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Mechanistic modeling of cyclic voltammetry: a helpful tool for understanding biosensor principles and supporting design optimization

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Highlights
- The physicochemical parameters required for mathematical modeling were either found in literature or estimated on the basis of experimental data. Thus, the applicability of the developed model is not limited by the dataset or biosensor design.
- The developed cyclic voltammetry simulator was applied for interpreting the experimental results at various mediator concentrations, membrane thickness/compositions and operating conditions of the proposed multi-layer biosensor system.
- An accurate electrochemical, morphological and microscopic characterization of the biosensor system coupled with the model predictions allowed to identify the parameters crucial for the stable biosensor response.
- Based on the model predictions, a more favourable design of the biosensor system was developed, which subsequently reduced the reagent usage and waste generation.

Abstract
Design, optimization and integration of biosensors hold a great potential for the development of cost-effective screening and point-of-care technologies. However, significant progress in this field can still be obtained on condition that sufficiently accurate mathematical models will be developed. Herein, we present a novel approach for the improvement of mechanistic models which do not only combine the fundamental principles but readily incorporate the results of electrochemical and morphological studies. The first generation glucose biosensors were chosen as a case study for model development and to perform cyclic voltammetry (CV) measurements. As initial step in the model development we proposed the interpretation of experimental voltammograms obtained in the absence of substrate (glucose). The model equations describe dynamic diffusion and reaction of the involved species (oxygen, oxidized/reduced forms of the mediator – Prussian Blue/Prussian White). Furthermore, the developed model was applied under various operating conditions as a crucial tool for biosensor design optimization. The obtained qualitative and quantitative dependencies towards amperometric biosensors design...
optimization were independently supported by results of cyclic voltammetry and multi-analytical studies, such as scanning electron microscopy (SEM), energy dispersive X-ray spectroscopy (EDX) and liquid chromatography-electrospray ionization-tandem mass spectrometry (LC-ESI-MS/MS). Remarkably, a linear response of the optimized biosensors tested at the applied voltage (-0.14 V) in the presence of the glucose was obtained from $10^{-1}$ to $10^{2}$ M (relative standard deviation (RSD) < 7% per electrode). We believe that the presented model can be used to determine the exact mechanism driving the electrochemical reactions and to identify critical system parameters affecting the biosensor response that would significantly contribute to the knowledge on biosensing, device’s design and bioengineering strategies in the future.

Keywords
Mechanistic Modeling, Cyclic Voltammograms, Amperometric Biosensors, Glucose Biosensors, SEM/EDX, LC-ESI-MS/MS.

1. Introduction
The development of a crucial tool for an accurate and reliable diagnostics and continuous monitoring of glucose concentrations, mainly for diabetes patients, resulted in more than 50 years of research and the establishment of the amperometric glucose sensors in clinical diagnostics [1,2]. Being compact, relatively stable and cheap, biosensors nowadays found their application in medicine [3,4], pharmacology [5], microbiology [6], the food industry [7], defense technologies [8] and others. Moreover, glucose biosensors hold a great potential for glucose monitoring in fermentation processes [9,10] addressing the needs within biotechnological strain development. However, the reliability of the biosensor response in the continuous monitoring is still a limiting factor for their further integration in biotechnology.

Common detection techniques applied to biosensors, such as electrochemical impedance spectroscopy (EIS), chronocoulometry (AM) and cyclic voltammetry (CV), allow getting more detailed insights into the principles of sensing mechanisms [11]. In order to get a better understanding of the nature of the electrode reactions and to improve the biosensor performance, mathematical models were applied to electrochemical biosensors [12]. The first model for the amperometric response of an enzyme electrode for the glucose - glucose oxidase system was presented by Mell and Maloy [13] in the seventies, after Guilbault and Lubrano [14] constructed an amperometric glucose sensitive electrode. The first theoretical treatment of the cyclic voltammograms was presented by Nicholson and Shain [15]. In their work, the reversible and irreversible charge transfer mechanisms were coupled with homogenous first order chemical or electrochemical reactions. Moreover, the analytical solution was also presented for the electrochemical reaction followed by the mediated enzyme reaction. A commercially available simulation program for cyclic voltammetry, DigiSim (Bioanalytical Systems, West Lafayette, IN), developed by Feldberg and Rudolph [16] describes the electrochemical reactions coupled with first- and/or second-order chemical reactions. However, the mechanism of the enzymatic reactions is very complex and the assumption that the kinetics obey a first-order reaction can only be applied in very rare cases. Yokoyama and Kayanuma [17] developed a cyclic voltammetry simulator for electrochemically mediated enzyme reactions for various mediator and substrate concentrations, therefore not being limited by first- or pseudo-first-order reaction kinetics. The presented model allowed determining the kinetic constants for the homogeneous reaction between glucose oxidase (GOx) and glucose in the presence of ferrocene derivatives. Later on, the model principles were applied for modeling the reversible electrochemical reaction with one electron followed by the mediated reaction of immobilized enzyme with two electrons [18]. The simulation of cyclic voltammetry was also applied for studying the influence of ohmic drop [19,20], electrode area, electrochemical reaction constants and transferring coefficients [21], as well as the effect of flow rates [22-24] on the current response and wave shape. Analyzing the curve shape, peak shifts and amplitudes between the first cycle and successive scans in the obtained cyclic voltammograms is an important key in providing useful information on the mechanism of the electrochemical reaction as well as the adsorption mechanism and the diffusivities of the electrochemical species [25]. All these experimental data make CV a powerful analytical tool to identify the correlations between the sensor morphology and system parameters, underlying the desired biosensor response. However, only the works of Cannes et al. [26,27] demonstrated how the analytical techniques, such as CV measurements and scanning electrochemical microscopy (SECM), can be combined with simple numerical simulations for quantitative estimation of biosensor system parameters.

