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# Geometrical tuning of nanoscale split-ring resonators

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**Abstract:** We investigate the capacitance tuning of nanoscale split-ring resonators. An  $LC$ -model predicts a simple dependence of resonance frequency on slit aspect ratio. Experimental and numerical data follow the predictions of the  $LC$ -model.

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## 1. Introduction

Metamaterials are artificially structured materials with exceptional optical properties inherited from the structure of the sub-wavelength, mesoscopic unit-cell. Designing negative index materials with simultaneously negative permittivity  $\epsilon$  as well as a negative permeability  $\mu$  is one of the promising aspects of metamaterials. Since a negative electric response is common in metals at e.g. optical frequencies, the search has primarily focused on designing structures with a negative magnetic response. Different types of split-ring resonator (SRR) geometries [1–3] are particularly central in this context and have been realized at Terahertz [1, 4] to visible frequencies [3, 5]. The analogy with inductor-capacitor ( $LC$ ) circuits have motivated considerable efforts in establishing simple circuit models, allowing for an estimate of the resonance frequency  $\omega_0 = 1/\sqrt{LC}$  in terms of geometrical parameters of the split-ring resonator structure, see. e.g. Refs. [6–7] and references therein. The  $LC$ -model has proven to be a good approximation as long as the coupling response of the SRR array is small compared to the response of a single SRR, hence the period  $\Lambda$  has to be sufficiently large [8]. Tuning of the resonance has been accomplished by scaling of a single geometrical dimension [9], linear scaling of all SRR dimensions [5], and finally by altering the cladding [10].

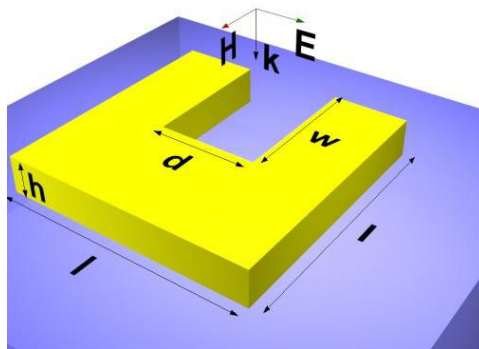


Figure 1. Schematic drawing of the split-ring resonator design, indicating central geometrical parameters as well as the polarization configuration of the excitation.

In this paper, the influence on resonance frequency of geometrical scaling of split-ring resonators is studied experimentally and by means of full-wave numerical simulations. The SRRs are placed in a periodic array keeping the period constant and large,  $\Lambda=500$  nm, to minimize coupling effects. The system is described by an  $LC$ -model [7]. The model predicts a data collapse, which is experimentally verified.

$$(k_0 l)^2 \sim d/w \quad (1)$$

where  $k_0$  is the free-space wave number,  $l$  is the side length,  $d$  is the slit width,  $w$  is the slit length, see Fig. 1.

## 2. Results

The LC-model is compared to experimental and numerical simulation data. Full-wave simulations were performed in CST Microwave Studios. The numerical data in Fig. 2(b) are calculated for a structure with  $l=200$  nm,  $d=80$  nm,  $h=30$  nm,  $\Lambda=440$  nm. The numerical data support the predicted linear scaling of the LC-model.

For the experimental investigations, 8 samples with 2 mm by 2 mm arrays of gold SRRs were fabricated on glass substrates by electron beam lithography and lift-off [7], see Fig. 2(a). The geometrical parameters of the samples covered:  $d=80$  nm,  $w=90$ -110 nm,  $l=200$  nm,  $h=35$  nm.

The transmission was measured using a 1 mm diameter laser spot, thus effectively probing an ensemble of  $10^8$ - $10^9$  SRRs. The experimental data are fitted to the LC-model in Fig. 2(b), using  $k=2\pi/\lambda$ , where  $\lambda$  is the measured resonance wavelength  $\lambda$ , and the split ring dimensions  $d$ ,  $l$ ,  $w$  are measured by SEM inspections.

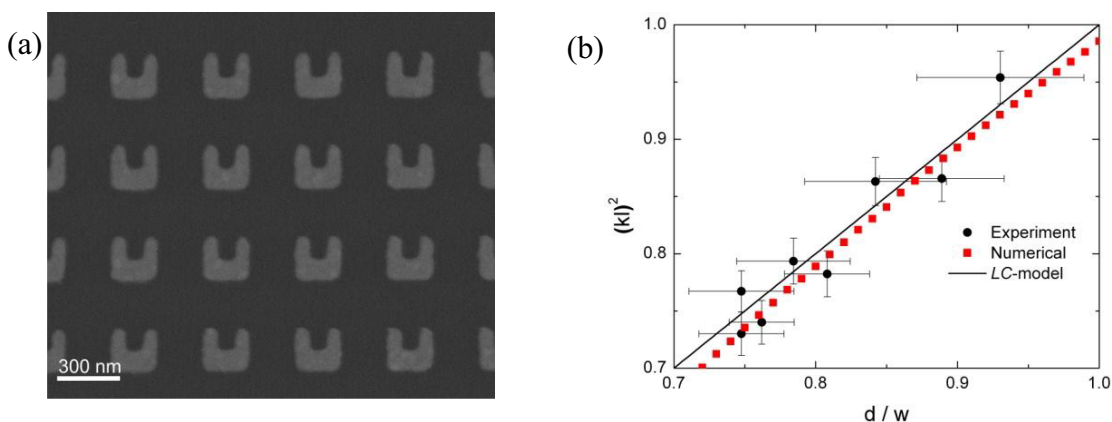


Figure 2. (a) Micrograph of a SRR array with pitch  $\Lambda = 440$  nm. This sample has  $l = 200$  nm,  $w = 95$  nm,  $d = 80$  nm, and  $h = 35$  nm. (b) Plot of  $(k_0 l)^2$  versus  $d/w$  where experimental and numerical data are plotted together with the LC-model. The x-error bars on the experimental data represent the standard deviation (SD) of ten individual measurements of  $w$ , and  $d$  added together. The y-error bars are the 1 nm spectral resolution of the Ando AQ-6315E Optical Spectrum Analyzer added to the SD of ten measurements of the length.

In conclusion, we have fabricated periodic arrays of subwavelength, nanoscale split-ring resonators to investigate geometrical tuning. Our key observation is that the experimental and numerical data follow the predictions of the LC-model.

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