



## **An experimental investigation of heat transfer enhancement in minichannel: Combination of nanofluid and micro fin structure techniques**

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1 **An experimental investigation of heat transfer enhancement**  
2 **in minichannel: combination of nanofluid and micro fin**  
3 **structure techniques**

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11 **Abstract**

12 This work experimentally studied the single-phase heat transfer and pressure drop  
13 characteristics by using two heat transfer enhancement techniques (micro fin structure  
14 and nanofluids) in multiport minichannel flat tube (MMFT). MMFT consisted of  
15 numerous parallel rectangular minichannels and is widely used in industry as the heat  
16 transfer unit of a heat exchanger. Firstly, the enhanced heat transfer performances by  
17 individually using one enhancement technique were investigated by testing Nusselt  
18 number, friction factor and performance evaluation criterion (PEC). In this section, five  
19 MMFTs with different micro fin numbers ( $N = 0, 1, 2, 3$  and  $4$ ) and nanofluids with  
20 three volume concentrations ( $\varphi = 0.005\%$ ,  $0.01\%$  and  $0.1\%$ ) were used as test sections  
21 and working fluids respectively. Secondly, the experiments using two combined

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1 enhancement technique were performed. By using conjunctively two enhancement  
 2 techniques, Nusselt number increases by up to 158% at about  $Re = 3600$  and the  
 3 maximum PEC value can reach 2.0 at  $Re = 5150$ . Finally, an optimal heat transfer  
 4 scheme was proposed based on test data.

5 **Keywords:** multiport minichannel flat tube, heat transfer enhancement, micro fin  
 6 structure, nanofluid, PEC

7

<b>Nomenclature</b>	
A	total wetted area, $m^2$
C	wetted perimeter, m
$c_p$	specific heat capacity, J/kg K
d	diameter, m
$D_h$	hydraulic diameter, m
$f$	friction factor
$\dot{m}$	mass flow rate, kg/s
H	Height, m
h	heat transfer coefficient, $W/m^2 K$
k	thermal conductivity, $W/m K$
L	length, m
MMFT	multiport minichannel flat tube
Nu	Nusselt number
Pe	perimeter, m
PEC	performance evaluation criterion
Pr	Prandtl number
$\Delta P$	total pressure differential, Pa
$\Delta P_{fri}$	frictional pressure loss, Pa
$\Delta P_m$	singular pressure loss, Pa
q	heat flux, $W/m^2$
Q	heat transfer rate gained by fluid, W
Re	Reynolds number
T	temperature, $^{\circ}C$
x	axial distance, m
W	Weight, m

Greek Symbols	
$\alpha$	aspect ratio, $b/a$ ( $0 < \alpha < 1$ )
$\phi$	volume concentration
$\mu$	dynamic viscosity, Pa•s
$\rho$	mass density, $kg/m^3$

Subscripts	
$bf$	base fluid
$f$	fluid
$nf$	nanofluid
$c$	channel
$fin$	fin
$in$	inlet
$out$	outlet
$w$	wall

8

## 1 **1. Introduction**

2 With the pioneering work of Tuckerman and Pease [1] in early 1981, concept of  
3 microchannel heat sinks was first demonstrated and potential heat flux removal rate of  
4 the order  $1000 \text{ W/cm}^2$  for single-phase forced convective cooling in microchannels was  
5 predicted. After that, micro-scale heat transfer in micro/minichannel has become  
6 increasingly popular and been applied in various fields due to their large surface area  
7 to volume ratios and high heat transfer coefficients. Moreover, it is of critical  
8 significance to develop the heat transfer enhancement techniques in micro/minichannel,  
9 confronted fast growing power consumption, energy and materials savings, high heat  
10 flux removal and device miniaturization. In a review of heat transfer in microchannels  
11 presented by Kandlikar et al. [2], it states that enhancing heat transfer in microchannels  
12 is of critical importance in successful development of microscale thermal devices. The  
13 heat transfer coefficient needs to be further increased, while dramatic reductions in  
14 pressure drop are warranted.

15 Wu and Sundén [3] performed a state-of-the-art overview of the most recent single-  
16 phase flow enhancement techniques, where microfins and additives were summarized  
17 as two key approaches to improve single-phase thermal performance in  
18 micro/minichannels. It was concluded that micro/minichannels within interrupted  
19 microfins are very promising for high heat-flux dissipation. Engineered fluids with  
20 additives, very popular in research during the last ten years, maybe an efficient way to  
21 significantly improve the thermal performance without large pressure drop penalty. For  
22 microfin structure, many literatures have proved that this technique can significantly

1 enhance heat transfer performance [4-7]. Lee et al. [8] performed an experimental  
2 investigation into enhancing heat transfer by employing sectional oblique fins in  
3 microchannel heat sink. The results found that heat transfer performance of the  
4 enhanced microchannel is greatly augmented and when the Reynolds number is  
5 increased beyond 600, heat transfer enhancement reaches 2.2. Meanwhile, nanofluid as  
6 the most common product of particle additives also shows great ability to improve the  
7 thermal performance in micro/minichannel [9-11]. Ho et al. [12] experimentally  
8 investigated the forced convective cooling performance of a copper microchannel heat  
9 sink with Al<sub>2</sub>O<sub>3</sub>-water nanofluid as the coolant. For the largest flow rate tested for the  
10 nanofluid of 1 vol.%, the average heat transfer coefficient increased by about 70%  
11 compared with that with water.

12 Based on above research results, in order to achieve the better heat transfer  
13 performance, the combined effects of micro fin structure and nanofluids on the heat  
14 transfer enhancement in the microchannel are worth to be expected. However, the  
15 enhanced heat transfers using micro fins and nanofluids often accompany complicated  
16 mechanism, especially for nanofluids. As concluded in Ref. [13], low weight  
17 percentages of nanoparticles seem to provide the best performance. The mechanisms  
18 for enhanced lubrication performance are manifold and depend on the material structure  
19 of the nanoparticles. Moreover, in the literatures about single-phase flow heat transfer  
20 of nanofluid in smooth micro/minichannel, some novel phenomena have been found  
21 including the delay of laminar-turbulent transition [14] and discrete precipitation of  
22 agglomerated nanoparticles in the channel [15]. Therefore, applicability that using

1 nanofluids in micro/minichannel with micro fin to enhance heat transfer should be  
2 further studied. Furthermore, from the literature survey, it can be found that the  
3 experimental investigations combining micro fin and nanofluids are much less  
4 compared with those just using one enhancement technique. Therefore, more  
5 investigations regarding the research of combined these two enhancement techniques  
6 should be performed, which have significance to further study the comprehensive  
7 strengthening effect and design the optimal enhanced heat exchange scheme.

8 Few research regarding flow and heat transfer characteristics of nanofluid in  
9 micro/minichannel with micro fin structure have been presented in the open literatures.  
10 Aliabadi et al. [16] performed an experimental assessment of the copper–water  
11 nanofluid flow through seven plate-fin channels. It was found that the best thermal–  
12 hydraulic performance is obtained by the vortex in comparison with the plain one  
13 generator. Meanwhile, the use of nanofluid in this channel had more benefit at the lower  
14 flow rates and high nanoparticles weight fractions. Roshani et al. [17] investigated  
15 experimentally the hydrodynamic and thermal performance of a miniature plate pin-  
16 finned heat sink by utilizing two widely used nanofluids,  $\text{Al}_2\text{O}_3$ –water and  $\text{TiO}_2$ –water.  
17 The results found that although 15% and 30% increase in the pumping power for the  
18 volume concentration of 2%  $\text{Al}_2\text{O}_3$ –water and  $\text{TiO}_2$ –water nanofluids, respectively, the  
19 average heat transfer coefficients increased by 16% and 14% and the thermal resistance  
20 decreased by 17% and 14% for each nanofluid. Eiamsa-ard and Wongcharee [18]  
21 conducted an experimental research to study the effect of combined heat transfer  
22 enhancement techniques (dual twisted-tapes, a micro-fin tube as well as nanofluids) on

1 heat transfer, friction factor and thermal performance factor. The test results indicated  
2 that the beneficial effect for the energy saving by the uses of the combined techniques,  
3 especially at low Reynolds number. Duangthongsuk and Wongwises [19] reported an  
4 experimental investigation into the thermal performance and pressure drop  
5 characteristics of nanofluid-cooled heat sinks with miniature circular-fin and square-fin  
6 structures. The experimental results indicated that the heat transfer coefficient increased  
7 with increasing Reynolds numbers and particle concentrations. The miniature circular-  
8 fin gave greater heat transfer performance than that of the square-fin by about 6–9%.  
9 From the current research which show the combined effects of micro fin structure and  
10 nanofluids on the heat transfer enhancement, it could be found that a comprehensive  
11 performance factor that simultaneously considers the improvements of heat transfer and  
12 pressure drop was calculated in the most studies. However, not all the results of  
13 performance factor could indicate that combination of two enhancement techniques  
14 have positive effects to enhance heat transfer performance. This phenomenon illustrates  
15 again the necessity and urgency of research in this field.

