sites, and it is particularly successful in Desert Rock and Langley. It is also consistent with Figure 6 where G_2 is significantly higher in Desert Rock for LQR_s , t_NGR and NR_GEV models.

6.2. Discussion related to CRPS Moments-Contributions

In order to consolidate the results obtained in Figure 6, a complete analysis of the statistical moments of the probability distributions produced by the forecasting methods has been conducted. This kind of study is traditionally done to assess the strengths and weaknesses of a forecasting model. Although the deterministic measure of a statistical moment is not a proper scoring rule, it is of great interest to use it to understand the behaviour of the forecasting models.

First, an evaluation of the accuracy of the first moment has been conducted. A good forecasting model should have the ability to give a mean value of the forecasting distributions as close as possible to the mean of the observation values. A measure of this ability can be obtained by calculating the Root Mean Square Error (RMSE) or Mean Absolute Error (MAE) of the mean of the forecasting distributions. In this study, the MAE has been chosen as it is exactly the definition of $CRPS_{m1}$ introduced in section 3.3 (see [38] for details). Figure 6 gives therefore the results related to the accuracy of the first moment of the distributions.

Second, a probabilistic forecast also provides an estimation on the level of uncertainty, which is reflected by the spread of the forecasting distribution (i.e. the second statistical moment). Some works have been specifically dedicated to the assessment of the accuracy of the spread of the predictive distributions. Among others, one can cite the studies related to the spread-skill relationship (see [48] or [49]). These works are guided by the idea that the variance of a probabilistic forecast should be larger if the uncertainty of the forecast is so. Fortin et al. [50] proposed a criterion for the evaluation of the accuracy of the second moment of the distributions. This criterion is based on the fact that statistical consistency requires that the spread of the forecasting distributions should be equal to the RMSE of the mean of the forecast. Following [50], spread is calculated as the square root of the mean of the variances of the forecasting distributions. The accuracy of the second moment is therefore measured by calculating the RMSE of the differences between spread and RMSE of the mean of the distributions (i.e. $RMSE_M$). Figure 8 plots the RMSE of the difference ($spread-RMSE_M$), computed over the evaluation period.

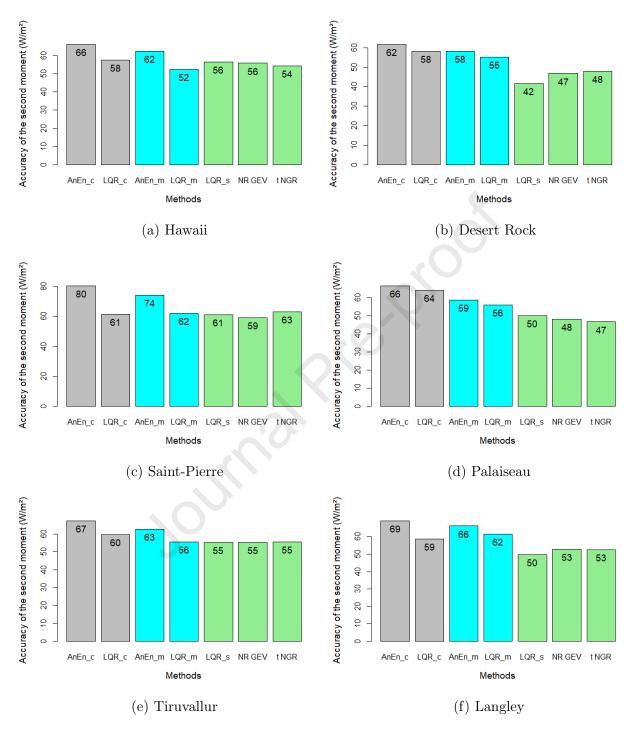


Figure 8: Accuracy of the second moment for the six studied sites and all forecasting models

Conversely to the first moment, the accuracy of the second moment gradually improves when the information taken by the forecasting model is more complete. Using the mean of members instead of the control member increases the second moment accuracy. Taking

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into account the spread of the EPS improves further the accuracy by approximately the same extent (except for Hawaii, for the reasons discussed in section 6.1). Nevertheless, this improvement depends on the site. As shown by Figure 8, the accuracy of the second moment for Hawaii is almost equal for each model. It is consistent with the results depicted in Figure 7, showing that the information of the second moment of the EPS distribution in Langley and Desert Rock is the most valuable, as opposed to the information of Hawaii EPS distribution.

