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1 Performance analysis of a cascade high temperature heat pump using R245fa and
2 BY-3 as working fluid

3 Xuelian Ma^a, Yufeng Zhang^a, Lei Fang^b,

4 Xiaohui Yu^a, Xiaoqiong Li^a, Ying Sheng^{a,*}, Yan Zhang^c,

5 ^a School of Environmental Science and Engineering, Tianjin University, Tianjin, 300072, PR China

6 ^b International Centre for Indoor Environment and Energy, Department of Civil Engineering, Technical University of
7 Denmark, Lyngby 2800, Denmark

8 ^c School of Architecture, Tianjin University, Tianjin, 300072, PR China.

9

10 **ABSTRACT:** A high temperature cascade heat pump (HTCHP) using a
11 near-zeotropic mixture named BY-3 as the working fluid in the low-stage refrigerant
12 cycle and R245fa as working fluid in the high-stage refrigerant cycle was proposed in
13 this study. Several experiments were carried out to investigate the performance of the
14 HTCHP at the evaporating temperature from 40°C to 60°C and the water outlet
15 temperature on the condensing unit of the high-stage cycle can reach 142°C with the
16 coefficient of performance (COP) of 1.72. The results showed that BY-3 was feasible
17 to be used in the low-stage cycle. A numerical model of the HTCHP was proposed
18 and validated in this study to evaluate its performance. The comparison between the
19 experimental results and the simulated results showed that the HTCHP system using
20 BY-3 and R245fa can product hot water at 142°C with good performance and the

* Corresponding author: Ying Sheng

E-mail: ysheng@tju.edu.cn

Address: No. 135 Yaguan Road, Jinnan District, Tianjin, China.

21 temperature lift of the HTCHP can reach 100°C.

22 **Keywords:** High-temperature Cascade Heat Pump; Modeling Analysis;

23 Experimental Verification; Performance Evaluation

Nomenclature	
COP	Coefficient of performance
EEV	Electronic expansion valve
HX	Heat exchanger
C _p	Specific heat(kJ/kg·K)
m	Mass flow rate(kg/h)
P	Power consumption(kW)
h	Enthalpy(kJ/kg)
T	Temperature(°C)
Q	Capacity(kW)
W	Power input(kW)
HTCHP	High temperature cascade heat pump
P _c	critical pressure(bar)
P _{theo}	Theoretical power(kW)
P _{in}	Input power (kW)
GWP	Global Warming Potential
ODP	Ozone Depleting Potential
r	Latent heat(kW/kg)
Ø	EEV opening degree
Subscripts	
w	water
v	vapor
l	liquid
L	Low –stage refrigerant cycle
H	High-stage refrigerant cycle
cond	condenser
evap	evaporator
ref	refrigerant
t	total
out	outlet
in	inlet
Greek symbols	
ρ	density(kg/m ³)
	acentric factor
η _s	volumetric efficiency

η_m	friction efficiency
η_e	motor efficiency
1,2,3,4,5,6,7,8,9,10	state point

24 **1. Introduction**

25 Environmental concerns such as global warming, ozone depletion, global climate
 26 change and air pollution have become worldwide issues in the past several decades
 27 mainly due to anthropogenic activities such as vehicle emission, pollutions from
 28 power plants, steel mills, and many other industrial sectors^{[1][2]}. The use of substantial
 29 fossil fuels contributes this the most, especially the fuel consumption on the industrial
 30 aspect. It was reported that the energy was accounted for more than 70% of China's
 31 total energy consumption in 2010. In the U.S., the industrial sector accounted for
 32 about one third of the total energy consumed and it was estimated that 20 to 50% of
 33 industrial energy input was lost as waste heat in different forms^[3]. Consequently, new
 34 technologies that can improve energy efficiency and recover waste heat losses provide
 35 an attractive challenge for an emission-free and less-costly energy resource.

36 The cascade refrigeration system composed of two independent refrigerant
 37 cycles was first introduced in 1930s to overcome the disadvantage such as high
 38 pressure ratio and low COP of single-stage refrigeration in low-temperature
 39 refrigeration systems in the range from -30°C to -100°C^{[4][5]}. Jung et al. drew the
 40 conclusion that the cascade heat pump was much more competitive than single-stage
 41 heat pump by studying a cascade multifunctional heat pump using R410A and R134a
 42 as working fluids experimentally^[6].

43 Many researches have been done to investigate the performance of the cascade
 44 heat pump systems. Wang et al. performed series of experiments to analyze the

45 impact of different operation parameters on the performance of cascade refrigeration
46 and concluded that the NH₃/CO₂ cascade was competitive in low temperature
47 applications [7]. Alberto et al. designed and built a cascade refrigeration system with
48 NH₃ and CO₂ to study the system performance and the results accords with the trends
49 obtained from the theoretical researches published in technical literature [8]. Qu et al.
50 presented a control method of air source heat pump and verified it experimentally and
51 the experimental results showed that the control strategy could realize the control of
52 evaporating temperature and intermediate pressure with high accuracy and sensitivity
53 to adjust the system load variation [9]. Park^[10] set up a mathematical model of
54 R134a/R410A cascade heat pump to predict the optimal intermediate temperature to
55 make sure that the system can run with higher COP based on thermodynamic laws
56 and thermodynamic properties of refrigerants. Kim^[11] verified the optimal
57 intermediate temperature by experimental investigation conducted on an air to water
58 heat pump, and the numerical model can predict the experimental results with high
59 accuracy. Hansaem^[12] et.al studied the performance of a cascade heat pump system by
60 quasi-steady state analysis and Cho^[13] et al. investigated a two-stage CO₂ system in
61 cooling mode operation.

62 As a main contributor to productivity and employment in China, the petroleum
63 refining industry consumed approximately 15%^[14] of industrial fuel oil and 10% of
64 industrial coal. During recent years, capacity expansion activities had been carried out
65 for lots of petroleum refining companies, but during the design and construction, the
66 heating capacity between the new and old facilities was not integrated well.
67 Accordingly, lots of low temperature waste heating was produced. Take a a 10
68 million-ton refinery, the low temperature waste heat was about $1000 \times 10^4 \sim 12000 \times$
69 10^4 kcal / h, the current comprehensive utilization efficiency was only 30% to 50%,

70 through comprehensive optimization of low temperature heat, the comprehensive
71 utilization rate could increase to about 70%. In general, its energy saving potential
72 accounted for 10% to 20% of the total energy saving potential of the refinery.

73 Although a lot of manpower and material resources were invested to carry on the
74 transformation to the low temperature waste heating (below 50 °C) use system during
75 China's "Eleventh Five-Year" period, but depending on the energy-intensive
76 characteristic, more cost-effective investments for energy system optimization may be
77 a useful strategy to improve the competitiveness of China's refining industry.

