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# Effects of ambient pressure and nozzle diameter on ignition characteristics in diesel spray combustion

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## Abstract

Numerical simulations are performed to investigate the effects of ambient density ( $\rho_{\text{am}}$ ) and nozzle diameter ( $D_{\text{noz}}$ ) on the ignition characteristic of diesel spray combustion under engine-like conditions. A total of nine cases which consist of different  $\rho_{\text{am}}$  of 14.8, 30.0, and 58.5 kg/m<sup>3</sup> and different  $D_{\text{noz}}$  of 100, 180, and 363  $\mu\text{m}$  are considered. The results show that the predicted ignition delay times are in good agreement with measurements. The current results show that the mixture at the spray central region becomes more fuel-rich as  $D_{\text{noz}}$  increases. This leads to a shift in the high-temperature ignition location from the spray tip towards the spray periphery as  $D_{\text{noz}}$  increases at  $\rho_{\text{am}}$  of 14.8 kg/m<sup>3</sup>. At higher  $\rho_{\text{am}}$  of 30.0 and 58.5 kg/m<sup>3</sup>, the ignition locations for all  $D_{\text{noz}}$  cases occur at the spray periphery due to shorter ignition timing and the overly fuel-rich spray central region. The numerical results show that the first ignition location during the high-temperature ignition occurs at the fuel-rich region at  $\rho_{\text{am}} \leq 30.0$  kg/m<sup>3</sup> across different  $D_{\text{noz}}$ . At  $\rho_{\text{am}} = 58.5$  kg/m<sup>3</sup>, the ignition occurs at the fuel-lean region for the 100 and 180  $\mu\text{m}$  cases, but at the fuel-rich region for the 363  $\mu\text{m}$  nozzle case. This distinctive difference in the result at 58.5 kg/m<sup>3</sup> is

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likely due to the relatively longer ignition delay time in the  $363\ \mu\text{m}$  nozzle case. Furthermore, the longer ignition delay time as  $D_{\text{noz}}$  increases can be related to the higher local scalar dissipation rate in the large nozzle case.

*Keywords:* Spray flame, Transported probability density function, Ignition process, Ambient density effect, Nozzle diameter effect

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## 1. Introduction

Automotive and marine industries have worked to improve the understanding of in-cylinder processes in order to design engines that are cleaner and more efficient. Sandia National Laboratory and numerous research groups have shared their optical measurements and numerical modeling results through the Engine Combustion Network (ECN) [1] to facilitate the study of diesel spray combustion and for validation of numerical model. Effects of a wide range of diesel engine parameters on fuel penetration, ignition delay time (IDT), flame lift-off length (LOL), and soot emissions have been studied [2, 3, 4]. Extensive and comprehensive studies have been carried out for Spray A configuration, where the ambient gas density ( $\rho_{\text{am}}$ ) and nozzle diameter size ( $D_{\text{noz}}$ ) are set to  $22.8\ \text{kg/m}^3$  and  $90\ \mu\text{m}$ , respectively. The ambient temperature ( $T_{\text{am}}$ ) is set to  $900\ \text{K}$ , while its corresponding ambient pressure ( $P_{\text{am}}$ ) is  $58\ \text{bar}$ . Significant emphasis has been placed on understanding its ignition and flame stabilization processes [5, 6, 7, 8]. It was only recently that ECN introduced the Spray D configuration [9, 10], which has the same operating conditions as Spray A, but uses a larger nozzle diameter,  $D_{\text{noz}} = 186\ \mu\text{m}$ . Different ignition characteristics were observed in Spray D than that in Spray A at  $900\ \text{K}$ , where ignition was shown to occur at the spray periphery in the former case [10] instead of occurring at the spray head for the latter case. The results suggest that the favorable ignition location shifts to the peripheral of the spray as nozzle diameter increases.

It is important to note that most of the aforementioned studies were performed at ambient density,  $\rho_{\text{am}} = 14.8 - 30.0\ \text{kg/m}^3$ . However, the  $\rho_{\text{am}}$  at the start of injection is approximately  $60.0\ \text{kg/m}^3$  under full load conditions in typical

25 heavy-duty engines and large two-stroke marine engines. Meanwhile, the  $D_{\text{noz}}$   
26 in marine engines are generally larger in order to deliver a greater amount of  
27 fuel. For instance, the fuel injector in the medium-speed four-stroke marine  
28 engines simulated by Kyriakides et al. [11] and Kilpinen [12] had a size of  
29  $370\ \mu\text{m}$  and  $388\ \mu\text{m}$ , respectively. Ishibashi and Tsuru [13] performed multiple  
30 injection experiments under marine engine-like conditions, in which the pilot  
31 diesel injector and main diesel injector had a size of  $160\ \mu\text{m}$  and  $500\ \mu\text{m}$ , respectively.  
32 Schmid et al. [14] conducted experiments using an optical accessible marine  
33 spray combustion chamber with swirling flow, in which the fuel is injected from  
34 a  $875\ \mu\text{m}$  nozzle. Bolla et al. [15] later used the same experimental setup to study  
35 a range of  $D_{\text{noz}}$  from 200 to  $1200\ \mu\text{m}$ . However, it is important to note that the  
36 experiment is only conducted at a constant density of  $33\ \text{kg}/\text{m}^3$ . Experimental  
37 studies of spray combustion conducted in a constant volume chamber under  
38 high  $\rho_{\text{am}}$  (or  $P_{\text{am}}$ ) and large  $D_{\text{noz}}$  were reported by Siebers and co-workers  
39 [3, 16, 17, 18, 19]. The experimental studies were carried out for a range of  $\rho_{\text{am}}$   
40 from  $7.3$  to  $58.5\ \text{kg}/\text{m}^3$ , which corresponds to  $P_{\text{am}}$  of 20 to 170 bar when  $T_{\text{am}}$   
41 is at 1000 K. Both liquid and vapor penetration lengths were found to decrease  
42 with increasing  $\rho_{\text{am}}$ . Meanwhile, spray flame at quasi-steady state were found  
43 to reduce in size (both in length and width) when  $\rho_{\text{am}}$  increases [3, 18]. In terms  
44 of ignition and premixed combustion processes, Higgins et al. [19] investigated  
45 them up to  $45.0\ \text{kg}/\text{m}^3$  but only for  $D_{\text{noz}}$  of  $246\ \mu\text{m}$ . Their work showed that  
46 increasing density decreases the time for ignition to occur. In addition, the  
47 ignition location was shown to move around the central region of the spray  
48 containing liquid-phase fuel and extend upstream along its sides.

49 From a simulation point of view, Cung et al. [20] performed Unsteady  
50 Reynolds Averaged Navier-Stokes (URANS) simulations to study the influence  
51 of nozzle diameter on spray combustion and soot emissions in Spray A conditions.  
52 The SAGE detailed chemistry solver [21], which is a well-mixed reactor based  
53 model was used in the study. The tested nozzle diameters ranged from 30 to  
54  $129\ \mu\text{m}$ . They noticed that the IDT varies non-linearly with nozzle diameter  
55 where the shortest ignition delay occurs for the  $70\ \mu\text{m}$  nozzle case. Nozzles with

56 smaller diameter delayed the ignition due to leaner mixture (less injected fuel  
57 mass and high levels of air entrainment) at ignition sites [20]. As the nozzle  
58 diameter decreased, the equivalence ratio contour line shifted toward leaner  
59 mixtures at the same axis location. Comparison of Spray A and Spray D was  
60 carried out in the numerical study by Desantes et al. [22]. The unsteady flamelet  
61 progress variable (UFPV) model was employed in the study. It was shown that  
62 a reduction in  $D_{\text{noz}}$  promotes faster mixing which shortens the time needed to  
63 reach ignitable equivalence ratio, therefore a shorter IDT was observed in the  
64 Spray A case. In addition, Ong et al. [23] compared the ignition characteristics  
65 between Spray A and Spray D by performing large eddy simulations coupled  
66 with partially-stirred reactor model. Their simulations were able to predict the  
67 annular ignition sites for Spray D at ambient temperatures of 1000 and 900 K,  
68 which is consistent with the experimental observation in [10]. It was suggested  
69 by Ong et al. [23] that the less fuel-rich mixture at the spray periphery is  
70 more favorable for ignition than the relatively more fuel-rich mixture at the  
71 core of the spray in Spray D. Pang et al. [24] performed a URANS study on  
72 reacting sprays in a constant volume combustion vessel with  $D_{\text{noz}}$  of 100, 180,  
73 and  $363 \mu\text{m}$ . Their numerical results showed that as  $D_{\text{noz}}$  becomes larger, the  
74 low-temperature region of the spray tends to get more fuel-rich. Their simulation  
75 was able to capture the spray flame feature across different  $D_{\text{noz}}$ , in particular  
76 the flame penetration length. However, little focus was placed on the ignition  
77 characteristic of different  $D_{\text{noz}}$ .