The accuracy of the second moment can be linked to the gain G_2 introduced in the MC-CRPS section (see section 3.3). The correlation between these two values is highlighted in Figure 9, which shows the ratio $G_2/CRPS_{m1}$ versus the accuracy of the second moment.

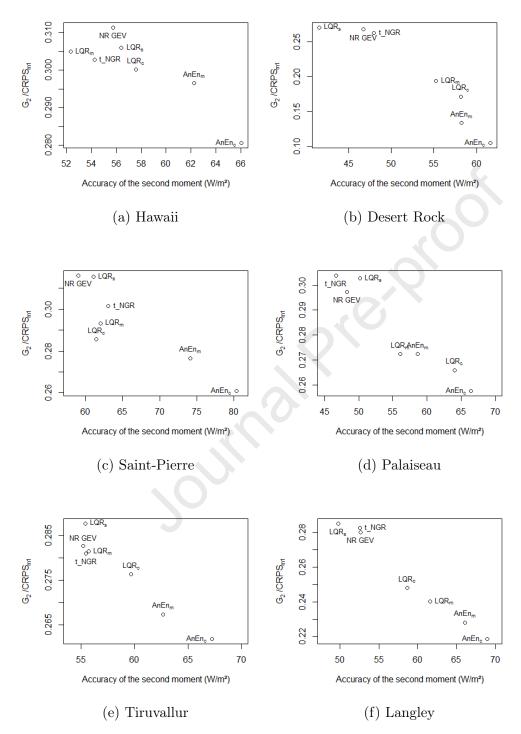


Figure 9: Link between G_2 and the accuracy of the second moment.

To sum up, the great advantage of the MC-CRPS is to reconcile the score of a probabilistic forecasting model and the explanation of its performance by examining the accuracy

of the moment-based distributions.

Moreover, the link between the calibration of the moments and the score is highlighted, because the contribution of the accuracy of the moments to the score is quantified. Here, in the proposed new diagnostic tool MC-CRPS, the accuracy of the statistical moments of the forecasting distributions is quantified by the proper score itself. This diagnostic tool is complementary of the decomposition discussed in section 3.2.3, i.e. the reliability and resolution of f_{m1} and f_{m2} can also be computed and studied. The MC-CRPS diagnostic tool also highlights the benefits of probabilistic forecasting, as the comparison between $CRPS_{m1}$ and CRPS provides a measure of the quality difference between deterministic and probabilistic forecasting.

7. Conclusions

Based on the two types of forecasts i.e deterministic or ensemble forecast (denoted by the term EPS for ensemble prediction system) issued by the meteorological centre ECWMF, two approaches for generating day-ahead solar irradiance probabilistic forecasts were proposed. The first approach creates probabilistic forecasts from the deterministic day-ahead GHI predictor while the second one generates probabilistic forecasts from the calibration of the EPS or from information inferred from the EPS.

The goal of this work was to quantify the possible added-value of the EPS on the quality of the forecasts. Six sites experiencing different sky conditions were chosen for the appraisal of the different probabilistic models. Quality of the different probabilistic models have been evaluated with common diagnostic tools such as the CRPS and its decomposition. A new diagnostic tool called MC-CRPS has also been introduced. It consists in the measure of the contribution of each statistical moment of the forecasting distributions to the CRPS.

Overall, models adopting the ensemble-based approach have been found to issue probabilistic forecasts with better quality than the ones based on the deterministic-based approach. The gain in quality, based on the CRPS metric, ranges from 4 % up to 16 %.