78 Based on the current situation of the petroleum refining industry, in this study, a
79 water source cascade heat pump system using a new binary near-zeotropic refrigerant
80 named BY-3^[15] and R245fa as working fluid in the low-stage and high-stage
81 refrigeration cycle, respectively, was studied numerically and experimentally. The
82 system was simulated at different water inlet temperature and the simulated results
83 were validated by the experimental results with high accuracy.

84 **2. Methodology**

85 2.1 Working principle of HTCHP system

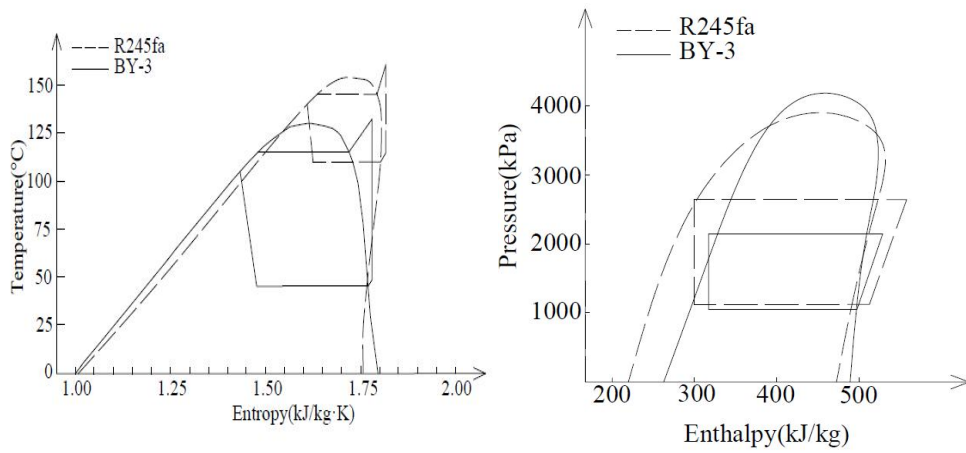
86 The working principle for the cascade heat pump system is:

- 87 a. For the low-stage refrigerant cycle, the new near-zeotropic mixture named
88 BY-3 absorbs heat in the evaporator while evaporating. The low pressure and
89 temperature BY-3 vapor comes out from the evaporator is then compressed in
90 the hermetic scroll compressor made by Danfoss into high pressure and
91 temperature vapor. The BY-3 vapor discharges from the low-stage cycle
92 compressor then releases heat in the low-stage cycle condenser and turns into

93 liquid with high pressure and temperature. Then the liquid goes into the EEV
94 of the low-stage cycle and changes to liquid with low pressure and
95 temperature, and then the liquid goes into the low-stage cycle evaporator to
96 finish the low-stage refrigerant cycle.

97 b. For the high-stage refrigerant cycle, the working fluid R245fa absorbs heat in
98 the evaporator while evaporating. The low pressure and temperature R245fa
99 vapor comes out from the evaporator is then compressed in the hermetic
100 scroll compressor made and modified by Danfoss into high pressure and
101 temperature vapor. The R245fa vapor discharges from the high-stage cycle
102 compressor then releases heat in the high-stage cycle condenser and turns
103 into liquid with high pressure and temperature. Then the liquid goes into the
104 EEV of the high-stage cycle and changes to liquid with low pressure and
105 temperature, and then the liquid goes into the high-stage cycle evaporator to
106 finish the high-stage refrigerant cycle.

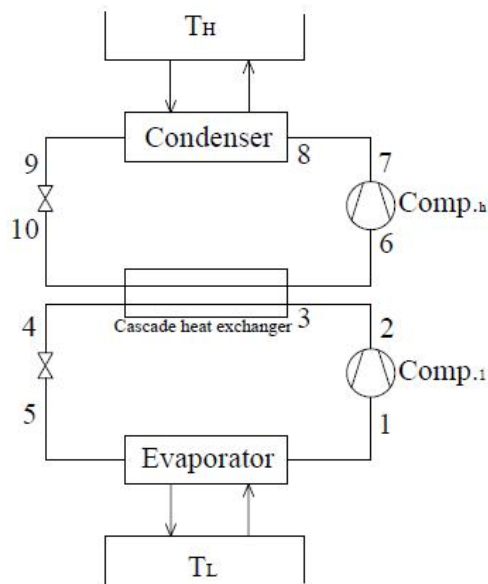
107 The P-h and T-s diagram of the cascade system are shown in **Fig.1** and the heat
108 flow of a cascade heat pump system is shown in **Fig. 2**.



109

110

Fig.1. P-h and T-s diagram of cascade cycle



111

112

Fig.2 Principle of Cascade heat pump system

113 2.2 Modeling

114 A new mathematical model is proposed to evaluate the system performance of
 115 the cascade high temperature heat pump. The model is based on the seven main parts
 116 of the cascade system: evaporator, cascade heat exchanger, condenser, high-stage and
 117 low-stage compressor, high-stage and low-stage EEV.

118 Some hypotheses are necessary to setup the system model:

- 119 (1) The refrigerants in the cascade heat pump are in steady state.
- 120 (2) Refrigerants are saturated at the outlet of the evaporator, the cascade heat
121 exchanger and the condenser.
- 122 (3) The heat dissipation from the cascade heat exchangers and pipes to
123 environment is negligible, i.e. the heat released from the low-temperature
124 water is totally transferred to the refrigerant in the low-stage refrigerant
125 cycle.
- 126 (4) The pressure loss in heat exchangers and the pipes is negligible.
- 127 (5) The compression in the compressors is isentropic.

128 According to the hypotheses mentioned above, the conservation of the mass and
129 energy formula of the refrigerant can be acquired as shown in **Eq.(1).**and **Eq.(2).**

$$130 \quad \sum_{in} m = \sum_{out} m \quad (1)$$

$$131 \quad Q - W + \sum_{in} mh - \sum_{out} mh = 0 \quad (2)$$

132 2.2.1 Evaporator in the low-stage cycle

133 According to the principle described above, the heat transfer in the low-stage
134 cycle can be described in:

135 Low temperature heat source side:

$$136 \quad Q_l = c_w m_{evap,w} (t_{evap,w,in} - t_{evap,w,out}) \quad (3)$$

137 Refrigerant side:

$$138 \quad Q_l = (h_5 - h_1) m_{l,ref}$$

139 (4)

140 According to **Eq. (3)** and **(4)**, the mass flow rate of refrigerant in the low-stage
 141 cycle can be described as:

$$142 \quad m_{l,ref} = \frac{Q_l}{h_5 - h_1} \quad (5)$$

143 The specific heat of water (C_w) in **Eq.3** is shown in **Eq.6**, and based on a
 144 regression analysis, the correlation coefficient can be 100% in high temperature zone
 145 of 60-145°C [16].

$$146 \quad C_w(t) = 4.20734 - 1.02 \times 10^{-3}t + 1.10155 \times 10^{-5}t^2 + 5.53737 \times 10^{-20}t^3 \quad (6)$$

147 To simply the calculation, the expression of C_w can be described as shown in
 148 **Eq.7**:

$$149 \quad C_w = \frac{C_w(t_{w,in}) + C_w(t_{w,out})}{2} \quad (7)$$

150 2.2.2 Hermetic scroll compressor

151 Hermetic scroll compressors were chosen in this paper due to the excellent
 152 properties such as simple structure, high reliability, low vibration, high efficiency, and
 153 low noise [17].