16 In this study, one type of multiport minichannel flat tube (MMFT) was used as the  
17 test section. MMFTs are widely applied in various fields as a heat exchanger unit due  
18 to the efficient heat transfer performance. Moreover, one type of continuous fin  
19 structure along axial direction (two-dimensional fin) in micro/minichannel also was  
20 used in this study. This type of fin structure can be fabricated by heat extrusion with  
21 MMFT at one time, which is a much simpler and more low-cost technique compared  
22 with those of the staggered fin array (three-dimensional fin) which are investigated in

1 most literatures. An experimental investigation of single-phase convection of  $\text{TiO}_2$ -  
 2 water nanofluid in MMFTs with different fin numbers was presented in this paper,  
 3 which aims to study whether combination of continuous fin structure and  $\text{TiO}_2$ -water  
 4 nanofluids can further improve heat transfer performance relative to just using one of  
 5 enhancement techniques. Finally, an optimal heat transfer scheme would be proposed.

6

## 7 2. MMFT and Nanofluid

### 8 2.1 MMFT

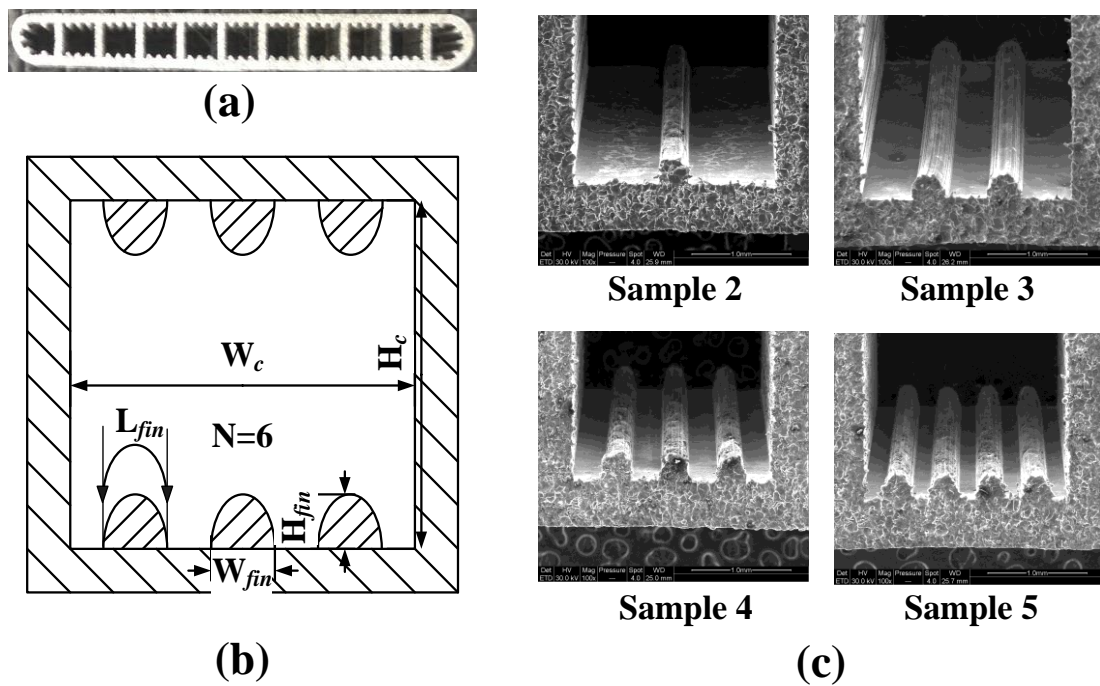


Fig. 1 The cross-section of MMFT

11 In this study, five aluminum MMFTs with different fin numbers were fabricated and  
 12 used as test sections, which are defined as sample 1, sample 2, sample 3, sample 4 and  
 13 sample 5 respectively. Taking sample 4 as an example, Fig. 1a shows the cross-section



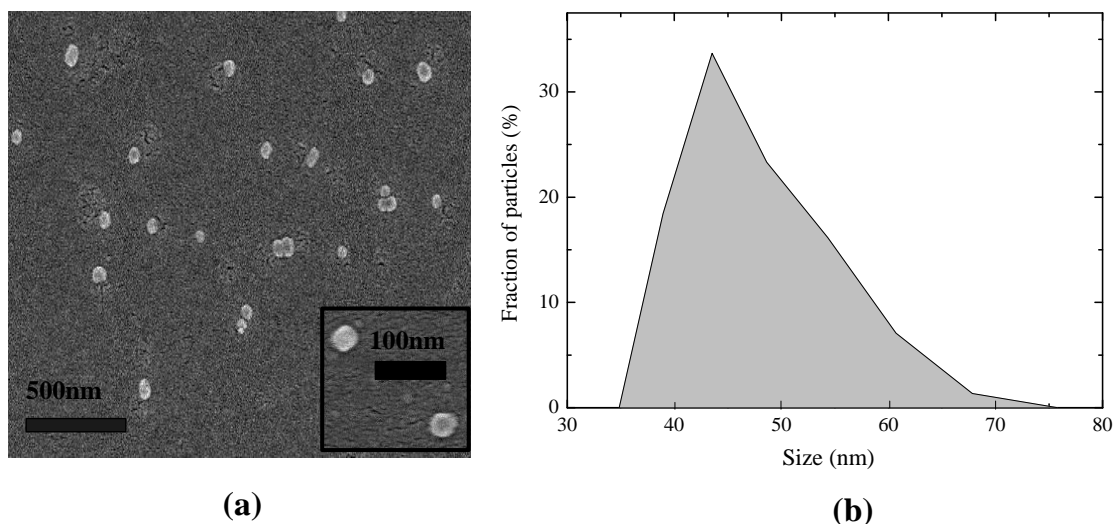
1 of MMFT. Five MMFTs are all composed of 11 parallel and independent square  
2 minichannels. Moreover, except for the fin number, five MMFT have same other  
3 parameters, including both dimension and shape of each square minichannel and fin  
4 structure. Fig. 1b illustrates the schematic drawing of an independent square  
5 minichannels with micro fin structure. The height and width of channel  $H_c$  and  $W_c$   
6 both are 2 mm, while height of fin  $H_f$  and bottom width  $W_f$  of fin are 0.24 mm and 0.28  
7 mm respectively. Fig. 1c presents a scanning electron microscopy (SEM) photograph of  
8 fins for Sample 2-5. As shown in figures, fins are distributed symmetrically at the upper  
9 and lower internal surfaces of each minichannel and fabricated continuously along axial  
10 direction, and thereby can be considered as two-dimensional structure. Fin numbers of  
11 Sample 1-5 are 0, 2, 4, 6 and 8 respectively. Therefore, sample 1 is a smooth tube  
12 without fin structure, and the experimental results using this tube as test section and  
13 water as working fluid can not only verify the integrity of the experimental facility but  
14 also provide baseline information to compare the improvement of heat transfer  
15 performance using different enhancement techniques.

## 16 ***2.2 Nanofluid***

17  $\text{TiO}_2$ -water nanofluids with 0.005%, 0.01% and 0.1% volume concentrations were  
18 prepared by two-step method in this study. The production method of nanofluids is  
19 characterized by the following steps: firstly, adding  $\text{TiO}_2$  nanoparticles with particle  
20 diameter  $d_p = 10$  nm into base fluid, water. Cetyl trimethyl ammonium bromide (CTAB),  
21 a dispersant with mass that is 0.2 times higher than that of the nanoparticles, was then  
22 dispersed in the water. Finally, the solid-liquid mixture was oscillated in an ultrasonic

1 washer for 1 h and then allowed stand for another hour. The final step was repeated but  
2 oscillation was instead conducted for 3-5 h. Mixtures with higher volume concentration  
3 required longer oscillation time.

