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A numerical model to evaluate the flow distribution in a large solar collector field

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Abstract

This study presents a numerical model to evaluate the flow distribution in a large solar collector field, with solar collectors connected both in series and in parallel. The boundary conditions of the systems, such as flow rate, temperature, fluid type and layout of the collector field can be easily changed in the model. The model was developed in Matlab and the calculated pressure drop and flow distribution were compared with measurements from a solar collector field. A good agreement between model and measurements was found. The model was then used to study the flow distribution in different conditions. Balancing valves proved to be an effective way to achieve uniform flow distribution also in conditions different from those for which the valves were regulated. For small solar collector fields with limited number of collector rows connected in parallel, balancing valves are not strictly necessary if the pressure drop across the collector rows is much higher than the pressure drop along the longest distribution pipe.

Keywords: solar collector, solar collector field, flow balancing, flow distribution, parallel connection.

1. Introduction

1.1. Background

An increasing number of large solar collector fields have been built in Europe in the last years. The main market for this technology has been Denmark, with 77% of the total collector area installed in European large scale solar heating plants at the end of 2015 (Mauthner et al., 2016). This development has been driven by some specific factors, such as high taxation on fossil fuels and widespread use of district heating (DH), to which large collector areas can be connected (Furbo et al., 2015). At the end of 2015, Denmark had more than 800,000 m² of solar collector fields, and more plants are expected to be installed in the next years (Figure 1). Also the size of the collector fields has been increasing. In 2015 the current largest collector field was installed in Vojens, with a collector area of 70,000 m² (Mauthner et al., 2016). In 2016 a 150,000 m² collector field is expected to be completed in Silkeborg (EnergySupply, 2016).
The larger the solar collector field and the number of collector rows, the higher the risk of non-uniform flow distribution from one row to another and decreased thermal performance. In fact, identical collector rows supplied with different flow rates reach different outlet temperatures. Mixing flows at different temperatures causes a lower temperature rise across the collector field compared to the case with uniform flow distribution and identical outlet temperatures. If different rows have a different number of collectors (and different aperture areas), these should be supplied by different flow rates, proportional to the collector row area, resulting in the same outlet temperature for all rows.

1.2. Literature review

Flow distribution in solar thermal systems has been the topic of many investigations, both at collector level and array level. The negative effect of the flow maldistribution on the thermal performance of a single collector with parallel channels was investigated by Chiou (1982). He presents a method to determine how much the collector efficiency is penalized by the flow maldistribution. Wang and Wu (1990) developed a numerical model to predict the flow distribution in collector arrays with vertical pipes, both in U-type and Z-type configuration. Compared to the Z-type configuration, the U-type presents a higher maldistribution, with the flow rates in the absorber pipes decreasing monotonically with the distance from the array inlet. The same trend is found by Jones and Lior (1994), who considered a single collector with vertical pipes, instead of an entire array. Weitbrecht et al. (2002) present both an experimental and analytical study on the flow distribution in a Z-type collector in isothermal conditions, verifying the results from Wang and Wu (1990) and Jones and Lior (1994). They conclude that a more uniform flow distribution is achieved when the pressure losses in the absorber pipes are much higher than in the manifolds. Fan et al. (2007) studied the flow and temperature distribution in a solar collector for large collector fields applications. Calculations with a CFD model and experimental measurements are compared. The authors conclude that the flow distribution is determined by friction (and hence buoyancy can be neglected), if the velocity in the collector pipes is high compared to the temperature rise across the collector. Bava and Furbo (2015) propose a numerical model to evaluate the pressure drop and flow distribution in a collector with horizontal U-connected pipes. Based on the findings of Fan et al. (2007), the authors argue that in large collector fields for DH applications the relation between the fluid velocity in the absorber pipes and the temperature rise across the collector is such that buoyancy can be neglected. The model was validated against measurements carried out on a collector for solar assisted DH plants.

Uniform flow distribution is of great importance also for the efficient operation of the entire collector field, but it is often overlooked (Dorantes et al., 2014). Ideally, the layout of a collector array should keep the pipe lengths as short and the flow distribution as uniform as possible. Shorter pipe lengths entail lower material
and installation costs, lower thermal losses from the distribution lines, reduced pressure drop and consequently lower pumping power. Since reduction in pipe length and uniform flow distribution cannot be optimized simultaneously, a compromise between the two needs to be found. Rohde and Knoll (1976) investigate different hydraulic solutions for minimizing the flow maldistribution in a collector field of 12 collector rows connected in parallel. These solutions include various size manifolds, orifices and balancing valves. The last two are proposed as the best solutions, both in terms of performance and cost. It is noted that a configuration of valve settings maintains the desired flow distribution only at a certain flow rate. Finally, laminar flow produces less uniform flow distribution than turbulent flow. Also Knabl et al. (2014) present different solutions to achieve uniform flow distribution. A solution consists of maintaining a constant pipe diameter in the supply and return pipe. An example is represented by the first large collector fields built in Sweden, such as Falkenberg (1989) and Nykvarn II (1991). Another possibility is to adopt a Z-configuration (or reverse return). Though, both these solutions entail higher costs due to the additional material. Balancing valves can be installed in each row, but these increase the investment cost, installation time and maintenance (in case of defective valves). Installing pipes with different diameters within each collector row is a cheaper solution, but must be calculated in advance exactly, as a later adjustment would be very expensive.

1.3. Solar collector fields for DH applications

In Denmark the majority of large collector fields are installed next to a heating plant supplying a DH network. The inlet temperature to the collector field is determined by the return temperature from the DH network. Typical return temperatures are in the interval 35-45 °C (Windeleff and Nielsen, 2014). The control strategy of the collector field aims at reaching a constant outlet temperature, by continuously regulating the total flow rate based on the solar irradiance (Heller, 2000). The desired outlet temperature is the DH supply temperature. Typical supply temperatures are in the interval 70-85 °C (Windeleff and Nielsen, 2014). The temperature drop across the heat exchanger should be considered. When sufficiently high temperatures cannot be reached, for example in periods with low solar irradiance, the additional energy is provided by an auxiliary energy source.

