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An efficient approach to separate CO$_2$ using supersonic flows for carbon capture and storage

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Abstract: The mitigation of CO$_2$ emissions is an effective measure to solve the climate change issue. In the present study, we propose an alternative approach for CO$_2$ capture by employing supersonic flows. For this purpose, we first develop a computational fluid dynamics (CFD) model to predict the CO$_2$ condensing flow in a supersonic nozzle. Adding two transport equations to describe the liquid fraction and droplet number, the detailed numerical model can describe the heat and mass transfer characteristics during the CO$_2$ phase change process under the supersonic expansion conditions. A comparative study is performed to evaluate the effect of CO$_2$ condensation using the condensation model and dry gas assumption. The results show that the developed CFD model predicts accurately the distribution of the static temperature contrary to the dry
gas assumption. Furthermore, the condensing flow model predicts a CO\(_2\) liquid fraction up to 18.6% of the total mass, which leads to the release of the latent heat to the vapour phase. The investigation performed in this study suggests that the CO\(_2\) condensation in supersonic flows provides an efficient and eco-friendly way to mitigate the CO\(_2\) emissions to the environment.

**Keywords:** CO\(_2\) separation, carbon capture and storage, supersonic flow, CO\(_2\) emission

1 Introduction

Carbon capture and storage (CCS) has been proposed as a potential way to mitigate greenhouse gas emissions, such as carbon dioxide (CO\(_2\)) [1]. This can lead to a cleaner utilization of fossil energy [2], which has been recognised as one of the most promising measures to improve the sustainable development of the coal, oil and gas industries with regards to the CO\(_2\) emission [3]. One of the promising applications is to use the captured CO\(_2\) for the enhanced oil recovery and carbon storage in shale oil reservoirs [4]. Kim et al. [5] evaluated CO\(_2\) injection in shale gas reservoirs considering the influences of the multi-component transport and geomechanical effects. Singh [6] evaluated the influence of CO\(_2\) injection schemes on the reservoir pressure and saturation, and the results showed that the cyclic injection scheme is a better choice to store CO\(_2\) in storage reservoirs. Zhang et al. [7] assessed the potential of CO\(_2\) injection for the geological storage in geothermal reservoirs of China, and they presented three types of geothermal reservoirs suitable for CO\(_2\) injection.

Currently, CO\(_2\) can be removed using the following conventional techniques: absorption [8], adsorption [9], cryogenics [10] and membrane [11], which may have
some drawbacks, such as the relatively large facilities, a considerable investment, complex mechanical work, and the possibility of having a negative impact on the environment [12]. In addition, nanofluids have been used to enhance the CO₂ absorption for decades, including SiO₂ [13], Fe₃O₄ [14], Al₂O₃ [15] nanoparticles. The enhancement mechanisms of nanofluids can be explained by the grazing effect and the hydrodynamic effect in the gas-liquid boundary layer and inhibition of bubble coalescence. The detailed information about this novel approach can be found in a state-of-the-art review by Zhang et al. [16].

The supersonic separation, a revolutionary technique, has been introduced to remove water vapour from natural gas, which overcomes some of the disadvantages of conventional separation technologies [17]. The supersonic separation technology also provides a potential for CO₂ removal from natural gas contributing to CCS [18]. The condensable gas components are condensed to the liquid phase due to the extremely non-equilibrium state in supersonic flows [19]. The condensed liquids are then removed from the gas-liquid mixture on account of the high centrifugal force generated by swirling devices inserted into the flow channel [20]. As a static device, the supersonic separator has no rotating parts, enabling high reliability and availability. Furthermore, during these processes, the supersonic separation technology presents an environmental-friendly approach since it does not need any chemicals for CO₂ separation and also does not produce any pollution to the environments [21]. Therefore, the CO₂ supersonic separation is proposed as an alternative way to mitigate the CO₂ emissions to the environments from fossil power generation.
Most of the numerical studies on the supersonic separation in recent years are focused on the single-phase flow or particle flows without considering the condensation phenomenon. Secchi et al. [22] employed a 1D model and NIST REFPROP thermodynamics properties for the preliminary design of a supersonic separator involving the flow acceleration in a Laval nozzle and the swirling effects. Bian et al. [23] performed the structure optimization of the supersonic separator by using the assumption of the single-phase flow. Based on the assumption of the single-phase flow, Wang et al. optimized the geometrical parameters of the supersonic separator, such as the blade angle [24], discharge chamber [25] and reflow channel [26]. Niknam et al. [27] performed the numerical simulation on the flow behaviour inside a supersonic separator, including the detailed distribution of the static pressure, temperature and Mach number. Liu and Liu [28] numerically investigated the detailed distribution of the flow field inside the supersonic separator and analysed the effect of the static pressure in the shock wave position with the assumptions of single-phase flow and ideal gas model. Jiang et al. [29] employed the discrete particle method to predict the particle trajectories inside a supersonic separator based on the assumed particle size instead of the real condensed droplet size.

