Single-mode regime in large-mode-area rare-earth-doped rod-type PCFs

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Abstract—In this paper, large-mode-area, double-cladding, rare-earth-doped photonic crystal fibers are investigated in order to understand how the refractive index distribution and the mode competition given by the amplification can assure single-mode propagation. Fibers with different core diameters, i.e., 35, 60, and 100 μm, are considered. The analysis of the mode effective index, overlap, effective area, gain, and power evolution along the doped fiber provides clear guidelines on the fiber physical characteristics to be matched in the fabrication process to obtain a truly or effectively single-mode output beam.

Index Terms—Photonic crystal fibers (PCFs), rare-earth-doped fibers, rod-type fibers, single-mode regime.

I. INTRODUCTION

HIGH- and medium-power applications of fiber lasers are gaining interest day by day in many different fields ranging from spectroscopy to medicine, from monitoring and sensing to micromachining and material processing [1]. The well-established fiber and doped fiber technology is one of the keys to this success. In particular, rare-earth-doped double-cladding (DC) fibers [2], made as step-index fibers with a polymer outer cladding, are usually exploited for these kinds of applications. Recently, the advent of photonic crystal fibers (PCFs) with their novel optical properties [3] has further boosted the process. Large-mode area (LMA) DC PCFs, usually called air-clad fibers, seem to be particularly promising [4]–[6]. In these fibers, the LMA structure, with a doped core in a photonic crystal inner cladding, is placed inside an air-clad pump guide, characterized by a ring of large air holes. A very high numerical aperture is provided for the pump core/outer cladding, thus allowing efficient coupling of light from inexpensive high-power pump diodes having a poor beam quality. The main advantage of the PCF is related to the possibility, due to the high index control, to fabricate LMA single-mode doped cores, which allow to reach high power levels, avoiding nonlinear effects and providing a good overlap between pump and signal. Moreover, since air holes are used instead of polymers for the air-clad PCF outer cladding [6], the thermal conductivity is greatly improved compared to the traditional DC fibers, and the material degradation is avoided [7]. A recent development is the manufacture of DC PCFs, called rod-type fibers, with the outer dimension of a rod laser, i.e., a diameter of few millimeters [8]. While the large outer diameter provides a reduction of macro- and microbend losses, the device retains the stability and the performances of a fiber laser.

An important issue for these LMA PCFs is still to keep the excellent quality of the output beam, first of all by proper fiber designs that can assure the single-mode propagation. In fact, even if single-mode lasing has been experimentally demonstrated for Yb-doped rod-type fibers [8], [9], numerical simulations have previously shown that the single-mode regime of all-silica PCFs is significantly reduced when a core region as large as in rod-type fibers is considered [10]. This paper aims to provide guidelines on geometry and refractive index distribution in order to allow manufacturers to fabricate LMA DC doped PCFs that are single-mode, or effectively single mode at the lasing wavelength of interest, strongly related to the rare-earth element added in the fiber core.

The analysis will first focus on the modal properties of the fundamental and higher order modes as a function of the doped core refractive index. Its value, in fact, increases with the doping, and manufacturers often attempt to match again the pure silica one by counter doping [9]. Slight variations, above or below the value for silica used in the cladding region, can considerably change the guidance characteristics of the modes, in particular of the higher order ones. A down-doped core surrounded by a photonic crystal cladding, for example, can guide due to the microstructure [9] and even lead to a short-wavelength cutoff for the fundamental mode [11]. By means of the finite-element method (FEM), we will, in this paper, analyze fibers with three different values of the doped core diameter, i.e., 35, 60, and 100 μm, showing, in particular, the mode effective index and the mode field distribution-doped region overlap versus the core refractive index.

As a second step, the analysis will consider the propagation of the modes along the doped fiber, showing how their gain competition can lead to effectively single-mode propagation, even for fibers that from simpler analysis would appear multimode. Results of this analysis will further confirm conclusions obtained from the computed overlap about the mode field and doped material interaction. Population and propagation rate equations will be mainly applied to Yb-doped PCFs, showing results at 1064 nm. Extension to Er-doped fiber working at 1550 nm is straightforward.
II. NUMERICAL APPROACH