The general idea underlying this study is the development of a novel mathematical tool for amperometric biosensor operation and design optimization. To achieve this goal, we have used, as a first step, the combination of a mechanistic model for cyclic voltammograms with experimental multi - analytical studies. As a case study, the biosensor design with enhanced stability was adopted from the works of Ricci et al. [28,29]. The surface of the working electrode (WE) of commercially available screen-printed electrodes was chemically modified with a hydrogen peroxide sensitive catalyst, Prussian Blue [30], and covered with an enzyme/membrane layer (see Figure S1, Supplementary Materials). The experimental voltammograms were compared with simulation results, which allowed to use the formulated model not only for studying the processes occurring inside the biosensor system, but also to identify the critical system parameters. The results of the model predictions were fully supported by subsequent electrochemical (CV), bioanalytical (LC-ESI-MS/MS, EDX) and morphological (SEM) studies.
2. Mathematical Modeling

2.1. Computational Domain and Governing Equations

The main objective of the model was to predict cyclic voltammetry curves for the reversible electrochemical reaction coupled with oxidation/reduction of the catalyst in the absence of substrate (glucose) for an air saturated phosphate buffer solution, at different operating conditions. The biosensor was modeled spatially as a one-dimensional system. Non-linear second order partial differential equations combine the dynamic diffusion and reaction of the involved chemical species in the enzymatic/membrane layer, as well as electrochemical reaction on the surface of the electrode. Different regions of the multi-layer glucose biosensor system (electrode surface, enzyme/membrane layer and stagnant diffusion layer) were associated with diffusion fluxes, chemical and electrochemical reactions (see Figure S2, Supplementary Materials). It was assumed that the oxidized form (M$_{ox}$) of artificial peroxidase - Prussian Blue (PB), was deposited on the surface of the working electrode, whereas the reduced form (M$_{red}$) - Prussian White (PW), was produced during the reversible two - electron transfer reaction [31] (note that the PB/PW abbreviation is simplified to M$_{ox}$/M$_{red}$ since historically Prussian Blue was called a “mediator” in the literature):

\[
\text{M}^{\text{insoluble}}_{\text{(ox)}} + 2e^- \xrightarrow{k_{\text{(red)}}} \text{M}_{\text{(red)}}
\]

The complete reduction of molecular oxygen in the presence of Prussian White was described as a four - electron transfer reaction taking place inside of the enzyme/membrane layer [32]:

\[
\text{O}_2 + \text{M}_{\text{(red)}} \xrightarrow{k_1} \text{M}_{\text{(ox)}} + 4e^- + \text{H}_2\text{O}
\]

The kinetics of the electrochemical reactions were assumed to be fully reversible, whereas the oxygen reduction followed a second order kinetics. Considering one-dimensional diffusion, the governing equations for oxygen (1), (4), oxidized (2) and reduced (3) forms of the mediator were formulated as follows:

Enzyme/membrane layer, \( t > 0 \), and \( 0 < x < d_e \):

\[
\frac{\partial [\text{O}_2]}{\partial t} = D_{\text{O}_2} \frac{\partial^2 [\text{O}_2]}{\partial x^2} - r([\text{O}_2], [\text{M}_{\text{red}}]) \tag{1}
\]

\[
\frac{\partial [\text{M}_{\text{ox}}]}{\partial t} = D_{\text{M}_{\text{ox}}} \frac{\partial^2 [\text{M}_{\text{ox}}]}{\partial x^2} + r([\text{O}_2], [\text{M}_{\text{red}}]) \tag{2}
\]

\[
\frac{\partial [\text{M}_{\text{red}}]}{\partial t} = D_{\text{M}_{\text{red}}} \frac{\partial^2 [\text{M}_{\text{red}}]}{\partial x^2} - r([\text{O}_2], [\text{M}_{\text{red}}]) \tag{3}
\]