154 The input power of the compressor P_{in} in low-stage and high –stage refrigerant
 155 cycle is described in Eq.8 and 9:

$$156 \quad P_{in,l} = \frac{P_{theo,l}}{\eta_s \eta_e \eta_m} = \frac{m_{ref,l}(h_2 - h_1)}{\eta_s \eta_e \eta_m} \quad (8)$$

$$157 \quad P_{in,h} = \frac{P_{theo,h}}{\eta_s \eta_e \eta_m} = \frac{m_{ref,h}(h_7 - h_6)}{\eta_s \eta_e \eta_m} \quad (9)$$

158 Where h_1 and h_2 refers to the enthalpy of the refrigerant at the inlet and outlet of the
 159 low-stage cycle compressor, h_6 and h_7 refers to the enthalpy of the refrigerant at the

160 inlet and outlet of the high-stage cycle compressor and η_s , η_m and η_e refer to the
161 isentropic efficiency (refers to AHRI540-2004 standard rating condition), the
162 volumetric efficiency and the motor efficiency, and normally the values for fixed
163 speed scroll compressor are 0.7, 0.8 and 0.85, respectively.

164 2.2.3 Cascade heat exchanger

165 Condenser in the low-stage refrigerant cycle:

$$166 \quad Q_{\text{cond},l} = m_{l,\text{ref}}(h_3 - h_4) \quad (10)$$

167 Where h_3 and h_4 refers to the enthalpy at the inlet and outlet of the condenser in
168 the low-stage refrigerant cycle.

169 Evaporator in the high-stage refrigerant cycle:

$$170 \quad Q_{\text{evap},h} = m_{\text{ref},h}(h_{10} - h_6) \quad (11)$$

171 2.2.4 Condenser

172 Water side:

$$173 \quad Q_h = C_{\text{cond},w,h}(t_{\text{cond},w,\text{out},h} - t_{\text{cond},w,\text{in},h}) \quad (12)$$

174 Where Q_h , $C_{\text{cond},w,h}$, $t_{\text{cond},w,\text{out},h}$ and $t_{\text{cond},w,\text{in},h}$ refers to the heating capacity in the
175 high-stage refrigerant cycle, the specific heat of the water in the condenser in the
176 high-stage refrigerant cycle, the water temperature at the outlet and inlet of the
177 condenser in the high-stage refrigerant cycle, respectively.

178 Refrigerant side:

$$179 \quad Q_h = m_{\text{ref},h}(h_8 - h_9) \quad (13)$$

180 2.2.5 Electronic expansion valve

181 For the low-stage cycle, the refrigerant mass and enthalpy can be described in
182 Eq.13 and14.

$$183 \quad m_4 = m_5 = m_{l,ref} \quad (14)$$

$$184 \quad h_4 = h_5 \quad (15)$$

185 For the high-stage cycle, the refrigerant mass and enthalpy can be described in
186 Eq.13 and 14.

$$187 \quad m_9 = m_{10} = m_{h,ref} \quad (16)$$

$$188 \quad h_9 = h_{10} \quad (17)$$

189 According to the precious analysis, COP can be obtained as below.

$$190 \quad COP = \frac{Q_h}{P} = \frac{Q_h}{P_{in,l} + P_{in,h}} \quad (18)$$

191 **3. Test rig setup**

192 3.1 Refrigerant and test rig

193 Refrigerant is very important in the HTCHP system which can affect the
194 performance and the safe-operation, etc., and during the selection of the refrigerant
195 some rules need to be considered ^[18-20], such as eco-friendly, good at thermodynamics,
196 flammability and toxicity. According to these concerns, a new near-zeotropic mixture
197 named BY-3 was proposed as the working fluid in the low-stage refrigerant cycle, and
198 R245fa was proposed to use in the high-stage refrigerant cycle. The basic properties
199 for BY-3 and R245fa are shown in Table 1.The properties of the refrigerant in this
200 paper are using the data from the software NISTREFPROP9.1.

201 **Table 1**The properties of BY-3 and R245fa

Substance	T _c (°C)	P _c (MP _a)	ODP	GWP(100yr)	Security Level
BY-3	126.2	4.664	0.04	2100	A ^{a1b}
R245fa	154.01	3.65	0	950	B ^{a1b}

202 Note: a, According to TLV-TWA [21], while the refrigerant concentration is equal to or
203 less than 400*10⁻⁴%, it is non-toxic; b, There is no flame spreading in the air if the
204 refrigerant is tested under the condition of 102.3kPa and 21°C.

205 Based on the physical parameters of BY-3, a regression analysis was done and
206 shown in Eq.19-20. The analysis results suggested the correlation coefficients are 99.
207 87% and 99.89% for liquid and vapor, respectively.

$$208 \quad h_{l,BY3} = 9 \times 10^{-5}t^3 - 1.05 \times 10^{-2} \times t^2 + 2.552 \times t + 191.72 \quad (19)$$

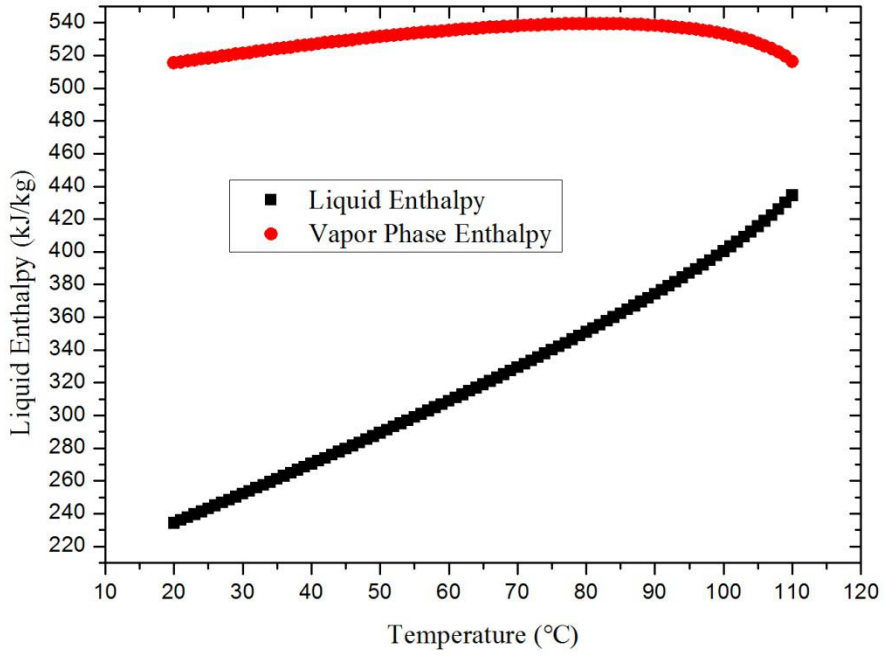
$$209 \quad h_{v,BY3} = -1 \times 10^{-4}t^3 + 1.74 \times 10^{-2}t^2 - 2.068 \times 10^{-1}t + 515.07 \quad (20)$$