A. Modal Analysis

The modal analysis is performed through a full-vector modal solver based on the FEM [12], [13], which requires as input data the actual refractive index profile of the doped fiber. The solver used here is based on the magnetic field curl–curl equation obtained by decoupling the Maxwell equations. Once the problem domain is suitably divided into a patchwork of finite subregions, called finite elements, the application of the standard variational FEM procedure yields the algebraic eigenproblem to be solved. When structural symmetries can be exploited, just one half or even one quarter of the whole domain can be considered. Fig. 1 shows the domain quarter used for the simulations. The vertical and horizontal boundaries, which cut the fiber core, define two possible symmetry axes where electric and magnetic perfect conductor conditions can be properly imposed to select all the possible fundamental mode (FM) and higher order mode (HOM) field distributions. The computed eigenvector represents the magnetic field distribution of the modes on the transverse fiber cross section, while the eigenvalue provides the attenuation constant and the effective index $n_{\text{eff}}$ of the modes. From the knowledge of the field, through the Poynting vector, the mode intensity, the effective area, and the mode overlap are straightforwardly computed.

B. Propagation Analysis

The propagation of the modes along the doped fiber is computed through a spatial model [14] that describes the power evolution by solving the propagation equations and the population rate equations, characterized, in terms of emission and absorption cross sections, dopant concentration, lifetime, etc., according to the considered doping material, i.e., ytterbium or erbium. Details of the model equations can be found in [15]. This spatial model uses the field distributions computed through the FEM to evaluate the intensities of the pump and of each propagating mode at the signal wavelength.

It is important to highlight that the model is not restricted to the description of a single mode, but it is able to consider, besides the pump, the propagation of more than one mode simultaneously, thus showing how they compete with each other in exploiting the pump energy and the inverted population. This model feature is very important to verify the effectively single-mode operation of the doped fibers.

III. MODE GUIDING PROPERTIES

A. 60-µm Rod-Type PCF

First, a detailed analysis of a LMA DC Yb-doped rod-type PCF with core diameter of 60 µm is presented, showing later the fiber behavior by decreasing and increasing the core dimensions. The discussed PCF has a circular ytterbium-doped core, obtained by removing 19 air holes, surrounded by the triangular lattice of the inner cladding that is characterized by four air hole rings, $\Lambda = 12.5$ µm and $d = 2.375$ µm, giving a ratio $d/\Lambda = 0.19$, $\Lambda$ and $d$ being the pitch and air hole diameter, respectively [9]. The outer cladding is obtained through a compact ring of large air holes, separated by silica bridges about 400 nm wide and 10 µm long. The refractive index of pure silica is equal to 1.45, whereas for the doped core, different refractive index values are considered, ranging from 1.4495 to 1.45, in order to investigate the effect of down-doping, which decreases the core index below the silica one. Fig. 1(left) shows a quarter of the studied structure, while Fig. 1(right) reports the mesh used for the FEM computations. The light gray region indicates the pure silica, the dark gray ones the air holes, and the black one the doped core.

The guiding properties of the FM and the first HOMs as a function of the doped core refractive index value have been evaluated. Fig. 2 reports the guided-mode effective index $n_{\text{eff}}$, computed at 1064 nm. The effective index of the inner cladding space-filling mode (SFM) $n_{\text{SFM}}$, which is assumed as the limit for the mode guidance, is reported in Fig. 2 as reference, but the present analysis does not depend on $n_{\text{SFM}}$. The fiber is clearly multimode for a core index equal to the pure silica one.
However, as the core refractive index decreases, the guided mode $n_{\text{eff}}$ values become lower, down to the extent of crossing the SFM line. The modes thus become less and less confined, and eventually no longer guided as their effective index is lower than $n_{\text{SFM}}$. In particular, this happens first for the HOMs, and then also for the FM, so that the fiber can be designed to be truly single-mode in a restricted range of the core refractive index, through a very precise choice of its value. Notice that when $n_{\text{core}}$ gets close to $n_{\text{SFM}}$, the guided mode can be regarded as one of the many cladding modes, among these the one with the higher effective index has been selected, and its value has been reported in Fig. 2.

In practice, however, the refractive index is controlled to a certainly accuracy (typically around $\pm 1 \times 10^{-4}$), which makes it difficult to assure single-mode propagation through this technique. This point will be further discussed in the following sections when studying amplification.

The mode behavior just described when decreasing the core refractive index can also be observed in the magnetic field distribution of the FM, reported in Fig. 3. The mode field clearly spreads from the inner region of the core, displacing more and more into the microstructured cladding. The figure reports the computed solutions for $n_{\text{core}} = 1.45, 1.44975, 1.44965, \text{and } 1.4496$. Similar behaviors have also been observed for the HOMs, of course considering higher values of the core refractive index.

