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1 Intercalibration of survey methods using paired fishing
2 operations and log-Gaussian Cox processes

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Abstract

We present a statistical method for intercalibration of fishery surveys methods, i.e. determining the difference in catchability and size selectivity of two methods, such as trawl gears or vessels, based on data from paired fishing operations. The model estimates the selectivity ratios in each length class by modelling the size distribution of the underlying population at each station and the size-structured clustering of fish at small temporal and spatial scales. The model allows for overdispersion and correlation between catch counts in neighboring size classes. This is obtained by assuming Poisson distributed catch numbers conditional on unobserved log-Gaussian variables, i.e. the catch is modelled using log-Gaussian Cox processes. We apply the method to catches of hake (*Merluccius Paradoxus* and *M. Capensis*) in 341 paired trawl hauls performed by two different vessels, viz. the RV Dr. Fridtjof Nansen and the FV Blue Sea, operating off the coast of Namibia. The results demonstrate that it is feasible to estimate the selectivity ratio in each size class, and to test statistically the hypothesis that the selectivity is independent of size or of species. For the specific case, we find that differences between size classes and between species are statistically significant.

Keywords: Selectivity; Intercalibration; Mixed-effects models; and Log-Gaussian Cox processes

1 Introduction

Fishery-independent surveys are of pivotal importance for fish stock assessments, where they provide a relative abundance index, as well as for basic biological research [Millar, 1992]. While the objective of a survey is to assess the abundance of the underlying population, it only provides a filtered view, specified by the selectivity of the operation. The vessels, riggings, and gears applied in these surveys often develop or shift over time, as do fishing methods by captains [Weinberg and Kotwicky, 2008], leading to changes in size selectivity and overall catch efficiency [Miller, 2013, Thorson and Ward, 2014]. To maintain as long time series as possible, it is often desirable to combine information from different operations. However, differences in selectivity of vessel-gear combinations must be accounted for before time series and spatial distribution data can be combined and synthesized, which can be problematic [Axelsen and Johnsen, 2015]. To this end, dedicated experiments may be performed, involving two or more vessel-gear combinations, with the objective of calibrating these combinations against each other, i.e. intercalibration. Here, the difference in catch rates are investigated by performing pairwise near-simultaneous hauls in the same area, so as to minimize the time-space variation of the fished population between the hauls. With such data, the selectivity ratios, which measure the efficiency of the two vessel-gear combinations against each other, can be estimated for

62 each species and each size class. Then, these selectivity ratios can be used as calibration
63 factors by adjusting catches from one type of operation so that they are comparable with
64 the catches from the other operation [Kotwicky et al., 2017].

65 Multiple calibration procedures have been proposed and applied over time, in partic-
66 ular differing in how the size dependency in selectivity ratios is modelled and estimated.
67 When considering the selectivity curve of a single gear, a common choice is to restrict
68 attention to a parametric family of curves; for example logistic functions for towed gear
69 and Gaussian functions for gill nets [Millar and Fryer, 1999]. When comparing two gears,
70 a typical choice has been to use polynomials in length to describe the ratio between
71 the two selectivity curves [Millar et al., 2004, Lewy et al., 2004, Holst and Reville, 2009,
72 Kotwicky et al., 2017]. The coefficients in these polynomials may be estimated in a GLM
73 framework, but a point of particular importance is to allow for overdispersion relative
74 to Poisson counts [Lewy et al., 2004]. This overdispersion arises for many reasons, in-
75 cluding between-haul variation in the selectivity [Millar, 1993]. If this effect is ignored,
76 and catches from different hauls are pooled, it will lead to overconfidence in the accuracy
77 of estimates; a remedy is to use a double bootstrap to assess the accuracy of estimates
78 [Millar, 1993, Sistiaga et al., 2016]. An alternative is a GLMM approach where the rela-
79 tive selectivity curves are allowed to vary between hauls; either non-parametrically using
80 autoregressive processes [Cadigan et al., 2006] or parametrically in terms of shifting and
81 scaling slope base curves [Cadigan and Dowden, 2010]. Alternatives to fixed polynomi-
82 als include orthogonal polynomials, GAMs or Smooth-Curve Mixed Models [Fryer et al.,
83 2003, Miller, 2013]. A typical problem of these data is the large number of zero catches;
84 therefore Thorson and Ward [2014] considered delta-GLMM's, where the probability of
85 zero catch is explicitly modeled. Kotwicky et al. [2017] compared three models, two of
86 which included polynomials to account for the dependence on length, and one which used
87 GAM's to this effect, and advocated cross-validation techniques to select the best fitting
88 model for a given data set.

89 When the original assumption is that the catch in each size class and in each haul
90 is Poisson distributed conditional on the abundance, a common approach is to condition
91 on the total catch in each size class. Then, the catch in the individual haul is binomially
92 distributed [Millar, 1992]. Conceptually, a related approach is the beta regression, in
93 which a ratio of Catches Per Unit Effort in each size class is assumed to be beta distributed
94 [Kotwicky et al., 2017].

95 A common phenomenon for size structures in catches is that not only are the num-
96 bers in each length group overdispersed, there is also strong tendency for positive cor-
97 relations between nearby size classes in the same haul [Pennington and Vølstad, 1994,
98 Kristensen et al., 2014]. If not taken into account, this phenomenon means that fluctua-
99 tions across size classes in raw selectivity ratios will be over-interpreted. Pragmatically,
100 the consequence of this is that estimated selectivity ratio curves should be smoothed, but

101 preferably, the size correlations should be included in the statistical model structure.
102 This ensures that the model describes the fluctuations in data adequately which is a
103 prerequisite for the statistical analysis to be valid.

104 Overdispersion and correlation in count data are, in general, conveniently modeled
105 using compound Poisson distributions. These are hierarchical models, where it is as-
106 sumed that the random data is generated through a two-stage procedure: In the first
107 stage, a random *intensity* is generated for each data point. In the second stage, this
108 intensity is used as the mean value for Poisson variables which constitute the count data.
109 With this construction, the variance of the random intensity yields overdispersion rela-
110 tive to Poisson data, while the correlation structure of the intensity cascades to the count
111 data. A recent example of such a model structure is Miller et al. [2018]. A particular
112 framework of interest is that of log-Gaussian Cox processes [Diggle et al., 2013], where
113 the log-intensity is a Gaussian process. Since a Gaussian process is fully described by
114 its mean and covariance, this framework is highly operational and lends itself readily to
115 computations. Log-Gaussian Cox processes have previously been applied to the spatio-
116 temporal modeling of size structured populations, where it has elucidated distributions
117 of cod (*Gadus morhua*) in the North Sea [Lewy and Kristensen, 2009, Kristensen et al.,
118 2014], of whiting (*Merlangius merlangus*) in the Baltic [Nielsen et al., 2014], of the larvae
119 and juveniles of mackerel (*Scomber scombrus*) in the North Sea [Jansen et al., 2012, 2015],
120 and of shallow-water hake (*Merluccius capensis*) [Jansen et al., 2016] and deep-water hake
121 (*M. paradoxus*) [Jansen et al., 2017] in the Benguela current system.

