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PostPrint

Preliminary assessment of increased main engine load as a consequence of added wave resistance in the light of minimum propulsion power

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Abstract

This paper addresses the connection between added wave resistance and required propulsion power of ships, having focus on the early stage of new ship designs, notably tankers and bulk carriers. The paper investigates how mean added wave resistance affects the required torque of a fixed pitch propeller and thus also the operational conditions of a directly coupled main engine. The interest of the study has its background in the assessment of minimum propulsion power, and the study considers the prescriptive guidelines of the IMO as basis. Specifically, the study focuses on an assessment of the minimum forward speed attainable under consideration of the propeller light running margin and static load limits of engines in the early phase of new ship designs, where details of hull geometry are not available. The study considers three semi-empirical methods for predicting mean added wave resistance. All methods are known to be applied in the industry, emphasising that only methods relying solely on main particulars, together with information about sea state and advance speed, are of interest. The paper contains a case study used to illustrate the importance of the added wave resistance prediction with respect to the loading of the main engine. It is shown that, despite small absolute differences, the consequence in relation to the loading of the propeller and hereby the directly coupled main engine can be relatively large. Furthermore, the study illustrates that the propeller light running margin of a fixed pitch propeller directly coupled to the main engine has crucial influence on the attainable speed during adverse weather conditions.

Keywords:

Minimum propulsion power, engine load diagram, propeller light running margin, added wave resistance, semi-empirical methods

1. Introduction

The International Maritime Organization has released interim guidelines [1] on minimum propulsion power (MPP) for bulk carriers and tankers equipped with fixed pitch (FP) propellers. The guidelines are results of the tendency to reduce the power of the main engine installed on new ships; noting that a reduction in power allows the ship to attain a better energy efficiency design index (EEDI) [2], without changing from traditional fuel. However, the reduced main engine power may lead to a lower forward speed in adverse weather resulting in an increased risk of losing manoeuvrability during encounters of heavy weather: The resistance from wind and waves may increase the torque required by the FP propeller to such an extent that the operational point (torque vs. rpm) continuously falls outside of the static load diagram of the typical prime mover, i.e. a two-stroke low speed marine engine, ultimately resulting in a reduction of engine speed. In such conditions, the advance speed drops and, ultimately, the ship may be prevented from steering into the dominant wave direction or even maintain a forward speed sufficient for keeping its course.

The present study, in line with assessment level 2 of the IMO guidelines on MPP [1] as described in the following section, focuses on a utilisation of three methods for estimating mean added wave resistance in head seas in order to predict the forward speed attainable under consideration of the static load limits of a main engine directly coupled to a FP propeller. This sole evaluation of the attainable minimum forward speed represents a simplified assessment of the complex situation of manoeuvring in adverse weather conditions. By this simplified approach, no considerations are given to a ship's capability to steer into the dominant wave direction, nor to dynamic limits of the directly coupled main engine, effects of dynamic propeller ventilation, wake fraction fluctuations, etc. Such effects are not considered in the present study, as the focus lies on an early evaluation of a design's compliance with [1]; but it is noteworthy that all effects are important to consider later in the design spiral, when the exact hull design, propeller, and main engine are known, thus making manoeuvring simulations or wave tank tests possible.

The focus of this study is solely on FP propellers and the effects of added wave resistance towards the operational point of the directly coupled main engine; that is, the study does not consider controllable pitch (CP) propellers. Although a CP propeller in theory can load a directly coupled main engine at any point within the engine load diagram in any condition and provides advantages with respect to manoeuvrability, FP propellers - as a result of higher efficiency and

31 lower cost - dominate the segment of larger merchant vessels performing week- or month-long ocean
32 crossings.

33 *1.1. Minimum propulsion power*

34 As indicated, the MPP guidelines [1] are in place to evaluate the design of new ships with respect
35 to required main engine power.* Essentially, the guidelines distinguish between two assessment
36 levels, where the ship should be considered to have sufficient power to maintain the manoeuvrability
37 in adverse conditions if it fulfils one of these assessment levels. Assessment level 1 relates the
38 requirement for MPP to the capacity of the ship in deadweight tonnage (DWT) through the
39 simple expression: $MPP = a \times DWT + b$, with coefficients a and b defined by [1].

