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Novel Predictive Stator Flux Control Techniques for PMSM drives

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Abstract—In this paper, a predictive stator flux control (PSFC) algorithm for permanent magnet synchronous motor (PMSM) drives is proposed, which can eliminate the influence of flux linkage parameter perturbation and rotor position error. First, the sensitivity of conventional predictive current control (PCC) to the flux linkage parameter and rotor position is analyzed. Then, the novel composite discrete time sliding mode observer (SMO) based on stator flux state is designed, which can estimate the flux linkage parameter perturbation, rotor position error and load torque simultaneously. Finally, a novel PSFC method is developed, which can enhance the robustness of PCC against flux linkage parameter perturbation and rotor position error by using composite discrete time SMO. Simulation and experimental results indicate that the proposed PSFC can achieve low stator current harmonics, low torque ripple and excellent steady-state performance under the flux linkage parameter perturbation and rotor position error.

Index Terms — Sliding mode observer, flux linkage parameter perturbation, rotor position error, permanent magnet synchronous motor, predictive current control.

I. INTRODUCTION

Permanent magnet synchronous motor (PMSM) drives have been extensively employed in industrial applications, such as robots, electrical vehicles, and wind power generators[1,2], due to its advantages of compact structure, excellent dynamic properties, high performance operations [3,4]. In order to achieve desired servo control performance, field-oriented control (FOC) strategy has been used in most PMS drive systems. In an FOC-based PMSM drive, the double loop controller is usually adopted. The outer loop controller is to control rotor speed, and the inner loop controller is to control stator current. The PCC has received extensive attention for the inner loop controller as it has the advantages of excellent transient response characteristics and accurate reference current tracking [5,6]. The performance of PCC method crucially depends on the accuracy of the stator inductance, flux linkage parameter as well as rotor position. However, the permanent magnet (PM) flux linkage parameter may change due to temperature rise and magnet saturation, especially under high temperature operation conditions [7]. In engineering, the temperature change will inevitably leads to permanent magnet demagnetization, a 20% flux reduction for a ferrite-based magnet occurs per 100 °C increase in ambient temperature [8]. Although the permanent magnet has positive coefficient of coercivity, the flux linkage parameter of the motor still changes with the temperature variation, especially the motor used in tank and high-speed train. On the other hand, the rotor position measured by the resolver or the encoder attached to the PMSM shaft may deviate from the true position due to the misalignment of the mechanical sensor components mounted on the PMSM [9-11], which causes the Park coordinate transformation providing a mistaken feedback current to the PCC algorithm. As a result, the control performance of the PMSM is deteriorated.

The main approach to improve flux linkage parameter robustness for the PCC is based on identification. In [12], an improved deadbeat PCC algorithm based on stator current and disturbance observer is proposed for the PMSM drive systems, which can optimize the PCC performance of the PMSM system with flux linkage parameter mismatch. In[13], a Kalman filter and a Luenberger observer are designed to estimate rotor state variables. In [14,15], the robust PCC algorithm based on disturbance observer is adopted for the PMSM drives, which can overcome flux linkage parameter mismatch on the effect of the PCC and obtain high dynamic performance. In [16], a robust fault-tolerant PCC algorithm based on a composite SMO is proposed for PMSM, which can guarantee the performance of the system regardless of parameter perturbation, permanent magnet demagnetization, and one step delay. In [17], a model-free PCC method of interior PMSM drives based on a current difference detection technique is proposed, which does not require any motor parameters. However, the higher current sampling frequency tends to limit its industrial application. In [18,19], a flux immunity robust PCC algorithm for PMSM drives is proposed to eliminate the using of PM flux linkage parameter in prediction model, but the method ignores the effect caused by rotor position measurement error.

The accuracy of rotor position is crucial for FOC when the minimum torque ripple is demanded over the entire operating range of the motor. In [9-11], the experimental results show that the torque oscillation caused by other factors is almost negligible compared with the rotor position error. In [20], a PMSM torque predictive control scheme is proposed, which can eliminate high current harmonics and torque ripples caused by rotor position error. In [21], a new torque predictive...
control method of PMSM drives is proposed, which can control the torque by using the magnitude of the stator voltage vector. In [22], the sensorless predictive torque control scheme relies on the anisotropy of the inductance is proposed, which can achieve the low torque ripple during the full speed range. The control methods mentioned above provide low torque ripple under rotor position error. However, the flux linkage parameter is looked on as constant in these control methods, which can’t be guaranteed in engineering.

In this paper, a novel PSFC techniques is developed to guarantee the performance of PMSM drives regardless of flux linkage parameter perturbation, rotor position error, and one step delay in digital control. In contrast to the conventional PCC method, the proposed PSFC method can achieve the lower torque ripple and stator current harmonics by applying a novel composite discrete time SMO based on stator flux state. The performance of the proposed PSFC method is validated by simulation and experimental results.

