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Prediction method for ignition delay time of liquid spray combustion in constant volume chamber

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Abstract

A prediction method, known as the Coupled Time Scale (CTS) method, is proposed in the current work to estimate the ignition delay time (IDT) of liquid spray combustion by only performing an inert spray simulation and a zero-dimensional (0-D) homogeneous reactor (HR) simulation. The method is built upon the assumption that if the majority of the vapor regions in a spray has composition close to the most reactive mixture fraction, which can be obtained by performing 0-D HR calculations, then these regions will have a high probability to undergo high-temperature ignition and ultimately leading to autoignition in spray. The proposed method is applied to estimate high-temperature IDT of *n*-dodecane sprays. Two nozzle diameters (D_{noz}) of $90\mu\text{m}$ and $186\mu\text{m}$ are considered, which correspond to Spray A and Spray D in the Engine Combustion Network [1], respectively. Both D_{noz} are tested at three ambient temperatures (T_{am}) of 800 K, 900 K and 1000 K. The fidelity of the proposed CTS method is verified by comparing the predicted IDT against CFD simulated IDT and measured IDT. Comparison of the estimated IDT from the CTS method to measured IDT yields a maximum relative difference of 24%. Meanwhile, a maximum relative difference of 33% is obtained between the IDT computed from the CTS method and the computed IDT from the large eddy

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simulations of the associated reacting sprays across the different T_{am} , D_{noz} and chemical mechanisms considered in this study.

Keywords: Ignition delay time, Homogeneous reactor, Probability density function, Large eddy simulations, n-dodecane spray

1. Introduction

Ignition delay time (IDT) plays a vital role in a diesel engine as it significantly influences the engine combustion and emission characteristics. Hence, an accurate prediction of the IDT in numerical studies is of the utmost importance. Apart from the mixing process, the type of chemical mechanisms used in numerical studies have significant influence on the prediction of IDT. A detailed chemical mechanism consisting of hundreds of species is expected to provide a better accuracy across a wide range of conditions, but the use of such a large mechanism is computational demanding. This leads to the popularity of reduced mechanisms which retain only the essential chemical species and reactions for specific conditions to achieve a balance between accuracy and computational cost. Nevertheless, any chemical mechanisms must first be validated in zero-dimensional (0-D) homogeneous stagnant adiabatic mixtures, such as shock tubes [2] and rapid compression machines [3], before they are used for applications in three-dimensional (3-D) computational fluid dynamics (CFD). Using the correlation between temperature and mixture fraction predicted from CFD simulations [4, 5], the most reactive mixture fraction (Z_{mr}) and IDT (IDT_{mr}) [6] can be calculated from 0-D homogeneous reactor (HR) simulations of a diesel spray flame. The parameter Z_{mr} , defined as the mixture fraction which has the shortest IDT, is known to play a significant role in the autoignition process [7]. Autoignition in pure gaseous cases have shown to occur where the mixture composition is close to Z_{mr} and having low scalar dissipation [7]. Numerous studies in spray autoignition [8, 9, 10] showed similar observation in the ignition process. There are, however, also numerical studies [11, 12, 13] which disagreed with this observation and showed the ignition to occur in mixtures richer than Z_{mr} . On the other hand, the

26 corresponding IDT_{mr} , which is also computed from 0-D HR simulations, is
27 unable to represent the IDT of spray combustion as turbulence effects of fluid
28 flow and the liquid spray characteristics (*e.g.* breakup and evaporation) are not
29 considered [6] in 0-D HR simulations. This finding is supported by Dahms et
30 al. [14] who carried out one-dimensional flamelet calculations at the standard
31 Spray A condition from Engine Combustion Network (ECN) [1]. It is thus
32 apparent that performing a full reacting spray simulation, which accounts for
33 the turbulent flow field, is essential to obtain the IDT of the spray combustion.
34 However, this process may be costly depending on the size of the chemical
35 mechanism, grid resolutions, and combustion models used.

36 Setting against this background, the present work first examines the mixture
37 fraction of the ignition mixture, then proposes a method to estimate IDT of
38 spray combustion by only computing the inert spray and by performing 0-D
39 HR calculations, without the need to perform a full reacting spray simulation.
40 The method assumes that if the majority of the spray regions has composition
41 close to Z_{mr} , then the regions will have a high probability to undergo high-
42 temperature ignition. The method requires the probability density function
43 (PDF) of the mixture fraction (Z) computed from 3-D simulations of inert
44 sprays, as well as the Z_{mr} and IDT_{mr} obtained from 0-D HR simulations.
45 Since the proposed approach is based on the mixing time scale from inert spray
46 simulations and chemical time scale from 0-D HR simulations, it is henceforth
47 known as the Coupled Time Scale (CTS) method.

48 The paper is structured as follows. The next section describes the experimental
49 data used for model validation as well as the numerical setup. This is followed
50 by the results from inert spray simulations, 0-D HR simulations, and reacting
51 spray simulations in Sections 3.1, 3.2, and 3.3, respectively. The proposed CTS
52 method is subsequently described in Section 3.4. Verification of the estimated
53 IDT against measured and CFD simulated IDT is also shown in this section.
54 Next, a sensitivity study of the proposed CTS method using different mechanisms
55 is carried out and shown in Section 3.5. Conclusions from this work are outlined
56 in the final section.