78 All the numerical works mentioned above for different  $D_{\text{noz}}$  were only performed  
79 at a single  $\rho_{\text{am}}$ . On the other hand, the effects of  $\rho_{\text{am}}$  on ignition and spray flame  
80 were carried out by Pang et al. [25]. Their 3-D numerical study investigated  
81 the ignition behaviors and flame structures at different  $\rho_{\text{am}}$  of 14.8, 30.0, and  
82  $58.5 \text{ kg/m}^3$ . They found that the mixture fraction ( $Z$ ) of the first igniting  
83 location during the high-temperature ignition does not vary monotonically with  
84  $\rho_{\text{am}}$ . The ignition occurred at a fuel-rich mixture region for the 14.8 and  
85  $30.0 \text{ kg/m}^3$  cases, but at a fuel-lean mixture region for the  $58.5 \text{ kg/m}^3$  case.  
86 It is important to note that the work was carried out only for single  $D_{\text{noz}}$  of

87 180  $\mu\text{m}$ . The coupled effects between  $D_{\text{noz}}$  and  $\rho_{\text{am}}$  on ignition characteristics  
88 are still not completely understood. The variation of the ignition mixture during  
89 initial high-temperature ignition with respect to  $\rho_{\text{am}}$  may vary as  $D_{\text{noz}}$  becomes  
90 larger or smaller. This information is critical to the development of skeletal  
91 surrogate fuel mechanisms. Developing a mechanism that fits into a narrower  
92 range of operating conditions would allow the size of the fuel mechanisms to be  
93 further optimized, thus increasing computational efficiency.

94 Set against these backgrounds, the objective of the present CFD work is to  
95 investigate the effects of varying  $D_{\text{noz}}$  and  $\rho_{\text{am}}$  on the ignition process in diesel  
96 spray flame. The velocity, species, and temperature distribution profiles are  
97 computed and compared to elucidate the differences in the ignition process. The  
98 paper is structured such that experimental data used for model validation are  
99 first described in Section 2. Next is the descriptions of the numerical methods in  
100 Section 3. Sections 4 and 5 present the model validation as well as the numerical  
101 analysis of autoignition at different  $\rho_{\text{am}}$  and  $D_{\text{noz}}$ . Conclusions from this work  
102 are highlighted in the final section.

## 103 2. Case descriptions

104 The grade number two Diesel fuel (Diesel #2) spray experimental data  
105 [1, 17, 18] obtained from constant volume spray combustion experiment is  
106 used for model validation in this work. The constant volume chamber has  
107 an ambient gas composition of 21.0%  $\text{O}_2$ , 69.3%  $\text{N}_2$ , 6.1%  $\text{CO}_2$  and 3.6%  $\text{H}_2\text{O}$   
108 (by volume) before the start of spray injection. This experimental ambient gas  
109 composition is used in the current reacting spray cases to ensure identical initial  
110 thermochemical conditions.

111 As depicted in Table 1, reacting spray simulations are carried out for three  
112  $D_{\text{noz}}$  of 100, 180, and 363  $\mu\text{m}$ . Three  $\rho_{\text{am}}$  of 14.8, 30.0, and 58.5  $\text{kg}/\text{m}^3$  are  
113 considered for each  $D_{\text{noz}}$ . At  $T_{\text{am}} = 1000\text{ K}$ , the  $\rho_{\text{am}}$  considered corresponds to  
114  $P_{\text{am}}$  of 42, 85, and 170 bar, respectively. Initial flow and turbulence conditions  
115 can be found in the previous work [26]. The operating conditions and the

Table 1: Operating conditions and injection specifications.

Case	O <sub>2</sub> [% mol]	T <sub>am</sub> [K]	ρ <sub>am</sub> [kg/m <sup>3</sup> ]	D <sub>noz</sub> [μm]	P <sub>inj</sub> [bar]	ṁ <sub>f</sub> [g/s]
1	21	1000	14.8	100	1400	2.7
2	21	1000	30.0	100	1400	2.8
3*	21	1000	58.5	100	1400	2.8
4	21	1000	14.8	180	1400	8.8
5	21	1000	30.0	180	1400	9.0
6	21	1000	58.5	180	1400	9.2
7	21	1000	14.8	363	1400	35.8
8	21	1000	30.0	363	1400	36.3
9*	21	1000	58.5	363	1400	36.3

\*No experimental injected fuel mass flow rate ( $\dot{m}_f$ ) is available for  $\rho_{am} = 58.5 \text{ kg/m}^3$ . The  $\dot{m}_f$  for  $\rho_{am} = 30.0 \text{ kg/m}^3$  case is used instead.

116 injection specifications, such as  $D_{noz}$ , injection pressure ( $P_{inj}$ ), and injected fuel  
 117 mass flow rate ( $\dot{m}_f$ ), for each test cases are listed in Table 1.

### 118 3. CFD model formulation

119 The 3-D CFD spray combustion simulations are carried out using OpenFOAM-  
 120 v1712. The fuel spray, flow and combustion processes are modeled using the  
 121 Eulerian-Lagrangian approach within the URANS framework. Realizable  $k$ -  
 122  $\epsilon$  model [27] is employed for turbulence modeling. The injected liquid phase  
 123 of the fuel is modeled as discrete parcels whose motion is described using  
 124 the Lagrangian particle tracking approach. Each parcel represents a group  
 125 of spherical droplets whose position, size, and physical properties are similar.  
 126 Primary breakup of the injected fuel is considered by injecting computational  
 127 parcels with the Rosin-Rammler distribution of diameter ranging from  $0.1D_{noz}$   
 128 to  $D_{noz}$ . The secondary breakup is modeled by the Reitz-Diwakar spray model

129 [28]. As each nozzle has its own nozzle coefficients (available in [1]), the stripping  
130 breakup constant,  $C_s$ , in the Reitz-Diwakar model for the nozzle cases of 100,  
131 180, and 363  $\mu\text{m}$  are set to 13, 6, and 8, respectively. It is important to note  
132 that for each  $D_{\text{noz}}$  case the same  $C_s$  value is used across the three  $\rho_{\text{am}}$  tested.  
133 The liquid properties of tetradecane ( $\text{C}_{14}\text{H}_{30}$ ) are used to represent Diesel #2  
134 fuel [29]. The Frossling model and the Ranz-Marshall correlation are employed  
135 to account for the droplet evaporation and heat transfer with the surrounding  
136 gas phase respectively.

137 The turbulence-chemistry interaction (TCI) is modeled using an Eulerian-  
138 based transported probability density function (PDF) method, the Eulerian  
139 Stochastic Field (ESF) method [30]. Similar to the Lagrangian particle transported  
140 PDF method, the ESF method is a general approach to account for TCI effect. It  
141 can be used to simulate the autoignition as well as different levels of “premixedness”,  
142 *i.e.*, premixed, partially premixed and non-premixed. Details of the ESF formulation  
143 are available in [30]. The model has been applied successfully to simulate diesel  
144 spray combustion [24, 25, 31, 32]. The number of stochastic fields is set to  
145 32 as the result was shown to have reached convergence [32]. The Chemistry  
146 Coordinate Mapping (CCM) approach is coupled with the ESF solver to speed  
147 up the integration process of the chemical reaction rates [33]. The current work  
148 uses a four-dimensional phase space based on temperature, local equivalence  
149 ratio, scalar dissipation rate, and the mass fraction of fuel, where the resolutions  
150 of CCM are fixed at 5K, 0.01, 0.025, and 0.001, respectively [32, 33].

151 The computational domain is a constant volume cubic chamber with side  
152 lengths of 108 mm, which corresponds to the volume of the experimental combustion  
153 vessel [1]. The ambient mixture composition, pressure, and temperature are  
154 initiated as uniform field while the velocity field is set to zero. All boundaries are  
155 set as no-slip wall with Neumann boundary condition for the ambient mixture  
156 composition, pressure, and temperature. The injector is placed at the center  
157 of one of the chamber walls. The mesh configuration used in [25] is employed  
158 in the present study which involves an isotropic cell size of 0.5 mm within the  
159 spray combustion region. This mesh configuration was shown to reach mesh



160 independence in [25].