A few numerical studies have considered the condensing flow of water vapour in supersonic separators. Ma et al. [30] established a two-fluid flow model to investigate the spontaneous condensation of water vapour. Ma et al. [31] also studied the effect of the location where the external particles were added on the droplet condensation by using the heterogeneous nucleation theory, and proposed that it is reasonable to add
external nuclei to increase the size of the condensed droplets. Schooshtari et al. [32] developed a new theoretical approach based on the mass transfer rates to calculate the liquid droplet growth in supersonic conditions for binary mixtures, and also analysed the condensing flow of the multi-component gas mixtures with the nucleation theory [33]. Castier [34] carried out numerical simulations of natural gas flow within a Laval nozzle both considering both single-phase flow and phase equilibrium processes. Shooshtari and Shahsavand [35] developed the heterogeneous condensation model to optimize the supersonic separator for the removal of water vapour.

In the present study, we propose and evaluate the potential of the supersonic separation technique for CO$_2$ removal, which is still not comprehensively understood in the aforementioned studies. A computational fluid dynamics (CFD) model is developed to predict the non-equilibrium condensation phenomenon of CO$_2$ in supersonic flows. The developed CFD model is subsequently validated and verified against experimental data including the static pressure and droplet radius inside a high-pressure nozzle. The developed condensing flow model is further compared to the conventional dry gas assumption without considering the phase change to demonstrate the significant effect of the condensation process on the CO$_2$ supersonic separation. The condensation parameters of CO$_2$ under the supersonic non-equilibrium state is described in detailed including the nucleation rate, a liquid fraction and droplet radius.

2 Mathematical modelling

The nucleation and condensation of condensable gases are overwhelmingly complicated due to the non-equilibrium state in supersonic flows. For the mathematical
modelling of this kind of flow behaviour, the following assumptions are used in this study: a) external particles are neglected since the focus is on the spontaneous condensation phenomenon [36], b) the effect of gravitational forces is negligible in numerical simulations [37], c) the tiny condensed droplets follow the vapour-phase streamlines with no slip velocity [38], d) the condensed liquid cannot evaporate. Correspondingly, the fundamental equations are based on the single-fluid Eulerian model employed to predict the compressible supersonic flow and the condensation phenomenon. The governing equations including the mass, momentum and energy equations are used for the gas-liquid mixture. In addition, two transport equations are coupled to model the phase change from the gaseous phase to the liquid phase, namely, the conservation of the liquid mass fraction and droplet number.

2.1 Conservation equations for gas-liquid mixture

The conservation equations of mass, momentum and energy for the vapour-liquid mixture are described as follows.

\[
\frac{\partial \rho}{\partial t} + \frac{\partial (\rho u_j)}{\partial x_j} = S_m
\]

\[
\frac{\partial (\rho u_i)}{\partial t} + \frac{\partial (\rho u_i u_j)}{\partial x_j} = -\frac{\partial p}{\partial x_i} + \frac{\partial \tau_{uj}}{\partial x_j} + S_u
\]

\[
\frac{\partial (\rho H)}{\partial t} + \frac{\partial (\rho u_i H + p)}{\partial x_j} = -\frac{\partial (\lambda_{eff} \frac{\partial T}{\partial x_j})}{\partial x_j} + \frac{\partial (u_i \tau_{uj})}{\partial x_j} + S_h
\]

where \(\rho, u_i, p, T\) and \(H\) are the density, velocity, pressure, temperature and total enthalpy, respectively. \(\lambda_{eff}\) is the effective conductivity, \(\lambda_{eff} = \lambda_v + \lambda_t\), where \(\lambda_v\) and \(\lambda_t\) are the vapour conductivity and turbulent thermal conductivity, respectively. The source terms, \(S_m\), \(S_u\) and \(S_h\) account for the mass, momentum and energy transfer associated with
condensation.

