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# Condensation heat transfer and pressure drop correlations in plate heat exchangers for heat pump and organic Rankine cycle systems

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## Abstract

An accurate prediction method of flow condensation heat transfer in plate heat exchangers is important for the design of condensers. The existing prediction methods are semi-empirical correlations, whose applicability highly rely on the range of original test data used for the correlation development. In this study, prediction methods of frictional pressure drop and heat transfer coefficient of flow condensation in a plate heat exchanger which were tailored for the applications in heat pump and organic Rankine cycle systems, were developed. We conducted a comprehensive experimental investigation, building a database including 283 data points for both pressure drop and heat transfer. We tested seven working fluids, classified by hydrofluorocarbons – R134a, R236fa and R245fa, hydrofluoroolefins – R1234ze(E) and R1233zd(E), and hydrocarbons – propane and isobutane, for a wide range of condensation temperatures varying from 30 °C to 90 °C. Two dimensionless numbers, the density ratio of liquid phase to vapour phase and the Bond number, were involved for developing the new prediction methods. The paper presents data for higher temperatures than those presented in previous works, and novel analysis and prediction methods. The new correlations achieve an improved prediction, enabling an 8.9 % and a 10.3 % mean absolute percentage deviation for heat transfer and pressure drop data, respectively.

**Keywords:** condensation, plate heat exchanger, high condensation temperature, correlation

## Nomenclature

### Symbols

$b$	corrugation amplitude, m
Bd	Bond number
$D_h$	hydraulic diameter, m
$f$	friction factor
$G$	mass flux of working fluid, kg/m <sup>2</sup> s
$h$	heat transfer coefficient, W/m <sup>2</sup> K
$k$	thermal conductivity, W/m K
$N$	number of the plate
Nu	Nusselt Number
$P$	pressure, Pa
Pr	Prandtl number
Re	Reynolds number
$T$	temperature, °C
$x$	vapour quality

### Subscripts

eq	equivalent
exp	experimental
fri	frictional
l	liquid
m	mean
out	outlet
pred	predicted
sat	saturation
sub	subcooled
sup	superheated
v	vapour
wf	working fluid

### Greek Symbols

$\mu$	dynamic viscosity, Pa s
$\rho$	mass density, kg/m <sup>3</sup>
$\rho^*$	density ratio of liquid phase to vapour phase
$\Delta$	difference
$\sigma$	surface tension, N/m

### Abbreviations

HC	hydrocarbon
HFC	hydrofluorocarbon
HFO	hydrofluoroolefin
MAPD	mean absolute percentage deviation
ORC	organic Rankine cycle

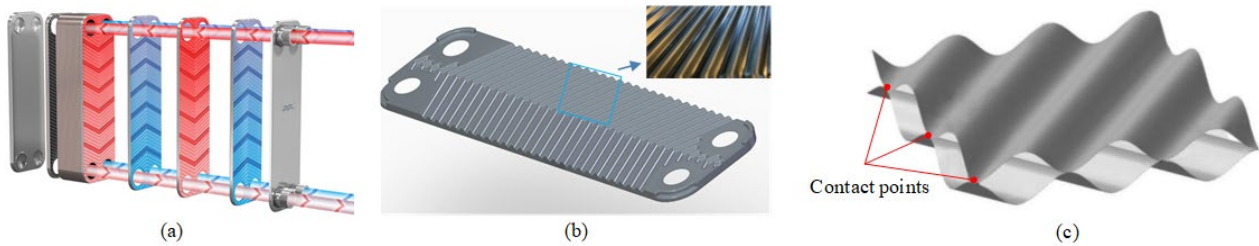
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$\beta$	chevron angle	PHE	plate heat exchanger
$\lambda$	wavelength of surface corrugation, m		
$\gamma$	dimensionless corrugation parameter		
$\phi$	area enlargement factor		

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### 1. Introduction

Plate heat exchangers (PHEs) consist of multiple chevron-corrugated plates; see Figs. 1 (a) and (b). The working fluid flows through a cross-corrugated channel formed by adjacent plates, in which the fluid path is further subdivided into numerous interconnected units by contact points of peaks and troughs of two adjacent plates; see Fig 1. (c). This complex flow morphology induces turbulence and enhances heat transfer [1]. The structure-determined advantages, e.g. thermal effectiveness, compactness and design flexibility, make the PHE increasingly used as condensers in a wide range of applications (e.g. organic Rankine cycle (ORC) [2] and heat pump systems [3]). Consequently, a reliable model for predicting the flow condensation heat transfer in PHEs is of crucial importance for the condenser design. An oversized or undersized design for the condenser will deteriorate the overall economic performance of the systems.



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Figure 1. Illustration of (a) a PHE (by courtesy of Alfa Laval), (b) a chevron-corrugated plate, and (c) a cross-corrugated channel between two plates [4].

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However, the complex flow morphology in the cross-corrugated channel makes it difficult to understand the internal two-phase flow. Vakili-Farahani et al. [5] recently carried out a review work on flow condensation in PHEs, and the authors stated that it is difficult to make theoretical predictions due to the limited studies in this field. Existing models used for predicting the condensation pressure drop and heat transfer coefficient in the cross-corrugated channels of PHEs are semi-empirical correlations developed using regression of experimental data. Tao and Ferreira [6] built a database including 2376 and 1590 data points for heat transfer and frictional pressure drop, respectively, to assess the predictive performances of the existing prediction methods. Although the correlations developed by Longo et al. [7] and Kuo et al. [8] showed the best accuracy among the eight heat transfer correlations selected in the paper, they are only able to predict 62.0 % and 58.5 % of the heat transfer data within  $\pm 30$  % bandwidth, respectively. Up to 30 % deviation between the respective actual and predicted values is considered acceptable in industry [5]. It is even worse for the pressure drop correlation, i.e. the correlation developed by Amalfi et al. [9] only predicted 52.7 % of the pressure drop data within  $\pm 50$  % bandwidth. This was even the best prediction result among those provided by the six selected pressure drop correlations. These results indicate that there is no reliable correlation that can be widely used for various applications.

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Kim et al. [10] studied the two-phase flow in a channel of the PHE with a visualisation method. The authors observed that the two-phase flow in the millimetre-size PHE channel has similar thermo-physical characteristics as has been found in mini- and microchannels, i.e. bubbles can be elongated until fully approaching the diameter of the channel, which is different from turbulent mixing flow in conventional macroscale channels. Moreover, Amalfi et al. [9] suggested to introduce a parameter to characterise the transition between macro-to-microscale flow in PHEs, and separately develop the correlations for macro- and microscale heat transfer. The microscale heat transfer phenomenon identified in [9,10] suggests that the surface tension whose effects are usually negligible in macroscale channels, becomes important in PHE condensation [11]. The convection between the vapour and liquid phases can be affected by the surface tension, through a modification of liquid phase behaviour [12]. In our previous work [13], a widely used correlation (Yan et al. [14]) was modified by introducing a dimensionless number, the Bond number, which involves the surface tension, and thereby an improvement of the predictive performance of the new correlation for the experimental results was demonstrated. To the best of our knowledge, no other research work has incorporated the effects of surface tension when developing prediction methods of the thermal-hydraulic performance of condensation in PHEs.