## 161 4. Model Validation

### 162 4.1. Inert spray validation

163 Model evaluation is performed on evaporating sprays (Cases 1-9 shown in  
 164 Table 1) at different  $\rho_{\text{am}}$  and  $D_{\text{noz}}$  values by computing the liquid penetration  
 165 length (LPL) and vapor penetration length (VPL). This is first carried out by  
 166 performing inert spray simulations where  $\text{O}_2$  is set to zero. LPL is defined as  
 167 the maximum axial location from the injector to the location where 95 % of the  
 168 total liquid mass is found; VPL is determined using the farthest downstream  
 169 location of 0.1 % fuel mass fraction.

170 Since experimental data are not available, model evaluation of the liquid-  
 171 phase is carried out by comparing against the LPL obtained from the liquid  
 172 scaling law [16]. The liquid properties of *n*-heptadecane are used in the liquid  
 173 scaling law to produce Diesel #2 liquid length [16] since these resemble the  
 174 properties of Diesel #2. Figure 1 shows the computed LPL and VPL for different  
 175  $D_{\text{noz}}$  at different  $\rho_{\text{am}}$  of 14.8, 30.0, and 58.5 kg/m<sup>3</sup>. In the figure, the computed  
 176 LPL are shown to be comparable to the LPL obtained from the liquid scaling  
 law across different  $\rho_{\text{am}}$ .

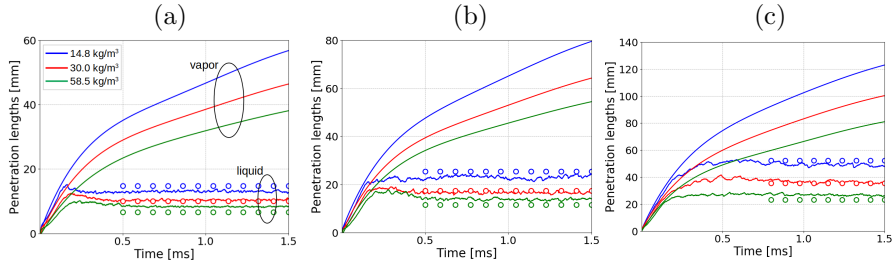


Figure 1: Liquid and vapor penetration lengths of the non-reacting sprays as a function of time after start of injection (ASI) for different  $D_{\text{noz}}$  of (a) 100, (b) 180, and (c) 363  $\mu\text{m}$ . Solid lines denote the simulations results. Circle markers denote the liquid scaling law results [16].

177

178 On the other hand, the associated VPLs shown in Figure 1 are evaluated  
 179 using the dimensionless penetration length,  $\sigma$  and dimensionless penetration

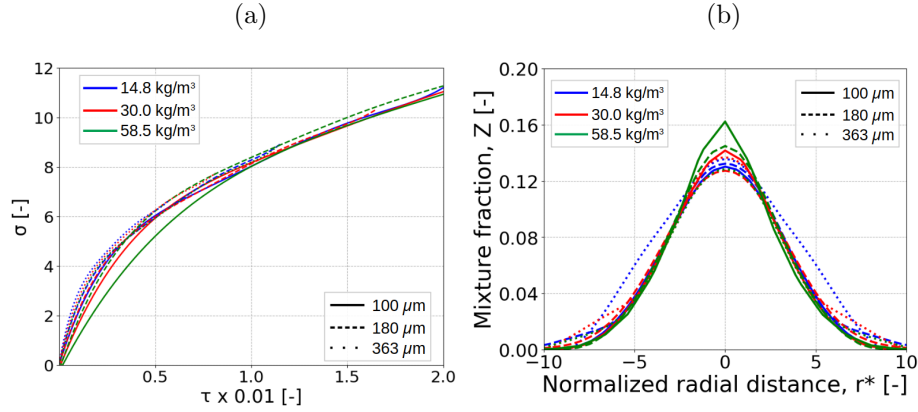


Figure 2: (a) Dimensionless penetration length ( $\sigma$ ) as a function of dimensionless penetration time ( $\tau$ ) and (b) mixture fraction distribution along normalized radial direction,  $r^*$  at normalized axial distance,  $x^* = 40$  for different  $\rho_{am}$  of 14.8, 30.0, and 58.5 kg/m<sup>3</sup>. Solid-, dashed- and dotted-lines are results for  $D_{noz}$  of 100, 180, and 363 μm, respectively.

180 time,  $\tau$ . Detailed methodology to calculate  $\sigma$  and  $\tau$  can be found in [17]. As  
 181 seen in Figure 2a, all the  $\sigma$  curves collapse on to one another, which agrees with  
 182 the trend reported in [17]. This indicates that the dependence of VPL on  $D_{noz}$   
 183 and  $\rho_{am}$  is successfully simulated by the model.

184 It is shown in [10, 22] that the profiles of mixture fraction for two different  
 185  $D_{noz}$  collapse onto one another in normalized coordinates. Therefore, similar  
 186 methodology from [10, 22] is applied to analyze the profiles of mixture fraction  
 187 for Cases 1–9 (in Table 1. Figure 2b shows the mixture fraction ( $Z$ ) fields from  
 188 cases with varying  $\rho_{am}$  and  $D_{noz}$  (Cases 1–9) compared together in normalized  
 189 radial ( $r^*$ ) and axial ( $x^*$ ) coordinates. The normalized coordinates  $r^*$  and  $x^*$   
 190 are computed by normalizing the radial ( $r$ ) and axial coordinate ( $x$ ) by the  
 191 equivalent diameter ( $d_{eq}$ ) of each nozzle, i.e.,  $r^* = r/d_{eq}$  and  $x^* = x/d_{eq}$  [10, 22].  
 192 The equivalent diameter is calculated as  $d_{eq} = D_{noz} \sqrt{\rho_f/\rho_{am}}$ , where  $\rho_f$  denotes  
 193 the density of the fuel. It is shown in Figure 2b that the mixture fraction profiles  
 194 from different  $\rho_{am}$  and  $D_{noz}$  collapse onto one another. This implies that the  
 195 dependence of mixture fraction distribution on  $\rho_{am}$  and  $D_{noz}$  is also successfully  
 196 simulated by the model.

197 *4.2. Reacting Spray Validation*

198 Two *n*-heptane (C<sub>7</sub>H<sub>16</sub>) mechanisms are evaluated in this section. The two  
199 mechanisms are the reduced C<sub>7</sub>H<sub>16</sub> mechanism (68 species and 283 reactions)  
200 developed by Lu et al. [34], and the mechanism (44 species and 112 reactions)  
201 developed by Liu et al. [35]. The mechanisms are henceforth denoted as Lu68  
202 and Liu44, respectively. These two mechanisms have shown good performance  
203 in spray combustion context [24, 32, 25, 36]. The IDTs predicted by the two  
204 mechanisms for different  $D_{\text{noz}}$  and  $\rho_{\text{am}}$  are simulated and compared against  
205 measurement data [1], as shown in Figure 3. The IDT is defined as the time  
206 taken for the mixture temperature to increase by 400 K from its initial temperature  
207 ( $\Delta T = 400$  K), following the definition in [25]. The IDT predicted by Liu44  
208 overpredicts the IDT by 27 % in the low density case (14.8 kg/m<sup>3</sup>), but underpredicts  
209 by 37 % in the high density case (58.5 kg/m<sup>3</sup>). Overall, the results from Lu68 are  
210 in better agreement than those of Liu44 with the experimental data. For a fixed  
211  $D_{\text{noz}}$ , the computed IDTs are shown in Figure 3 to decrease with increasing  
212  $\rho_{\text{am}}$ , which correspond with measurements. At all three  $\rho_{\text{am}}$ , the simulated  
213 IDTs are shown to increase with  $D_{\text{noz}}$ . This agrees with the measurement  
214 trend at  $\rho_{\text{am}} = 14.8$  kg/m<sup>3</sup>. However, a non-monotonic trend is observed  
215 for the measurement data at 30.0 kg/m<sup>3</sup> where the IDT increases from 100  
216 to 180  $\mu\text{m}$ , but decreases from 180 to 363  $\mu\text{m}$ . This discrepancy may be due  
217 to the experimental uncertainties caused by the hydraulic delay during fuel  
218 injection [37]. Despite this, the relative errors across different  $\rho_{\text{am}}$  and  $D_{\text{noz}}$  are  
219 less than 50 % for the Lu68 mechanism. In addition to this, the performance of  
220 the Lu68 mechanism in a zero-dimensional homogeneous reactor is available in  
221 the Appendix A1.

