Characteristic sizes of life in the oceans - from bacteria to whales

Andersen, Ken Haste; Berge, T.; Goncalves, R.; Hartvig, Martin; Heuschele, Jan; Hylander, Samuel; Jacobsen, Nis Sand; Lindemann, Christian; Martens, Erik Andreas; Neuheimer, Anna

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K.H. Andersen¹,²: kha@aqua.dtu.dk. Corresponding author, tel. +45 35 88 33 99.
T. Berge¹,⁸: tberge@bio.ku.dk
R. J. Gonçalves¹,²,¹⁰: rgon@aqua.dtu.dk
M. Hartvig²,³,⁴: mh@hvig.dk
J. Heuschele¹,²: janheuschele@gmail.com
S. Hylander²,⁹: samuel.hylander@lnu.se
N.S. Jacobsen¹,²: nsja@aqua.dtu.dk
C. Lindemann¹,²: chrli@aqua.dtu.dk
E.A. Martens¹,²,⁷: erik.martens@ds.mpg.de
A.B. Neuheimer²,³,⁶: annabn@hawaii.edu
K. Olsson¹,²: karol@aqua.dtu.dk
A. Palacz¹,²: arpa@aqua.dtu.dk
F. Prowe¹,²,¹¹: fprowe@geomar.de
J. Sainmont¹,²: jusa@aqua.dtu.dk
24  S.J. Traving\textsuperscript{1,8}: sjtraving@bio.ku.dk
25  A.W. Visser\textsuperscript{1,2}: awv@aqua.dtu.dk
26  N. Wadhwa\textsuperscript{1,5}: nawa@fysik.dtu.dk
27  T. Kiørboe\textsuperscript{1,2}: tk@aqua.dtu.dk

1: VKR Centre for Ocean Life.
2: National Institute of Aquatic Resources, Technical University of Denmark,
Charlottenlund Slot, Jægersborg Allé, DK-2920 Charlottenlund, Denmark
3: Center for Macroecology, Evolution and Climate, Natural History Museum of
Denmark, University of Copenhagen, Universitetsparken 15, 2100 Copenhagen,
4: Systemic Conservation Biology, J.F. Blumenbach Institute of Zoology and
Anthropology, University of Göttingen, Berliner Strasse 28, 37073 Göttingen,
5: Department of Physics, Technical University of Denmark
6: Department of Oceanography, University of Hawai‘i at Mānoa, 1000 Pope
Road, Marine Sciences Building, Honolulu, HI 96822, USA.
7: Department of Biomedical Sciences, Copenhagen University, Blegdamsvej 3,
2200 Copenhagen, Denmark
8: Marine Biological Section, University of Copenhagen, Strandpromenaden 5,
3000 Helsingør, Denmark
9: Faculty of Health and Life Sciences, Linnaeus University, Kalmar, Sweden
10: Consejo Nacional de Investigaciones Científicas y Técnicas, Argentina
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The size of an individual organism is a key trait to characterize its physiology and feeding ecology. Size-based scaling laws may have a limited size range of validity or undergo a transition from one scaling exponent to another at some characteristic size. We collate and review data on size-based scaling laws for resource acquisition, mobility, sensory range and progeny size for all pelagic marine life, from bacteria to whales. Further, we review and develop simple theoretical arguments for observed scaling laws and the characteristic sizes of a
We divide life in the ocean into seven major realms based on their trophic strategy, physiology and life history strategy. Such a categorization represents a move away from a taxonomically oriented description towards a trait-based description of life in the oceans. Finally, we discuss life forms that transgress the simple size-based rules and identify unanswered questions.
Introduction

Since the essay by Haldane (1928) “On being the right size” biologists have used organism size as a master trait to characterize the capabilities and limitations of individual organisms. There are good reasons for doing so. It is evident that the physiology and ecology of a copepod and a dolphin are vastly different, much more so than the difference between a copepod and a fish larva. Organism size describes individual physiology across major taxa through power-law functions (Peters 1983): metabolism, leading to the celebrated 3/4 law for the scaling of resting metabolism with size (Hemmingsen 1960, Kleiber 1932, West et al. 1997, Winberg 1956), population growth rates (Fenchel 1974, Gillooly et al. 2002), predator-prey relationships in terms of functional response (Hansen et al. 1997; Kiørboe 2011; Rall et al. 2012) and predator-prey ratios (Barnes et al. 2008, Cohen et al. 1993, Hansen et al. 1994), fluid-mechanical forces (Bejan & Marden 2006), swimming speed (Ware 1978; Kiørboe 2011), vision (Dunbrack & Ware 1987), diffusive uptake affinities (Aksnes & Egge 1991, Berg & Purcell 1977, Edwards et al. 2012, Litchman et al. 2007, Munk & Riley 1952, Tambi et al. 2009) and, for phytoplankton, affinities for light (Finkel 2001, Taguchi 1976) and maximum uptake rates (Edwards et al. 2012, Marañón et al. 2013). Size has also been used to describe macro-ecological patterns of size-dependent species diversity (Fenchel & Finlay 2004, May 1975, Reuman et al. 2014), and the biomass distribution of individuals as a function of size across major taxa (Boudreau & Dickie 1992, Sheldon & Prakash 1972) has been explained theoretically using the size relationships describing individual physiology (Sheldon et al. 1977; Andersen & Beyer 2006). While developing these size-
based relations the focus has been on determining the exponent (the “slope”) and the constant (“intercept”), with less attention being paid to the sizes that limits the range of their validity.

On closer inspection, some power-laws relationships are seen to change scaling exponent and/or intercept around some particular size or even break down altogether beyond a range of validity. The fluid flow around a whale, for example, is turbulent leading to dominance of inertial forces with a drag force scaling with the length and velocity squared. In contrast, the flow around a unicellular organism is laminar and dominated by viscous forces with a drag force scaling linearly with velocity and length. Consequently, the scaling of drag force changes at the organism size where there is a transition between viscous and turbulent flow. As example of a breakdown, consider the visual range. The larger the eye, the longer an organism can see. However, there is an upper visual range determined by the sensitivity of the retina (Dunbrack & Ware 1987), as well as a lower limit of eye size determined by the size of the visual elements in the retina and the wavelength of light. The scaling law for visual range is therefore valid only within the upper and lower limits. Such changes or breakdowns in scaling laws have consequences for adaptations and strategies of marine organisms. For example, predators so large that they are in the inertial fluid regime develop a streamlined body shape for efficient swimming and predators smaller than the lower size of an eye cannot rely on vision.
Haldane (1928) concluded that “For every type of animal there is a most convenient size, and a large change in size inevitably carries with it a change of form”. Our aim is to determine the sizes where scaling relationships change or break down and to use those characteristic sizes to explain the fundamental differences in the form and function of marine organisms with different sizes. To this end we build on the large existing literature of empirical size-based scaling relations and their theoretic explanations.

We categorize pelagic life in the ocean based on size in seven general realms: molecular life (viruses), osmo-heterotrophic bacteria, unicellular phototrophs, unicellular mixotrophs and heterotrophs, planktonic multi-cellular heterotrophs (e.g. copepods), visually foraging poikilotherms (e.g. fish), and homeothermic animals (whales). This categorization of life is a deliberately crude representation of the roughly 200,000 eukaryotic species, plus an unknown number of archa and bacteria, in the ocean (May & Godfrey 1994), as it is explicitly designed to facilitate an understanding based on size. We describe the life forms in each realm according to their body size and determine characteristic sizes where there is a transition from one realm to another. In this manner we emphasize body size as a fundamental driver of macro-ecological patterns in the oceans.

