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Dynamics of an Interacting Particle System: Evidence of Critical Slowing Down

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The dynamics of a magnetic particle system consisting of ultrafine Fe-C particles of monodisperse nature has been investigated in a large time window, 10^{-9} – 10^4 s, using Mössbauer spectroscopy, ac susceptibility, and zero field cooled magnetic relaxation measurements. By studying two samples from the same dilution series, with concentrations of 5 and 6×10^{-3} vol %, respectively, it has been found that dipole-dipole interaction increases the characteristic relaxation time of the particle system at all temperatures investigated. The results for the most concentrated particle assembly are indicative of collective magnetic dynamics and critical slowing down at a finite temperature, $T_g \approx 40$ K. Close to and below the transition temperature, an aging phenomenon is observed, another manifestation of collective magnetic dynamics. [S0031-9007(97)04826-6]

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The dynamics of magnetic nanoparticle systems is currently a subject of considerable interest. In a noninteracting particle assembly the superparamagnetic relaxation time essentially follows the predictions of the Néel-Brown theory [1,2], implying relaxation times from picoseconds to geological time scales depending on the magnetic anisotropy, the particle volume, temperature, and applied magnetic field. Different approximate expressions for the relaxation time of noninteracting-particle systems [2,3] have been derived. Several experimental studies support the validity of the theoretical models [4–6].

In particle assemblies with significant dipole-dipole interaction the magnetic relaxation is known to be affected by the interaction. Ac susceptibility and dc magnetization measurements indicate an increase in the characteristic relaxation time with increasing interaction strength [7–10], while Mössbauer results in some cases indicate the opposite behavior [11,12]. Different and conflicting models have been proposed to explain the experimental results [7,11,13,14]. In most cases, these models address the question of what happens to the energy barrier of the individual particle magnetic moment as the interaction strength increases and less attention is given to the more complex problem of having collective dynamics contributing to the observed magnetic relaxation. If collective particle behavior is an essential ingredient in an interacting particle assembly, it may be possible that a phase transition to a super spin-glass phase occurs at a finite temperature, since such a system exhibits both random and frustrated magnetic interactions.

In this Letter, Mössbauer, ac susceptibility, and zero field cooled (ZFC) magnetic relaxation measurements have been performed to study the dynamics of a nanoparticle system of nearly monodisperse nature. By studying two samples with different concentrations of magnetic particles, both taken from the same batch of ferrofluid,

the effects of dipole-dipole interaction on the magnetic dynamics have been scrutinized. For the first time, it is found that the dynamics of a concentrated nanoparticle sample displays critical slowing down at a finite temperature, reminiscent of the critical behavior observed in spin-glass materials [15]. Close to and below the critical temperature, the magnetic relaxation displays an aging phenomenon, giving further support for a low temperature super spin-glass phase in the concentrated particle system.

The experiments were performed on two samples consisting of nanosized particles of amorphous $\text{Fe}_{1-x}\text{C}_x$ with $x \approx 0.22$. The particle system was prepared as a ferrofluid by thermal decomposition of $\text{Fe}(\text{CO})_5$ in decalin using oleic acid as a surfactant. The details of the preparation technique are described in Ref. [16]. After preparation, the ferrofluid was up-concentrated and different concentrations were prepared by dilution of the concentrated product. The nominal concentrations of the samples used in this study were $\epsilon = 5$ and $\epsilon = 6 \times 10^{-3}$ vol %, respectively.

The concentrated sample was studied by transmission electron microscopy (TEM). These studies [17] showed a close to spherical particle shape and that there is no significant tendency of particle agglomeration. The volume weighted particle size distribution as seen in TEM fitted well to a log-normal distribution with a remarkably narrow width of $\sigma_V = 0.22$ and a median volume of $V_m = 5.3 \times 10^{-26} \text{ m}^3$ ($d_m \approx 4.7 \text{ nm}$) [17].