222 **5. Results & Discussion**

223 In this section, the autoignition characteristics for different  $D_{\text{noz}}$  at  $\rho_{\text{am}}$   
224 of 14.8 kg/m<sup>3</sup> (Figure 4), 30.0 kg/m<sup>3</sup> (Figure 6), and 58.5 kg/m<sup>3</sup> (Figure 8)  
225 are studied using scatter plots of the temperature-mixture fraction ( $T$ - $Z$ ) and

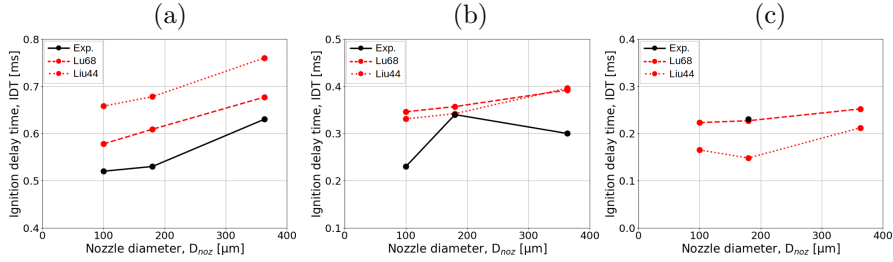


Figure 3: Ignition delay time, IDT as a function of nozzle diameter,  $D_{noz}$  at different  $\rho_{am}$  of (a) 14.8, (b) 30.0, and (c) 58.5 kg/m<sup>3</sup>. Solid-lines denote experimental results. Dashed- and dotted-lines denote the simulation results from Lu68 and Liu44 mechanisms, respectively.

226 contours of various combustion products. For all the cases (shown in Table 1),  
 227 the low-temperature ignition first initiates in fuel-lean region ( $Z < Z_{st}$ ), where  
 228  $Z_{st}$  is the stoichiometric mixture fraction with a value of 0.062. It is followed by  
 229 a temperature rise within the fuel-rich region ( $Z > Z_{st}$ ). Thereafter, the high-  
 230 temperature combustion occurs within a relatively less-rich mixture. These  
 231 observations agree with the findings by Pei et al. [38]. Despite this, there are  
 232 still distinct differences in the ignition characteristics as  $\rho_{am}$  and  $D_{noz}$  change,  
 233 which will be discussed in detail in the following sections.

### 234 5.1. Ignition characteristics at $\rho_{am} = 14.8 \text{ kg/m}^3$

235 For the 100  $\mu\text{m}$  case at 14.8 kg/m<sup>3</sup>, high concentration of RO<sub>2</sub> is shown  
 236 to form in the fuel-rich inner core of the spray at  $t = 0.540 \text{ ms}$  (cf. Figure 4a).  
 237 Through the low-temperature reaction pathway, RO<sub>2</sub> oxidizes to form ketohydro-  
 238 peroxide (KET) which also resides in the inner core of the spray. At this time  
 239 instance, HO<sub>2</sub> radicals form around the vicinity of KET where the spray region  
 240 is fuel-rich, as shown in Figure 4a. The  $T$ - $Z$  diagram in Figure 4a also shows  
 241 the presence of OH in the fuel-rich side with a peak temperature of  $\sim 1100 \text{ K}$ . It  
 242 is notable that RO<sub>2</sub>, KET and HO<sub>2</sub> are formed downstream of the liquid fuel.

243 At  $t = 0.588 \text{ ms}$  (Figure 4b), high concentration of HO<sub>2</sub> is seen forming at  
 244 two distinct regions in the spray: the L-region which has low local temperature  
 245 with fuel-richer mixture composition, and the H-region which has relatively  
 246 higher local temperature as well as less fuel-rich mixture composition. Moreover,

247 it is illustrated in Figure 4b that OH is present at the H-region, thus implying  
 248 that HO<sub>2</sub> has been consumed and undergone high-temperature reaction to form  
 249 OH. The local temperature is also shown to increase beyond the temperature  
 250 threshold of 1400 K (400 K above  $T_{\text{am}}$ ), which indicates the onset of the main  
 251 ignition.

252 The ignition characteristics for the 180 and 363  $\mu\text{m}$  nozzle cases are illustrated  
 253 in Figures 4d-f and 4g-i, respectively. During the low-temperature ignition stage  
 254 at 0.574 ms, HO<sub>2</sub> and OH are present at the fuel-rich side in the 180  $\mu\text{m}$  case  
 255 (cf. Figure 4d). It is also important to note that the high-temperature ignition  
 256 in all three  $D_{\text{noz}}$  cases occurs in the fuel-rich side at  $\rho_{\text{am}}$  of 14.8 kg/m<sup>3</sup>.

257 A noticeable difference when  $D_{\text{noz}}$  increases is the low- and high-temperature  
 258 ignition process occurring later in time. This is expected as the IDT is shown  
 259 previously to increase with increasing  $D_{\text{noz}}$  (cf. Figure 3). The effects of  $D_{\text{noz}}$   
 260 and  $\rho_{\text{am}}$  on IDT will be further discussed in Section 5.4. Meanwhile, it is shown  
 261 in Figure 4 that the onset of high-temperature ignition occurs at the spray head  
 262 for  $D_{\text{noz}}$  of 100  $\mu\text{m}$ , which is similarly obtained in the 3-D large eddy simulations  
 263 by Irannejad et al. [39]. However, the ignition location is seen to shift to the  
 264 spray periphery as  $D_{\text{noz}}$  increases to 363  $\mu\text{m}$ . This can be attributed to the  
 265 overly fuel-rich region in the spray central region as  $D_{\text{noz}}$  increases. Figure 5  
 266 shows the scatter plots of  $T$ , colored by different ranges of  $Z$ , along the spray axis  
 267 for both the central and peripheral region of different  $D_{\text{noz}}$  at  $\rho_{\text{am}} = 14.8 \text{ kg/m}^3$ .  
 268 The radial distance from the spray axis is denoted as  $R$ . The central region of  
 269 the spray is defined as the region where  $R \leq d_{\text{eq}}$ , while the peripheral region  
 270 is defined as  $R > d_{\text{eq}}$ . Onset of high-temperature ignition is observed at both  
 271 the spray center and periphery for the 100  $\mu\text{m}$  case, as depicted in Figure 5a.  
 272 However, as  $D_{\text{noz}}$  increases to 180  $\mu\text{m}$  and 363  $\mu\text{m}$ , the onset of high-temperature  
 273 ignition is shown to occur at the spray periphery (cf. Figures 5b and c), where  
 274 the temperature rise in spray central region of the latter case is significantly  
 275 lower than in the spray periphery.

276 Moreover, the evaporative cooling of the injected liquid fuel reduces the  
 277 temperature of the mixtures at the inner spray region near the LPL, as compared