Most of the Danish collector fields are made of 12-14 m² flat plate harp collectors (Windeleff and Nielsen, 2014). The diameter of the supply and return pipes to and from the collectors is progressively decreased as the fluid is diverted to the collector rows. A uniform flow distribution across the collector field is achieved by installing balancing valves at the inlet of each collector row. Unlike orifices, the setting of these valves can be changed if needed, so providing a higher flexibility. Additionally, if coupled with an on/off valve at the row outlet, balancing valves can be used for maintenance purposes. For example, in case of leakage in a row, this can be isolated, while the rest of the collector field continues its normal operation. The setting of the valves is usually chosen in such a way that the desired flow distribution is achieved in nominal operating conditions, i.e. high solar irradiance, high flow rate, nominal inlet and outlet temperatures. As found by Rohde and Knoll (1976), these valve settings provide a perfectly uniform flow distribution only in a specific operating condition, while deviations can be expected in other conditions.

Being able to evaluate these deviations is of great interest, as it allows understanding how the collector field performance is affected by off-design conditions. Additionally, it is of particular importance with respect to critical conditions such as incipient stagnation and anti-freezing mode. A collector row supplied with a lower flow rate is more likely to experience stagnation or freezing. This represents a risk for the entire system and penalizes the overall performance. If one row is not supplied by the proper flow rate and so reaches too high temperatures, this may trigger an alarm signal, which interrupts the normal operation of the collector field with consequent loss of useful energy production. On the other hand, when the system switches to anti-freezing mode, the solar collector fluid (usually 30-40% propylene glycol/water mixture (Windeleff and Nielsen, 2014)) is circulated across the collector field. Rows supplied with lower flow rates are more likely to incur into freezing in case of extended cold periods.

The aim of this study was to develop a numerical model for calculating the flow distribution across a large collector field. The reliability of the model was verified by comparing its results against experimental measurements. Different scenarios were treated to analyze how different operating conditions, layouts and design choices can affect the flow distribution. The Matlab source code of the model is publicly available online (Bava, 2016) and can be edited to treat different configurations.
2. Material and method

2.1. Numerical model

2.1.1 Pressure drop correlations

To evaluate the flow distribution in a parallel hydraulic system, the relation between flow rate and pressure drop across each component needs to be known. In a parallel hydraulic system, the fluid flow distributes so that the pressure drop along each hydraulic path is the same. Consequently, hydraulic paths characterized by higher hydraulic resistance will receive lower flow rates. As the relation between pressure drop and fluid velocity is neither generally linear nor constant, the flow distribution across a parallel system changes depending on the total flow rate. Also variations of the fluid viscosity and density can affect the flow distribution.

In a solar collector field it is possible to distinguish three main types of hydraulic components: solar collectors, pipes (distribution pipes and row inlet/outlet) and fittings (bends, tee junctions, valves, etc.). The pressure drop characteristic of a solar collector can be difficult to find in technical datasheets, as it is not compulsory for the manufacturer to provide (ISO, 2014). Even if provided, this relation is usually given for a specific fluid and temperature. So, care should be taken when using other fluids and/or temperatures.

In this study the collector pressure drop was calculated using the model proposed by Bava and Furbo (2016). The modeled collector was a HTHEATStore 35/08 from the company Arcon-Sunmark A/S (SP, 2015). This is a flat plate harp collector with U-type configuration and an aperture area of 12.60 m². Its 18 absorber pipes are 5.80 m long, have an inner diameter of 7.3 mm and an intermediate spacing of 122 mm. The manifolds have an inner diameter of 32.9 mm. The calculated pressure drop is shown in Figure 2 as function of temperature and flow rate for a 35% propylene glycol/water mixture. The thermophysical properties of the fluid were evaluated through (Eq. 8) and (Eq. 9).

![Figure 2: Pressure drop of a HTHEATstore 35/08 collector as function of temperature and flow rate for 35% propylene glycol/water mixture.](image)

The friction loss along a straight pipe of constant cross section can be calculated by the Darcy-Weisbach equation:

\[ \Delta p = \frac{\lambda l \rho w^2}{D_h} \]  

(Eq. 1)

where \( \Delta p \) is the pressure drop [Pa],

\( \lambda \) is the Darcy friction factor [-],
The pipe length \(l\) [m],

\(D_h\) is the pipe hydraulic diameter, which equals the inner diameter for a full flow circular pipe [m],

\(\rho\) is the density of the fluid [kg \(\text{m}^{-3}\)],

\(w\) is the mean fluid velocity [m s\(^{-1}\)].

In case of Reynolds numbers (\(Re\)) lower than 2300, laminar flow regime was assumed (Holman, 2002) and the Darcy friction factor was calculated through the Hagen-Poiseuille law (Eq. 2):

\[ \lambda = \frac{64}{Re} \quad \text{(Eq. 2)} \]

For \(Re\geq 4000\), the flow was assumed turbulent (Holman, 2002) and the friction factor was calculated through the Haaland (1983) correlation for rough pipes (Eq. 3), as the distribution pipes were made of steel with roughness \(\varepsilon=10^{-4}\) m (Li and Svendsen, 2013).

\[ \lambda^{-1/2} = -1.8 \log_{10}\left\{ \left[ 3.7 \frac{D_h}{\varepsilon} \right]^{1.11} + 6.9/Re \right\} \quad \text{(Eq. 3)} \]

where \(\varepsilon\) is the absolute surface roughness of the pipe inner surface [m].

The Haaland correlation is an explicit, and hence faster to solve, formulation of the Colebrook (1939) equation. Beside the mentioned correlations, other correlations were implemented in the model, such as those proposed by Colebrook (1939) for turbulent flow in rough pipes, by Blasius (1913) for turbulent flow in smooth pipes and by Joseph and Yang (2010) for any flow regime in smooth pipes.

Following the example of Jones and Lior (1994), the friction factor in the transition region (2300<\(Re<4000\)) was calculated by linear interpolation between the value obtained from (Eq. 2) for \(Re=2300\) and that obtained from (Eq. 3) for \(Re=4000\).

