

Power Angle Small Signal Stability Analysis of Grid-Forming Inverter with VSM Control

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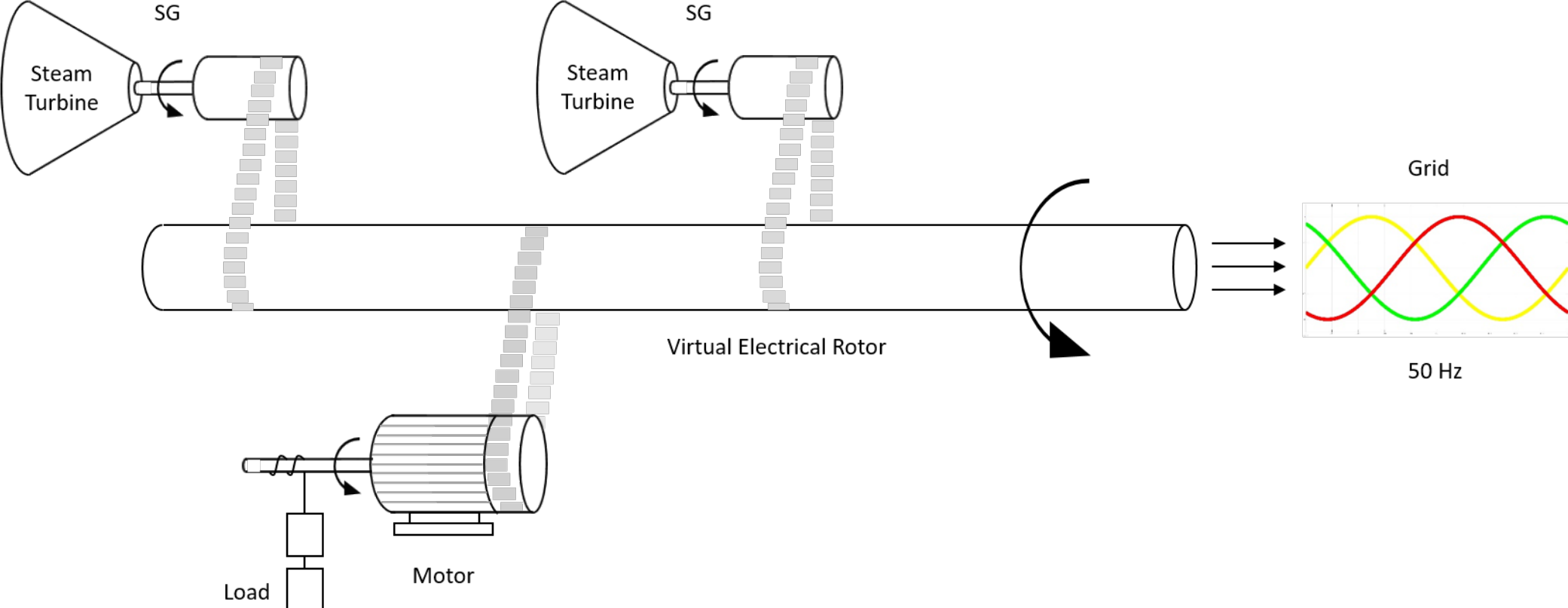
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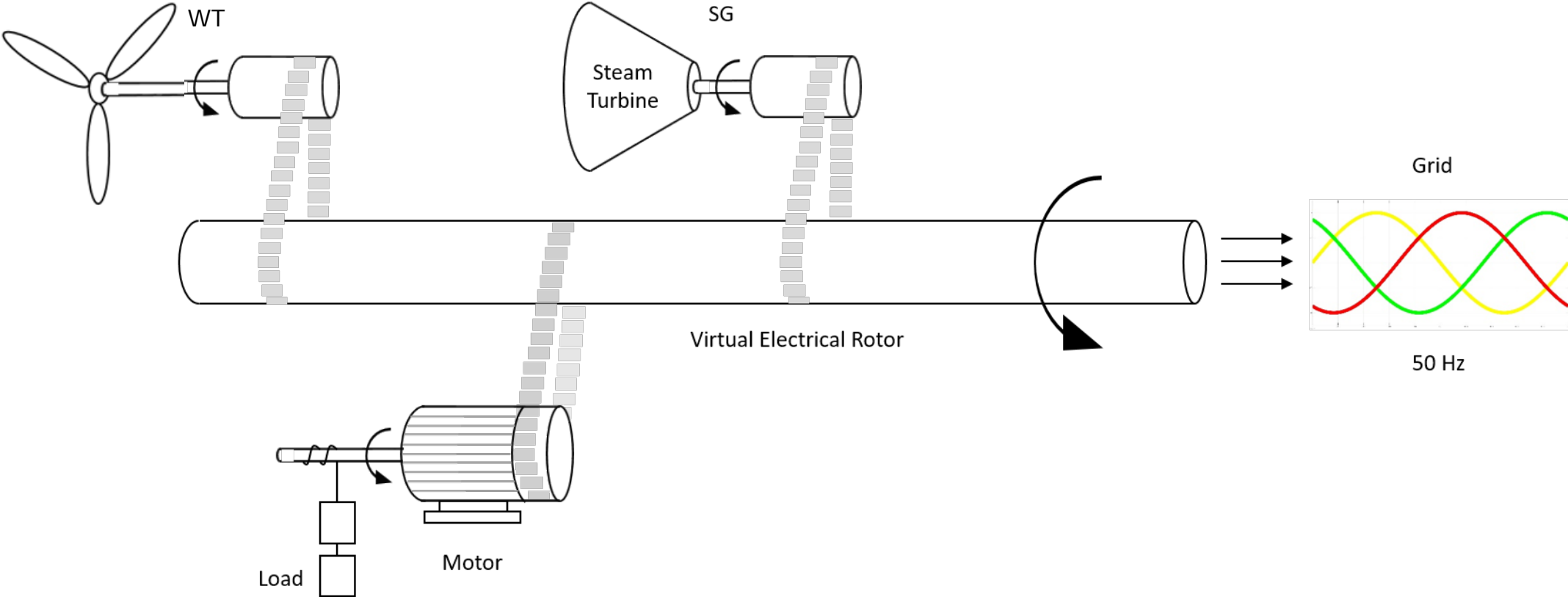