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2 High temperature condensation has numerous applications. One of the most typical applications is large-scale  
3 heat pumps connected to district heating systems. A survey for Europe indicates that 70 °C to 80 °C is the most  
4 common condensation temperature, and some systems operate at even higher temperatures [15]. In addition,  
5 this high temperature condensation is also applied in ORC systems used for combined heat and power  
6 generation (e.g. [16]). As previously mentioned, the applicable range of existing correlations highly relies on  
7 the original operating conditions of the experimental results used for deriving the correlations. Nevertheless,  
8 the condensation temperatures in almost all the studies were concentrated between 20 °C and 40 °C, and only  
9 a few tests were carried out with relatively high temperatures up to about 70 °C [6,13]. It is well known that  
10 the saturation temperature is an important factor in the condensation process, and the heat transfer can be  
11 enhanced by increasing the saturation temperature, meanwhile with an increased pressure drop [5]. Therefore,  
12 the applicability of existing condensation correlations for high temperature conditions needs to be evaluated.  
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14 The goal of this paper is to develop prediction methods of the thermal-hydraulic performance for the flow  
15 condensation in PHEs that can be widely applicable for the working conditions in condensers of heat pump  
16 and ORC systems. In order to achieve this goal, a series of experiments was carried out with condensation  
17 temperatures varying from 30 °C to 90 °C and with various mass flow rates. Specifically, the (40 to 90) °C  
18 and (30 to 50) °C condensation temperatures are commonly applied in the condenser of heat pump and ORC  
19 systems, respectively [2,17] and the high temperatures of (70 to 90) °C are also applicable for the condenser  
20 in ORC-based combined heat and power plants [16]. Seven working fluids commonly used in the two systems  
21 [17,18] were selected for the experimental tests; these consisted of three hydrofluorocarbons (HFCs), R245fa,  
22 R236fa and R134a, two hydrofluoroolefins (HFOs), R1233zd(E) and R1234ze(E), and two hydrocarbons  
23 (HCs), isobutane and propane. Subsequently, we carried out an experimental analysis to identify the most  
24 important parameters (among which the surface tension is considered) and used the test data to evaluate the  
25 existing correlations' predictive performances. Based on the analysis, the identified parameters were integrated  
26 with the existing correlations to develop the new prediction methods.  
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28 The paper includes the following novel contributions. First, the flow condensation characteristics under the  
29 high temperature condensation (70 °C to 90 °C) were systematically investigated, while relevant recent works  
30 targeted temperatures lower than 70 °C [6,13]. Second, the experimental results and thermo-physical properties  
31 of seven working fluids were compared, aiming at identifying the most influential parameters on thermal-  
32 hydraulic performance. Such comparison among different working fluids is lacking in the existing research  
33 works. Third, two dimensionless parameters, the density ratio of liquid phase to vapour phase and the Bond  
34 number, were used for developing the new prediction methods. In addition, based on our previous study [13]  
35 we improve the condensation process used for the acquisition of experimental data, i.e. excluding the liquid  
36 subcooling region from the whole condensation process and thus improving the accuracy of condensation data  
37 (see Section 2.1).  
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39 Section 2 presents the methods of the experimental campaign, data reduction and uncertainty analysis. Section  
40 3 presents experimental results of PHE condensation, a comparison of thermal-hydraulic performance among  
41 the working fluids, an evaluation of predictive performance of existing correlations for the test data and a  
42 development of new prediction methods. Important findings and conclusions are presented in Section 4 and  
43 Section 5, respectively.  
44

## 45 2. Methods

### 46 2.1 Experimental campaign

47 A PHE test facility at the Technical University of Denmark was used for the experiments. A brazed PHE  
48 having a 3.4 mm hydraulic diameter  $D_h$  and a 65° chevron angle  $\beta$  is placed in the working fluid loop and used  
49 as the test section (condenser). Further details of the test facility and the PHE geometry can be found in [13].  
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51 Table 1 summarises the differences in working conditions between the present study and the previous work  
52 [13]. First, three new working fluids (R236fa, isobutane, propane) were added, especially the inclusion of a  
53 new type of working fluid, HC that has significantly different thermo-physical properties than those of HFCs  
54 and hydrofluoroolefin HFOs (e.g. HCs have much lower density of the liquid phase). Second, the range of  
55 condensation temperatures used for testing was extended, i.e. the lower temperature for all working fluids is  
56 30 °C, while the upper temperature of four of the working fluids is 90 °C. Third, the working fluids were  
57 controlled as the saturated liquid with the vapour quality of 0.01 to 0.05 at the outlet of the condenser. In the

1 previous study [13], the condensation process in the condenser included also the liquid subcooling region,  
 2 characterised by a subcooling of (0 to 5.3) K at the outlet of the condenser. Accordingly, the liquid subcooling  
 3 region was excluded from the whole heat transfer process in the data reduction of previous work [13]. The  
 4 liquid single-phase heat transfer coefficient and the frictional pressure drop in the subcooling region, and thus  
 5 the heat transfer area of the subcooling region, were estimated using existing single-phase flow correlations,  
 6 which may ultimately cause deviations in the results of condensation heat transfer from actual values. In  
 7 general, the working conditions used in the present study will be beneficial for developing condensation  
 8 correlations enabling an improved accuracy and a wider applicable range both in terms of working fluids and  
 9 temperatures. Moreover, the vapour at the inlet of the condenser kept the superheating within 5 K. The mass  
 10 flux of the working fluids ranged from 12 kg/m<sup>2</sup>s to 92 kg/m<sup>2</sup>s. The Refprop 10.0 [19] was used to calculate  
 11 the thermo-physical properties of the working fluid.

12  
 13 Table 1. Comparison of working conditions between the present and previous experiments [13].

	Working fluids	Condensation temperature	Working fluid condition at outlet of condenser
Present study	R236fa R245fa R1233zd(E) Isobutane	30 °C, 40 °C, 50 °C 70 °C, 80 °C, 90 °C	Two-phase fluid with a vapour quality of 0.01 to 0.05
	R134a R1234ze(E) Propane	30 °C, 40 °C, 50 °C	
Previous study [13]	R134a	30 °C, 40 °C	Liquid subcooled 0.0 K to 5.5 K
	R1234ze(E)	50 °C, 60 °C	
	R245fa	40 °C, 50 °C	
	R1233zd(E)	60 °C, 70 °C	

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15 *2.2 Data analysis*

16 The data reduction method for the condensation process studied in the present paper, i.e. condensation of the  
 17 working fluids from slightly superheated vapour to the almost saturated liquid, has been presented in our  
 18 previous work [13]. The heat transfer coefficient  $h_{wf}$ , frictional pressure drop  $\Delta p_{fri}$ , friction factor  $f$  of the working  
 19 fluid for flow condensation in the PHE as well as the other relevant parameters were calculated. Following the  
 20 method suggested by Kline and McClintock [20], the uncertainties of  $h_{wf}$  and  $\Delta P_{fri}$  were calculated based on  
 21 those of the directly measured parameters, whose values can be found in [13]. The uncertainties of  $h_{wf}$  and  
 22  $\Delta P_{fri}$  range from 3.9 % to 13.4 % and from 4.1 % to 14.8 %, respectively.

23

24 **3. Results**

25 *3.1 Experimental results*

26 For validation purposes, we compared the heat transfer results obtained in the present study with those from  
 27 another study that carried out experiments using similar working conditions. Longo [21] tested the complete  
 28 condensation of R134a, i.e. a superheating of about 10 K at the condenser inlet and a subcooling of about 3 K  
 29 at the condenser outlet, which is closest to the working conditions used in the present research among the  
 30 studies found in literature. The condensation heat transfer coefficients of R134a obtained in the present study  
 31 and the study reported by Longo [21] are compared in Figure 2 under the same saturation temperature  $T_{sat}$  of  
 32 40 °C and almost the same range of mass fluxes of working fluid  $G$ . Figure 2 shows that the data points from  
 33 Longo [21] fall in the uncertainty range of heat transfer results obtained in the present study, indicating an  
 34 agreement between the results of the two studies.

