



Teaching First-Order Logic with the Natural Deduction Assistant (NaDeA)

From, Asta Halkjær; Hatteland, Helge; Villadsen, Jørgen

Publication date:
2018

Document Version
Publisher's PDF, also known as Version of record

[Link back to DTU Orbit](#)

Citation (APA):
From, A. H., Hatteland, H., & Villadsen, J. (2018). *Teaching First-Order Logic with the Natural Deduction Assistant (NaDeA)*. Paper presented at 10th Scandinavian Logic Symposium, Gothenburg, Sweden.

General rights

Copyright and moral rights for the publications made accessible in the public portal are retained by the authors and/or other copyright owners and it is a condition of accessing publications that users recognise and abide by the legal requirements associated with these rights.

- Users may download and print one copy of any publication from the public portal for the purpose of private study or research.
- You may not further distribute the material or use it for any profit-making activity or commercial gain
- You may freely distribute the URL identifying the publication in the public portal

If you believe that this document breaches copyright please contact us providing details, and we will remove access to the work immediately and investigate your claim.

- ▶ ANDREAS HALKJÆR FROM, HELGE HATTELAND, AND JØRGEN VILLADSEN, *Teaching first-order logic with the natural deduction assistant (NaDeA)*. DTU Compute, AlgoLoG, Technical University of Denmark, 2800 Kongens Lyngby, Denmark.

E-mail: s144442@student.dtu.dk s144457@student.dtu.dk jovi@dtu.dk.

The natural deduction proof system is a popular way of teaching logic. It is also important in the philosophy of logic and the foundations of mathematics, in particular for systems of intuitionistic logic and constructive type theory, and it is used in many proof assistants along with automatic proof methods like the tableaux procedure and the resolution calculus.

The natural deduction assistant (NaDeA) has been used for teaching first-order logic to hundreds of computer science bachelor students since 2015 [1, 2]. NaDeA runs in a standard browser and is open source software. Upon completion of a natural deduction proof the student obtains a formal proof in the interactive proof assistant Isabelle/HOL [3] of not only the correctness of the student's natural deduction proof but also of the validity of the formula with respect to the classical semantics of formulas in first-order logic.

Our formalization of the syntax, semantics and the inductive definition of the natural deduction proof system extends work by Stefan Berghofer [4] and Melvin Fitting [5] but with a much more detailed soundness proof that can be examined and tested by the students. The corresponding completeness proof is also available but it is of course quite demanding. We describe the main advantages and disadvantages of using an advanced e-learning tools like NaDeA for teaching logic. Furthermore we briefly survey related and future work.

NaDeA can be used with or without installing Isabelle and is available online.

URL Address: <https://nadea.compute.dtu.dk/>.

[1] JØRGEN VILLADSEN, ALEXANDER BIRCH JENSEN AND ANDERS SCHLICHTKRULL, *NaDeA: A Natural Deduction Assistant with a Formalization in Isabelle*, **IFCoLog Journal of Logics and their Applications**, vol. 4 (2017), no. 1, pp. 55–82.

[2] JØRGEN VILLADSEN, ANDREAS HALKJÆR FROM AND ANDERS SCHLICHTKRULL, *Natural Deduction and the Isabelle Proof Assistant*, Proceedings 6th International Workshop on **Theorem proving components for Educational software** (Gothenburg, Sweden), (Pedro Quaresma and Walther Neuper, editors), vol. 267, Electronic Proceedings in Theoretical Computer Science, Open Publishing Association, 2018, pp. 140–155.

URL Address: <http://eptcs.org/paper.cgi?ThEdu17.9>.

[3] TOBIAS NIPKOW, LAWRENCE C. PAULSON AND MARKUS WENZEL, *Isabelle/HOL — A Proof Assistant for Higher-Order Logic*, vol. 2283, Lecture Notes in Computer Science, Springer, 2002.

[4] STEFAN BERGHOFER, *First-Order Logic According to Fitting*, **Archive of Formal Proofs**, August 2007.

URL Address: <http://isa-afp.org/entries/FOL-Fitting.html>.

[5] MELVIN FITTING, *First-Order Logic and Automated Theorem Proving, Second Edition*, Graduate Texts in Computer Science, Springer, 1996.