The fluid flow within the supersonic nozzles is violently turbulent and a suitable turbulence model is needed to capture the complicated compressible flows. For this purpose, the shear stress transport (SST) $k$-$\omega$ turbulence model is used due to the good accuracy to predict the supersonic nozzle flow [39] and the condensation phenomenon [40]. The equations for these turbulence models are not documented here for brevity, however, they are well documented by Menter [41].

2.2 Liquid phase equations

Two transport equations are utilized to describe the phase change process during the CO$_2$ condensation in supersonic nozzles. The conservation equations include the liquid fraction ($Y$) and droplet number ($N$):

$$\frac{\partial (\rho Y)}{\partial t} + \frac{\partial}{\partial x_j} (\rho Y u_j) = S_Y$$

(4)

$$\frac{\partial (\rho N)}{\partial t} + \frac{\partial}{\partial x_j} (\rho N u_j) = \rho J$$

(5)

where the source term $S_Y$ describes the condensation rate of the water vapour, and $J$ is the nucleation rate, respectively. $N$ is the number of droplets per volume. The source terms are defined as follows:

$$S_m = -\Gamma$$

(6)

$$S_{in} = -u_i \Gamma$$

(7)

$$S_h = -h \Gamma$$

(8)

$$S_Y = \Gamma$$

(9)

$$\Gamma = \frac{4\pi r_c^3}{3} \rho_l J + 4\pi r^2 \rho_l N \frac{dr}{dt}$$

(10)
where \( \Gamma \) is the condensation mass per unit vapour volume per unit time, \( \rho_i \) is the droplet density, \( r \) is the droplet radius. \( dr/dt \) is the growth rate of droplets. The \( r_c \) is the Kelvin-Helmholtz critical droplet radius.

The nucleation rate, \( J \), is calculated by the modified classical nucleation theory, which uses the non-isothermal correction of Kantrowitz [42] as follows:

\[
J = \frac{q_c}{1 + \phi} \frac{\rho_i^2}{\rho_l} \sqrt{\frac{2\sigma}{\pi m_v^2}} \exp\left(-\frac{4\pi\sigma}{3k_BT} r_c^2\right) \tag{11}
\]

where \( q_c \) is the condensation coefficient, \( \sigma \) is the liquid surface tension, \( m_v \) is the mass of a vapour molecule, \( k_b \) is the Boltzmann's constant, \( T_v \) is the vapour temperature. \( \phi \) is a correction factor proposed by Kantrowitz [42]:

\[
\phi = 2\gamma - 1 \frac{h}{\gamma + 1} \frac{R_T}{R_T} \left( \frac{h}{R_T} - 1 \right) \tag{12}
\]

where \( \gamma \) is the specific heat ratio, \( R_v \) is the gas constant.

The critical droplet radius, \( r_c \) is defined as:

\[
r_c = \frac{2\sigma}{\rho_l R_T \ln(S)} \tag{13}
\]

where \( S \) is the supersaturation ratio, which is defined as the ratio of vapour pressure, \( p_v \) to the equilibrium saturation pressure, \( p_{sat}(T) \).

\[
S = \frac{p_v}{p_{sat}(T)} \tag{14}
\]

The growth rate of droplets due to evaporation and condensation, \( dr/dt \), is calculated by Young’s model [43],

\[
\frac{dr}{dt} = \frac{\lambda_i (T_i - T_v)}{\rho_i h r} \left[ \frac{(1 - r^2/r)}{1 + 2\beta Kn} + \frac{3.78(1 - v)}{Kn Pr} \right] \tag{15}
\]
where $h$ is the specific enthalpy, $T_s$ is the saturated temperature, $Pr$ is the Prandtl number, $Kn$ is the Knudsen number, and $\nu$ is the modelling correction coefficient:

$$\nu = \frac{RT_s}{h} \left( \alpha - 0.5 - \frac{2 - q_c}{2q_c} \left( \gamma + 1 \right) \left( \frac{c_{pv} T_s}{h} \right) \right)$$

(16)

where $\alpha$ and $\beta$ are the modelling parameters, $c_{pv}$ is the vapour constant pressure specific heat. The modelling parameters used in this study are as follows: $q_c = 1.0$, $\alpha = 1.0$, $\beta = 0.0$.