This paper is organized as follows. A nonlinear PMSM model under flux linkage parameter perturbation and rotor position error is developed in section II. The influence of flux linkage parameter perturbation and rotor position error on conventional PCC is analyzed in Section III. The PSFC method is proposed in Section IV. The composite discrete time SMO based on stator flux state is designed in Section V. The simulations and experiments are setup in Section VI and Section VII, respectively. Section VIII concludes this paper.

II. NONLINEAR PMSM MODEL

The voltage state-space equations of the PMSM are described in Eq. (1) [18].

\[
\begin{align*}
\frac{d}{dt}i_d &= -\frac{R}{L_d}i_d + \frac{L_q}{L_d}\omega i_q + \frac{1}{L_d}u_d \\
\frac{d}{dt}i_q &= -\frac{R}{L_q}i_q - \frac{L_d}{L_q}\omega i_d - \frac{1}{L_q}\psi_{ro} + \frac{1}{L_q}u_q
\end{align*}
\]

where, \(\frac{L_q}{L_d}\omega i_q\) and \(-\frac{L_d}{L_q}\omega i_d\) are d-and q-axis cross-coupling terms, respectively. According to (1), the voltage state-space equations of the SPMSM are,

\[
\begin{align*}
\frac{d}{dt}i_d &= -\frac{R}{L}i_d + \omega i_q + \frac{1}{L}u_d \\
\frac{d}{dt}i_q &= -\frac{R}{L}i_q - \omega i_d - \frac{\psi_{ro}}{L} + \frac{1}{L}u_q
\end{align*}
\]

For surface-mounted PMSM (SPSM), \(L_d = L_q = L\). The d-and q-axis cross-coupling terms are \(\omega i_q\) and \(-\omega i_d\), respectively. According to (2), the d-and q-axis voltage equations of the SPMSM are,

\[
\begin{align*}
u_d &= Ri_d + \frac{d\psi_d}{dt} - \omega\psi_q \\
u_q &= Ri_q + \frac{d\psi_q}{dt} + \omega\psi_d
\end{align*}
\]

where,

\[
\begin{align*}
\psi_d &= Li_d + \psi_{ro} \\
\psi_q &= Li_q
\end{align*}
\]

The electromagnetic torque produced by the SPMSM is,

\[
T_e = \frac{3}{2}n_p\psi_{ro}i_q = \frac{3}{2}n_p\psi_{ro}\frac{\psi_q}{L}
\]

The mechanical dynamic model of the SPMSM can be described as follows,

\[
\frac{J}{n_p}\frac{d\omega}{dt} = T_e - T_L
\]

where, \(u_d\) and \(u_q\) represent the d-and q-axis stator voltages, respectively; \(i_d\) and \(i_q\) are the d-and q-axis currents, respectively; \(\psi_d\) and \(\psi_q\) are the d-and q-axis stator flux components, respectively; \(R\), \(L\) and \(J\) are the stator resistance, stator inductance and the moment of inertia, respectively; \(\omega\) is the electrical rotor speed, \(\psi_{ro}\) is the flux linkage, \(n_p\) is the number of pole pairs, \(T_e\) is the electromagnetic torque, and \(T_L\) is the load torque.

Fig. 1. Variation of PMSM flux linkage.

The variation of flux linkage is illustrated in Fig. 1. Where, “\(\theta_o\)” and “\(\theta\)” are the actual value and measurement value of the rotor position, respectively. There exists an error \(\Delta\theta\) between \(\theta\) and \(\theta_o\) when the rotor position measurement is inaccurate. “\(\psi_r\)” and “\(\psi_{ro}\)” are the actual and nominal values of the flux linkage parameters, respectively. There also exists an error between “\(\psi_r\)” and “\(\psi_{ro}\)” due to temperature rise and saturation. The flux linkage parameter perturbation rate is defined as,
\[ \lambda = \frac{\psi_{ro} - \psi_r}{\psi_{ro}} \]  

(6)

The d- and q-axis flux linkage equations can be expressed as follows when there exists flux linkage parameter perturbation and rotor position error.

\[
\begin{align*}
\psi_d &= \psi_{ro} + L_i d + \Delta \psi_{rd} \\
\psi_q &= L_i q + \Delta \psi_{rq}
\end{align*}
\]

(7)

with,

\[
\begin{align*}
\Delta \psi_{rd} &= \psi_r \cos(\Delta \theta) - \psi_{ro} \quad (1 - \lambda) \cos(\Delta \theta) - 1 \\
\Delta \psi_{rq} &= \psi_r \sin(\Delta \theta) - \psi_{ro} \quad (1 - \lambda) \sin(\Delta \theta)
\end{align*}
\]

(8)

where, \( \Delta \psi_{rd} \) and \( \Delta \psi_{rq} \) are the d- and q-axis flux linkage components under flux linkage parameter perturbation and rotor position error, respectively.