One other important contribution of this work is the new diagnostic tool related to the CRPS score based on the moments of the ensemble distribution called MC-CRPS. This MC-CRPS tool allowed to identify two characteristics of EPS that have an impact on the quality of probabilistic forecasts. First, the aggregation of deterministic predictors of the ensemble leads to an improvement of the estimation of the first moment and thus, raises the overall quality of a probabilistic forecast. Second, the spread of the EPS members turns to be a good predictor that permits to enhance the estimation of the second moment of the forecasting distributions. Finally, in terms of forecast quality, it can be concluded that using an EPS (which requires high computing capacities) to produce day-ahead GHI probabilistic forecasts should be favored compared to a deterministic (less demanding) approach. This work opens the way to the assessment of the forecast value of each approach i.e. the benefit (economical or others) gained from the use of these probabilistic forecasts in an operational context.

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Appendix A. Data quality check

A quality check has been conducted for the observation data of each of the six studied sites. As the decomposition of irradiance into diffuse and direct has not been measured, the exhaustive set of BSRN recommended quality checks could not been conducted (see [51]), but only the first plot. It consists in the plot of measured irradiance versus solar zenith angle. The rarely reached limit is plotted in dashed line and the physical possible limit is plotted in solid line. The second check is a frequency histogram of the clear-sky index (k*)

for each site. k* is defined as:

$$k* = \frac{Irradiance}{ClearSky\ Irradiance} \tag{A.1}$$

where the clear-sky irradiance is calculated with the Bird clear-sky model [52]. The maximum of the observed frequency is supposed to be at $k^* = 1$. The third check is a plot of the k^* , only for clear-sky days. The morning data is reported by black dots and afternoon data by red dots. From this plot, it is possible to see if clear-sky irradiances are well-reported by the measurement data. If not, the line drawn by the dots is not straight. To extract clear-sky days from the data, the process proposed in Badosa et al. [42] has been followed. The last figure is a plot of the k^* for each hour and day of the year. It allows to detect if systematical biases exist at some days/hours of the year. It also allows to easily detect missing data.