Regarding local losses in fittings, such as bends, tee junctions, changes of flow section area, etc., correlations from Idelchik (1994) were used. Regarding balancing valves, the relation between flow rate and pressure drop is usually provided by the manufacturer in terms of flow factor \(K_v\) (Eq. 4):

\[ K_v = \frac{V}{\sqrt{S_G \Delta p}} \quad \text{(Eq. 4)} \]

where \(V\) is the fluid flow rate [m\(^3\) h\(^{-1}\)],

\(S_G\) is the fluid specific gravity [-].

The \(K_v\) values are given as function of the valve setting and refer to water and fluids with similar viscosity. Deviations from the nominal \(K_v\) value are expected for other types of fluid and at flow rates significantly smaller than the valve nominal flow rate (IMI Hydronic, 2015a). In these cases, corrections need to be applied. In this study, valves from IMI-Hydronic were used and their \(K_v\) values in different operating conditions were estimated though the software HySelect (IMI Hydronic, 2014).

### 2.1.2 Fluid properties

Usually propylene glycol/water mixtures are used as solar collector fluid in solar collector fields. For the relevant thermophysical properties of these mixtures, the following correlations were implemented in the model (Conde, 2011).

\[ \rho = 508.4 - 0.1824x + 965.8T^* + 0.2803xT^* - 472.2(10)^{-5} \quad \text{(Eq. 5)} \]

\[ c_p = 4476 + 608.6 - 715.0T^* - 1939xT^* + 478.7(10)^{-5} \quad \text{(Eq. 6)} \]

\[ \ln \mu = -1.028 - 0.1003x - 19.947T^* + 0.1464xT^* + 14.6205(10)^{-5} \quad \text{(Eq. 7)} \]

where \(c_p\) is the specific heat of the fluid [J kg\(^{-1}\) K\(^{-1}\)],

\(\mu\) is dynamic viscosity of the fluid [Pa s],

\(x\) is the mass concentration of propylene glycol in the mixture [%],

\(T^*\) is a factor defined as \(T^*=273.15/(T+273.15)\), where \(T\) is the fluid temperature [°C].
A large variability of the properties of propylene glycol/water mixtures was found when comparing different sources in literature (Conde, 2011; George and Sastry, 2003; Melinder, 2007; Sun and Teja, 2004; Tsierkezos and Palaiologou, 2009) or product datasheets (DOW, 2008; Skovrup, 2005). In fact, different commercial propylene glycols may contain different amounts and types of additives to prevent corrosion. Additionally, propylene glycol is known to suffer acidic degradation and hence change its composition over time, especially when exposed to high temperatures (Clifton et al., 1985; Rossiter et al., 1985). For these reasons, when performing the model validation, a sample of propylene glycol/water mixture was taken from the specific collector field and its density and viscosity were experimentally determined. For this purpose, an Anton Paar DMA 4100 densimeter and an Anton Paar AMV 200 viscometer were used. The mixture (glycol mass content of 35%) was tested at temperatures between 20 °C to 80 °C with an intermediate step of 10 °C. The experimental data points were then interpolated with the expressions (Eq. 8) and (Eq. 9). The specific heat was not determined, as it was not needed for the validation.

\[
\rho = 1038.3 - 0.4419T - 1.940 \times 10^{-3} T^2 \quad \text{(Eq. 8)}
\]

\[
\mu = \begin{cases} 
-1.449 \times 10^{-8} T^3 + 3.066 \times 10^{-6} T^2 - 2.337 \times 10^{-4} T + 7.289 \times 10^{-3} & \text{if } T < 38 \, ^\circ\text{C} \\
0.1803 T^{-1.232} & \text{if } T > 38 \, ^\circ\text{C}
\end{cases} \quad \text{(Eq. 9)}
\]

### 2.1.3 Matlab implementation

Using the pressure drop correlations and the fluid properties described in the previous sections, a numerical model was developed in Matlab to compute the flow distribution in a solar collector field. To provide the necessary input data to the model, the layout of the collector field, pressure drop in the collectors, valves and settings, dimensions of distribution pipes and type of fittings must be known. Also the fluid type and operating conditions, such as field flow rate and fluid inlet temperature, need to be inserted. The temperature profile along the collector rows, used to evaluate the fluid properties, can be estimated in two ways. The first possibility is to define an outlet temperature, equal for all collector rows, and a linear temperature profile is assumed along the collector row. For the second possibility, the collector efficiency coefficients and weather conditions, such as solar irradiance on the collector plane and ambient temperature, must be provided instead. The temperature profile across each collector row is then calculated solving the differential equation (Eq. 10), which assumes steady state conditions.

\[
\frac{\dot{m} c_p}{A} \frac{dT}{dA} = G \eta_0 K_0 - a_1 \cdot (T - T_{amb}) - a_2 \cdot (T - T_{amb})^2 \quad \text{(Eq. 10)}
\]

where \( \dot{m} \) is the mass flow rate [kg s\(^{-1}\)], \( A \) is the gross/aperture collector area [m\(^2\)], \( G \) is the hemispherical solar irradiance on the collector plane [W m\(^{-2}\)], \( \eta_0 \) is the peak efficiency of the solar collector coherent with the definition of \( A \) [-], \( K_0 \) is the incident angle modifier [-], \( a_1 \) is the first order heat loss coefficient coherent with the definition of \( A \) [W m\(^{-2}\) K\(^{-1}\)], \( a_2 \) is the second order heat loss coefficient coherent with the definition of \( A \) [W m\(^{-2}\) K\(^{-2}\)].

\( amb \) subscript denotes ambient temperature.