### 2.3 Numerical implementation

The commercial package ANSYS FLUENT 18 is employed as the computational platform. The conservation equations (1) - (3) for vapour-liquid mixture are directly solved in FLUENT, while the governing equations (4) - (16) for liquid phase and the source terms are performed by the User-Defined-Scalar (UDS) and User-Defined-Function (UDF) interfaces. The implicit density-based solver is employed to perform the numerical simulation considering the supersonic and condensing flows. The second-order upwind scheme is adopted for an accurate spatial prediction. The transient state solution is used in the numerical studies with a time step of $10^{-6}$ s. The pressure inlet conditions are assigned for the nozzle entrance, while the nozzle exit utilises the pressure outlet condition.

### 3 Results and discussion

#### 3.1 Model validation

The Gyarmathy’s high-pressure nozzle [44] is employed to evaluate the CFD modelling of the condensation behaviour in supersonic flows. The high-pressure nozzle is designed as a half-Laval nozzle with the height of the throat of 10.00 mm, as shown
in Fig. 1. The contour of one side of the supersonic nozzle is a flat wall, where the pressure tap is installed to test the static pressure during the experiments. The other side of the supersonic nozzle is a curved wall as described in Table 1. The main dimensions include the length of the converging section of 30 mm and the length of the diverging section of 100 mm. The heights of the inlet and outlet of the supersonic nozzle are 19.99 mm and 17.91 mm, respectively. The computational conditions and modelling parameters are listed in Table 2.

![Fig. 1 Geometry of Gyarmathy’s nozzle](image)

**Table 1. Curve contour of Gyarmathy’s nozzle**

<table>
<thead>
<tr>
<th>x (mm)</th>
<th>y (mm)</th>
<th>x (mm)</th>
<th>y (mm)</th>
<th>x (mm)</th>
<th>y (mm)</th>
<th>x (mm)</th>
<th>y (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>-24</td>
<td>10.79</td>
<td>-2</td>
<td>16.49</td>
<td>18</td>
<td>15.94</td>
<td>50</td>
<td>13.74</td>
</tr>
<tr>
<td>-20</td>
<td>12.97</td>
<td>0</td>
<td>16.50</td>
<td>20</td>
<td>15.84</td>
<td>54</td>
<td>13.40</td>
</tr>
<tr>
<td>-18</td>
<td>13.85</td>
<td>2</td>
<td>16.49</td>
<td>22</td>
<td>15.73</td>
<td>60</td>
<td>12.87</td>
</tr>
<tr>
<td>-16</td>
<td>14.60</td>
<td>4</td>
<td>16.46</td>
<td>24</td>
<td>15.61</td>
<td>64</td>
<td>12.50</td>
</tr>
<tr>
<td>-14</td>
<td>15.21</td>
<td>6</td>
<td>16.42</td>
<td>26</td>
<td>15.49</td>
<td>70</td>
<td>11.92</td>
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<tr>
<td>-12</td>
<td>15.69</td>
<td>8</td>
<td>16.36</td>
<td>28</td>
<td>15.37</td>
<td>80</td>
<td>10.89</td>
</tr>
<tr>
<td>-10</td>
<td>16.03</td>
<td>10</td>
<td>16.29</td>
<td>30</td>
<td>15.24</td>
<td>90</td>
<td>9.78</td>
</tr>
<tr>
<td>-8</td>
<td>16.24</td>
<td>12</td>
<td>16.22</td>
<td>34</td>
<td>14.97</td>
<td>100</td>
<td>8.59</td>
</tr>
<tr>
<td>-6</td>
<td>16.37</td>
<td>14</td>
<td>16.13</td>
<td>40</td>
<td>14.53</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Table 2. The computational condition for Gyarmathy’s nozzle

<table>
<thead>
<tr>
<th>Inlet conditions</th>
<th>Outlet conditions</th>
<th>Wall conditions</th>
<th>Modelling parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td>Total pressure: 89 bar</td>
<td>No-slip Supersonic flows</td>
<td>Adiabatic wall</td>
<td>$q_c = 1.0$, $\alpha = 1.0$, $\beta = 0.0$</td>
</tr>
<tr>
<td>Total temperature: 619.96 K</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