4 In order to investigate particle distribution and effective particle size in the  
5 suspensions, scanning electron microscopy (SEM) and dynamic light scattering (DLS)  
6 were adopted respectively for nanofluids with different volume concentrations. Taking  
7 0.01% nanofluid as an example, Fig. 2a and Fig. 2b show SEM image and particle size  
8 distribution of 0.01% TiO<sub>2</sub>-water nanofluid respectively. From Fig. 2a, it can be found  
9 that nanoparticles distribute uniformly in the suspensions and particle size is about 50  
10 nm, which is consistent with the result obtained by DLS measurement and much bigger  
11 than 10 nm specified by the supplier. Moreover, it should be noted that the test results  
12 reveal no significant difference in effective particle size among nanofluids with  
13 different volume concentrations.



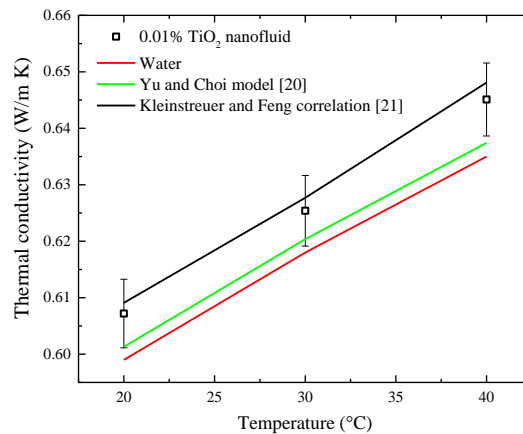
14 (a) (b)  
15 Fig. 2 (a) SEM image and (b) DLS measurement of effective particle size (0.01% TiO<sub>2</sub>-water  
16 nanofluid)

1 All the thermophysical properties of nanofluids were calculated or measured to be  
 2 used in the data reduction. The effective density and specific heat of the nanofluid are  
 3 calculated by

$$4 \quad \rho_{nf}(T) = (1 - \varphi)\rho_{bf}(T) + \varphi\rho_p(T) \quad (1)$$

$$5 \quad c_{p,nf} = \frac{\varphi \cdot (\rho c_p)_p(T) + (1 - \varphi)(\rho c_p)_{bf}(T)}{\rho_{nf}(T)} \quad (2)$$

6 The effective thermal conductivity of nanofluids were measured by using a transient  
 7 hot wire method under different temperatures and compared with the theoretical values  
 8 calculated with the model of Yu and Choi [20] and Kleinstreuer and Feng correlation  
 9 [21]. In this study, the measurement data of thermal conductivity are reasonably  
 10 correlated with the theoretical values from Kleinstreuer and Feng correlation [21].  
 11 Taking 0.1% TiO<sub>2</sub>-water nanofluid as an example, Fig. 3 shows the comparisons of the  
 12 measurement values and theoretical values under different temperatures. It can be found  
 13 that the relative errors between these two values are about 1%, which indicates that  
 14 model of Kleinstreuer and Feng correlation can [21] be used to predict the effective  
 15 thermal conductivity of TiO<sub>2</sub>-water nanofluids in this study.



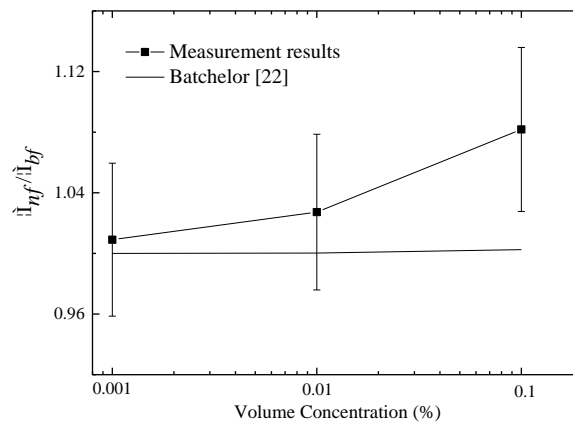
16

1 Fig. 3. Effective thermal conductivity of 0.1% TiO<sub>2</sub>-water nanofluid (error bar ±1%)

2 The effective viscosity of the nanofluids was measured using a rotating viscometer  
3 and the relative viscosity of the nanofluids at 20 °C is presented in Fig. 4, along with  
4 the well-known Batchelor correlation [22]

$$5 \quad \mu_{nf} = \mu_{bf} (1 + 2.5\phi + 6.25\phi^2) \quad (3)$$

6 From the figure, it can be found that the viscosity ratio of nanofluid to water increases  
7 with the increase of volume concentration and is higher than that obtained by Batchelor  
8 correlation [22].

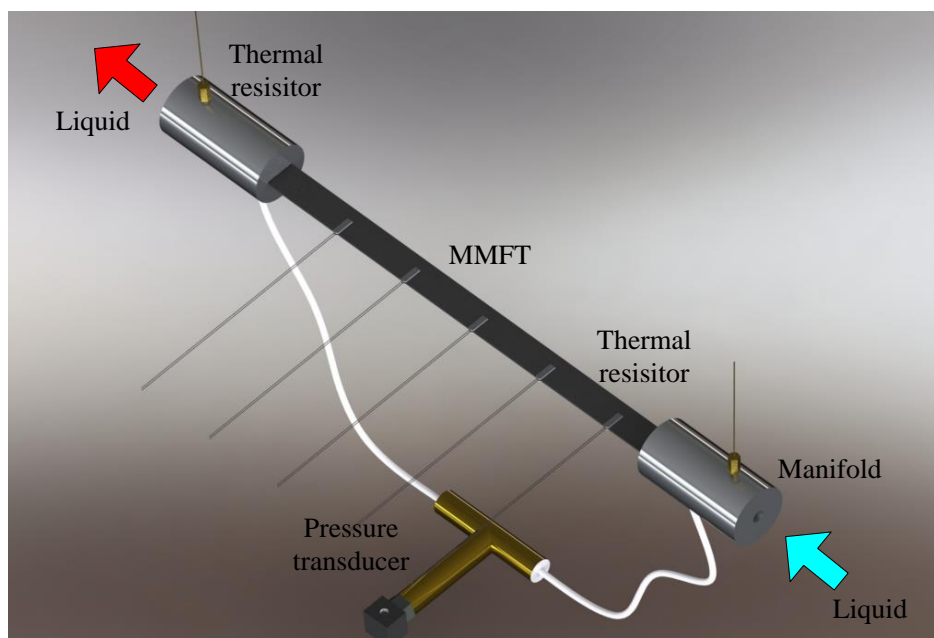


9  
10 Fig. 4 Effective viscosity of the nanofluid at various volume concentrations (error bar ± 5%)

### 11 3. Experimental apparatus

12 Fig. 5 shows the schematic of test section. As well known, a manifold which induce  
13 a uniform flow distribution in each channel and keep the fluid at a stable state is of  
14 crucial importance in the experimental test of parallel flow multilayer channels. In this  
15 study, the inlet and outlet of MMFT are connected with a manifold respectively by braze  
16 welding. Moreover, thermal resistors and pressure transducer are installed in the

1 manifolds to measure temperature and pressure difference of the test section inlet and  
2 outlet. Two heating plates are covered the upper and lower wall surfaces of MMFT to  
3 provide constant heat flux. Meanwhile, between the MMFT and heating plate, five flat  
4 thermal resistances are fixed with equidistance on the upper and lower surface of  
5 MMFT respectively to measure the axial wall surface temperature distribution. Finally,  
6 test section is tightly wrapped by 50 mm-thick thermal insulation material to achieve  
7 thermal insulation.



8

9

Fig. 5 Schematic of test section

10 The schematic of test system is presented in Fig. 6. The working fluid is driven from  
11 liquid storage tank by pump and then flow through filter, Coriolis mass flow meter and  
12 test section. In order to recover initial temperature, the working fluid heat in the test  
13 section enters into the double-pipe heat exchanger and cooled with water coolant  
14 provided by water chilling unit. Finally, working fluid flow back to liquid storage tank,

1 finishing the main loop.