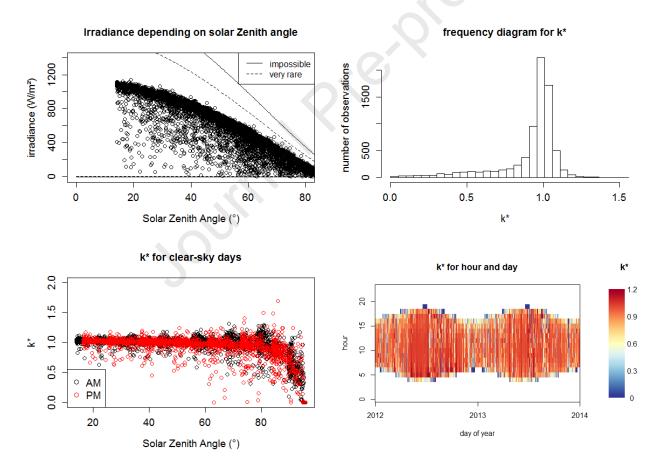


Figure A.10: Desert Rock

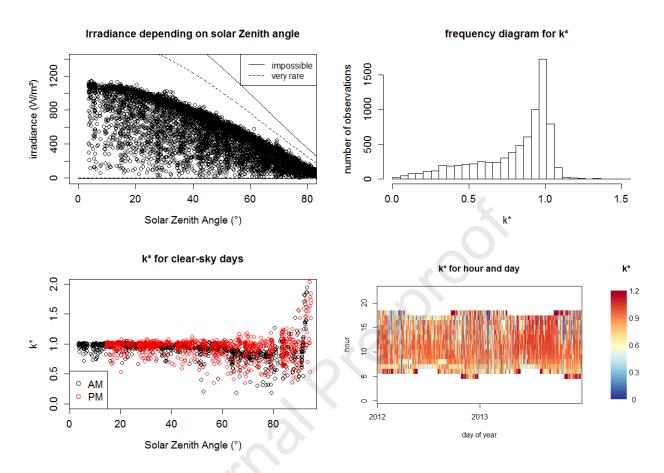


Figure A.11: Saint-Pierre

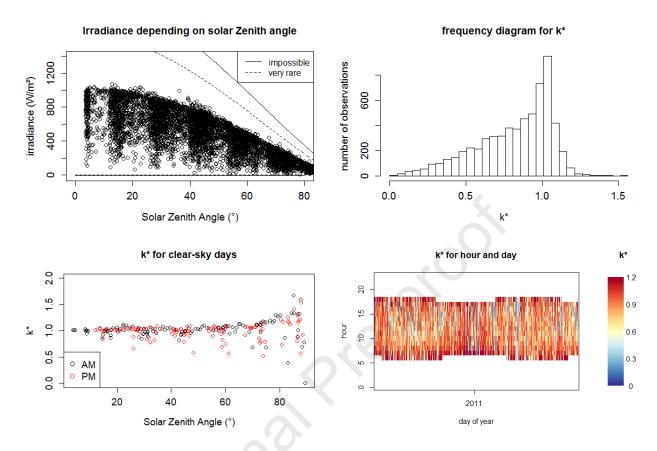


Figure A.12: Hawaii

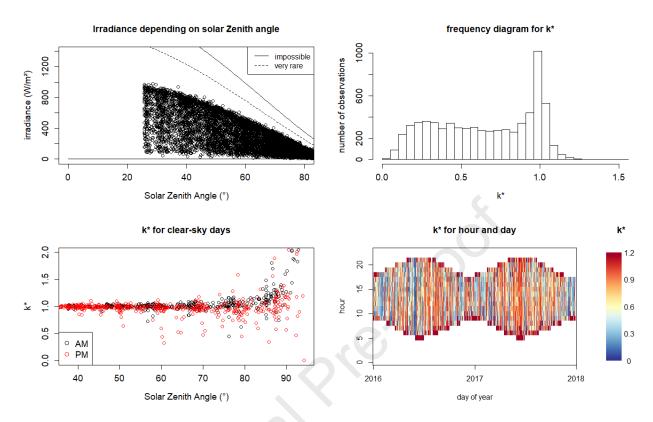


Figure A.13: Palaiseau

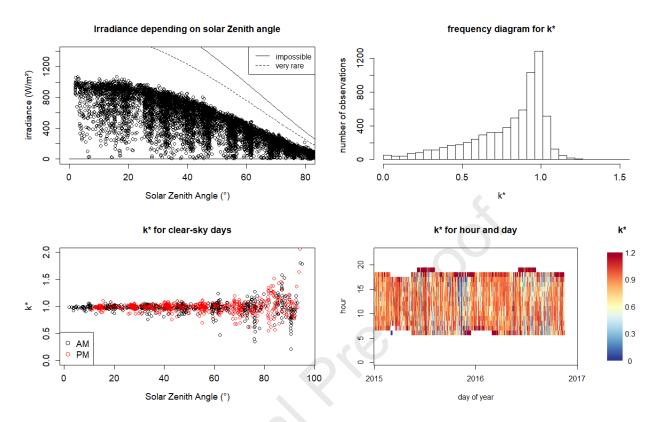


Figure A.14: Tiruvallur

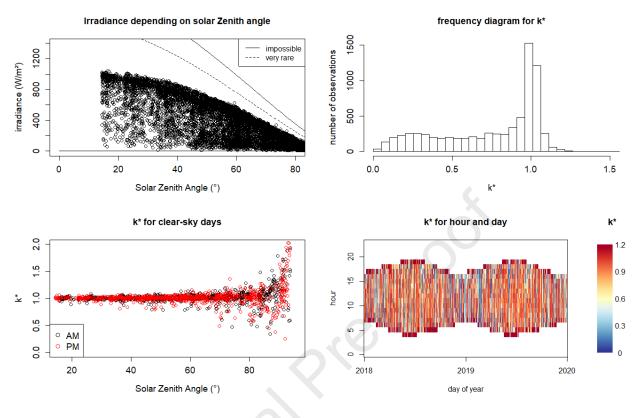


Figure A.15: Langley

No major issues have been detected concerning the six studied sites. For some sites (Tiruvallur, Langley, Saint-Pierre), it is possible to guess that some reflexions occur for extreme hours and some seasons. This leads to the phenomenon of overirradiance where k* can easily reach a value of 4.