The resolution of the grid is one of the key issues for the prediction of the CO$_2$ condensing behaviour in supersonic flows, which presents an extraordinarily complicated fluid flow phenomenon including the transonic flow, shock wave and flow separation. For this reason, a multi-block structure mesh is performed for the supersonic nozzle, while the fine grid scheme is adopted in the boundary layer to ensure that $y^+$ is less than 1 for the SST $k$-$\omega$ turbulence model. The grid of Gyarmathy’s nozzle is shown in Fig. 2. The numerical results are performed with a medium mesh of 22800 cells after evaluating the mesh independence with 7920, 22800 and 40000 cells, respectively. Fig. 3 presents the numerical and experimental results of the flow field and droplet radius inside the high-pressure nozzle. The results of the calculated static pressure are in good agreement with the experimental data. The model accurately captures the onset of the condensation process, which occurs approximately at $x = 0.033$ m. Furthermore, the CFD model predicts the droplet radius of 0.121 µm at $x = 0.093$ m, while the measurement was approximately 0.143 µm in the experimental test. This indicates that the developed CFD modelling accurately predicts and captures the condensation behaviour in supersonic flows.
Fig. 2 Grid of Gyarmathy’s nozzle

Fig. 3 Numerical and experimental results of flow field and droplet radius inside Gyarmathy’s nozzle
3.2 Effect of CO$_2$ condensation on the flow field

The converging-diverging nozzle from Moses and Stein experiments [45] was employed to study the non-equilibrium condensation of CO$_2$ in supersonic flows, as shown in Fig. 4. The configuration and main dimensions of the supersonic nozzle used in the CFD simulation are described in Fig. 4 and Table 3, respectively. The area ratio of the supersonic nozzle is 3.55, which is defined as the ratio of the nozzle exit area to the nozzle throat area. The 2D geometry was employed in the CFD model to evaluate the performance of the supersonic nozzle. The computational domain was discretized by a structured mesh to reduce the numerical diffusion, as shown in Fig. 4. Approximately 50 000 cells were employed for the numerical simulation after the mesh independence tests. The computational conditions and modelling parameters are listed in Table 4.

Fig. 4 Geometry and grid of converging-diverging nozzle
Table 3. Dimensions of the converging-diverging nozzle

<table>
<thead>
<tr>
<th>Geometrical parameters</th>
<th>Value (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Diameter of nozzle inlet ($D_1$)</td>
<td>40.00</td>
</tr>
<tr>
<td>Diameter of nozzle throat ($D_2$)</td>
<td>10.00</td>
</tr>
<tr>
<td>Diameter of nozzle outlet ($D_3$)</td>
<td>18.85</td>
</tr>
<tr>
<td>Converging length of the supersonic nozzle ($L_1$)</td>
<td>57.53</td>
</tr>
<tr>
<td>Diverging length of the supersonic nozzle ($L_2$)</td>
<td>102.47</td>
</tr>
</tbody>
</table>

Table 4. The computational condition for the converging-diverging nozzle

<table>
<thead>
<tr>
<th>Inlet conditions</th>
<th>Outlet conditions</th>
<th>Wall conditions</th>
<th>Modelling parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td>Total pressure: 40 bar</td>
<td>No-slip,</td>
<td>$q_e = 1.0$, $\alpha = 1.0$, $\beta = 0.0$</td>
<td></td>
</tr>
<tr>
<td>Total temperature: 283 K</td>
<td>Supersonic flows</td>
<td>adiabatic wall</td>
<td></td>
</tr>
</tbody>
</table>

Fig. 5 describes the contours of CO$_2$ Mach number based on the dry gas and condensing flow models. The results clearly demonstrate the effect of the condensation phenomenon on the CO$_2$ expansion processes inside the converging-diverging nozzle. It can be seen that the dry gas and condensing flows both achieve the supersonic velocity in the diverging part, while they both predict the choked flows at the nozzle throat. The increase of the Mach number shows that the CO$_2$ gas flows further accelerate and expand to the nozzle exit. However, the dry gas and condensing flow approaches predict different Mach number values. The dry gas assumption over-predicts a further expansion than the condensing flow model. For example, the dry gas
predicts a Mach number of 2.33 at the exit plane of the supersonic nozzle, while the condensing flow gives a Mach number of 2.18. The difference of Mach number values between these two approaches reaches 6.9% at the nozzle outlet for CO$_2$ flows. This indicates that the CO$_2$ condensation significantly influences the expansion characteristics in the supersonic flows.