All measurements were performed at low temperatures with the carrier liquid frozen, implying that the particles were fixed randomly in the sample. Since the frozen carrier liquid provides an insulating matrix for the magnetic particles and since the particles are coated with a surfactant layer preventing the particles from agglomerating, the interparticle magnetic interaction is of dipole-dipole type. Assuming a homogeneous dispersion, the mean

interaction energy between two neighboring particles can be estimated from $E_{d-d}/k_B = (\mu_0/4\pi k_B)M_s^2 V_m \epsilon$, where M_s is the saturation magnetization of the $\text{Fe}_{1-x}\text{C}_x$ particles. Using the low temperature value of the saturation magnetization, $M_s \approx 1.5 \times 10^6$ A/m, this expression gives $E_{d-d}/k_B = 44$ K and $E_{d-d}/k_B = 0.05$ K for the concentrated and dilute samples, respectively.

A specially designed SQUID magnetometer [18] was used for the ac susceptibility and the magnetic relaxation measurements. The magnitude of the ac fields were $h_{ac} = 5$ mOe and $h_{ac} = 0.1$ Oe for the concentrated and dilute samples, respectively. The covered ac frequency ranges were $17 \text{ mHz} \leq \omega/2\pi \leq 51 \text{ kHz}$ for the concentrated sample and $17 \text{ mHz} \leq \omega/2\pi \leq 5.1 \text{ kHz}$ for the dilute sample.

The dynamics of the particle assemblies was also studied by ZFC magnetic relaxation measurements. In the ZFC experiments the sample was cooled in zero field from a high temperature where the sample showed a superparamagnetic behavior. When reaching the measurement temperature, T , the sample was equilibrated a wait time t_w before a weak magnetic field was applied and the magnetization, $M(T, t)$, recorded in the time window $3 \times 10^{-1} < t < 10^4$ s after the field application. The fields used were $h = 1$ Oe and $h = 10$ Oe for the concentrated and dilute samples, respectively. The Mössbauer data were collected using a ^{57}Co source in a Rh matrix.

The ac susceptibility measurements cover observation times ($1/\omega$) ranging from 3×10^{-6} to 10 s. By use of ZFC relaxation measurements it is possible to extend the experimentally accessible observation time window to longer time scales. The results from ac susceptibility and ZFC relaxation measurements are related by [19]

$$M(T, t)/h = \chi(T, t) \approx \chi'(T, \omega) \quad (1)$$

with $t = 1/\omega$. In Fig. 1(a), $\chi(T, t)$ and $\chi'(T, \omega)$ are plotted for the concentrated sample. The low temperature behavior of the equilibrium susceptibility, $\chi_{eq}(T)$, is drawn, extrapolating the high temperature behavior of the $\chi(T)$ curves which in the temperature region 48 to 100 K obey a Curie-Weiss law, $\chi = 0.62/(T + 11.40)$ [emu/Oe]. The out-of-phase component of the ac susceptibility, $\chi''(T, \omega)$, is shown in Fig. 1(b). The corresponding results for the dilute sample has, for comparison, been included in this figure. In accordance with observations made on other systems [7–10], the characteristic frequency dependence of the ac susceptibility is shifted toward higher temperatures for the interacting sample. It is obvious from this figure that at temperatures near the peaks of $\chi''(T)$ for the concentrated sample the corresponding out-of-phase components of the dilute sample remain virtually zero, indicating that the characteristic relaxation times, τ , of the dilute sample at these temperatures are much shorter than the time scale of the ac susceptibility experiment, $\tau \ll 1/\omega$. Such a clear separation between the characteristic relaxation times of a concentrated and a dilute sample, taken from the same