122 Since log-Gaussian Cox processes proved suitable for these applications, it is natural
123 to ask if the framework is also suitable for the problem of estimating selectivity ratios.
124 The paper addresses this question. When applying the framework of log-Gaussian Cox
125 processes to the selectivity ratios, the unobserved size-dependent phenomena include the
126 selectivity ratios, which is the primary object of inference, but also the local abundance
127 present for each pair of operations, as well as aggregations that are specific to the individ-
128 ual operation. Each of these phenomena is characterized by a covariance structure, which
129 describes both the magnitude of fluctuations and their persistence across size ranges. The
130 construction is a fairly simple application of the log-Gaussian Cox framework, and has
131 the appeal that we can specify the properties of the various processes affecting the catch,
132 from which the properties of the log-intensity follow automatically.

133 In this paper we describe the framework and the resulting method. We demonstrate
134 the method using data from a case where the objective was to investigate differences
135 between two vessels which used gear with the same specifications: The RV Dr. Fridtjof
136 Nansen and the FV Blue Sea, which have been used for surveying the stocks of hake
137 in Namibian waters. The objective of the analysis is to estimate the selectivity ratios
138 between the two vessels, including confidence intervals, and to test if the ratios depend on
139 size and the particular hake species. In addition, we perform a simulation experiment to

140 verify the model, test for significance of certain specific model components, and compare
141 the full model with a simplified model where inference is conditional on total catch at
142 length for each station.

143 2 Methods

144 2.1 Statistical model

145 Our method for intercalibration is based on a statistical model for the selectivity ratios
146 which explains the size composition of the catch in survey operations, and in particular
147 differences in this composition between operations conducted differently on the same fish
148 population. For ease of reference, we refer to these operations as 'hauls', whether the
149 gear involved is e.g. trawls, longlines or gill nets. Similarly, we refer to differences be-
150 tween 'gear', even if the actual differences between operations could also involve different
151 vessels, different personel, or different procedures. The model is a non-linear mixed effect
152 model involving both fixed effects parameters and random effects. We conduct inference
153 in the model using numerical maximum likelihood estimation, employing the Laplace
154 approximation [Kristensen et al., 2016] to integrate out random effects.

155 The observed quantities are count data, N_{ijk} , which represents number of individuals
156 caught at station $i = 1, \dots, n_s$, with gear $j = 1, 2$, and in length group $k = 1, \dots, n_l$.
157 Thus, at each station i , two operations have been performed; one with each gear j , and
158 the size distribution of the catch has been measured.

159 We assume that these catches depend on swept area A_{ij} (or a similar measure of
160 effort) and three sets of random variables, which all depend on the size class k : First,
161 Φ_{ik} which for a given station i characterizes the distribution across size of the population
162 encountered by both hauls j . Second, haul-specific fluctuations R_{ijk} in the size compo-
163 sition which we will term the "nugget effect" with a reference to geostatistics [Cressie,
164 1993, Petitgas, 2001] and elaborate on in the following. Third, the relative selectivity S_{jk}
165 which is specific to the gear. Given these random variables Φ , R , S , we assume that the
166 count data is Poisson distributed:

$$N_{ijk} | \Phi, R, S \sim \text{Poisson}(A_{ij} \cdot \exp(S_{jk} + \Phi_{ik} + R_{ijk}))$$

167 The swept area A_{ij} is a known input to the model. This is Cox model of catches, also
168 referred to as a doubly stochastic Poisson model, in that the mean values for the Poisson
169 variates are themselves random. The joint distribution of the processes S , Φ , and R is
170 Gaussian, so that the entire model is a log-Gaussian Cox process [Møller et al., 1998,
171 Diggle et al., 2013]. We now describe the details of the processes S , Φ and R .

172 First, the selectivity (on the log scale) S_{jk} of gear j in size group k is the main object

173 of interest. Since we do not know the actual size distribution of the stock, we cannot
 174 estimate the absolute selectivities S_{1k} and S_{2k} of the two types of gear, but only the
 175 relative selectivity, i.e. $S_{1k} - S_{2k}$. We therefore require

$$S_{1k} = -S_{2k}, \quad (1)$$

176 which allows us to focus on S_{1k} . This symmetric choice ensures that N_{i1k} and N_{i2k}
 177 are identically distributed, which ultimately implies that the estimated selectivities S_{jk}
 178 simply change sign if the gears are relabeled.

179 We note an alternative would be to enforce $S_{1k} = 0$ and estimate S_{2k} . This would be
 180 reasonable when the first gear is a reference gear that we measure the second gear against.
 181 In that case the variance on N_{i1k} would then be smaller than that on N_{i2k} , since N_{i2k}
 182 would contain the extra variance component S_{2k} . This asymmetry would cascade to the
 183 estimates, so that the estimated relative selectivities depend on which gear is considered
 184 the reference gear. In the present study, we have no reason to consider the one gear a
 185 reference, and therefore we prefer the symmetric choice $S_{1k} = -S_{2k}$.

186 To interpret the selectivities S_{jk} , it is useful to momentarily disregard the nugget effect
 187 R . Then, conditional on Φ and S , the expected catches at station i and in size class k
 188 with the two types of gear are $A_{i1} \exp(\Phi_{ik} + S_{1k})$ and $A_{i2} \exp(\Phi_{ik} - S_{1k})$, respectively.
 189 Thus, $\exp(2S_{1k})$ is the ratio between the expected catch per unit effort with the two types
 190 of gear:

$$\exp(2S_{1k}) = \frac{\mathbb{E}\{N_{i1k}/A_{i1}|\Phi, S\}}{\mathbb{E}\{N_{i2k}/A_{i2}|\Phi, S\}}. \quad (2)$$

191 This ratio is termed the selectivity ratio [Kotwicki et al., 2017]. Since this ratio must
 192 be positive, and since we do not assume a particular parametric form, it is convenient to
 193 represent it on the log scale, i.e. in terms of the process S . We model S_{1k} as a random
 194 walk in size k , i.e.

$$S_{1(k+1)} - S_{1k} \sim N(0, \sigma_S^2) \text{ for } k = 1, \dots, n_l - 1$$

195 and assume independence between increments. To ensure that the log-selectivity ratio
 196 S is a well defined stochastic process, we complement this recursion with initial conditions
 197 $S_{j1} \sim N(0, \sigma_1^2)$ where σ_1 is fixed at a “large” value 10, which from a practical point of
 198 view implies that the level of the estimated log-sensitivity ratio S is not dictated by the
 199 prior model but rather by data.