Fig. 6 shows the Mach number profiles at the central line of the supersonic model for the dry gas and condensing flow models. It is also demonstrated that the dry gas assumption predicts a higher Mach number in the diverging part of the supersonic nozzle than the condensing flow model, which means that the dry gas assumption over-predicts the expansion characteristics of the supersonic flows. This clearly illustrates the significant influence of the condensation phenomenon due to the supersonic flow. From the profile of the condensing flow model, one can see that the CO$_2$ Mach number increases along the supersonic nozzle and starts to deviate from the dry gas assumption in the diverging part of the supersonic nozzle. This indicates that the occurrence of the condensed liquids causes more energy losses, which cannot be described by the dry gas assumption.

![Mach number profiles](image)

**Fig. 5 CO$_2$ Mach number contours in converging-diverging nozzles**
Fig. 6 CO₂ Mach number profiles at the central line of converging-diverging nozzles

Fig. 7 describes the distribution of the static temperature of CO₂ flow along the supersonic nozzle for the dry gas assumption and condensing flow model. The differences are evident between the dry gas and condensing flow simulations. Without considering the condensation process inside the supersonic nozzle, the dry gas assumption obtains unphysical results, i.e., the static temperature limitlessly decreases to the nozzle exit. For instance, the dry gas assumption predicts the minimum static temperature of approximately 177 K, which is much lower than the triple point of 217 K for CO₂. Combining the pressure-temperature profiles in Fig. 8, it correspondingly leads to the confusion that the formation of CO₂ ice may occur in such a low temperature. In fact, this is an artefact due to the assumption of the dry gas model.

For the condensing flow model, the static temperature decreases along the supersonic nozzle and presents a sudden jump when the condensation phenomenon of
CO₂ occurs downstream of the nozzle throat. The heat is released during the phase change from the vapour to the liquid, which forces the vapour-liquid mixture to return to the equilibrium state. The static temperature distribution distinctly shows that the condensing flow model limits the drop of the static temperature lower than the triple point. This thereby eliminates the artefact of the CO₂ ice formation. On the other hand, it also demonstrates that the developed condensing flow model accurately captures the CO₂ condensation process in supersonic flows.

Fig. 7 Static temperature along the converging-diverging nozzle for dry gas and condensing flow models
3.3 CO₂ condensation characteristics

Fig. 9 presents the degree of supercooling and the degree of supersaturation for the flow of CO₂ inside the converging-diverging nozzle, which both describe the vapour state during the supersonic expansion. The degree of supercooling, $\Delta T = T_s - T_v$, is defined as the difference between the saturation temperature ($T_s$) and local vapour temperature ($T_v$). The nucleation rate profile at the central line of the supersonic nozzle is shown in Fig. 10. One can see that the condensation does not occur immediately when the CO₂ reaches the saturation state at $x=0.038$ m. The reason is that we only consider the spontaneous condensation of the CO₂ fluids without involving heterogeneous condensation, i.e., the effect of foreign particles present in the flow. The static pressure and temperature sequentially decrease because of the vapour expansion in the diverging part of the supersonic nozzle. The vapour correspondingly diverges
further from the equilibrium state. For instance, the peaks of the degree of supercooling and the degree of supersaturation are approximately 8.36 K and 1.14 at \( x = 0.066 \) m, respectively. The highly non-equilibrium state induces the appearance of the nucleation and condensation of CO\(_2\) in a remarkably small area, which can be observed in the distribution of the nucleation rate in Fig. 10. The vapour returns to the quasi-equilibrium state due to the latent heat release to the vapour phase during the condensation process, as shown in Fig. 9.

Fig. 11 presents the liquid fraction along the supersonic nozzle. Combined with the distribution of the nucleation rate in Fig. 10, it is observed that the liquid fraction increases with the occurrence of the nucleation process. The rapid nucleation and condensation induce the sharp increase of the liquid fraction until the exit plane of the supersonic nozzle. The liquid fraction reaches a peak value of approximately 0.186 at this point, which shows that the amount of the liquid fraction has a significant influence on the vapour phase. Fig. 12 describes the distribution of the droplet radius along the flow direction in the supersonic nozzle. We can see that the droplet radius presents a similar distribution with the liquid fraction. The maximum size of the condensed CO\(_2\) droplets is approximately 1 \( \mu \)m at the nozzle exit. This indicates that the assumptions of the tiny particles following the vapour phase and the no-slip velocity between the vapour and liquid phases are reasonable in the CFD modelling of the CO\(_2\) condensation phenomenon inside the supersonic nozzle.
Fig. 9 Degree of supercooling and degree of supersaturation along the converging-diverging nozzle