The solution of (Eq. 10) represents the temperature profile along the collector row and is given by (Eq. 11):

\[
T(A) = \frac{d \cdot \tan \left[ \frac{T_{amb} (K d + A d)}{2a} \right] - b}{2a} \quad \text{(Eq. 11)}
\]

where \( a \) is parameter defined as
\[
a = \frac{-a_2}{\dot{m} c_p},
\]

\( b \) is parameter defined as
\[
b = \frac{2a_2 T_{amb} - a_1}{\dot{m} c_p},
\]
\[ c \text{ is parameter defined as } c = G \eta_0 K + a_1 T_{amb} - a_2 T_{amb}^2 / \dot{m}_p, \]

\[ d \text{ is parameter defined as } d = \sqrt{4ac - b^2}, \]

\[ K \text{ is the integration constant, defined based on the inlet temperature boundary condition } T_{in} \text{ [°C] as } \]

\[ K = \frac{2}{d} \tan^{-1} \left( \frac{b + 2aT_{in}}{d} \right) \]

As can be seen from (Eq. 11), the temperature profile along a collector row is function of its flow rate, so rows supplied lower flow rates reach higher temperatures.

Given an initial total flow rate as input, the model assumes that the flow is uniformly distributed across the collector field. To calculate the true flow distribution, the numerical model solves iteratively the set of equations (Eq. 12), which impose both the conservation of mass across the collector field (first line in (Eq. 12)) and the uniformity of pressure drop along the different hydraulic paths (from second line downward):

\[
\begin{pmatrix}
1 & 1 & 1 & 1 & 1 & \cdots \\
0 & 0 & 0 & 0 & 0 & \cdots \\
0 & 0 & 0 & 0 & 0 & \cdots \\
\vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\
0 & 0 & 0 & 0 & 0 & \cdots \\
k_{N-1,j} \dot{m}_{N-1,j} & k_{N,j} \dot{m}_{N,j} & \cdots & k_N \dot{m}_N & \cdots & k_{N-1} \dot{m}_{N-1} \\
\end{pmatrix}
\begin{pmatrix}
\dot{m}_{1,j} \\
\dot{m}_{2,j} \\
\dot{m}_{3,j} \\
\vdots \\
\dot{m}_{N-1,j} \\
\dot{m}_N \\
\end{pmatrix}
= \begin{pmatrix}
\dot{m}_{tot} \\
0 \\
0 \\
\vdots \\
0 \\
0 \\
\end{pmatrix}
\]

(Eq. 12)

where \( k \) is a hydraulic resistance coefficient \([\text{kg}^{-1} \text{ m}^{-1}]\),

1, 2, ..., \( N \) subscripts denote the collector row and \( N \) is the total number collector rows,

tot subscript refers to the total flow rate supplied to the solar collector field,

\( j \) subscript denotes the iteration number.

The hydraulic resistance coefficient \( k_i \) is defined so that the product \( (k_i \cdot \dot{m}_i)^2 \) corresponds to the pressure drop (in Pascal) along the entire \( i \)-th hydraulic path. The value of \( k_i \) is representative of the pressure drop along the \( i \)-th collector row, which is proportional to the square of the row flow rate \( \dot{m}_i \), as well as the pressure drop across the supply/return pipes segments and tees included in the \( i \)-th hydraulic path, properly normalized to the flow rate \( \dot{m}_i \). In general, \( k_i \) is defined by a formulation of the type (Eq. 13):

\[ k_i = k_i' + \sum_{\gamma=1}^{\gamma} \left( k_{\gamma'} \frac{\dot{m}_\gamma^2}{\dot{m}_i^2} \right) \]

(Eq. 13)

where \( k_i' \) \([\text{kg}^{-1} \text{ m}^{-1}]\) is the contribution to the coefficient \( k_i \) such that the product \( (k_i' \cdot \dot{m}_i)^2 \) gives the pressure drop in those components whose pressure drop is proportional to the square of the row flow rate, such as collectors, row inlet/outlet, balancing valves, etc.

\( k_{\gamma'} \) \([\text{kg}^{-1} \text{ m}^{-1}]\) is the contribution to the coefficient \( k_i \) such that the product \( (k_{\gamma'} \cdot \dot{m}_{\gamma-1-\gamma})^2 \) gives the pressure drop in the components of the \((\gamma-1-\gamma)\)-th distribution line segment, such as supply/return pipe segments and tee junctions,

\( \gamma-1-\gamma \) subscript denotes the supply/return pipe segment between the \((\gamma-1)\)-th and \( \gamma \)-th collector row.

The system of equations (Eq. 12) is iteratively solved until the maximum difference in the collector row flow rates between two consecutive iterations is lower than 0.1%. Assuming a collector array with 24 hydraulic paths, such as that used in this study, a typical calculation is performed in approximately 0.1 seconds for a computer with quad-core CPU and 2.4 GHz CPU frequency.

The Matlab code of the model is publicly available online (Bava, 2016).

### 2.2. Description of the solar collector field

#### 2.2.1. Collector field layout

The developed model was based on the layout of the solar collector field near Høje Taastrup (Denmark). The layout of the collector field is shown in Figure 3. The collector field had a collector area of 3024 m² and consisted of two subfields, having 12 collector rows each. Each row was made up of 10 HTHEATStore
35/08 collectors (Section 2.1.1) and the row distance was 5.5 m. The collectors had a tilt angle of 43° and an orientation of 2.5° W. The supply pipes ran along the outer sides of the collector field (blue lines in Figure 3). One return pipe collected the fluid in the middle of the field (red line in Figure 3). Pumps, heat exchanger, expansion vessels and control system were located in the technical building in the north-east corner of the collector field. Because there was no auxiliary heating plant nearby, the outlet temperature from the collector field had always to reach approximately the DH supply temperature. The collector field was usually operated between an inlet temperature of 50-55 °C and an outlet temperature of 90-95 °C. The flow rate ranged between 8 and 50 m³ h⁻¹.