210 A regression analysis was also done based on the physical parameters of R245fa
211 as shown in Eq.21-22. The analysis results suggest that the correlation coefficients are
212 99.88% and 99.92% for liquid and vapor, respectively.

$$213 \quad h_{l,R245fa} = 5 \times 10^{-5}t^3 - 1.17 \times 10^{-2} \times t^2 + 2.3858 \times t + 167.74 \quad (21)$$

$$214 \quad h_{v,R245fa} = -8 \times 10^{-5}t^3 + 2.14 \times 10^{-2}t^2 - 1.1363 \times 10^{-1}t + 451.47 \quad (22)$$

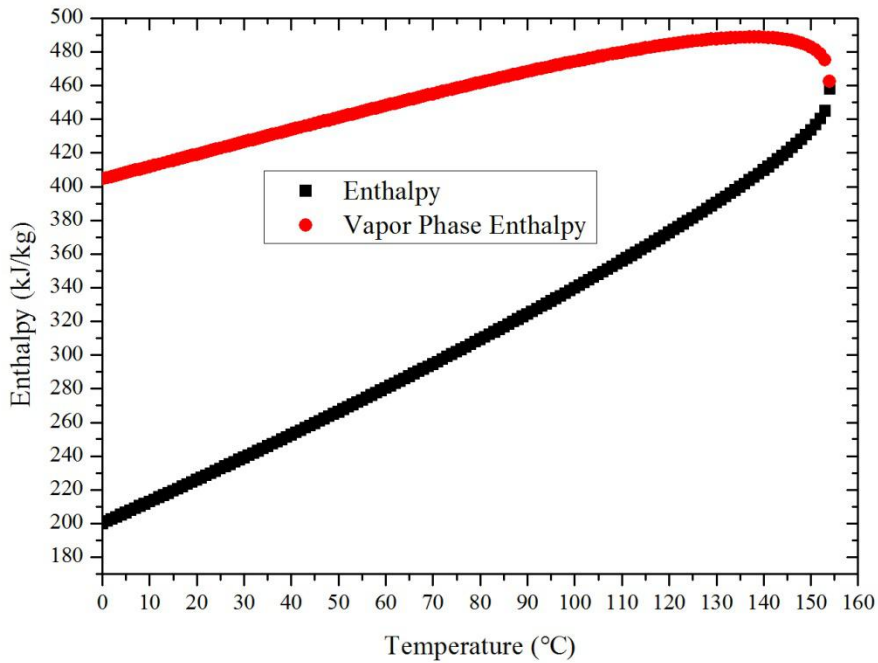
215 The t-h diagram of BY-3 and R245fa is shown in **Fig 3** and**4**.



216

217

Fig.3. t-h diagram of BY-3



218

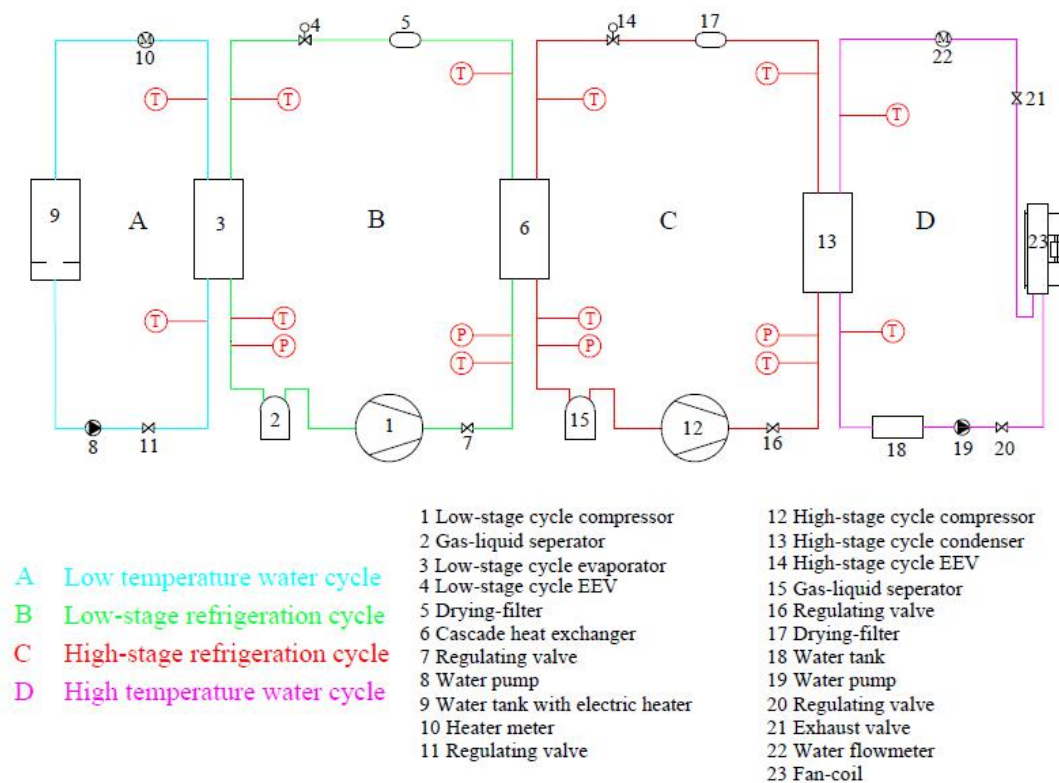
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Fig.4. t-h diagram of R245fa

220

Based on the theoretical analysis above, one test rig was designed in this research

221 to verify the performance of the HTCHP. The test rig was composed of three
 222 independent parts: the refrigerant cycle consisted of the low-stage refrigerant and the
 223 high-stage refrigerant cycle; a low-temperature water tank with an electric heater
 224 which can supply water at the constant temperature so that the evaporating
 225 temperature in the evaporator could be controlled and a hermetic high temperature
 226 water reservoir was used to support the high-temperature water cycle. The schematic
 227 of the HTCHP is shown in **Fig.5**.