57 2. Case descriptions & CFD model formulation

58 The simulated spray combustion cases conducted in the present study correspond
59 to the Spray A [1] and Spray D conditions [1, 15] of the ECN. Details of the
60 ambient gas composition, thermodynamic conditions, and injector parameters
61 are shown in Table 1. The nominal nozzle diameter (D_{noz}) for Spray A and
62 Spray D are $90\ \mu\text{m}$ and $186\ \mu\text{m}$, respectively. Both Spray A and Spray D involve
63 injecting liquid *n*-dodecane ($\text{C}_{12}\text{H}_{26}$) through their respective nozzle with an
64 injection pressure of 150 MPa into a constant volume combustion vessel. Three
65 ambient temperatures (T_{am}) of 800 K, 900 K and 1000 K are tested in the present
66 study. In the inert spray case, the molar fraction of O_2 is set to 0%, whereas in
67 the reacting spray case, it is set to 15%. An Eulerian-Lagrangian approach is
68 used within the LES framework for the spray modeling in OpenFOAM-v1712.
69 Both temporal and spatial terms are discretized using second-order schemes.
70 The sub-grid scale (SGS) is modeled using the Dynamic *k*-equation [16]. The
71 injected liquid phase of $\text{C}_{12}\text{H}_{26}$ is modeled as discrete parcels whose motion is
72 described using the Lagrangian particle tracking approach. Spray breakup is
73 modeled by the Reitz-Diwakar spray model [17], where the stripping breakup
74 constant, C_s is set to 10. The skeletal $\text{C}_{12}\text{H}_{26}$ mechanism developed by Yao et
75 al. [18] (54 species and 269 reactions) is used in this work. Detailed description
76 of the mechanism can be found therein [18]. The mechanism has shown good
77 performance in spray combustion context [19, 20]. The partially stirred reactor
78 (PaSR) [21] combustion model coupled with Chemistry Coordinate Mapping
79 (CCM) [22] is used here to account for the turbulence-chemistry interactions.
80 The mixing constant, C_{mix} in the PaSR model is set to 0.3. Details about
81 the CCM approach is available in [22, 23]. The computational domain is a
82 constant volume cubic chamber with side lengths of 108 mm, which corresponds
83 to the volume of the experimental combustion vessel [1]. The ambient mixture
84 composition, pressure, and temperature are initiated as uniform field based
85 on the values shown in Table 1, while the velocity field is set to zero. All
86 boundaries are set as no-slip wall with Neumann boundary condition for the

Table 1: Injector specifications and operating conditions [1, 15].

	Spray A	Spray D
Nozzle diameter, D_{noz} [μm]	90	186
Injected fuel mass flow rate [g/s]	2.295	11.71
Injection pressure [MPa]	150	
Ambient density, ρ_{am} [kg/m^3]	22.8	
Ambient temperature, T_{am} [K]	800, 900, 1000	
Ambient gas composition [mol %]	Inert	Reacting
O ₂	0.00	15.00
N ₂	89.71	75.15
CO ₂	6.52	6.22
H ₂ O	3.77	3.62

87 ambient mixture composition, pressure, and temperature. The injector is placed
 88 at the center of one of the chamber walls. A uniform mesh spacing of 0.125 mm
 89 is used for the spray combustion region (80 mm axially and 15 mm radially from
 90 the nozzle location) with coarser mesh outside the region.

91 **3. Results & Discussion**

92 *3.1. Inert spray*

93 The validation of the computational setup is carried out by comparing
 94 the liquid penetration length (LPL) and vapor penetration length (VPL) with
 95 experimental data [1, 15, 24]. LPL is defined as the maximum axial location
 96 from the injector to the location where 95 % of the total liquid mass is found.
 97 VPL is determined using the farthest downstream location of 0.1 % fuel mass
 98 fraction. It is shown in Figure 1 that the simulated LPL and VPL for Spray A
 99 and Spray D agree well with measurement data. The LPLs are shown to decrease
 100 with increasing T_{am} for both Spray A and Spray D, with the trend being more
 101 apparent in the Spray D cases [24]. On the other hand, the VPLs for Spray A

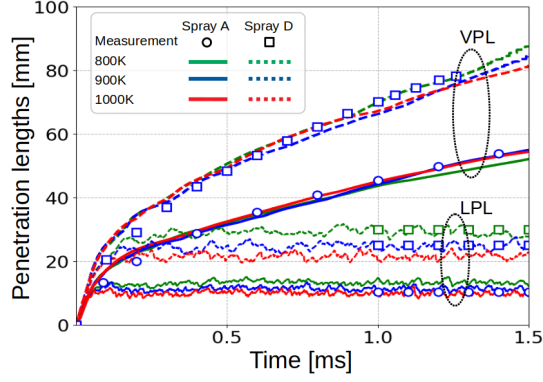


Figure 1: Temporal evolution of liquid penetration lengths (LPL) and vapor penetration lengths (VPL) for Spray A and Spray D at varying T_{am} . Symbols represent measurement data.

102 and Spray D are shown to be insensitive to temperature variation. This also
 103 agrees with the experimental findings [24].

104 From the inert spray simulations, one can extract the temperature (T) in
 105 the flow field as a function of the local mixture fraction (Z) for Spray A and
 106 Spray D at various T_{am} . The upper boundary of the T - Z diagram follows a
 107 quadratic relation,

$$T(T_{\text{am}}, Z) = T_{\text{am}} + b(T_{\text{am}})Z + c(T_{\text{am}})Z^2, \quad 800 \text{ K} \geq T_{\text{am}} \geq 1000 \text{ K} \quad (1)$$

108 where $b(T_{\text{am}}) = -4T_{\text{am}} + 2700$, and $c(T_{\text{am}}) = 6T_{\text{am}} - 4700$ for Spray A; $b(T_{\text{am}}) =$
 109 $-2T_{\text{am}} + 1100$, and $c(T_{\text{am}}) = T_{\text{am}} - 300$ for Spray D. This fitting function is
 110 known as the spray mixing line, which shows the maximum T that can be
 111 achieved at different Z for the inert spray case. The T - Z diagram and the
 112 corresponding spray mixing line for Spray A at $T_{\text{am}} = 900 \text{ K}$ is provided in
 113 Figure 2 for illustration purpose. The most reactive state, Z_{mr} and IDT_{mr} is
 114 obtained by performing 0-D HR simulations along the spray mixing line, which
 115 is shown in the next section.