The distribution pipes were made of preinsulated steel pipes. The pipes between the technical building and the collector field, along which the entire field flow rate flows, had an inner diameter of 10.7 cm. The diameter progressively decreased as part of the flow rate was diverted to the collector rows. For each collector row the supply line had a diverging tee junction which directed part of the supplied fluid to the collector row through the row inlet. The row inlet consisted of two preinsulated steel pipes, connected to each other through a balancing valve. The balancing valves installed in the collector field were of type STAD20 from row 1 to 11 and STAD25 from row 12 to 24 (IMI Hydronic, 2015a). In the middle of the field, the flows coming from each couple of side-by-side rows merged through a merging tee junction and flowed into the return pipe through a converging tee junction. Before the merging tee junction, each row outlet was equipped with a three way ball valve. This valve, together with the balancing valve at the row inlet, could be used to isolate a specific row from the rest of the field, when maintenance was needed.

The heat transfer fluid in the collector field was a 35% propylene glycol/water mixture (Section 2.1.2).

### 2.2.2. Measuring equipment

To measure the flow rate in the different collector rows, a differential pressure sensor TA-SCOPE from IMI Hydronic was used (IMI Hydronic, 2015b). The balancing valves are equipped with two measuring points, one before and one after the valve member. From the measured pressure drop across the valve and the valve flow factor (Eq. 4), the flow rate is calculated. The TA-SCOPE device is also equipped with a temperature sensor, so that, by specifying the type of fluid, it calculates its density and viscosity and corrects the flow factor accordingly. The nominal accuracy of the differential pressure sensor is given by the higher value between 0.1 kPa and 1% of the measured value. However, when using the TA-SCOPE sensor to evaluate the flow rate across a STAD valve, the accuracy is worse. Figure 4 shows the expected uncertainty as function of the valve setting. As the uncertainty increases sharply at low valve settings, it is generally advised to use a
setting higher than two. This rule of thumb was respected in Høje Taastrup collector field, where the lowest valve setting was 2.2.

A first series of measurements on the field flow distribution showed that the difference in the row flow rates was lower than the uncertainty of the measurement method. A validation of the model in these conditions would not have been completely decisive, as the error band of the measured points would be larger than the differences in flow rate that the model is meant to predict. Consequently, a second series of measurements was carried out. This time the setting of the first 10 balancing valves in the eastern subfield were modified, so to induce a stronger flow maldistribution, which could be more easily detected.

As the total field flow rate was expected to be the most important parameter affecting the flow distribution, three different flow rates were tested: a high flow rate of approximately 50 m$^3$ h$^{-1}$, which is the highest flow rate supplied to the field in full load conditions; a low flow rate of 14 m$^3$ h$^{-1}$, which was regarded as the lowest flow rate still able to cause a pressure drop across the valves high enough to make the measurement meaningful; and an intermediate flow rate of 30 m$^3$ h$^{-1}$. As measuring the flow rate in all the rows took approximately 30-40 minutes, it was important that the operating conditions of the collector field were kept as constant as possible during this procedure. Hence, the measurements were performed during a cloudy day, to avoid significant temperature variations, and the pump was run at constant speed. The relevant operating conditions during the tests are listed in Table 1.

<table>
<thead>
<tr>
<th>Test</th>
<th>Test 2</th>
<th>Test 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Duration [min]</td>
<td>29</td>
<td>32</td>
</tr>
<tr>
<td>Field flow rate [m$^3$ h$^{-1}$]</td>
<td>50.3 ± 0.3%</td>
<td>30.4 ± 0.3%</td>
</tr>
<tr>
<td>Inlet temperature [°C]</td>
<td>45.0 ± 1.2</td>
<td>46.7 ± 1.2</td>
</tr>
<tr>
<td>Outlet temperature [°C]</td>
<td>45.1 ± 1.2</td>
<td>47.5 ± 1.3</td>
</tr>
</tbody>
</table>

The volume flow rate to the collector field was measured by an electromagnetic flow meter with an accuracy of 0.5%. The fluid temperature was measured by RTD temperature sensors with accuracy of 0.25 °C. The temperature was monitored at the beginning of the supply pipe and at the end of the return pipe, as well as at the inlet and outlet of four collector rows. The pressure in the system was measured by piezoresistive pressure sensor with maximum accuracy of 0.5%. In the solar collector loop there were three of these sensors: one after the pump, one right before the heat exchanger and one after the heat exchanger. The first and the second sensor could hence be used to evaluate the pressure drop across the collector field.

The instantaneous values of the monitored data were recorded once per minute.

2.3. Investigated scenarios
Using the developed model, the field flow distribution was evaluated in different scenarios:

- **Case 1.** The operating conditions used for the simulation were similar to those actually used in Høje Taastrup collector field. The inlet temperature was 55 °C and the solar irradiance on the collector plane was varied with the total flow rate in such a way that the outlet temperature was approximately 95 °C (see Eq. 11)). A 35% propylene glycol/water mixture was assumed as collector fluid (Eq. 5-Eq. 7). The same settings of the balancing valves as used in Høje Taastrup in case of normal operation were assumed in the model.

- **Case 2.** The effect of a fluid temperature close to the freezing point was investigated. In case of very cold temperatures, the solar collector fluid is circulated in the collector loop to prevent freezing. Collector rows supplied with lower flow rates are more likely to freeze in case of extended cold periods. As the viscosity of propylene glycol/water mixtures is strongly dependent on the temperature, it is important to verify that also in these conditions all collector rows receive a sufficient flow. According to DOW (2008), the freezing point of a 35% propylene glycol/water mixture should be -16 °C. Consequently, a slightly higher fluid temperature of -13 °C was assumed in the model simulations.

- **Case 3.** The operating conditions were the same as in case 1, but no balancing valves were installed. A method for achieving good flow distribution without balancing valves consists in keeping constant the diameters of the supply and return pipes throughout their length. This approach was for example used in the first large collector fields built in Sweden (Section 1.2).

  This case was divided in two subcases. Subcase 3.1 used the same distribution pipes as in case 1, so the pipe diameter changed along the pipe length. In subcase 3.2 constant diameters in supply and return pipes were assumed, more specifically 8.25 cm for the supply pipe and 10.7 cm for the return pipe. Additionally, to avoid unbalance between the two subfields, the technical building was assumed to be located right above where row 1 and 13 face each other (see Figure 3).