Diffusion layer, \( t > 0 \), and \( d_e < x < d_e + d_d \):

\[
\frac{\partial [\text{O}_2]}{\partial t} = D_{\text{O}_2} \frac{\partial^2 [\text{O}_2]}{\partial x^2} \tag{4}
\]

where \( D_{\text{O}_2} \) and \( D_{\text{M}_{\text{x}}} \) are diffusion coefficients for the oxygen inside the enzyme/membrane and diffusion layers, respectively. Inside the enzyme/membrane layer, \( D_{\text{M}_{\text{ox}}} \) and \( D_{\text{M}_{\text{red}}} \) refer to the diffusion coefficients of the reduced and oxidized form of the mediator, respectively. The thickness of the enzyme/membrane layer was set as \( d_e \), whereas for the diffusion layer it was \( d_d \). The mediator layer thickness was neglected in the model, assuming that PB crystals are adsorbed inside the cavities of the graphene oxide layer surface (see Figure S3, Supplementary Materials). The rate (\( r \)) of the homogeneous reaction (5) between the reduced form of the mediator and oxygen is provided in the equation below:

\[
r([\text{O}_2], [\text{M}_{\text{red}}]) = k_k \cdot [\text{O}_2] \cdot [\text{M}_{\text{red}}] \tag{5}
\]

where \( k_k \) is a kinetic constant for the complete PW oxidation in the presence of oxygen for air saturated solutions [32].

2.2. Initial and Boundary Conditions

The zero mediator concentration inside the enzyme/membrane layer (6), as well as the oxygen absence (7) inside the diffusion and enzyme/membrane layers, were set as the initial conditions of the model following the equations below:

\[
t = 0, \text{ and } 0 < x < d_e \quad [\text{M}_{\text{ox}}] = [\text{M}_{\text{red}}] = 0 \tag{6}
\]
\[ t = 0, \text{ and } 0 < x < d_e + d_d \quad [O_2] = 0 \] (7)

The boundary conditions for oxygen dissolved in the bulk solution (8), the continuity of oxygen diffusion fluxes at the interface between the enzyme/membrane and diffusion layer (9) and the zero oxygen flux at the electrode surface (10) were set in the model as follows:

\[ t > 0, \text{ and } x = d_e + d_d \quad [O_2] = [O_{2,\text{bulk}}] \] (8)

\[ t > 0, \text{ and } x = d_e \quad D_{O_{2\text{,d}}} \frac{\partial [O_2]}{\partial x} = D_{O_{2\text{,d}}} \frac{\partial [O_2]}{\partial x} \] (9)

\[ t > 0, \text{ and } x = 0 \quad D_{O_{2\text{,d}}} \frac{\partial [O_2]}{\partial x} = 0 \] (10)

The zero mediator concentration at the boundary of the enzyme/membrane layer (11) and the concentration ratio between oxidized and reduced forms of the mediator controlled by the Nernst equation at the electrode surface (12) were given by:

\[ t > 0, \text{ and } x = d_e \quad [M_{\text{ox}}] = [M_{\text{red}}] = 0 \] (11)

\[ t > 0, \text{ and } x = 0 \quad \frac{[M_{\text{ox}}]}{[M_{\text{red}}]} = \exp \left( \frac{n_e \cdot F}{R \cdot T} \cdot (E - E^\circ) \right) \] (12)

where \( n_e \) is a number of electrons involved in a charge transfer, \( F \) is the Faraday constant, \( R \) represents the universal gas constant, \( T \) is temperature, \( E \) is the applied potential vs. the reference electrode and \( E^\circ \) is the standard potential. The biosensor response (13), measured as the current as a function of time, \( i(t) \), was governed by:

\[ i(t) = n_e \cdot A \cdot F \cdot D_{M_{\text{red}}} \cdot \frac{\partial [M_{\text{red}}]}{\partial x} \] (13)

where \( A \) is the surface area of the working electrode.

2.3. Model Implementation

The governing model equations were discretized by the finite difference method (FDM) and numerically solved using an explicit Euler scheme. The proposed model for cyclic voltammetry responses was implemented in both MATLAB® and FORTRAN languages. Following the IUPAC recommendation, the arising positive current in the voltammogram corresponds to the oxidation process (anodic current), whereas the negative current represents the reduction process (cathodic current).