200 Next, Φ_{ik} is a log-density which describes the size distribution of the fish caught at
 201 station i - Specifically, $A_{ij} \exp(\Phi_{ik})$ is the expected number of fish caught in size group
 202 k at station i with a hypothetical gear which averages the two gears $j = 1$ and $j = 2$, in
 203 absence of nuggets ($R = 0$).

204 We assume independence of size distributions at different stations, i.e. Φ_{ik} and $\Phi_{i'k'}$
 205 are independent for $i \neq i'$. At each station i , we assume that the log-density of the size
 206 distribution is a random walk over size groups, i.e.

$$\Phi_{i(k+1)} - \Phi_{ik} \sim N(0, \sigma_{\Phi}^2) \text{ for } k = 1, \dots, n_l - 1 \quad ,$$

207 and that these increments are independent. Thus, the prior on the log-density Φ is a
 208 standard random walk which enforces continuity; the most probable density is flat. We
 209 add initial conditions

$$\Phi_{i1} \sim N(0, \sigma_1^2)$$

210 with the same “large” standard deviation $\sigma_1 = 10$, so that the overall level of Φ is
 211 not dictated by the prior model but rather by the total catch. The parameter σ_{Φ}^2 is
 212 estimated. Since we assume independence between stations, we do not attempt to model
 213 any large-scale spatiotemporal structure of the population. We note that this is the main
 214 difference between this model and the GeoPop model [Kristensen et al., 2014], where
 215 emphasis is exactly on this spatiotemporal structure.

216 Finally, the haul-specific fluctuations R_{ijk} are akin to the nugget effect in spatial statis-
 217 tics; i.e. they describe variability in the catch data on very small spatial and temporal
 218 scales. While the term “nugget” originates in applications to mining, where repeated
 219 measurements on the same location may hit or miss a nugget, the envisioned mechanism
 220 in survey operations is that the gear may hit or miss aggregations of fish such as schools
 221 or shoals, that have limited range in space and quickly form, move, dissolve and regroup.
 222 Since the two hauls at one station have been performed at slightly different locations
 223 and times, they will encounter different aggregations, and therefore R_{ijk} and $R_{i'j'k'}$ are
 224 independent unless $(i, j) = (i', j')$, i.e. the same haul. Thus, at a given station i and in
 225 a given size class k , Φ_{ik} models the population that is common to the two hauls, while
 226 R_{ijk} models independent components which are distinct to each haul. We think of the
 227 aggregations giving rise to the nugget effect R_{ijk} as size-structured, and therefore, for a
 228 given haul (i, j) and as a function of size k , the nugget effect arises as the sum of a white
 229 noise process and a zero-mean first order autoregressive process. Specifically

$$R_{ijk} = R_{ijk}^{WN} + R_{ijk}^{AR}$$

230 where $R_{ijk}^{WN} \sim N(0, \sigma_{WN}^2)$ and are independent. In turn $R_{ijk}^{AR} \sim N(0, \sigma_{AR}^2)$ and are
 231 independent for different stations i or gear j , but correlated between size classes at a
 232 given station i and gear j so that $\mathbb{E}(R_{ijk}^{AR} R_{i'jk'}^{AR}) = \sigma_{AR}^2 \rho^{|k-k'|}$. The white noise component
 233 allows overdispersion relative to Poisson without correlation, while the autoregressive
 234 component models the size-specific clustering: If a particular size group is more abundant

235 in the haul than expected, we would expect the same to apply to nearby size groups but
236 not necessarily to very different size groups. We note that this same model structure was
237 used by Cadigan et al. [2006] with the same motivation, but also that the effect could
238 equally well represent other differences between the individuals hauls, e.g. differences in
239 the way the gear is deployed, or combinations of such differences.

240 The model has five fixed effects parameters which are estimated, viz. the variance
241 parameters σ_S^2 , σ_Φ^2 , σ_{WN}^2 , σ_{AR}^2 , and the correlation ρ . In addition there are a large number
242 of random effects: Φ has $n_s n_l$ variables, S has n_l , and R has $n_s 2n_l$.

243 2.2 Implementation

244 The statistical model in section 2.1 defines the joint distribution of the count data, N ,
245 and the unobserved random variables Φ , R , S , for given parameters σ_S , σ_Φ , σ_{WN} , σ_{AR}
246 and ρ . The unobserved Φ , R and S are integrated out using the Laplace approximation,
247 to yield the likelihood as a function of the five parameters. The likelihood function is
248 maximized to yield estimates of the five parameters, after which the posterior modes of
249 the random effects Φ , R , and in particular S are reported.

250 The computations are performed in R version 3.1.2; we use the Template Model Builder
251 (TMB) package [Kristensen et al., 2016] for evaluating the likelihood function and its
252 derivatives, and in particular for integrating out unobserved random variables using the
253 Laplace approximation. Typical run-times for the models considered in this paper, where
254 there are 77,680 random effects, are 25 seconds on a standard laptop computer. The code
255 is available at GitHub in package `github.com/Uffe-H-Thygesen/Intercalibration`.

256 The code and the statistical model is verified by simulation. Briefly, we simulate 1,000
257 realizations of random effects and data sets, adjusting the mean of the size distributions
258 Φ so that the total catch in the simulated data sets are approximately 17,000 fish, which
259 corresponds to the total catch in the case described in the following. For each realization,
260 we re-estimate the parameters in the model and the log-selectivity ratios. The variance
261 parameters σ_S^2 , σ_Φ^2 , σ_{WN}^2 , and σ_{AR}^2 are estimated on the log scale. We construct 1σ confi-
262 dence intervals for each of the five parameters using the estimated standard deviation as
263 computed from the Hessian of the log-likelihood. Theoretically, these confidence intervals
264 should contain the true parameters for 68% of the simulated data sets; we find that they
265 do so for between 66 % and 71 % of the simulated data sets, except for the parameter
266 $\log \sigma_\Phi^2$, where the coverage is only 48 %. For this parameter, the low coverage is explained
267 by a bias in the estimates: The mean estimate is 0.07 smaller than the true value, which
268 should be compared with an estimated standard deviation which is also 0.07. While neg-
269 ative bias is not uncommon for maximum likelihood estimates of variance parameters, it
270 could possibly be reduced with restricted maximum likelihood (REML) [Pawitan, 2001].
271 We also constructed 2- σ confidence limits, which should contain the true value in 95 %

272 of the runs, and find that they do so for between 86 % and 96 % of the simulated data
 273 sets. The relative uncertainties on the variance parameters σ_S^2 and σ_{AR}^2 (measured from
 274 the standard deviation on estimates) are 13 % and 7 %, respectively, with a bias which
 275 is an order of magnitude smaller. The relative uncertainty on ρ is 2% with a bias of 0.2
 276 %. In roughly half the simulations, the model cannot identify the white noise component
 277 in the residuals and consequently estimates σ_{WN}^2 to be very low ($\sigma_{WN}^2/\sigma_{AR}^2 < 10^{-5}$);
 278 in these cases, also the estimated variance on $\log \sigma_{WN}^2$ is very large (i.e. > 10) so that
 279 the confidence intervals still cover the true value. While the white noise component is
 280 effectively removed from the model through the estimation for these simulated data sets,
 281 the reduced model is estimated well. We note that such problems of estimating sepa-
 282 rate variance components in hierarchical models are not uncommon [Auger-Méthé et al.,
 283 2016]. With this caveat, the simulation experiments verifies the code and the model.