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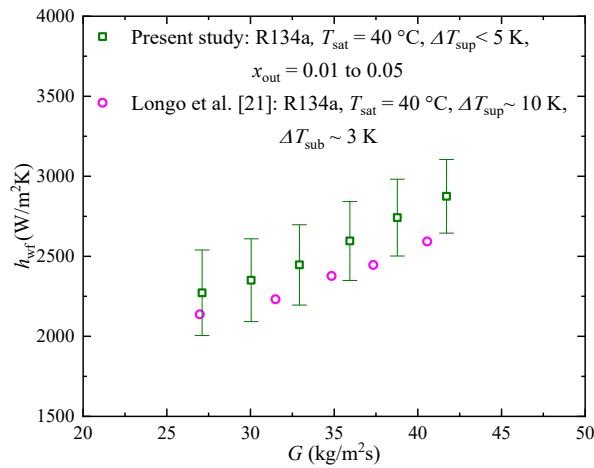
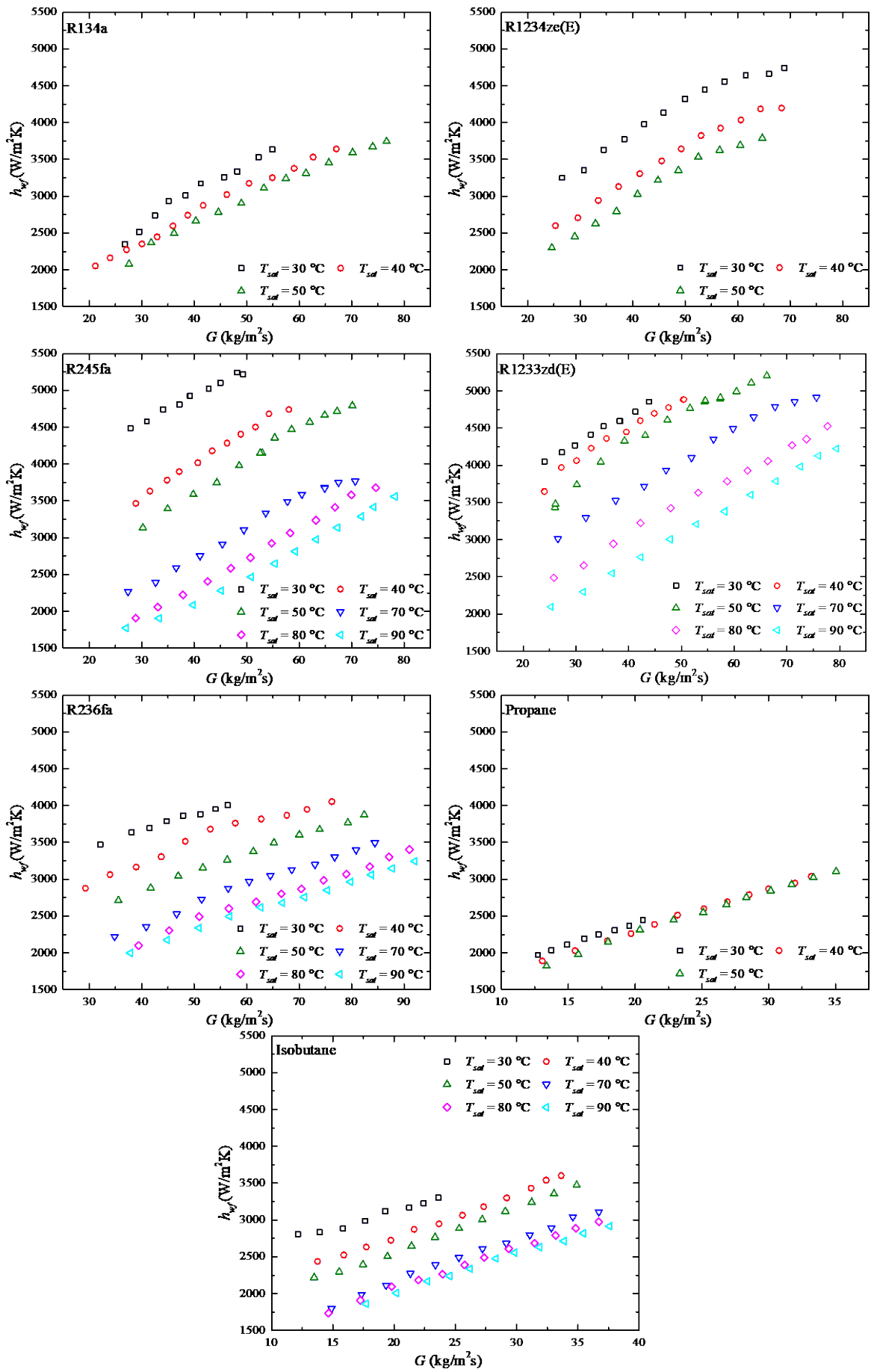


Figure 2. Comparison of  $h_{wf}$  of R134a obtained in the present paper and the study reported by Longo [21].

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Figures 3 and 4 depict the test results of heat transfer and pressure drop of the seven working fluids with various working conditions. A wide range of heat transfer coefficients and length-specific frictional pressure drops (frictional pressure drop per unit length of the plate) were obtained in the study. Overall, the heat transfer coefficient and the length-specific frictional pressure drop vary from 1819 W/m<sup>2</sup>K to 5242 W/m<sup>2</sup>K and from 10.5 kPa/m to 108 kPa/m, respectively. The heat transfer coefficient and the frictional pressure drop of all working fluids increase with the mass flux and decrease with the saturation temperature, which is a typical characteristic of a shear-controlled condensation mainly realised by convective heat transfer at the interface of the liquid and vapour phases [5]. Moreover, this result is in line with the general findings concluded in the review work by Vakili-Farahani et al. [5]. In particular, both the higher mass flux and the lower saturation temperature enable a higher vapour velocity and thus more shear stress and turbulence at the liquid-vapour interface, resulting in an increased heat transfer coefficient and associated frictional pressure drop.



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Figure 3. Heat transfer results of the seven working fluids.

