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# Real-Time Power Market Clearing Model with Improved Network Constraints Considering PTDF Correction and Fast-Calculated Dynamic Line Rating

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**Abstract**—The increasing penetration of renewables in power systems reconfigures the generation mix and geography distribution, resulting in more frequent power flow congestion. Conventionally, a relatively conservative dispatch margin for transmission congestion in network constraints was reserved to ensure safe operation due to potential deviations introduced by DC power flow modeling and conservative line rating. This paper proposes a real-time power market clearing model with improved network constraints considering power transfer distribution factor (PTDF) correction and fast-calculated dynamic line rating. The clearing model based on PTDF correction is proposed first employing the Taylor expansion with the voltage and phase angle approximation. An improved dynamic line rating model is further applied into the clearing model based on the piecewise linear approximation method, which calculates real-time conductor temperature faster with sufficient precision. We test and verify the validity of the proposed model based on three independent systems including the IEEE 39-bus system, the IEEE 2383-bus system, and the real power grid system in Yunnan province of China, respectively. The results show that the improved clearing model reduces the calculated power flow deviation between the clearing results and real conditions compared with traditional security constraints, where the efficiency of power grid operation is also increased.

**Index Terms**—Real-time market, network constraints, PTDF correction, dynamic line rating

## I. INTRODUCTION

The generation mix and geographical distribution have been reconfigured gradually in power systems with the increasing penetration of renewables [1]. Thus, the original power equilibrium in the network will be changed, resulting in unbalanced power flow distribution with more frequent congestion. The risk of power flow overload in heavy-loaded lines might be increased under traditional security constraints. Meanwhile, the power generation and dispatch schemes have

been readjusted to adapt to the market clearing in China because of its infancy reform since 2015 [2][3], which aggravates the issue. Therefore, an improved clearing model is required to confront such challenges.

However, electricity power market clearing models still experience shortfalls in light of network congestion [4][5]. A relatively conservative dispatch margin was reserved in network constraints to ensure the safe operation of the power system generally, which leads to the low line utilization rate. Two main reasons cause the problem. Firstly, existing mainstream clearing models are solved based on DC optimal power flow (DCOPF). Thus, the calculated power flow deviation between the clearing results and real conditions is difficult to be eliminated for imprecision in the DC power flow model compared with the AC power flow model [6], where the deviation will be named as ‘AC/DC deviation’ in the following. Power flow congestion might be misjudged with the increasing load when some line is heavy-loaded. Secondly, static line rating (SLR), used to determine the maximum transmission capacity, will lead to a lower line utilization rate due to underestimation of the available line rating in various weather conditions [7].

Moreover, real-time market (RTM) demands accurate market clearing results in the shortest time periods. The contradictory requirements between accuracy and expeditiousness are hard to be obtained. These characteristics also make the heat balance equation (HBE) for dynamic line rating more difficult to be integrated into existing real-time market clearing models. Thus, real-time conductor temperature is impossible to be calculated dynamically.

Several researches have been conducted on reducing AC/DC deviation [8]-[13]. On one hand, network loss has been improved. Reference [8]-[12] discussed the network loss approximation and its transmission. However, losses cannot be calculated precisely in the linear clearing model due to the squared term of current. On the other hand, the power flow

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model has been improved. Reference [13] proposed a linearized optimal power flow model with reactive power and voltage magnitude based on Taylor expansion. However, such studies cannot be applied into existing RTM clearing models solved by linear programming due to the nonlinear terms of voltage and phase angle. Meanwhile, the active and reactive power balance demands massive calculations with a longer time, which cannot adapt to the short time periods in RTM. Moreover, no existing researches consider the essence of power flow distribution and propose innovations from the perspective of power transfer distribution factor (PTDF) correction. Thus, the AC/DC deviation cannot be reduced fundamentally.

Several researches have also been carried out on the calculation of dynamic line rating (DLR) in optimal power flow under the transmission system [14]-[24]. Reference [15]-[17] proposed the calculation methods of DLR. However, these studies cannot calculate the real-time conductor temperature efficiently and fast in DCOPF because of many nonlinear terms in steady-state heat balance or complicated models. Reference [18]-[24] applied DLR calculation into AC optimal power flow problems in the day-ahead operation and real-time market of the power system. However, such studies demand massive calculations with a long time on the active and reactive power balance, which is hard to adapt to the short time periods in RTM.

This paper proposes an improved real-time market clearing model considering PTDF correction and fast-calculated dynamic line rating. PTDF correction based on Taylor expansion approximation improves the accuracy of power flow distribution. Improved dynamic line rating model with faster speed in calculating real-time conductor temperature further reduces the relatively conservative dispatch margin. Moreover, the line utilization rate can be improved due to elastic network constraints according to various weather conditions. In the context of the previous research, our paper provides the following contributions.

- 1) We propose an improved real-time market clearing model using DCOPF based on PTDF correction to reduce the AC/DC deviation. The correction factor is first derived from the AC power flow by Taylor expansion, then simplified by combining the characteristic such as the short time periods in RTM. The proposed model avoids the extensive computation of active and reactive power balances and improves the calculation accuracy of the DC power flow model without increasing the amount of calculation, which is also convenient to be integrated into the existing RTM model based on DCOPF.
- 2) We propose a fast-calculated dynamic line rating model in DCOPF based on the piecewise linear approximation method. The model considers the weather condition changes across the line spans and is simplified from the most rigorous dynamic line rating model at the dispatch level. During each time period, HBE can be represented by linear expressions at the dispatch level. The maximum transmission capacity can be adjusted flexibly according to ambient temperature and weather conditions.
- 3) We test and verify the validity of the proposed model in three independent systems, which are the IEEE 39-bus

system, IEEE 2383-system, and the real power grid in Yunnan province of China, respectively. The results have been proven effective in the real-world electricity spot market, which provides a reference for power grid system or electricity spot market in similar situations.