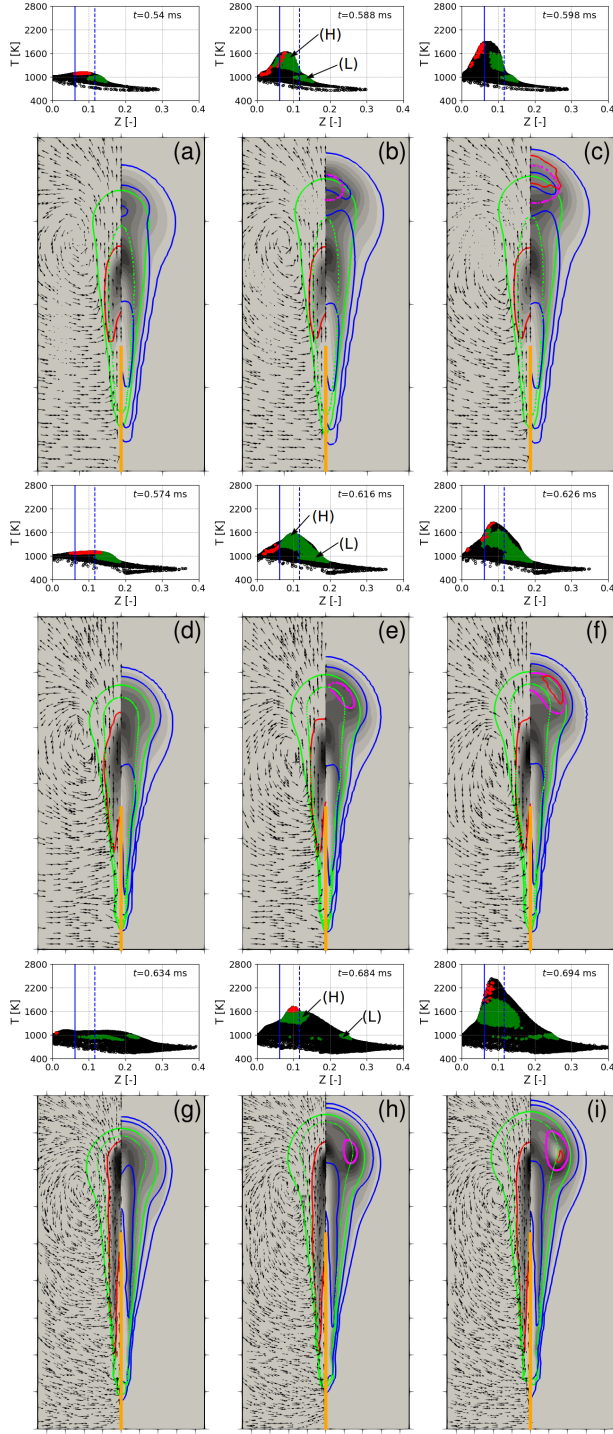


Figure 4: Velocity vectors and contours of combustion products in the  $14.8 \text{ kg/m}^3$  case for  $D_{\text{noz}}$  of (a-c)  $100 \mu\text{m}$ , (d-f)  $180 \mu\text{m}$ , and (g-i)  $363 \mu\text{m}$ . Above them are their corresponding scatter plot of temperature-mixture fraction ( $T$ - $Z$ ). Left, middle and right columns represent the low-temperature ignition stage, onset of high-temperature ignition, and formation of a classical diesel spray flame. Scatter plots: Cells with substantial formation of  $\text{HO}_2$  and  $\text{OH}$  are marked with green and red, respectively. The thresholds are set to 70% of their respective maximum mass fraction. Stoichiometric and most reactive mixture fractions are represented by solid blue and dashed blue lines, respectively. Contours (a-i): (Left) Ketohydroperoxide contour with velocity vectors (black arrows) and  $\text{RO}_2$  mass fraction of  $1 \times 10^{-4}$  (solid red); and (Right)  $\text{HO}_2$  contour with isolines of scalar dissipation rates of 1, 10, and 100 (solid blue),  $\text{OH}$  mass fraction of  $1 \times 10^{-4}$  (solid red), and temperature of 1400 K (magenta). Maximum mass fraction of  $\text{KET}$  and  $\text{HO}_2$  are fixed at 0.003 and 0.0006, respectively. Solid green lines indicate the stoichiometric line and the orange line represent the averaged liquid length. Each frame in (a-c) shows  $20 \times 40 \text{ mm}$ , (d-f) shows  $30 \times 60 \text{ mm}$ , and (g-i) shows  $45 \times 90 \text{ mm}$ .

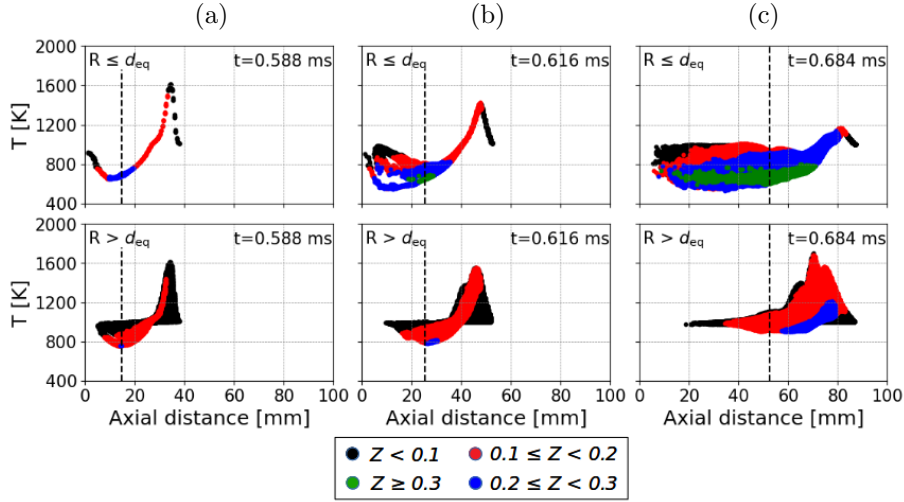


Figure 5: Scatter plots of temperature ( $T$ ) colored by different ranges of mixture fraction ( $Z$ ) at the onset of high-temperature ignition for  $D_{\text{noz}}$  of (a)  $100\ \mu\text{m}$ , (b)  $180\ \mu\text{m}$ , and (c)  $363\ \mu\text{m}$  at  $\rho_{\text{am}}$  of  $14.8\ \text{kg}/\text{m}^3$ . Dashed vertical lines represent the liquid penetration length. Top row: spray central region ( $R \leq d_{\text{eq}}$ ). Bottom row: spray periphery ( $R > d_{\text{eq}}$ ).

278 to that in the spray periphery (cf. Figures 5). The overly fuel-rich region  
 279 ( $Z > 0.2$ ), which has a lower temperature, in the spray central region is,  
 280 hence, expected to be unfavorable for ignition. This observation is supported by  
 281 findings from the large eddy simulation results in [23] and the two-dimensional  
 282 direct numerical simulation conducted by Krisman et al. [40]. It is shown that  
 283 the cool-flame takes a longer time to reach the most fuel-rich mixture [40].  
 284 Meanwhile, the fuel-rich mixture itself takes a longer time to have a spontaneous  
 285 ignition due to having a longer low-temperature IDT as shown in the zero-  
 286 dimensional homogeneous reactor simulation results (see Figure A1 in Appendix  
 287 A1). This corresponds well to the findings in [41]. These reasons may explain  
 288 the observation where the high-temperature ignition is more inclined to occur  
 289 at the spray periphery than at the spray center region as  $D_{\text{noz}}$  increases.

## 290 5.2. Ignition characteristics at $\rho_{\text{am}} = 30.0\ \text{kg}/\text{m}^3$

291 At a higher ambient density of  $\rho_{\text{am}} = 30.0\ \text{kg}/\text{m}^3$  (Figure 6), the formation of  
 292  $\text{RO}_2$ ,  $\text{KET}$  and  $\text{HO}_2$  starts earlier for the  $100\ \mu\text{m}$  nozzle case. From Figures 6a,

293 HO<sub>2</sub> are also formed in the fuel-rich region where local temperature exceeds  
 294 1100 K. The same phenomenon is observed for the larger  $D_{\text{noz}}$  cases of 180 and  
 295 363  $\mu\text{m}$ . However, at this high  $\rho_{\text{am}}$ , HO<sub>2</sub> does not form at two distinct regions  
 296 during the onset of high-temperature ignition as that observed at a lower  $\rho_{\text{am}}$   
 297 of 14.8 kg/m<sup>3</sup>. Instead, HO<sub>2</sub> is shown to form across a wide range of  $Z$  and  $T$ ,  
 298 as shown in the  $T$ - $Z$  diagrams of Figures 6b, 6e, and 6h. The high-temperature  
 299 ignitions across different  $D_{\text{noz}}$  occur at the fuel-rich side. This observation  
 300 is similar to that observed in the 14.8 kg/m<sup>3</sup> case discussed above, although  
 301 the transition period from low- to high-temperature ignition is now shorter.  
 302 This is expected as a shorter transition is also observed in the homogeneous  
 303 reactor calculation (see Figure A1 in Appendix A1) as well as in [25]. With a  
 304 shorter transition time, the ignition location are now nearer to the liquid jet  
 305 which is highly fuel-rich at the inner core. This, consequently, results in the  
 306 ignition location to occur at the spray periphery which is relatively less fuel-  
 307 rich. Figure 7 shows the scatter plots of  $T$ , colored by different ranges of  $Z$ ,  
 308 along the spray axis for both the central and peripheral region of different  $D_{\text{noz}}$   
 309 at  $\rho_{\text{am}}$  of 30.0 kg/m<sup>3</sup>. In all three  $D_{\text{noz}}$  cases, the high-temperature ignitions  
 310 occur at  $R > d_{\text{eq}}$  as well as being closer to the liquid jet. As shown in the top  
 311 row of Figure 7, the inner cores of the spray are more fuel-rich ( $Z > 0.2$ ) and  
 312 have low temperature, which makes them unfavorable for ignition to occur. The  
 313 above explanation agrees with the experimental results presented by Higgins et  
 314 al. [19] for  $D_{\text{noz}} = 246 \mu\text{m}$ .