It is also important to highlight how the outer ring of large air holes make up a strong barrier against the field leakage in the outer silica region of the rod-type PCF. For this reason, these fibers, even bent, suffer negligible leakage losses. Bending, however, may lead to undesired coupling between the core and inner-cladding modes.

Further insight is gained from the analysis of the guided-mode field overlap with the doped-core region and of the effective area $A_{\text{eff}}$, reported, respectively, in Figs. 4 and 5 versus $n_{\text{core}}$, still at 1064 nm. By decreasing the core refractive index, the HOM overlap is reduced much more than the FM one, being, for example, with $n_{\text{core}} = 1.4497$, only 0.64 and 0.21, respectively, for HOM$_1$ and HOM$_2$, against 0.9 for the FM. The overlap is a very important parameter when considering the field propagation in a doped and pumped fiber. The values reported in Fig. 4 predict high differential gain to the advantage of the FM, so that the HOMs may be effectively suppressed even if their $n_{\text{eff}}$ is above $n_{\text{SFM}}$.

The effective area still keeps very high values, around thousands of square micrometers, according to the achieved $n_{\text{core}}$. Of course, as the FM effective index becomes lower than $n_{\text{SFM}}$, with decreasing $n_{\text{core}}$, the field spreads into the cladding providing very high effective area values that, however, do not correspond to a guided solution.

Finally, it is interesting to note that a strong reduction of $n_{\text{core}}$ gives the possibility to achieve the FM cutoff also as its effective index curve crosses the SFM one. This FM property can be exploited, for example, to suppress the amplified spontaneous emission in order to obtain amplification in the long wavelength range, for instance, in L band when considering an Er-doped rod-type PCF.

**B. 35-µm and 100-µm Core Diameter Rod-Type PCF**

A similar analysis, in terms of effective index, field distribution, overlap, and effective area, has also been performed considering rod-type PCFs with different core diameters, i.e., 35 and 100 µm, whose geometrical characteristics are summarized in Table I. In particular, the first one has been already manufactured with a Yb-doped core, formed by removing seven air holes, a triangular lattice of the inner cladding characterized by $d/\Lambda = 0.33$ with $\Lambda = 12 \mu m$, and an hexagonal air-cladding [8], whereas the second one has been designed by scaling the 60-µm PCF previously studied, and fabricated only in a passive version [9]. The values of $d$ and $\Lambda$ have been scaled by a factor 1.666, whereas the ratio $d/\Lambda$ has been unchanged, and the study has been performed at 1064 nm.

The behavior of the two fibers qualitatively retraces the one already presented and, for the sake of brevity, it will not be discussed again. However, to highlight the differences arisen in the numerical results, it is very interesting to compare the overlap values of all the fibers, since this is an important figure of merit for the following discussion. Notice that the 35-µm fiber air-cladding is hexagonal [8], unlike the circular one of the two other rod-type PCFs considered here. The overlap with the doped core of the FM and of the first HOM at 1064 nm is shown in Fig. 6(a) for the 35 µm core PCF, and in Fig. 6(b) for the 60 and 100 µm core diameter. For each fiber, the figures report a set of three curves always decreasing by reducing the core refractive index, however, with quite different slopes. While the overlaps in the 35-µm rod-type PCF change only slightly with $n_{\text{core}}$, in the 60 µm one, already discussed, changes are much more pronounced, and finally, the 100 µm fiber presents very steep curves with strong variations in a limited range of $n_{\text{core}}$. Targeting a very high overlap value for the FM in this PCF, for example, as close to 1.0 as possible, the core refractive index must be very close to the pure silica one, resulting in HOMs that also maintain high overlaps. This could yield a
Fig. 3. Magnetic field distribution of the FM at 1064 nm with decreasing core refractive index. From left-top to right-bottom: $n_{\text{core}} = 1.45, 1.44975, 1.44965,$ and 1.4496.

Fig. 4. Field overlap with the doped core of the FM and HOMs at 1064 nm versus the core refractive index.

strong competition between amplifying modes. On the contrary, by slightly reducing $n_{\text{core}}$, the HOMs are pushed close, or even below, the $n_{\text{SFM}}$ curve and their overlap with the doped region decreases considerably.