228

229 **Fig.5.** Schematic diagram of the HTCHP test rig

230 The refrigerant liquid in the low-stage cycle absorbed heat from the
 231 low-temperature water and turned into vapor, and then the low temperature and
 232 pressure refrigerant vapor was compressed in the low-stage cycle compressor into
 233 high temperature and pressure vapor. The cascade heat exchanger of the refrigerant

234 cycle was a double-pipe heat exchanger so that the long flow path can make sure that
 235 the refrigerant in the low and high-stage cycle can change heat sufficiently. The low
 236 temperature and pressure refrigerant liquid (R245fa) in the high-stage cycle absorbed
 237 heat from the high temperature and pressure BY-3 vapor and then was compressed in
 238 the high-stage cycle compressor into high temperature and pressure vapor. And then
 239 the heat was transferred to the water in the fan coil. In order to reduce the heat
 240 emitting to the environment, all the pipes of the cascade system are packaged with
 241 thermal insulation material.

242 The compressors used in this research were made and modified by Danfoss. The
 243 specification of the compressors and heat exchangers is shown in **Table 2** and 3.

244 **Table2:** Parameters of the compressors used in the cascade experimental system

Unit	Model	Manufactur e	Rated Load Amps(A)	Cooling capacity(w) @ARI 50HZ	Power input(kW) @ARI 50HZ	Swept volume (cm3/rev)	Pressur e vessel code
BY-3&R245 fa Compressor	SH090A4AL C	Danfoss	14.3	22490	7.215	88.4	PED

245 **Table 3:** Parameters of the heat exchangers

Unit	Model	Design pressure(B ar)	Design temperature(°C)	Relative directions of fluids	Heat Exchang ed (kW)	Pressu re vessel code
evaporat or	CB60-26 M	40	-196.0/225.0	Countercurr ent	20	PED
Cascade heat exchang er	n/a	40	-196.0/225.0	Countercurr ent	25	PED
Condens	CB60-32	40	-196.0/225.0	Countercurr	36	PED

264 be adjusted since that the high-stage compressor worked in a high suction temperature
 265 which will cause the unexpected compressor motor trapped. Normally, the set for
 266 motor protector is 85-115 °C ,which means if the suction temperature is higher than
 267 115 °C ,the protector will be trapped and the compressor stops working, and when the
 268 motor temperature is lower than 85 °C , the circuit will become close again so that the
 269 compressor can be restarted. In this paper, the protector parameter of the high-stage
 270 cycle was changed to 115-145 °C according to the working condition.

271 In order to adapt the high discharge temperature in the high-stage cycle, a
 272 high-temperature applicative lubricant was used in this research.

273 **Table 4** The properties of lubricant used in high-stage cycle

Item	Kinematic viscosity(40°C)	Pour point	Water content	Density (15°C)	Specific Resistance
unit	mm ² /s	°C	ppm	g/m ³	T Ω m
specification	61.2-74.8	-30	200	0.929-0.945	0.01

274 3.3 Measurement equipment and data acquisition

275 In this study, the signal of the mass flowmeter, the temperature and the
 276 pressure were all sent to Agilent 34972A data acquisition machine for further
 277 analysis. The values of power consumption and heat meter were recorded in the
 278 same time with the temperatures. The parameters of the measurement equipment
 279 are shown in **Table 5** as follows:

280 **Table5:** Parameters of the measurement equipment used in the cascade experimental system

Part	model	accuracy	comment
Pt100	n/a	+/-0.3°C	n/a

Pressure transducer(suction)	HSTL-800A,0-1.5MPa	0.2%F.S	Beijing Zhong xing Ltd. corp
Pressure transducer(discharge)	HSTL-800A,0-5.0MPa	0.2%F.S	Beijing Zhong xing Ltd. corp
Heat meter	IC-3	+/-2%	Yidu
Mass flowmeter	HH-LUCB-32	1.0 grade	Huai an
Power meter	DED194E-9SYK02	+/(0.5%+1)	Shanghai Dingde
Data acquisition	34972A	n/a	Agilent

281 3.4 Measurement Uncertainty

282 The uncertainty evaluation is necessary in order to evaluate the test data more
283 effectively. Normally, uncertainty is composed of Uncertainty Type A and Uncertainty
284 Type B [22]. And the uncertainty discussed in this paper is relative overall uncertainty.
285 The basic equation of uncertainty analysis [23] is shown in Eq. (19).

$$286 \quad \delta R = \left\{ \sum_{i=1}^N \left(\frac{\delta R}{\delta X_i} \delta X_i \right)^2 \right\}^{1/2} \quad (19)$$

287 Where X_i , δX_i and δR refers to the measurement value, the uncertainty of X_i
288 and the overall uncertainty, respectively.

289 The maximum relative overall uncertainties of COP and heating capacity are
290 4.15% and 4.30%, respectively.

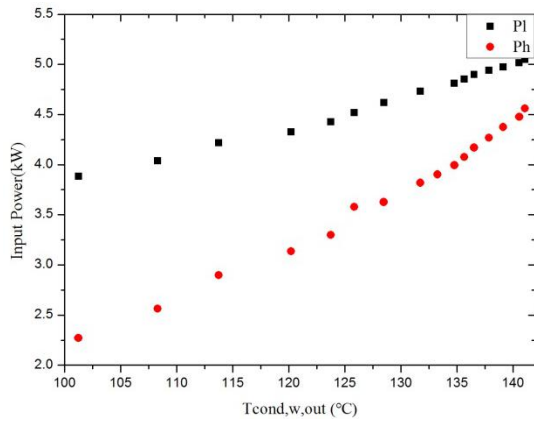
291 4. Results and discussion

292 4.1 Experimental results and discussion

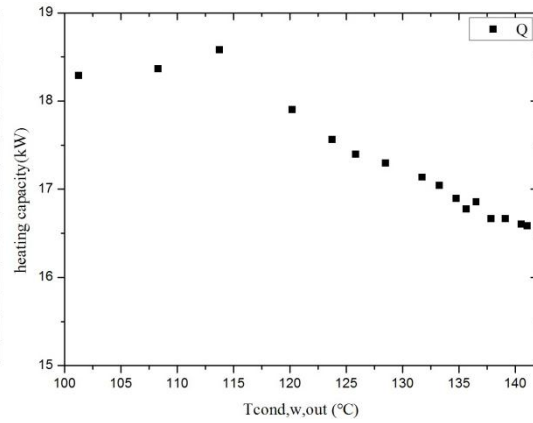
293 4.1.1 Performance variation of cascade system due to the water outlet