The structure of the paper is the following: Section II presents PTDF correction derivations based on an improved power flow model via Taylor expansion approximation. Section III presents the piecewise linear approximation method to calculate real-time conductor temperature, and formulates the improved real-time market clearing model considering fast-calculated dynamic line rating. Three independent systems simulation results of the proposed model, as well as analysis of four different methods, are presented in Section IV. Conclusions are presented in Section V.

We note that a preliminary conference paper addressed the issue of AC/DC deviation in [25], and this paper extends the more refined correction derivations and improved dynamic line rating model. The clearing model with network constraints representation and the iteration algorithm in RTM has also been researched further.

## II. PTDF CORRECTION DERIVATIONS

Here, we formulate the improved clearing model by PTDF correction. The mathematical model is derived from the improved power flow model in RTM based on Taylor's expansion with voltage and angle approximation combining with the real-time market characteristics. Quasi-steady-state correction is also considered to increase stability. We also improve the method to calculate marginal line losses more accurately.

### A. Improved Power Flow Model in RTM

Using the AC power flow model and ignoring the transformers, power flow through branch  $k \in K$  can be defined from node  $i$  to  $j$ ,

$$P_{ijk} = g_{ijk}(v_i^2 - v_i v_j \cos \theta_{ijk}) - b_{ijk} v_i v_j \sin \theta_{ijk} \quad (1)$$

where  $g_{ijk}$  and  $b_{ijk}$  represent the branch conductance and susceptance respectively.  $\theta_i$  is the phase angle and  $v_i$  represents the voltage magnitude. Formula (1) is applicable to the case of a single line with two nodes connected. Parallel processing is necessary when multiple lines are connected.

In actual power system operation, the fluctuation of phase angle and voltage is relatively small. Therefore, three main assumptions have been proposed on the simplified AC power flow approximation:

- (i) Voltage multiplied with angle is close to one per unit (p.u.) at all nodes, which means  $v_i v_j \theta_{ij} \approx \theta_{ij}$ .
- (ii) Voltage multiplied with branch conductance can be rewritten to another form, which means,

$$\frac{1}{2} g_{ijk} v_{ij}^2 \approx \frac{1}{2} g_{ijk} \left( \frac{v_i + v_j}{v_{i,0} + v_{j,0}} \right)^2 v_{ij}^2 \quad (2)$$

- (iii) Phase angle differences are small, i.e.,

$$\sin \theta_{ij} \approx \theta_{ij}, \cos \theta_{ij} \approx 1 - \frac{1}{2} \theta_{ij}^2 \quad (3)$$

Furthermore, the Taylor expansion of voltage and phase angle is carried out as follows:

$$\frac{1}{2} g_{ij} \theta_{ij}^2 \approx g_{ij} \theta_{ij,0} \theta_{ij} - \frac{1}{2} g_{ij} \theta_{ij,0}^2 \quad (4)$$

$$\begin{aligned} \frac{1}{2} g_{ij} \left( \frac{v_i + v_j}{v_{i,0} + v_{j,0}} \right)^2 v_{ij}^2 &\approx g_{ij} \frac{v_{i,0} - v_{j,0}}{v_{i,0} + v_{j,0}} (v_i^2 - v_j^2) \\ &- \frac{1}{2} g_{ij} (v_{i,0} - v_{j,0})^2 \end{aligned} \quad (5)$$

Here, we use the initial or the last moment state for the base conditions to fit the voltage  $v_{i,0}$ ,  $v_{j,0}$  and phase angle  $\theta_{ij,0}$ .

Combining equations from (1) to (5) formulates the simplified AC power flow model,

$$\begin{aligned} P_{ij} = g_{ij} \left( 1 + 2 \frac{v_{i,0} - v_{j,0}}{v_{i,0} + v_{j,0}} \right) &\left( \frac{v_i^2 - v_j^2}{2} \right) \\ &+ (g_{ij} \theta_{ij,0} - b_{ij}) \theta_{ij} - \frac{1}{2} g_{ij} [\theta_{ij,0}^2 + (v_{i,0} - v_{j,0})^2] \end{aligned} \quad (6)$$

where  $v_{i,0}$ ,  $v_{j,0}$  are the voltages and  $\theta_{i,0}$ ,  $\theta_{j,0}$  are the phase angles in base condition.

Equation (6) is more accurate compared with the traditional DC power flow model. However, voltage is still in a high power state, which cannot be integrated into linear programming in security constrained economic dispatch (SCED). In real-time market, the load fluctuation is generally small between time periods, as well as the voltage amplitude and phase angle fluctuations. So we choose the forecasting solution or the day-ahead market results to replace the voltage variable and simplify the phase angle terms by considering the characteristics. The approximation can be represented as,

$$(g_{ij} \theta_{ij,0} - b_{ij}) \theta_{ij} \approx -b_{ij} \theta_{ij} \quad (7)$$

$$v_i \approx v_{i,0}, v_j \approx v_{j,0} \quad (8)$$

Finally, the improved power flow model in real-time market can be expressed by,

$$\begin{aligned} P_{ij} = -b_{ij} \theta_{ij} + g_{ij} \left( 1 + 2 \frac{v_{i,0} - v_{j,0}}{v_{i,0} + v_{j,0}} \right) &\left( \frac{v_i^2 - v_j^2}{2} \right) \\ &- \frac{1}{2} g_{ij} [\theta_{ij,0}^2 + (v_{i,0} - v_{j,0})^2] \end{aligned} \quad (9)$$

Equation (9) has two parts. The first part is the traditional DC flow model formulated as  $-b_{ij} \theta_{ij}$ , and the second part can be regarded as a constant decided by the real-time grid state. For convenience, we name the second part the Taylor factor  $T_{ij}$ .

### B. PTDF correction

PTDF is the core of DCOPF defined as the ratio of the power flow distribution on each line to the total power flow injected into the network, which is derived from the traditional DC power flow model [26],

$$P_s = B \theta_s \quad (10)$$

$$P_s = M_{m,n} \cdot \omega \quad (11)$$

where  $P_s$  is the vector of node real power injections,  $B$  is the node susceptance matrix,  $\theta_s$  is the vector of node phase angles,

$M_{m,n}$  is the node-transaction incidence vector, and  $\omega$  is the value of transactions from node  $m$  to node  $n$ .