We examine five aspects of life where size is a dominant driver: (i) resource encounter through predation, diffusive uptake or photosynthesis, (ii) mobility, (iii) sensing through chemical and hydromechanical signals, vision, and
echolocation, (iv) life history strategy in terms of adult and progeny sizes and (v) body temperature (Figure 1). To this end we draw on a wide range of theories: diffusion theory, fluid mechanics, optics, metabolic theory, and optimal life history theory. We review established theoretical and empirical scaling laws and establish characteristic sizes where the scaling laws change or break down. These characteristic sizes are used to formulate hypotheses about the dominant strategy for organisms of a given size within the five aspects, e.g. how an organism obtains carbon (through photosynthetic assimilation of inorganic carbon, from dissolved organic matter, or from particulate organic matter), or which senses it employs for prey encounter. We test the hypotheses by collecting data on strategies of individuals as a function of their size. Since our arguments are general in nature they apply largely to all aquatic life but our focus is pelagic marine life. The final synthesis is a description of the dominant forms and functions of life in the oceans. This is used to frame a discussion of strategies and life forms that transcends the general size-based patterns and to point towards open unanswered questions.

What is ‘size’?

The size of an organism can be characterized by its length or by its weight. Wet weight, dry weight and carbon weight are the most common weight measures, while length is typically measured as the largest linear dimension or the equivalent spherical diameter (ESD). Depending on the question one measure may be more appropriate than the other. For example the flow around an organism is determined by its linear size and shape, not by its weight. Conversely, the bioenergetic budget of an organism is adequately described in
terms of weight since the energetic budget should reflect a conservation of mass.

For microbes weight is often measured in carbon or in units of the limiting nutrients since water content and ratios between fundamental elements vary between organisms (Klausmeier et al. 2004). The elemental ratios and water content of vertebrates vary less than they do for invertebrates so wet weight is often preferred as an intuitive measure of weight for vertebrates. Even though it would be possible, we do not find it useful to convert all sizes to a common measure and consequently use the most convenient measure depending on the situation. We will use the symbols \( w \) for a weight and \( l \) for length, \( d \) for diameter and \( r \) for radius and frequently make use of the conversion between length and weight as \( w \propto l^3 \). Units of weight are indicated with subscripts: \( g_{WW} \), \( g_C \), referring to wet weight and carbon weight. Conversion relations are provided in Table S1.1.

**Resource acquisition and trophic strategies**

Organisms acquire carbon and nutrients through feeding on encountered resources. “Resources” is here understood broadly as dissolved inorganic nutrients, dissolved organic molecules, photons or prey organisms. The encounter with resources occurs by three mechanisms: 1) active encounter through cruising, ambushing or creation of a feeding current, 2) fixation of carbon through photosynthesis or, 3) passive encounter with food items which diffuse towards the feeding individual. The encounter rate (biomass per time) is described as:
\[ E = \beta C \] (1)

where \( \beta \) is the clearance rate (volume per time) and \( C \) the resource concentration (biomass per volume). In terms of a type II functional response (Holling 1959) the clearance rate is the slope at the origin i.e., the potential volume of water cleared for resources per unit time when uptake is not limited by handling time or physiological limits (digestion). These limitations are not considered here. The clearance rate is described as a power function of size \( \beta = bl^a \). We employ the linear dimension \( l \) to characterize size because resource uptake is determined by the physical size of an organism, not by its weight. In the following we describe how the exponent \( a \) and the factor \( b \) depends on size for the three different resource acquisition mechanisms on the basis of physical processes and empirical cross-species relationships. This analysis allows us to characterize the dominant trophic strategy of organisms, e.g. phototrophs or heterotrophs, as a function of their size and the biotic and abiotic environment.

Active predation

Large protozoans and metazoa have three fundamental modes of actively encountering prey: ambushing, generating a feeding current or cruising through the water searching for prey (Kiørboe, 2011). The clearance rate of each mode \( \beta_A \) can be estimated as a velocity multiplied by an encounter cross section. A planktonic filter-feeder, for example, captures prey on its filter with a size scaling as the length of the organism squared \( l^2 \), with a feeding-current velocity \( u \approx l^{0.8} \) (Huntley & Zhou 2004) leading to a scaling exponent of the clearance rate of
Using similar arguments for the other feeding modes all lead to exponents \( \approx 2.8 \), i.e. slightly below 3, but multiplied by different factors (Kiørboe 2011). Since one feeding mode replaces the other depending on environmental conditions and the size of the prey and the predator, the average life-form-transcending scaling exponent becomes around 3 (Figure 2a; Table S1.2):

\[
\beta_A = b_A l^3
\]

Weight-specific uptake rates, \( \propto \beta_A/w \), are therefore independent of size since \( w \propto l^3 \) (Kiørboe & Hirst 2014).

**Photosynthesis**

Fixation of dissolved CO\(_2\) by photosynthesis requires encounter with photons (we assume that CO\(_2\) is not limiting). Photosynthesis can in principle occur throughout the cell but for larger cells it is limited by self-shading of photons (the "package effect") (Morel & Bricaud 1981). For the present arguments, it is sufficient to consider that the cross-sectional area of the cell \( \propto l^2 \) limits photosynthesis (Figure 2b):

\[
\beta_l = b_l l^2 \quad (2).
\]
The clearance rate $\beta_L$ is often termed light affinity or photosynthetic efficiency and is measured in dimensions of carbon fixed per photon multiplied by area. In terms of weight specific scaling, the power 2 scaling of $\beta_L$ results in a scaling of weight specific rates of carbon fixation $\beta_L/w \propto w^{-1/3}$, i.e. smaller organisms have a higher specific rate of carbon fixation than larger ones. Organisms smaller than a certain size are therefore able to fix more carbon by photosynthesis than by active encounter since specific uptake by active encounter is independent of size.

**Diffusion feeding**

Organisms that encounter resource items as they bump into the surface of the organism due to Brownian motion are termed “diffusion feeding” (Fenchel 1984). Diffusion feeding is used to assimilate dissolved organic molecules, inorganic carbon and nutrients. The uptake rate is limited by the number of uptake sites on the surface of the cell, which can be expected to scale with $l^2$. However, the uptake also removes resources from the vicinity of the cell surface and creates a boundary layer of lower resource concentrations near the cell than far away (Munk & Riley 1952). This effectively leads to the clearance rate $\beta_D$ being limited rather by diffusion than by the surface, with a scaling proportional to the linear dimension of the cell (reviewed by Fiksen et al. 2013):

$$\beta_D = b_D l^3 \quad (3).$$
Weight specific uptake rates are then $\propto w^{-2/3}$, i.e., high for small cells and declining with size. Small diffusion feeding cells therefore have a higher encounter rate with dissolved nutrients or macromolecules than they could have obtained by active feeding. The theoretic scaling prediction fits with data for phosphate affinity (Figure 2c). Data for nitrogen affinity are less clear, with some being consistent with the theoretic scaling ($a_D = 1.2$) (Litchman et al. 2007) and others not ($a_D = 2.25$) (Edwards et al. 2012).