294 *temperature in high-stage refrigerant cycle*

295 Fig7 shows the experimental results (water inlet temperature at 50 °C) at the
296 optimum refrigerant charge amount of R245fa equals to 3400g and BY-3 equals to
297 2000g in the low & high-stage refrigerant cycle, respectively. From Fig 7-a, we can
298 see that with the water outlet temperature increasing, the input power in both
299 low-stage and high-stage refrigerant cycle increased accordingly due to the
300 compression ratio increased in the low and high-stage refrigerant cycle. From Fig7-d,
301 it could be found that the evaporating temperature in high-stage refrigerant cycle kept
302 nearly stable before the water outlet temperature reached 115°C, and then it increased
303 according to the water outlet temperature. Consequently, the heating capacity
304 increased firstly and then when the water outlet temperature reached 115°C, the
305 heating capacity decreased according to the water outlet temperature increasing. The
306 temperature difference between DT in high-stage and water outlet temperature is
307 about 5-6 °C , and the value increased a little when the water outlet temperature
308 reached 130 °C due to the decreasing latent heat of the refrigerant. The total COP of
309 the HTCHP decreased according to the increasing of the water outlet temperature in
310 the high-stage cycle condenser due to the input power and heating capacity changing.



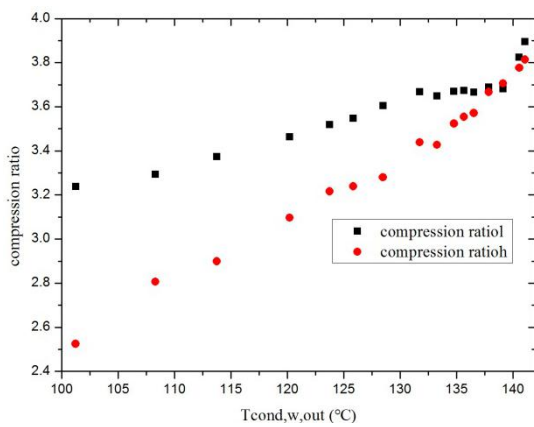
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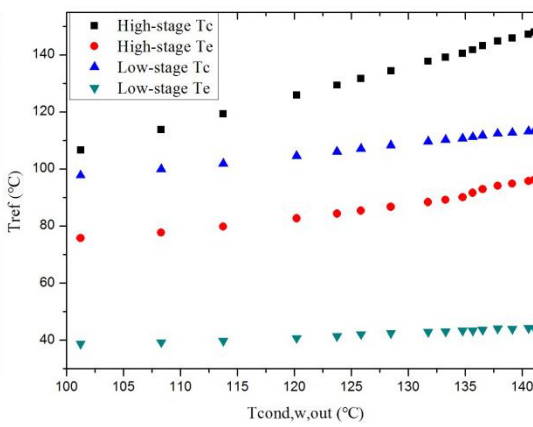
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(a) Input Power

(b) heating capacity



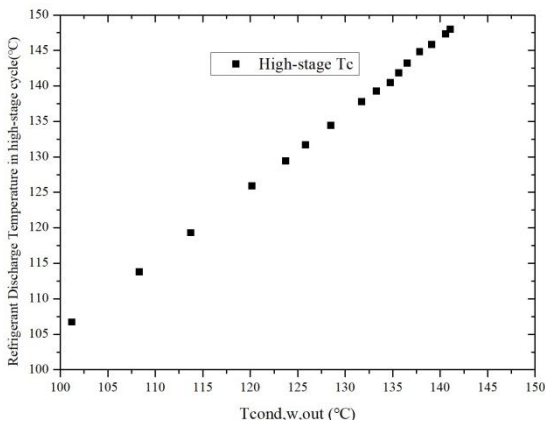
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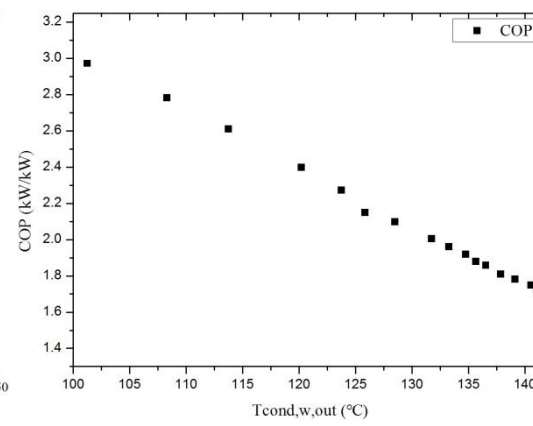
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(c) compression ratio

(d) refrigerant temperature



315



316

(e) High-stage DT

(f) COP

317

Fig. 7. Variations of (a) Input Power , (b) heating capacity,(c) compression ratio, (d) refrigerant

318

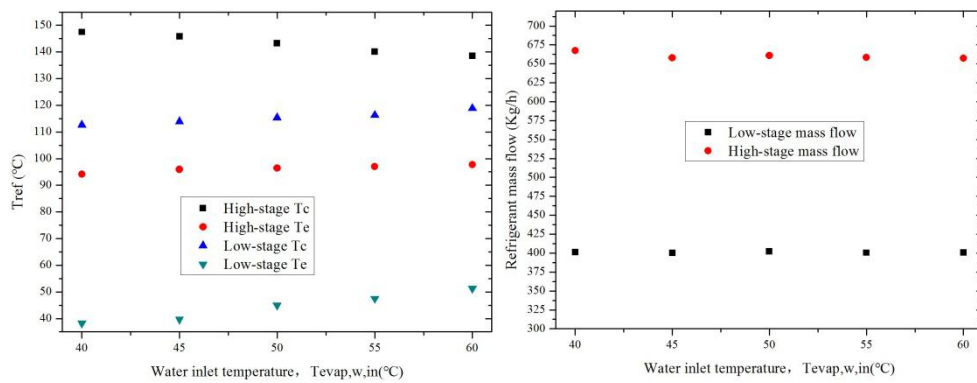
temperature, (e) High-stage DT and (f) COP according to water outlet temperature in high-stage

319

condenser

320 4.1.2 Performance variation of cascade system due to the water inlet
 321 temperature in low-stage refrigerant cycle

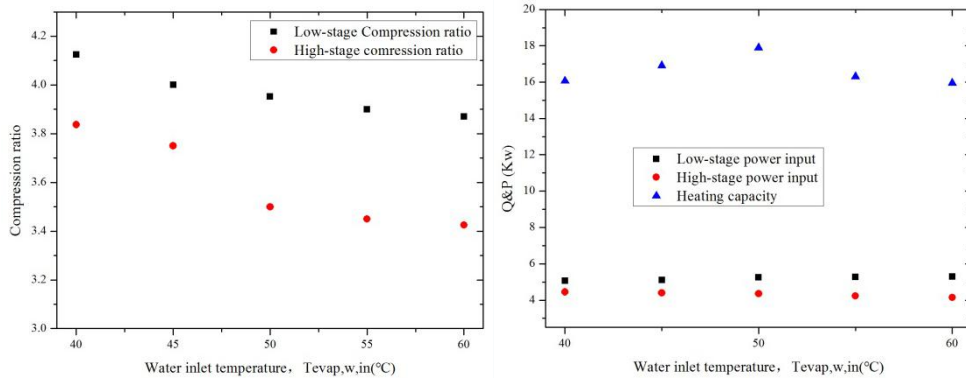
322 The performance of the cascade system was investigated by changing the water
 323 inlet temperature in the evaporator of the low-stage cycle at the optimum refrigerant
 324 charge amount of 3400g and 2000g in the low-stage and high-stage refrigerant cycle,
 325 respectively. The water flow rate in the low-stage cycle was fixed at 1630kg/h.