The major part of the physicochemical parameters required for the mathematical model was found in the literature (Table 1). The mediator concentration and standard redox potential values had to be adjusted based on the difference between the fabrication procedures of biosensor systems (values are also presented in Table 1). The thickness of the enzyme/membrane layer was estimated from SEM analysis presented in section 4.3. The thickness of the diffusion layer was set as 1 µm in all simulations.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
<th>Model value</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>( D_{O_{2\text{,d}}} ) [m²/s]</td>
<td>Diffusivity of oxygen in polymeric membrane</td>
<td>( 5.0 \times 10^{-12} )</td>
<td>[33]</td>
</tr>
<tr>
<td>( D_{M_{\text{ox}}} ) [m²/s]</td>
<td>Diffusivity of oxidized form of mediator in polymeric membrane</td>
<td>( 1.0 \times 10^{-14} )</td>
<td>[34,35]</td>
</tr>
<tr>
<td>( D_{M_{\text{red}}} ) [m²/s]</td>
<td>Diffusivity of reduced form of mediator in polymeric membrane</td>
<td>( 7.0 \times 10^{-13} )</td>
<td></td>
</tr>
<tr>
<td>( D_{O_{2\text{,d}}} ) [m²/s]</td>
<td>Diffusivity of oxygen in diffusion layer</td>
<td>( 2.0 \times 10^{-09} )</td>
<td>[33]</td>
</tr>
<tr>
<td>( k_1 ) [M⁻¹s⁻¹]</td>
<td>Kinetic constant for the oxygen reduction by PB</td>
<td>0.107</td>
<td>[32]</td>
</tr>
<tr>
<td>( n_e )</td>
<td>Electrons involved in the PB redox reaction</td>
<td>2</td>
<td>[36,37]</td>
</tr>
<tr>
<td>( O_2 ) [mol/m³]</td>
<td>Oxygen concentration dissolved in</td>
<td>0.271563</td>
<td>[38]</td>
</tr>
<tr>
<td>$M_{sw}$ [mol/m$^3$]</td>
<td>Water</td>
<td>5/20/100</td>
<td>experiment</td>
</tr>
<tr>
<td>---------------------</td>
<td>-------</td>
<td>----------</td>
<td>------------</td>
</tr>
<tr>
<td>$E^\circ$ [V]</td>
<td>Standard Potential</td>
<td>PW/PB redox couple</td>
<td>0.13/-0.05</td>
</tr>
<tr>
<td>$d_e$ [m]</td>
<td>Thickness of the enzyme/membrane layer</td>
<td>7.0 x 10$^{-6}$</td>
<td>SEM experiment</td>
</tr>
<tr>
<td>$d_d$ [m]</td>
<td>Thickness of the diffusion layer</td>
<td>1.0 x 10$^{-6}$</td>
<td>estimation</td>
</tr>
<tr>
<td>$A$ [m$^2$]</td>
<td>Surface area of the working electrode</td>
<td>1.257 x 10$^{-5}$</td>
<td>experiment</td>
</tr>
<tr>
<td>$T$ [K]</td>
<td>Temperature</td>
<td>298.15</td>
<td>experiment</td>
</tr>
</tbody>
</table>

3. Experimental Section

3.1. Materials and reagents

Screen printed electrodes (SPEs) DRP-PW-110DGPHOX were customized by DropSens (Llanera, Spain). The electrodes were printed on polyester substrate and each sensor consists of a carbon working electrode modified with graphene oxide, a carbon counter electrode and a silver reference electrode. The diameter of the working electrode was 0.4 cm, resulting in an apparent geometric area of 0.126 cm$^2$.

Glucose oxidase (GOx) (EC 1.1.3.4, type VII, 248 U/g solid) and bovine serum albumin (BSA) were obtained from Sigma (St. Louis, MO, USA). Glutaraldehyde solution (25% (v/v), ethanol (UV HPLC gradient, 99.9%) and potassium hexacyanoferrate (III) (ACS reagent, ≥99.0%) were purchased from Sigma – Aldrich (St. Louis, MO, USA). Iron (III) chloride (anhydrous, 99.99%) and Nafion®117 solution (∼5% (v/v) in a mixture of lower aliphatic alcohols and water) were provided by Aldrich (Steinheim, Germany). D-Glucose (anhydrous) was provided by Fluka (Loughborough, UK). Mono – and di-potassium hydrogen phosphates (anhydrous) were obtained from Merck (Darmstadt, Germany). Sodium hydroxide (50% (w/w)) and hydrochloric acid (37% (w/v)) solutions were purchased from VWR International A/S (Søborg, Denmark). All the solutions were prepared with 0.1 M phosphate buffer supplemented with 0.1 M KCl (pH = 6), unless stated otherwise.