Trophic strategies

An organism's trophic strategy, i.e., which type of food it consumes, is to a large degree determined by its resource acquisition mechanism. It can be an osmo-heterotroph that diffusion feeds on dissolved organic matter (bacteria), a phototroph that captures light and diffusion feeds on dissolved inorganic nutrients (phytoplankton), a mixotroph that captures light and feeds on other organisms, or an actively feeding heterotroph (animals and many protists). If we use clearance rate as a proxy for competitive ability at low resource concentrations, we can assume that the dominant trophic strategy of organisms at a given size is determined by the resource acquisition mechanism yielding the highest encounter rate. The encounter rates for the four trophic strategies as a function of size is given by Eq. 1 where the resource may be either concentrations of dissolved organic molecules $C_{DOM}$, nutrients $C_N$, other prey organisms $C_P$, or the light flux $C_L$. Phototrophs need special treatment since they assimilate inorganic carbon and nutrients by two different processes. Carbon is
assimilated through photosynthesis and combined with diffusively encountered nutrients to achieve a C/N ratio $c_{CN}$. The limiting compound determines encounter as described by Liebig’s law of the minima:

$$E = \min\{c_{CN} \cdot \beta_d \cdot C_N, \beta_L \cdot C_L\}.$$  

For a particular environment of light, nutrients, organic matter and prey, an organism encounters different specific amounts of resources from the various encounter mechanisms (Figure 3). The smallest organisms get the highest encounter rate from diffusive encounter with dissolved organic matter. Diffusion feeding heterotrophic bacteria (osmo-heterotrophs) will therefore dominate among the smallest organisms. As size increases, encounter with photons becomes sufficiently high to make photosynthesis combined with diffusive uptake of inorganic nutrients optimal, i.e., the dominant strategy becomes phototrophy. The transition size is when carbon fixation by photosynthesis $\beta_l C_l = b_l l^2 C_l$ becomes equal to the diffusive encounter with dissolved organic matter $\beta_d C_{DOM} = b_d l C_{DOM}$, which occurs at a size:

$$l = \frac{C_{DOM} b_d}{C_l b_L}. \quad (4)$$  

Cells larger than this size are expected to be light-limited phototrophs. When the cells reach a size
\[ l = \frac{c_{CN}C_Nb_D}{C_Lb_L} \] (5)

\[ l = \frac{c_{CN}C_Nb_D}{C_Fb_A} \] (6)

the diffusive uptake of inorganic nutrients becomes limiting (Mei et al. 2009).

Larger cells will still benefit from acquisition of carbon through the aid of photosynthesis but they will be nutrient limited. At a size

\[ l = \frac{c_{CN}C_Nb_D}{C_Fb_A} \] (6)

active encounter with prey organisms provides the highest encounter rates, i.e., heterotrophic animals. There is a particular range where photosynthesis will provide more carbon than active encounter (predation) but where active encounter provides more nutrients than diffusive uptake of inorganic nutrients.

In this size-range a mixotrophic strategy is profitable, i.e. using photosynthesis, either from ingested or own chloroplast, predominantly to provide carbon for metabolism, and using active feeding to assimilate nutrients and carbon for biomass synthesis (mixotrophs of type II and III; Stoecker, 1998).

The size range where a certain trophic strategy gives the highest yield depends on the concentration of available resources. If, for example, the concentration of prey organisms is increased, the lower size limit where active feeding gives the highest yield is decreased. The transition size between the dominant feeding strategies will therefore be different under oligotrophic conditions (high light and low nutrient concentrations, such as summer surface conditions in seasonal
environments or oceanic regions) than under eutrophic conditions (low light and high nutrient concentrations, such as spring surface conditions in seasonal environments or conditions at depth) (Figure 4a+b). The general pattern of small diffusion feeders, medium phototrophs, and large active feeders is identical between oligotrophic and eutrophic environments, but the sizes where the transitions occur vary: oligotrophic conditions give rise to smaller phototrophs and a large size-range of mixotrophs, while eutrophic situations conditions lead to larger osmo-heterotrophic bacteria, phototrophs and mixotrophs. The general pattern fits well with the classical interpretation of the seasonal succession of cell size in temperate systems (Kiørboe, 1993): large (diatoms) cells dominate during nutrient rich spring conditions but are overtaken by smaller cells (dinoflagellates and cryptophytes), often with a mixotrophic strategy during the nutrient depleted summer conditions (Barton et al. 2013).

A compilation of the dominant trophic strategies according to size largely confirms the theoretical predictions while also highlighting the large overlap in the size-range between phototrophs, mixotrophs and small heterotrophs (Figure 4c). The overlap reflects that the compilation is based on the observations from various environmental conditions that, as demonstrated above, create a significant variation in the transition sizes where one trophic strategy gives a higher yield than another strategy.

**Mobility**

Movement is powered by muscles or flagellae and constrained by friction from the water. From an organism’s perspective the nature of the water changes.
dramatically with size: large organisms use their inertia to coast through the water while smaller organisms experience water as thick and sticky. Very small organisms have to cope with the random forces of molecules that induce Brownian motion (Dusenbery 2009). The hydromechanics of movement can therefore be divided into three regimes: an inertial regime, a viscous regime and a Brownian regime. Here we are mainly concerned with the difference between the inertial and viscous regimes. The hydrodynamic regime determines the forces upon the body, which in turn influences the optimal shape. In the viscous regime the dominating force is surface friction, which scales with the linear dimensions of the body. In the viscous regime it is therefore optimal to reduce the surface area, i.e. to be spherical (actually, the optimal shape is deviating slightly from spherical; Dusenbery, 2009). In the inertial regime the drag force is proportional to the projected frontal area of the organisms making it optimal to reduce this area by streamlining.

Whether an organism is in the inertial or viscous regime depends on the Reynolds number \( Re = ul/\nu \) that describes the ratio between inertial and viscous forces operating on a body of size \( l \) moving at velocity \( u \) through water with kinematic viscosity \( \nu \approx 10^{-2} \text{ cm}^2/\text{s} \). The crossover between the two regimes is at \( Re \approx 20 - 30 \) (Webb 1988). The scaling of swimming velocity with size in the two regimes differs: in the viscous regime the velocity was found empirically to scale as \( l^{0.79} \) (Kiørboe, 2011) while in the inertial regime theoretic arguments predict a length scaling with exponents 0.42 (Ware 1978) or 0.5 (Bejan & Marden 2006); observation suggest a scaling \( u \propto l^{0.45} \) (Figure 5a). The
empirical data indicate a crossover size between the viscous and inertial regime at body length of around 7 cm corresponding to a Reynolds number on the order of 1000. The relevance of size for body shape is evident (Figure 5b): small organisms do not appear constrained on their body shape, while fish and mammals are streamlined with an average aspect ratio around 0.25. Copepods are in between; they have a significantly larger aspect ratio than fish. During jumps, however, the Reynolds number becomes large thus giving them the advantage of a relatively slender body plan (Kiørboe et al. 2010).

**Size and sensing**

Actively feeding organisms perceive their prey by chemical or hydromechanical cues, vision, or echolocation. The range of sensing is determined by the size of the predator and the prey; a blue whale with an eye diameter of 15 cm sees much further than a fish larva with an eye diameter of 1 mm. The sense with the furthest range for organisms of a given size can be expected to dominate among organisms of that size. Organisms using more than one sense complicate the analysis of senses. For example, sharks use smell to follow the trail of a prey at great distances. When closing in on the prey, vision becomes important (Hueter et al. 2004). At distances below one meter they use electro-sensing for the precise localization of their prey (Collin & Whitehead 2004). Copepods are generally considered mechanosensing organisms, yet they can sense and follow the chemical trail of a settling marine snow particle (Kiørboe 2001) or the pheromone trail of a potential mate (Bagøien & Kiørboe 2005). Leaving such complications aside we nevertheless proceed to review estimates of the sensory
range of four senses where the sensing range depend on the size of the predator: chemical sensing, sensing of hydromechanical signals, vision and echolocation.

**Chemosensing**

In that all organisms depend on chemistry in one way or another, it may be safely assumed that they have machinery for chemical sensing. The question is how chemosensing together with behavior can bring organisms into contact with remote resources. The way organism’s experience the coherence of chemical gradients and trails is determined by individual size in relation to turbulent eddies. Turbulence is characterized by three length scales (Tennekes & Lumley 1972): the Batchelor scale, \( \approx 10 \, \mu m \) in the upper ocean, where turbulence starts to erode the regularity of a gradient, the Kolmogorov scale \( \approx 1000 \, \mu m \) where turbulence starts to impede the organism’s ability to maintain direction, and the integral scale \( \approx 1-10 \, m \) where turbulent energy is injected by large-scale motions.