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$P = \frac{1}{2} \rho A v^3 C_p$
 $\int_a^b \epsilon \Theta + \Omega \int \delta e^{i\pi} = -1$
 $\infty = \{2.7182818284\}$
 χ^2
 Σ
 \approx
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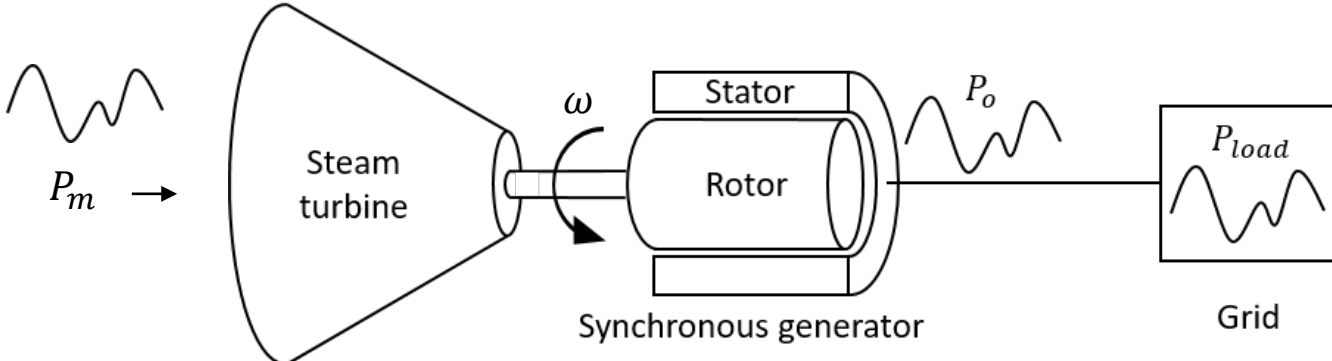
Power System Frequency Stability