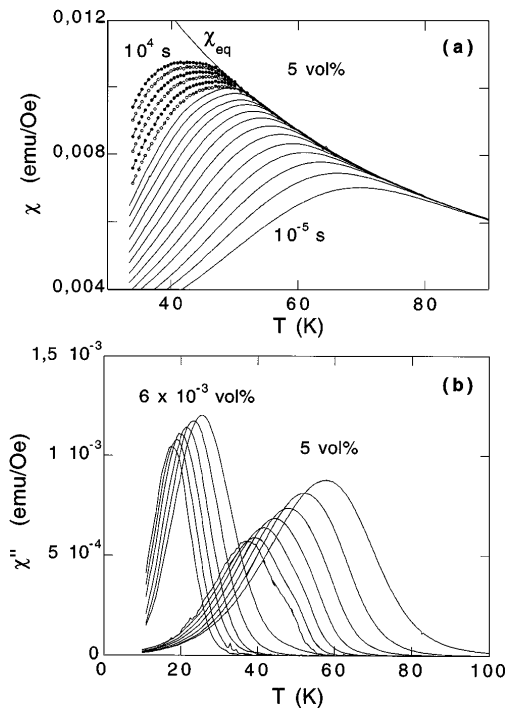


FIG. 1. (a) $\chi'(T, \omega)$ (solid lines) and $\chi(T, t)$ (symbols) vs temperature for the 5 vol% sample. The different curves correspond to different observation times $t = 1/\omega$ (top to bottom): 10^4 , 3×10^3 , 10^3 , 3×10^2 , 10^2 , 30, 10, 3, 1, 3×10^{-1} , 10^{-1} , 3×10^{-2} , 10^{-2} , 3×10^{-3} , 10^{-3} , 3×10^{-4} , 10^{-4} , 3×10^{-5} , and 10^{-5} s. (b) $\chi''(\omega)$ vs temperature for the 5 and 6×10^{-3} vol% samples. The results of the noninteracting sample has been multiplied by the ratio between the concentrations of the two samples. The different curves correspond to different observation times 10, 1, 10^{-1} , 10^{-2} , 10^{-3} , 10^{-4} , and 10^{-5} s for the 5 vol% sample, and 10, 10^{-1} , 10^{-2} , 10^{-3} , and 10^{-4} s for the 6×10^{-3} vol% sample.

batch of magnetic nanoparticles, has not been reported previously.

A method, which aims at studying the temperature dependence of the longest relaxation time of the magnetic system, focuses on small departures of the $\chi(T, t)$ curves from the equilibrium susceptibility curve. The relaxation time τ equals t and the corresponding temperature is found from the ratio $\chi(T, t)/\chi_{eq}$, which should be set to a fixed value close to 1 [20]. In Fig. 2, the relaxation time, as defined from the condition $\chi(T, t)/\chi_{eq} = 0.98$, is plotted versus temperature for the concentrated sample. The corresponding results of the Mössbauer experiments are also plotted. The latter results were obtained by measuring the count rate at zero velocity as a function of temperature. In this way one can estimate a temperature at which essentially all particles have a relaxation time faster than about 5×10^{-10} s [21]. This time scale corresponds to the onset of a broadening of the superparamagnetic component. The relaxation times for the dilute sample have been included for comparison. The dashed line corresponds to the result of fitting a Vogel-Fulcher law to the temperature dependence of the relaxation time of the

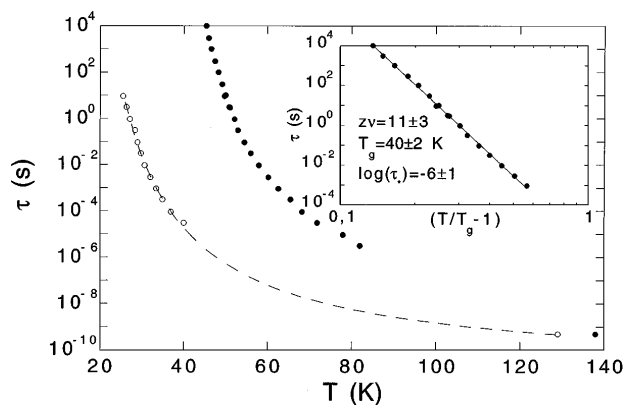


FIG. 2. Relaxation time vs temperature for the 5 vol % (filled symbols) and 6×10^{-3} vol % (open symbols) samples. The dashed line was obtained by fitting a Vogel-Fulcher law to the results of the dilute sample. The inset shows the critical slowing down analysis made for the concentrated sample using relaxation time data corresponding to the temperature interval 45–65 K.