In engineering, the time constant of the electrical system is much less than that of the mechanical system. Therefore, \( \Delta \psi_{rd} \) and \( \Delta \psi_{rq} \) can be looked on as,

\[
\frac{d \Delta \psi_{rd}}{dt} \approx 0
\]

\[
\frac{d \Delta \psi_{rq}}{dt} \approx 0
\]

Substituting (7) into (3), we can get,

\[
\begin{bmatrix}
\dot{i}_d \\
\dot{i}_q
\end{bmatrix} =
\begin{bmatrix}
\frac{R}{L} & \omega \\
-\omega & \frac{R}{L}
\end{bmatrix}
\begin{bmatrix}
i_d \\
i_q
\end{bmatrix} +
\begin{bmatrix}
0 & \frac{L}{\omega} \\
0 & 0
\end{bmatrix}
\begin{bmatrix}
\psi_{ro} + \Delta \psi_{rd} \\
\Delta \psi_{rq}
\end{bmatrix}
\]

(9)

According to (7), Eq. (4) is changed to,

\[
T_e = \frac{3}{2} n_p (\psi_{ro} + \Delta \psi_{rd}) \frac{\psi_q + \Delta \psi_{rq}}{L}
\]

(10)

Substituting (10) into (5), we can get,

\[
\frac{d \omega}{dt} = \frac{3 n_p^2 \psi_{ro}}{2 J L} \omega - \frac{n_p}{J} T_e + \frac{n_p}{2 J L} f_o
\]

(11)

with,

\[
f_o = 3 n_p \left[ \psi_{ro} \Delta \psi_{pr} + \Delta \psi_{rd} \psi_q + \Delta \psi_{rd} \Delta \psi_{rq} \right]
\]

(12)

where, \( f_o \) is the equivalent disturbance caused by flux linkage parameter perturbation and rotor position error.

III. SENSITIVITY ANALYSIS OF FLUX LINKAGE PARAMETER AND ROTOR POSITION ON CONVENTIONAL PCC

In order to evaluate the sensitivity of conventional PCC to the flux linkage parameter and rotor position, the influence of flux linkage parameter mismatch and rotor position error are analyzed in this section. The block diagram of conventional PCC is illustrated in Fig. 2.

![Fig. 2. Block diagram of the conventional PCC.](image)

The output voltage vectors of the PCC are expressed by [18],

\[
u(k) = F^{-1} \left[ \begin{array}{c} \mathbf{i}^{ref}(k+1) - \mathbf{G}(k) \mathbf{i}(k) - \mathbf{P}(k) \end{array} \right]
\]

(13)

where, \( \mathbf{i}^{ref}(k+1) = \begin{bmatrix} \mathbf{i}^{ref}_d(k+1) \\ \mathbf{i}^{ref}_q(k+1) \end{bmatrix} \), \( \mathbf{i}(k) = \begin{bmatrix} i_d(k) \\ i_q(k) \end{bmatrix} \),

\[
u(k) = \begin{bmatrix} u_d(k) \\ u_q(k) \end{bmatrix}, \quad F = \begin{bmatrix} T_s L \\ 0 \\ T_s L \end{bmatrix}, \quad G(k) = \begin{bmatrix} 1 - \frac{R}{L} T_s \\ -T_s \omega(k) - \frac{1 - R}{L} T_s \end{bmatrix}, \quad P(k) = \begin{bmatrix} 0 \\ -\frac{\psi_{ro} T_s \omega(k)}{L} \end{bmatrix}
\]

According to (9), the discrete model of the PMSM under flux linkage parameter perturbation and rotor position error can be expressed by,

\[
i(k+1) = G(k) \cdot \mathbf{i}(k) + F \cdot \mathbf{u}(k) + \mathbf{P}(k)
\]

(14)

where, \( \mathbf{P}(k) = \begin{bmatrix} \frac{\Delta \psi_{rd} T_s \omega(k)}{L} \\ -\frac{\psi_{ro} T_s \omega(k)}{L} - \frac{\Delta \psi_{rd} T_s \omega(k)}{L} \end{bmatrix} \).

For sampling delay, the conventional PCC method employed in the practical application belong to one beat delay control. At the \((k+1) T_s\) moment, the voltage vector \( \mathbf{u}(k) \) is applied to the PMSM. Therefore, substituting (13) into (14) yields,

\[
i_d(k+1) = i_d^{ref}(k+1) + \Delta i_d(k+1)
\]

(15)

\[
i_q(k+1) = i_q^{ref}(k+1) + \Delta i_q(k+1)
\]

(16)

with

\[
\begin{align*}
\Delta i_d(k+1) &= \frac{\Delta \psi_{rd}}{L} T_s \omega(k) - \frac{1 - \lambda}{L} \psi_{ro} T_s \omega(k) \\
\Delta i_q(k+1) &= \frac{\Delta \psi_{rd}}{L} T_s \omega(k) - \frac{1 - \lambda}{L} \psi_{ro} T_s \omega(k)
\end{align*}
\]

(17)
From (15) and (16), it can be found that there exits an error between the current response value and the current reference value under flux linkage parameter perturbation and rotor position error. According to (17), the current error is related to the speed, the flux linkage parameter perturbation rate and the rotor position error. The PMSM is uncontrollable if the rotor position error range exceeds $\pm 5^\circ$ [23]. Therefore, in the case of the rotor position allowable error range (i.e. $\pm 5^\circ$), the influence of rotor position error on PCC is analyzed in this paper.