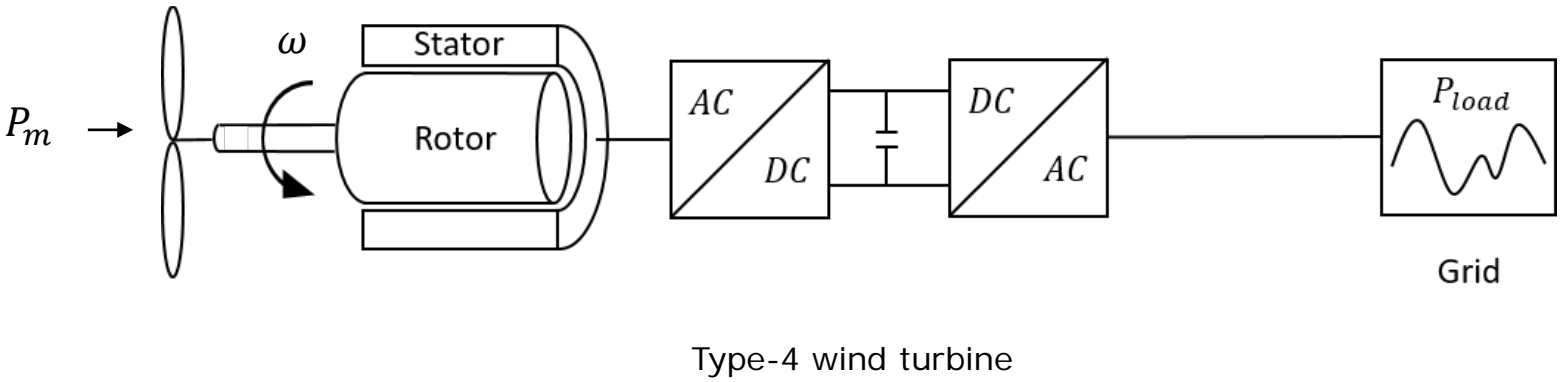
Power System Frequency Stability



Power System Frequency Stability

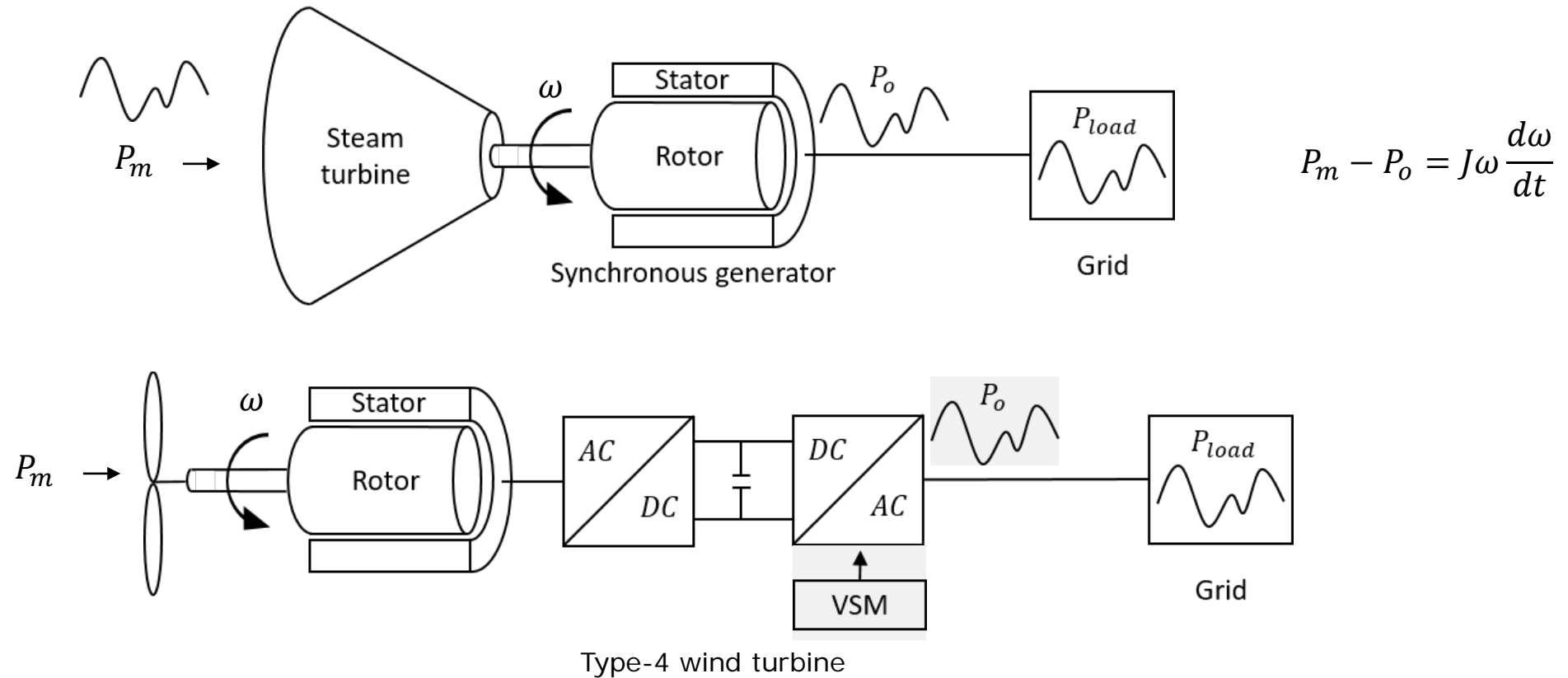


$$P_m - P_o = J\omega \frac{d\omega}{dt}$$



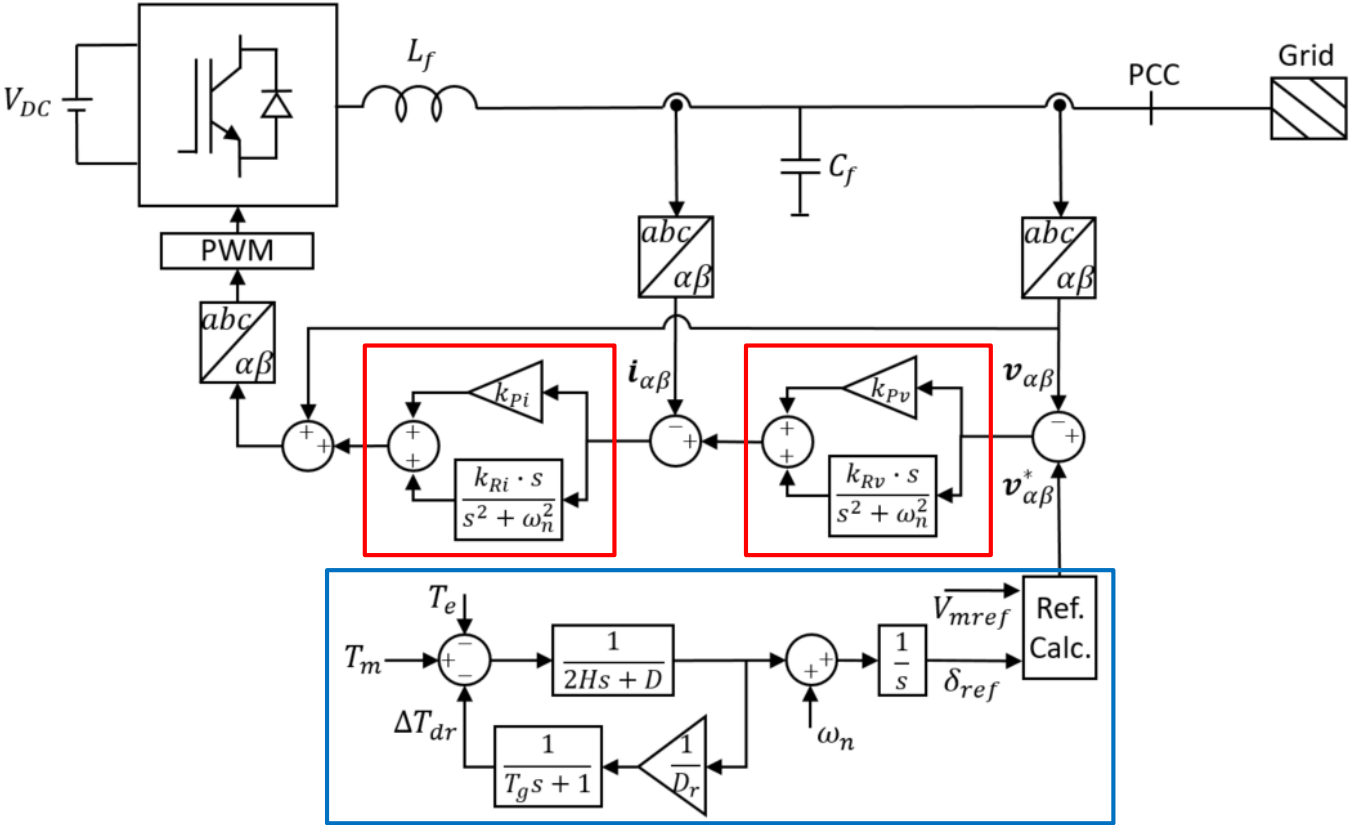
Virtual Synchronous Machine (VSM) Control

- A control scheme for a converter to enable renewable power sources to behave as a synchronous machine (SM) by adding the model and control of an SM within the control scheme;