326
 327

(a) refrigerant temperature

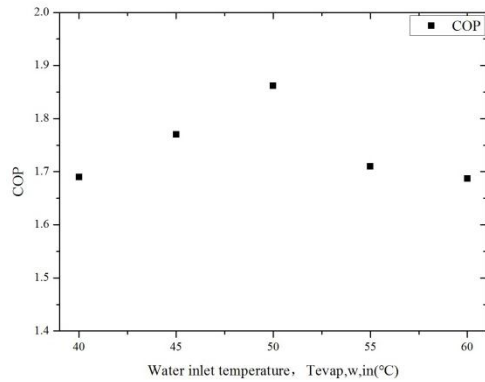
(b) mass flow



328
 329

(c) compression ratio

(d) power input and heating capacity



(e) COP

Fig.8. Variations of (a) refrigerant temperature (b) mass flow and (c) compression ratio (d) power input and heating capacity (e) COP according to the water inlet temperature in the low-stage evaporator

As shown in **Fig.8**, the change of the refrigerant temperatures, the refrigerant mass flow, the compression ratio, input power and heating capacity and COP according to the water inlet temperature were studied.

The low-stage cycle evaporating temperature increased due to the increasing water inlet temperature. The condensing temperature in the low-stage cycle increased according to the water inlet temperature and the rate of the condensing temperature is less than the evaporating temperature due to the decreasing compression ratio in the low-stage cycle as shown in Fig.8-c. The high-stage cycle evaporating temperature increased due to the increasing condensing temperature in the low-stage cycle according to the water inlet temperature. The high-stage cycle condensing temperature decreased due to the decreasing rate of the compression ratio in the high-stage cycle is larger than the increasing ratio of the evaporating temperature in the high-stage cycle. The input power in the low and high-stage cycle kept nearly the same due to the constant refrigerant mass flow. The heating capacity of the cascade system increased firstly and when the water inlet temperature reached 50°C, it reached the maximum

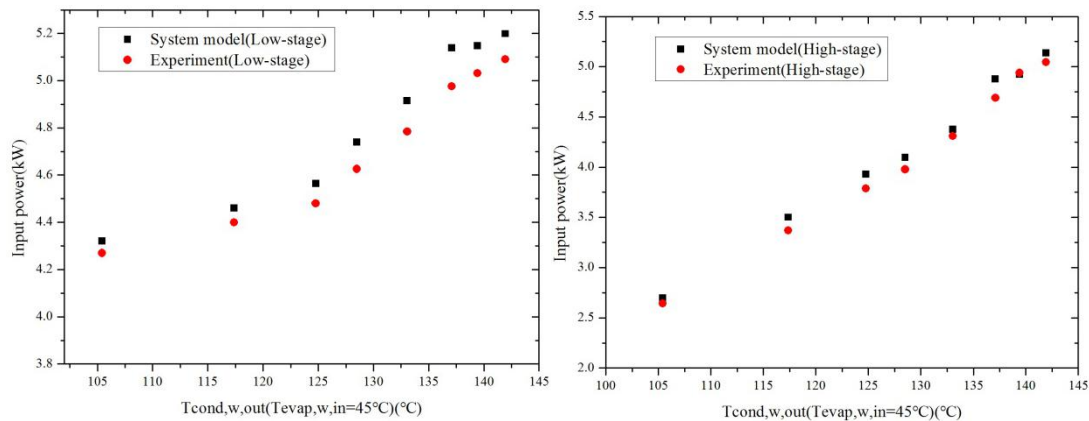
349 and then it decreased according to the water inlet temperature increasing because of
 350 the compressor running map(at the same evaporating temperature, when the
 351 condensing temperature increases, power input will increase while the cooling
 352 capacity will decrease). Accordingly, the COP of the cascade heat pump system
 353 followed the same tendency as the heating capacity.

354 4.2 Simulated results

355 4.2.1 Model validation

356 The presented model was verified comparing the experimental and simulated
 357 results.

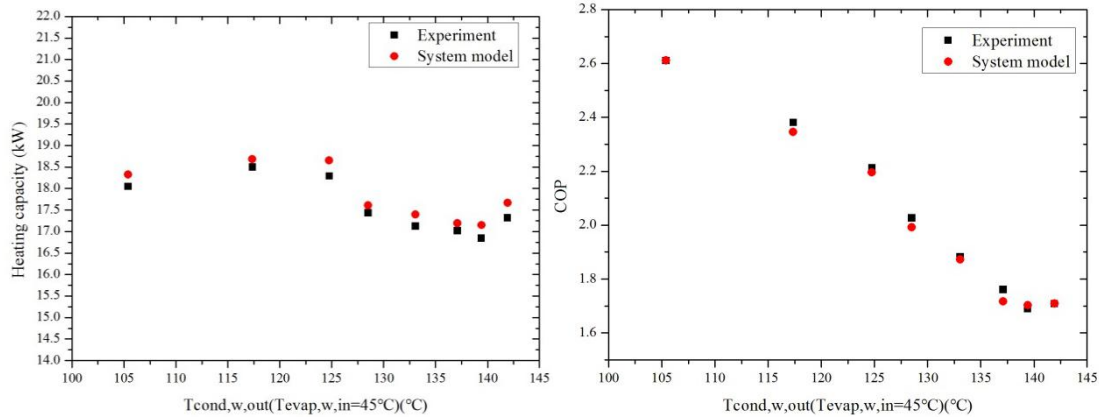
358 The input power (low-stage and high-stage), heating capacity and COP of
 359 experiment and system model according to outlet water temperature (with water inlet
 360 temperature of 45°C) were shown in Fig. 9.