We distinguish between two modes of chemosensing: gradient climbing (e.g. bacterial run-tumble) and trail following (e.g. a shark following a prey trail). Gradient climbing relies on a chemical gradient set up by molecular diffusion of a solute from a source. The regularity of such gradients would be scale independent if it were not for turbulence. We can place an upper boundary for gradient climbing at between the Batchelor scale and the Kolmogorov scale, in the range from 10-1000 \( \mu m \). Another limitation of the ability to follow gradients created by molecular diffusion is whether the trail is diffusing faster than the
movement of the prey. This criterion sets an upper limit for predator size of 50 μm (Kiørboe 2011). For trail following, additional criteria come into effect: the movement of the target organism, the rate at which it releases solute and how well the searching organism can detect this solute above background levels. In any case, organisms smaller than the energy containing turbulent eddies will experience the trail as patchy and therefore need to search large areas relative to their own size to follow the trail. This scenario is relevant for organisms of a size between the Kolmogorov and the integral length scales, i.e. organisms smaller than 1 m. Organisms larger than the integral scale are able to integrate over the subscale trail details and follow a trail without detours. Trail following is therefore most advantageous for large organisms and/or quiescent environments, e.g. the deep oceans (Martens et al.).

Mechanosensing

Ambush feeders may sense their prey via the fluid mechanical disturbance created by a moving prey (reviewed by Kiørboe 2011). To enhance the sensory range they employ special sensory arrangements protruding from the body, like the long setae-studded antennules on copepods or the sensory hairs arranged along the slender body of chaetognaths (arrow worms). The fluid mechanical disturbance of a self-propelling prey can be modelled as a stress-let which implies that the signal attenuates as the cube of the distance away from the prey (Visser 2001). The range that this signal can be sensed is

\[ R \approx \left(3 l_{prey}^2 l_{sensor} u_{prey}/u^*\right)^{1/3} \]

where \( u^* \) is the detection limit of the velocity disturbance and \( l_{sensor} \) is the length of the sensor, approximately the size of the
predator. Using $u_{\text{prey}} = b l_{\text{prey}}^{0.74}$ and a predator-prey length ratio $B \approx 10$ the sensing distance is $R \approx c l^{1.24}$ with $c \approx 1.4 \text{ cm}^{-0.24}$ for $u^* = 33 \mu\text{m/s}$ (Kørboe 2011) (Figure 6). An upper range comes into effect when the turbulent shear $\gamma$ across the body of the predator organism approaches the sensitivity; i.e. when $u^* = \gamma l$. For moderate turbulent shears found in the upper ocean (0.03 s$^{-1}$ which in the middle of the typical range of $10^{-4}$-10$^{-1}$ s$^{-1}$; Visser & Jackson 2004), this happens for $l$ in the range 500-1000 µm. Mechanosensing is therefore most advantageous for small organisms (<1 cm) or on short ranges for large organisms.

**Vision**

Eyes contain photoreceptors that detect light and convert it into neuronal signals. The simple eyes of some microorganisms are only able to detect changes in the ambient light sufficient for detection of diurnal rhythms, orientation towards the surface and nearby movement. Active visual predation requires an eye with sufficient resolution to form an image and preferably also active optical machinery to focus a targeted object. With regards to feeding, the most important property of the eye is the distance at which it can discern a suitable prey.

[Sidebar 1 near here]

Dunbrack and Ware (1987) modelled the optical and sensing abilities of a camera eye to estimate the visual range of a predator of length $l$ searching for
prey with a fixed fraction of the predator size (Sidebar 1). Two important conclusions emerge from their arguments: First, the sensing range scales as $l^{1.75}$ in clear water under high light conditions. Second the maximum range of large organism is limited by the optical properties of the water. Under perfect conditions the range is between 40-70 m (Davies-Colley & Smith 1995). The range decreases with the ambient light such that at depth, where the inherent contrast is low, visual range is mainly limited by the optical properties of the water.

A lower size limit of a functioning eye is determined by the finite size of the photoreceptor. Photoreceptors' functioning relies on opsin molecules (rhodopsin) stacked in rod cells with a width $d_{rod} \approx 1\ \mu m$ (Curcio et al. 1990). Taking account of the universality of the opsin design for photoreception, we may consider this length a limiting factor for building eyes. Considering a minimal resolution of, say $100^2$ for sufficient image formation, results in a retina size of $d_r \approx 0.1\ mm$. This is about $1/10$ of the size of the smallest aquatic organisms with camera eyes: larval fish and cephalopods. Therefore, vision is only a viable sensing mode for organisms in the size range from a few millimetres and up.

Echolocation

Echolocation is an active sensing mode, where the animal emits ultrasonic calls and interprets the environment based upon the echo of these calls. It is common
for toothed whales (Odontocetes) and while it is also used for orientation, here
we focus on echolocation and its role in prey detection.

We can estimate how the range $R$ of echolocation scales with the size of the
animal based on three assumptions: 1) The sensitivity of the ear $P_0$ is
independent of the size of the animal, 2) the emitted power scales with an
exponent $p$ as $P_e \propto w^p \propto l^{3p}$, 3) we ignore frequency dependent attenuation of
sound in seawater because this attenuation is small compared to the conical
spread of the sound wave. In free space the emitted signal spreads as a conic
beam resulting in the attenuation of the signal power as $R^{-2}$. The power of the
reflected signal is $P_r \propto P_e l^2_{\text{prey}} (2R)^{-2}$ where $l^2_{\text{prey}}$ is the area of the reflecting
target and the factor 2 is because the signal attenuates both as it travels towards
the target as well as when it returns. Inserting the power of the emitted signal
and absorbing the factor 2 in the proportionality constant gives $P_r \propto l^{3p} l^2_{\text{prey}} R^{-2}$.
The distance where the strength of the returned signal is just at the sensitivity of
the ear, i.e. $P_0 = P_r$, scales as $R \propto P_0^{-1/2} l^3_{\text{prey}} $. If the preferred prey size scales
with the size of the predator, i.e. $l_{\text{prey}} \propto l$, then:

$$ R \propto P_0^{-1/2} l^{1+3p}/2. $$

If the power of the emitted sound follows metabolic scaling, $p = 3/4$ then the
exponent becomes 17/8. This argument only provides the scaling of the sensing
range; the factor can be found by fitting to data (Figure 6a).
Size and sense

The theoretic arguments outlined above identified three characteristic sizes where one sense becomes more efficient than another: 1) an upper size limit for gradient climbing at a predator size of around 100 μm; 2) predators larger than that 100 μm but smaller than 1 mm are expected to rely predominantly on hydromechanical sensing, 3) a size where vision becomes viable for a predator's of around 1 cm, and 4) a size of around 1 meter or larger where predators are able to realize the upper visible range of up to 80 meter in clear water. An extension of the sensory range beyond this length can only be achieved by trail-following chemical tracers or by echolocation.

Analysis of body size and senses used by marine organisms reveals that the number of possible senses available to a predator increases with size (Figure 6b). Large organisms typically combine several senses for foraging. The lower size limit of vision around 1 cm is clearly borne out; this size indeed corresponds to the smallest size of fish and cephalopods larvae. Some large life forms do not use vision to detect prey, most notably the gelatinous zooplankton, even though they are much larger than 1 cm. Seen in this perspective, the strategy of gelatinous zooplankton is to avoid building a vertebrate body with its associated high metabolic requirements to utilize the increasing sensing range that vision provides but rather depend on an inflated body to increase the prey encounter cross section (Kiørboe 2013). The superiority of vision declines with
ambient light so the relative disadvantage of gelatinous zooplankton versus fish diminishes in turbid water or in deep waters (Sørnes & Aksnes 2004).