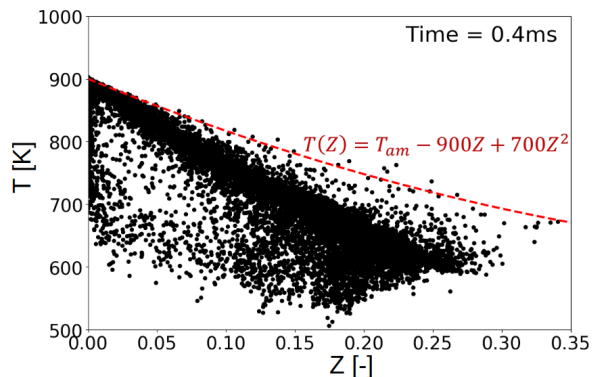


Figure 2: Scatter plots of temperature (T) and mixture fraction (Z) for Spray A at T_{amb} of 900 K. Spray mixing line is represented by the red dashed-line.

116 *3.2. Autoignition of homogeneous mixture*

117 The 0-D HR simulations are carried out using the ANSYS CHEMKIN-PRO
 118 software. The predicted IDT profiles for Spray A and Spray D from the 0-D
 119 HR simulation using the Yao mechanism are shown in Figure 3. The IDT here
 120 is defined as the time when the mixture temperature increases to 400 K above
 121 the initial temperature ($T_{t=0}$). From the figure, one can extract Z_{mr} which is
 122 characterized as the Z with the shortest IDT, also known as IDT_{mr} , for different
 123 T_{amb} . It is depicted in Figure 3 that Z_{mr} increases with increasing T_{amb} for both
 124 Spray A and Spray D.

125 The extracted IDT_{mr} for Spray A and Spray D are shown together with
 126 the measured IDT from reacting spray experiments in Figure 4. It is apparent
 127 from the figure that IDT_{mr} are significantly lower than the measured reacting
 128 spray IDT. Furthermore, the difference in IDT_{mr} between Spray A and Spray D
 129 does not vary with T_{amb} . This observation is inconsistent with the experimental
 130 findings [15, 25] which shows increasing difference in the IDT between Spray A
 131 and Spray D as T_{amb} decreases. This result also indicates that IDT_{mr} itself is
 132 unable to represent the IDT of the reacting spray.

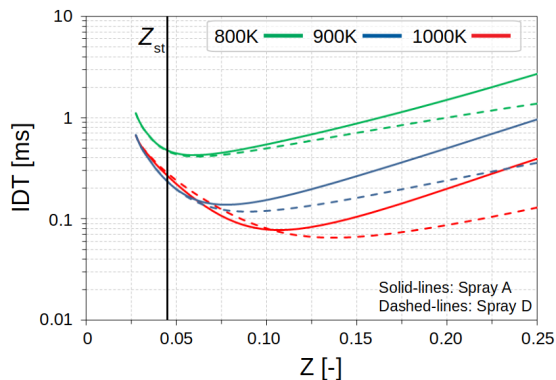


Figure 3: Ignition delay time (IDT) of homogeneous mixtures as a function of mixture fraction (Z) for Spray A and Spray D at different T_{amb} . Solid black line represents stoichiometric mixture fraction, $Z_{\text{st}} = 0.045$.

133 3.3. Reacting spray

134 In this section, 3-D LES of reacting spray cases are performed using the
 135 same setup used in Section 3.1. The reacting spray cases are validated by
 136 comparing the simulated IDTs for Spray A and Spray D at different T_{amb} against
 137 measurement data, which is depicted in Figure 4. The computed IDT from
 138 3-D LES (henceforth known as $\text{IDT}_{\text{HT,CFD}}$) have the same definition as the
 139 measurement data, which is the time from start of injection to the time when
 140 the maximum rate of maximum temperature rise in the domain occurs [13]. This
 141 definition is in accordance with the ECN recommendation [1]. The predicted
 142 $\text{IDT}_{\text{HT,CFD}}$ across different T_{amb} and D_{noz} has a maximum relative difference of
 143 14% compared to measurements.

144 Further analysis of the ignition process in mixture fraction space for Spray A
 145 and Spray D at different T_{amb} is conducted by examining the transition from low-
 146 to high-temperature ignition events, as shown in Figure 5. The low-temperature
 147 ignition first initiates in the fuel-lean region ($Z < Z_{\text{st}}$) (not shown here), where
 148 Z_{st} is the stoichiometric mixture fraction with a value of 0.045. It is followed
 149 by an apparent temperature rise within the fuel-rich region ($Z > Z_{\text{st}}$), as shown
 150 in Figure 5a. Thereafter, the temperature rise “propagates” back towards a

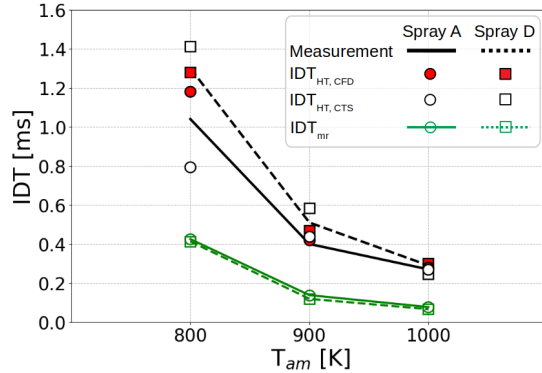


Figure 4: Comparison of most reactive IDT (IDT_{mr}), IDT from CTS method ($IDT_{HT,CTS}$), IDT from CFD simulations ($IDT_{HT,CFD}$), and measurements for Spray A and Spray D at various T_{am} .