361

362 (a) Input power in low-stage

(b) Input power in high-stage



363

364

(c) Heating capacity

(d) COP

365

Fig.9 Comparisons of System model and Experimental results of (a) Input power in low-stage (b)

366

Input power in high-stage (c) Heating capacity (d) COP according to the water outlet temperature

367

In Fig.9, the changing current of the system model results of the input power,

368

heating capacity and COP followed the same tendency with that of the experimental

369

results. In the low-stage refrigeration cycle, the system model of the input power was

370

higher than that of the experimental results with the maximum relative deviation of

371

3.27%. The system model result of the input power in the high-stage refrigeration

372

cycle was a little higher than that of the experimental result and the maximum

373

deviation is 3.93%.The heating capacity of the system model was higher than that of

374

the experimental result with the maximum deviation of 1.96%. Consequently, the

375

COP of the system model was lower than the experimental result and the maximum

376

deviation was -2.53%. In this case, the system model was validated with the

377

experimental result.

378

5. Conclusions

379

The system model was validated via lots of experimental results in this paper,

380 and the following conclusions could be drawn based on the results discussed before:

381 (1) The experimental results showed that the cascade heat pump system could
382 reach water outlet temperature of 142 °C and the maximum temperature lift
383 could reach 100 °C which was the highest level in the opening literature.
384 BY-3 was proved to have good performance as the working fluid in the
385 low-stage refrigeration cycle. The pressure ratio in the high and low-stage
386 refrigeration cycle was 3.4 and 3.9, respectively with the system COP of
387 1.72.

388 (2) The system model was validated with high feasibility via the experimental
389 results. The maximum relative deviation of input power in high & low-stage,
390 the heating capacity and the COP between the system model and the
391 experimental results was 3.93%,3.27%,1.96% and -2.53%, respectively.

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395 **References**

396 [1] I. Dincer, Renewable energy and sustainable development: a crucial review,
397 Renew. Sustain. Energy Rev. 4 (2) (2000) 157-175.

398 [2] Yang M, Patiño-Echeverri D, Yang F, et al. Industrial energy efficiency in China:
399 achievements, challenges and opportunities, Energy Strategy Reviews, 2015, 6(1):
400 20-29.

- 401 [3] Johnson I, Choate W T, Davidson A. Waste Heat Recovery. Technology and
402 Opportunities in US Industry, BCS, Inc., Laurel, MD (United States), 2008.
- 403 [4] S.S. Bertsch, E.A. Groll, Tspump for residential heating and cooling applications
404 in northern US climates, Int. J.Refrig. 31(2008) 1282– 1292.
- 405 [5] P.K. Bansal, S. Jain, Cascade systems: past, present, and future, ASHRAE Trans.
406 113 (1) (2007) 245-252.
- 407 [6] Hae Won Jung, Hoon Kang, Won Ja Yoon, Yongchan Kim, Performance
408 comparison between a single-stage and a cascade multi-functional heat pump for both
409 air heating and hot water supply, Int. J. Refrig 36 (2013) 1431-1441
- 410 [7]Wang Bingming, Wu Huagen, Li Jianfeng, Xing Ziwen, Experimental investigation
411 on the performance of NH₃/CO₂ cascade refrigeration system with twin-screw
412 compressor ,Int. J. Refrig 32 (2009) 1358–1365.
- 413 [8]J. Alberto Dopazo, Jose´Ferna´ndez-Seara, Experimental evaluation of a cascade
414 refrigeration system prototype with CO₂ and NH₃ for freezing process applications,
415 Int. J. Refrig 34 (2011) 257-267.
- 416 [9] Qu Minglu, Fan Yanan, Chen Jianbo, Li Tianrui, Li Zhao, Li He, Experimental
417 study of a control strategy for a cascade air source heat pump water heater Applied
418 Thermal Engineering 110 (2017) 835–843.
- 419 [10] Han saem Park, Dong Ho Kim, Min Soo Kim, Thermodynamic analysis of
420 optimal intermediate temperatures in R134a&R410A cascade refrigeration systems
421 and its experimental verification, Applied Thermal Engineering 54 (2013) 319-327.

- 422 [11] Dong Ho Kim, Han Saem Park, Min Soo Kim, Optimal temperature between
423 high and low stage cycles for R134a/R410A cascade heat pump based water heater
424 system , Thermal and Fluid Science 47 (2013) 172–179.
- 425 [12] Hansaem Park, Dong Ho Kim, Min Soo Kim ,Performance investigation of a
426 cascade heat pump water heating system with a quasi-steady state analysis, Energy
427 63(2013) 283-294.
- 428 [13] H. Cho, C. Baek, C. Park, Y. Kim, Performance evaluation of a two-stage CO₂
429 cycle with gas injection in the cooling mode operation, Int. J. Refrig. 32 (2009)
430 40–46.
- 431 [14] Xiaoyu Liu, Dingjiang Chen, An assessment of the energy-saving potential in
432 China's petroleum refining industry from a technical perspective, Energy 59 (2013)
433 38-49.
- 434 [15] CHEN Chengmin, ZHANG Yufeng, DENG Na, MA Hongting, ZHANG Yansuo,
435 MA Lijun , HU Xiaowei, Experimental Performance of Moderate and High
436 Temperature Heat Pump Charged with Refrigerant Mixture BY-3, Trans. Tianjin Univ.
437 2011, 17: 386-390
- 438 [16] Danxing Z. Fluid and process thermodynamics, Textbook Publishing Center of
439 Chemical Industry Press, 2005
- 440 [17] Morini M, Pavan C, Pinelli M, et al. Analysis of a scroll machine for micro ORC
441 applications by means of a RE/CFD methodology, Applied Thermal Engineering,
442 2015, 80: 132-140.

- 443 [18] Shengjun Z, Huaixin W, Tao G. Experimental investigation of moderately high
444 temperature water source heat pump with non-zeotropic refrigerant mixtures, *Applied*
445 *Energy*, 2010, 87(5): 1554-1561.
- 446 [19] Yongmei X. Theoretical and experimental study on new alternative refrigerants,
447 Ph. D. Thesis, Zhejiang University, China, 2004.
- 448 [20] Defibaugh D R, Morrison G. Interaction coefficients for 15 mixtures of
449 flammable and non-flammable components, *International journal of refrigeration*,
450 1995, 18(8): 518-523.
- 451 [21] Cao D S, Shi L. Refrigerant Manual[M]. Metallurgical Industry Press, Beijing,
452 China, 2003(in Chinese).
- 453 [22] State Administration of Quality Supervision, Inspection and
454 Quarantine, JJF1059.1-2012, National Metrology Technical Specifications of People's
455 Republic of China, Beijing: National Legal Measurement Management and
456 Measurement Technical Committee, 2012
- 457 [23] R.J. Moffat, Describing the uncertainties in experimental results, *Int. J. Exp.*
458 *Therm. Fluid Sci.* 1 (1998) 3–17.