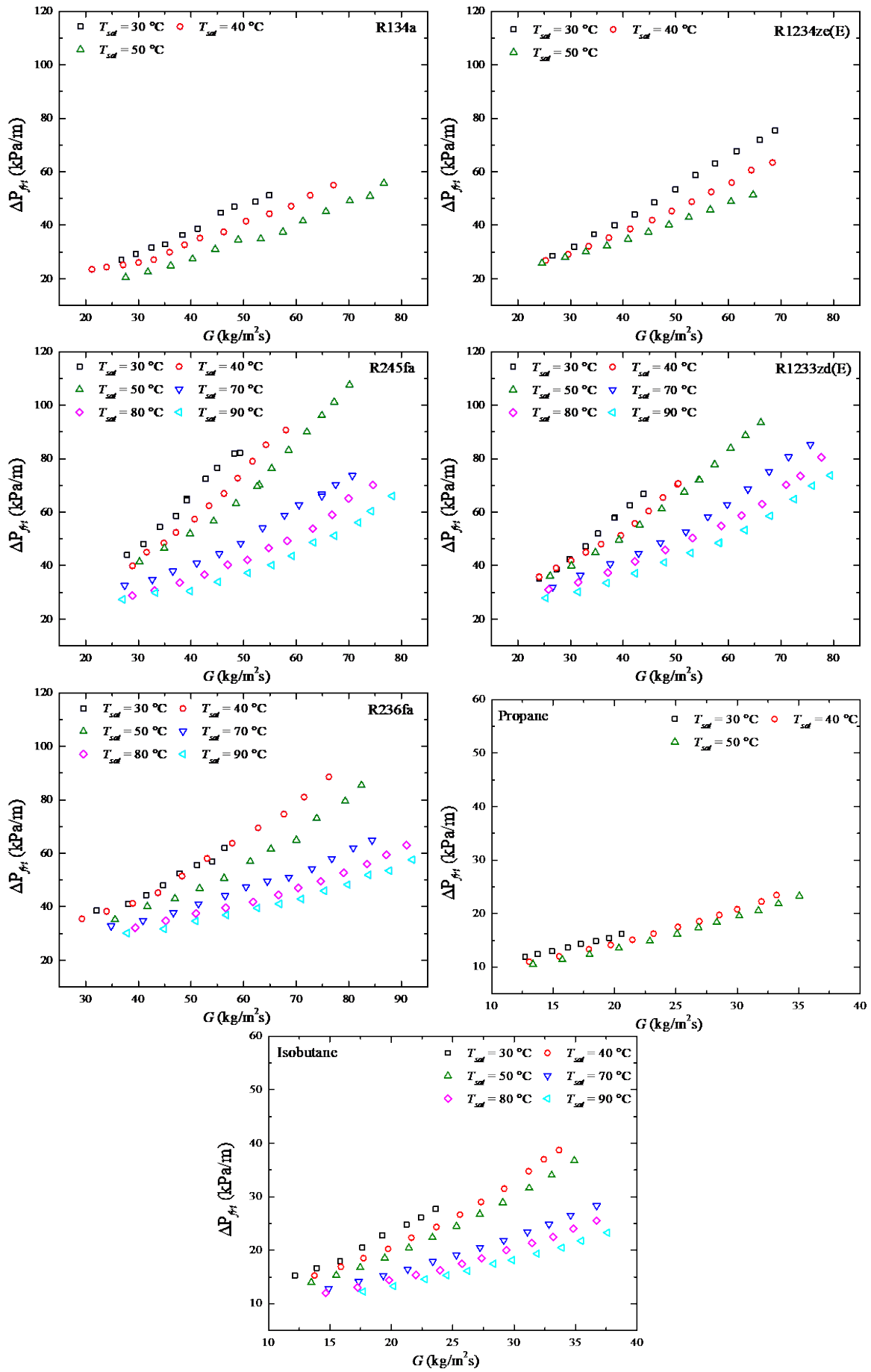


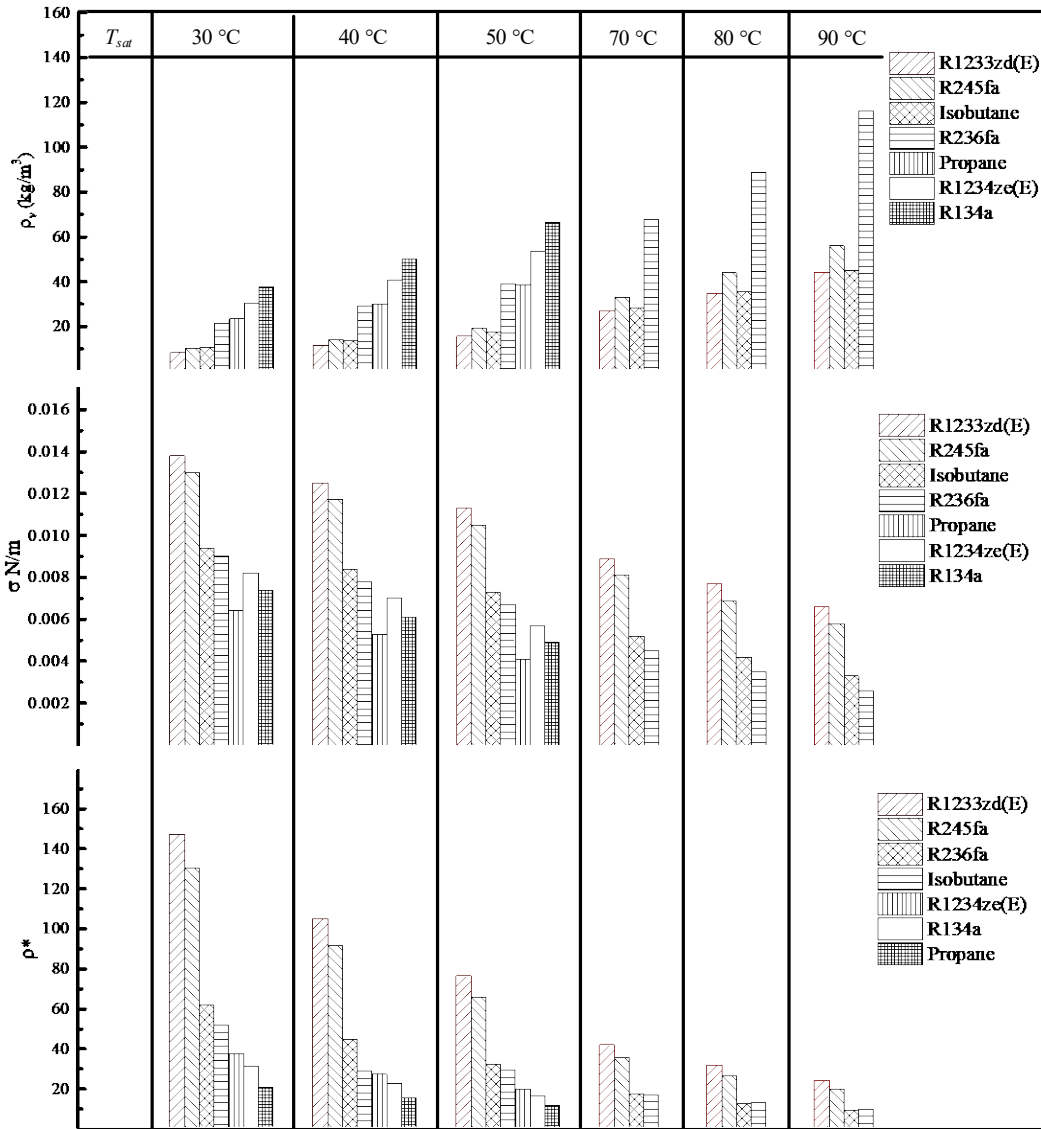
Figure 4. Pressure drop results of the seven working fluids.