40 Assessment level 2 constitutes an evaluation of the torque reserve between the main engine load
41 limits and the light (design) propeller curve, rather than an evaluation of maximum power installed.
42 Thus, on the basis of the mean added resistance resulting from the prescribed sea state for, it is
43 evaluated if the increase of required torque of the FP propeller can be maintained/ensured within
44 the static load limits of the main engine. The simplified principle of the assessment is that, if the
45 propulsion plant can provide the required torque to propel the ship with a certain advance speed
46 in head waves and wind, the ship will also be able to keep course in waves and wind from any other
47 direction. The minimum ship speed of advance in head waves and wind is thus selected depending
48 on ship design, in such a way that the fulfilment of the ship speed of advance requirements means
49 fulfilment of course-keeping requirements [1]. As a result, all resistance components (i.e., bare
50 hull resistance in calm water, resistance due to appendages, aerodynamic resistance, and added
51 resistance due to waves) must be determined when assessment of MPP is made in accordance with
52 level 2.

In accordance with [1], the minimum forward speed required to ensure course keeping is in the
range 4-9 knots, depending on the ratio between frontal and lateral wind area and relative rudder
area. Based on a ship's length between perpendiculars L_{pp} , level 2 of the MPP-guidelines defines
two 'limiting sea states' as adverse conditions, in which the minimum forward speed is to be kept.

*The guidelines are initially for EEDI Phase 0 and 1, but are expected to be extended to include Phase 2 and
Phase 3, possibly in a modified form.

The criteria for the significant wave height H_s and mean wind speed V_{wind} are:

$$L_{pp} < 200 \text{ m: } H_s = 4.0 \text{ m and } V_{wind} = 15.7 \text{ m/s} \quad (1)$$

$$L_{pp} > 250 \text{ m: } H_s = 5.5 \text{ m and } V_{wind} = 19 \text{ m/s} \quad (2)$$

53 where values are to be linearly interpolated for $200 \leq L_{pp} \leq 250$ m. Furthermore, assessment level
54 2 requires that MPP is calculated for a range of wave spectra, by varying the peak wave periods
55 from 7.0 s to 15.0 s. The intervals of significant wave heights and wind speeds to be considered
56 imply that two categories of ships are especially challenged: Ships of just $L_{pp} = 250$ m, and smaller
57 ships of 20,000 DWT where the EEDI-requirements are full in phase for tankers and bulk carriers
58 [2]. These smaller ships are typically significantly shorter than $L_{pp} = 200$ m, and therefore they
59 will experience the relatively most severe sea state.

60 As the MPP requirement set by assessment level 1 often returns values which hinder tradition-
61 ally fueled ships in attaining compliance with EEDI Phase 2, an increase in designs that will have
62 to be evaluated at assessment level 2 is expected. On a side note, it is assumed that traditional
63 fuels continue to dominate the new-building market and concerns about MPP are thus believed to
64 be relevant throughout the next decade(s).

65 As pointed out above, in assessment level 2, the capabilities of the specific propulsion plant
66 are considered relative to the total resistance on the ship. At low to vanishing speed in a severe
67 sea, the added wave resistance will often be the major resistance component, especially for smaller
68 ships. The added wave resistance on a ship can be computed if the associated transfer functions
69 are available; and the MPP-guidelines require that the transfer functions are derived from model
70 tests as per ITTC procedures [3, 4]. However, since model-scale tests can only be performed late
71 in the design stage, uncertainty regarding a ship's performance in adverse conditions will be large
72 in the early design phases, where the detailed hull geometry is not available. This concern has
73 been reflected by debates about making updated MPP-guidelines in which model-scale tests can
74 be replaced by a simple and reliable numerical model for estimation of the added wave resistance,
75 recognising that the variation of main particulars and characteristic coefficients within the popula-
76 tion of bulk carriers and tankers is limited. One approach to this has been proposed to the MEPC
77 [5] based on joint work between SHOPERA[†] and the Japan Society of Naval Architects and Ocean

[†]Energy Efficient Safe SHip OPERATIONS, see more at <http://shopera.org/>

78 Engineers; however, the sea state in which the ship is to be able to maintain safe manoeuvring
79 could not be agreed on. A description of the work by SHOPERA [5, 6] is given in Section 2.1.2.