**Life history and progeny size**

Though obvious on the individual level, the concept of size becomes ambiguous when applied at the species level since all life differs in the size of adults and progeny; even unicellular organisms need to double their size before they can divide. The difference between adult and progeny size is most extreme among the teleosts (bony fish) where the weight ratio between adults and larvae can be up to $10^8$ for bluefin tuna.

[sidebar 2 near here]

**Optimal life history theory**

The evolution of life history with a pronounced difference between adult and offspring size can be understood from optimal life history theory (Andersen et al. 2008, Christiansen & Fenchel 1979). If we assume 1) standard metabolic scaling of consumption $= Aw^n$ with $n \approx 3/4$ (West et al. 1997); 2) metabolic scaling of mortality $a Aw^{n-1}$ (Andersen & Beyer 2006, Hirst & Kiørboe 2002, Peterson & Wroblewski 1984); and 3) determinate growth, then the lifetime reproductive output $R_0$ becomes (Sidebar 2):

$$R_0 = \frac{\varepsilon}{2\alpha} \left(\frac{W}{w_0}\right)^{1-\alpha}, \quad (7)$$
where $W/w_0$ is the ratio between the weight at maturation and weight of offspring, $\epsilon$ is the efficiency of reproduction and $\alpha$ is the physiological mortality, which is less than 1 (Andersen et al. 2008). Because the exponent $1 - \alpha$ is positive $R_0$ is an increasing function of $W/w_0$. The metabolic assumptions thus predict an evolutionary pressure towards a life history with as large a ratio between adult size and offspring size as possible. Since no organisms has an infinite ratio between adult size and offspring size, a full understanding of what limits actual offspring size cannot be achieved from optimal life history theory based on metabolic scaling laws alone; the actual offspring size will be limited by other processes.

Offspring size strategies

Observed offspring size strategies employed by marine life can roughly be partitioned into two groups: a “fixed-ratio” strategy where offspring size is a constant fraction of the adult size and a “small-eggs” strategy where offspring size is the same, independent of adult size (Neuheimer et al.) (Figure 7). Crustaceans, cartilaginous fish and whales employ the fixed-ratio strategy with an adult:offspring weight ratio around 100:1. The metabolic optimal life history theory (eq. 7) is unable to predict the fixed-ratio strategy. For marine mammals the fixed-ratio strategy can be explained by the need to perform parental care (Shine 1978). For the other groups, the fixed-ratio strategy can be explained by an elaboration of the evolutionary argument in sidebar 2, to account for density dependent effects (Olsson et al.). Such elaboration shows that the strategy that maximizes $W/w_0$ is only optimal if the
offspring do not experience density dependent effects right at the time of hatching. If they do experience density dependent survival early in life, an evolutionary stable strategy with $W/w_0 \approx 100$ emerges.

**Transitions between life forms**

We have reviewed how size influences resource acquisition, mobility, ability to sense prey, and life-history strategy, based on theoretical arguments and cross-species empiric analyses. We now use these relations to understand the mechanisms behind the transitions between the seven realms of marine life: molecular life, osmo-heterotrophic bacteria, unicellular phototrophs, unicellular mixotrophs and heterotrophs, planktonic multi-cellular heterotrophs with ontogenetic growth, visually foraging poikilotherms, and homeothermic animals (Figure 1 and Table 1). These seven realms correspond to the traditional taxonomic division of life between viruses, bacteria, phytoplankton, uni- and multicellular zooplankton, fish and marine mammals. Our alternative naming reflects the function of the groups and highlights the factor that determines the characteristic size where there is a transition between the groups.

A central theme is that development of larger size opens new possibilities for resource acquisition and sensing. Examples are how the battery of available senses increases with size (Figure 6), how the emergence of multicellularity makes it possible to increase the adult:offspring size ratio and thereby increase fitness (Sidebar 2), or how mortality decreases with size. Larger size therefore increases the competitive
edge, provides access to new resources as well as increases survival. The sizes where new possibilities appear often mark a transition between the major life forms because the utilization of new senses etc. require fundamental changes in body plan and life strategy.

From viruses to cells

The smallest size of a cell is around $10^{-15}$ gC with a diameter around 0.1 – 1 μm. Organisms this small are believed to be functionally limited by metabolic constraints (Kempes et al. 2012) and the size of non-scalable components: genome size (DeLong et al. 2010) and in particular the cell wall (Raven 1994).

The wall size along can be used to calculate a lower limit for cell size: The wall has a mass $c_{\text{wall}}d^2$ and the cell itself $cd^3$ where $c_{\text{wall}}$ and $c$ are constants. If we ignore the genome a theoretical lower limit to cell size is when all cell mass is used by the wall:

$$
\frac{d_{\text{limit}}}{d} = \frac{c_{\text{wall}}}{c}
$$

For a 0.5 μm cell the wall comprises about 30 % of the total mass (Raven 1994), so $c_{\text{wall}}/c \approx 0.3 \times 0.5$ μm. This gives a lower limit cell size of $d_{\text{limit}} \approx 0.15$ μm.

From osmo-heterotrophs to phototrophs

The smallest unicellular organisms are heterotrophic bacteria feeding on dissolved organic matter encountered through diffusion. At a diameter
\[ \frac{C_{\text{DOM}} b_d}{C_L b_L} \] (eq. 4), it becomes favourable to fix inorganic carbon through photosynthesis instead of relying on dissolved organic matter. This size depends on the relative concentrations of dissolved organic matter \( C_{\text{DOM}} \) and light \( C_L \), but it can be as small as \( 10^{-14} \text{ g}_C \) in the upper photic zone with concentrations of dissolved organic matter \( C_{\text{DOM}} \approx 5 \text{ \( \mu \text{g}_C \)/l} \) and abundant light \( (C_L \approx 7 \text{ J day}^{-1} \text{m}^{-2}) \) and increases as a light decreases (Figure 4).

**From phototrophs to heterotrophs**

The smallest phototrophs are expected to be carbon limited (which in practice means that they are limited by the amount of light since dissolved inorganic carbon is assumed to be plentiful), while the largest phototrophs are expected to be nutrient limited. This difference emerges from the different scaling of nutrient encounter that scales with \( l^1 \) and light encounter that scales with \( l^2 \) (Eqs. 2 and 3 and Figure 3). As before, the exact sizes where the transitions between light limited phototrophs, nutrient limited phototrophs, and heterotrophs occur depend on the specific conditions of dissolved nutrients, light and suitable prey (Figure 4b).

An order-of-magnitude estimation of the characteristic transition between phototrophs and pure heterotrophs is \( 10^{-7} \text{ g}_C \) \( (l \approx 6 \times 10^{-2} \text{ cm}) \), but it can vary between \( 10^{-8} \text{ g}_C \) in low light and high nutrients situations and \( 10^{-5} \text{ g}_C \) in situations of high light.
The size that marks the transition between phototrophs and heterotrophs is blurred by a large group of mixotrophic organisms that acquire nutrients and carbon for biomass synthesis from phagotrophy while photosynthesis primarily provides carbon for metabolism. The mixotrophic strategy is most favourable for organisms with sizes in the transition between phototrophy and heterotrophy. The size range where the mixotrophic strategy is favourable varies with environmental conditions: it is vanishingly small in eutrophic conditions and increases to more than a factor 10 in diameter in oligotrophic conditions, in agreement with observations (Barton et al. 2013).