3.2. Glucose biosensor preparation

Preparation method 1:
The chemical deposition procedure of PB was adopted from works of Ricci et al. [29]. A 10 µL drop (total volume) of freshly made precursor solution, containing 0.1 M potassium ferrocyanide (K$_3$Fe(CN)$_6$) in 10 mM HCl mixed with 0.1 M ferric chloride (FeCl$_3$) solution in 10 mM HCl (1:1 proportion (v/v)), was directly placed over the working electrode (WE) surface of the SPEs. The sensors were left to dry for 15 (sensor 1) or 40 (sensor 2) minutes at room temperature and then washed with a 10 mM HCl solution and deionized water. In order to stabilize the PB layer, the sensors were placed in the oven at 100°C for 2 h. Prior to glucose oxidase (GOx) immobilization, a 2.5 µL droplet of freshly prepared glutaraldehyde solution (1% (v/v) diluted in water) was placed over the WE of the PB modified SPEs and was left to dry at room temperature for 30 min. After the glutaraldehyde solution layer was dried, the enzyme/membrane layer was deposited. The fresh enzyme/membrane solution was made by mixing GOx solution (53.7 U in phosphate buffer), BSA (5 vol. % diluted in water) and Nafion®117 (0.2 vol. % diluted in water) in a 1:1:1 proportion (v/v/v). A drop of 3 µL of the final solution was placed over the working electrode of the PB/glutaraldehyde modified SPEs.

Preparation method 2:
In order to remove the impurities, the surfaces of all electrodes were pre-treated in a phosphate buffer solution under chronoamperometric conditions with applied potential of +1.7 V. The chronoamperometric measurement was performed using MultiEmStat (PalmSens, Utrecht, The Netherlands) with a DRP-CAST1X8 interface (DropSens, Llanera, Spain) controlled by MultiTrace 3.4 software (PalmSens, Utrecht, The Netherlands). After the stable current was obtained, the surface of the working electrode was modified with a Prussian Blue (PB) layer. The PB chemical deposition procedure presented in preparation method 1 was modified. Thus, a 5 µL drop of 0.1 M solution of potassium ferrocyanide K$_3$Fe(CN)$_6$ in 10 mM HCl was placed over the working electrode and mixed with a 5 µL drop of 0.1 M solution of ferric chloride, FeCl$_3$ in 10 mM HCl directly on the surface of the electrode. The sensors were left to dry for 40 min at room temperature and then washed with a 10 mM HCl solution, deionized water and dried with air. In order to stabilize the PB layer, the sensors were placed in the oven at 100°C for 1 h. Similar to preparation method 1, the surface of WE for PB modified SPEs was pretreated with glutaraldehyde solution prior to enzyme/membrane layer deposition. In contrast to preparation method 1, Nafion®117 (2 vol. %) neutralized in ethanol [39] was mixed with GOx solution (53.7 U in phosphate buffer) and BSA (5 vol. % diluted in water) in a 1:1:1 proportion (v/v/v). A drop of 3 µL of final solution was placed over the working electrode of the PB/glutaraldehyde modified SPEs, yielding sensor 3 batch.

Regardless of the preparation method, sensors with deposited enzyme/membrane layer were placed to dry overnight in a climate chamber at 40% of humidity and 8°C. Moreover, both PB modified SPEs and complete glucose biosensors were stored in the dark, at room temperature and 4°C, respectively.

3.3. Glucose Oxidase activity measurement
The GOx activity measurement prior to the immobilization step of the stock solutions, as well as the enzyme/membrane mixtures, was performed by using an OXSOLV solvent-resistant, fiber-optic oxygen sensor (Pyro Science GmbH, Aachen, Germany) connected to a FireStingO2 fiber-optic meter (Pyro Science GmbH, Aachen, Germany) and controlled by Pyro Oxygen Logger software (Pyro Science GmbH, Aachen, Germany). The measurement was based on on-line monitoring of the dissolved oxygen (DO) consumption in the reaction of GOx with 100 mM glucose solution at room temperature (see Figure S5, Supplementary Materials). The setup—assembly, as well as the experimental procedure, were adopted from the works of Bolivar et al. [40,41]. A glass beaker with a liquid working volume of 10 mL and a magnetic stirrer (10 × 5 mm) were used for the experiments. The magnetic stirring was performed at 600 rpm (IKA® RET Basic, Staufen im Breisgau, Germany). The 100 µL of glucose solution was dissolved in 7 mL of buffer solution. The oxidation reaction was initialized by addition of different volumes of the GOx stock solution or the enzyme/membrane mixtures after the value of DO was stabilized. For the enzyme activity calculations, one unit (U) of enzyme corresponds to a substrate consumption of 1 µmol per min. The GOx activity in the enzyme/membrane mixture prior to immobilization was estimated as 0.179 U/µL.

3.4. Cyclic voltammetry behavior of glucose biosensors in phosphate buffer

Cyclic voltammetry (CV) measurements were performed using MultiEmStat (PalmSens, Utrecht, The Netherlands) with a DRP-CASTIX8 interface (DropSens, Llanera, Spain) controlled by MultiTrace 3.4 software (PalmSens, Utrecht, The Netherlands). A 100 µL droplet of phosphate buffer was placed over all three electrodes of SPE. The voltammograms were recorded at different scan rates in a potential range from -0.5 V to +0.5 V. After each run sample droplets were collected for subsequent LC-ESI-MS/MS analysis.