151 relatively less-rich mixture where the high-temperature ignition occurs, which
 152 is illustrated in Figure 5c. These observations agree with the findings from the
 153 LES performed by Pei et al. [13]. It is notable in Figure 5b that the transition
 154 from the low- to high-temperature ignition stage is shown to occur near Z_{mr} .
 155 This implies that Z_{mr} plays an important role in the ignition process.

156 3.4. Coupled Time Scale (CTS) method

157 Recently, Borghesi et al. [9] investigated the spontaneous ignition of n -
 158 heptane sprays at high-pressure using 3-D direct numerical simulations. The
 159 study demonstrated that the higher the probability of finding regions with
 160 composition closer to Z_{mr} , the larger the number of ignition spots. This leads
 161 to the proposed CTS method which builds upon similar hypothesis that, if the
 162 majority of the vapor regions in a spray has composition close to the Z_{mr} ,
 163 these regions will undergo high-temperature ignition and ultimately result in
 164 the ignition of the whole spray. Two main assumptions are considered: i)
 165 the mixture composition at Z_{mr} undergoing high-temperature ignition has an
 166 IDT equal to IDT_{mr} , and ii) the whole spray is assumed to undergo high-
 167 temperature ignition when the majority of the vapor regions in the spray has
 168 mixture composition equal to Z_{mr} . It is also worth mentioning that scalar

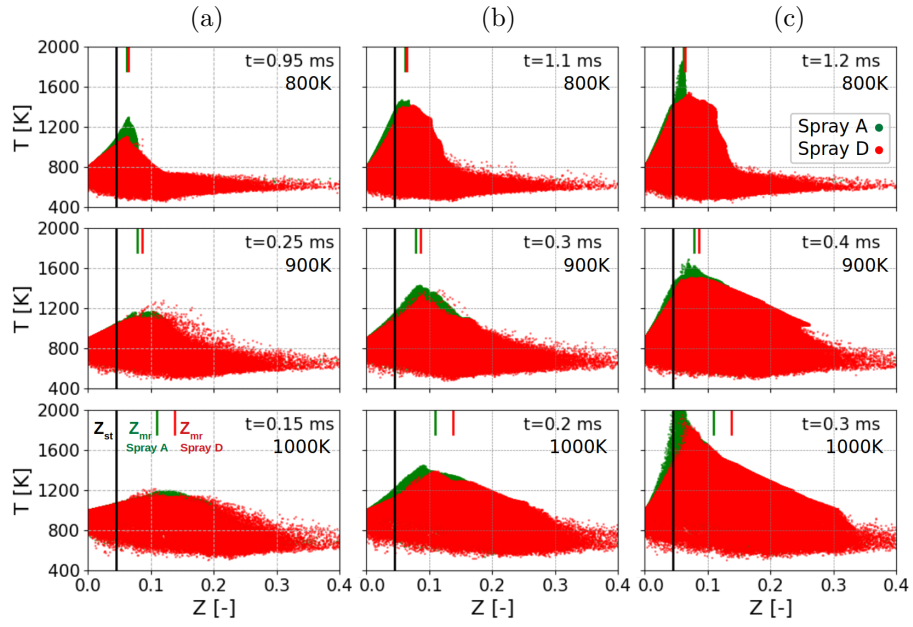


Figure 5: Temporal evolution of the scatter plot of temperature (T) and mixture fraction (Z) for Spray A and Spray D at various T_{amb} conditions. Solid vertical black line represents the stoichiometric mixture fraction (Z_{st}). Green and red solid vertical lines represent most reactive mixture fraction (Z_{mr}) for Spray A and Spray D, respectively. Columns (a), (b), and (c) represent the low-temperature ignition stage, transition stage, and high-temperature ignition stage, respectively.

169 dissipation rate is not considered in the proposed method. In order to examine
 170 the distribution of mixture composition in the spray, a probability density
 171 function (PDF) of Z is computed. It is expected that the spray distribution in
 172 the reacting spray case (before ignition) and in the inert spray case are similar
 173 to one another. Therefore, the PDF of Z is carried out only for the inert spray
 174 cases.

175 3.4.1 Probability density function of Z for inert sprays

176 The PDF of Z is computed from the inert spray cases in Section 3.1 to
 177 examine the distribution of the mass originated from the fuel. The PDF of Z
 178 is defined as

$$p(Z) = \frac{\sum_{i=1}^{N_{\text{cell}}} \rho_i Z_i V_i \alpha_i}{\Delta Z \sum_{i=1}^{N_{\text{cell}}} \rho_i Z_i V_i}, \quad \alpha_i = \begin{cases} 1, & Z_i \in (Z - \Delta Z/2, Z + \Delta Z/2) \\ 0, & \text{otherwise} \end{cases} \quad (2)$$

179 where V_i is the volume of the i -th mesh cell, ρ_i is the density, and N_{cell} is the
 180 total number of cells in the domain. ΔZ is the interval of Z and is set to 0.005.
 181 A moving average is then carried out on the $p(Z)$ to filter out fluctuations.
 182 Figure 6 illustrates the different time instances of $p(Z)$ obtained from the inert
 183 Spray A case at $T_{\text{am}} = 900$ K. The Z value with the highest probability is
 184 denoted as Z_{peak} , which is indicated by the symbols in Figure 6. It is noticeable
 185 from the figure that the Z_{peak} at $t = 0.1$ ms and 0.2 ms are debatable as the PDF
 186 of Z at these two time instances shows a plateau with two peaks. Nevertheless,
 187 it does not change the fact that Z_{peak} is still decreasing over time as the PDF
 188 of Z is shifting towards Z_{st} .