Fig. 10 Nucleation rate along the converging-diverging nozzle
Fig. 11 Liquid fraction along the converging-diverging nozzle

Fig. 12 Droplet radius along the converging-diverging nozzle

3.4 Discussion

This study presents the preliminary results of the CO$_2$ phase change in supersonic
flows, where only the Laval nozzle is considered without implementation of a swirling device and a diffuser for a supersonic separator. Correspondingly, the flow behaviour is simplified for the numerical simulation, while more complicated flows are neglected including the shock wave, flow separation, strong swirling flows.

Bian et al. [22] carried out the numerical simulation for the water vapour removal inside a supersonic separator, and the single-phase flow model predicted a minimum value of the static temperature of 199.43 K. Hu et al. [26] predicted a static temperature lower than 180 K without considering the phase change processes of the water vapour in a supersonic separator. Moreover, Secchi et al. [22] obtained the minimum static temperature of approximately 140 K according to the 1D model without involving condensing flow processes. Considering our numerical results of the condensing flow behaviour, the assumption of the dry gas model over-predicts the gas expansion in supersonic flows and give an artefact of the static temperature. This also demonstrates that the implementation of the condensing flow model is essential to estimate the possibility of the removal of either water vapour or CO₂ using supersonic separation.

Furthermore, it is worth noting that the condensing flow model is a semi-empirical model, which employs the modelling parameters to predict the nucleation and droplet growth processes. The values of the modelling parameters, $\alpha$, $\beta$, $q_c$, are various in different investigator's models. Starzmann et al. [46] validated their model against experimental data from the Moses and Stein nozzle [45] with $q_c = 1.0$, $\alpha = 11.0$. Grübel et al. [47] used the modelling parameters $q_c = 1.0$, $\alpha = 0.0$, $\beta = 0.0$ to validate and verify their CFD model with the Moses and Stein nozzle [45]. In this study, the model
validation indicates that the modelling parameters, \( q_c = 1.0, \alpha = 1.0, \beta = 0.0 \) show a good agreement with experimental data from the Gyarmathy’s high-pressure nozzle [44] with the working fluid of water vapour. The same modelling parameters are implemented for CO\(_2\) simulation because there are no available experimental data for the validation and verification of CO\(_2\) condensation in supersonic flows. The computational results, at least, demonstrate in the qualitative analysis that it is a potential way to condense CO\(_2\) in supersonic flows. The condensing flow model, therefore, needs to be further validated against experimental tests with the working fluid of CO\(_2\) in future work.

5 Conclusions

This study shows an alternative approach of mitigating CO\(_2\) emissions to the environment. The modelling using computational fluid dynamics developed in this study can predict the nucleation and condensation of CO\(_2\) due to the non-equilibrium phenomenon in supersonic flows. The single-fluid flow model is employed for the modelling with the assumption of no-slip velocity between vapour and liquid phases, while two conservation equations of liquid fraction and liquid number are used to describe the phase change processes.

The developed condensing flow model and conventional dry gas model are compared to show the different predictions on the flow structures and condensation characteristics during the CO\(_2\) phase change in supersonic flows. The dry gas assumption predicts an incorrect distribution of the static temperature without considering the condensation process, which leads to a minimum static temperature of
approximately 177 K, much lower than the CO₂ triple point of 217 K. This may result in the misunderstanding of CO₂ ice formation problem in such a low temperature. The condensing flow model eliminates this artefact by considering the heat and mass transfer during the condensation process in supersonic flows. The condensing flow model predicts the liquid fraction of 18.6% of the total mass due to the high expansion of the supersonic flow. The amount of the condensed liquid influences the vapour phase by heat and mass transfer.

This study has presented an alternative solution of mitigating CO₂ emissions in an efficient and environment-friendly way. The developed CFD model provides a basic method to predict non-equilibrium condensation of CO₂ in supersonic flows. This study provides the insights to design and optimisation of the supersonic separation technique for future applications of CO₂ removal contributing to CCS.

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