### 315 5.3. Ignition characteristics at $\rho_{\text{am}} = 58.5 \text{ kg/m}^3$

316 The phenomena are akin to those observed at 30.0 kg/m<sup>3</sup>. From Figure 8, it  
 317 is also obvious that the ignition locations for all three  $D_{\text{am}}$  are all at the spray  
 318 periphery. This can again be explained by analyzing the  $T$  and  $Z$  along the  
 319 spray axis. Figure 9 shows the scatter plots of  $T$ , colored by different ranges of  
 320  $Z$ , along the spray axis for both the central and peripheral region of different  
 321  $D_{\text{noz}}$  at  $\rho_{\text{am}} = 58.5 \text{ kg/m}^3$ . From the figure, the inner core is shown to be too  
 322 fuel-rich to be conducive for ignition, thus ignition occurs at the sides instead.



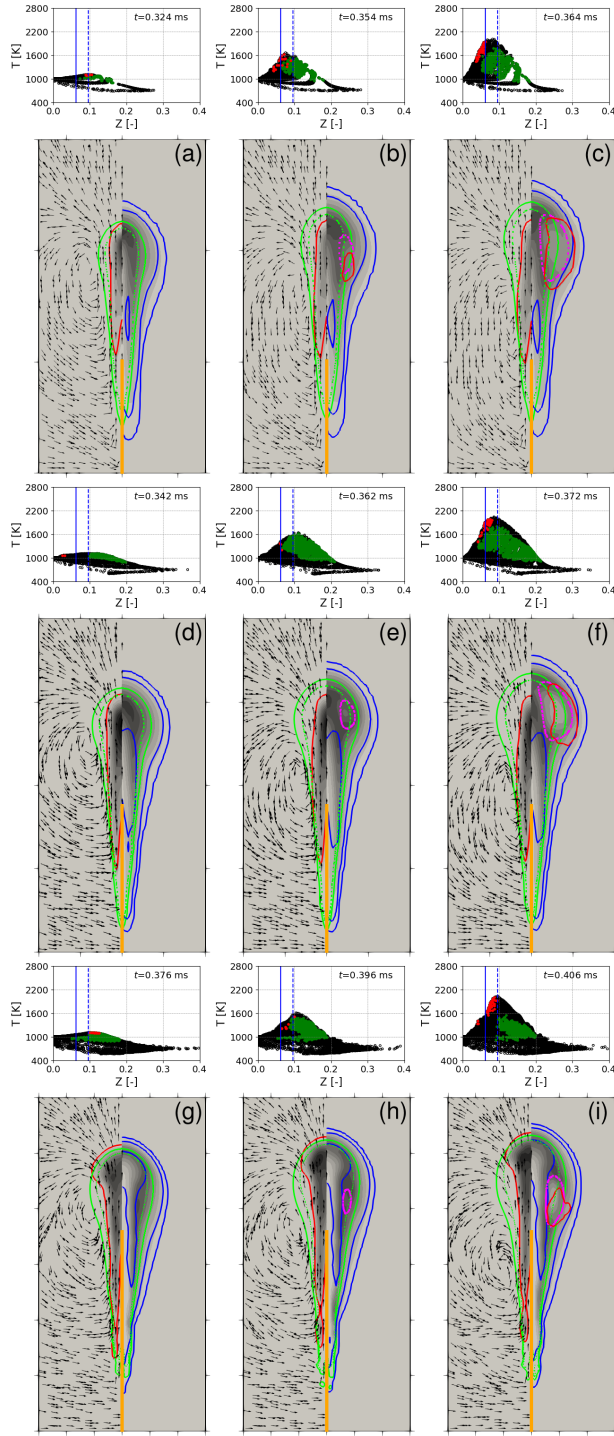


Figure 6: Velocity vectors and contours of combustion products in the  $30.0 \text{ kg/m}^3$  case for  $D_{\text{hoz}}$  of (a-c)  $100 \mu\text{m}$ , (d-f)  $180 \mu\text{m}$ , and (g-i)  $363 \mu\text{m}$  at different times. Above them are their corresponding scatter plot of temperature-mixture fraction ( $T$ - $Z$ ). Descriptions can be found in the caption of Figure 4. Each frame in (a-c) shows  $20 \times 40 \text{ mm}$ , and (g-i) shows  $30 \times 60 \text{ mm}$ .

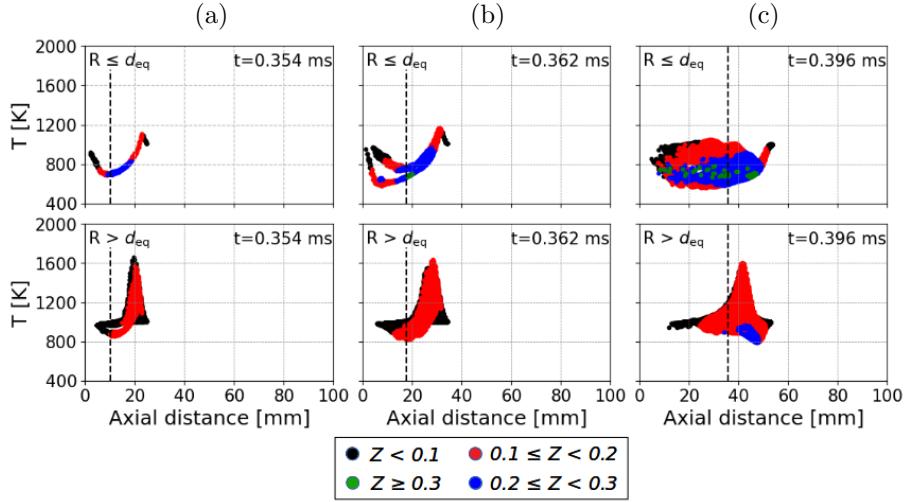


Figure 7: Scatter plots of temperature ( $T$ ) colored by different ranges of mixture fraction ( $Z$ ) at the onset of high-temperature ignition for  $D_{noz}$  of (a) 100  $\mu\text{m}$ , (b) 180  $\mu\text{m}$ , and (c) 363  $\mu\text{m}$  at  $\rho_{am}$  of 30.0  $\text{kg}/\text{m}^3$ . Dashed vertical lines represent the liquid penetration length. Top row: spray central region ( $R \leq d_{eq}$ ). Bottom row: spray periphery ( $R > d_{eq}$ ).

323 Furthermore, it is also illustrated in Figure 9 that the ignition location is closer  
 324 to the liquid jet at this high  $\rho_{am}$  condition than in the low  $\rho_{am}$  cases. This is  
 325 expected as the ambient density increases even further, the transition from low-  
 326 to high-temperature ignition shortens considerably. This consequently leads to  
 327 the ignition to occur much closer to the liquid jet.

328 In this high  $\rho_{am}$  case of 58.5  $\text{kg}/\text{m}^3$ , the high-temperature ignitions for both  
 329 100  $\mu\text{m}$  and 180  $\mu\text{m}$  cases occur at fuel-lean region. The observation for the  
 330 180  $\mu\text{m}$  case agrees with a similar work from literature [25] which simulated the  
 331 exact same setup by using a smaller  $n$ -heptane mechanism. However, this is  
 332 not the case when  $D_{noz}$  increase to 363  $\mu\text{m}$  which shows the ignition to occur  
 333 at the fuel-rich region. This difference is likely attributed to the longer IDT for  
 334 the 363  $\mu\text{m}$ , 58.5  $\text{kg}/\text{m}^3$  case, which causes significant amount of  $\text{HO}_2$  to form in  
 335 the fuel-rich region and consequently resulting in the fuel-rich mixture igniting.  
 336 Another reason can be related to the overly fuel-rich mixture at the spray core  
 337 as shown in Figure 9c. Evaporative cooling is more significant in the large nozzle

338 case as more liquid fuel is injected and longer LPL is observed. The stronger  
339 evaporative cooling of the liquid fuel in the large nozzle case prevents ignition  
340 to occur at  $Z < 0.1$  as observed in the 100 and 180  $\mu\text{m}$  cases (cf. Figures 9a and  
341 9b). Only until the cool-flame has spread to a relatively fuel-rich region that  
342 leads to high-temperature ignition. This also leads to a longer IDT observed for  
343 the 363  $\mu\text{m}$  nozzle case.