189 The Z_{peak} at each time instance are extracted and subsequently plotted in
 190 Figures 7a and 7b for Spray A and Spray D, respectively, at different T_{am} . It
 191 is shown in Figure 7 that in all three T_{am} cases the Z_{peak} are initially fuel
 192 rich ($Z > 0.1$) and slowly decreasing towards Z_{st} as time progresses. This is
 193 expected as more liquid fuel evaporates and mixes with the ambient air. It is
 194 also notable that the initial Z_{peak} in Spray A is relatively richer than in Spray D
 195 (cf. Figures 7a and 7b). However, the rate at which Z_{peak} approaches Z_{st} is

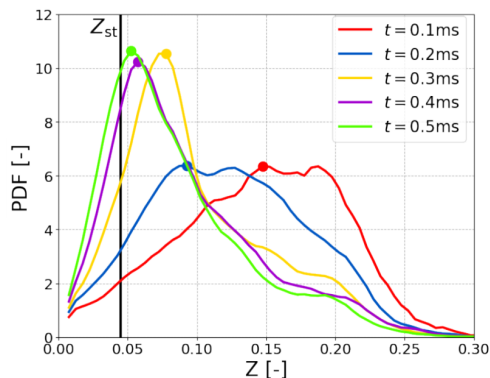


Figure 6: Probability density function (PDF) of mixture fraction (Z) at different time instances for Spray A at $T_{\text{amb}} = 900\text{K}$. Solid black line represents stoichiometric mixture fraction (Z_{st}). Symbols represent mixture fraction at peak PDF (Z_{peak}).

196 much faster in Spray A than in Spray D. This implies that Spray A has a faster
 197 mixing time than in Spray D, which is similarly shown in [25, 26]. As the mixing
 198 time is slower in Spray D, the majority of the spray is more fuel-rich than in
 199 Spray A at the same time instances, as shown in Figure 7.

200 3.4.2 IDT from CTS method

201 The Z_{mr} obtained from the 0-D HR simulation in Section 3.2 at various
 202 T_{amb} are represented by horizontal dashed-lines in Figure 7. The time instance
 203 when Z_{peak} intersects with the horizontal Z_{mr} line is denoted as t_{mr} , which
 204 is represented as symbols in Figure 7. The parameter t_{mr} indicates the time
 205 taken for the majority of the spray to achieve a mixture composition close
 206 to Z_{mr} . It can also be interpreted as the mixing time of the spray to attain
 207 mixture composition which is favorable for high-temperature ignition. Following
 208 the assumption (ii) highlighted in Section 3.4, once t_{mr} is attained the spray
 209 undergoes similar autoignition process as computed in the 0-D HR simulations
 210 with an IDT of IDT_{mr} . Therefore, the high-temperature IDT of spray combustion
 211 can be estimated by adding t_{mr} to its corresponding IDT_{mr} . This estimated
 212 high-temperature IDT from using the CTS method is henceforth known $\text{IDT}_{\text{HT,CTS}}$.

213 The $\text{IDT}_{\text{HT,CTS}}$ for each case is shown in Figure 4 together with the measured

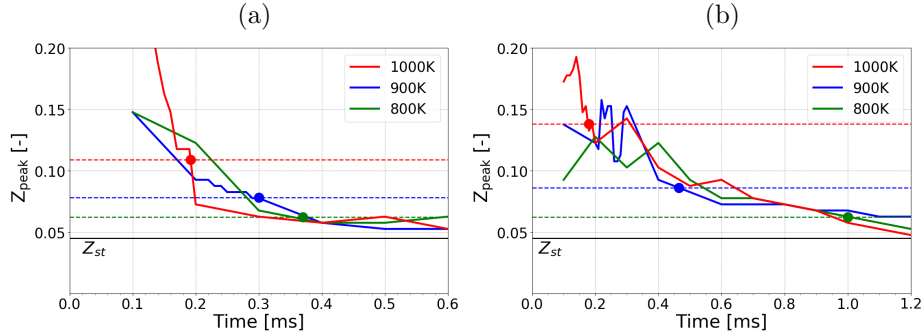


Figure 7: Temporal evolution of mixture fraction at peak PDF (Z_{peak}) for (a) Spray A and (b) Spray D at different T_{amb} . Horizontal dashed-lines represent most reactive mixture fraction (Z_{mr}) at different T_{amb} . Symbols (•) indicate t_{mr} .

214 IDT [1, 15] and CFD simulated $\text{IDT}_{\text{HT,CFD}}$. Comparison of $\text{IDT}_{\text{HT,CTS}}$ with
 215 the measurement data shows good agreement with the relative differences being
 216 less than 24%. Furthermore, comparison of $\text{IDT}_{\text{HT,CTS}}$ with $\text{IDT}_{\text{HT,CFD}}$ also
 217 shows good agreement for both Spray A and Spray D cases across all three T_{amb} .
 218 The relative differences of $\text{IDT}_{\text{HT,CTS}}$ to $\text{IDT}_{\text{HT,CFD}}$ are less than 33% across
 219 different T_{amb} and D_{noz} . Scalar dissipation rate is shown to play a significant
 220 role at low T_{amb} [27]. Its omission from the proposed method is likely the reason
 221 for the larger discrepancy observed at T_{amb} of 800 K (cf. Figure 4).