Combing (10) and (11) gives,

$$\theta_s = B^{-1} \cdot M_{m,n} \cdot \omega \quad (12)$$

Each branch power flow can be calculated by the difference of phase angles, which means,

$$P_{mn} = -b_{mn} M_l^T \theta_s \quad (13)$$

where  $M_l^T$  is the node-branch incidence vector.

Combing (12) with (13), the traditional PTDF on branch  $l$  from node  $m$  to  $n$  is,

$$PTDF_{m,n,l} = \frac{1}{x_l} M_l^T B^{-1} M_{m,n} \quad (14)$$

where  $x_l$  is the reactance on branch  $l$ .

Replacing equation (13) by (9), then the PTDF correction on branch  $l$  is given,

$$PTDF_{m,n,l}^C = PTDF_{m,n,l} + k \cdot C_l \quad (15)$$

where  $k$  is the scale factor,  $C_l$  is the PTDF correction factor defined as  $T/P_l$ ,  $T_l$  is the Taylor factor on branch  $l$ , and  $P_l$  is the power flow on branch  $l$ . The sign of  $C_l$  is related to the direction of the line flow, which is positive when the flow is in the same direction as the given positive direction, and negative when opposite.

Equation (15) is applicable to a single power flow injection. In the actual power grid, multiple power flows are injected into the network simultaneously. In this case, we further extend the model to the matrix form,

$$\Psi = \begin{bmatrix} \psi_1^{w_1} & \psi_1^{w_2} & \cdots & \psi_1^{w_N} \\ \psi_2^{w_1} & \psi_2^{w_2} & \cdots & \psi_2^{w_N} \\ \vdots & & \ddots & \\ \psi_L^{w_1} & & & \psi_L^{w_N} \end{bmatrix} \quad (16)$$

where  $\psi_l^w$  is the ratio of power flow in the  $l$ -th line to the  $w$ -th transaction injecting to the grid. Equation (16) represents the case with  $n$  power flows and  $l$  transactions in any network, and the corresponding PTDF can be calculated as follows,

$$\Psi = x_b^{-1} \begin{pmatrix} M_1^T \\ M_2^T \\ \vdots \\ M_L^T \end{pmatrix} B^{-1} (M_{w_1} \quad M_{w_2} \quad \cdots \quad M_{w_N}) + C \quad (17)$$

where  $x_b$  is the reactance matrix, and  $C$  is the correction factor matrix.

Quasi-steady-state sensitivity correction is also considered to overcome the shortcoming that traditional PTDF analysis cannot simulate the physical response of the actual power system [27],

$$PTDF^{CQ} = PTDF^C \cdot F_u \quad (18)$$

where  $F_u$  is the linearized coefficient matrix expressing the quasi-steady-state physical response of the control variable to system disturbance.

In the electricity market,  $F_u$  can generally be calculated as,

$$F_u = I - \alpha \cdot \mathbf{1}^T \quad (19)$$

where  $\alpha$  is the active power distribution factor determined by the output of each node usually,  $I$  is a unit matrix, and  $\mathbf{1}$  is a vector in which all the elements are 1.

### C. Marginal Line Losses Correction

Marginal line losses is a method to calculate the network losses without the square terms, which is reflected on each node through the loss distribution factor. Based on the above assumptions, the line losses is given as a multiplication of line resistance  $r_l$  and quadratic function of power flow  $P_l$ ,

$$loss = \sum_l r_l P_l^2 \quad (20)$$

In the improved power flow model approximation, nodal injections are related to real power flow by PTDF. The power flow  $P_l$  is determined as,

$$P_l = \sum_n PTDF_{n-l}^{CO} \times P_n \quad (21)$$

where  $P_n$  is the net load of the  $n$ -th node.

The loss factor defines the linear sensitivity of total system losses to real power injections in each node. Equation (21) leads to the following calculation for loss factor,

$$LF_n = 2 \sum_l r_l \cdot P_l \times PTDF_{n-l}^{CO} \quad (22)$$

The system marginal line losses can be given as,

$$loss = loss_0 + LF^T (P_g - P_d) \quad (23)$$

where  $loss_0$  is a constant calculated at the base point,  $P_g$  is the unit output vector and  $P_d$  is the demand vector.

## III. REAL-TIME MARKET CLEARING MODEL

Here, the piecewise linear approximation method is proposed to adapt to the characteristics of short time periods in RTM. The step current assumption is also presented to simplify the calculation. Then an iterative clearing algorithm and the real-time market clearing model with improved network constraints representation considering PTDF correction and DLR will be introduced.

### A. DLR in Real-Time Market

The safe and stable operation of the power grid is crucial in real-time market, which not only considers the maximum transmission capacity constraints, but also pays attention to whether the conductor temperature would cause potential thermal problems due to various weather conditions or peak load. The conductor temperature depends on 1) ambient temperature and weather conditions, 2) line current, and 3) conductor physical parameters, and the representative formula is the heat balance equation [28]. The HBE is composed of heat gain and heat loss. The heat gain consists of solar heat gain and Joule heat gain, while the heat loss is convective heat loss and radiated heat loss terms. It reflects the heat energy that enters, leaves and gets stored in the conductor per unit time, causing the temperature change [29]. Two types of HBE are derived, one is applied to the ‘Steady-state heat balance’,

$$q_c + q_r = q_s + q_j \quad (24)$$

and the other is applied to the ‘Non-steady-state heat balance’,

$$q_c + q_r + m \cdot C_p \cdot \frac{dT_s}{dt} = q_s + q_j \quad (25)$$

where  $q_c$  and  $q_r$  represent the convective and radiated heat loss rates respectively, the solar heat gain rate is expressed as  $q_s$  and  $q_j$  is the Joule heating, which can also be represented by line losses.  $T_s$  is the conductor surface temperature, restricted by the maximum allowable temperature in the power system operation,  $mC_p$  represents the total heat capacity of the conductor and  $dT_s/dt$  represents the time derivative of the conductor temperature.