Motivation

A VSM Control Scheme for WTs



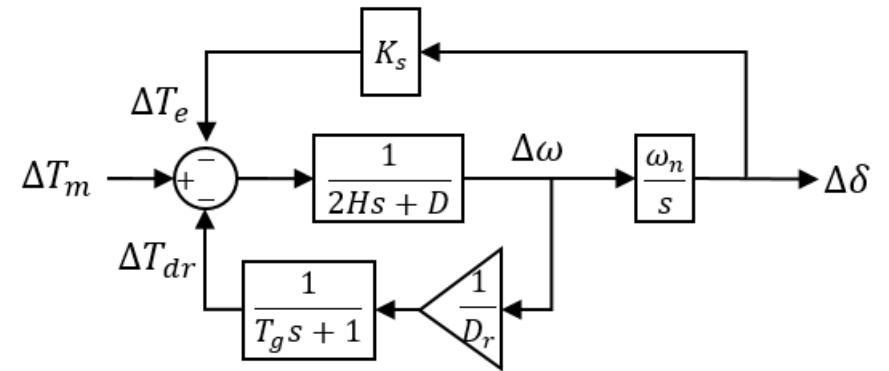
Power Angle Small Signal Stability

- Focusing on the power loop while idealizing inner voltage and current loops;
- State space representation and block diagram of an inverter connected to an infinite bus;
- Influence of parameters on the stability by analyzing eigenvalue trajectories;

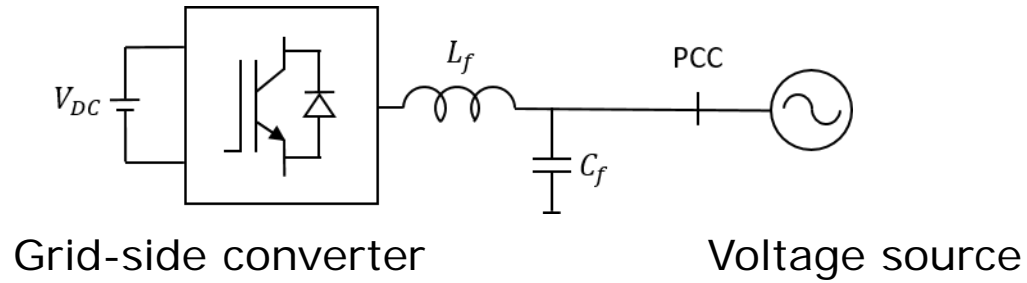
Power Angle Small Signal Stability (PAS) Model