222 It is shown experimentally in [15, 25] that IDT for Spray D is relatively longer
 223 than Spray A. In addition, the difference between measured IDTs for Spray A
 224 and Spray D increases as T_{amb} decreases. It is previously shown in Section 3.2
 225 that IDT_{mr} fails to capture these experimental trend. In contrast, $\text{IDT}_{\text{HT,CTS}}$
 226 is depicted in Figure 4 to correspond well with the measurement trend observed
 227 across different T_{amb} and D_{noz} . There is, however, a discrepancy at T_{amb} of 1000 K
 228 where $\text{IDT}_{\text{HT,CTS}}$ for Spray D is shorter than Spray A. This can be attributed
 229 to the uncertainty of the CTS method as the relative difference of the measured
 230 IDT between Spray A and Spray D at 1000 K is ~ 0.02 ms. Nevertheless, it is
 231 clear that between IDT_{mr} and $\text{IDT}_{\text{HT,CTS}}$, the latter has a better agreement
 232 with the experimental trend.

233 Another important feature of the proposed CTS method is the ability to

Table 2: Summary of IDTs for Spray A and Spray D at various T_{am} .

	Exp [ms]	IDT _{mr} [ms]	IDT _{HT,CFD} [ms]	IDT _{HT,CTS} [ms]
Spray A, 800 K	1.04	0.43	1.18	0.80
Spray A, 900 K	0.40	0.14	0.42	0.44
Spray A, 1000 K	0.27	0.08	0.28	0.27
Spray D, 800 K	1.30	0.41	1.28	1.41
Spray D, 900 K	0.51	0.12	0.47	0.58
Spray D, 1000 K	0.29	0.07	0.30	0.25

234 quantify the spray mixing time needed to achieve favorable mixture composition
 235 for high-temperature ignition through the parameter t_{mr} . This can be demonstrated
 236 by analyzing the IDTs for the Spray A and Spray D cases at T_{am} of 800 K. It
 237 is previously shown in Figure 3 that the most reactive states (Z_{mr} and IDT_{mr})
 238 at 800 K are similar for both Spray A and Spray D. However, a noticeable
 239 difference in the IDT_{HT,CTS} for Spray A and Spray D at T_{am} of 800 K can be
 240 seen in Figure 4. This result can be attributed to the relatively longer t_{mr}
 241 obtained for Spray D than Spray A at 800 K (cf. Figure 7). This implies that
 242 more time is needed to achieve the optimum composition for ignition in Spray D
 243 than in Spray A due to the former having slower mixing time, which is similarly
 244 postulated in [24, 25]. Overall, the results have demonstrated the feasibility of
 245 the proposed CTS method in estimating the IDT for reacting spray combustion
 246 without the need to perform a full reacting spray combustion simulation, as
 247 well as highlight the advantages of IDT_{HT,CTS} over IDT_{mr}. The IDTs calculated
 248 using the three methods across different conditions are also tabulated in Table 2
 249 to facilitate quantitative comparisons.

250 3.5. Sensitivity of chemical mechanism

251 In this section, the sensitivity of the proposed CTS method to the chemical
 252 mechanisms used is evaluated by testing three other reduced mechanisms: (1)
 253 the 57-species mechanism by Cai et al. [28] (Cai), (2) the 130-species mechanism
 254 by Ranzi et al. [29] (Polimi), and (3) the 257-species mechanism by Narayanaswamy

Table 3: IDTs and relative differences for different chemical mechanisms.

Mechanisms	IDT _{HT,CTS} [ms]	IDT _{HT,CFD} [ms]	Relative difference %
Cai	0.350	0.333	5.1
Polimi	0.438	0.390 [31]	11.4
Stanford	0.570	0.530 [31]	8.6

255 et al. [30] (Stanford). Detailed description of each mechanisms can be referred to
 256 in their original publications. The same methodology as those carried out for the
 257 Yao mechanism in the previous sections is applied to the three aforementioned
 258 mechanisms. It is worth mentioning that the sensitivity study is only carried
 259 out for Spray A at T_{am} of 900 K.

260 The IDTs profiles along the spray mixing line from all three chemical mechanisms
 261 are computed from the 0-D HR simulations and shown in Figures 8. The Z_{mr}
 262 obtained from Figure 8 for each chemical mechanism is plotted in Figure 9.
 263 Their corresponding t_{mr} are then extracted from the intersection points between
 264 Z_{peak} and Z_{mr} . Table 3 shows the calculated IDT_{HT,CTS} for each mechanism.
 265 It is also shown that the relative difference between IDT_{HT,CTS} and IDT_{HT,CFD}
 266 for Cai mechanism is only 5.1%. It is important to note that the IDT_{HT,CFD}
 267 presented in Table 3 for Cai mechanism is obtained by performing a 3-D LES
 268 reacting spray combustion simulation using the numerical setup presented in the
 269 current work. On the other hand, the IDT_{HT,CFD} for the Polimi and Stanford
 270 mechanisms shown in Table 3 are obtained from the LES results performed
 271 independently and separately by Wehrfritz et al. [31] under similar Spray A
 272 conditions at T_{am} of 900 K. Despite obtaining the IDT_{HT,CFD} from a different
 273 numerical setup [31] than the present work, the IDT_{HT,CTS} computed using the
 274 proposed method are still comparable with it. The relative difference for the
 275 Polimi and Stanford mechanisms are within 12%. This further demonstrates
 276 the feasibility of the proposed prediction method in predicting IDT of reacting
 277 spray combustion using different chemical mechanisms.