Assuming that the steady-state current and temperature are given, when the current step occurs, it takes almost one hour for the conductor temperature to reach a new steady-state thermal balance with the 1-minute calculation interval. The temperature changes rapidly in the first tens of minutes, and climbs gradually during most of the remaining time. Therefore, in the entire period, the conductor temperature has the linear characteristic in the first ten minutes, which coincides with the short time periods in RTM.

In addition, DLR is highly dependent on weather conditions. The span lengths of conductors and corresponding ambient weather changes in DLR systems will affect the actual temperature of the conductors. The real-time status of the conductor needs to be dynamically monitored, including the adverse sagging, the wire tension and the angle of the wire cut by the wind in different weather. These accurate models will be critical to efficiently compute the dynamic line rating and provide reliable load ability information.

However, the real-time dispatch model, due to the limitation of short scheduling periods and complex calculations in the dispatch center of parameters such as sagging, the line tension and the line section angle, has to be simplified from the most rigorous dynamic line rating model. The dispatching center only needs to calculate the power flow of the system according to the transmission data to allocate the output of the unit. Therefore, we have conducted our study at the dispatch level and simplified the calculation of corresponding data in our model for practical engineering considerations in DCOFP. One real-time market time period is 15 minutes. Load data, bidding prices and weather conditions are provided to the dispatching center every time period. During the 15 minutes, the dispatch center will adjust network constraints based on the conductor temperature, which is calculated by the weather conditions across the line spans in each monitoring region and the expected current value. Starting from the initial state of the time period, the conductor temperature is calculated every minute. Then the conductor convection and radiant heat loss items are updated according to the calculated temperature every minute, while the solar energy and Joule heating gain remain unchanged. The temperature at the end of the time period will be obtained after iterating 15 times in this way.

According to the results, the conductor temperature presents an approximately linear trend within one time period in RTM. So the piecewise linear approximation method for the conductor temperature can solve the above problems. The

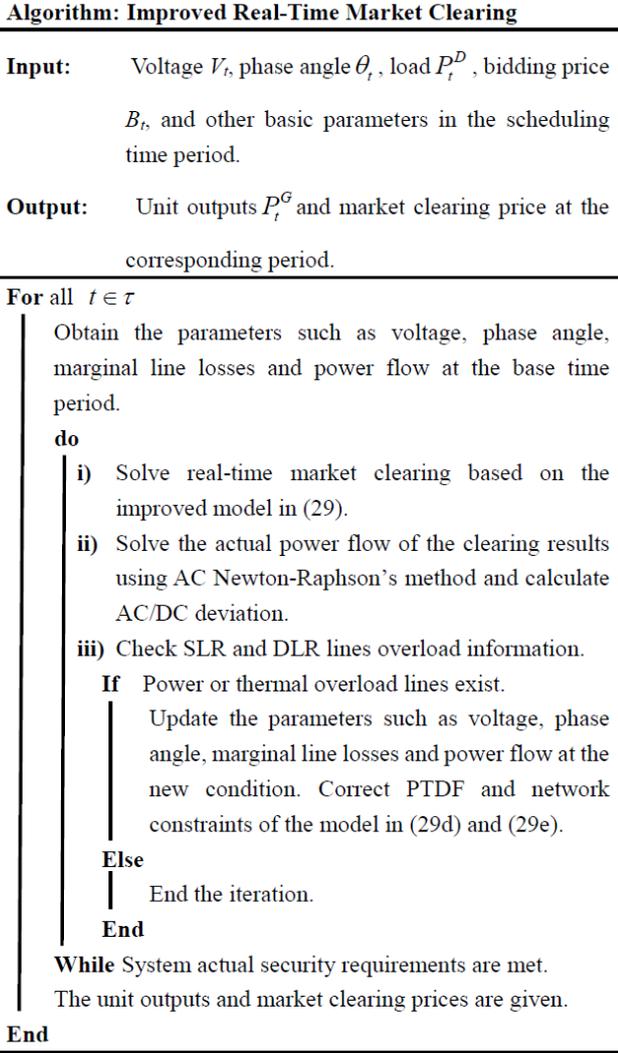


Fig. 1. Algorithm of the improved real-time market clearing model.

conductor temperature at the end of the time period can be expressed as,

$$T_{15} = T_0 + \left( \sum_{i=1}^U c_i l_i K \right) \cdot 15 \quad (26)$$

$$\sum_{i=1}^U c_i = 1 \quad (27)$$

where  $T_0$  is the conductor temperature at the initial moment,  $T_{15}$  is the conductor temperature in the 15-th minute,  $U$  is the number of segments divided by one time period,  $c$  is the coefficient corresponding to each segment,  $l$  is the length of each segment and  $K$  is the tangent of the temperature curve at the initial moment. It can be obtained by deriving the temperature function, or calculated by a physical expression:

$$K = \frac{(q_{j,0} + q_{s,0} - q_{c,0} - q_{r,0})}{m \cdot C_p (T_{s,0} - T_{a,0})} \quad (28)$$

where  $T_{a,0}$  is the ambient temperature at the initial moment. At the initial moment of each time period, parameters in (28) can be obtained through device observation. So  $K$  can be calculated before scheduling. By linearizing the HBE, we can calculate the

temperature at the end of the time period.

In addition, the age and loading induced failure of the lines with aleatory uncertainty and epistemic uncertainty, which is illustrated by the Arrhenius and Weibull models, are needed to be considered when our model is used in the power grid for a long time [30][31]. The failure rate of the existing lines should be calculated in RTM and the proportion of DLR applied in the system should be adjusted according to the desired expected-energy-not-served (EENS) value.