284 2.3 Data

285 We apply the method to a case study involving two vessels, the Norwegian fisheries
 286 research vessel Dr Fridtjof Nansen and the commercial trawler F/V Blue Sea, conducting
 287 hake surveys in Namibian waters.

288 Following independence of Namibia in 1990, abundance of Namibias hake stocks was
 289 monitored by trawl surveys conducted by the R/V Dr Fridtjof Nansen. From 2000 the
 290 Ministry of Fisheries and Marine Resources in Namibia (MFMR) conducted the surveys
 291 using the F/V Blue Sea. In 1998 and 1999, before the shift, extensive experiments were
 292 performed by completing the entire annual survey in parallel with both vessels. The two
 293 vessels used Gisund fishing gear and rigging following the same specifications; neverthe-
 294 less, some difference in the performance of the gear must be anticipated [Weinberg and
 295 Kotwicki, 2008]. The stations are mapped in Figure 2.

296 Catch data collected from these surveys were extracted from the NAN-SIS database
 297 in November 2014 [Strømme, 1992]. The analysis was based on 341 of the 365 pairs of
 298 trawl hauls. 24 pairs were excluded because the trawl durations were less than 15 minutes
 299 and/or the difference in trawl durations exceeded 10 minutes.

300 Catch in numbers per length group and the hauling distance were available for each
 301 haul. Figure 3 shows all catches, summed over all stations, for the two species *M. Para-*
 302 *doxus* (deep-water hake) and *M. Capensis* (shallow-water hake). Since the two species
 303 have different preferred habitats but are morphologically very similar [Jansen et al., 2016,
 304 2017], a question of particular relevance is if the two species have the same selectivity.

3 Results

Figure 4 shows the selectivity ratio from (2), i.e. $\exp(2S_{1k})$, between the RV Dr. Fridtjof Nansen and the FV Blue Sea. Index 1 corresponding to FV Blue Sea, so that a ratio above 1 indicates that the FV Blue Sea has higher expected catch than the RV Dr. Fridtjof Nansen. Estimated parameters, including standard errors derived from the Hessian of the log-likelihood function, are shown in Table 1. Since the gears used on the two vessels have the same specifications, a reasonable hypothesis is that there is no size structure in these calibration factors. This hypothesis could be accepted for *M. Capensis* (a likelihood ratio test of the hypothesis $\sigma_S = 0$ has critical significance level $p \sim 0.08$) but is rejected strongly for *M. Paradoxus* ($p < 10^{-9}$). These p -values have been computed with the standard asymptotic χ^2 -distribution of the log-likelihood ratio, which does not strictly apply since the null hypothesis $\sigma_S = 0$ is on the boundary of the parameter space, so that the correct p -values may be somewhat smaller. It holds for both species that the FV Blue Sea is more efficient at catching larger hakes than the RV Dr. Fridtjof Nansen. The size dependency is more pronounced for *M. Paradoxus*, where the FV Blue Sea is less efficient in the small size classes. The selection of small *M. Capensis* is similar for the two vessels. The estimated relative selectivity appears to fluctuate more between neighboring size classes for *M. paradoxus* than for *M. capensis*. This may be because the smaller catches of *M. capensis* imply less statistical certainty, so that the smooth prior is more visible in the estimates. It could also be connected to the observation that the estimated correlation ρ is closer to 1 for *M. paradoxus* than for *M. capensis* so that small scale fluctuations in the data is attributed to the nugget effect for *M. capensis* but, to a larger degree, to fluctuations in the relative selectivity for *M. paradoxus*.

Since there is no clear prior explanation why the selectivity curves for the two species would differ, a reasonable hypothesis is that they are identical. This hypothesis appears to be strengthened by the qualitative similarity between the estimated curves in Figure 4. This suggests to estimate a combined selectivity ratios for the two species, see Figure 5. In this combined model, we assume that the size distribution and the nugget effect applies to the two species separately, i.e. the small-scale clustering of fish is species-specific. Since each fit yields a likelihood, it is possible to select between the two models (i.e., the two species have the same relative selectivity curve, or two different curves) using an information criterion such as that of Akaike, the AIC. The log-likelihood of the combined model is 258 less than that of the original model; this decrease results from the reduction of the number of parameters (fixed effects) from 10 to 5. Thus, the AIC will prefer strongly the model where the two species have separate selectivity ratios; for a likelihood ratio test, the critical p -value would be 10^{-108} . We note that since the primary objective of inference is on the relative selectivity curves, which are random effects in the model, one could argue that model selection should be performed with the *conditional*

Species	$\log \sigma_\Phi$	ρ	$\log \sigma_{WN}$	$\log \sigma_{AR}$	$\log \sigma_S$	$-\log L$	DF
<i>M. Capensis</i>	-0.15 ± 0.02	0.95 ± 0.01	-0.41 ± 0.02	-0.05 ± 0.04	-4.17 ± 0.50	44940	5
<i>M. Paradoxus</i>	-0.25 ± 0.02	0.98 ± 0.01	-0.95 ± 0.03	0.06 ± 0.05	-3.29 ± 0.24	34607	5
Sum						79547	10
Combined	-0.19 ± 0.01	0.96 ± 0.01	-0.61 ± 0.01	0.01 ± 0.03	-3.68 ± 0.24	79805	5
Combined w/o ρ	-0.18 ± 0.01		-0.10 ± 0.01		-3.87 ± 0.27	82417	3

Table 1: Parameter estimate for the two species separately and combined, with estimated standard deviations. Included is also the negative log-likelihood and the number of parameters (fixed effects) of the model.

343 AIC [Vaida and Blanchard, 2005]. While the computation of the conditional AIC is a
344 non-trivial task in our settings, a bound can be obtained by including the random effects
345 in the degrees of freedom; this holds because each random effect in the cAIC framework
346 is associated with a non-integer degree of freedom between 0 and 1. Then, the difference
347 in log-likelihood should be compared with a maximum difference of 76 in the degrees of
348 freedom, which would still favour strongly separate selectivity ratios for the two species.
349 We conclude that the differences between the two species are statistically significant, even
350 if the relative selectivity curves for the two species show similar qualitative features.