dilute sample, $\tau = 1.4 \times 10^{-11} \times \exp[420/(T - 10.2)]$ s. Fitting an Arrhenius law to the same experimental data yields too small a value for the microscopic relaxation time τ_0 , which indicates that even this sample displays some interparticle interactions. This suggests that the dilute sample is not completely homogeneous and that there exists small agglomerates of particles in this sample.

To investigate if the dynamics of the concentrated sample shows critical slowing down, one can make use of the dynamic scaling hypothesis, which states that the characteristic relaxation time close to the transition temperature is related to the particle-particle correlation length, ξ , according to $\tau \propto \xi^z$. Since the correlation length diverges at the transition temperature, the relaxation time is expected to obey the temperature dependence [22]

$$\tau = \tau_*(T/T_g - 1)^{-z\nu}, \quad T > T_g, \quad (2)$$

where T_g is the transition temperature, τ_* is related to the relaxation time of the individual particle magnetic moments, and $z\nu$ is a critical exponent. The result of the analysis, using data corresponding to the temperature range 45–65 K, is shown in the inset of Fig. 2. The value of $z\nu = 11 \pm 3$ is in good agreement with values derived for spin-glass materials [15]. The value of $\tau_* = 10^{-6}$ s may seem too large when compared to values derived for spin glasses. However, in spin glasses τ_* is determined by the spin flip time of the atomic magnetic moments ($\approx 10^{-13}$ s), while τ_* in a magnetic particle system is determined by the flip time of the noninteracting particle magnetic moments, which essentially should follow a temperature dependence as that shown in Fig. 2 for the relaxation time of the dilute sample. Consulting this figure, it is seen that the value extracted for τ_* from the critical scaling analysis is in accordance with the relaxation times of the dilute system in the temperature region used for the scaling analysis. The success of fitting a Vogel-Fulcher law to the temperature dependence of the relaxa-

tion time of the dilute sample indicates some influence of interparticle interaction even for this sample. This effect, however, should not, in the temperature range used for the scaling analysis, significantly change the relaxation times of the dilute sample from that of a perfectly noninteracting sample. Neglecting the temperature dependence of τ_* in the dynamic scaling analysis probably yields slightly too large a value for the exponent $z\nu$. The error introduced by this is, however, smaller than the margins of error given above for extracted value of the critical exponent. Also, it is worth noting that using the maxima in the $\chi''(T, \omega)$ curves to determine the temperatures corresponding to different observation times $1/\omega$, yield, within the experimental uncertainty, the same values of $z\nu$ and τ_* as those given above.

The temperature dependence of the characteristic relaxation time of a spin glass can also be obtained from the frequency dependence of $\chi''/(\omega\chi')$. It can be shown that the following relation holds [22,23]

$$\chi''/\omega\chi' \propto \tau^{1-\beta/z\nu} \propto (T/T_g - 1)^{-z\nu+\beta},$$

$$\omega\tau \rightarrow 0, \quad (3)$$

where β is the order parameter critical exponent, which for spin-glass materials typically takes a value in the range 0.6–0.8 [20]. In the zero frequency limit, the left-hand side of Eq. (3), for each temperature, attains a frequency independent value related to the characteristic relaxation time of the magnetic system. Figure 3 shows $\chi''/(\omega\chi')$ vs $\omega/2\pi$ for the concentrated sample. In the low frequency limit and at a given temperature it can be seen that $\chi''/(\omega\chi')$ approaches a frequency independent value. Fitting the values thus extracted to the power-law divergence in Eq. (3) gives, using $T_g = 40$ K, $z\nu - \beta = 10.4$. Assuming the critical exponent β for the interacting particle system to take a value close to that of archetypal spin glasses, this result is in good agreement with the result of the previous scaling analysis.