- **Case 4.** The number and the composition of the collector rows were the same as in the previous cases, but the rows were now all connected in parallel. The resulting layout is shown in Figure 5. Three different subcases were investigated. In subcases 4.1 and 4.2 the diameter of the supply and return pipes was progressively decreased as more fluid was diverted. The diameters of the pipes were chosen from commercially available preinsulated pipes (Logstor, 2005) and in such a way that the highest fluid velocity was lower than 1.65 m/s. The difference between the two subcases was that in subcase 4.1 balancing valves were regulated to obtain a more uniform flow distribution at the flow rate of 50 m³ h⁻¹. In subcase 4.2 no valves were used. Finally, in subcase 4.3 the diameter of the distribution pipes was kept constant and equal to 10.7 cm, i.e. the largest pipe diameter used in subcases 4.1 and 4.2. The operating conditions were the same as in case 1.
3. Results

3.1. Validation of the model

3.1.1. Pressure drop across the collector field

The comparison between the measured and calculated pressure drops as function of the flow rate is shown in Figure 6. The measured data are from the period June 10th-July 8th 2015. To reduce the scatter of the data caused by transient periods with fast variation of the field flow rate, only the data points where the flow rate differed less than 10% from the previous recorded value are shown. In Figure 6 the data points referring to the period 1st-2nd July are highlighted. These days presented clear sky conditions. Due to the control strategy (Section 1.3), the flow rate varied smoothly following the solar irradiance. The inlet and outlet temperature were fairly constant throughout the day and equal to 56 °C and 95 °C respectively. These boundary conditions were used as input for the model to calculate the pressure drop across the collector field (continuous curve in Figure 6).
At null flow the measured pressure difference was approximately $13 \pm 1$ kPa. This was because the two manometers (see Section 2.2.2) had an elevation difference of 1.36 m, which caused different hydrostatic pressures. Apart from this offset, the typical quadratic relation between pressure drop and flow rate was observed, as the measured points are approximately aligned along a parabolic trajectory.

The pressure drop curve calculated by the model fits the measured data accurately. The coefficient of determination $R^2$ between the measured data and the model is 0.97, if the entire data set is used, and 0.98, if only data from the period 1st-2nd July are used.

### 3.1.2. Flow distribution

The flow distribution was expressed in terms of dimensionless flow rate in the collector rows, defined as:

$$V' = \frac{V_i}{(\sum_{i=1}^{N} V_i)/N} \quad \text{(Eq. 14)}$$

where $V'_i$ is the dimensionless flow rate in the $i$-th collector row [-], $V_i$ is the volume flow rate in the $i$-th collector row [m$^3$ h$^{-1}$], and $N$ is the number of collector rows [-].

Figure 7, Figure 8 and Figure 9 show the measured and modeled flow distribution in terms of dimensionless flow rate for field flow rates of 50, 30 and 14 m$^3$ h$^{-1}$. The shown error bars are based on the information contained in Figure 4.
Figure 7: Comparison between measured and modeled flow distribution for a field flow rate of 50 m³ h⁻¹.

Figure 8: Comparison between measured and modeled flow distribution for a field flow rate of 30 m³ h⁻¹.
The difference in flow distribution between the eastern subfield (rows 1-12) and the western subfield (rows 13-24) is easily recognized. In the eastern subfield the valve settings were changed so to introduce a stronger maldistribution than in normal operation. The settings of the first 10 valves were modified, so to cause a decreasing flow rate profile. In the western subfield the valve settings were not changed, so the flow distribution was much more uniform.

To evaluate the accuracy of the model, the root-mean-square deviation (RMSD) is introduced (Eq. 15).

\[
RMSD = \sqrt{\frac{\sum_{i=1}^{N} (\dot{z}_i - z_i)^2}{N}} \quad \text{(Eq. 15)}
\]

where \(z\) is the measured value of the investigated parameter,
\(\dot{z}\) is the estimator of the investigated parameter.

To make the different RMSDs immediately comparable irrespective of the field flow rate, the RMSDs were evaluated using the dimensionless flow rate \(V'\) (Eq. 14). Table 2 lists the RMSDs and the maximum relative difference for the three flow distribution tests.

<table>
<thead>
<tr>
<th>Test 1</th>
<th>Test 2</th>
<th>Test 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Field flow rate [m³ h⁻¹]</td>
<td>50.3</td>
<td>30.4</td>
</tr>
<tr>
<td>RMSD((V'))</td>
<td>0.022</td>
<td>0.027</td>
</tr>
<tr>
<td>Max. deviation (row number)</td>
<td>4.2% (3)</td>
<td>5.9% (3)</td>
</tr>
</tbody>
</table>

An overall good agreement between measurements and model was found, with the RMSD ranging between 0.020 and 0.027. The highest deviations were between 4.2% and 5.9% depending on the tested flow rate. It is also noted that at the lowest flow rate of 14 m³ h⁻¹ the measured flow distribution is less uniform that in the other two cases. Especially the very first rows received higher fractions of the total flow rate, with dimensionless flow rates up to 1.20. Conversely, in the other two tests, this value did not exceed 1.15.

### 3.2. Investigated scenarios

#### 3.2.1. Case 1: normal operating conditions

The calculated flow distribution in case 1 is shown in Figure 10 for different field flow rates.
In the simulated scenarios the RMSD was used as main parameter to evaluate the degree of maldistribution. Unlike in the model validation, the term of comparison was now the uniform distribution profile ($z=1$ in Eq. 15).

It can be noted that the higher the flow rate, the more uniform the flow distribution. At flow rates equal to or higher than 30 m$^3$ h$^{-1}$ the RMSD was approximately constant and equal to 0.015. At lower flow rates this value increased up to 0.025 for a flow rate of 8 m$^3$ h$^{-1}$. The highest deviation from the ideal flow rate was lower than 6%, and the maximum difference between highest and lowest row flow rates was within 8%.

For the different flow rates, the pressure drop across the field was in agreement with Figure 6.