The motor parameters are shown in Table I. The d-and q-axis current errors are plotted under flux linkage parameter perturbation and rotor position error, as shown in Fig. 3 and 4. Fig. 3 shows the d- and q-axis current errors under flux linkage parameter mismatch. The q-axis current response value is greater than its reference, but the flux linkage parameter mismatch does not affect the d-axis current. Fig. 4 shows the relationship between the current error and the speed under flux linkage parameter mismatch and rotor position error. When the rotor position error range is positive, the d-and q-axis response current is greater than the current reference. When the rotor position error range is negative, the q-axis response current is greater than the current reference, and the d-axis response current is less than the current reference. The q-axis current error increase with the increase of speed under flux linkage parameter perturbation and rotor position error. Through the analysis above, it can be concluded that the q-axis current of conventional PCC is mostly sensitive to rotor position and flux linkage parameters, while the influence of d-axis current can be neglected.

Fig. 3. d- and q-axis current errors under flux linkage parameter mismatch.

According to (9), (10) and (11), we can express the state equations of the PMSM as follows when flux linkage parameter mismatch and rotor position error occur.

\[
\frac{dx}{dt} = Ax + Bu + Cf_{\psi} + Df_{a}
\]

(18)

where, \( x = \begin{bmatrix} \psi_d \\ \psi_q \\ \omega \end{bmatrix} \), \( x_1 = \begin{bmatrix} i_d \\ i_q \\ \omega \end{bmatrix} \), \( u = \begin{bmatrix} u_d \\ u_q \end{bmatrix} \), \( f_{\psi} = \begin{bmatrix} \psi_{ro} \\ \psi_{ro} \end{bmatrix} \), and

\[
f_a = \begin{bmatrix} \Delta \psi_{rd} \\ \Delta \psi_{rq} \\ T_L \frac{f_{wo}}{2L} \end{bmatrix}
\]

are state variables, system inputs, system outputs, PM flux linkage, and fault function, respectively.

Fig. 4. d- and q-axis current errors under flux linkage parameter mismatch and rotor position error.

IV. PREDICTIVE STATOR FLUX CONTROL

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The coefficient matrices of the state equations are
\[
A = \begin{bmatrix}
-\frac{R}{L} & \omega & 0 \\
-\omega & -\frac{R}{L} & 0 \\
0 & 0 & 0 \\
\end{bmatrix},
B = \begin{bmatrix}
1 & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & \frac{3n_p^2\psi_{ro}}{2JL} \\
\end{bmatrix},
C = \begin{bmatrix}
R & 0 & 0 \\
0 & 0 & 0 \\
0 & 0 & 0 \\
\end{bmatrix}.
\]

The discrete expression of (18) is,
\[
\begin{bmatrix}
u_d(k) \\
u_q(k) \\
\psi_d(k) \\
\psi_q(k)
\end{bmatrix} =
\begin{bmatrix}
u_d(k+1) \\
u_q(k+1) \\
\psi_d(k+1) \\
\psi_q(k+1)
\end{bmatrix} +
\begin{bmatrix}
1 & -\frac{R}{L} & \omega(k) \\
0 & 1 & \omega(k) \\
\frac{1}{T_s} & 0 & 0 \\
0 & \frac{1}{T_s} & 0
\end{bmatrix}
\begin{bmatrix}
u_{dref}(k+1) \\
u_{qref}(k+1) \\
\psi_{dref}(k+1) \\
\psi_{qref}(k+1)
\end{bmatrix} \Delta k
\]

where, \(\Delta k\) is the sampling time of the external speed loop, and \(\psi_{dref}(k+1)\) and \(\psi_{qref}(k+1)\) are the d-and q-axis stator flux references, respectively.

In order to achieve an accurate value of the d-and q-axis stator flux references (i.e. \(\psi_{dref}(k+2)\) and \(\psi_{qref}(k+2)\)), a second-order expansion for the rotor speed is proposed.

\[
o(k+1) = \omega(k) + \frac{d\omega}{dt}T_{ds} + \frac{d^2\omega}{dt^2}T_{ds}^2
\]

where, \(T_{ds}\) is the sampling time of the external speed loop, and \(T_{ds} = 10T_s\).