$$\frac{d}{dt} \begin{bmatrix} \Delta\omega \\ \Delta\delta \\ \Delta T_{dr} \end{bmatrix} = \begin{bmatrix} -\frac{D}{2H} & -\frac{K_s}{2H} & -\frac{1}{2H} \\ \omega_n & 0 & 0 \\ \frac{1}{T_g D_r} & 0 & -\frac{1}{T_g} \end{bmatrix} \begin{bmatrix} \Delta\omega \\ \Delta\delta \\ \Delta T_{dr} \end{bmatrix} + \begin{bmatrix} \frac{1}{2H} \\ 0 \\ 0 \end{bmatrix} \Delta T_m$$

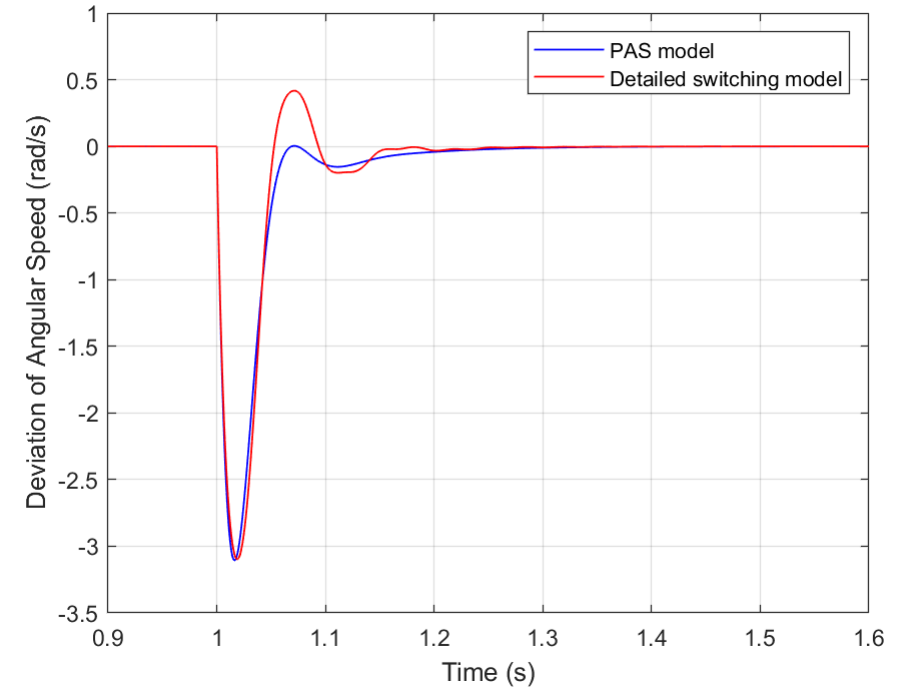
$$K_s = \frac{E'E_b}{X} \cos \delta_0$$



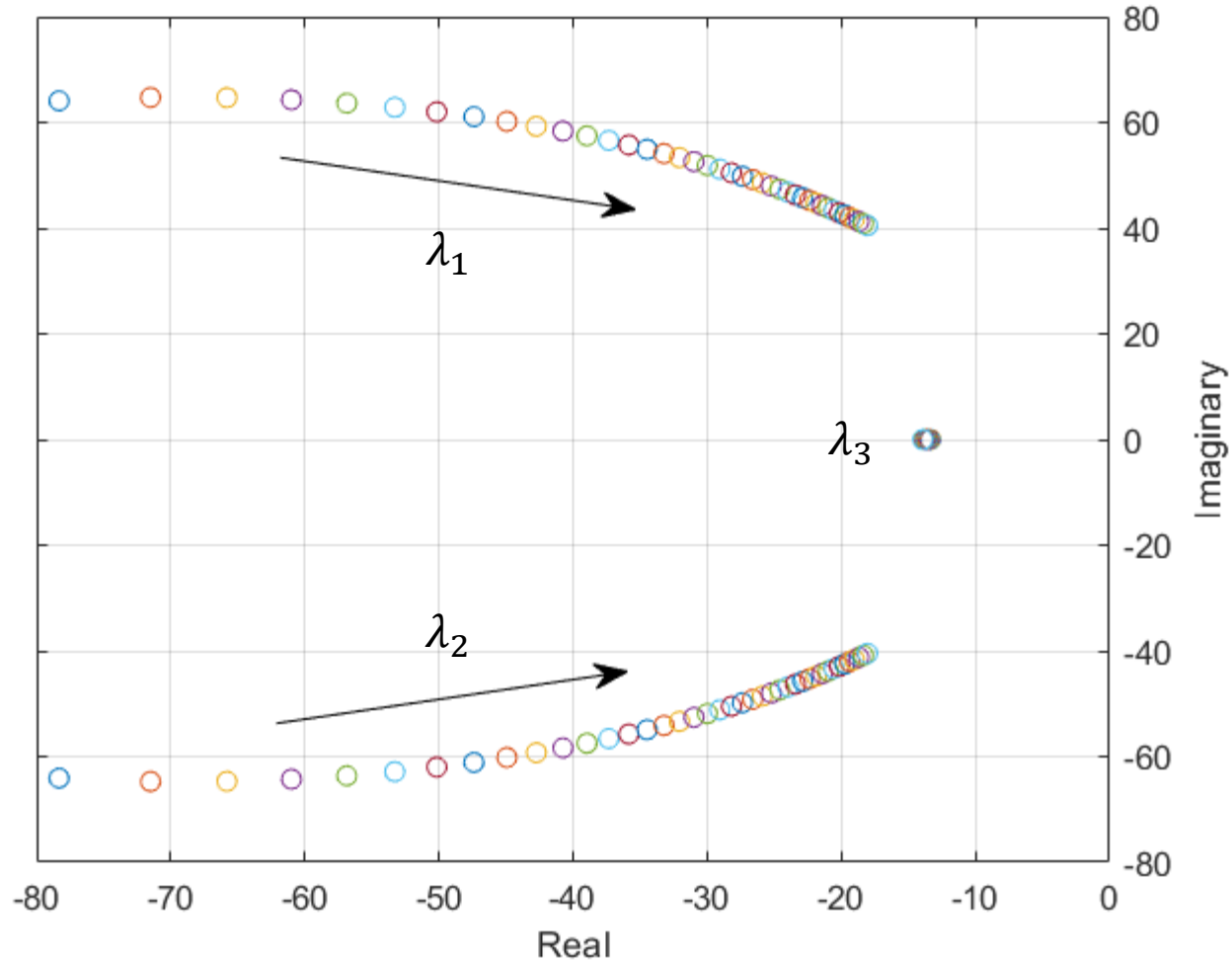
Verification



- $t = 1s$, T_m is dropped by 0.5 pu, or P_m is dropped by 5 kw

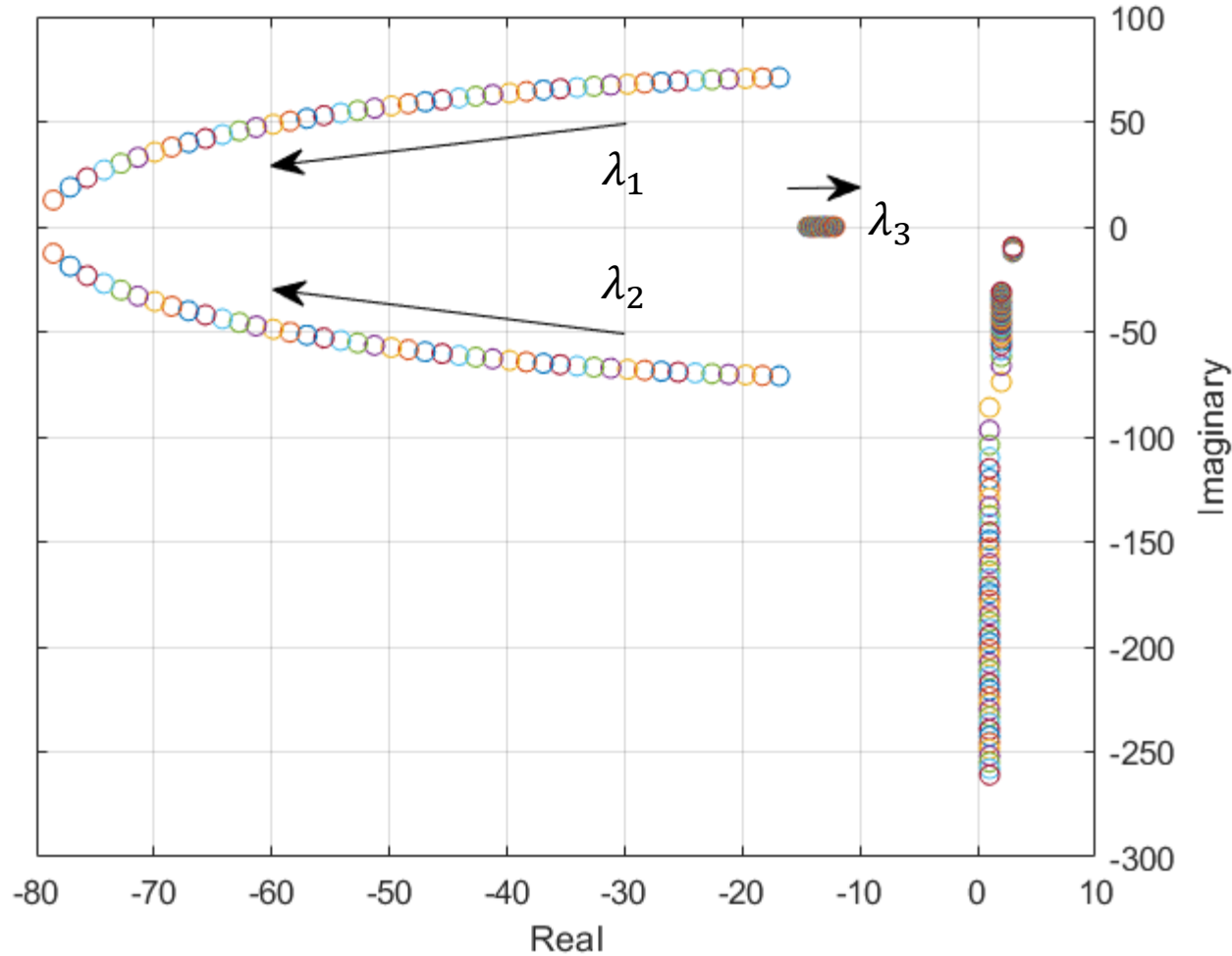