The ZFC relaxation rate, $S = 1/h \times \partial M / \partial \ln(t)$, for the concentrated sample is displayed in Fig. 4 for the

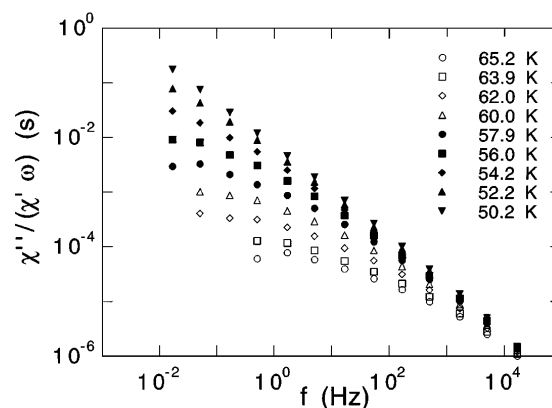


FIG. 3. $\chi''/\omega\chi'$ vs $\omega/2\pi$ at different temperatures for the 5 vol % sample.

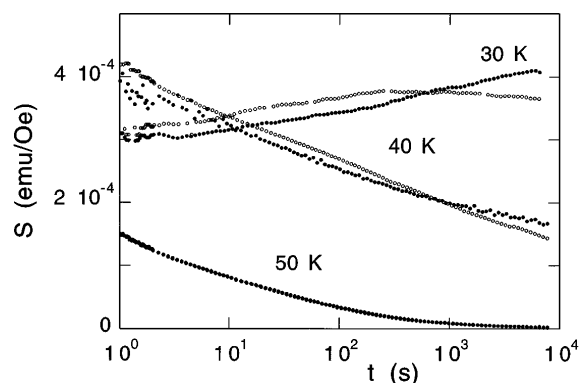


FIG. 4. Relaxation rate S vs time at the temperatures 30, 40, and 50 K for the 5 vol % sample. The wait time t_w at constant temperature before applying the probe field was 10^2 s (open symbols) and 10^4 s (filled symbols).

temperatures 30, 40, and 50 K. At each temperature, the time dependence of the ZFC magnetization has been recorded using two different wait times, $t_w = 10^2$ s and $t_w = 10^4$ s. At and below the extracted transition temperature, a wait time dependence of the relaxation rate is observed. At $T = 50$ K, the wait time dependence cannot be resolved in the experimental time window. This behavior is similar to the behavior observed in spin-glass materials [20], where at temperatures below the spin-glass temperature, the ZFC relaxation displays a clear wait time dependence, while at temperatures higher than this temperature the wait time dependence vanishes in the experimental wait time and observation time windows. The effect of the wait time on the magnetic relaxation seen in Fig. 4 is of the same magnitude as that observed for an interacting maghemite sample in Ref. [9]. It is worth pointing out, however, that the wait time dependence of the magnetic relaxation is weaker in the magnetic particle systems as compared to that of an archetypal spin glass [20].

It has been shown that in this nearly monodisperse system of magnetic nanoparticles we are able to clearly separate the relaxation of the particles in the dilute sample, primarily governed by the anisotropy energy barrier, from effects induced by magnetic interparticle interactions. In a range of temperatures and time scales we have observed that the magnetic relaxation in the concentrated sample is governed by collective particle dynamics. The collective behavior has been evidenced by (i) critical slowing down of the dynamics at a finite temperature $T_g \approx 40$ K and (ii) the appearance of magnetic aging at low temperatures, thus giving evidence of a low temperature super spin-glass phase.

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