According to (11), due to the load torque being invariant in the sampling time, and the change of flux linkage components being slow, therefore, \(\frac{dT_L}{dt} = 0\) and \(\frac{d\omega}{dt} = 3n_p\Delta\psi_{rd}\frac{d\psi_q}{dt}\), one yields

\[
\frac{d^2\omega}{dt^2} = \frac{3n_p^2\psi_{ro}}{2JL}\frac{d\psi_q}{dt} + 3n_p\Delta\psi_{rd}\frac{d\psi_q}{dt}
\]

Substituting (11) and (22) into (21), we can get,

\[
o(k+1) = \omega(k) + \frac{3n_p^2\psi_{ro}}{2JL}\psi_q(k) - \frac{n_p}{J}T_L + \frac{n_p}{2JL}f_{\alpha}:T_{ds}
\]

Taking \(\psi_{qref}(k)\) and \(\omega_{ref}\) as the references of \(\psi_q(k)\) and \(\omega(k+1)\), respectively, the following equation can be obtained from (23),
where, $\psi_q^r(k)$ and $\omega^{ref}(k)$ are the stator flux reference and speed reference, respectively; $\Delta \dot{\psi}_d = \psi_{ref} \left[1 - \dot{\lambda} \cos(\Delta \dot{\theta}) - 1\right]$; $\dot{T}_L$ and $i_{d0}$ are the observed values of the load torque and unknown external disturbances, respectively.

Then, the stator flux reference is calculated using Lagrange extrapolation under $i_{d0}^{ref}(k) = 0$, as expressed by,

$$
\begin{align*}
\psi_d^{ref}(k+2) &= \psi_d^{ref}(k+1) = \psi_d^{ref}(k) = \psi_{ro} + Ld_0^{ref}(k) = \psi_{ro} \\
\psi_q^{ref}(k+2) &= 3\psi_q^{ref}(k) - 3\psi_q^{ref}(k-1) + \psi_q^{ref}(k-2)
\end{align*}
$$

(25)

**Fig. 5. Block diagram of the PMSM drive system with PSFC method.**

The block diagram of the PMSM drive system with PSFC method is shown in Fig. 5. The proposed PSFC method is used to substitute conventional PCC to overcome the influence of flux linkage parameter mismatch, rotor position error and one step delay.

**V. DESIGN OF COMPOSITE DISCRETE TIME SMO**

The key to realizing PSFC method is to estimate the flux linkage parameter perturbation rate, rotor position error, and load torque. The composite discrete time SMO can simultaneously estimate these unknown factors. Based on (18), the composite SMO is designed as follows,

$$
\begin{align*}
\frac{d\hat{\theta}}{dt} &= A\hat{x} + Bu + Cf_{\psi} + \omega Me + \omega H \text{sgn}(e) \\
\hat{x} &= E\hat{x}_1 + f_{\psi}
\end{align*}
$$

(26)

where, $\hat{x}$ is the observed value of $x$; $\text{sgn}()$ is the sliding mode control function; $M$ and $H$ are the designed gain matrices of composite SMO.

The time-varying sliding surface is defined as,

$$
e = x - \hat{x} = E(x_1 - \hat{x}_1)
$$

(27)

The dynamic equation considering the estimation error is obtained by subtracting (18) from (26),

$$
\frac{de}{dt} = Ae + Df_a - \omega Me - \omega H \text{sgn}(e)
$$

(28)

Differentiating (28) and combining (27), one yields.

$$
\frac{dV}{dt} = e^T(Ae + Df_a - \omega Me - \omega H \text{sgn}(e))
$$

(29)

where, $M$ and $H$ are designed as $M = \begin{bmatrix} 0 & 1 & 0 \\ -1 & 0 & 0 \end{bmatrix}$ and $H = \begin{bmatrix} h_1 & 0 & 0 \\ 0 & h_2 & 0 \\ 0 & 0 & h_3 \end{bmatrix}$, respectively.

Simplifying (29) yields,

$$
\frac{dV}{dt} = \frac{R}{L} e_1^2 - \frac{R}{L} e_2^2 + e^T Df_a - e^T \omega H \text{sgn}(e)
$$

$$
\leq e^T Df_a - e^T \omega H \text{sgn}(e)
$$

$$
= (\alpha \Delta \psi_{rq} e_1 - \omega h_1 e_1) + (-\alpha \Delta \psi_{rq} e_2 - \omega h_2 e_2) + \left(\frac{n_p}{J} (T_L - \frac{f_w}{2L}) e_3 - \omega h_3 e_3\right)
$$

(30)

In engineering, the fault function $f_a$ is bounded, that is,

$$
[\Delta \psi_{rd}] \leq N_1, [\Delta \psi_{rq}] \leq N_2, \left|T_L - \frac{f_w}{2L}\right| \leq N_3, \text{ where, } N_1, N_2, N_3 \text{ are the boundary values. If } H \text{ satisfies } h_1 \geq N_2 \geq |\Delta \psi_{rq}|, h_2 \geq N_1 \geq |\Delta \psi_{rd}|, h_3 \geq \frac{n_p N_3}{J} \geq \frac{n_p}{J} \left(T_L - \frac{f_w}{2L}\right), \text{ then } V \leq 0.
$$

Therefore, the stability and convergence of the composite SMO is guaranteed. When the composite SMO is stable, the observed value will converge to the actual value.