Parameter Design -- H



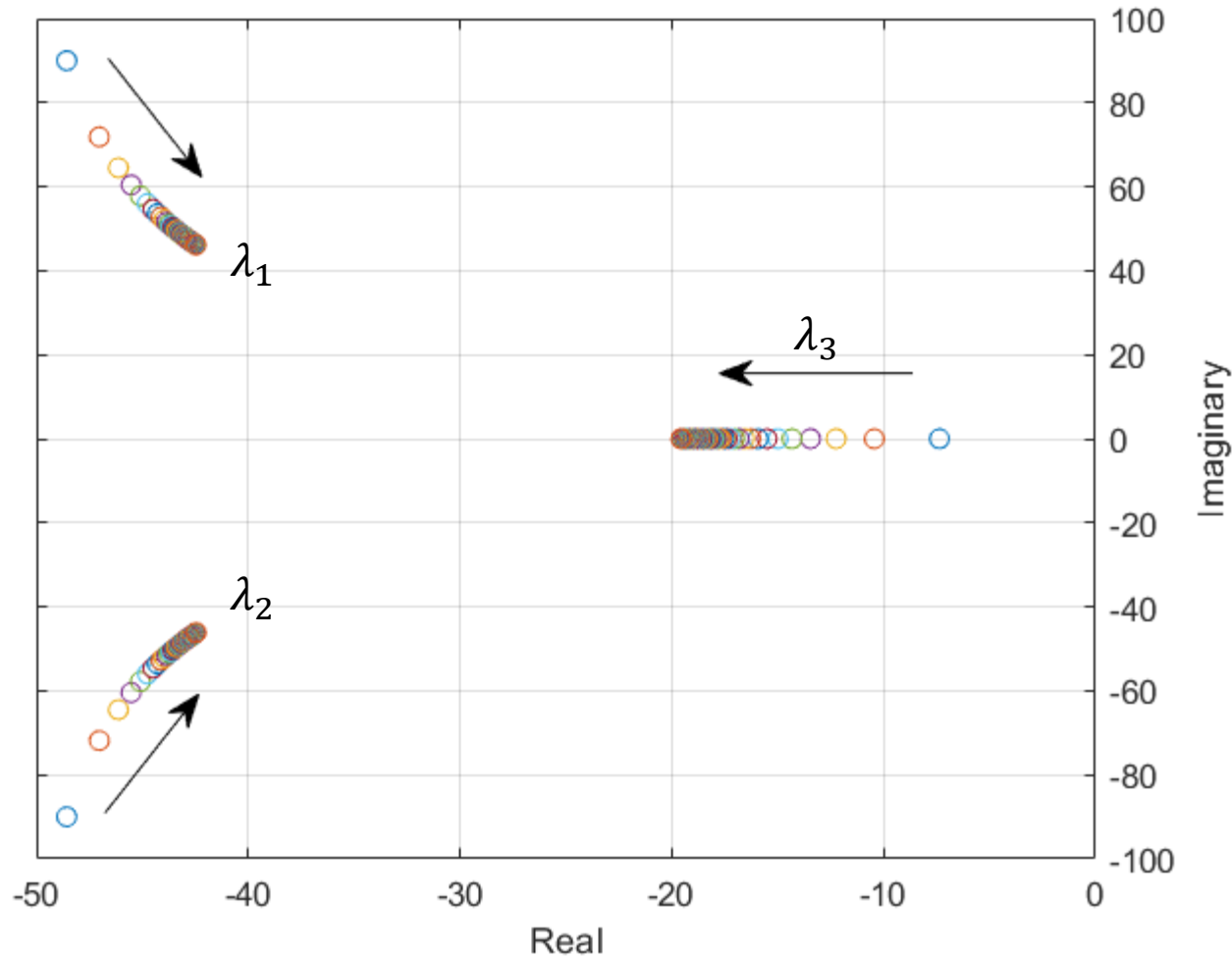
- 0.1 ~ 0.5;
- Little influence on λ_3 ;
- Stability margin reduced by increasing H ;
- A larger H is better for inertia response;
- A compromise;
- Exact value also depends on grid code requirements and converter rating;