351 To illustrate the importance of the correlation between the different size classes, we
352 fit a new model to this combined data set, in which the autoregressive component of
353 the nugget effect has been removed, so that the nugget effect acts independently at each
354 size class (Figure 5, right panel). Removing this component from the model results in
355 a decrease in the maximum log-likelihood of 2612 while decreasing the numbers of pa-
356 rameters by 2; thus this autoregressive component is extremely significant ($p \approx 10^{-1134}$).
357 Nevertheless, the estimates from this reduced model agree qualitatively with the those
358 from the model that includes autocorrelation in the nugget effect (compare Figure 5, left
359 panel), although some minor differences are noticeable. Moreover, omitting the autocor-
360 relation decreases the estimated variance associated with the selectivity ratio curves, so
361 that the simpler model indicates higher accuracy than warranted.

362 Since several previous studies including [Millar, 1992, Lewy et al., 2004, Cadigan and
363 Dowden, 2010] have considered a conditional approach, where inference is conditional on
364 the total catch at length at each station, appendix A compares such a conditional model
365 with the model as described in section 2.1. The two models give qualitatively similar
366 results, but the estimated selectivity ratios from the unconditional model are generally
367 closer to 1. The unconditional model has slightly narrower confidence intervals and is
368 slightly more demanding in terms of computing time.

369 4 Discussion

370 We developed a statistical method for intercalibrating survey gear and vessels, based
371 on estimating the selectivity ratios from paired hauls. The method is directly available
372 through an R package on `GitHub`. The envisioned application of our method is to adjust
373 data obtained from multiple surveys, thus allowing them to be combined to yield a longer
374 time series which may enter into a stock assessment. The adjustment would take place by
375 multiplying the one series with the estimated selectivity ratios. The uncertainties on the
376 estimated selectivity ratios would then propagate to the adjusted time series, for example
377 using the delta method as implemented in TMB [Kristensen et al., 2016]. While one could
378 envision integrated stock assessment models that use multiple raw survey indices as well
379 as data from paired fishing operations, the preliminary step of adjusting and combining

380 surveys appears to be preferable at least in the foreseeable future.

381 Our model is based on log-Gaussian Cox processes, which have been used earlier in
382 the context of fisheries surveys to map spatiotemporal dynamics of stocks [Kristensen
383 et al., 2014, Jansen et al., 2016], but not in the present way for comparing selectivities.
384 The framework uses a non-parametric model for the relative selectivity and allows for
385 overdispersion relative to the Poisson distribution, as well as correlations between size
386 groups in paired trawl catches. These features all contribute to larger variability in data,
387 and the Gaussian structure of the components simplifies analysis and computations. If the
388 statistical analysis is based on models which fail to include such variance contributions,
389 there is a risk that the confidence in the results are inflated, e.g. in the sense that
390 confidence intervals appear narrower than justified. Such phenomena of overconfidence
391 are well known, both in general statistics and in the specific context of selectivity studies
392 [Fryer, 1991]. They can be seen as a manifestation of the general bias-variance trade-off.
393 Previous methods to address between-haul and within-haul variation include bootstrap
394 [Millar, 1993, Sistiaga et al., 2016] in addition to mixed effects models [Cadigan et al.,
395 2006]. In the present study, an example of such overconfidence is seen in Figure 5,
396 comparing the two panels, where the right panel is based on a simplified model in which
397 the autoregressive component of the nugget effect has been removed. Recalling that a
398 hypothesis test rejected this simplification, and noticing that the reduced model produces
399 estimated confidence intervals which are considerably narrower, we can conclude that
400 these confidence intervals give an overoptimistic view on the accuracy of estimates. This
401 overoptimism can be attributed to the omission of an important variance component.

402 As another example of possible overconfidence, selectivity ratios can be modeled as
403 constants which apply to all size classes, as size-dependent functions using parametric
404 forms, or non-parametrically as we have done here. While specific parametric families
405 of functions are convenient in the analysis, it is difficult to hypothesize a reasonable
406 functional form prior to seeing the data. If a specific functional form is postulated, then
407 it is likely that parameters in this form can be estimated with seemingly high accuracy.
408 However, the sensitivity of the results to mis-specification of the functional form needs to
409 be taken into consideration which is not straightforward. As a result, we would be prone
410 to overestimate our confidence in estimated selectivity ratio curves, by the same reasoning
411 as in the previous paragraph. Thus nonparametric curves, such as the ones we provide
412 in this study, involve the smallest number of assumptions and are the most conservative
413 choice in the sense of not risking overinterpretation of data. For some applications it
414 is convenient to report parametric forms. This would be a minor extension, technically,
415 but a subsequent step of model validation needs to ensure that the parametric family
416 is suitable. On the other hand, non-parametric estimates require some regularization to
417 avoid erratic fluctuations in the estimated curves. Here, we have obtained this smoothness
418 by using a random walk prior on the relative selectivity curve, which is a minimal way of

419 enforcing continuity. An alternative is to use smooth basis functions or smoothing splines
420 [Miller, 2013].

421 The core of our approach is to take into consideration the covariance between different
422 size classes, both in the selectivity ratio curves that we aim to estimate, and in the catch
423 data. Neglecting this covariance would require that data is binned into large size bins
424 with sufficiently high catch numbers, so that we can estimate the selectivity in each
425 bin without borrowing information from neighboring bins. If the true selectivity ratios
426 vary with size, this would lead to a classical trade-off between bias and variance of the
427 estimates. Specifying the fluctuations between size classes, as we have done, bypasses
428 this trade-off and will give consistent results regardless of how small size bins are chosen.
429 The crux of this approach is the correct specification of the covariance structure. Here,
430 we have taken a conservative approach in that we model the log-densities Φ and the
431 relative selectivity S as random walks across size, which amounts to enforcing continuous
432 dependency on size. In turn, the nugget effect is an autoregressive process. The effect
433 of this structure is that large catches across size groups in a specific haul is attributed
434 to high selectivity (S) or to high density at the station (Φ), whereas an isolated peak in
435 catch numbers at a given size range in a specific haul is attributed to size-specific shoaling
436 aggregations, i.e. the nugget effect R .

437 In our model, the random walks have unbiased and identically distributed steps. One
438 would expect that the selectivity ratios fluctuate more in those size classes, where the
439 selectivity curve of each gear changes the most, and less for the large size classes where
440 both gears have full selectivity. Similarly, we would expect that the size distributions are
441 skewed towards the smaller size classes. Thus, our model structure relies on simplifying
442 assumptions, and we do not expect the model to fully describe all variability in the data.
443 Nevertheless, our simulation study indicates that the model structure allows estimation
444 of the selectivity ratios which is the objective of the model.

445 Inspecting the appearance of the nugget effect in the model, we see that it could
446 equally well be interpreted as a factor that modifies the selectivity of the gear in the
447 operation, although we interpret it as a factor affecting the local abundance. Such ran-
448 dom fluctuations in selectivity have been considered previously [Fryer, 1991, Miller, 2013].
449 Based on the information in data sets such as the present, the two effects are confounded
450 [Cadigan and Dowden, 2010]: It is not possible to tell if a high catch in one particular op-
451 eration was because the gear encountered an aggregation, or because the gear functioned
452 better than average in that operation. In both cases, the net effect is a larger variability
453 between repeated hauls.