80 *1.2. Scope and novelty of study*

81 This study considers three semi-empirical numerical methods for predicting added wave resis-
82 tance on ships; emphasising that the methods - as a constraint - take just the ship's main particulars
83 as input. This means that the methods are useful for early resistance prediction in the design phase
84 of ships, where detailed hull lines will not be available. The methods, which will be presented in
85 some detail in Subsection 2.1, are the STAwave-2 method, the SHOPERA equation, and the DTU
86 Design Tool where the latter is a computational method developed at the Technical University of
87 Denmark.

88 The paper presents a small sensitivity study, where the three methods for added wave resis-
89 tance prediction are directly compared by studying the influence of various input parameters, such
90 as advance speed and draught. The main achievement of the paper is a case study focused on
91 the relation between added wave resistance, propeller light running margin, and MPP for three
92 example ships. In the case study, the propeller's operational point is predicted for a given ship
93 in various sea states; thus leading to an assessment of the operational points of the propeller in
94 relation to the load limits of the main engine, and hereby returning a prediction of the forward
95 speed that the ship can maintain in the given sea state. Indeed, the novelty of the study is the
96 combined engineering considering resistance, propulsion, operational conditions, *and* engine load-
97 ing altogether in a preliminary assessment of MPP for a ship sailing in a given sea state; all of it
98 considered from a practical perspective.

99 It seems relevant to mention that [7] contains a study that has some similarity to the present
100 work. In [7], the focus is on the need for resistance estimation considering design of ships with
101 special attention to added wave resistance, however, without the particular concerns related to
102 minimum propulsion power and propeller light running margin, as discussed in the present paper.

103 *1.3. Composition of paper*

104 The paper contains five sections in total, and the contents of the four remaining sections are
105 summarised in the following. Section 2 presents the theoretical background and the methodology
106 of the study. Section 3 contains the comparisons of the numerical methods used for the prediction

107 of added wave resistance. The practical relevance of the study is exemplified in Section 4 by
108 a numerical case study focused on an evaluation of the operational points (power and rpm) in
109 relevant sea states, relative to the engine load diagram, as provided by a designer of two-stroke
110 main engines. Finally, conclusions and suggestions for future research and topics to consider in the
111 legislation are given in Section 5.

112 **2. Theoretical Background and Methodology**

113 This section outlines the basics of added wave resistance on ships together with the numerical
114 methods later compared. The section also includes a description related to the estimation of
115 the *total* resistance on a ship in a seaway. Moreover, the section gives an overview of the most
116 fundamental aspects in connection with ship propulsion. The latter parts, regarding total resistance
117 and propulsion, will be used in the numerical case study focused on an evaluation of minimum
118 propulsion power according to assessment level 2 for given ship design and main engine including
119 the associated load diagram. Note, at most places, the physical parameters and symbols used in
120 the stated formulas are defined in the main text along with the actual mathematical expressions,
121 but for convenience Table 1 summarises the complete list of the most important symbols.

122 *2.1. Predicting added resistance in waves*

123 Added wave resistance on a ship is a result of the forces associated with diffraction and reflection
124 of waves around the hull together with radiation of waves because of ship motions due to the wave
125 excitation loads. The literature about added resistance in waves is wide, and the references [8, 9, 10]
126 are all useful to obtain a sound background on the topic. On the other hand, this paper has no
127 intention to carry out detailed numerical calculations of added wave resistance for what reason
128 reference to the huge special literature, notably on CFD-based studies, is excluded.

129 Generally, added wave resistance on a ship can be represented by a transfer function $\Phi(\omega)$,
130 which expresses the response per unit wave amplitude as function of wave frequency ω or wave
131 length λ . A qualitative example is shown in Figure 1 where L is the length of the ship and B is the
132 breadth, while ρ and g are the density of water and the acceleration of gravity, respectively. The
133 domain of resistance due to diffraction of the incident wave (bow wave reflections) and the domain
134 of radiation due to ship motions are also roughly indicated in the figure. It is seen that the added

Table 1: Parameters relevant for the estimation of added wave resistance.