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Appendix B. Bias and standard deviation of EPS members distribution and observations for the six sites

The definition of the probabilistic forecast presented in section 2.3.1 is often underdispersive, and consequently obtains poor scores. The associated rank histograms usually get characteristic U-shapes, with overpopulated extreme ranks. In this section, we attempt to demonstrate why a calibration procedure is needed for raw forecasts. To this end, a comparison between members distributions and observation distributions depending on the level of forecasting has been conducted for the 2 first statistical moments. These plots show clearly under-dispersive raw ensembles. The standard deviations need to be corrected. The discrepancy between distributions of members and observations indicates a statistical inconsistency between observations and forecasts, and therefore a bad reliability, and justifies the use of calibration models.

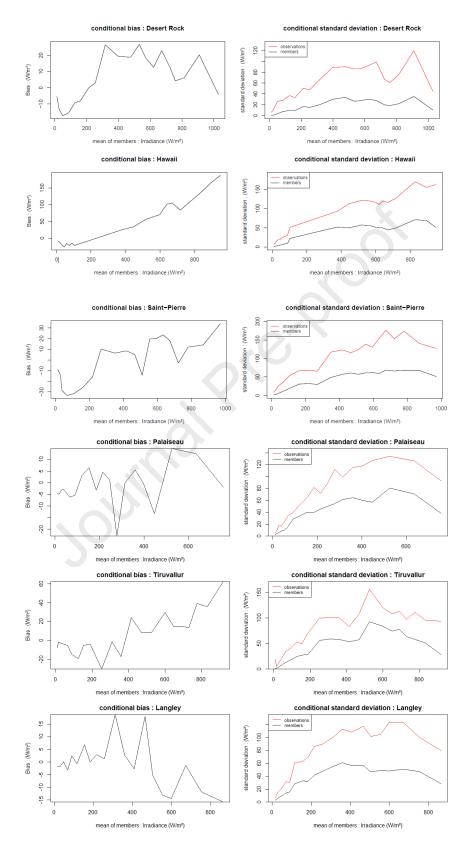


Figure B.16: Bias and standard deviation of EPS members distribution and observations for the six sites, depending on the level of forecasting

Appendix C. Selection of the optimal α

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Figure C.17 presents the results related to the optimal selection of the parameter α . As shown by Figure C.17, regardless of the site under study, the optimal value corresponds to the minimum of the CRPS calculated on the training evaluation set.

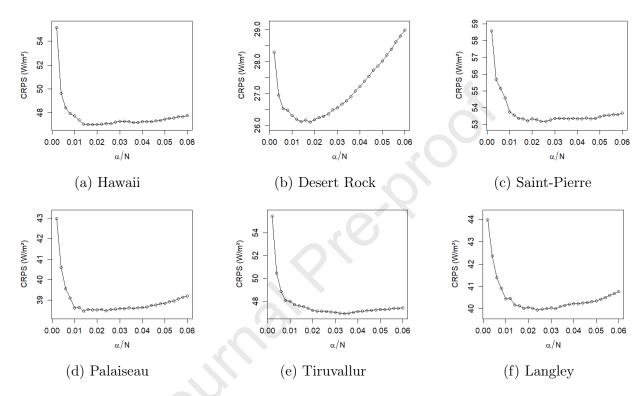


Figure C.17: Determination of the α . The optimal value corresponds to the minimum of the CRPS.

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- Probabilistic forecasts from deterministic informations and from Ensembles compared
- Several models either parametric and non-parametric are compared
- New tool to quantify the contributions of the statistical moments to the quality
- Sites with very different sky conditions are considered
- Using Ensemble Prediction Systems improve the quality of forecasts

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Declaration of interests	
oximes The authors declare that they have no known competing that could have appeared to influence the work reported in t	·
☐ The authors declare the following financial interests/perso as potential competing interests:	onal relationships which may be considered
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