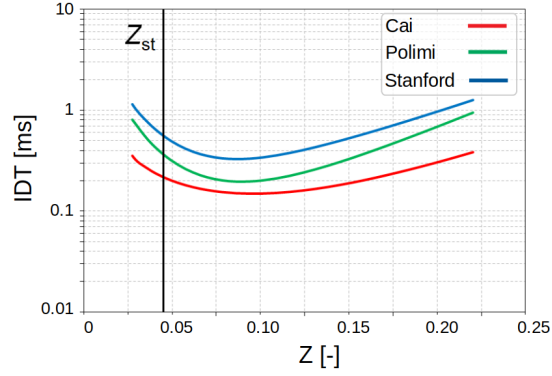


Figure 8: Ignition delay time (IDT) of homogeneous mixtures as a function of mixture fraction (Z) for Spray A at $T_{\text{amb}} = 900$ K from different mechanisms.

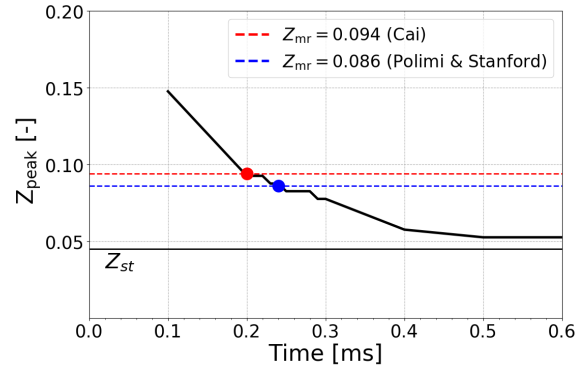


Figure 9: Temporal evolution of mixture fraction at peak PDF (Z_{peak}) for Spray A at $T_{\text{amb}} = 900$ K. Horizontal dashed-lines represent most reactive mixture fraction (Z_{mr}) for different mechanisms. Symbols (\bullet) indicate t_{mr} .

278 4. Conclusion

279 The Coupled Time Scale (CTS) method is proposed to estimate high-temperature
280 ignition delay time (IDT) of liquid spray combustion. The method is applied to
281 *n*-dodecane spray under the ECN Spray A and Spray D conditions at ambient
282 temperature (T_{am}) of 800 K, 900 K, and 1000 K, where their ignitions are shown
283 to initiate at mixtures close to the most reactive mixture fraction (Z_{mr}). The
284 method requires the probability density functions of mixture fraction (Z) computed
285 from 3-D LES inert spray cases, as well as the Z_{mr} and most reactive IDT
286 (IDT_{mr}) obtained from the 0-D homogeneous reactor simulations. The fidelity of
287 the proposed CTS method is verified by comparing the predicted IDT ($\text{IDT}_{\text{HT,CTS}}$)
288 against measured IDT and CFD simulated IDT. The relative difference of $\text{IDT}_{\text{HT,CTS}}$
289 to measured IDT are less than 24 %. Meanwhile, the relative differences between
290 the $\text{IDT}_{\text{HT,CTS}}$ and the computed IDT from CFD calculation are within 33 %
291 across different T_{am} , D_{noz} and chemical mechanisms. It is noteworthy that scalar
292 dissipation rate is not considered in this method, which is likely the cause for
293 the larger discrepancy observed at low T_{am} . Nevertheless, the proposed method
294 is shown to be capable of estimating high-temperature IDT of reacting spray
295 combustion.

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301 References

- 302 [1] Engine combustion network.
303 URL <https://ecn.sandia.gov/>

- 304 [2] H.-P. S. Shen, J. Steinberg, J. Vanderover, M. A. Oehlschlaeger, A shock
305 tube study of the ignition of n-heptane, n-decane, n-dodecane, and n-
306 tetradecane at elevated pressures, *Energy & Fuels* 23 (5) (2009) 2482–2489.
- 307 [3] J. M. Desantes, J. J. López, J. M. García-Oliver, D. López-Pintor,
308 Experimental validation and analysis of seven different chemical kinetic
309 mechanisms for n-dodecane using a rapid compression-expansion machine,
310 *Combustion and Flame* 182 (2017) 76–89.
- 311 [4] Y. Pei, E. R. Hawkes, S. Kook, A comprehensive study of effects of mixing
312 and chemical kinetic models on predictions of n-heptane jet ignitions with
313 the PDF method, *Flow, Turbulence and Combustion* 91 (2) (2013) 249–280.
- 314 [5] K. M. Pang, M. Jangi, X.-S. Bai, J. Schramm, J. H. Walther, P. Glarborg,
315 Effects of ambient pressure on ignition and flame characteristics in diesel
316 spray combustion, *Fuel* 237 (2019) 676–685.
- 317 [6] E. Mastorakos, T. Baritaud, T. Poinsot, Numerical simulations of
318 autoignition in turbulent mixing flows, *Combustion and Flame* 109 (1-2)
319 (1997) 198–223.
- 320 [7] E. Mastorakos, Ignition of turbulent non-premixed flames, *Progress in*
321 *Energy and Combustion Science* 35 (1) (2009) 57–97.
- 322 [8] P. Schroll, A. P. Wandel, R. S. Cant, E. Mastorakos, Direct numerical
323 simulations of autoignition in turbulent two-phase flows, *Proceedings of*
324 *the Combustion Institute* 32 (2) (2009) 2275–2282.
- 325 [9] G. Borghesi, E. Mastorakos, R. S. Cant, Complex chemistry DNS of n-
326 heptane spray autoignition at high pressure and intermediate temperature
327 conditions, *Combustion and Flame* 160 (7) (2013) 1254–1275.
- 328 [10] T. Zhou, M. Zhao, M. Zhu, T. Ye, M. Liu, Three-dimensional direct
329 numerical simulation of n-dodecane spray autoignition with complex
330 chemistry, *Energy & Fuels* 32 (9) (2018) 9838–9849.