**B. Expression of Composite Discrete Time SMO**
Since the proposed PSFC is computed at discrete instants, it is necessary to deduce the discrete expression of the composite SMO. If the sampling period is short enough, the composite discrete time SMO can be expressed by (31) according to (26).

\[
\begin{aligned}
\psi_a(k+1) &= \left(1-\frac{R}{L}T_s\right)\psi_a(k) + \omega(k)T_s\psi_q(k) + T_s u_d(k) \\
&\quad + \frac{-T_s}{L}\psi_y + \omega(k)T_s e_2(k) + h_1\omega(k)T_s \text{sgn}(e_1(k)) \\
\psi_q(k+1) &= \left(1-\frac{R}{L}T_s\right)\psi_q(k) - \omega(k)T_s\psi_y(k) + T_s u_q(k) \\
&\quad - \omega(k)T_s e_1(k) + h_2\omega(k)T_s \text{sgn}(e_2(k)) \\
\dot{\omega}(k+1) &= \dot{\omega}(k) + \frac{3n_p^2\psi_{ro}T_s}{2JL} - \psi_y(k) + h_3\omega(k)T_s \text{sgn}(e_3(k)) \\
\end{aligned}
\]

(31)

C. Estimation of Flux Linkage Parameter Perturbation Rate, Rotor Position Error, Equivalent Disturbance and Load Torque

According to (27), when the system reaches the sliding mode surface, that is \( \text{det}J = e = 0 \), the discrete form of fault function is obtained as follows,

\[
Df_a = \omega(k)H \text{sgn}(e(k))
\]

(32)

From (32), the estimated load torque and new flux-linkage components are obtained.

\[
\begin{aligned}
\Delta\psi_{rd} &= -h_2 \text{sgn}(e_2(k)) \\
\Delta\psi_{rq} &= h_1 \text{sgn}(e_1(k)) \\
\dot{\hat{T}}_L &= \frac{j\omega(k)}{n_p} h_3 \text{sgn}(e_3(k)) + \frac{\dot{\omega}}{2L}
\end{aligned}
\]

(33)

From (12), the equivalent disturbance is expressed as,

\[
\dot{\hat{f}}_o = 3n_p \left[\psi_{ro}\Delta\psi_{rq} + \Delta\psi_{rd}\psi_q(k) + \Delta\psi_{rd}\Delta\psi_{rq}\right]
\]

(34)

In order to eliminate the chattering of the sign function, the sign function is replaced with a hyperbolic tangent function with smooth continuity. The hyperbolic tangent function is defined as,

\[
\text{sgn}(v) = \tanh(v) = \frac{e^{\rho v} - 1}{e^{\rho v} + 1}
\]

(35)

where, \( \rho \) is a coefficient of regulation, and must be greater than zero.

According to (33) and Fig. 1, we can deduce the following equations for the rotor position error and PM flux linkage parameter.

\[
\Delta\hat{\theta} = \tan^{-1}\left(\frac{\Delta\psi_{rq}}{\psi_{ro} - |\Delta\psi_{rd}|}\right)
\]

(36)

\[
\psi_{e} = \frac{\Delta\psi_{rq}}{\sin(\Delta\hat{\theta})}
\]

(37)

VI. SIMULATIONS

The parameters of PMSM used in the simulation are shown in tables I. The sampling frequencies for current control loop and speed control loop are 10kHz and 1kHz, respectively; the proposed composite discrete time SMO parameters are \( h_1 = 2.5 \), \( h_2 = 1.5 \), \( h_3 = 50 \) and \( \rho = 2 \). At 0s, the speed reference steps from 0 to 800rad/s. And at 0.4 and 0.6s, the load torque is increased suddenly from no-load to rated load and decreased from rated load to no-load, respectively.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rated power</td>
<td>125kW</td>
</tr>
<tr>
<td>Rated speed</td>
<td>2000r/min</td>
</tr>
<tr>
<td>Rate torque</td>
<td>600N.m</td>
</tr>
<tr>
<td>Stator phase resistance(Ω)</td>
<td>0.02Ω</td>
</tr>
<tr>
<td>Number of pole pairs (n_p)</td>
<td>4</td>
</tr>
<tr>
<td>Inductances(L)</td>
<td>1mH</td>
</tr>
<tr>
<td>Flux linkage of PM (Ψ_ro)</td>
<td>0.892Wb</td>
</tr>
<tr>
<td>Rotational inertia (J)</td>
<td>1.57kg.m²</td>
</tr>
<tr>
<td>Type of magnet</td>
<td>NdFeB</td>
</tr>
<tr>
<td>Magnet coercivity</td>
<td>889kA/m</td>
</tr>
<tr>
<td>Operating temperature</td>
<td>20°C</td>
</tr>
</tbody>
</table>

A. Simulation for PMSM under flux linkage parameter mismatch(\( \lambda = 0.5 \))

In this simulation, the control performance comparison between conventional PCC and proposed PSFC under flux linkage parameter mismatch are investigated. The simulation results of the conventional PCC and the proposed PSFC are shown in Fig. 6 and Fig. 7, respectively.
Fig. 6. Simulation results of the conventional PCC. (a) the phase current, speed and torque. (b) d- and q-axis current.