3.2.2. Case 2: temperature close to freezing point

Despite the much higher viscosity of the glycol/water mixture at low temperature, the flow distribution was
very uniform. The maximum deviation of row flow rate from the perfectly uniform case was 3.5%. Unlike case 1, higher flow rates did not necessarily entail a more uniform flow distribution. In fact, the value of RMSD varied from a minimum of 0.005 at 20 m$^3$ h$^{-1}$ to a maximum of 0.018 at 50 m$^3$ h$^{-1}$.

### 3.2.3. Case 3: no balancing valves

In subcase 3.1 only the balancing valves were removed, while the layout and the dimensions of the distribution pipes were maintained as in case 1. The resulting flow distributions are presented in Figure 12. Given the longer pipe length from the pump to the western subfield, this solution caused this subfield to be supplied with a much lower flow rate (12-14% lower compared to the eastern subfield depending on the field flow rate). Within the same subfield the relative difference between the lowest and the highest collector row flow rate was 6-8% depending on the field flow rate. The RMSDs in this case were much higher, ranging between 0.068 and 0.082.

![Figure 12: Modeled flow distributions for different field flow rates in subcase 3.1.](image)

In subcase 3.2 the diameters of the supply and return pipes were maintained constant and each of them equal to the largest installed diameter (8.25 cm for the supply pipe and 10.7 cm for the return pipe). Given the symmetry of the resulting field layout, the flow distribution was identical in both subfields. Hence, Figure 13 shows the flow distribution only for the eastern subfield. Due to the constant pipe diameters, the relative difference between the lowest and the highest collector row flow rate was 5-6% depending on the field flow rate, so slightly better than in subcase 3.1.

Without balancing valves and due to the larger pipe diameters, the pressure drop across the collector field was approximately 20-25% smaller compared to case 1. However, as the connection to the DH network is located in the north-east corner of the field, the additional 2×65 m pipes to carry the fluid to this point would result in a reduction of 10% only.
3.2.4. Case 4: different field layout: 24 rows in parallel

Looking at Figure 13 it may be thought that balancing valves are not strictly necessary to reach a good flow distribution. For this reason, a different collector field layout (Figure 5) was investigated to verify whether this could be generalized. Figure 14 presents the flow distributions in subcase 4.1 with balancing valves, subcase 4.2 without balancing valves and subcase 4.3 without balancing valves and constant distribution pipe diameter. For each subcase the two flow rates, which gave the most and least uniform distribution, are shown.

It can be noted that only subcase 4.1, which makes use of balancing valves, gave a uniform flow distribution. As expected the better distribution was found for the flow rate of 50 m$^3$/h ($\text{RMSD}=3.5 \cdot 10^{-3}$), at which the balancing valves were regulated. In this case the flow rate in each row never differed more than 1% from the perfectly uniform distribution. This deviation increased at lower flow rates and at 8 m$^3$/h$^1$ it was within 2%, while the RMSD was 0.01.

Removing the balancing valves while decreasing the distribution pipe diameter with the flow rate (subcase
4.2) gave the highest maldistribution, with deviations up to 13% compared to perfectly uniform distribution. Comparing the highest and the lowest row flow rate, the former was about 30% higher than the latter. The RMSD was 0.086 at 8 m$^3$ h$^{-1}$ and 0.073 at 20 m$^3$ h$^{-1}$. Maintaining constant diameter along the entire length of the distribution pipes (subcase 4.3) improved the flow distribution compared to subcase 4.2, and the highest row flow rate was 12% higher than the lowest row flow rate. The RMSDs decreased to 0.036 and 0.030 at 8 and 20 m$^3$ h$^{-1}$, but were still considerably higher than in case 4.1.

4. Discussion

4.1. Validation of the model

From Figure 7, Figure 8, Figure 9 and Table 2, an overall good agreement between modeled results and measurements can be noted, with the RMSD ranging between 0.020 and 0.027. In the eastern subfield the measured and modeled flow distribution profiles presented the same trend, with the only exception represented by the third row. In fact, this collector row was characterized by the highest deviation between measured and modeled flow rate in both test 1 and 2 (Table 2). For this row the measured flow rate was significantly lower than the flow rate in the neighboring rows in all the three tests. This was most likely due to some additional flow resistance in this collector row, maybe due to some obstruction or dirt clog. In fact, also the original setting of its balancing valve was larger (and hence the valve more open) than the valve settings of neighboring rows and had the same value as the valve in the 11th collector row, significantly farther away. This means that, already when balancing the flow at the start-up phase of the collector field, it was noted that, in order for the third row to receive the design flow rate, its valve had to be opened more than expected. It is not reasonable to assume that this difference was caused by an inaccurate correlation for its tee junction used by the model. In fact, being the two subfields symmetric, a similar behavior should appear in the corresponding collector row (the 15th) in the western subfield.

At the lowest flow rate, row 24 had the highest deviation between measurement and model (Table 2). In this case the accuracy of the differential pressure sensor might play a significant role. Given the low flow rate and the completely open balancing valve, the pressure drop across the valve was very low (0.5 kPa). As the accuracy of the TA-SCOPE sensor is 0.1 kPa (Section 2.2.2), the measurement error can be higher than that shown in Figure 4.

4.2. Investigated scenarios

Comparing the scenario in normal operating conditions (Figure 10) with the validation results (Figure 7, Figure 8 and Figure 9), it can be seen that the correct setting of the balancing valves significantly improved the flow distribution. The most uniform flow distribution occurred at the highest flow rate of 50 m$^3$ h$^{-1}$. This was expected, as the balancing valves were set to give a uniform distribution at the nominal field flow rate, i.e. the highest flow rate the collector field operates at. This was about 55 m$^3$ h$^{-1}$ in Høje Taastrup collector field.

As the relation between flow rate and pressure drop varies differently for the different components in the collector loop, a higher maldistribution is likely to occur when the field flow rate increasingly deviates from the nominal one. Despite this, the balancing valves resulted in a good flow distribution in all simulated conditions. The highest relative difference between row flow rate and its ideal value was always well within 10%, which is considered the maximum acceptable deviation according to the German standard VDI (2004).