3.5. Biosensor sensitivity determination

In order to estimate the sensitivity of the developed biosensors, chronoamperometric studies were carried out in the presence of glucose solutions (concentration range: 10⁻¹⁻10⁻³ M) at the applied voltage equal to the peak potential of the reduction curve (-0.14 V). Moreover, the biosensors were characterized in the presence of the analytical range of glucose concentrations (0.1 to 2 mM). All measurements from the same biosensor were repeated at least in triplicates.

3.6. Scanning electron microscopy (SEM) and energy dispersive X-ray spectroscopy (EDX)

Micrographs of the bare and PB/GOx (Nafion) modified SPEs were obtained by scanning electron microscopy (SEM) using a FEI (Hilsboro, OR, USA) Quanta 400 FEG, operating at 10 kV accelerating voltage. Secondary (SE) and backscattered (BSE) electron images were collected in low vacuum mode (pH₂O = 100 Pa). The microscope was equipped with an EDAX (Mahwah, NJ, USA) Genesis V6.04 energy dispersive X-ray (EDX) system in order to obtain information on elemental composition of the biosensor surfaces. The measuring time per sample was equal to 100 sec. In addition, the correlative SEM/EDX analysis allowed determining the composition of the multi-layer biosensor.

3.7. Liquid chromatography-electrospray ionization-tandem mass spectrometry (LC-ESI-MS/MS)

In order to verify the chemical stability of the biosensor layers deposited over the surface of the working electrode, liquid chromatography electrospray ionization tandem mass spectrometry (LC-ESI-MS/MS) was utilized. The HPLC analysis was performed on an Agilent Infinity 1260 series instrument (Agilent Technologies, CA, USA) coupled with a quadrupole time-of-flight mass spectrometer Q-TOF LC/MS 6545 (Agilent Technologies, CA, USA) equipped with Jet Stream Thermal Focusing Technology ESI source. The data acquisition was controlled by MassHunter Software Tools. For LC-ESI-MS/MS experiments, a 30 µL water droplet spotted for 30 min on the glucose biosensors, previously not used in electrochemical studies, was taken. The obtained results were compared with data obtained in the LC-ESI-MS/MS study of buffer samples collected after each scan in CV. Chromatographic separation was achieved on the ZORBAX Eclipse Plus C 18 column (2.1 × 50 mm, particle size 1.8 µm) (Agilent, CA, USA). The mobile phase consisting of 0.3% formic acid in water (Solvent A) and acetonitrile (Solvent B) was used in the following gradient elution step: 90% Solvent A, was held for 2 min, then decreased to 10% in 9 min andheld for 2 min, and returned back to the starting conditions in 0.5 min for 8 min equilibration. The column operation temperature was fixed at 30°C, the mobile phase flow rate was 0.3 mL/min and the injection volume was 10 µL. MS scans were performed in a negative ion mode, operating under capillary voltage at 4500 V; the fragmentor voltage was set at 70 eV; dry gas temperature at 350°C; gas flow at 9 L/min; nebulizing gas pressure at 45 psi. The mass spectra for all samples were recorded at m/z 100-1500. The MS/MS experiments were conducted in product ion scan mode at collision energies ranging from 10 to 50 eV. The elemental compositions were identified based on the accurate mass measurements and data processing of total ion chromatograms (TICs) of the parent ions and fragments obtained in the MS/MS experiments.

4. Results and Discussion

4.1. Mathematical Model Validation

The initial design of the glucose biosensor system was based on the preparation method 1. In Figure 1 a good qualitative response of the numerical solutions is presented together with the experimental voltammograms obtained at 50 mV/sec for the two types of glucose biosensors with different PB modification time.
Comparison of the model output (dashed line) vs. experimental data (solid line) for two types of glucose biosensor fabricated according to preparation method 1: sensor 1 represents the results of 15 min PB deposition time, whereas sensor 2 refers to the 40 min procedure. The presented voltammograms were recorded/simulated for 50 mV/sec scanning speed.

In both simulations, the initial value for the deposited PB had to be adjusted for the two different types of biosensor: for sensor 1 the concentration of the deposited oxidized form of mediator ($M_{ox}$) was estimated as 5 mM, whereas for sensor 2 this parameter value was equal to 20 mM. From Figure 1 it is clear that no significant quantitative response can be obtained for the reduction curve, especially in case of higher mediator loadings. In order to validate the developed model, an additional set of experiments for the glucose biosensors was proposed. The sensor 2 type was tested at a potential range from -0.5 V to +0.5 V with higher scan rates: from 100 to 500 mV/sec. The obtained voltammograms were compared with the model output shown in Figure 2.