#### 344 5.4. Effects of $D_{\text{noz}}$ and $\rho_{\text{am}}$ on ignition delay time

345 As shown previously (Figure 3) the IDT increases as  $D_{\text{noz}}$  increases. This  
346 can be attributed to the different values of local scalar dissipation rate ( $\chi$ ) for  
347 different  $D_{\text{noz}}$  and at varying  $\rho_{\text{am}}$ , as shown in Figure 10. Figure 10 shows  
348 the scatter plot of OH and  $\chi$  for varying  $D_{\text{noz}}$  at  $\rho_{\text{am}}$  of (a) 14.8  $\text{kg}/\text{m}^3$ , (b)  
349 30.0  $\text{kg}/\text{m}^3$ , and (c) 58.5  $\text{kg}/\text{m}^3$  during the onset of high-temperature ignition.  
350 From the figure, the  $\chi$  for the 363  $\mu\text{m}$  nozzle case is consistently larger than the  
351 100  $\mu\text{m}$  case by at least a factor of 3. A high  $\chi$  leads to longer IDT [41], hence  
352 explaining the longer IDT obtained as  $D_{\text{noz}}$  increases.

353 It is also depicted in Figure 3 that IDT becomes shorter as  $\rho_{\text{am}}$  increases.  
354 As aforementioned in Section 5.2, the shorter IDT is likely attributed to the  
355 shorter chemical time scale when the ambient density increases. The findings  
356 are supported by the homogeneous reactor results (see Figure A1 in Appendix  
357 A1) and the results in [25], which show shorter IDT as  $\rho_{\text{am}}$  increases from 14.8  
358 to 58.5  $\text{kg}/\text{m}^3$ .

## 359 6. Conclusion

360 The present work performed an Unsteady Reynolds Averaged Navier-Stokes  
361 simulations coupled with Eulerian Stochastic Field method to study the effects  
362 of nozzle diameter ( $D_{\text{noz}}$ ) and ambient density ( $\rho_{\text{am}}$ ) on ignition characteristics  
363 in Diesel #2 spray flames. The numerical model is able to capture the ignition  
364 processes for different  $D_{\text{noz}}$  of 100, 180, and 363  $\mu\text{m}$  at  $\rho_{\text{am}}$  of 14.8, 30.0, and  
365 58.5  $\text{kg}/\text{m}^3$ . Comparisons to measurements show that the ignition delay times  
366 are well predicted.

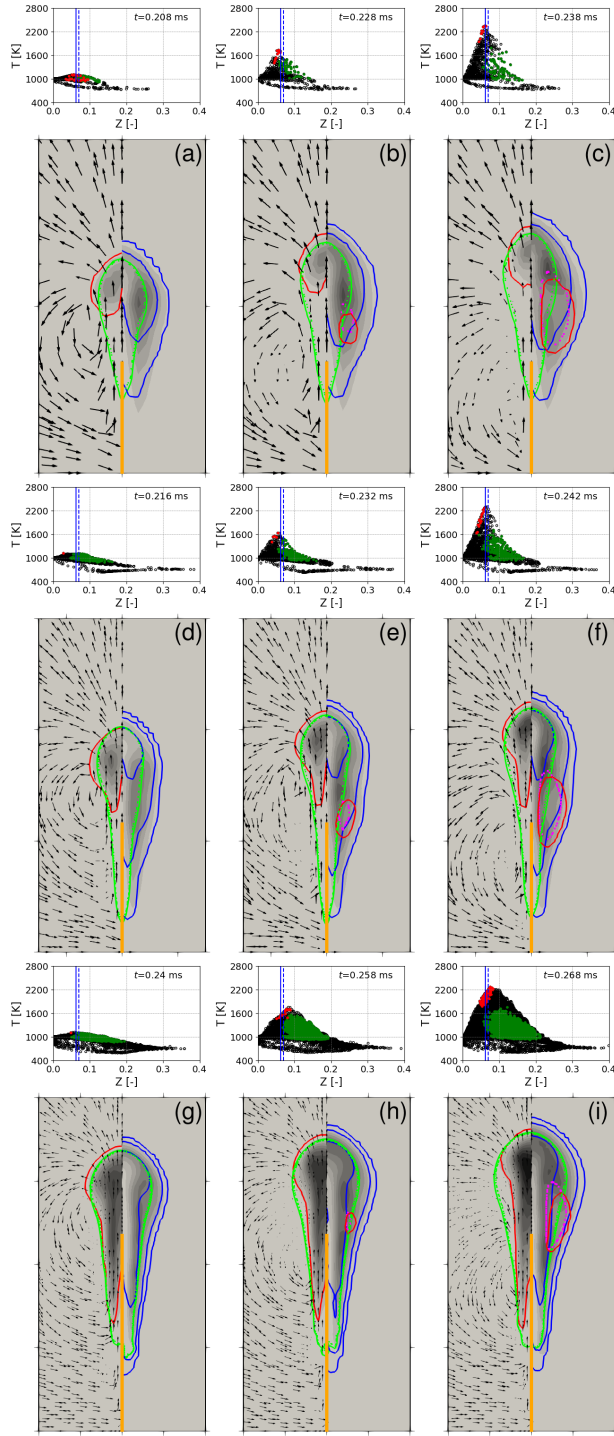


Figure 8: Velocity vectors and contours of combustion products in the  $58.5 \text{ kg/m}^3$  case for  $D_{\text{hoz}}$  of (a-c)  $100 \mu\text{m}$ , (d-f)  $180 \mu\text{m}$ , and (g-i)  $363 \mu\text{m}$  at different times. Above them are their corresponding scatter plot of temperature-mixture fraction ( $T$ - $Z$ ). Descriptions can be found in the caption of Figure 4. Each frame in (a-c) shows  $15 \times 30 \text{ mm}$ , (d-f) shows  $15 \times 30 \text{ mm}$ , and (g-i) shows  $20 \times 40 \text{ mm}$ .

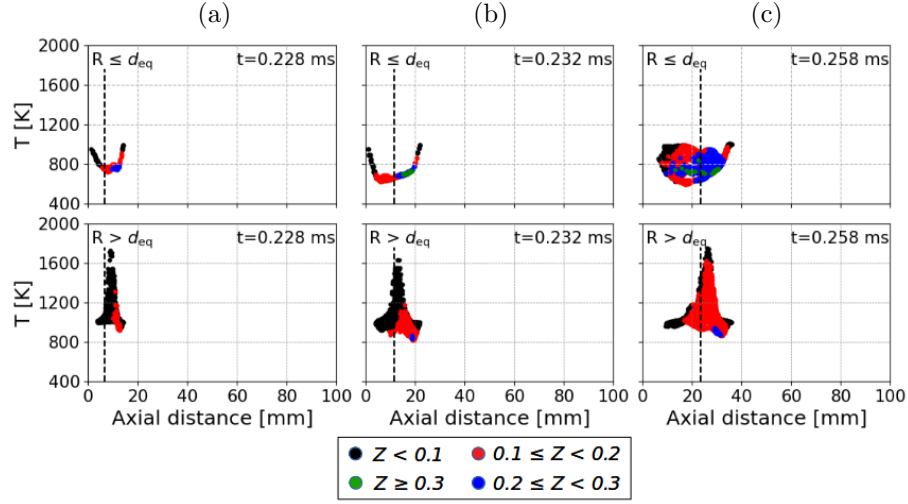


Figure 9: Scatter plots of temperature ( $T$ ) colored by different ranges of mixture fraction ( $Z$ ) at the onset of high-temperature ignition for  $D_{noz}$  of (a) 100  $\mu\text{m}$ , (b) 180  $\mu\text{m}$ , and (c) 363  $\mu\text{m}$  at  $\rho_{am}$  of 58.5  $\text{kg}/\text{m}^3$ . Dashed vertical lines represent the liquid penetration length. Top row: spray central region ( $R \leq d_{eq}$ ). Bottom row: spray periphery ( $R > d_{eq}$ ).

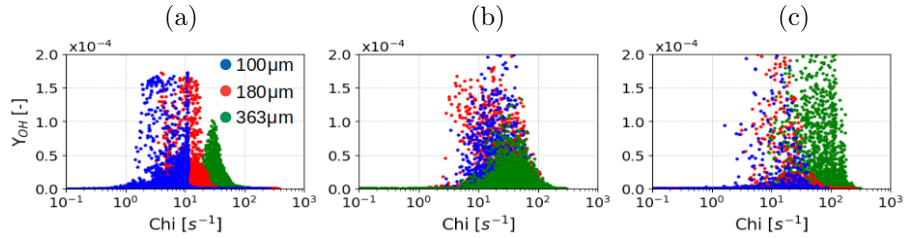


Figure 10: Scatter plots of mass fraction of OH and scalar dissipation rate (OH- $\chi$ ) at the onset of high-temperature ignition for different  $\rho_{am}$  of (a) 14.8  $\text{kg}/\text{m}^3$ , (b) 30.0  $\text{kg}/\text{m}^3$ , and (c) 58.5  $\text{kg}/\text{m}^3$ , as well as  $D_{noz}$  of 100, 180, and 363  $\mu\text{m}$ .