454 A key question that the model aims to answer is if the gear (or vessel) effect can
455 be assumed to be identical for all size classes, and it is interesting to notice that this
456 does not appear to be the case for *M. Paradoxus*. Similarly, it is interesting that the
457 two species appear to have different selectivity ratios. Although there is no single clear

458 biological explanation for this, there will always be several minor differences in the nets,
459 the rigging, and the way the hauls are performed, which can contribute to such differences
460 [Weinberg and Kotwicky, 2008], keeping in mind the numerous processes that interact
461 and influence the catchability. At the same time caution must be exercised: The results
462 indicate that the size structure in the catches would be extremely improbable if the gear
463 effect acted identically on all size classes, or identically to the two species, under the
464 assumptions in the model. The result therefore hinges on the model representing the
465 variability in catches correctly. While informal model checks suggest that this is the
466 case, we have not performed a stringent model validation using e.g. the techniques in
467 [Thygesen et al., 2017], as the computations would be prohibitive. Thus, there is a risk
468 that some overdispersion in the data is not included in the model, and that the apparent
469 differences between size classes and species are artifacts of this overdispersion.

470 While our main motivation for investigating the relative selectivity is scientific sur-
471 veys, another important area of application is the selectivity of commercial gear. Here,
472 trade-offs between efficiency and environmental impact is one concern that motivates
473 comparative studies of the selectivity of different gear [Sistiaga et al., 2015, Vogel et al.,
474 2017].

475 An underlying assumption behind our analysis is that the two operations at a given
476 station do not affect each other. This assumption conflicts somewhat with the require-
477 ment that the two operations are performed close to each other, both in space and time,
478 so that it is plausible that they encounter the same population. In contrast, Lewy et al.
479 [2004] focused on the disturbance effect that a first haul has on the local fished popula-
480 tion, and the implications for the second haul. In the present study, none of the pairs
481 in the available dataset are exceedingly close, so it would be superfluous to include such
482 effects. Nevertheless, when applying the method to other data sets, it would be possible
483 to parametrize such an effect and include it in the model. A logical extension would be
484 to let the variance on the nugget effect increase with the distance between the two oper-
485 ations in space and time; however, it may be difficult to identify such structures reliably.
486 The limiting case of unpaired fishing operations [Sistiaga et al., 2016] is straightforward
487 to analyze with our present framework but we have not investigated the quality of the
488 resulting estimates.

489 Several previous similar studies have used a conditional approach along the lines in
490 appendix A. In the present study, we found that the estimates from the conditional and
491 unconditional model differed somewhat with estimates from the unconditional model gen-
492 erally being closer to 1. The conditional model has fewer random effects, but computing
493 times are becoming less important thanks to the efficiency of Template Model Builder.
494 The unconditional model has the advantage that it is applicable also to data sets with
495 unpaired, or partially paired, hauls, but it is conceivable that the prior model for the size
496 distribution in the population (Φ) is more critical in such situations and would require

497 further scrutiny.

498 **5 Conclusion**

499 We have demonstrated the feasibility of estimating size-specific selectivity ratios from
500 paired fishing operations, using conditional Poisson distributions while overdispersion
501 and the covariance structure is modelled using unobserved random fields. These fields
502 represent stock size composition, small scale size structured clustering, and gear selec-
503 tivity. The Laplace approximation, implemented in TMB, allows us to integrate out the
504 many unobserved random variables so that the model is computationally feasible. The
505 model allows testing of various hypotheses using the likelihood ratio principle, and model
506 selection using for example AIC. The model, of which an R implementation is publically
507 available, yields non-parametric selectivity ratios, including confidence regions, which can
508 be used to integrate survey catches obtained with different vessels or gear configurations.

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A Conditioning on the total catch at length and station

We compare the model as described in section 2.1 with a variant where we condition on the total catch at length and station. Specifically, let $N_{i \cdot k} = N_{i1k} + N_{i2k}$ be the total catch at station i in length group k . Then the conditional distribution of the catch in the first haul, N_{i1k} given this total catch $N_{i \cdot k}$ is binomial:

$$N_{i1k} | \Phi, R, S, N_{i \cdot k} \sim \text{Binom}(N_{i \cdot k}, \frac{A_{i1} \exp(S_{1k} + R_{i1k})}{A_{i1} \exp(S_{1k} + R_{i1k}) + A_{i2} \exp(S_{2k} + R_{i2k})}) \quad (3)$$

In turn, the probabilities of the total catches $N_{i \cdot k}$ are

$$N_{i \cdot k} | \Phi, R, S \sim \text{Poisson}(A_{i1} \exp(\Phi_{ik} + S_{1k} + R_{i1k}) + A_{i2} \exp(\Phi_{ik} + S_{2k} + R_{i2k})) \quad (4)$$

The joint density as developed in section 2.1 could therefore alternatively be written as a product of these binomial probabilities (3), the Poisson probabilities (4), and the prior density of the Gaussian processes Φ, R, S . We may now condition the inference on the total catch $N_{i \cdot k}$ and thus remove the term in the joint density that originates from the total catches $N_{i \cdot k}$, i.e. the terms (4). Since the size distributions Φ do not enter into the conditional probabilities (3), they only appear in the joint density through their prior distribution. Thus, the size distributions Φ vanish after integration, so they can be removed from the model.

Figure 6 shows the result from this modified model. The Figure should be compared with Figure 4, which shows the corresponding results for the original model. Notice that the estimates of the selectivity curves are not completely identical, since the omitted term (4) does depend on the selectivities, but still fairly similar. The estimates from the unconditional model are, in general, closer to 1, and the marginal confidence intervals are somewhat wider when conditioning on the total catches. This is not surprising, since this model excludes the information in the total catches. The conditional model has 20 % less random effects, which allows faster computations, although our code does not fully exploit this.

Capensis at station IC_1998_2325_IC_1998_2325

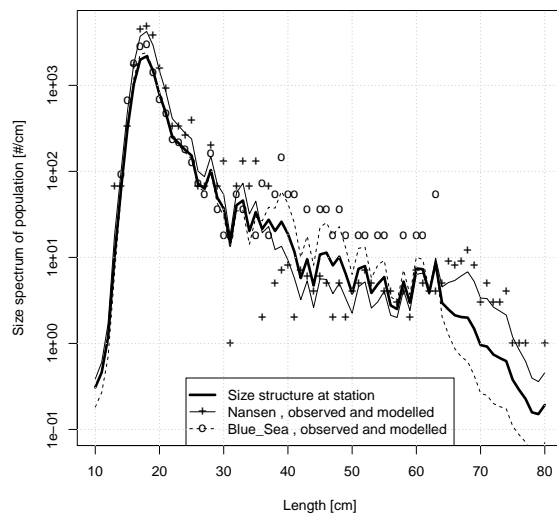


Figure 1: Example of data and model components. Estimated density $\exp(\Phi)$ of the size distribution at one particular station (thick solid lines). Different nugget effects R apply to the two hauls and results in different size structures encountered by the two hauls (thin solid and dashed lines). The relative selectivity S modifies the expected catch in each size group and for each haul (not shown). Observed counts N in each size group and in each haul are shown with “o” and “+”, respectively. Note log scale on the count axis; zero catches are not shown.