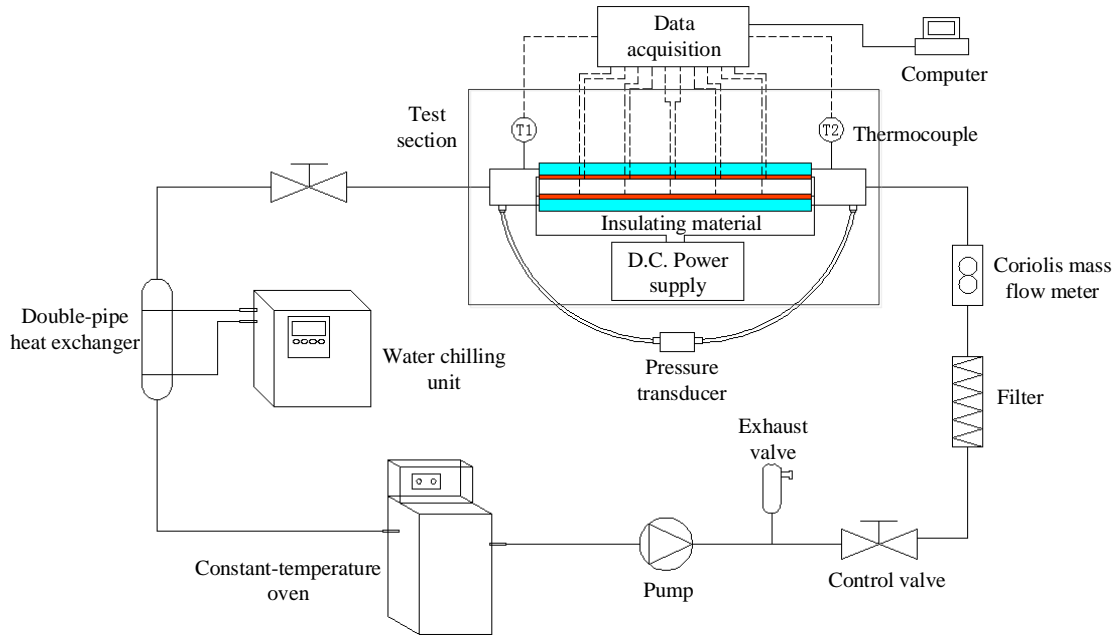


Fig. 6 Schematic of test system

## 4. Data analysis

### 4.1 Data reduction

The hydraulic diameter and aspect ratio of the rectangular minichannels are respectively defined as

$$D_h = \frac{4A}{c} = \frac{4(H_c W_c - A_{fin})}{2H_c + 2W_c + N(L_{fin} - W_{fin})} \quad \text{and} \quad \alpha = \frac{W_c}{H_c} \quad (4)$$

The total pressure differential in the test section is expressed as

$$\Delta p = \Delta p_{fri} + \Delta p_m \quad (5)$$

Frictional pressure loss is calculated using Eq. (7), and singular pressure loss ( $\Delta P_m$ ) is

1 calculated using the method mentioned in the Ref. [23].

$$2 \quad f = \Delta p_{fri} \frac{D_h}{L} \cdot \frac{\rho_f \cdot (H_c W_c - A_{fin})^2}{\dot{m}^2} \quad (6)$$

3 The heat gained by the fluid that is heated throughout the test section is expressed as

$$4 \quad Q = \dot{m} \cdot c_p \cdot (T_{f,out} - T_{f,in}) \quad (7)$$

5 The heat flux can be calculated from the heat gain by the fluid as

$$6 \quad q = \frac{Q}{L_c \cdot Pe} \quad (8)$$

7 According to the energy balance, the fluid temperature at longitudinal x position is  
8 calculated as

$$9 \quad T_f(x) = T_{f,in} + \frac{Q}{\dot{m} \cdot c_{p,f}(x) \cdot L} \cdot x \quad (9)$$

10 The local heat transfer coefficient is given by

$$11 \quad h(x) = \frac{q}{T_w(x) - T_f(x)} \quad (10)$$

12 Based on the energy balance, heat loss rate is defined as

$$13 \quad \varepsilon = \frac{VI - \dot{m} \cdot c_p \cdot (T_{f,out} - T_{f,in})}{VI} \quad (11)$$

14 The local Nusselt number is defined as

$$15 \quad Nu(x) = \frac{h(x) \cdot D_h}{k_f(x)} \quad (12)$$

16 The local Reynolds number is defined as

1 
$$Re(x) = \frac{\dot{m} \cdot D_h}{A \cdot \mu_f(x)} \quad (13)$$

2 Accordingly, the averaged Nusselt number and Reynolds number are given by

3 
$$\overline{Nu} = \sum_{n=1}^{10} Nu_n \quad \text{and} \quad \overline{Re} = \sum_{n=1}^{10} Re_n \quad (14)$$

4 **4.2 Uncertainties analysis**

5 In this study, the uncertainties in temperature and mass flow rate measurements are  
 6  $\pm 0.1^\circ\text{C}$  and  $\pm 0.2\%$ , respectively. The error associated with the pressure difference  
 7 transducer is  $\pm 0.25\%$ . The uncertainties of the parameters calculated by using  
 8 directly measured values, such as  $f$ ,  $Nu$ , and  $Re$ , are generally denoted as  $\delta z$  and  
 9 calculated as

10 
$$z = f(y_1, y_2, \dots, y_n)$$

11 
$$\delta z = \left[ \left( \frac{\partial z}{\partial y_1} \delta y_1 \right)^2 + \left( \frac{\partial z}{\partial y_2} \delta y_2 \right)^2 + \dots + \left( \frac{\partial z}{\partial y_n} \delta y_n \right)^2 \right]^{\frac{1}{2}} \quad (15)$$

12 where  $\delta y_1, \delta y_2, \dots, \delta y_n$  are the uncertainties of directly measured values.

13 The test ranges and uncertainties of some relevant parameters are summarized in

14 Table 1.

15 Table 1 Operating conditions

	value	uncertainty		value	uncertainty
G (Kg/h)	10-405	0.2%	$D_h$ (mm)	2.02-2.05	2.0-2.5%
$A_{fin}$ (mm <sup>2</sup> )	0.08-0.31	3.5-7%	Re	129-5650	2.2-11.2%



$T_w$ (K)	294-315	0.1K	$f$	0.025-0.6	3.2-15.2%
$T_f$ (K)	292-302	0.1K	Nu	4.57-52	3.6-15.9%
Q (W)	185-208	3.1-8.0%	PEC	0.93-2	4.6-17.2%

1

## 2 **5. Results and discussion**

3 For the experimental investigations, the pressure drop and heat transfer  
4 characteristics of Sample 1 were firstly studied, which aims to verify the integrity of  
5 the experimental facility and provide baseline information to compare the experimental  
6 results using different enhancement techniques. Next, research just using one  
7 enhancement technique were performed. Specifically, the pressure drop and heat  
8 transfer characteristics of water in sample 2-5 and nanofluids in sample 1 were studied.  
9 Finally, the experimental results using two combined enhancement techniques were  
10 obtained and then compared with those of previous experiments.

### 11 **5.1 Experiments with sample 1**

12 The friction factor is plotted as functions of Reynolds number in Fig. 5, together with  
13 the Shah and London [24] correlation for a fully developed laminar flow in rectangular  
14 channels,

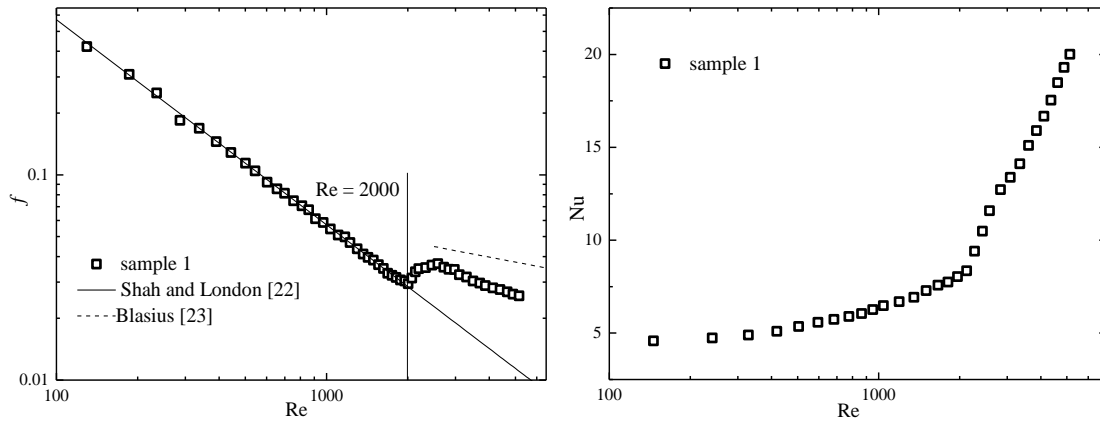
$$15 \quad f \cdot \text{Re} = 96(1 - 1.3553 \cdot \alpha + 1.9467 \cdot \alpha^2 - 1.7012 \cdot \alpha^3 + 0.9564 \cdot \alpha^4 - 0.2537 \cdot \alpha^5) \quad (16)$$

16 The well-known Blasius [25] correlation for fully developed turbulent flows,

1

$$f = 0.316 \cdot \text{Re}^{-0.25} \quad (17)$$

2



3

Fig. 7(a) Friction factor and (b) Nusselt number versus Reynolds number for sample 1

4

5

6

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8

From Fig. 7(a), it can be found that the test data of sample 1 agrees excellently with the theoretical value obtained by Shah and London correlation in the laminar and is smaller compared with Blasius correlation in the turbulent region. The laminar-turbulent transition is clear visible for about  $Re_{cr} = 2000$ , which is an accepted value for macrotube.