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1 3.2 Thermal-hydraulic performance comparison

2 In order to identify the parameters which are most influential on heat transfer and pressure drop, the  
 3 experimental results of the seven working fluids are compared in this section. The comparison indicates that  
 4 working fluids having the lower vapour density,  $\rho_v$  (higher vapour velocity), and higher surface tension,  $\sigma$ ,  
 5 generally have a better heat transfer performance. The vapour density and the surface tension of the seven  
 6 working fluids are shown in Figure 5. Consequently, R1233zd(E), isobutane and R245fa have the highest  $h_{wf}$ ,  
 7 while R134a has the lowest  $h_{wf}$  among the seven working fluids used for  $T_{sat} = 30\text{ }^\circ\text{C}$  to  $50\text{ }^\circ\text{C}$  experiments and  
 8 R236fa has the lowest  $h_{wf}$  among the four working fluids used for  $T_{sat} = 70\text{ }^\circ\text{C}$  to  $90\text{ }^\circ\text{C}$  experiments. For the  
 9 frictional pressure drop, an influential parameter was identified, namely, the density ratio of liquid phase to  
 10 vapour phase (see Figure 5),  $\rho^* = \rho_l/\rho_v$ , since the pressure drop among the different working fluids is  
 11 correlated with their density ratios at a certain temperature. A larger liquid–vapour density difference means  
 12 an increased shear stress of the vapour phase on the liquid phase, thus intensifying the convection at the  
 13 interface and inducing a higher frictional pressure drop [22].  
 14



15 Figure 5. Thermo-physical property comparison of the working fluids at various temperatures.

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 18 For quantifying the thermal-hydraulic performance difference among the working fluids, an average  $h_{wf}$  and  
 19  $\Delta p_{fi}$  of each fluid was computed based on the same range of mass fluxes, and their differences are presented  
 20 in Table 2. Isobutane was selected as the base fluid. No comparison was made for  $T_{sat} = 30\text{ }^\circ\text{C}$ , because there  
 21 is no common range of mass fluxes for propane and isobutene with other working fluids. From the table, the  
 22 key findings with respect to the experimental test of the  $T_{sat} = 40\text{ }^\circ\text{C}$  and  $50\text{ }^\circ\text{C}$  can be drawn as follows. First,  
 23 R1233zd(E) has a 20 % and 16 % higher heat transfer coefficient than isobutane at  $T_{sat} = 40\text{ }^\circ\text{C}$  and  $50\text{ }^\circ\text{C}$ ,  
 24 respectively. However, a 22 % increase in frictional pressure drop is also achieved by R1233zd(E) compared

1 with isobutane. Second, although propane has the weaker heat transfer performance compared to isobutane  
 2 (11 % and 15 % lower heat transfer coefficient at  $T_{\text{sat}} = 40 \text{ }^{\circ}\text{C}$  and  $50 \text{ }^{\circ}\text{C}$ , respectively), it enables a 37 % lower  
 3 pressure drop. Third, the remaining working fluids, R245fa, R236fa, R134a and R1234ze(E), show less  
 4 competition in the thermal-hydraulic performance, e.g. all of them have the lower  $h_{\text{wf}}$ , but higher  $\Delta p_{\text{fri}}$  than  
 5 propane. In the experimental test of the  $T_{\text{sat}} = 70 \text{ }^{\circ}\text{C}$  to  $90 \text{ }^{\circ}\text{C}$ , isobutane shows better performance than the  
 6 other three working fluids, which is attributed to its highest  $h_{\text{wf}}$  and lowest  $\Delta p_{\text{fri}}$ .  
 7

8 Table 2. Differences of average  $h_{\text{wf}}$  and  $\Delta p_{\text{fri}}$  of working fluids when selecting isobutane as the base fluid.

	R1233zd	R245fa	R236fa	Propane	R134a	R1234ze(E)
40 °C	+20 %/+22 %	+5 %/+25 %	-14 %/+4 %	-15 %/-37 %	-31 %/-25 %	-19 %/-14 %
50 °C	+16 %/+22 %	-2 %/+26 %	-22 %/-4 %	-11 %/-37 %	-30 %/-35 %	-22 %/-15 %
	R1233zd	R245fa	R236fa			
70 °C	+12 %/+45 %	-18 %/+37 %	-18 %/+24 %			
80 °C	-1 %/+46 %	-25 %/+32 %	-29 %/+26 %			
90 °C	-13 %/+44 %	-32 %/+30 %	-31 %/+30 %			

9

### 10 3.3 Evaluation of existing correlations

11 The heat transfer correlations derived by Longo et al. [7], Kuo et al. [8], Yan et al. [14] and Zhang et al. [13]  
 12 were selected for the comparison. Tao and Ferreira [6] found that the correlations derived by Longo et al. [7],  
 13 Kuo et al. [8] and Yan et al. [14] provide the best prediction for the database including 2376 heat transfer data  
 14 points. These correlations are also the most commonly used in literature for condenser design. The correlation  
 15 from Zhang et al. [13] was developed in our previous work [13]. Moreover, two pressure drop correlations  
 16 derived by Amalfi et al. [9] and Zhang et al. [13] were considered in the present study. Amalfi et al. [9] built  
 17 a database by collecting pressure drop data of evaporation in PHEs and derived a correlation using dimensional  
 18 analysis-based multiple regression. The correlation derived by Amalfi et al. [9] was evaluated as the one having  
 19 the best predictive performance by Tao and Ferreira [6].  
 20

21 The predicted values of the  $h_{\text{wf}}$  and  $\Delta p_{\text{fri}}$  using the selected existing correlations are shown in Figures 6 and 7,  
 22 respectively. Furthermore, a parameter, namely the mean absolute percentage deviation (MAPD), was  
 23 introduced to indicate the deviation between the predicted values using the selected correlation and the test  
 24 results, calculated by  
 25

$$26 \quad \text{MAPD} = \frac{1}{n} \sum_{i=1}^n \left| \frac{\text{data}_{i,\text{pred}} - \text{data}_{i,\text{exp}}}{\text{data}_{i,\text{exp}}} \right| \times 100\%. \quad (1)$$