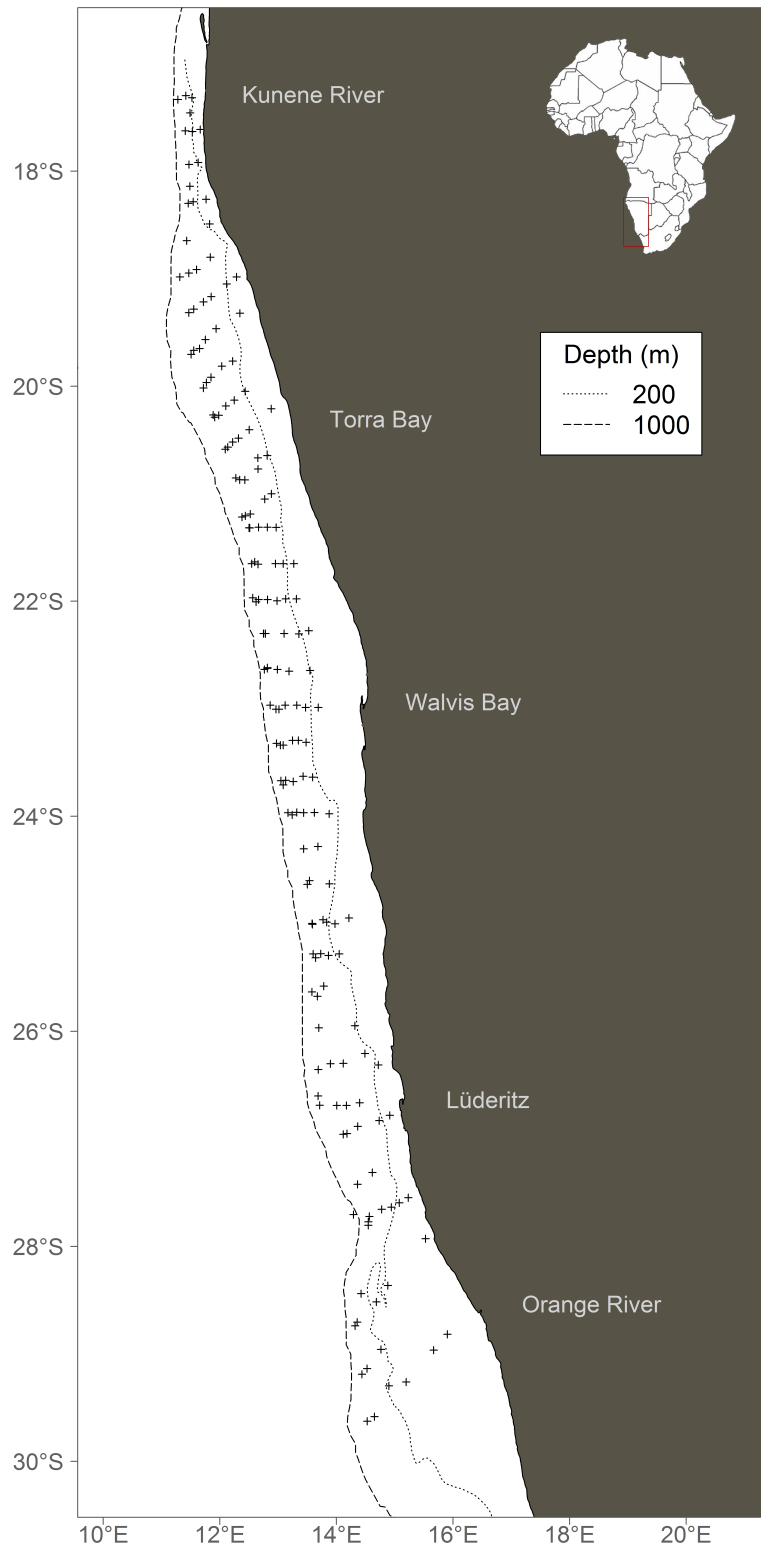


Figure 2: Map of the study area.

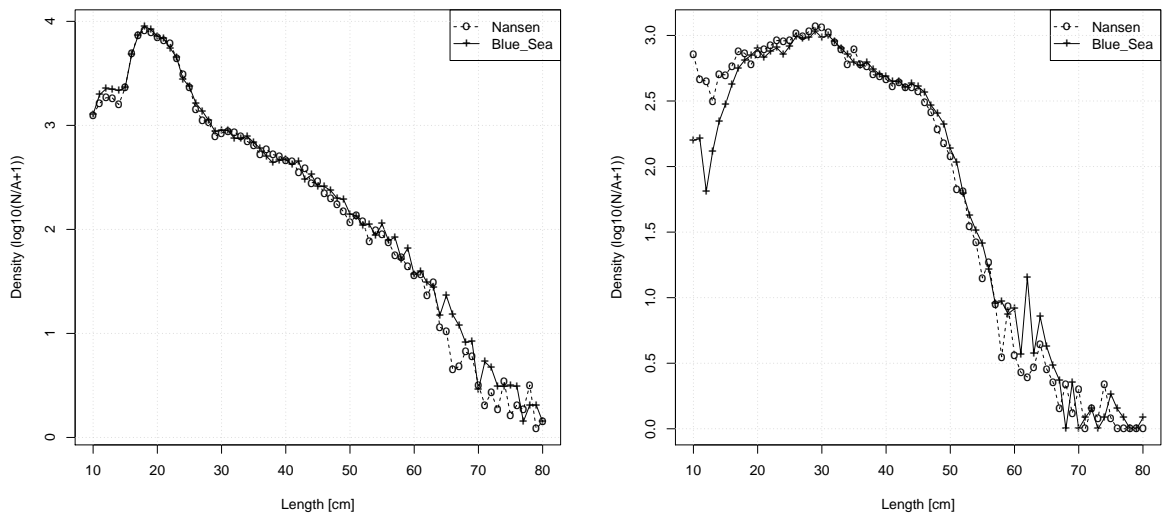


Figure 3: Density (total catch divided by swept area) by size, summed over all hauls. Left panel: *M. Capensis*. Right panel: *M. Paradoxus*.