Symbol	Description	Unit
\bar{R}_{AW}	Mean added wave (AW) resistance	N
$\Phi_{AW}(\omega)$	Transfer function of added wave resistance	N
$S(\omega)$	Wave spectrum density	m ² s/rad
ρ	Water density	kg/m ³
g	Acceleration of gravity	m/s ²
ω	Angular wave frequency (absolute)	rad/s
$\bar{\omega}$	Angular wave frequency (encountered)	rad/s
ζ_A	Wave amplitude	m
λ	Wave length	m
k	Wave number	rad/m
H_s	Significant wave height	m
T_1	Mean wave period	s
L_{pp}	Length between particulars	m
T_M	Draught amidships	m
B	Breadth	m
C_B	Block coefficient	-
Fr	Froude number	-
V_S	Ship's speed-through-water	m/s
r_{yy}	Pitch radius of gyration	m
$I_1(x)$	Modified Bessel function of the first kind of order 1. <i>x</i> is the argument	-
$K_1(x)$	Modified Bessel function of the second kind of order 1. <i>x</i> is the argument	-

135 wave resistance attains a maximum in the frequency range dominated by radiation of waves due
 136 to movements of the ship. Typically, the peak value is found around $\lambda/L \approx 1$.

Based on the transfer function, it is possible to describe the added wave resistance in an irregular sea using the wave energy (density) spectrum. Thus, if the sea state is described by a wave energy spectrum $S(\omega)$, the mean added resistance \bar{R}_{AW} , in the surge direction, can for constant speed and (wave) heading be determined by Eq. (3), cf. [9]. Here, the transfer function $\Phi_{AW}(\omega)$ for the added wave resistance is normalised by the square of the wave amplitude ζ :

$$\bar{R}_{AW} = 2 \int_0^\infty S(\omega) \frac{\Phi_{AW}(\omega)}{\zeta^2} d\omega \quad (3)$$

137 The main concern about Eq. (3) is that the calculation of the transfer function requires detailed
 138 information about the considered ships's hull lines, which are rarely available in the design stage
 139 in connection with assessment of (minimum) propulsion power. In terms of the MPP-guidelines
 140 [1], the requirement is, in fact, one step beyond, since accordingly the transfer function must
 141 be obtained from model-scale tests. However, in the early phases of ship design, it is beneficial

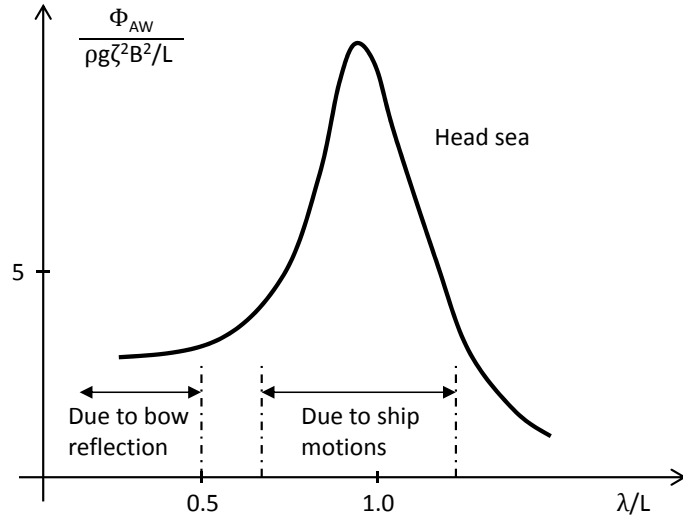


Figure 1: Principal illustration of the non-dimensionalised transfer function for added wave resistance in head seas as a function of the ratio between wavelength and ship length. With inspiration from [9].

142 to rely on method(s) taking just a limited number of variables as input; for instance, the main
 143 particulars of the hull together with a specification of the operating conditions including sea state.
 144 In the following, consideration is therefore only given to such formulas, as they may be useful when
 145 new ship designs are investigated with respect to (minimum) propulsion power; especially when
 146 added wave resistance is the major component as is the case for smaller ships at low to vanishing
 147 speed in severe seas. On a side note, it can be mentioned that "intermediate" approaches for
 148 predicting added wave resistance exist. Thus, the appendix of [5], taken from [11], contains a
 149 method that can be used to determine a quadratic transfer function. This method resembles that
 150 of STAwave-2, see below, but requires additional information about the waterline of the vessel.
 151 Similarly, the experimentally-based study [12] facilitates a relatively simple formula, derived from
 152 regression analysis, for the estimation of added wave resistance when knowledge about the waterline
 153 is available (or assumed). In future studies, it should be interesting to include predictions based
 154 on these methods. However, in the present work, the actual accuracy, in absolute terms, of the
 155 models is not the central topic but rather it is the influence on the calculation of the loading of the
 156 main engine, as illustrated in the case study in section 4.

