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Response of an annular electrostatic probe for a planar dielectric spacer: II

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Abstract: The response of annular electrostatic probes mounted in an electrode is examined with reference to a planar dielectric spacer. On this occasion the presence of a high-voltage point electrode is included in the system geometry. The study involves using the probe λ function to derive characteristic parameters. These parameters enable the response of such probes to be quantitatively assessed.

Introduction

Recently, the response of bound annular electrostatic probes has been examined with respect to a plane dielectric spacer alone [1]. Such probes were used by Yamamoto and colleagues to examine the surface charge resulting from the development of a discharge across the surface of a planar gas/solid-dielectric interface [2-4]. In these studies a high-voltage point electrode was employed to promote discharge development across the surface of the solid dielectric.

The word bound signifies that the probe is mounted in the electrode in contact with the solid dielectric. Thus, as the probe is an integral part of this electrode, such probes lack the freedom of movement necessary to implement a scanning procedure. This is required for a correct quantitative evaluation of the surface charge to be made [5-7].

The relationship between the charge induced on a probe and the charge density at the gas/solid-dielectric interface is expressible in terms of a general function, the λ function [8]. Using this function it is possible to examine the response of electrostatic probes. In the present study, the response of annular probes to surface charge on a planar dielectric spacer, in the presence of a high-voltage electrode, is investigated. For a system of concentric annular probes, the point electrode is shown to have a strong effect on the λ functions of the inner electrodes. In turn this influences the charge induced on these probes, and hence the response is considerably modified by the presence of the high-voltage electrode.

The λ function

The λ function is the proportionality factor between the charge induced on the probe to any charge within the dielectric volume or at an interface [8]. If it is

assumed that the volume charge density in the solid dielectric is zero, then this relationship can be expressed simply as

$$q = - \iint_{A_0} \lambda \sigma dA \quad (1)$$

where q is the Poissonian induced charge on the probe sensor plate, and σ is the surface charge density on the surface element dA of A_0 , the surface of the solid dielectric.

The dimensionless parameter λ is a solution of the general Laplace equation for the complete system geometry:

$$\vec{\nabla} \cdot (\epsilon \vec{\nabla} \lambda) = 0 \quad (2)$$

The boundary conditions are $\lambda = 1$ at the sensor plate of the probe in question and $\lambda = 0$ at all other electrodes. In addition, at dielectric interfaces the normal derivatives of λ must obey the condition

$$\epsilon_+ \left(\frac{\partial \lambda}{\partial n} \right)_+ = \epsilon_- \left(\frac{\partial \lambda}{\partial n} \right)_- \quad (3)$$

where the + and - signs refer to the opposite sides of the interface. As (2) is just Laplace's equation, any standard method of solving this equation can be employed to evaluate the variation of λ along the interface. On this occasion, solutions of Laplace's equation were obtained using a finite element software package. These solutions were then used to study the dependence of the probe response upon the surface charge distribution.

Probe/dielectric geometry

To establish the characteristics of a system of annular probes with an *in situ* high-voltage electrode, we will consider a system involving 8 concentric probes. The essential geometry of the system is shown schematically in Figure 1, in which r_i and r_o are the inner and outer radii of an annular probe sensor plate,

while w represents the width of this sensor, *i.e.* $w = r_o - r_i$. In the present study, $w = 2$ mm. The gap between the sensor plate and a neighbouring probe is Δ . As in [2-4] this spacing is fixed at 0.2 mm. If i represents the probe number, with $i = 1, 2, 3, \dots, 8$, then the relative geometric dimensions of the 8 probes are listed in Table 1. The central probe ($i = 1$) with $r_i = 0$ is just a circular disc. It should be noted that the probe dimensions are identical to those used in [1].

The high-voltage point electrode is a hemispherically-ended cylindrical rod, of radius $R = 5$ mm, in contact with the upper surface of the dielectric plate, see Figure 1. The length of this electrode is much longer than the thickness of the dielectric plate.

Figure 1: Annular-probes/planar-dielectric geometry.

The planar dielectric, of relative permittivity ϵ_r , has a thickness t in a direction normal to the plane electrode which is grounded. As in [2-4], $t = 2$ mm. In the direction normal to probe/gap axis, the extent of

Table 1: Relative geometry of annular probes.

i	r_i / w	r_o / w
1	0	1.0
2	1.1	2.1
3	2.2	3.2
4	3.3	4.3
5	4.4	5.4
6	5.5	6.5
7	6.6	7.6
8	7.7	8.7

r_i - inner probe radius

r_o - outer probe radius

probe width $w = 2$ mm

probe separation $\Delta = 0.2$ mm

point radius $R = 5$ mm

thickness of dielectric $t = 2$ mm

the plane electrode/planar dielectric is much greater than the probe lateral dimensions.

Results

The variation of the λ_i along the planar dielectric interface, where i denotes the probe number, for $\epsilon_r = 4$ is shown in Figure 2. As the charge induced by the same source differs from probe to probe, it is necessary to evaluate the λ function for each probe: *i.e.* we have $\lambda_1, \lambda_2, \dots, \lambda_8$. Figure 2 refers to the four inner probes ($i = 1, \dots, 4$) as the λ functions exhibit clearly the influence of the point electrode ($\lambda = 0$).

A comparison with the corresponding Figures in [1] indicates that the existence of $\lambda = 0$ at $r = 0, z = t$ suppresses the maximum λ values associated with the inner probes and as a consequence the central probe no longer exhibits a bell-shaped λ distribution.

Figure 2: Variation of λ_i along the planar interface for the inner probes.