The results presented in Figure 2 clearly demonstrated a strong disagreement between the model predictions and experimental data at high cycling speeds: no relevant peak potential shifts and peak current increase were obtained with the model. Therefore, it was concluded that the assumed mechanisms of chemical and physical processes taking place inside the biosensor system proposed in the model were not sufficient. However, the variation of model parameters, namely $d_e$ and $M_{ox}$, and further comparison of the simulation results with the experimental voltammograms allowed assuming that the irreversible changes occur inside the biosensor system. Thus, the disagreement between the model predictions and the experimental data was mainly attributed to the constant decrease in the thickness of the enzyme/membrane layer, as well as in the concentration of deposited mediator after each scan. Moreover, a reversible electron transfer behaviour estimated at the lower scans was not present in the experimental voltammograms obtained at cycling speeds higher than 50 mV/sec. Varying the values of only two parameters ($d_e$, $M_{ox}$) within the model allowed to...
understand better the additional processes taking place inside the biosensor, and to focus on the optimization of the PB deposition and membrane composition methods. In a subsequent part of the study the model was used to identify the crucial biosensor system parameters that were further optimized in a new preparation method for the glucose biosensors.

4.2. Biosensor Design Optimization

In order to achieve a reproducible response and improved stability of the biosensor system layers the preparation method 2 was proposed. In this procedure, two crucial aspects had to be fulfilled: first, to achieve a higher and stable loading of PB, and second, to guarantee the stability of the enzyme/membrane layer under different operating conditions. Therefore, the deposition procedure of the PB layer had to be modified together with the composition of the Nafion membrane. In order to avoid changes in the biosensor topology, such as mechanical decomposition of the PB and the membrane layer and its subsequent leakage, that affected the switch from reversible to irreversible electron transfer behavior of the biosensor system, the optimized biosensors from preparation method 2 (sensor 3 type) were cycled at scan rates lower than 50 mV/sec. The potential range of the PB/PW redox couple from -0.5 V to +0.5 V was applied, as shown in Figure 3. Similar model parameters were used as for the simulations done for the preparation method 1. The value for the concentration of the deposited PB and the standard redox potential were now fixed to 100 mM and -0.05 V, respectively.

![Figure 3 – Comparison of the experimental voltammograms obtained at the various scan rates for the optimized glucose biosensor design (preparation method 2) and the model output (A). The recorded difference of peak current values (ΔI, µA) vs. scan rates is summarized in graph B, comparing experimental and simulation results.](image)

The optimized method was analyzed for the sensor 3 type and the expected increase in the current response following the increase in the scan rates was obtained in all experiments for both oxidation and reduction processes (Figure 3B). Moreover, the simulated voltammograms presented in Figure 3A showed a fair agreement with the experimental curves, especially with respect to the peak current values. To study the influence of the scan rate and the amount of Nafion®117 present in the enzyme/membrane mixture on the stability of the biosensor layers and the response, PB modified SPEs from preparation method 2 were used to design sensor 4 type, where the preparation method 1 for the enzyme/membrane mixture was adopted. Thus, the principal difference between the sensor 3 and sensor 4 series was the composition and concentration of the Nafion membrane: 2.0% and 0.2% Nafion, respectively. The constructed glucose biosensors were tested for different scan rates and the results of electrochemical studies were further compared with the data obtained by liquid chromatography-electrospray ionization-tandem mass spectrometry (LC-ESI-MS/MS) and scanning electron microscopy (SEM) coupled with energy dispersive X-ray (EDX) analysis. The obtained results are presented in the following section 4.3.

4.3. The effect of the scan rate and membrane composition on the biosensor layers stability and response

Concerning the changes in the topology of the biosensor system from one scan to another in CV, it was interesting to investigate the content of the buffer probes collected after each measurement by means of liquid chromatography tandem mass spectrometry (LC-MS/MS). Therefore, the glucose biosensors from the sensor 3 and sensor 4 series were scanned at the potential range from -0.5 V to +0.5 V at 10, 20 and 50 mV/sec sweep speeds (see Figure 5S, A, Supplementary Materials). Since no significant difference was obtained between the voltammograms for sensor 3 and sensor 4 designs, the probes were collected for 10 and 20 mV/sec scan rate experiments. To verify the correlation between the scan rate value or number of scans and the enzyme/membrane film stability, a fresh sensor was used for each scan rate. Moreover, to prove the influence of the electrochemical measurements on the biosensor layer stability one of