Unicellular to multicellular life

The drive to develop larger size eventually leads to multicellular organisms. Multicellularity opens the possibility of specialized tissue for, e.g., sensory organs. Among microscopic metazoans the dominant group of copepods has developed sensory apparatus to detect prey via hydromechanical cues and appendages to generate feeding currents and make jumps to escape predators. We have not developed a specific argument for the size where the transition to multicellularity occurs, but since life-history theory predicts that increasing offspring-adult size ratio increases lifetime reproductive output (Eq. 7), it is likely to occur at the smallest possible size. DeLong et al. (2010) argue that this is when it becomes possible to develop a fractal delivery network, around $10^{-6} \text{g}_{C}$ ($\approx 1 \text{µm}$). The drive towards minimization of offspring and maximization of adult size means that each metazoan group strives to extend its size range, but is
only able to do so within the limits defined by the sizes where there is a breakdown in a scaling relationship describing a vital function.

From copepods to fish

Fish (including cephalopods) are the dominant organisms in the size-range from 1 mg\textsubscript{ww} to about 100 kg (1 cm to 2 m). Fish are characterized by being streamlined, visual predators. At a size smaller than 1 mg\textsubscript{ww} the dominating organisms are blind copepods, with a very non-streamlined body plan. The transition size between these two very different life forms is characterized by the transition from the superior sensing mode being mechanosensing to vision and the transition from a viscous to an inertial hydromechanical regime. The change in hydromechanical regime explains the slender fish shape, but it also entails a change in feeding mode. Fish larvae employ suction feeding, which becomes increasingly difficult the smaller they are (China & Holzman 2014). Probably the most important transition is in sensing, with the lower size limit of fish coinciding with the lower size of a functioning eye. Were fish to make smaller eggs their larvae would be unable to compete with the tactile sensing copepod with a morphology designed for optimal movement and prey capture in a viscous fluid environment; were copepods to become larger they would be outcompeted by visually sensing fish with streamlined bodies.

From fish to whales

Whales are the largest organisms in the oceans, occupying the size range from about 100 kg and up. It is tempting to attribute the transition from fish to whales
to the appearance of echolocation as a possible sensing mode. However, only
toothed whales employ echolocation for sensing, whereas baleen whales rely on
the same senses as fish. If there are no change in the power law relationships
determining sensing and food encounter, why, then, have teleosts not evolved
even larger sizes than the few hundred kilos of the largest fish (bluefin tuna or
sunfish with maximum weights of 450 and 1000 kg)711? We propose two
arguments for the transition between fish and marine mammals: a metabolically
based upper limit of a water-breathing organism (Freedman & Noakes 2002;
Makarieva et al. 2004, Supp.) and a lower size limit of a homeothermic (warm-
blooded) organism.

We have focused on acquisition of resources in terms of carbon and nutrients,
but heterotrophs also need oxygen to fuel their metabolism. The absorption of
oxygen through gills is limited by the surface of the gills. Since the surface of gills
is fractal it will scale with an exponent between 2/3 and 1, probably very close to
the metabolic exponent of 3/4. The acquisition of oxygen therefore scales with a
similar exponent as metabolism, so the relative ability to acquire food and
oxygen is independent of size. However, larger organisms accumulate heat
created by activity and use this to elevate their metabolism. Notable examples
are the scombroids (tuna and marlin) and pelagic sharks (Block 1991). A high
body temperature means higher activity and therefore higher predatory success
against slower heterothermic (cold-blooded) prey. Such an increase in
metabolism will eventually require more oxygen than can be obtained by
pumping water over the gills. This problem is solved by ram ventilation, which
provides a higher flow of water around the gills and therefore a higher oxygen absorption rate. Evidence for this is provided by the largest fish being either very active ram-ventilating (large scombroids or sharks) or relatively sluggish pumping (sunfish). We conjecture that it would be impossible for fish to develop homeothermy as a means of competing with marine mammals; the solubility of oxygen in water is simply too low to fuel a homeothermic metabolism. Marine mammals fuel their high homeothermic metabolism by breathing air, which has a much higher solubility of oxygen than water.

For homeotherms the loss of body heat should be included in the energy budget as this defines a lower limit for the size of a homeotherm (Haldane 1928). Heat loss is a surface process that scales as \( \propto \kappa w^{2/3} \) where \( \kappa \) is the thermal conductivity of water. Since organisms wish to minimize heat loss their surface is not fractal and the exponent is not larger than 2/3. The energy for heating comes from the acquisition of resources (oxygen and food), which scales metabolically as \( A w^{3/4} \). The size where there is a balance between loss of heat and acquisition of resources defines a lower limit of homeothermy as \( (A/\kappa)^{12} \) (Andersen et al. 2008). This lower limit is very sensitive to the value of the parameters \( A \) and \( \kappa \) since their ratio is raised to a high exponent. For example, the ratio between the lower limits calculated for a marine and a terrestrial habitat is the ratio between the heat conductivity in air and water (\( \approx 20 \)), raised to power 12 which gives \( 4 \times 10^{15} \). This factor is much larger than the ratio between the smallest whale, a harbour porpoise calf of around 10 kg, and the smallest terrestrial homeotherm, an Etruscan shrew (\( Suncus etruscus \)) at around 0.1 g. Nevertheless it seems
evident that the smallest land animals are limited by loss of heat, e.g. shrews
huddle together to conserve heat, so how can whales manage to attain a small
size in the face of a larger heat loss? We hypothesise that whales do that by
having an insulating layer of blubber. To achieve a lower size of 10 kg (a factor
10^6 smaller than predicted), whales need to decrease heat losses by a factor
10^{6/12} \approx 3.2 relative to terrestrial animals, which is not out of scope.

Beyond size

We posit that individual size is the most important trait characterizing a pelagic
organism. Knowing the size, it is possible to estimate, often within an order of
magnitude, the metabolic rate, the clearance rate, the swimming speed and the
sensory range. We have shown how that information facilitates inference of
trophic strategy, sensory mode, body shape, and, to some degree, reproductive
strategy. Though important, we have largely ignored the subtle interplay
between temperature, oxygen concentration and size (Verberk & Atkinson
2013). Even though size can be characterized as a “master trait” (Litchman &
Klausmeier 2008), it is not the only trait that characterizes an organism. The
relevant question is then which other traits best characterize the variation
around the mean in the reviewed relations with size (Figure 2, 5 and 7). We propose three candidate traits to consider: predator-prey
size ratio, “feeding mode” for heterotrophic metazoans and “jellyness”.

Among heterotrophic metazoans there appear to be two dominant strategies to
 predator-prey size ratio: a fixed predator-prey length ratio in the range 10-100, which is the strategy followed by most fish and copepods (Barnes et al. 2008), or
a strategy aimed at preying on organisms much smaller than the predator. The small-prey strategy is used by the largest zooplankton, the pelagic tunicates, and by the largest vertebrates, the whale sharks and the baleen whales. Organisms with a large predator-prey size ratio rely on filtering the water to catch the prey. It is presently unknown what drives the development of the two alternative, but apparently equally competitive, strategies.

The feeding mode determines whether an actively feeding predator encounters its prey through ambushing or cruising. It is often assumed that predation pressure is a function of size only and therefore independent of feeding strategy or sensing mode. This is not quite true. It is becoming increasingly evident that feeding strategy is associated with a trade-off in mortality: an ambush feeder will encounter less prey than a cruising predator but it will also have less exposure to predation and therefore lower mortality. A quantitative demonstration of this trade-off has been made for zooplankton based on laboratory experiments (Kiørboe 2013b) and the importance for the seasonal succession has been modelled (Mariani et al. 2013). These trade-offs likely apply at least qualitatively to other predators, e.g. fish.