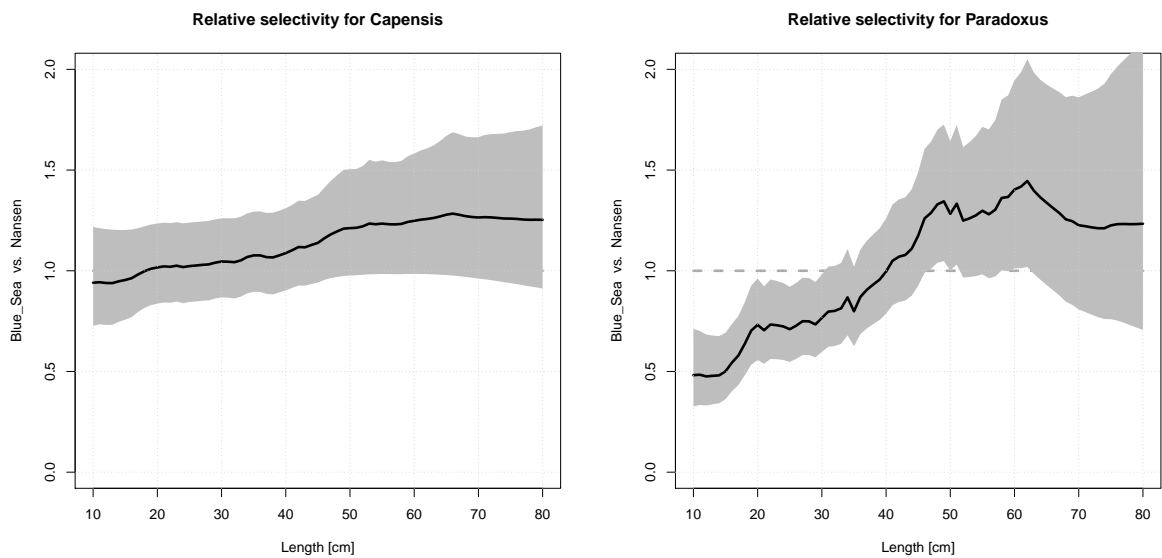


Figure 4: Relative selectivity (vessel calibration factor), comparing catches of *M. Capensis* (left) and *M. Paradoxus* (right) with Gisund gear on RV Dr. Fridtjof Nansen and FV Blue Sea. Large values indicate that the FV Blue Sea has higher selectivity. Solid curve: Estimated relative selectivity (posterior mode). Grey region: Marginal 95 % confidence intervals for the relative selectivity, computed as $1.96\text{-}\sigma$ -intervals on the log scale.

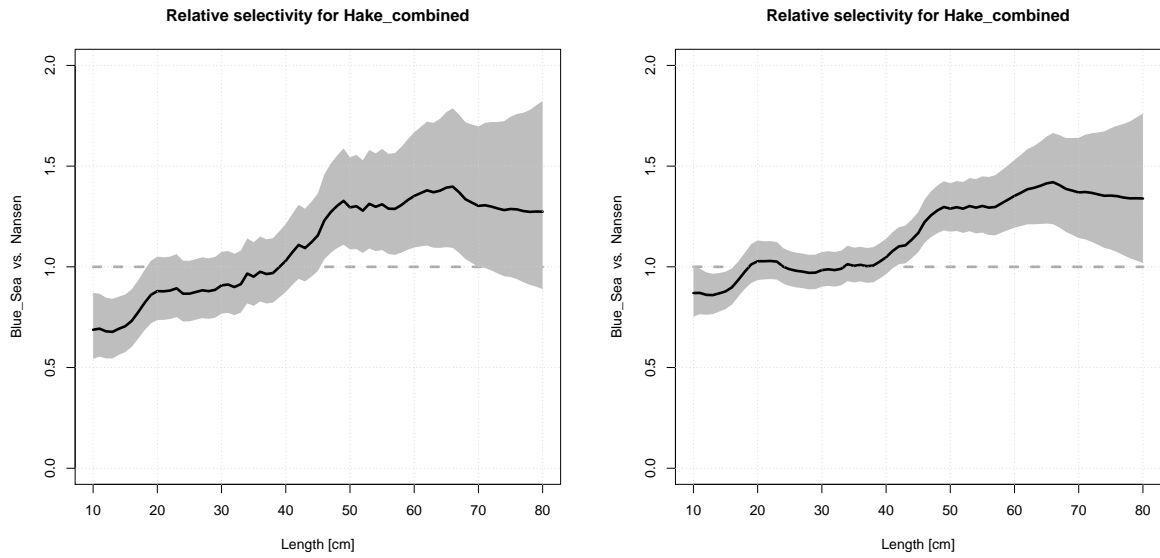


Figure 5: Left panel: Relative selectivity, as in Figure 4, for the two species combined. Right panel: Same, but without the autoregressive component in the nugget effect.

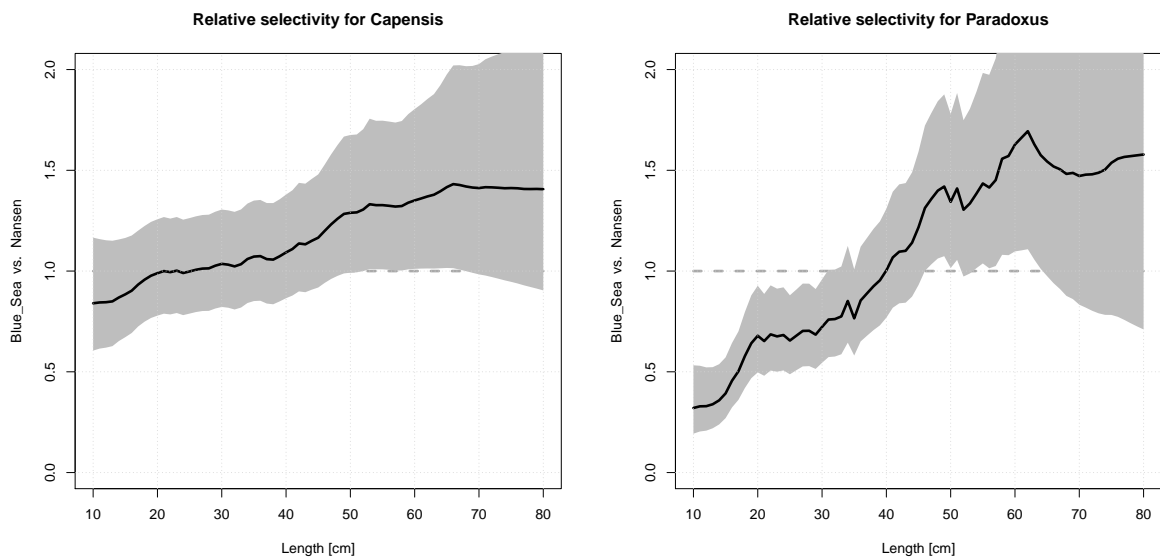


Figure 6: As figure 4, but based on the model where we condition on the total catch in each length group, i.e. without the terms (4) in the likelihood.