From Fig. 6, it can be seen that the q-axis current response is larger than the current reference in the transient process. In addition, an apparent static error between q-axis current response and the current reference can be observed. According to the simulation results, it can be observed that flux linkage parameters mismatch has effect on current response in conventional PCC method. Compared with the conventional PCC method, the proposed PSFC method can achieve a lowest level of torque ripple as shown in Fig. 7(a). The reason is that the composite discrete time SMO employed in the proposed PSFC can significantly suppress the flux linkage parameter mismatch.

Fig. 7. Simulation results of the proposed PSFC. (a) the phase current, speed and torque. (b) d- and q-axis stator flux linkage.

Fig. 8 depicts the three-dimensional rotor flux trajectories of the conventional PCC and proposed PSFC under flux linkage parameter mismatch. The stator flux linkage error of conventional PCC and proposed PSFC are 3.4% and 1.5%, respectively. The static error of q-axis current in Fig. 6(b), is responsible for the large flux linkage error in Fig. 8(a). While in the proposed PSFC, the flux linkage error is drastically reduced for the reason that it can track the stator flux reference accurately. The frequency spectra of the conventional PCC and proposed PSFC under rated load conditions are illustrated in Fig. 9. With Fourier analysis, the stator current THD of conventional PCC under flux linkage parameter mismatch is 10.96%. While, it is reduced to 7.91% when the proposed PSFC is applied. The torque ripple decreases from 5.5% to 4.4%.

Fig. 8. The three-dimensional rotor flux trajectories. (a) Conventional PCC. (b) Proposed PSFC.

Fig. 10 shows the reference and estimated values of flux linkage. According to Eq. (27), the error equation of the composite discrete time SMO is based on d- and q-axis current. In the process of motor start-up, the d- and q-axis current are not stable, and the observed values of d- and q-axis current deviate greatly from the actual values. Therefore, there is a large estimation error in the initial load torque observation.
The results reflect that the proposed composite discrete time SMO can accurately estimate the flux linkage parameter perturbation rate, rotor position error, disturbance, and load torque when the motor runs to steady state.

![Image](image1.png)

**Fig. 9.** The frequency spectra of the stator current $i_a$ at rated load. (a) Conventional PCC. (b) Proposed PSFC.

![Image](image2.png)

![Image](image3.png)

![Image](image4.png)

![Image](image5.png)

**Fig. 10.** Simulation results of the reference and estimated values under flux linkage parameter mismatch ($\lambda = 0.5$). (a) Flux linkage parameter perturbation rate. (b) Rotor position error. (c) Disturbance. (d) Load torque.

**B. Simulation for PMSM under flux linkage parameter mismatch ($\lambda = 0.5$) and rotor position error ($\Delta \theta = -\pi/36$)**

Fig. 11 and Fig. 12 show the simulated results of conventional PCC and proposed PSFC under flux linkage parameter mismatch and rotor position error. The steady-state error exists in the q-axis current when taking the conventional PCC method. The reason is that the conventional PCC must rely on the precise mathematical model of the motor. From Fig. 12(b), it can be seen that the proposed PSFC method can exactly track stator flux linkage references under the flux linkage parameter mismatch and rotor position error. Moreover, it also can be seen that the torque ripple and stator flux linkage error are effectively suppressed.
Fig. 11. Simulation results of the conventional PCC. (a) the phase current, speed and torque. (b) the d-and q-axis current.

Fig. 13 depicts the three-dimensional rotor flux trajectories of the conventional PCC and proposed PSFC under the flux linkage parameter mismatch and rotor position error. The stator flux linkage error of conventional PCC and proposed PSFC are 3.2% and 1.8%, respectively. It can be observed that the PSFC method has satisfying steady-state performance (smaller α-β stator flux linkage error) compared with the conventional PCC method. The frequency spectra of the conventional PCC and proposed PSFC under flux linkage parameter mismatch and rotor position error are illustrated in Fig. 14. Compared to the conventional PCC, the stator current THD of proposed PSFC decreases from 7.99% to 7.42% under flux linkage parameter mismatch and rotor position error. The peak-to-peak torque ripple decreases from 5.4% to 4.5%, while the tracking time of the two control methods is almost the same, that’s about 39ms. Fig. 15 shows reference and estimated values of flux linkage. It can be seen that the composite discrete time SMO based on stator flux state can simultaneously estimate the flux linkage parameter perturbation rate, rotor position error, disturbance, and load torque in real time.

Fig. 12. Simulation results of the proposed PSFC. (a) the phase current, speed and torque. (b) d-and q-axis stator flux linkage.

Fig. 13. The three-dimensional rotor flux trajectories. (a) Conventional PCC. (b) Proposed PSFC.