The accuracy of our model will also be affected by the cyber layer when a signal transmission interruption occurs. In order to address the issues, the cyber layer can be established to interface with the existing physical layer via phasor measurement units (PMU) deployment across the network, providing monitoring and protection functions for DLR and system integrity protection schemes (SIPS) implementation [32][33]. When weather data uncertainty occurs, the use of fuzzy sets in DTR calculations, known as Fuzzy-DTR-OTS (FDTR-OTS), is also an effective method to enhance network reliability [34].

### B. Improved Real-Time Market Clearing Model

The real-time market clearing model is summarized as follows:

$$\min \sum_{t=1}^{\tau} \sum_{j=1}^J B_{j,t}(P_{j,t}^G) \quad (29a)$$

$$\text{s.t. } P_t^G - P_t^D = \text{loss}_t, \quad \forall t \quad (29b)$$

$$\text{loss}_t = \text{loss}_{t,0} + LF^T \times (P_t^G - P_t^D), \quad \forall t \quad (29c)$$

$$PTDF^{CQ} \times (P_t^G - P_t^D - LD \cdot \text{loss}_t) + Pf_t^+ \leq P_k^{\max}, \quad \forall k \in Z, \forall t \quad (29d)$$

$$PTDF^{CQ} \times (P_t^G - P_t^D - LD \cdot \text{loss}_t) + Pf_t^- \leq -P_k^{\max}, \quad \forall k \in Z, \forall t \quad (29e)$$

$$T_{k,s,t} \leq T_t^{\max} \quad \forall k \in Z, \forall s \in S, \forall t \quad (29f)$$

$$P_{j,t}^{G \min} \leq P_{j,t}^G \leq P_{j,t}^{G \max}, \quad \forall j, \forall t \quad (29g)$$

$$-\Delta P_j^{GD} \leq P_{j,t}^G - P_{j,t-1}^G \leq \Delta P_j^{GU}, \quad \forall j, \forall t \quad (29h)$$

$$\Delta SR_t^U \leq \sum_{j=1}^J P_{j,t+1}^{G \max} - P_{j,t} \leq -\Delta SR_t^D, \quad \forall j, \forall t \quad (29i)$$

The cost objective function is minimized as (29a), in which  $B_j(\cdot)$  is the bidding price function of unit  $j$  and  $P_{j,t}^G$  is the output of unit  $j$  in time period  $t$ .  $j \in J$  is the index and set of units, and  $t \in \tau$  is the index and set of time periods. Load balance is established by (29b), and marginal line losses is calculated by (29c), in which  $P_t^G$  and  $P_t^D$  are the unit output vector and load demand vector in nodes respectively. The power flow are constrained by (29d) and (29e), where  $k \in Z$  is the index and set of network lines.  $PTDF^{CQ}$  is the PTDF correction matrix of the grid, and  $LD$  is the vector of loss distribution factors.  $Pf^+$ ,  $Pf^-$  are the dynamic line constraints for positive and negative trends, respectively, and  $P_k^{\max}$  is the maximum transmission capacity of the  $k$ -th line.  $s \in S$  is the index and set of regions. The

TABLE I  
DEFINITION OF THE FOUR METHODS

Method	Definition
SLR	traditional DCOPF method with static line rating
SLR-L	DCOPF method considering marginal line losses with static line rating
SLR-C	DCOPF method considering PTFDF correction, marginal line losses and iteration with static line rating
DLR-C	DCOPF method considering PTFDF correction, marginal line losses and iteration with dynamic line rating

maximum allowable conductor temperature limits at time period  $t$  are given by (29f), which is determined by the worst weather conditions across the conductor span. Active power limits are imposed by (29g), where  $P_{j,t}^{Gmin}$ ,  $P_{j,t}^{Gmax}$  are the minimum and maximum output of unit  $j$  in time period  $t$ . Unit output are constrained by ramp-up rates as well as by ramp-down rates (29h), where  $\Delta P_i^{GU}$ ,  $\Delta P_i^{GD}$  are the ramp-up limit and ramp-down limit of the unit  $j$ . Equation (29i) gives the spinning reserve constraints, in which  $\Delta SR_t^U$ ,  $\Delta SR_t^D$  are the spinning-up reserve requirement and spinning-down reserve requirement in time period  $t$ .

Based on the theory derived from Section II, SCED for power systems can be implemented by the improved real-time market clearing method as illustrated in Fig.1. The parameters will be updated and iterated during the whole clearing process in real time until the system actual security requirements calculated by AC method are met. In the initial operation, the amount of calculation will be relatively large. In subsequent operations, the calculation time will be reduced due to the little difference between the parameters of adjacent time periods.

Compared with existing clearing models, the network constraints in our model are improved by (29d)-(29f) during the iteration to increase the line utilization rate. PTFDF correction increases the accuracy of clearing results through the improved power flow model in RTM, and fast-calculated dynamic line rating adjusts the maximum transmission capacity flexibly according to various weather conditions.  $P_f^*$ ,  $P_f$  are also applied into clearing to further reduce the AC/DC deviation.

#### IV. CASE STUDY

The proposed method has been implemented in three different independent systems, which are the IEEE 39-bus system, the IEEE 2383-bus system and the real-world power system in Yunnan province of China. Four methods are compared to illustrate the gap between the models, which are SLR, SLR-L, SLR-C and DLR-C shown in TABLE I. To evaluate the effectiveness of the proposed method, this section is divided into two parts. The first section tests the improvement in reducing AC/DC deviation using PTFDF correction. The second section shows the further impact and promotion of SLR-C using dynamic line rating.