For the four outer probes ($i = 5, \dots, 8$), a comparison with the λ functions shown in [1] indicates that the influence of the point electrode is negligible: *i.e.* the λ functions for these probes are effectively identical with those presented in [1].

The behaviour of λ_i with permittivity is as expected for bound probes: *i.e.* an increase in ϵ_r produces an increase in the magnitude of λ_i .

Charge is also induced on the point electrode, and therefore the relevant λ function, λ_p , has been evaluated. In contrast to the λ_i distributions, the variation of λ_p along the dielectric interface is quite different, with a maximum value of unity on the axis, see Figure 3. This Figure also demonstrates that, unlike the annular probes, an increase in ϵ_r now leads to a reduction in the λ_p values away from the axis.

The significance of the variations in the λ_i functions can be quantified by examining the behaviour of another parameter which describes the

Figure 3: Variation of λ_p along the planar interface for the point electrode

detection sensitivity S_e of the probe with respect to a surface charge at the dielectric interface.

If (r, z) represent cylindrical coordinates, see Figure 1, then for a circular disc of constant surface charge density σ_0 , the charge q_i induced on probe i is given by

$$q_i(r) = -2\pi\sigma_0 \int_0^r \lambda_i r' dr' \quad (4)$$

where r' is a dummy variable.

Traditionally, electrostatic probe measurements are interpreted as though the probe responds only to the charge directly subtended by the sensor plate, i.e. the value of charge Q_i assumed to be measured is given by

$$Q_i = \pi(r_0^2 - r_i^2)_i \sigma_0 \quad (5)$$

By using this charge value as a normalising factor, it is possible, with respect to induced charge, to define a detection sensitivity as

$$S_{ei} = \frac{|q_i|}{Q_i} = \frac{2}{(r_0^2 - r_i^2)_i} \int_0^r \lambda_i r' dr' \quad (6)$$

A typical radial extent of the streamer discharge reported in [2-4] was approximately 15 mm: i.e. if r_0 denotes the radial extent of the surface charge, then we assume $r_0/w = 7.5$. On this basis, the variation of S_{ei} for the probes was evaluated and the results for the inner probes ($i = 1, \dots, 4$) are illustrated in Figure 4.

In comparison to the S_{ei} results shown in [1] for the inner probes, S_{ei} does not attain a value > 1 . The reduction in the S_{ei} value is of course a consequence

Figure 4: Variation of S_{ei} for the inner probes.

of the reduced λ_i values, with probes 1 and 2 exhibiting the greatest reductions. The S_{ei} results for the outer probes ($i = 5, \dots, 8$) are essentially identical to the results discussed in [1].

For the same surface charge conditions, the charge q_p induced on the point electrode is given by

$$q_p(r) = -2\pi\sigma_0 \int_0^r \lambda_p r' dr' \quad (7)$$

where r' is again a dummy variable.

Owing to the very different forms of λ_i and λ_p , it is of interest to consider the relation between q_i and q_p . The basis for a comparison may be obtained by combining (4) and (7) to give

$$\frac{q_i}{q_p} = \frac{\int_0^r \lambda_i r' dr'}{\int_0^r \lambda_p r' dr'} \quad (10)$$

The variation of the ratio q_i/q_p is illustrated in Figure 5 for the inner probes.

Figure 5: Variation of q_i/q_p for the inner probes.

For probes 1 and 2, it is seen that, as $q_i/q_p < 1$, the charge induced on the point is greater than that induced on probe. With the exception of probe 8, see [1], the maximum value of $q_i/q_p > 1$ for the remaining probes, implying that the charge induced on these probes is greater than that induced on the point electrode.

The above behaviour can be understood with respect to the different λ functions. The values of λ_1 and λ_2 are reduced markedly owing to their proximity to the point electrode, while λ_p decreases rapidly with distance from axis of the system.

Discussion

We have examined the response of a system of annular probes with reference to a planar dielectric. In the present study, the existence of the high-voltage electrode was taken into account in the evaluation of the probe λ functions. It is shown that this electrode has a significant influence on the λ functions of the probes nearest to it, in this instance the inner probes ($i = 1, \dots, 4$). The influence is further reflected in the response of these inner probes.

For real-time measurements, during which a high voltage is applied to the point electrode, an additional aspect arises because the surface charge produced by the discharge induces charge on *all* electrodes in the system.

Depending on the electrode in question, these induced charges can produce changes in the electrode potentials. Through the partial capacitances these changes are registered at the measuring probe. Such a situation will make the interpretation of the probe measurements more difficult.

The significance of this situation has been demonstrated by assessing the ratio of the induced charge on a probe q_i to that on the point electrode q_p .

It is shown that $q_i/q_p < 1$ for the innermost probes ($i = 1, 2$). This suggests that the charge induced on the point can provide a significant fraction of the signals from these probes, leading to additional difficulties in the interpretation of measurements from probes 1 & 2.

In [2-4], the authors made simultaneous measurements from 4 probes. This implies that the signal from any probe reflects not only the induced charge from the point electrode, but also from the 3 other probes. Hence, without a knowledge of the relevant partial capacitances and changes in potential, a quantitative analysis of a probe record is not feasible.

Conclusion

For electrostatic probe measurements undertaken during the voltage application, the existence of the high-voltage electrode must be considered in the evaluation/analysis of the probe signals. This requirement arises because the electrode influences the λ function of the nearest probes, and thus the response of these probes. In addition, the charge induced on the high-voltage electrode is registered, via the partial capacitance and change in potential, at the measuring probe.

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