157 *2.1.1. STAwave-2*

158 The STAwave methods 1 and 2, as initially introduced by [13], were developed in order to correct
159 for the effect of waves during sea trials. STAwave-1 corrects only for the reflection contribution to
160 added wave resistance, and it is required that the ship does not pitch nor heave; thus radiation is
161 neglected. Because of this fact, STAwave-1 is not given any further attention in the present study,
162 since adverse weather conditions are of interest only. On the other hand, STAwave-2 considers
163 both reflection and radiation and, as shown below, closed-form expressions are formulated for the
164 transfer functions of both parts.

165 As mentioned, STAwave-2, e.g. [14, 15], is primarily used for the correction of sea trial data, and
166 thus low Froude number evaluations have not been included in the model tank test scheme upon
167 which the method is developed. Therefore, usability in a study focused on MPP is challenged by
168 a requirement that $Fr > 0.10$. This limitation is *not* set due to physical reasons but, as indicated,
169 due to the omission of data to perform a regression at lower Froude numbers. For the contribution
170 from wave reflection, the lower Froude number is not expected to influence the calculated value:
171 The low(er) encounter frequency, resulting due to low(er) forward speed, is not critical to the
172 magnitude of resistance from reflection as this contribution is constant. For the contribution from
173 radiation, resulting from ship motions, the situation is different as the application of a lower Froude
174 number in the regression equations will shift the peak value of the transfer function towards ratios of
175 $\lambda/L_{pp} < 1$ which is not in line with theory, e.g. [9, 10], nor in line with the original description [13].
176 One solution to this problem, from a practical point of view, is to include a correction factor that
177 adjusts, i.e. increases, the value of the pitch radius of gyration with decreasing Froude number,
178 in order to "relocate" the peak of the transfer function. This adjustment is nonphysical, but
179 corrects the regression-based transfer function to attain its well-known characteristics with a peak
180 located close to $\lambda/L_{pp} = 1.0$. Despite the non-physical character of this correction, the method of
181 STAwave-2 is included since it is known to have seen application in the industry[‡], even without the
182 correction factor. Clearly, it would be of interest to carry out validation of the corrected estimate
183 with experimental results at low(er) speed. While this is out of scope from the present study, it
184 has indeed interest as a future exercise. In the present study, the consequence of the introduced
185 modification to the STA2 method is investigated from a numerical perspective only; this happens

[‡]This has been observed by the first author in connection with development projects with industrial partners.

186 in the sensitivity study in Section 3, see also Figure 2, where methodical comparisons are made
 187 with the other semi-empirical methods.

As already stated, the STAwave-2 method formulates closed-form expressions for the transfer function for the added wave resistance. Subsequently, the transfer function is combined with a wave energy spectrum to determine the mean added wave resistance. The (parametric) transfer function $\Phi_{AW}(\omega)$ takes the form:

$$\Phi_{AW} = \Phi_{AW,RL} + \Phi_{AW,ML} \quad (4)$$

where $\Phi_{AW,ML}$ is the part due to wave-induced motions while $\Phi_{AW,RL}$ is due to wave reflections. The formulas of the two parts are given by,

$$\Phi_{AW,ML} = 4\rho g \zeta_A^2 \frac{B^2}{L_{pp}} \bar{r}_{aw}(\omega) \quad (5)$$

$$\Phi_{AW,RL} = \frac{1}{2} \rho g \zeta_A^2 B \alpha_1(\omega) \quad (6)$$

The definitions of the individual parameters are listed in the following, and Table 1 contains descriptions of those parameters that have a direct physical meaning:

$$\bar{r}_{aw}(\omega) = \bar{\omega}^{b_1} \exp\left(\frac{b_1}{d_1}(1 - \bar{\omega}^{d_1})\right) \cdot a_1 Fr^{1.50} \exp(-3.50Fr) \quad (7)$$