26

27 The correlation derived by Yan et al. [14] shows the best agreement with the heat transfer data, resulting in a  
 28 MAPD of 15.2 %, but it provides a relatively weak prediction for the two HFOs, R1234ze(E) and R1233zd(E).  
 29 The correlation derived by Longo et al. [7] provides a reasonable prediction for most of the data with a MAPD  
 30 of 22.6 %. However, it underestimates almost all the results of R1233zd(E) and R1234ze(E) and the results of  
 31 isobutane at low mass fluxes. The Kuo et al. [8] correlation underestimates most of the experimental results,  
 32 with a MAPD of 33.6 %. The correlation from Amalfi et al. [9], though developed using the experimental data  
 33 from evaporation two-phase flow, was able to provide a reasonable prediction for the  $\Delta p_{\text{fri}}$  with a 27.9 %  
 34 MAPD, while slightly over-predicting the results of R245fa, R236fa and isobutane at high condensation  
 35 temperatures,  $70 \text{ }^{\circ}\text{C}$  to  $90 \text{ }^{\circ}\text{C}$ . The correlation derived by Zhang et al. [13] provides good predictions for all  
 36 working fluids with respect to both the  $h_{\text{wf}}$  and  $\Delta p_{\text{fri}}$ , but fails to predict the results of propane and isobutane.  
 37 This may be attributed to the fact that the thermo-physical properties of these two HCs are quite different from  
 38 those of the HFC and HFO working fluids involved in the database used to develop the correlation.  
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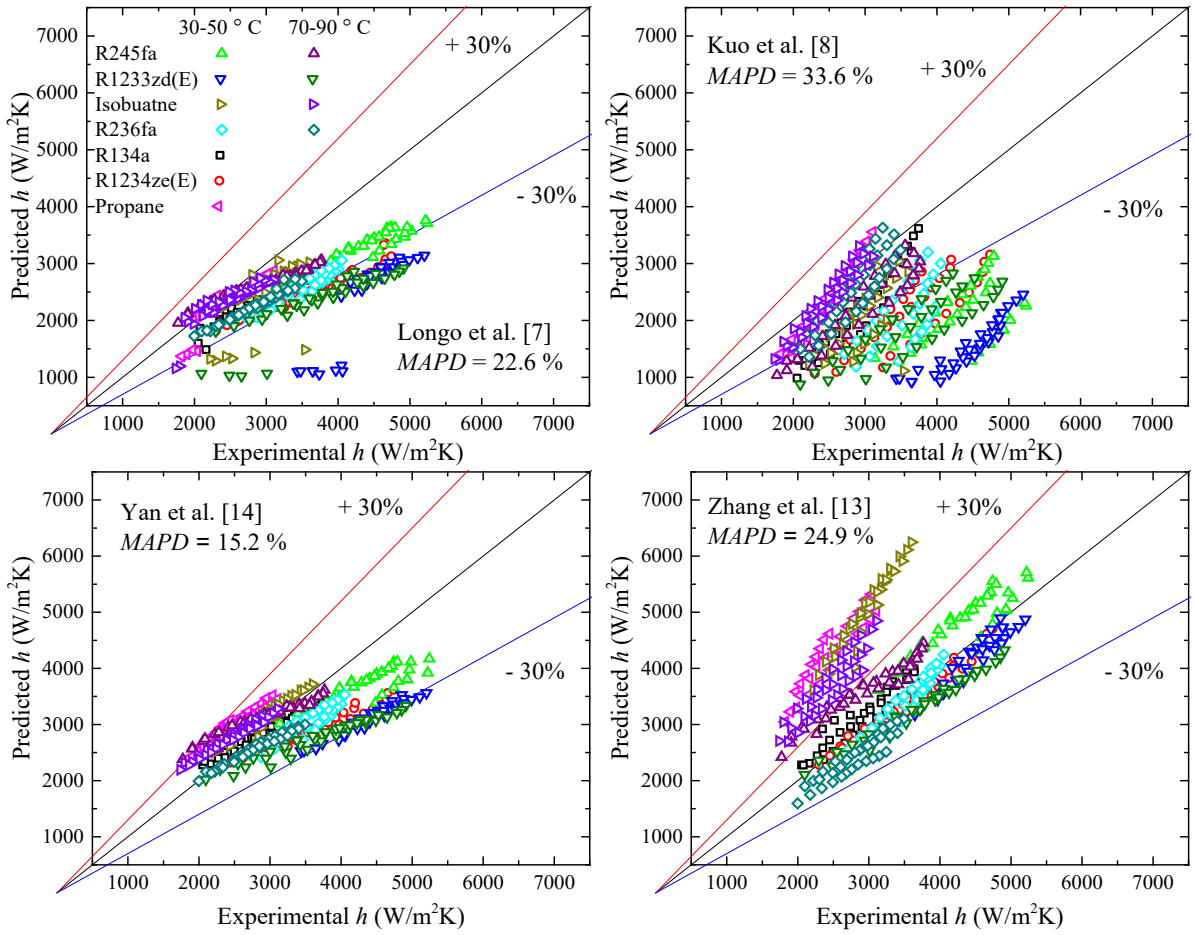


Figure 6. Predicted  $h_{wf}$  using the four selected correlations against the test results.

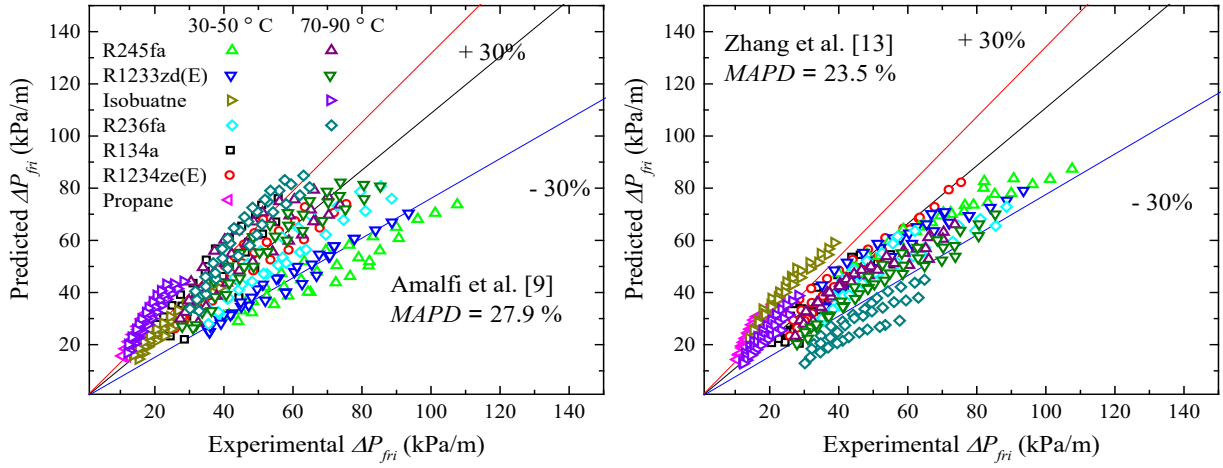


Figure 7. Predicted  $\Delta p_{fri}$  calculated by the two selected correlations against the test results.

### 3.4 New correlations

A new prediction method of heat transfer coefficient was developed in the present study, defined as

$$h_{wf} = 0.4703 Re_{eq}^{0.5221} Pr_1^{1/3} Bd^{0.1674} \rho^{*0.2126} (k_l/D_h), \quad (2)$$

where the hydraulic diameter  $D_h$  is defined as

$$D_h = 2b/\varphi, \quad (3)$$

where the  $b$  is the corrugation amplitude and the  $\varphi$  is the area enlargement factor caused by sinusoidal surface

1 waviness and is calculated by

$$\varphi = (1 + \sqrt{1 + \gamma^2} + 4\sqrt{1 + \gamma^2/2})/6, \quad (4)$$

3  
4 where the  $\gamma$  is a dimensionless corrugation parameter, defined as

$$\gamma = \pi b/\lambda, \quad (5)$$

6  
7 where the  $\lambda$  is the wavelength of surface corrugation

8  
9 Eq. (2) was derived by modifying the correlation from Yan et al. [14]:

$$\text{Nu} = 4.118\text{Re}_{\text{eq}}^{0.4}\text{Pr}_1^{1/3}, \quad (6)$$

11  
12 since it enables a best prediction for the experimental results among all selected correlations. Specifically, two  
13 dimensionless numbers, the density ratio ( $\rho^*$ ) and the Bond number (Bd), were added in the correlation with a  
14 multiple regression of test data. The density ratio represents the shear stress of the vapour phase acting on the  
15 liquid phase, while the Bond number represents the ratio of the gravitational force to the surface tension,  
16 accounting for the transition between macro-to-microscale two-phase flows. The Bond number is defined as

$$\text{Bd} = g(\rho_l - \rho_v)D_h^2/\sigma. \quad (7)$$

18  
19 The  $\text{Pr}_1$  is the Prandtl number of the liquid phase and the  $\text{Re}_{\text{eq}}$  is the equivalent Reynolds number, defined as

$$\text{Re}_{\text{eq}} = G_{\text{eq}}D_h/\mu_l, \quad (8)$$

21  
22 where the  $\mu_l$  is the liquid viscosity, and the equivalent mass flux  $G_{\text{eq}}$  is calculated by

$$G_{\text{eq}} = G[1 - x_m + x_m(\rho_l/\rho_v)^{0.5}], \quad (9)$$

24  
25 where  $x_m$  is the mean vapour quality of the working fluid over the whole condensation process in which the  
26 inlet vapour quality is 1 in this study.