- 331 [11] G. Borghesi, A. Krisman, T. Lu, J. H. Chen, Direct numerical simulation of
332 a temporally evolving air/n-dodecane jet at low-temperature diesel-relevant
333 conditions, *Combustion and Flame* 195 (2018) 183–202.
- 334 [12] A. Krisman, E. R. Hawkes, M. Talei, A. Bhagatwala, J. H. Chen, A direct
335 numerical simulation of cool-flame affected autoignition in diesel engine-
336 relevant conditions, *Proceedings of the Combustion Institute* 36 (3) (2017)
337 3567–3575.
- 338 [13] Y. Pei, S. Som, E. Pomraning, P. K. Senecal, S. A. Skeen, J. Manin, L. M.
339 Pickett, Large eddy simulation of a reacting spray flame with multiple
340 realizations under compression ignition engine conditions, *Combustion and*
341 *Flame* 162 (12) (2015) 4442–4455.
- 342 [14] R. N. Dahms, G. A. Paczko, S. A. Skeen, L. M. Pickett, Understanding
343 the ignition mechanism of high-pressure spray flames, *Proceedings of the*
344 *Combustion Institute* 36 (2) (2017) 2615–2623.
- 345 [15] F. Westlye, *Experimental Study of Liquid Fuel Spray Combustion*,
346 Technical University of Denmark (DTU), 2016.
- 347 [16] W.-W. Kim, S. Menon, A new dynamic one-equation subgrid-scale model
348 for large eddy simulations, in: *33rd Aerospace Sciences Meeting and*
349 *Exhibit*, 1995, p. 356.
- 350 [17] R. D. Reitz, R. Diwakar, Structure of high-pressure fuel sprays, *SAE*
351 *Transactions*, 870598 (1987) 492–509.
- 352 [18] T. Yao, Y. Pei, B.-J. Zhong, S. Som, T. Lu, K. H. Luo, A compact skeletal
353 mechanism for n-dodecane with optimized semi-global low-temperature
354 chemistry for diesel engine simulations, *Fuel* 191 (2017) 339–349.
- 355 [19] P. C. Ma, H. Wu, T. Jaravel, L. Bravo, M. Ihme, Large-eddy simulations
356 of transcritical injection and auto-ignition using diffuse-interface method
357 and finite-rate chemistry, *Proceedings of the Combustion Institute* 37 (3)
358 (2019) 3303–3310.

- 359 [20] H. Kahila, A. Wehrfritz, O. Kaario, V. Vuorinen, Large-eddy simulation of
360 dual-fuel ignition: Diesel spray injection into a lean methane-air mixture,
361 *Combustion and Flame* 199 (2019) 131–151.
- 362 [21] J. Chomiak, A. Karlsson, Flame liftoff in diesel sprays, in: *Symposium*
363 (International) on Combustion, Vol. 26, Elsevier, 1996, pp. 2557–2564.
- 364 [22] M. Jangi, R. Yu, X.-S. Bai, Development of chemistry coordinate mapping
365 approach for turbulent partially premixed combustion, *Flow, Turbulence*
366 *and Combustion* 90 (2) (2013) 285–299.
- 367 [23] K. M. Pang, M. Jangi, X.-S. Bai, J. Schramm, J. H. Walther, Modelling
368 of diesel spray flames under engine-like conditions using an accelerated
369 eulerian stochastic field method, *Combustion and Flame* 193 (2018) 363–
370 383.
- 371 [24] J. Gimeno, G. Bracho, P. Martí-Aldaraví, J. E. Peraza, Experimental study
372 of the injection conditions influence over n-dodecane and diesel sprays with
373 two ECN single-hole nozzles. Part I: Inert atmosphere, *Energy Conversion*
374 *and Management* 126 (2016) 1146–1156.
- 375 [25] J. V. Pastor, J. M. Garcia-Oliver, A. Garcia, A. M. López, An experimental
376 investigation on spray mixing and combustion characteristics for Spray C/D
377 nozzles in a constant pressure vessel, SAE Technical Paper, 2018-01-1783.
- 378 [26] J. M. Desantes, J. M. García-Oliver, R. Novella, L. Pachano, A numerical
379 study of the effect of nozzle diameter on diesel combustion ignition and
380 flame stabilization, *International Journal of Engine Research*.
- 381 [27] P. Kundu, M. M. Ameen, S. Som, Importance of turbulence-chemistry
382 interactions at low temperature engine conditions, *Combustion and Flame*
383 183 (2017) 283–298.
- 384 [28] M. Davidovic, T. Falkenstein, M. Bode, L. Cai, S. Kang, J. Hinrichs,
385 H. Pitsch, Les of n-dodecane spray combustion using a multiple

- 386 representative interactive flamelets model, *Oil & Gas Science and*
387 *Technology–Revue d’IFP Energies Nouvelles* 72 (5) (2017) 29.
- 388 [29] E. Ranzi, A. Frassoldati, A. Stagni, M. Pelucchi, A. Cuoci, T. Faravelli,
389 Reduced kinetic schemes of complex reaction systems: fossil and biomass-
390 derived transportation fuels, *International Journal of Chemical Kinetics*
391 46 (9) (2014) 512–542.
- 392 [30] K. Narayanaswamy, P. Pepiot, H. Pitsch, A chemical mechanism for low to
393 high temperature oxidation of n-dodecane as a component of transportation
394 fuel surrogates, *Combustion and Flame* 161 (4) (2014) 866–884.
- 395 [31] A. Wehrfritz, O. Kaario, V. Vuorinen, B. Somers, Large eddy simulation of
396 n-dodecane spray flames using Flamelet Generated Manifolds, *Combustion*
397 *and Flame* 167 (2016) 113–131.