##### A. Test of PTFDF correction

Three independent systems are used to illustrate the effect of

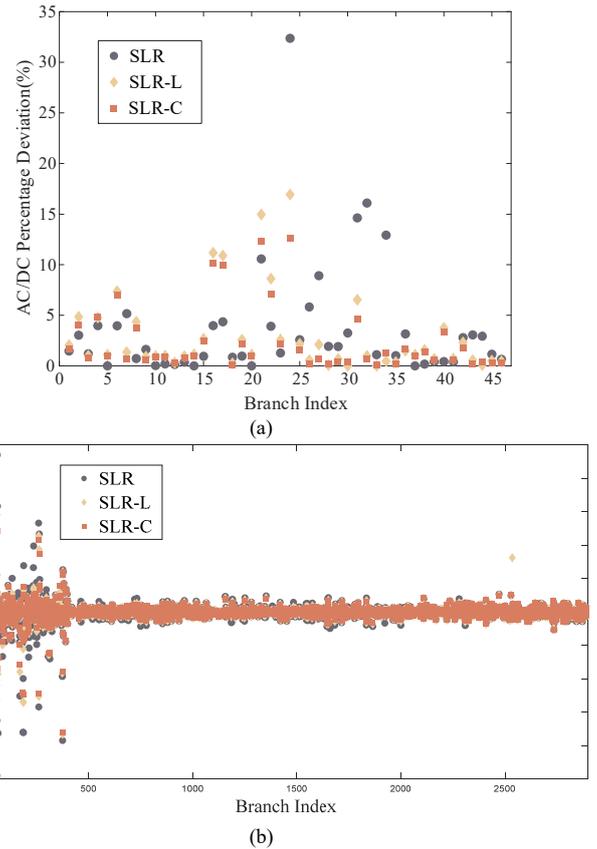


Fig. 2. AC/DC deviation comparison in peak time period among SLR, SLR-L and SLR-C. (a) AC/DC percentage deviation in Case I; (b) AC/DC deviation in Case II.

reducing AC/DC deviation, and curves all refer to the real daily operation of Yunnan province in China on a typical day. The cases are chosen as follows:

- Case I: IEEE 39-bus system with actual data in Yunnan
- Case II: IEEE 2383-bus system with actual data in Yunnan
- Case III: the real power system in Yunnan province of China

The 39-bus system consists of 39 nodes and 46 branches, among which the thermal generators are set up at 30~39 nodes with reference node 31. The IEEE 2383-bus system has 2383 nodes and 2896 lines. Compared to Case I, this system has more complete node line mapping similar to the real-world system, which contains multi-energy power generators. The real power grid system in Yunnan province contains 1691 nodes, 2149 lines or sections and 387 multi-energy power generators including large-scale cascade hydropower stations, runoff hydroelectric power stations, thermal power, wind power and photovoltaics.

We calculate real-time market clearing at 96 time periods in a single day based on model predictive control in given network constraints, and then make corresponding comparisons for the AC/DC deviation and line utilization rate. Two time dimensions are analyzed to compare the four methods, which are the single time period and total time period, respectively.

1) *Single time period*: We choose a typical time period in 96 time periods for the AC/DC deviation analysis, which is the peak load time period in the 68-th point. In the period, AC/DC deviation comparison in branches has been illustrated in Fig. 2.

TABLE II

PARAMETERS OF THE PEAK TIME PERIOD IN IEEE CASE SYSTEMS				
Case	Method	Variance (MW)	Maximum Deviation (MW)	Total Deviation (MW)
I	SLR	503.68	100.93	531.52
	SLR-L	17.02	14.81	273.58
	SLR-C	11.33	11.25	227.45
II	SLR	36.790	97.800	6352.3
	SLR-L	18.170	73.076	5171.7
	SLR-C	14.844	71.884	4901.9

TABLE III

RELATIVE AC/DC DEVIATION (%) IN TYPICAL LINES OF THE WHOLE DAY IN YUNNAN PROVINCE

Case	Line Name	SLR	SLR-L	SLR-C
I	The BaoJiu II line	6.8053	4.7591	3.9477
	The Duohong III line	17.4400	13.1393	10.0995
	The Tongda III line	16.0383	14.8433	13.0608
III	The Wenkai I line	8.9912	8.1353	7.8487
	The Daxia I line	7.1547	5.6480	5.0410

In most of lines, the deviations of SLR-L and SLR-C have been reduced to varying degrees compared to SLR while some increased for the power flow redistribution. SLR-L performs better than SLR generally. Among them, SLR-C is the most accurate method.

In addition, the variance, maximum AC/DC deviation and total AC/DC deviation of lines decrease in turn by comparing the three methods. In Case I, the variances are 503.68, 17.02 and 11.33, the maximum AC/DC deviations are 100.93MW, 14.81MW and 11.25MW, and the total deviations are 531.52MW, 273.58MW and 227.45MW, corresponding to SLR, SLR-L and SLR-C, respectively. In Case II, the variances are 36.790, 18.170 and 14.844, the maximum AC/DC deviations are 97.800MW, 73.076MW and 71.884MW, and the total deviations are 6352.3MW, 5171.7MW and 4901.9MW, corresponding to SLR, SLR-L and SLR-C, respectively. By contrast, SLR is the worst, SLR-L is relatively better, and SLR-C is the best. The detailed data is shown in TABLE II.

2) *Total time period*: Apart from the peak load time period, the operation of the whole day is also worthy of attention. Thus, we further analyze AC/DC deviation throughout 96 time periods. The AC/DC deviation of each time period is added by the AC/DC deviation in each branch at the time period, and all parameters are the sum of clearing data of 96 time periods.