Fig. 14. The frequency spectra of the stator current $i_a$ under rated load. (a) Conventional PCC. (b) Proposed PSFC.
The per-unit (p.u.) values of 2.2kW PMSM parameters are consistent with the simulation models. The rotor position error is simulated by artificially adding an angle to the measurement result of the mechanical sensor. The start-up of the experiment platform is as follows: the 380V AC power is firstly provided to the load motor. Then, the load motor drive controller and the energy feedback unit are started simultaneously. The output torque of the load motor is set to zero initially. Finally, the DSP controller of the SPMSM is power on to start up the SPMSM.

VII. EXPERIMENTAL RESULTS

For the purpose of verifying the proposed PSFC algorithm, experiments were conducted at a 2.2kW SPMSM laboratory platform, as is shown in Fig. 16. It is composed of two motors (drive and load machines), which are controlled by TMS320LF2812 DSP and SV-DB100-1R5-2-1R, respectively. The load motor provides load torque. The energy feedback unit can feed back the electric energy to the power grid and avoid the energy loss caused by resistance heating. The sampling frequencies are the same as those of simulations.

Fig. 16. Experimental platform of SPMSM drive.
The experimental results of $\alpha$-$\beta$ stator flux linkage behaviors are shown in Fig. 17. In Fig. 17(a), it can be seen that the existence of flux linkage parameter mismatch leads to the $\alpha$-$\beta$ stator flux linkage tracking error when the conventional PCC method is applied. By contrast, the proposed PSFC method can improve the robustness against this factor in Fig. 17(b). Fig. 18 presents experimental results of the torque and stator current $i_a$. The stator current THD of conventional PCC and proposed PSFC under flux parameter mismatch are 11.56% and 8.32%, respectively. Compared with conventional PCC, the stator current THD of proposed PSFC is reduced by 3.24%. The torque ripple decreases from 5.7% to 4.5% when the proposed PSFC is applied.

B. Control performance comparison between Conventional PCC and Proposed PSFC under flux linkage parameter mismatch ($\lambda = 0.5$) and rotor position error ($\Delta \theta = -\pi/36$)

Experimental results of the conventional PCC with speed change step from 0.3 p.u. to 1.0 p.u. are shown in Fig. 19. It is found that the d-and q-axis current errors increase with the increasing of speed under flux linkage parameter mismatch and rotor position error, which clearly confirms that the current error is closely related to the operation state of the motor.

Fig. 19. Experimental results of the conventional PCC with speed change step under flux linkage parameter mismatch and rotor position error. (a) The phase current and speed. (b) d-and q-axis current.
proposed PSFC. While, the maximum and minimum errors are 3.8% and 2.8% when taking the conventional PCC. The flux linkage error variation amplitude of the proposed PSFC method is only 0.6%, which verifies the effectiveness of the proposed PSFC. The torque and stator current $i_a$ under flux linkage parameter mismatch and rotor position error are shown in Fig. 21. The stator current THD of proposed PSFC is 9.76%, the conventional PCC is 10.32%, and it is also lower than that of the conventional PCC. Compared with traditional PCC, the stator current THD of proposed PSFC is only reduced by 0.56% in the case of flux parameter mismatch and rotor position error, but the stator flux tracking accuracy is improved. Furthermore, the torque ripple is reduced from 5.3% to 4.7%.

**Fig. 20. Experimental results of the $\alpha$-$\beta$ stator flux linkage under flux linkage parameter mismatch ($\lambda = 0.5$) and rotor position error ($\Delta \theta = -\pi/36$). (a) Conventional PCC. (b) Proposed PSFC.**

**Fig. 21. Experimental results of the torque and stator current $i_a$ with rated load under flux linkage parameter mismatch ($\lambda = 0.5$) and rotor position error ($\Delta \theta = -\pi/36$). (a) Conventional PCC. (b) Proposed PSFC.**

**VIII. CONCLUSION**

In this paper, a novel PSFC method has been proposed for PMSM drive system, which can effectively enhance robustness against flux linkage parameter mismatch and rotor position error. Furthermore, a composite discrete time SMO based on stator flux state is designed to estimate the flux linkage parameter perturbation rate, rotor position error and load torque. The proposed PSFC method utilizes the estimated value of composite discrete time SMO to eliminate the influence of flux linkage parameter mismatch and rotor position error. The stator flux linkage value of the next time is used to replace the current stator flux linkage in PSFC to compensate for the influence of the one-step delay. Compared with the conventional PCC, the proposed PSFC method increases the tracking accuracy of the stator flux linkage and decreases the torque ripples under flux linkage parameter perturbation and rotor position error. Simulation and experimental results verify the effectiveness of the proposed PSFC method, which shows its superiority in control precision.
and disturbance rejection under flux linkage parameter mismatch and rotor position error, while achieving the merits of low stator current THD, low torque ripple and excellent steady-state performance.

REFERENCES