9

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13

In Fig. 7(b), the Nusselt numbers are plotted against the Reynolds number for sample 1. The Nusselt numbers increase with the increase of the Reynolds number. As  $Re$  increases, the locations where the slope of the test data changes occurs at about  $Re = 2000$ , which corresponds to the onset of transition to turbulent. This result is consistent with above conclusion obtained from the friction factor.

14

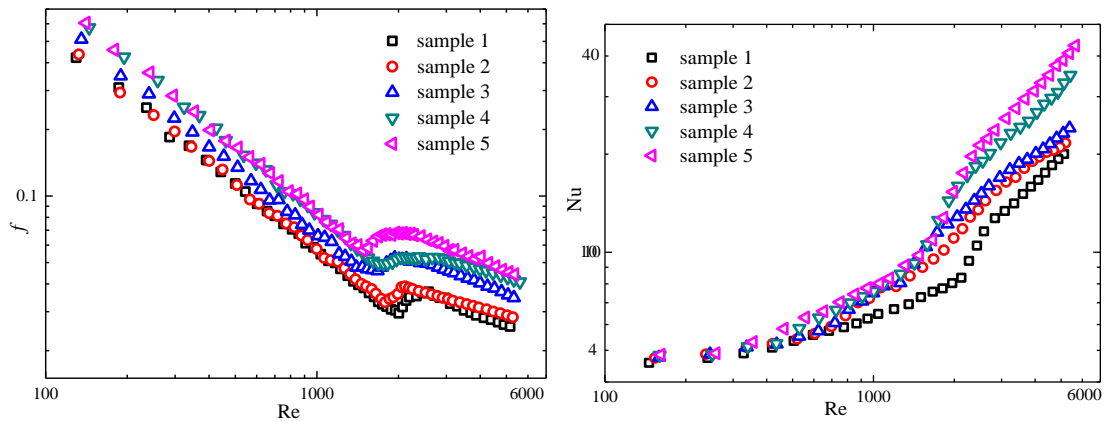
## 5.2 Experiments with one enhancement technique

15

16

In this section, flow and heat transfer characteristics of sample 2-5 using water as working fluid were investigated. Fig. 8(a) shows friction factors of sample 1-5. It is

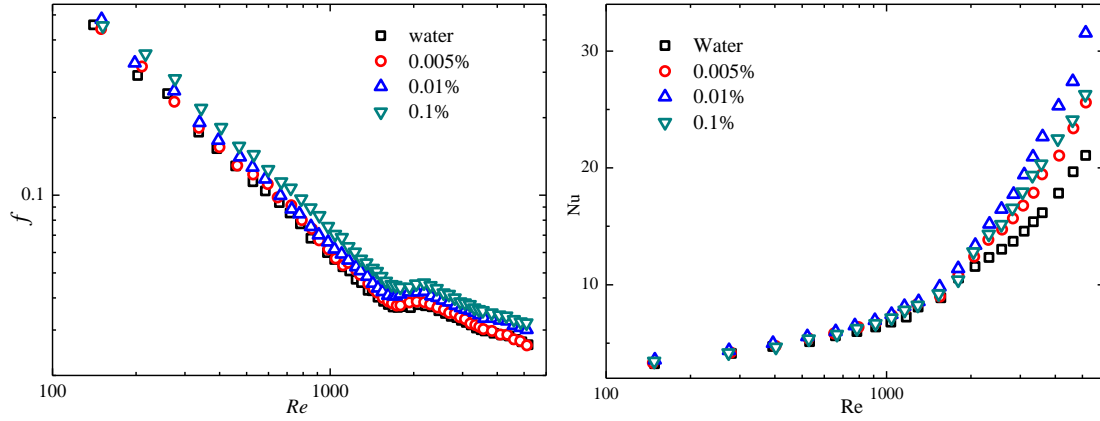
1 observed that friction factor of all samples with the fin structure is higher than that of  
 2 smooth tube, sample 1 and the friction factor increases with the increase of fin number.  
 3 From Fig. 8(a), it is further observed that for sample 2-5 with the fin structure, an earlier  
 4 laminar-turbulent transition occurs at  $Re = 1500-1900$  compared with the result of  
 5 sample 1. This behavior could be attributed to the more significant disturbance in the  
 6 flow caused by fin structure. The earliest laminar-turbulent transition occurs about at  
 7  $Re = 1500$  for sample 5. Fig. 8(b) shows averaged Nusselt numbers of sample 1-5.  
 8 Nusselt number of the samples with the fin structure is higher than that of sample 1.  
 9 The Nusselt number also increases with the increase of fin number and Nusselt number  
 10 can increase by up to 135% for sample 5.



11  
 12 Fig. 8(a) Friction factor and (b) Nusselt number versus Reynolds number for sample 1-5

13 Flow and heat transfer characteristics of sample 1 using  $TiO_2$ -water nanofluids as  
 14 working fluid were also investigated next. In Fig. 9(a), friction factors of nanofluids at  
 15 various volume concentrations are plotted against the Reynolds number. The friction  
 16 factors of nanofluids are all higher than those of water and increase with the increase  
 17 of volume concentrations. The average Nusselt numbers of nanofluids are plotted

1 against the Reynolds number at various volume concentrations in Fig. 9(b). As shown  
2 in the figure, Nusselt numbers of nanofluids also are all higher than those of water,  
3 especially in the turbulent region. Furthermore, at  $\phi \leq 0.01\%$ , Nusselt numbers  
4 increase with the increase in volume concentration; at  $\phi \geq 0.01\%$ , Nusselt numbers  
5 decrease with the increase in volume concentration, which indicates an optimal volume  
6 concentration of 0.01% for heat transfer performance. This phenomenon is consistent  
7 with the experimental results in Ref. [26-27]. As explained in Ref. [27], this  
8 phenomenon is attributed to the combined effect of the increases in thermal  
9 conductivity and viscosity. With the increase in volume concentration, thermal  
10 conductivity and viscosity both increase. The former can strengthen heat transfer,  
11 whereas the latter can weaken heat transfer due to the increase in the thickness of the  
12 thermal boundary layer. At  $\phi \leq 0.01\%$ , the positive effects of the thermal  
13 conductivity enhancement in the present work overcome the negative effect of viscosity.  
14 The opposite cases are true at  $\phi \geq 0.01\%$ . On the other hand, the energy exchanges  
15 between particles and particles, particles and water, and particles and wall resulting  
16 from the chaotic movement of nanoparticles enhance heat transfer. With the increase in  
17 volume concentration, more particles exist per unit volume. In the experiments  
18 conducted in this work, such kind of energy exchanges seem to weaken as the particle  
19 number increases to a certain value because large particle numbers may restrict the  
20 chaotic movement of nanoparticles. Nevertheless, the mechanism of the microscopical  
21 movement of nanoparticles for enhancing heat transfer need be studied further.



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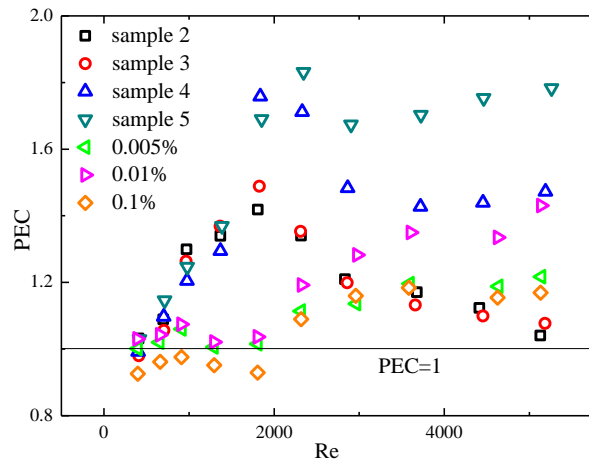
2 Fig. 9(a) Friction factor and (b) Nusselt number versus Reynolds number of nanofluids in sample 1

3 From above experimental results, it can be found that regardless of which  
 4 enhancement technique used, heat transfer can be enhanced but tend to increased  
 5 pressure drop. Thus, as a comprehensive assessment of nanofluid performance in terms  
 6 of heat transfer enhancement, a performance evaluation criterion (PEC) based on the  
 7 same pumping power consumption is defined as [28]

$$8 \quad PEC = \frac{Nu_{nf, samples 2-5} / Nu_{water, sample 1}}{(f_{nf, sample 2-5} / f_{water, sample 1})^{1/3}} \quad (18)$$

9 Fig. 10 presents the PEC values of samples 2-5 and nanofluids with different volume  
 10 concentration. As shown in the figure, PEC values of sample 2-5 are all higher than 1,  
 11 which demonstrates that using micro fin does enhance heat transfer performance.  
 12 Among sample 2-5, sample 5 has the highest PEC values and maximum value of PEC  
 13 is 1.83 for sample 5 at about  $Re = 2300$ . Moreover, for using nanofluids as working  
 14 fluids, except for 0.1% nanofluids and  $Re < 2000$ , the nanofluids could enhance heat  
 15 transfer performance without huge penalty of increased pumping power under other  
 16 conditions. 0.01% nanofluid has the best PEC in all nanofluids and the maximum value

1 is 1.43 occurring at  $Re = 5100$ .