We analyze the total AC/DC deviation among SLR, SLR-L and SLR-C. As shown in Fig. 3, the deviation and the load curve have roughly the same trend, with a smaller value at valley load and a larger value at peak load. In Case I, the deviation of the whole day in SLR is relatively large, with a total value of 41942.37MW, accounting for 5% of the daily output. SLR-L makes up for the inaccuracy of DCOPF, optimizes the scheduling results, and reduces the overall AC/DC deviation to 21657.78MW. On this basis, SLR-C further reduces the AC/DC deviation to 17545.53MW. In the total time period, the AC/DC deviation in SLR is relatively large, with a total value of 503526.1776MW. SLR-L reduces the overall AC/DC deviation

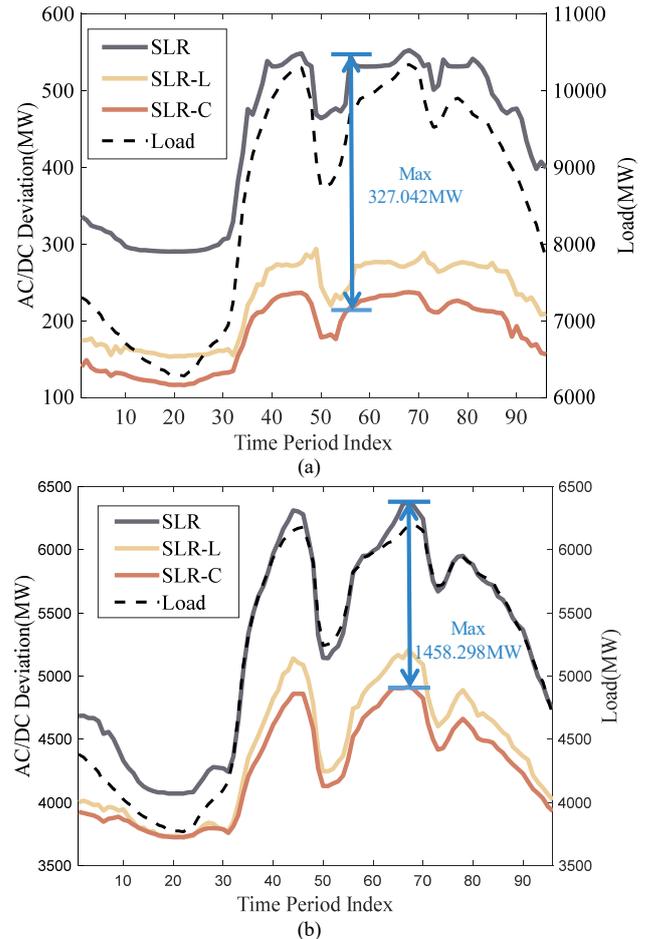


Fig. 3. Total AC/DC deviation of the daily operation among SLR, SLR-L and SLR-C. (a) Parameters in Case I; (b) Parameters in Case II.

to 422430.3812MW. On this basis, SLR-C further reduces the AC/DC deviation to 413260.5167MW, where the scheduling accuracy of the whole day is improved by about 2% compared to SLR-L. In Case II, the AC/DC deviation in SLR is 503526.1776MW. SLR-L reduces the overall AC/DC deviation to 422430.3812MW. SLR-C further reduces the AC/DC deviation to 413260.5167MW, where the scheduling accuracy of the whole day is also improved by about 2% compared to SLR-L. The detailed data is shown in Fig. 3. Therefore, in the daily dimension, SLR-C is still the best choice with an average 2% promotion in SLR-L.

Furthermore, we have conducted the simulation in the real-world electricity power market environment in Yunnan province. The load data, the wind and the photovoltaic output of a typical day from the actual power system in Yunnan are employed to justify the effectiveness. Considering that its actual power flow needs to be kept confidential, here we will show the statistical data in the typical lines.

The Baojiu II line, the Duohong III line, the Tongda III line, the Wenkai I line and the Daxia I line are used for analysis, which carry important transmission tasks and often cause network congestion. The data are shown in TABLE III in detail. The results show that the relative deviations of SLR-L and SLR-C have been significantly reduced compared to SLR in the five typical lines. SLR-L performs better than SLR generally

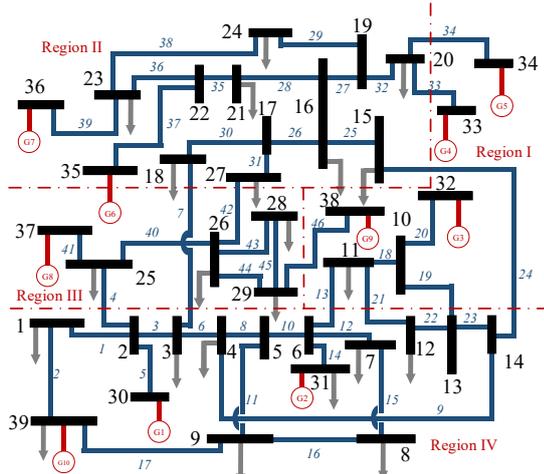


Fig. 4. Power grid topology of the 39-bus system.

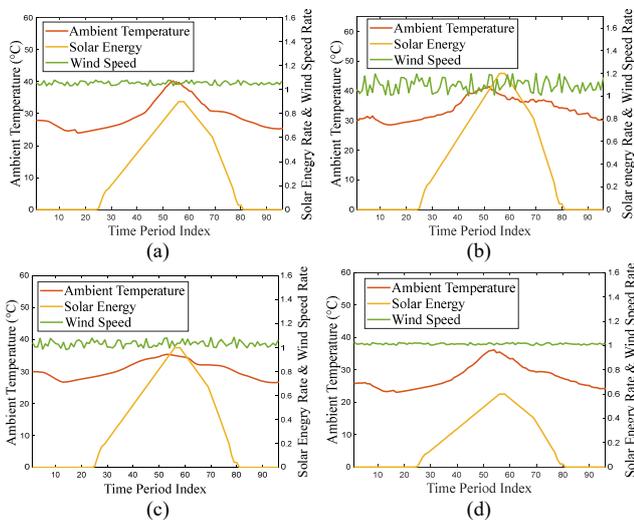


Fig. 5. Ambient temperature and weather conditions. (a) Parameters in Region I; (b) Parameters in Region II; (c) Parameters in Region III; (d) Parameters in Region IV.

with an average of 3% promotion. SLR-C further reduces the relative AC/DC deviation with an average of 2% improvement. The SLR-C solution performs best on The Duohong III line, where the relative AC/DC deviation is reduced by 7.3% lower than that of the traditional DCOPTF. SLR-C can effectively reduce the dispatch margin of these lines due to congestion, thereby improving grid security, which is the most accurate method in the actual real-time electricity market operation of Yunnan province.