A related trade-off is the development of a gelatinous body (jellyfish, box jellies and pelagic tunicates). We argued in section “sensing” that visual predators would be superior to predators sensing their prey through hydromechanical forces. However, the inflated body size of gelatinous organisms results in a large encounter cross-section and hence a higher clearance rate than a non-gelatinous
organisms with the same carbon body mass. This is what makes the jelly-
strategy effective even in the same size range where visual predation is possible
(Acuña et al. 2011), particularly under low light conditions (Sørnes & Aksnes
2004). At the same time the gelatinous body makes the organism less attractive
to predators thereby lowering its mortality. These two examples show how the
general “rules” inferred from size scaling of encounter, mobility, and sensing can
be transgressed by other traits.

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Acronyms and definitions

**Power law**: \( y = ax^b \) with factor \( a \) and exponent \( b \). Linear regression employs a logarithmic transformation: \( \log y = \log a + bx \), with \( \log a \) being “intercept” and \( b \) the “slope”.

**Poikilotherm**: An organism that maintains the same body temperature as the environment, in contrast to a **homeotherm** which maintains a constant body temperature due to internal heat sources.

**Protists** are simple, typically unicellular, eukaryotic organisms, living in aquatic environments.

An organism’s **trophic strategy** describes how it gathers nourishment. The suffix “troph” derives from ancient Greek: *trophe* = food, nourishment; *drepo* = to gather.

**Phototrophs** rely on photosynthesis as their carbon source and use **osmotrophic** diffusive uptake of nutrients. In contrast **phagotrophs** up carbon and nutrients by absorbing other living organisms. **Mixotrophs** employ a mixed strategy, typically combining photosynthesis with phagotrophy.

*Note for production:* The above definition is longer than 20 words (37), but it also defines four terms.
Cartilaginous fish (Chondrichthyes) are fish with skeletons made of cartilage rather than bone, containing elasmobranchs (sharks, rays and skates) and Holocephali ("ghost sharks").

Cephalopods are squid, octopi and cuttlefish, commonly referred to as “inkfish”.

The physiological mortality is the ratio between mortality and weight-specific consumption. With metabolic scaling of uptake $Aw^{3/4}$ and mortality $cw^{-1/4}$ the physiological mortality becomes $\alpha = c/A$.

Stresslet: A stokes flow produced by 2 co-linear anti-parallel point forces acting on a fluid.
Table 1. Characteristic sizes of transitions between major realms of life in the ocean.

<table>
<thead>
<tr>
<th>Transition</th>
<th>Size</th>
<th>Notes</th>
</tr>
</thead>
<tbody>
<tr>
<td>Lower size of a cell</td>
<td>$0.15 , \mu m \approx 10^{-15} , g_C$</td>
<td>Limited by cell wall and to a lesser extent genome size (Eq. 8)</td>
</tr>
<tr>
<td>Osmo-heterotrophs to phototrophs</td>
<td>$10^{-14}$ to $10^{-13} , g_C$</td>
<td>Transition from diffusion feeding on DOM to photosynthesis (Eq. 4).</td>
</tr>
<tr>
<td>Phototrophs to mixotrophs</td>
<td>$10^{-8} , g_C$</td>
<td>Transition from acquiring inorganic nutrients by diffusion feeding to acquiring nutrients by active feeding (Eq. 5)</td>
</tr>
<tr>
<td>Mixotrophs to heterotrophs</td>
<td>$10^{-7} , g_C$</td>
<td>Acquisitions of carbon and nutrients solely by predation through active feeding (Eq. 6)</td>
</tr>
<tr>
<td></td>
<td>$(10^{-8}$ to $10^{-6} , g_C)$</td>
<td></td>
</tr>
<tr>
<td>Single- to multicellular organisms</td>
<td>$10^{-6} , g_C$</td>
<td>Development of vascular networks.</td>
</tr>
<tr>
<td>Copepods to fish</td>
<td>$\approx 1 , mg_{ww}$</td>
<td>Smallest size of a functional camera eye</td>
</tr>
<tr>
<td>Fish to whales</td>
<td>$\approx 10 , kg_{ww}$</td>
<td>Lower size of maintaining a homeothermic metabolism</td>
</tr>
</tbody>
</table>
The maximum visual range in clear water can be estimated by considering the properties of a pin-hole camera eye as done in a largely unrecognized work by Dunbrack and Ware (1987). Here we provide a simplified derivation of their argument, which corrects a number of minor errors.

The projection of a visual image of a prey on the retina of a predator activates a number of visual elements $n$ proportional to the area of the projected image multiplied by the density of visual elements. Since we are interested in the maximum distance $R$ that an object can be discerned we can assume that the distance is large relative to the diameter of the eye such that the curvature of the eye can be ignored. The number of activated visual elements is:

$$ n \propto \rho l_{\text{eye}}^2 l_{\text{prey}}^2 R^{-2} $$

where $\rho$ is the density of visual elements and $l_{\text{eye}}$ is the diameter of the eye. The density of visual elements is a decreasing function of the size of the eye: $\rho \propto l_{\text{eye}}^{-d}$ with $d \approx 0.5$ (Dunbrack & Ware 1987). Assuming that the size of the eye and the preferred size of the prey scales with the length of the predator gives the number of visual elements as

$$ n \propto l^{4-d} R^{-2}. $$

The largest distance $R$ that a predator can discern a prey of size (length) $l_{\text{prey}}$ is when the apparent contrast (the difference between the visual imprint of the prey and the background) of the prey $C_a$ equals the contrast threshold that the predator can distinguish $C_c$. Apparent contrast of the prey declines away from the...
inherent contrast $C_0 = 0.3$ as:

$$C_a = C_0 e^{-\alpha R}.$$ 

Where $\alpha = 0.001$ cm$^{-1}$ is the attenuation of light by the water. The contrast threshold is a declining function of the number of visual elements $n$ involved in discerning the object:

$$C_t = C_{t,\text{min}} + 1/n$$

where $C_{t,\text{min}} = 0.15$ is the minimum contrast threshold for vision which depends on the ambient light. This semi-heuristic relationship is known as “Ricco’s law” (Northmore et al. 1978). The maximum distance where the prey can be perceived is when the apparent contrast reaches the contrast threshold, $C_a = C_t$:

$$C_0 e^{-\alpha R} = C_{t,\text{min}} + KR^2 l^{d-4}$$

where $K = 0.025$ cm$^{1.5}$ is a constant which characterizes the sensitivity of the eye. It is not possible to isolate $R$ from the expression above. However, two limiting cases can be derived: 1) the “clear-water” limit is when the visual range is limited by the resolution of the eye, i.e. where $e^{-\alpha R} \approx 1$ and $C_0 \gg C_{t,\text{min}}$:

$$R \approx \sqrt{C_0/K} l^{2-d/2}$$

In this case the maximum visual range increases with $l^{2-2/d} \approx l^{1.75}$ for $d = 0.5$. 2)
The “turbid-water” limit is when the visual range is limited by the sensitivity (the minimum contrast threshold) of a visual element, when $C_{t,\text{min}} > KR^2 l^{4-d}$:

$$R \approx \frac{\ln C_o - \ln C_{t,\text{min}}}{\alpha}$$

In this limit the size of the predator does not play a role and the minimum contrast threshold essentially limits the visual range. The visual range decreases if the light in the water is limited (lower minimum contrast threshold $C_{t,\text{min}}$) or the turbidity $\alpha$ is increased. The prediction of this limit has been subject of more elaborate models (Aksnes & Utne 1997).
Sidebar 2 Life-history optimization of offspring size

The optimal life history strategy in terms of offspring size and adult size is the strategy that maximizes lifetime reproductive output (Charnov 1993). In optimal life history theory lifetime reproductive output is determined by the mortality and the available energy as functions of size or age. Here we determine the offspring size which maximizes lifetime reproductive output using arguments from Christiansen & Fenchel (1979) and Andersen et al. (2008).