367 For the low density case ( $14.8 \text{ kg/m}^3$ ), the high-temperature ignition location  
368 is predicted to shift from the spray tip towards the spray periphery as  $D_{\text{noz}}$   
369 increases. The current result suggests that the mixture at the spray central  
370 region (including the spray tip) are getting more fuel-rich ( $Z > 0.2$ ) as  $D_{\text{noz}}$   
371 increases. This leads to the spray central region being unfavorable for ignition  
372 due to being overly fuel-rich and having lower temperature. Instead, the ignition  
373 occurs at the periphery of the spray where  $Z \leq 0.2$ . As  $\rho_{\text{am}}$  increases to 30.0  
374 and  $58.5 \text{ kg/m}^3$ , the ignition locations for all  $D_{\text{noz}}$  cases are occurring at the  
375 spray periphery. This is because of the shorter ignition timing and the overly  
376 fuel-rich spray central region.

377 The numerical results show that the mixture fraction of the first igniting  
378 mixture during the high-temperature ignition across different  $D_{\text{noz}}$  are at the  
379 fuel-rich region at  $\rho_{\text{am}}$  of 14.8 and  $30.0 \text{ kg/m}^3$ . However, this is not the case  
380 when  $\rho_{\text{am}}$  increases to  $58.5 \text{ kg/m}^3$ . The igniting mixture still occurs at the fuel-  
381 rich region for the  $363 \mu\text{m}$  nozzle case, but it occurs at the fuel-lean side for the  
382  $D_{\text{noz}}$  cases of 100 and  $180 \mu\text{m}$ . This can be attributed to the relatively longer  
383 ignition delay time in the  $363 \mu\text{m}$  nozzle case. The longer ignition delay time as  
384  $D_{\text{noz}}$  increases can be related to the higher local scalar dissipation rate observed  
385 in the large nozzle case.

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517 **Appendix**

518 *A1: Autoignition in 0-D homogeneous reactor*

519 The autoignition characteristics of Lu68 mechanism is first evaluated by  
520 performing a zero-dimensional (0-D) homogeneous reactor calculations at three  
521 different initial ambient density ( $\rho_{\text{am}}$ ) of 14.8, 30.0, and 58.5 kg/m<sup>3</sup> and three  
522 different nozzle diameter ( $D_{\text{noz}}$ ) of 100, 180, and 363  $\mu\text{m}$  using the Ansys CHEMKIN-  
523 PRO software. The high-temperature ignition delay time ( $\text{IDT}_{\text{HT}}$ ) here is  
524 defined as the time where the mixture temperature increase to 400 K above the  
525 initial temperature ( $T_{t=0}$ ). Mass fraction of heptyl radical, C<sub>7</sub>H<sub>15</sub>O<sub>2</sub> (RO<sub>2</sub> is  
526 henceforth used for brevity) is used as an indicator for the low-temperature  
527 ignition (LTI) activity. Therefore, the low-temperature ignition delay time  
528 ( $\text{IDT}_{\text{LT}}$ ) is defined here as the time where the maximum mass fraction of RO<sub>2</sub>  
529 is attained.

530 A quadratic correlation (Equation 1) between temperature and mixture  
531 fraction can be obtained by postprocessing the 3D-CFD reacting case results  
532 prior to the onset of LTI.

$$T_{t=0} = T_{\text{am}} + 1120Z^2 - 1370Z \quad (1)$$

533 In Equation 1,  $Z$  denotes the mixture fraction while  $T_{\text{am}}$  denotes the initial  
534 ambient temperature in the combustion chamber which is set as 1000 K. This  
535 quadratic correlation corresponds to the mixing of vapor fuel and hot ambient  
536 air. Therefore, it is also known as the spray mixing line. Equation 1 is  
537 constructed for  $0 \leq Z \leq 0.4$  and the equation is found to be applicable for  
538 all three  $\rho_{\text{am}}$  and three  $D_{\text{noz}}$  cases (not shown). The most reactive mixture  
539 fraction ( $Z_{\text{mr}}$ ) is defined as the mixture which has the shortest  $\text{IDT}_{\text{HT}}$ , and the  
540 associated IDT is known as most reactive IDT ( $\text{IDT}_{\text{mr}}$ ).

541 From Figure A1a,  $Z_{\text{mr}}$  is shown to decrease and move towards the stoichiometric  
542 mixture fraction ( $Z_{\text{st}}$ ) with increasing  $\rho_{\text{am}}$ . The  $Z_{\text{mr}}$  are recorded to be 0.117,  
543 0.096, and 0.070 for the 14.8, 30.0, and 58.5 kg/m<sup>3</sup> cases, respectively. The  
544 corresponding  $T_{t=0}$  are 855, 879, 905 K. As the same correlation (Eq. 1) is

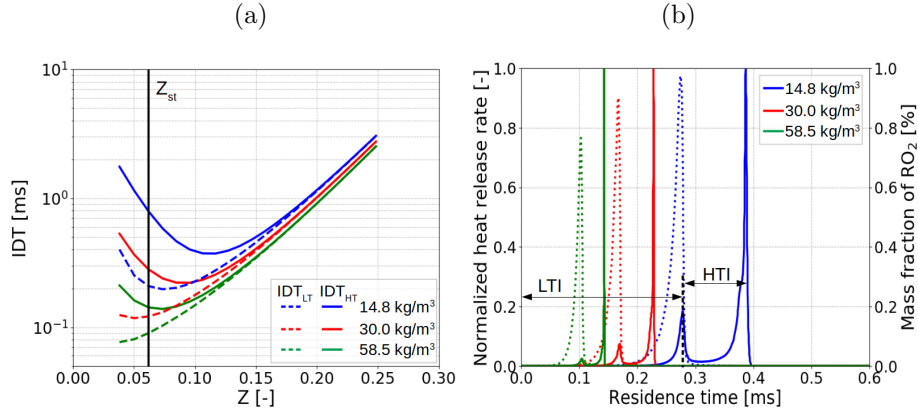


Figure A1: (a) Low-temperature ( $IDT_{LT}$ ) and high-temperature ignition delay times ( $IDT_{HT}$ ) of homogeneous mixtures for various initial mixture fractions ( $Z$ ) and temperatures ( $T$ ) at  $\rho_{am}$  of 14.8, 30.0, and 58.5 kg/m<sup>3</sup>. Solid vertical black line represents stoichiometric mixture fraction ( $Z_{st}$ ) of 0.062. (b) Temporal evolution of normalized heat release rate (HRR) of  $Z_{mr}$  computed in the 0-D homogeneous reactor model at  $\rho_{am}$  of 14.8, 30.0, and 58.5 kg/m<sup>3</sup>. Solid lines represent the normalized HRR. Dotted lines represent mass fraction of RO<sub>2</sub>.

545 applicable across different  $D_{noz}$  for a given  $\rho_{am}$ , the  $Z_{mr}$  obtained from Figure A1a  
 546 is applicable for all three  $D_{noz}$ . This also implies that  $D_{noz}$  has no significant  
 547 effect on  $Z_{mr}$  in the present study. In addition to this, Figure A1a also shows  
 548 that both  $IDT_{LT}$  and  $IDT_{HT}$  become shorter as  $\rho_{am}$  increases. Furthermore,  
 549 longer IDTs are obtained as the mixture becomes richer ( $Z$  increases) and has  
 550 a lower temperature ( $T_{t=0}$  decreases). It is also worth mentioning that the  
 551 dwell period between LTI and high-temperature ignition (HTI) decreases as the  
 552 mixture becomes richer (cf. Figure A1a). This is similarly shown for *n*-dodecane  
 553 fuel in [41].

554 Figure A1b depicts the simulated heat releases rate (HRR) at the most  
 555 reactive states for each  $\rho_{am}$  case. The temporal evolution of RO<sub>2</sub> of these cases  
 556 are also provided in the figure. It is evidently shown in Figure A1b that the LTI  
 557 and HTI stages coincide with the peak of RO<sub>2</sub> and HRR. Moreover, the HTI  
 558 stage is also shown to occur after RO<sub>2</sub> is consumed.