$$\bar{\omega} = \frac{\sqrt{\frac{L_{pp}}{g}} k_{yy}^{1/3}}{1.17 Fr^{-0.143}} \omega \quad (8)$$

$$a_1 = 60.3 C_B^{1.34} \quad (9)$$

$$b_1 = \begin{cases} 11.0, & \bar{\omega} < 1 \\ -8.5, & \bar{\omega} \geq 1 \end{cases} \quad (10)$$

$$d_1 = \begin{cases} 14.0, & \bar{\omega} < 1 \\ -566 \left(\frac{L_{pp}}{B}\right)^{-2.66}, & \bar{\omega} \geq 1 \end{cases} \quad (11)$$

$$\alpha_1(\omega) = \frac{\pi^2 I_1^2(1.5kT_M)}{\pi^2 I_1^2(1.5kT_M) + K_1^2(1.5kT_M)} f_1 \quad (12)$$

$$f_1 = 0.692 \left(\frac{V_S}{\sqrt{T_M g}}\right)^{0.769} + 1.81 C_B^{6.95} \quad (13)$$

188 It is noted that the transfer function is given as function of absolute frequency ω . However,
 189 implicitly the formulas depend on the vessel forward speed relative to wave propagation (direction
 190 and phase velocity of the waves), and the encounter frequency $\bar{\omega}$ is therefore introduced in Eq. (8).

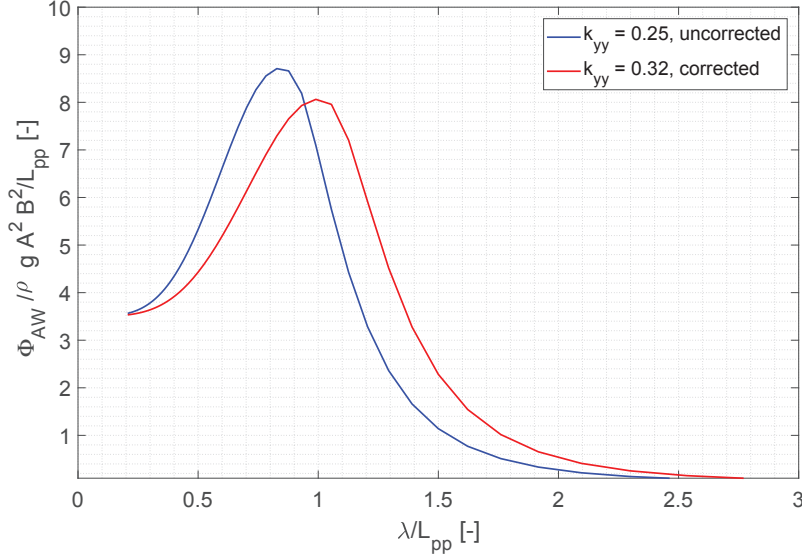


Figure 2: Transfer function estimated by STAwave-2, with and without correction of k_{yy} , for a 27,000 DWT tanker ($L_{pp} = 160$ m) at a speed of 6 knots.

191 From the formulas, and Table 1, it is noted that the transfer function can be calculated with
192 information only about the main particulars and the non-dimensional pitch radius of gyration
193 $k_{yy} = \frac{r_{yy}}{L_{pp}}$, which often is approximated by $k_{yy} = 0.25$, e.g. [16]. The application of the transfer
194 function is limited to the following conditions, cf. [15]: $L_{pp} > 75$ m, $4.0 < L_{pp}/B < 9.0$, $2.2 <$
195 $B/T_M < 9.0$, $0.10 < Fr < 0.30$, $0.50 < C_B < 0.90$, and relative wave direction is within 0 deg to \pm
196 45 deg off-bow, emphasising that the speed restriction is relaxed in the present study by correcting
197 the pitch radius of gyration. An example of the influence of the correction to the pitch radius of
198 gyration is illustrated in Figure 2 for a tanker of $L_{pp} = 160$ m at 6 knots, i.e. $Fr = 0.08$. It can be
199 appreciated that the peak is shifted to a larger wave length, roughly at $\lambda/L_{pp} = 1$. In this context,
200 it is interesting to note that results in [7] in fact suggest that the peak of STAwave-2, in its original
201 formulation without the modification of k_{yy} , also for higher speeds ($Fr \approx 0.15$) likely is located
202 at a too small wave length relative to experimental results and the method developed in [17]. In
203 other words, a finding that indicates a need to shift the location of the peak to a larger wave
204 length which, as seen herein, can be achieved by modifying the pitch gyration radius. Additional
205 discussions about the effect of the correction have been given by [18], and a few remarks are also
206 given in Sections 3 and 4 where results of STAwave-2 are compared to results obtained by the
207 other methods for predicting the mean added wave resistance.