Parameter Design -- D



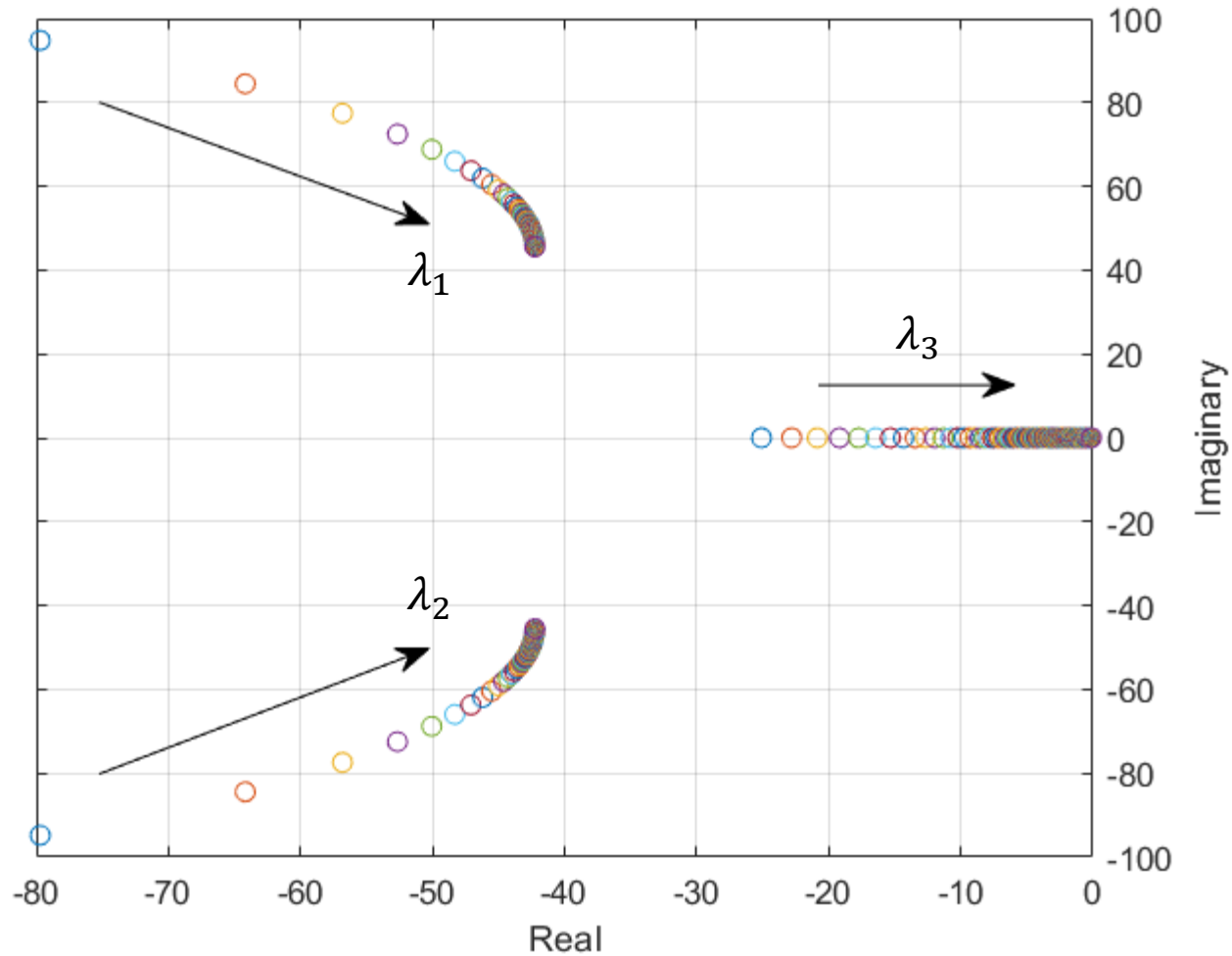
- 10~53: stable, 54~100: unstable;
- Little influence on λ_3 ;
- Stability margin improved by increasing D in the stable range;
- Positive effects of a smaller D ;
- A trade-off;

Parameter Design -- D_r



- 1% ~ 100%;
- Much influence on λ_3 ;
- Stability improved by increasing D_r ;
- Constraint and most likely determined by grid code requirements, converter rating and capacity of energy storage;

Parameter Design -- T_g



- 0.01 ~ 10;
- Much influence on λ_3 ;
- Stability is worse when increasing T_g ;

Conclusions & Future Work

- Power angle small signal stability (PAS) is proposed as a simpler way of analyzing the small signal stability of VSM-controlled grid-forming inverters;
 - Helpful for analyzing the rotor angle small signal stability of a big power system with large share of converter-interfaced renewable power sources;
 - A larger inertia constant H or damping coefficient D reduces the stability margin, but enhances the inertial response and frequency control capability;
 - A larger droop D_r or a smaller response time T_g helps improving the stability;
-
- ❑ Overall and systematic design of all parameters simultaneously considering practical constraints;
 - ❑ What is the optimal or acceptable power response from a non-synchronous power source for fast frequency regulation?

Thank you !

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