For all the three fibers considered, a FM overlap around 0.9 assures HOM$_1$ overlap values around 0.6, and HOM$_2$ ones below 0.3, which are quite effective to actually guarantee a single-mode

Fig. 5. Effective area of the FM at 1064 nm versus the core refractive index.

<table>
<thead>
<tr>
<th>TABLE I</th>
<th>SUMMARY OF THE GEOMETRICAL CHARACTERISTICS OF THE CONSIDERED ROD-TYPE PCFS</th>
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<tbody>
<tr>
<td>Rod-type (core diameter)</td>
<td>$\Lambda$ (µm)</td>
</tr>
<tr>
<td>35 µm</td>
<td>12</td>
</tr>
<tr>
<td>60 µm</td>
<td>12.5</td>
</tr>
<tr>
<td>100 µm</td>
<td>20.8</td>
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propagation, as will be shown in the next section. The main difference, of course, occurs in the value of the effective area that can be achieved with the three fibers, lower than 950 \( \mu \text{m}^2 \) for the 35 \( \mu \text{m} \) fiber and higher than 2500 \( \mu \text{m}^2 \) for the others, at 1064 nm. These results clearly suggest that a proper choice of the doped core refractive index can allow to design rod-type PCFs with very large mode area, in single-mode regime, or with very few HOMs that, however, present a low overlap with the doped core region. It must be noted that such a design will require a very precise control over the core refractive index, and that this accuracy becomes more critical with increasing core size.

**IV. AMPLIFIED BEHAVIOR**

In order to verify some conclusions drawn in the previous section while discussing the overlap results, the amplification properties of the rare-earth-doped rod-type PCFs have been investigated considering the mode propagation along the pumped fiber. Still focusing on the 60-\( \mu \text{m} \) rod-type Yb-doped PCF, a dopant concentration equal to 4.39 \( \times \) \( 10^{25} \) ions/m\(^3\) and a lifetime of the excited state equal to 1 ms have been considered. The ytterbium absorption and emission cross-sections have been assumed as in [16], and a copropagating pump at 976 nm with a power of 300 W has been used for a 1.5-m-long fiber. Results obtained by launching a total input power level of 3 W equally distributed among the modes.
Notice that this is a worst-case assumption as actual excitation conditions of the fiber usually favors the FM, rather than equally distributing the input power among all the propagating modes. Fig. 7 shows the different amplification undergone by the modes according to the values of the core refractive index, i.e., as observed in the previous section, according to the different values of the mode overlaps.

In the first case, corresponding to \( n_{\text{core}} = 1.45 \), all the three modes achieve a high output power level, being able to exploit in a similar way the population inversion in the doped core, as clearly described by the comparable values of the overlap in Fig. 4. When passing to \( n_{\text{core}} = 1.44965 \), the overlaps strongly differ, being about 0.62 for HOM\(_1\), and with HOM\(_2\) and HOM\(_3\) below \( n_{\text{SFM}} \). In these conditions, the mode competition favors the FM that achieves an output power level higher than 200 W, as reported in Fig. 7(b). Finally, with \( n_{\text{core}} = 1.44965 \), both the HOMs are below the \( n_{\text{SFM}} \) curve. Only HOM\(_1\) is considered for the propagation in the doped fiber, HOM\(_2\) being no more guided. Fig. 7(c) shows that the pump depletion is practically given only by the FM, which reaches a 250 W output power level with a very high conversion efficiency. Note that the two considered modes exhibit the same input power of 1.5 W, but at the output of the doped fiber, the power of HOM\(_1\) is only 8% with respect to the FM mode one.

Fig. 8 reports results obtained for a more realistic case. The distribution of 3 W input power among modes is 90% to the FM and 10% to the HOM\(_1\). In this case, the output power of HOM\(_1\) is only 0.5% with respect to the FM mode.

V. CONCLUSION

The possibility to obtain single-mode or effectively single-mode regime in LMA DC rod-type PCFs has been discussed. It has been numerically demonstrated how a slight core down-doping can push the high-order modes below the SFM effective index curve, or can provide overlap values with the doped core that assure the amplification of the FM to the detriment of the HOMs eventually excited in the fiber.

Examples of rod-type PCFs with 35, 60, and 100 \( \mu \)m core diameters have been considered, demonstrating, in all cases, that the doped core refractive index can be engineered to assure high-power single-mode output beams.

**REFERENCES**


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