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28 Likewise, a pressure drop correlation was derived by involving the density ratio and the Bond number:

$$f = 11557.62\text{Re}_{\text{eq}}^{-1.0041}\text{Bd}^{0.3002}\rho^{*-0.4268}. \quad (10)$$

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31 The basic format  $f = C\text{Re}_{\text{eq}}^n$  is commonly used for developing PHE two-phase correlations in the literature  
32 (e.g. [23,24]). The predicted  $h_{\text{wf}}$  and  $f$  calculated by Eqs. (2) and (10), respectively, were compared with the  
33 test results, shown in Figure 8. The comparison suggests that the new correlations are able to predict 98 % of  
34 both the heat transfer and pressure drop data within the  $\pm 30$  % bandwidth, having an 8.9 % and a 10.3 %  
35 MAPD, respectively. The ranges of the dimensionless numbers included in the correlations and the geometrical  
36 parameters of the PHE are presented in Table 3.

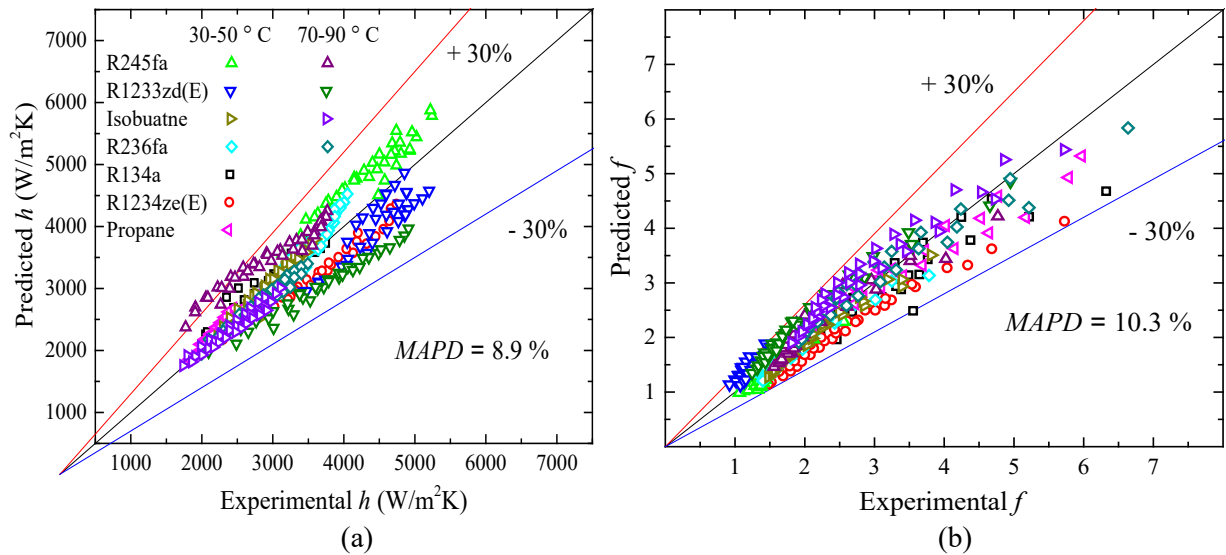


Figure 8. Comparison between the predicted values using the proposed correlations (Eqs. (2) and (10)) and the test results for (a)  $h_{wf}$  and (b)  $f$ .

Table 3 Ranges of the dimensionless numbers included in the correlations and the geometrical parameters of the PHE.

$Re_{eq}$	$Pr_l$	Bd	$\rho^*$	$D_h$	$\beta$
1237 to 5240	2.8 to 7.5	6.3 to 42.4	9.2 to 149.0	3.4 mm	65 °

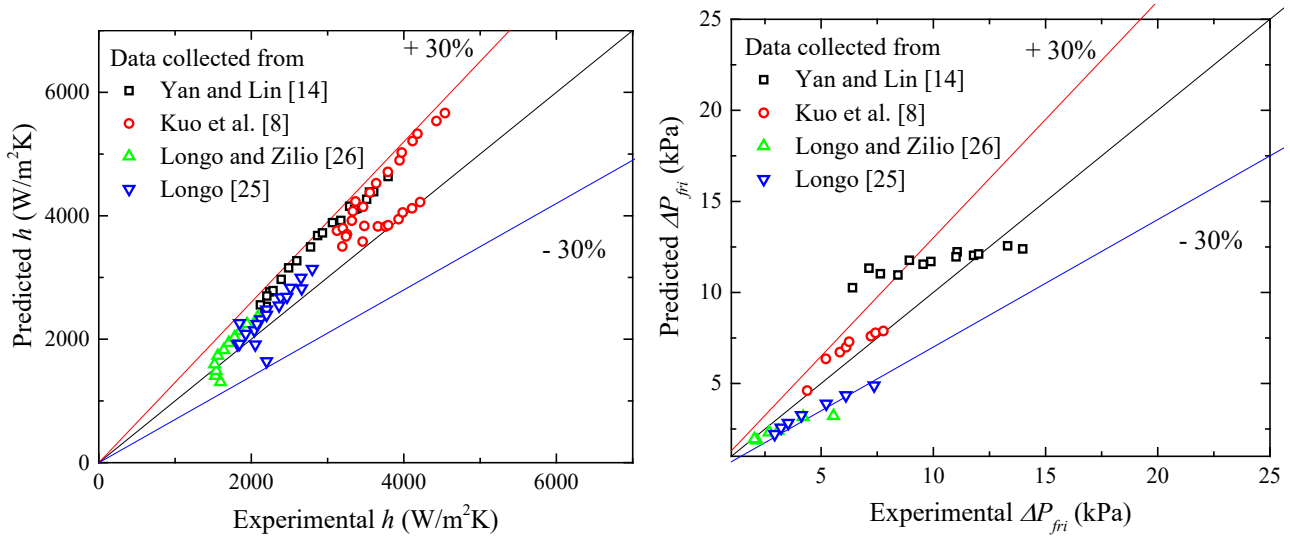
Table 4 Working conditions and PHE geometrical parameters used to obtain the experimental data in the previous research works, and MAPD, indicating the deviation between the predicted results calculated using Eq. (2) and Eq. (10) and the experimental results.

Study	PHE geometrical parameters						Working fluid	$T_{sat}$ (°C)	$G$ (kg/m²s)	Heat transfer process	MAPD (%)	
	$\beta$ (°)	$b$ (mm)	$\lambda$ (mm)	$D_h$ (mm)	$\phi$	$N^l$					Heat transfer	Pressure drop
Yan et al. [14]	60	3.3	10	5.4	1.23	3	R134a	27, 31 and 36	60	Partial condensation: $x_m = 0.11$ to 0.88	23.1	20.2
Kuo et al. [8]	60	3.3	10	5.4	1.23	3	R410a	20	50, 100 and 150	Partial condensation: $x_m = 0.10$ to 0.85	15.2	9.2
Longo [25]	65	2	8	3.5	1.14	10	Propylene	25 and 40	7 to 28	Complete condensation: $x_{in} = 0.95$ to 1 and $x_{out} = 0$ to 0.01	11.0	19.8
Longo and Zilio [26]	65	2	8	3.5	1.14	10	R1234yf	40	12 to 40	Complete condensation: $x_{in} = 0.95$ to 1 and $x_{out} = 0$ to 0.09	12.2	24.8
This study	65	2	7	3.4	1.18	16	R236fa, R245fa, R1233zd(E), Isobutane, R134a, R1234ze(E) and Propane	30, 40, 50, 70, 80 and 90	12 to 93	Complete condensation: $\Delta T_{sup} = 0$ to 5 K and $x_{out} = 0.01$ to 0.05	8.9	10.3

<sup>l</sup>  $N$ : number of plates in the tested PHE

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In order to further evaluate the applicability of the heat transfer and pressure drop correlations (Eq. (2) and Eq. (10)) developed in the paper, we used the correlations to predict four sets of experimental data collected from the previous research works. Table 4 summarizes the working conditions and PHE geometrical parameters of the four research works as well as the prediction results in terms of the MAPD. The first two sets of data collected from Kuo et al. [8] and Yan et al. [14] were obtained for partial condensation with the mean vapour quality of the condensation process varying from 0.10 to 0.88. The other two sets of data reported by Longo [25] and Longo and Zilio [26] were obtained for complete condensation, agreeing with our study, but using two working fluids not considered in our work, propylene and R1234yf. As shown in Table 4, the heat transfer correlation has MAPDs of 23.1 %, 15.2 %, 11.0 % and 12.2 % for the four sets of experimental data, respectively, while the pressure drop correlation has MAPDs of 20.2 %, 9.2 %, 19.8 % and 24.8 %, respectively. Figure 9 presents the predicted values calculated using Eq. (2) and Eq. (10) against the experimental data of previous works.