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**Figure 3 – Comparison of the experimental voltammograms obtained at the various scan rates for the optimized glucose biosensor design (preparation method 2) and the model output (A). The recorded difference of peak current values (ΔI, µA) vs. scan rates is summarized in graph B, comparing experimental and simulation results.**
the non-used glucose biosensors (sensor 3 and sensor 4 series) was tested in a steady state experiment with a water droplet. All the collected probes were investigated by subsequent LC-ESI-MS/MS analysis (Figure 4).
the same type of membrane reaches a constant trend already at the third scan. The tendency of Nafion membrane stabilization at a higher sweeping speed was demonstrated for both probes collected after the first scans in Figure 4G and could also be traced in the voltammograms recorded at scan rates equal to 10 and 20 mV/sec (see Figure 5S, B,C, Supplementary Materials). Comparing the elution profiles of Nafion-corresponded products, for probes collected after a steady state experiment and different scans in Figure 4G and Figure 4H, it is clear that the CV measurements allow faster stabilization of the membrane layer regardless of its composition. Moreover, the concentration profiles of Nafion-corresponded products for the sensor 4 (0.2% Nafion) series tested at 20 mV/sec (see Figure 5S, Supplementary Materials) showed a higher signal in comparison to the sensor 3 series (2.0% Nafion) at the first scans which corresponds to a lower stability of the 0.2% Nafion membrane. The stability of the 2.0% Nafion membrane was also confirmed in the subsequent SEM/EDX studies of the sensor 3 and sensor 4 samples (Figure 5), obtained after CV characterization.

Figure 5 – SEM images (A-E) and EDX spectra (F) of glucose biosensor layers. The enzyme/membrane layer of the sensor 4 series, without graphene oxide is presented in A. Top view of the enzyme/membrane layer is enlarged in B. For the sensor 3 series graphene oxide, PB and enzyme/membrane layers are shown in C. The PB layer of the sensor 3 series is enlarged in D, as well as a part of the enzyme/membrane layer (top right). The working electrode prior to modification steps is shown in E.
A non-uniform enzyme/membrane layered structure was observed in Figure 5A with a dense Nafion coating on top of the surface (Figure 5B). A more detailed view on the biosensor structure for the 2.0% Nafion membrane is presented in Figure 5C, where the graphene oxide layer with deposited Prussian Blue (Figure 5D) is covered by the enzyme/membrane film. Figure 5C clearly indicates that 2.0% Nafion coating allows the formation of a uniform layer with final thickness equal to 5-7 µm thickness (estimated by SEM). The graphene oxide layer (top) over the plastic substrate (bottom) for commercial SPEs was demonstrated in Figure 5E. Moreover, EDX spectra taken from the enzyme/membrane film, clearly indicated the presence of Nafion, based on the fluorine and sulphur spectral lines (Figure 5F). Therefore, EDX analysis demonstrated that the Nafion layer remains fixed on the biosensor surface after performing cyclic voltammetry measurements.

4.4. Chronoamperometric characterization of optimized biosensors

The analytical merit of the optimized biosensors (sensor 3 series) was evaluated via chronoamperometric studies in the presence of glucose. The linear response (Figure 6A) of the constructed biosensors was obtained in the range of glucose concentrations from $10^{-3}$ to $10^{-5}$ M (RSD < 7% per electrode). The biosensors were also calibrated in the analytical range of glucose concentrations between 0.1 and 2 mM (Figure 6B). The mean value of the slope estimated for the linear response (0 to 2 mM) was - 1.25 µA/mM with a standard deviation equal to 0.035 µA/mM. The obtained results are in a good agreement with literature data reported for fermentation monitoring [44,45].

![Figure 6](image)

Figure 6 – Calibration curve (A) obtained for the optimized sensor 3 biosensors in the presence of glucose. The current response is plotted towards the glucose concentration range equal to $10^{-5}$-$10^{-3}$ M. The zero glucose concentration corresponds to the phosphate buffer solution. The relative standard deviation per electrode is not shown, due to the low value (RSD = 7%). The chronoamperometric response (current vs time) of the analytical range of glucose concentrations is presented in B.

5. Conclusions and Future Work

The mathematical model of cyclic voltammetry response was developed for the glucose biosensors operating in aerobic conditions in the absence of glucose at low scan rates. The model was validated with the biosensors with various amounts of immobilized mediator and different enzyme/membrane film compositions. The biosensor system parameters required for numerical simulations were either found in literature or estimated from experimental data, therefore not limiting the applicability of the proposed model to a single biosensor design. In this work, we have demonstrated that combining the results of multi-analytical studies together with mechanistic modeling is an effective approach in identifying the key parameters of the biosensor system crucial for the optimal biosensors operation and design. Therefore, a more favorable composition of the enzyme/membrane layer (2.0% Nafion) was proposed and further proved to be stable at various operation conditions during cyclic voltammetry measurements.

In summary, the practical merit of the presented work is in the development of a time and cost effective tool crucial for amperometric biosensor design optimization. The demonstrated approach could potentially allow reducing the reagent usage and waste generation. As a future work, the optimized design of the glucose biosensor system will undergo further bioanalytical, morphological and amperometric studies, and the constructed model will be extended to describe the mediated enzymatic reaction of glucose oxidase in the presence of glucose. Thus, the proposed model will summarize all available process knowledge together with the results of bioanalytical and morphological analysis. Combining such model with global sensitivity and uncertainty analysis tools, will allow mapping the influence of the complete set of system input parameters on the biosensor response, which subsequently opens up the possibilities for optimization of the biosensor performance and ultimately the design of novel improved biosensors.
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