### B. Impact of dynamic line rating based on SLR-C

Here the 39-bus system is used for simulation. It is further geographically divided into four areas (Region I-IV) and then sectionalized with respect to different stations, which is shown in Fig. 4. The monitoring stations for weather conditions have been set in each area and transmit data continuously to the dispatching center in real time. The data transmitted to the dispatching center is assumed to be the actual value.

Assuming that the system is stable at 0:00, the calculation interval of the heat balance equation is selected as 1 minute. The temperature is measured every 15 minutes as one period in real-

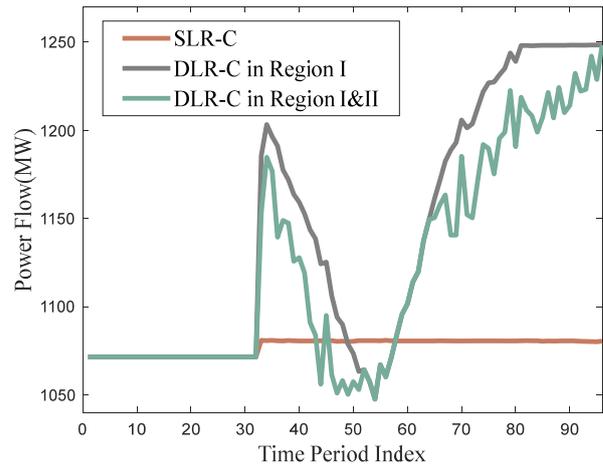


Fig. 6. Power flow in the 33-rd line between SLR-C and DLR-C.

time market. The ambient temperature and weather conditions in each region are shown in Fig. 5. The ambient temperature fluctuates around 30°C, which is low in the morning and evening, while high at noon. Solar energy starts to rise at about 6 am, reaches its peak at about 1 pm, and then decreases until disappears at about 8 pm. The wind speed rate fluctuates randomly with a reference of 0.61m/s perpendicular to the conductor. Al-St hinged conductor is used for analysis, and the maximum allowable conductor temperature of this material wire is 100 degrees Celsius.

The 33-rd line is one of the most important transmission lines, which spans Region I and Region II. Hence, its DLR will be determined by the worst weather conditions in the two areas. We conducted a comparison of the power flow in the 33-rd line between the two cases. The first is to ignore the line spans and their surrounding weather conditions, and the system is only in the weather conditions shown in Region I. The second takes into account line spans and surrounding weather changes, where the system is geographically divided into four regions and the 33-rd line passes through Region I&II. The result shows that the power flow in the 33-rd line reduced after considering the conductor span and weather conditions, as shown in Fig. 6.

Meanwhile, we analyze the relatively conservative dispatch margin reserved. We illustrate the issue by comparison of power flow changes in the 33-rd line between SLR-C and DLR-C. The 33-rd line is selected because its power flow is the largest, creating the most Joule heating. During peak load periods at noon and evening, the conductor temperature reaches the highest point. In SLR-C, under the given network constraints of the power grid and weather conditions, the temperature variation of the third branch is calculated iteratively by HBE. The maximum transmission capacity of the 33-rd line is formulated according to the critical temperature limit. Therefore, its power flow constraint can only be limited to about 1080MW throughout the day, even if the temperature decreases at night. When we introduce DLR into real-time market through the piecewise linear approximation method, the power flow has been greatly improved. As the temperature decreases, the power flow gradually increases, and finally reaches about 1250MW, making full use of the maximum

TABLE IV  
COMPARISONS OF LINE AVERAGE UTILIZATION RATE

Line Average Utilization Rate (%)	Maximum Transmission Capacity (MW)	SLR	SLR-L	SLR-C	DLR-C
5-th	1100	75.781	77.393	77.595	78.052
14-th	900	86.715	88.307	88.684	89.622
33-rd	1250	79.407	83.371	86.133	89.946
46-th	1000	84.449	85.810	86.239	90.073

transmission capacity, which is also illustrated in Fig. 6. In addition, the results indicate that power flow increments presented in Fig. 6 may not be positive in some rare cases for the consideration of grid security. At these moments, due to the harsh weather condition, the dynamic line rating is in fact lower than its static line rating value.

We further select four lines with heavier power flow and higher conductor temperature in the system to analyze the line utilization rate, which are the 5-th, the 14-th, the 33-rd and the 46-th lines, respectively. We calculated the line average utilization rate of 96 points in the four methods and the detailed data is shown in TABLE IV. The data proves that the line average utilization rate increases gradually in four methods. SLR is the lowest and SLR-L is better with about 2% promotion. Compared with SLR-L, SLR-C improves the line average utilization rate with 0.2~3% promotion. DLR-C further increases the line utilization rate by dynamic line rating based on SLR-C with an average of 2.3% promotion, which is the highest among all methods.

## V. CONCLUSION

In this paper, a real-time power market clearing model with improved network constraints considering PTDF correction and fast-calculated DLR is proposed. The PTDF correction derived from the improved power flow model in RTM is proposed first. The mathematical model is formulated based on Taylor expansion with voltage and phase angle approximation from the AC power flow model. Quasi-steady-state correction and marginal line losses correction are applied into the clearing model further. Meanwhile, dynamic line rating has been integrated into RTM by piecewise linear approximation method to calculate real-time conductor temperature faster, which adapts to the short time periods. Compared to SLR, the maximum transmission capacity can be adjusted according to the ambient temperature and weather conditions changes in RTM when using DLR.

PTDF correction improves the accuracy of power flow distribution and dynamic line rating further reduces the relatively conservative dispatch margin. Both improved methods can regulate network constraints dynamically to fit the instantaneous changes in RTM. Thus, the proposed model increases the line utilization rate and ensures the safe operation of the power grid. The clearing model can also improve the renewables accommodation effectively due to the accuracy in power dispatch and the adaptability to power fluctuations, which upgrades overall social welfare. More refined models

and adaptability to complex systems with various weather conditions will be analyzed in future work.

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