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Figure 9 Comparison between the predicted values using Eq. (2) and Eq. (10) and the experimental data collected from the previous research works [8,14,25,26].

#### 19 4. Discussion

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Although the correlations derived by Longo et al. [7] and Kuo et al. [8] have the best predictive performance for the database of 2376 heat transfer data points compiled by Tao and Ferreira [6], they fail to provide the best prediction for a much smaller database (283 data points) obtained in this study among selected existing correlations. This may be because each correlation targets different heat transfer processes. In the correlation derived by Longo et al. [7], the condensation heat transfer is considered to be in the gravity-controlled region as  $Re_{eq} < 1600$ , and the heat transfer of laminar film condensation in the region is calculated using the Nusselt equation. However, all the test data in this study, also including data points with  $Re_{eq} < 1600$ , belong to the shear-controlled region, demonstrated by a strong dependence of the heat transfer performance on the flow rate of the working fluids. The correlation from Kuo et al. [8] was developed from the partial condensation in which the  $x_m$  of the condenser is used as an important variable, ranging from about 0.1 to 0.9. This is different from a close to complete condensation applied in this study in which the mean vapour quality is always about 0.5. In addition, the discrepancy in evaluation results may be due to the differences in terms of mass fluxes and saturation temperatures in the databases. The database in this study includes data for a wider range of mass fluxes and higher saturation temperatures than the database compiled by Tao and Ferreira [6]. The contradiction in evaluation results indicates that a careful selection of the correlation based on the specific application is needed.

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The effects of the condensation temperature on the heat transfer process mainly result from the variation of the thermo-physical properties of the working fluids (e.g. the vapour density, density ratio of liquid to vapour phase and surface tension). The variation of temperature does not change the heat transfer mechanism, i.e. the convective condensation dominates the heat transfer process for the whole range of condensation temperatures in this study. Moreover, when using existing correlations that were developed using the data with relatively low condensation temperatures to predict the experimental results of a given working fluid, the prediction

1 accuracy is almost independent of the condensation temperature. This observation indicates that for the  
2 conditions of shear-controlled condensation, correlations can be applicable for temperatures that are out of the  
3 range of temperatures used for the correlation development. However, a wider range of temperature data will  
4 contribute to an increased reliability of extending the temperature applicability of the correlation.  
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6 The MAPD results presented in Table 4 indicate that the correlations developed in this study are able to predict  
7 the results of other works with a deviation of less than 30 % (except for a few data points for the pressure drop  
8 correlation), which is in agreement with engineering standard [5]. Specifically, the correlations are able to  
9 predict the results of other working fluids (propylene and R1234yf) than those used to derive the correlation.  
10 This may be attributed to the fact that working fluids covering a wide range of thermo-physical properties were  
11 used to derive the correlation. Furthermore, though the correlations were derived for experimental results of  
12 complete condensation, the comparison with previous works suggests that the correlations are able also to  
13 predict also the experimental results of partial condensation, covering only a narrow range of vapour quality  
14 between the condenser inlet and outlet.  
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16 Only one PHE was tested in the study, and thus the correlations were developed without considering the effects  
17 of PHE geometry on the thermal-hydraulic performance. A review work [27] found that the shear-controlled  
18 condensation is able to be enhanced by increasing the chevron angle of the corrugation. This is attributed to  
19 more turbulence in the flow caused by the larger chevron angle. The PHE used in the study has a relatively  
20 large chevron angle, 65 °, with respect to the range of chevron angles used in previous research works (27 °  
21 to 70 ° [27]), indicating that the heat transfer performances presented in the current paper are relatively high.  
22 In addition, the results of the limited comparison with previous works (see Table 4) suggests that the  
23 correlations are applicable also to other heat exchanger geometries. As shown in Table 4, the PHE geometrical  
24 parameters considered in Refs. [25,26] are almost identical to those of the PHE considered in our analysis,  
25 while the PHE used in Refs. [8,14] has larger dimensions than the PHE considered in our work. However, all  
26 the three PHEs can be categorized as small-scale heat exchangers. An evaluation of the applicability of the  
27 correlations for PHEs covering a wider range of geometrical parameters (e.g. large-scale channels and smaller  
28 chevron angles) remains to be done.  
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## 30 **5. Conclusion**

31 A comprehensive experimental investigation using seven organic fluids as working fluids and covering a wide  
32 range of condensation temperatures was conducted for developing the prediction methods of flow  
33 condensation in plate heat exchangers tailored specifically for organic Rankine cycle and heat pump systems.  
34 Four existing heat transfer correlations and two existing pressure drop correlations were used for predicting  
35 the experimental results obtained. New correlations were developed, considering two dimensionless numbers,  
36 the density ratio and the Bond number, accounting for the shear stress of the vapour phase on the liquid phase,  
37 the transition from macroscale to microscale two-phase flow and the surface tension effect.  
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39 The results suggest that the frictional pressure drop and heat transfer coefficient both increase with the increase  
40 of mass fluxes and decrease with the increase of condensation temperatures, indicating that shear-controlled  
41 condensation is dominating in the whole range of working conditions. Due to the lower vapour density and  
42 higher surface tension, and hence the more intensified convection at the liquid-vapour interface, R1233zd(E),  
43 isobutane and R245fa have a higher heat transfer coefficient than the other working fluids. Moreover,  
44 R1233zd(E), R236fa and R245fa have a higher frictional pressure drop due to their larger density ratio of  
45 liquid phase to vapour phase. The correlations derived by Yan et al. [14] and Zhang et al. [13] provided the  
46 best prediction for the heat transfer coefficient and frictional pressure drop with a mean absolute percentage  
47 deviation of 15.2 % and 23.5 %, respectively. Moreover, the results suggest that improved prediction  
48 accuracies are achieved with the new correlations, giving a mean absolute percentage deviation of 8.9 % and  
49 10.3 % for the heat transfer coefficient and the frictional pressure drop, respectively. A comparison with results  
50 of previous works indicates that the developed correlations are able to predict with reasonable accuracy the  
51 results of previous works considering other work fluids, heat exchanger geometries and operating conditions  
52 than those used to derive the correlations. Finally, it needs to be stressed that the correlations developed in the  
53 paper were obtain for a single plate heat exchanger geometry. The results of the limited comparison of the  
54 correlations with previous works suggests that the correlations are applicable also to other heat exchanger  
55 geometries, however, a thorough evaluation of the heat transfer and pressure drop correlations' applicability  
56 to plate heat exchangers covering a broad range of geometrical parameters remains to be done.  
57



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