The available energy can be assumed from metabolic scaling arguments to be 

\[ H(w) = Aw^n \]

where the usual metabolic assumption is \( n = 3/4 \) (West et al. 1997). Consumption results in a mortality rate on their prey of 

\[ \mu(w) = \alpha w^{n-1} \]

where \( \alpha \) is a dimensionless constant relating consumption and mortality (Andersen & Beyer 2006). For simplicity we assume determinate growth where a juvenile uses all acquired energy for growth and a mature individual of size \( W \) uses all energy for reproduction; however the central results are valid for indeterminate growth as well (Andersen et al. 2008). The lifetime reproductive output (expected number of offspring during life) is:

\[ R_0 = \frac{\epsilon}{2} P_{w_0 \rightarrow W} \frac{H(W)}{W_0 \mu(W)} \]

where \( \epsilon \) is the reproductive efficiency, \( \frac{1}{2} \) assumes an even sex ratio, \( H(W) \) is the adult rate of reproduction (mass per time), \( 1/\mu(W) \) is the expected adult lifespan, \( 1/w_0 \) is to convert from units of mass to number of offspring, and the probability
to survive from offspring size $w_0$ to adult size $W$ is:

$$P_{w_0 \rightarrow W} = \exp \left[ - \int_{w_0}^{W} \frac{\mu(w)}{H(w)} dw \right]$$

Inserting the metabolic assumptions, $H(w) = A w^n$ and $\mu(w) = \alpha A w^{n-1}$ yields a lifetime reproductive output of:

$$R_0 = \frac{\varepsilon}{2\alpha} \left( \frac{W}{w_0} \right)^{1-\alpha}$$

Three conclusions can be drawn from this result:

1) If $R_0 < 1$ each female produces less than a single offspring throughout life yielding an unsustainable population. This happens when $\alpha > 1$ and it can be concluded that $\alpha < 1$.

2) Lifetime reproductive output only depends on the ratio between adult size and offspring size. The absolute values of the two sizes do not matter.

3) The larger the ratio between adult and offspring size, the higher the fitness. Organisms will therefore strive to maximize this ratio under the constraints of other external factors (Neuheimer et al.).

The results do not depend on the value of the metabolic exponent $n$ as long as $n < 1$. This argument ignored the maintenance metabolism and indeterminate growth to simplify the mathematical derivation, but both of these effects can be
accounted for (Andersen et al. 2008).
Figure 1. The five aspects of pelagic marine life examined here (body temperature, resource encounter strategy, motility regime, sensing mode and life-history strategy) are illustrated with horizontal bars with the characteristic transitions indicated by changes in gray-scale. The transitions are explained throughout the text. The drawings in the top row illustrate the seven realms of life: viruses, osmo-heterotrophic bacteria, unicellular phototrophs, unicellular mixo- and heterotrophs, planktonic multi-cellular heterotrophs, visually foraging poikilotherms (teleosts, cephalopods and sharks) and homeothermic animals (whales).
Figure 2. Clearance rate vs. weight for organisms performing active predation, photosynthesis and diffusive feeding on phosphorous. The solid lines are fits to data with exponent given in each panel. The dashed lines are fits with theoretical exponents 3, 2 and 1 for panel a, b and c respectively (Table S1.2). (a) Clearance rate $\beta_A$ for active predation by zooplankton (circles) and fish (squares) from Kiørboe (2011). (b) Clearance rate $\beta_L$ (affinity) for carbon uptake from a series of experiments with diatoms under identical conditions (Taguchi 1976). Data compilations covering a wider range of sizes and phytoplankton groups give a similar exponent but a larger scatter (Schwaderer et al. 2011). (c) Clearance rate $\beta_D$ (affinity) for diffusive feeding on dissolved phosphate from Tambi et al. (2009) and Edwards et al. (2012).
Figure 3. Encounter rates as a function of size for four different resource acquisition mechanisms and resource types: diffusive uptake of dissolved organic matter scaling as $l^1$ (dark red), uptake of carbon through photosynthesis scaling as $l^2$ (light green), diffusive uptake of dissolved inorganic nutrients (dark green), and active encounter of prey organisms scaling as $l^3$ (yellow). The combined uptake of carbon and nutrients by phototrophs is limited by Liebig’s law and shown with solid green lines; light green for light-limited conditions and dark green for nutrient-limited conditions. The concentration of dissolved organic matter is $C_{\text{DOM}} = 5 \mu g_c/l$; inorganic nutrients is $C_N = 4 \mu \text{molN/l}$ (corresponding to 50 $\mu g_c l^{-1}$), the light intensity at depth is $C_L = 2 \text{ W m}^{-2}$ and the concentration of suitable prey organisms is $C_P = 10 \mu g_c/l$. 
Figure 4. Trophic strategy as a function of size: osmo-heterotrophs (dark red), phototrophs (green), mixotrophs (army green) and heterotrophs (yellow). (a) Prescribed variation of nutrient and light conditions from oligotrophic to eutrophic conditions. (b) Strategy that yields the highest resource encounter rate as a function of size (x-direction) and resource condition (y-direction) changing between oligotrophic (high light, low nutrients) to eutrophic conditions (low light, high nutrients). (c) Trophic strategy of 3020 marine organisms as a function of length. Ciliates and flagellates have been categorized as phototrophs, mixotrophs or heterotrophs depending on the trophic strategy for the specific species (Appendix S2 in Supporting Information). The groupings are whales.
(Cetacea only, i.e. dolphins and whales), cartilaginous fish (Elasmobranchii; sharks and rays), teleosts (Osteichthyes), Cephalopoda (“ink fish”), meroplanktonic larvae (i.e. planktonic larvae whose adult stages are benthic), jellies (Cnidaria, Ctenophora), rotifers (Rotifera), crustaceans (incl. copepods), and unicellular eukaryotes or prokaryotes.
Figure 5. Swimming speeds and body aspect ratio vs. body length. Length is measured as ESD for planktomic organisms and as longest length for fish larvae, krill, fish and whales. (a) Swimming speed: data for zooplankton (including fish larvae) from Kiørboe (2011); fish data (cruising speed) from Sambilay Jr. (1990). The lines are power law fits (Table 1). The split between the two data sets was determined as the size that gave the lowest total residual of the fits. The crossover size at 6.6 cm corresponds to a Reynolds number around 1000. (b) Aspect ratio as a function of length for motile marine organisms. Data contain nanoflagellates and dinoflagellates (Throndsn et al. 2003, Tomas 1997), copepods (Kiørboe et al. 2010), krill (Watkins & Brierley 2002), fish larvae (Ara et al. 2013, Morioka et al. 2013, Moser et al. 1986, Oka & Higashiji 2012) and adult fish (Froese & Pauly 2013).
Figure 6. Senses vs. size. Left axis and lines: Estimated range for sensing a prey a factor 10 shorter than a predator. (see Sidebar 1 for details). Echolocation range determined from tank and field measurements of tooth whales of different size (circles; Table S3.2). The line is fitted with exponent 17/8 (table 1). The vertical lines are estimates of limits of chemotaxis strategies; see text for details. Right axis and bars: Senses used for detecting prey grouped according to size and organismal group (Table S3.1).
Figure 7. Weights of adults and progeny for metazoans grouped by species of similar taxonomy. Estimates of mean adult and progeny size were compiled from the literature, with “adult” defined as individuals that had reached maturity and “progeny” the smallest size at which offspring are independent of the parent (Appendix S4). Original data included measures of volume, length, wet weight, dry weight and carbon dry weight. All were converted to carbon dry weight using either species-specific or, if unavailable, group-specific conversion factors from the literature. The solid line is a 1:1 progeny:adult size ratio and the dashed line is a 1:100 progeny:adult size ratio. Life forms following this line (whales, cartilaginous fish and crustaceans) follow the “fixed-ratio” strategy, while life forms with constant progeny size (most notably teleost fish) follow the “small-eggs” strategy.