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3 Fig. 10 PEC values versus Reynolds number for samples 2-5 and nanofluids with different  $\phi$

#### 4 **5.3 Experiments with two combined enhancement techniques**

5 In this section, the enhanced heat transfer performance were studied by using  
6 nanofluids in MMFTs with fin structures and comparing with the initial results of water  
7 in sample 1. The friction factors of nanofluids in sample 2-5 are plotted as functions of  
8 Reynolds number in Fig. 11 respectively. Compared with water in sample 1, nanofluids  
9 in samples with fin structures have the higher friction factors and show the earlier  
10 laminar-turbulent transition which is attributed to the effects of enhanced disturbance  
11 caused by micro fin structures.

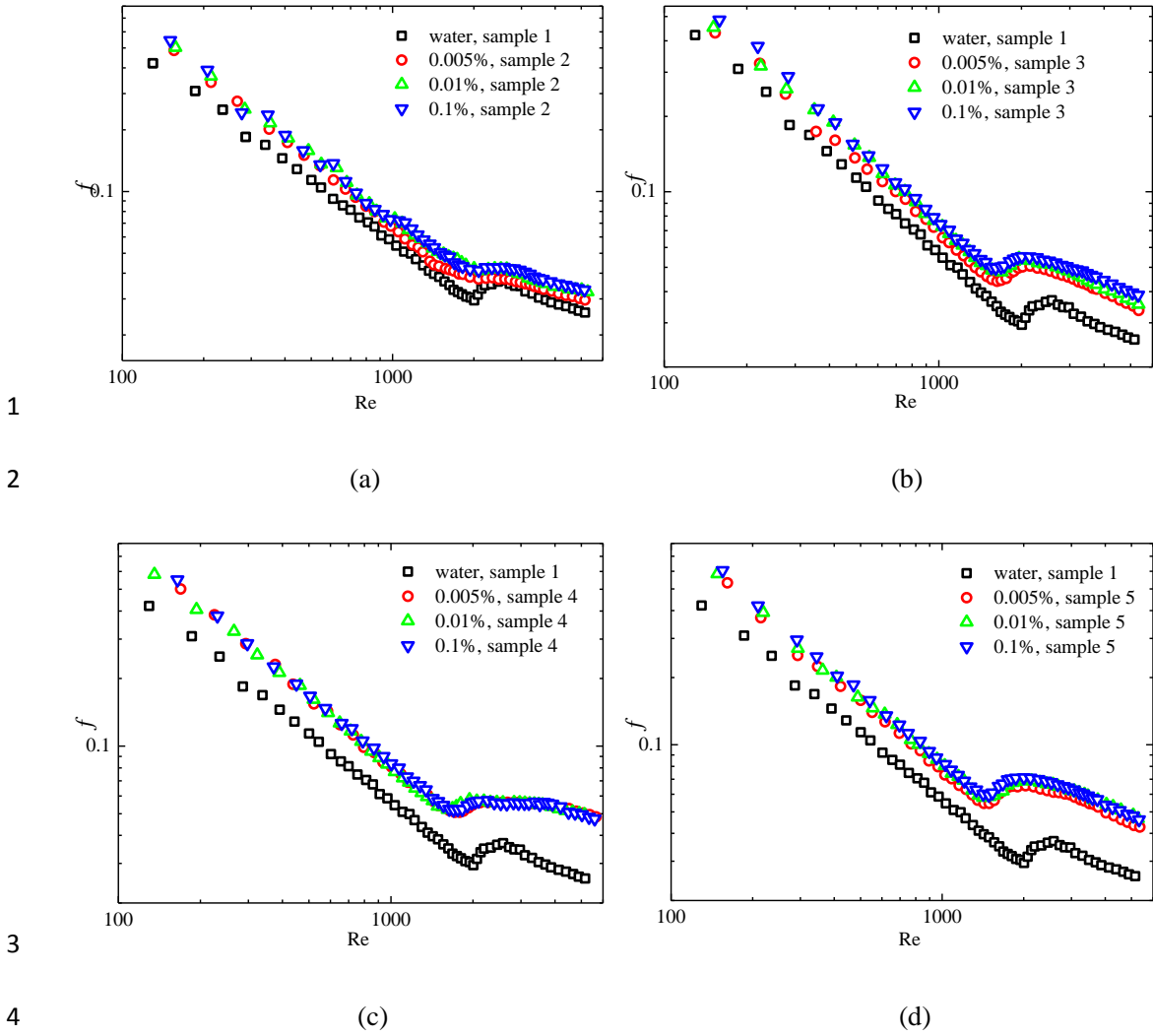
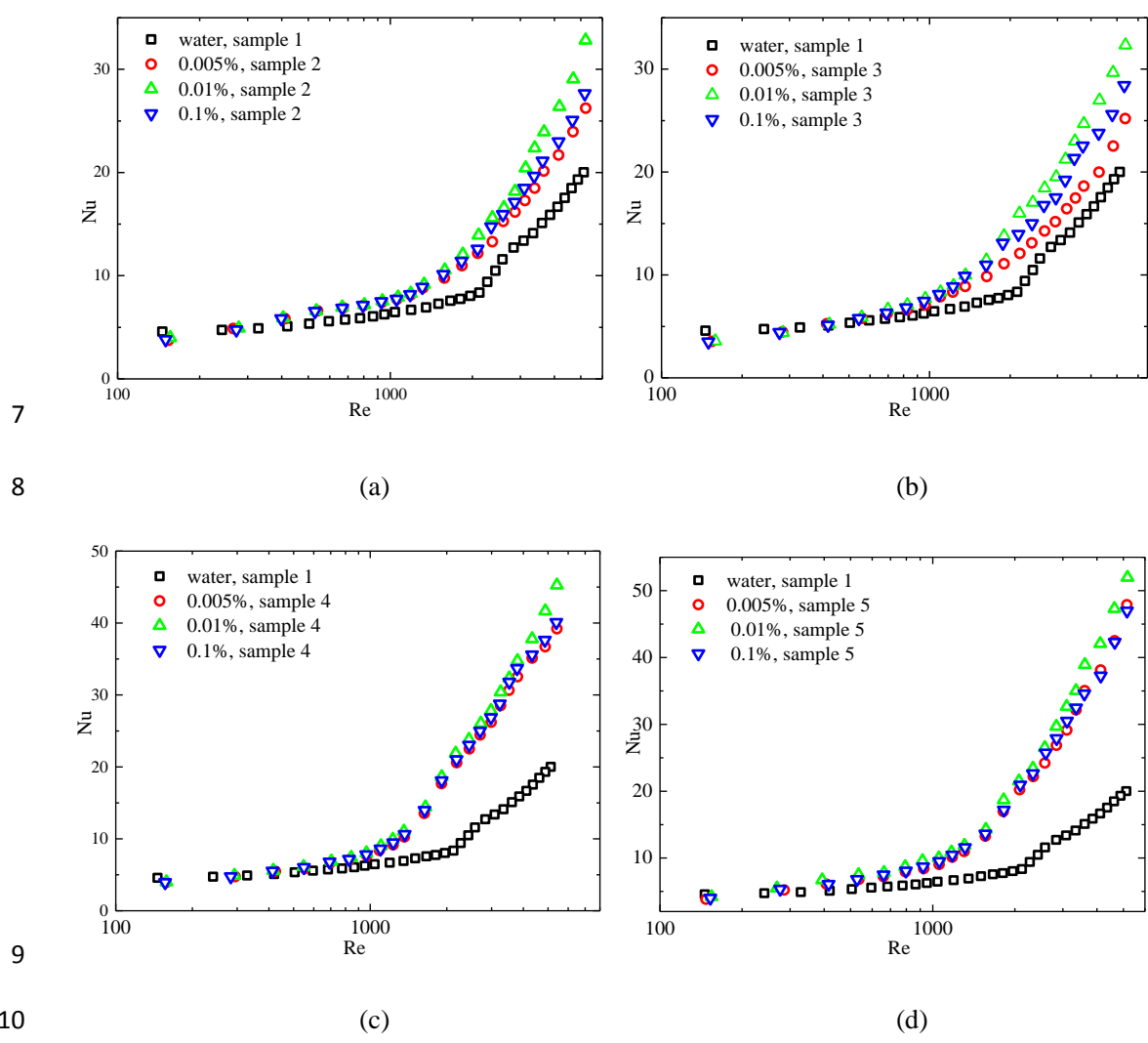