A good flow distribution was found also in case 2 (Figure 11) with low fluid temperature. A variation in flow distribution could have been expected, due to strong temperature dependence of the kinematic viscosity of the glycol/water mixture. In fact, this increased approximately 20 times when the mixture temperature decreased from 75 °C to -13 °C. Despite the very strong variation, all components in the circuit experienced this low viscosity, so the flow distribution was not significantly affected.

The effect of removing the balancing valves was investigated in case 3.1 (Figure 12). There was a significant flow unbalance between the two subfields, because the supply pipe to the western subfield was 122 m longer compared to the eastern subfield. If a collector field with the same layout as in Høje Taastrup was designed without balancing valves, the distribution pipes should be symmetrical to avoid unbalance between the two
subfields (case 3.2). This scenario was inspired by the first collector fields built in Sweden, such as Falkenberg and Nykvarn II. These plants were built connecting in parallel collector rows of 10 collectors each. The collectors had a U-type harp design, very similar to a HTHEATstore 35/08. Both plants were relatively small (5500 m² in Falkenberg and 3500 m² in Nykvarn II) and could achieve a uniform flow distribution without balancing valves, due to the regular layout and constant pipe diameter. Similarly, case 3.2 presented an acceptable flow distribution, as shown in Figure 13. This was possible due to the relatively small area of the collector field (3024 m²) and the limited number of rows connected in parallel (12 in each subfield). In this configuration the pressure drop across the collector row played the most significant role, representing 85-88% of the entire pressure drop along the hydraulic path for the first row and 76-81% for the last one. The required head of the pump in case 3.2 was 10% lower than in case 1.

However, collector fields having more collector rows connected directly in parallel are less likely to achieve uniform flow distribution (case 4.2 and 4.3), unless balancing valves are installed (case 4.1). Maintaining a large and constant diameter for the entire length of the distribution pipes help reduce the maldistribution (case 4.3), but this solution entails higher cost and heat losses due to the increased pipe size.

Comparing the results of simulations with different layouts, it was found that in absence of balancing valves the rule of thumb (Eq. 16) is generally valid, if the flow regime both in the distribution pipes and in the collectors is turbulent.

\[
\frac{\max(V_i) - \min(V_i)}{\max(V_i)} \approx 0.5 \frac{\Delta p_{distr.pipe}}{\Delta p_{row}} \quad \text{(Eq. 16)}
\]

where \( \max(V_i) \) is the highest volume flow rate in a collector row \([\text{m}^3 \text{ h}^{-1}]\), \( \min(V_i) \) is the lowest volume flow rate in a collector row \([\text{m}^3 \text{ h}^{-1}]\), \( \Delta p_{distr.pipe} \) is the pressure drop along the longest distribution pipe supplying a collector row \([\text{Pa}]\), \( \Delta p_{row} \) is the pressure drop across a collector row supplied by the average flow rate \([\text{Pa}]\),

For example, in order for the highest and the lowest row flow rate to differ less than 10%, the pressure drop along the longest supply and return pipes should be lower than 20% of the pressure drop across the average collector row. Figure 15 represents (Eq. 16) and shows the investigated scenarios 3.2, 4.2 and 4.3 along with other selected cases, to make the data set more complete.

\[ y = 0.48x \quad R^2 = 0.99 \]

**Figure 15:** Maximum deviation in row flow rate as function of the ratio between the pressure drop along the longest distribution line and the average pressure drop in a collector row.

### 4.3. Effect of the flow regime on the flow distribution

From Figure 12 and Figure 13 it can be noted that, in absence of balancing valves, higher flow rates did not necessarily entail a more uniform flow distribution. Figure 13 shows that the lowest flow rate had the highest maldistribution. Increasing the flow rate up to 20 m³ h⁻¹ gave a more uniform flow distribution, while for even higher flow rates this became less uniform. To analyze this trend in more detail, Figure 16 shows the RMSD as function of both flow rate and average Re in the absorber pipes of the collectors. The diagram was
based on the same collector field layout and operating conditions as in case 3.2, with the only difference of the fluid temperature, assumed constant and equal to 55 °C. This allowed having the same Re in all the collectors of the same row and simplified the analysis.

At low flow rates ($V<20 \text{ m}^3 \text{ h}^{-1}$), the flow regime in the collectors was still laminar while that in the distribution pipes was mainly turbulent with the exception of the very last pipe segments. In these conditions, a higher field flow rate increased the flow maldistribution. In fact, the increase in pressure drop in the distribution pipes (approximately quadratic with the flow rate in turbulent regime) was sharper than that in the collector rows (approximately linear in laminar regime). At higher flow rates ($V=20-30 \text{ m}^3 \text{ h}^{-1}$), the regime in the collector absorber pipes became progressively transitional. Given the assumption of linear interpolation made in the transition region (Section 2.1.1), the pressure drop was proportional to the cube of the fluid velocity, so the flow distribution improved rapidly and the RMSD decreased to its minimum. Finally, when the field flow rate was high enough to cause turbulent regime in all components ($V\geq35 \text{ m}^3 \text{ h}^{-1}$), the flow distribution became slightly less uniform and almost independent of the flow rate.

5. Conclusions

A model for estimating the flow distribution in a solar collector field was developed. The model results were compared against measurements, both in terms of pressure drop and flow distribution across a collector field. Good agreement was found.

By using the model, different scenarios were investigated. Installing balancing valves in each collector row proved to be a reliable way to guarantee uniform flow distribution. Although the valves were set in nominal conditions, the deviations occurring at different conditions were still within the generally accepted range of ±10%.

Relatively small fields with few collector rows and regular layout can also achieve good flow distribution without balancing valves. Keeping a constant and large pipe diameter along the entire distribution line favors a uniform distribution and decreases the pressure drop across the collector field. The final solution should be selected based on economic considerations, taking into account the cost of the pipes and valves, increased heat losses and decreased pressure drop.
For very large collector fields with a high number of rows, balancing valves seems to be the most reliable solution to achieve good flow distribution.

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