Fig. 11 Comparison of friction factors between water in sample 1 and  $\text{TiO}_2$ -water nanofluids in (a) samples 2, (b) sample 3, (c) sample 4 and (d) sample 5

Table 2 Average increase of  $f$  using enhancement techniques with respect to the water in sample 1

	Sample 1	Sample 2	Sample 3	Sample 4	Sample 5
Water	—	3.5%	21.2%	36.9%	43.9%
0.005% nanofluid	2.9%	16.4%	31.7%	58.2%	61.9%
0.01% nanofluid	10.9%	26.1%	41.4%	61.4%	71.9%
0.1% nanofluid	21.7%	30.0%	47.6%	65.7%	77.5%

1 To illustrate the effect of enhancement techniques on flow characteristic, Table 2  
 2 summarizes the increase in the friction factor of nanofluids in sample 2-5 as with  
 3 respect to the water in sample 1. From the comparison, it can be found that the friction  
 4 factor increases with the increases of the volume concentrations of nanofluids as well  
 5 as the fin number. A maximum 77.5% average increase of friction factor occurs for 0.1%  
 6 nanofluid in sample 5.



11 Fig. 12 Comparison of Nusselt numbers between water in sample 1 and TiO<sub>2</sub>-water nanofluids in  
 12 (a) samples 2, (b) sample 3, (c) sample 4 and (d) sample 5

13 Fig. 12 shows Nusselt numbers of nanofluids in sample 2-5 compared with those of



1 water in sample 1. As shown in the figure, all Nusselt numbers obtained by using two  
2 combined enhancement techniques are much higher than those of water in sample 1,  
3 especially in the turbulent region. Similarly, the increases of Nusselt number in laminar  
4 and turbulent regions for nanofluids in sample 2-5 as with respect to the water in sample  
5 1 are listed in Table 3 respectively. The quantified analysis of heat transfer enhancement  
6 shown in Table 3 indicate that combination of two enhancement techniques could  
7 further increase the Nusselt number compared with just using one enhancement  
8 technique. From Table 3, it can be further found that for each working condition, the  
9 increase of Nu in turbulent region is much higher than that in laminar region. As  
10 concluded in Ref. [29], two main mechanisms caused by micro fin structure can be used  
11 to explain the heat transfer enhancement. Specifically, based on continuous fin structure  
12 along axial direction, the increase in heat transfer area due to exist of micro fin is  
13 dominant in the laminar region, while more disturbances caused by fin structure has  
14 more significant effect on heat transfer enhancement in the turbulent region. In this case,  
15 micro fin structure causes more disturbances in turbulent flow, which contributes to  
16 more intense irregular movement of nanoparticles. Due to the stronger chaotic  
17 movement of nanoparticles, the energy transport among the wall, fluid, and particles  
18 become stronger and thereby improve heat transfer performance. Therefore, the heat  
19 transfer enhancement in turbulent region is more remarkable.

20 Based on the consideration about heat transfer of nanofluids, from Table 3, it also  
21 can be found that heat transfer performances of nanofluids mainly depend on two  
22 factors, nanofluid concentration and fin structure (fin number), which indicates that

1 these two factors both have significant effects on energy transport of nanofluids. From  
 2 the further comparison in Table 3, it can be found that the average increase of Nusselt  
 3 number increases up to 21% for just changing the concentrations, while the average  
 4 increase of Nusselt number increases up to 91% for just changing the fin numbers.  
 5 Therefore, it seems that fin structure has more significant effects on heat transfer  
 6 performance of nanofluids than nanofluids concentration in this study.

7 Table 3 Average increase of Nusselt numbers using enhancement techniques with respect to the  
 8 water in sample 1

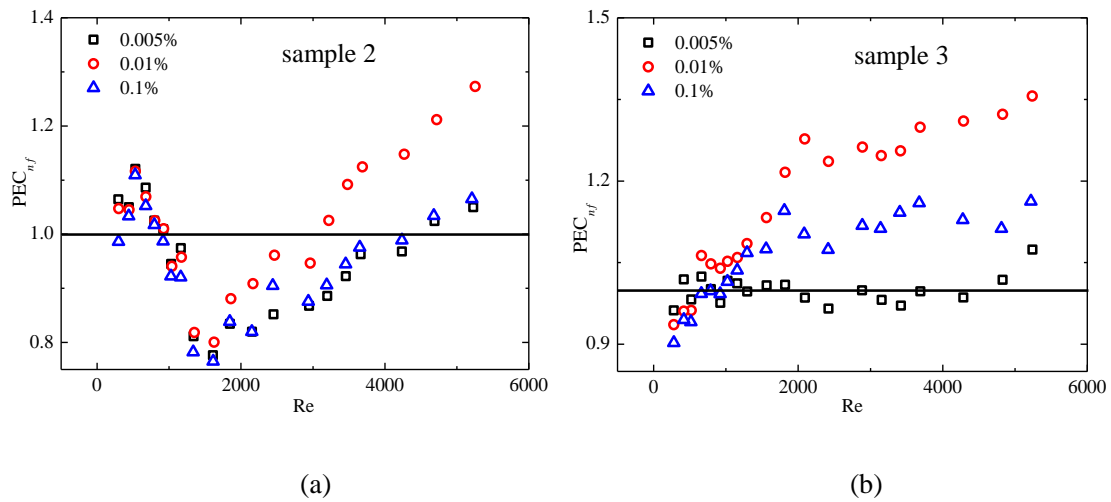
	water		0.005% nanofluid		0.01% nanofluid		0.1% nanofluid	
	Lam.	Tur.	Lam.	Tur.	Lam.	Tur.	Lam.	Tur.
Sample 1	—	—	3.4%	15.7%	8.3%	33.5%	4.0%	21.2%
Sample 2	12.4%	22.2%	13.8%	31.6%	22.7%	55.1%	19.3%	39.2%
Sample 3	18.8%	32.7%	18.9%	34.6%	23.2%	59.4%	19.8%	42.1%
Sample 4	24.8%	77.3%	32.0%	107.2%	38.9%	123.7%	34.7%	112.0%
Sample 5	30.9%	112.7%	40.6%	125.0%	53.6%	146.1%	44.4%	128.1%

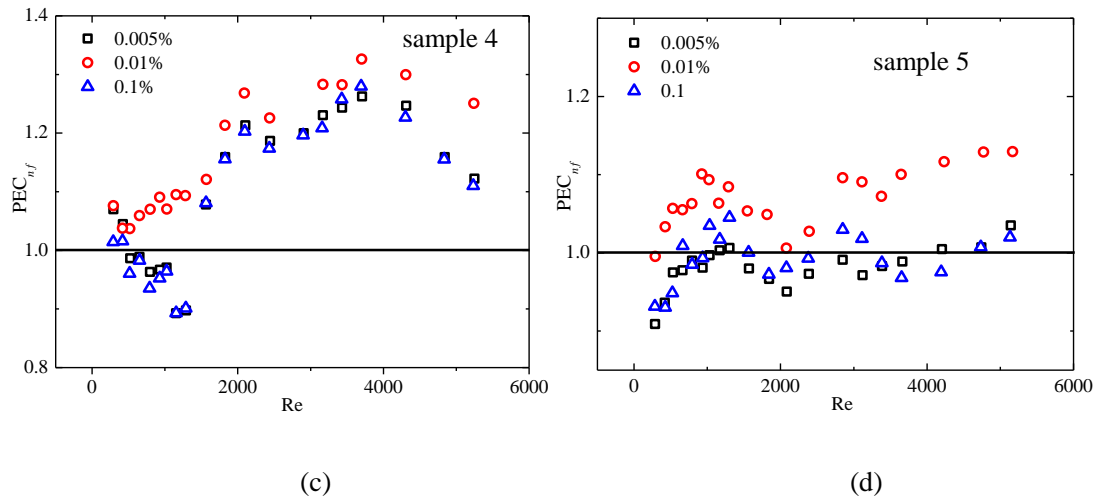
9 The optimal volume concentration is also 0.01% for nanofluids in each sample,  
 10 which is consistent with the conclusion obtained in the smooth tube-sample 1 and  
 11 Nusselt number increases with increase of fin number. The Nusselt number of 0.01%  
 12 nanofluid in sample 5 are highest while Nusselt number in laminar and turbulent region  
 13 can averagely increase by 53.6% and 146.1% respectively. Nusselt number increases  
 14 by up to 158% at about  $Re = 3600$ .

1 From above experimental results, it can be concluded that although using nanofluids  
 2 as work fluid in the MMFT with fin structures could increase Nusselt number, it also  
 3 accompany with the higher pressure drop. Therefore, in order to discuss whether using  
 4 nanofluids in MMFT with fin structure (sample 2-5) can further improve heat transfer  
 5 performance compared with using water in sample 2-5, a new parameter  $PEC_{nf}$  is  
 6 introduced and defined as

$$7 \quad PEC_{nf} = \frac{Nu_{nf, samples2-5} / Nu_{nf, sample1}}{(f_{nf, sample2-5} / f_{nf, sample1})^{1/3}} \quad (19)$$

8 From the Eq. (20), it could be found that the baseline data is the test results of nanofluids  
 9 in sample 1 when the  $PEC_{nf}$  is calculated. Fig. 13 shows the  $PEC_{nf}$  values of sample 2-  
 10 5. As shown in the figure,  $PEC_{nf}$  is irregular with the varying of Reynolds number in  
 11 term of each working condition. Moreover, not all the  $PEC_{nf}$  values are higher than 1,  
 12 which illustrates that adding nanofluids into MMFT with fin structure to further  
 13 improve heat transfer performance is not universally applicable. Specifically, a better  
 14 heat transfer performance can be obtained by using 0.01% nanofluids in sample 3-5.





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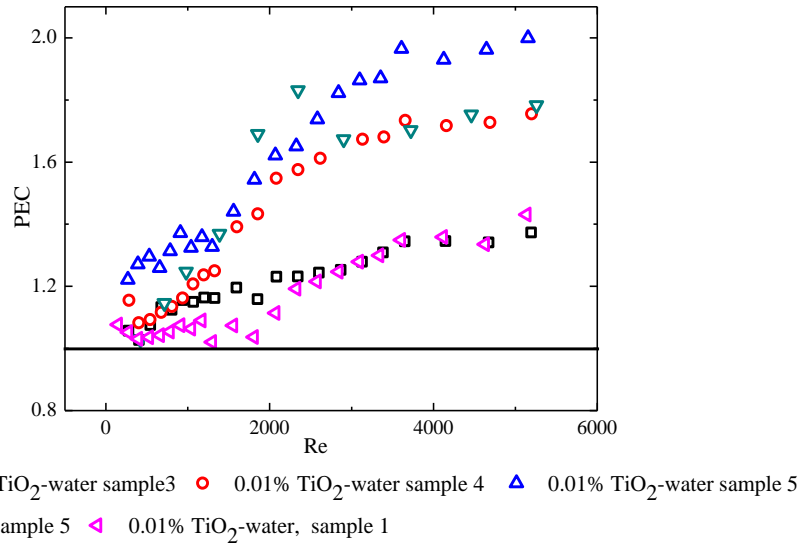
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Fig. 13  $PEC_{nf}$  values versus Reynolds number in (a) sample 2, (b) sample 3, (c) sample 4 and (d) sample 5

Based on above conclusion, PEC values under several potential optimal working condition in this study are presented in Fig. 14, including PECs of 0.01% nanofluid in sample 1 and sample 3-5 and water in sample 5. Generally, 0.01% nanofluid in sample 5 has the highest PEC values. The maximum PEC values of 0.01% nanofluid in sample 5 are 2.0 as  $Re = 5150$ . Moreover, using water in sample 5 also can achieve the good performance, which is attributed that PECs of water in sample 5 are higher than those of other working conditions except for 0.01% nanofluid in sample 5 and are even higher than those of 0.01% nanofluid in sample 5 as Reynolds number ranges about from 1700 to 2500. From the Fig. 14, it can be further found that micro fin structure has the better heat transfer performance than nanofluids in term of just using one enhancement technique.



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Fig. 14 Comparison of PEC under several conditions

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Finally, the PECs obtained under two optimal working conditions (0.01% nanofluid and water in sample 5 respectively) in this study are compared with those of other research, which are shown in Fig. 15. From the comparison, it can be found that two sets of PEC values in this study increase with the increase of Reynolds number in the turbulent region, which is attributed that improvement of heat transfer is higher than the increase of pressure drop. This behavior is much different with the results of other research shown in Fig. 15, which presents the decrease of PEC with the increase of Reynolds number in the larger Reynolds numbers (turbulent region). In Ref. [30-34], different kinds of inserts including twist, porous medium, coiled wire and twisted-ring used as turbulators were installed in the tube to enhance heat transfer performance. As well-known, the heat transfer enhancement caused by turbulator is more significant in laminar region. However, as mentioned above, heat transfer enhancements in this study that come from either energy transfer between nanoparticles and fluids or disturbances caused by fin structure both are stronger in the turbulent region. Therefore, different

1 enhancement mechanisms cause different growth characteristics of heat transfer  
 2 performance, and thereby the trend of PEC in present study is quite different from those  
 3 in the research using inserts as turbulator [30-34]. Comparing with the results in Ref.  
 4 [35-36] where only using nanofluid technique was used, it can be found that  
 5 combination of two enhancement techniques could obtain better heat transfer  
 6 performance. Unfortunately, due to the restriction of pressure drop, the test data in  
 7 larger Reynolds numbers could not be measured in this study. The corresponding  
 8 research need to be further studied and then compared with the results in similar  
 9 research. Generally, using enhancement technique in this study shows a good PEC  
 10 value and applicability to improve the heat transfer performance.

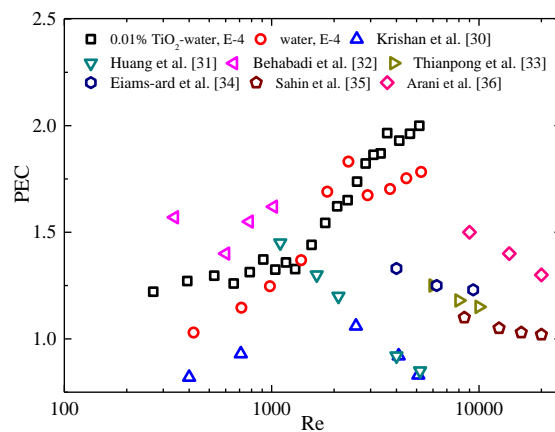


Fig. 15 Comparison of PEC values in this study with those of other research

## 6. Conclusion

The enhanced heat transfer performances by using two enhancement techniques (micro fin structure and nanofluid) both respectively and conjunctively were studied. Through testing the friction factor, Nusselt number as well as PEC, the key findings can

1 be concluded as follows.

2 (1) The Nusselt number and friction factor in samples with micro fin structures  
3 increase with the increase of fin numbers and also are both higher than those in smooth  
4 sample. Moreover, using TiO<sub>2</sub>-water nanofluids as working fluids also can improve the  
5 heat transfer but tend to increase pressure drop.

6 (2) Either micro fin structure or nanofluid is a suitable enhancement technique to  
7 improve the heat transfer performance in MMFT. Furthermore, from the comparison of  
8 these two enhancement techniques, using samples with micro fin structure has the  
9 higher PEC values than using nanofluid as working fluid in smooth sample.

10 (3) Compared with water in the sample with fin structure, only using nanofluid with  
11 volume concentration of 0.01% instead of water can further enhance the heat transfer  
12 generally. The optimal working condition is running 0.01% nanofluid in sample 5.  
13 Under this working condition, Nusselt number increases by up to 158% at about  $Re =$   
14 3600 and the maximum PEC value is 2.0 as  $Re = 5150$ .

15 (4) An optimal heat transfer scheme was proposed based on experimental results in  
16 this study. Generally, alone employ of micro fin technique is recommended due to its  
17 excellent heat transfer performance as well as the economic consideration. The  
18 combination of two enhancement techniques suggests to be employed in the turbulent  
19 region to face the demand of higher heat flux removal rate.

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