208 From the transfer function given in Eq. (4), the mean resistance increase due to long-crested
 209 head waves is given by Eq. (3). Note that any increased usage of the rudder in adverse conditions
 210 is not accounted for.

211 2.1.2. SHOPERA

The SHOPERA project was launched by the EU in response to the implementation of EEDI and associated concerns on MPP. The estimate of added wave resistance, developed as an outcome of the SHOPERA project, is in this study included in a modified form proposed to the MEPC in [5]. The formula for the mean added resistance in waves is given by,

$$\bar{R}_{AW} = 1336(5.3 + V_S) \left(\frac{B \cdot T_M}{L_{pp}} \right)^{0.75} H_s^2, \quad [\text{N}] \quad (14)$$

212 where the parameters are defined in Table 1. The details of the empirical relation are given by [6],
 213 but it is noteworthy that the formula is based on numerical evaluations of transfer functions using a
 214 Rankine panel method for resistance estimates of 50 bulk carriers, tankers and general cargo ships
 215 with main particulars limited by: $90\text{m} < L_{pp} < 320\text{m}$, $5.0 < L_{pp}/B < 7.9$, $2.0 < B/T_M < 3.3$,
 216 $0.78 < C_B < 0.87$. In addition, the following constraints apply: $0 < V_S < 8.0$ knots, and relative
 217 wave direction is within 0 deg to ± 30 deg off-bow.[§] To calculate the magnitude of the added
 218 resistance, a JONSWAP wave spectrum has been used by [6]. No direct explanation is given to
 219 this choice but, in general, focus in the project is/was on a ship's capability to weather-wane in
 220 areas close to the coast and, hence, it makes sense to consider a fetch-limited ocean wave spectrum.

221 As indicated by the constraints on the hull-parameters, the method of SHOPERA is established
 222 based on a regression of simulation results of hulls of very specific characteristics focused on tankers
 223 and bulk carriers. These ship types are accessed most likely to experience problems with MPP under
 224 the EEDI-scheme, and the calculations (and the resulting formula) are based on ships designed to
 225 fulfil EEDI phase 2, [6]. It is clear that the accuracy of the Rankine code is fundamental to the
 226 reliability of the formula, cf. Eq. (14). [19] has studied the performance of the specific code and
 227 make an evaluation of the motions predicted on deep water while [20] performs an evaluation of the
 228 motions predicted on shallow water. Both studies find good correlation to experimental results.
 229 However, as noted by [21], prediction of ship motions is only one step towards predicting the added

[§]In fact, [6] specifies ± 60 deg, while ± 30 deg is the range given in [5].

230 wave resistance, and a good prediction of the motions themselves does not necessarily guarantee
231 a good resistance estimate. A comparison of Eq. (14) with actual operational data is therefore
232 highly relevant, although this is left as a future exercise.

An important addition to Eq. (14) is the inclusion of added resistance arising from an increased usage of the rudder required to keep the course during adverse weather conditions. The magnitude of resistance from increased rudder usage, also known by *steering resistance*, is simply given as a function of the delivered thrust T , cf. [5],

$$R_{rud} = 0.03T \quad (15)$$

233 The SHOPERA method is as such the only method of the three methods included in the present
234 study, which specifically includes an increase of steering resistance in heavy weather. It is note-
235 worthy that the 'SHOPERA estimate' is stated to be conservative [6]. Thus, the result of Eqs.
236 (14) and (15) in combination is adjusted to return values greater than the individual results of the
237 numerical simulations upon which the method is based.

238 As a final remark - and as a word of caution - about the empirical formula expressed by Eq.
239 (14), it is a concern that the right-hand side of the equation is not dimensionally consistent. This
240 makes it difficult to properly assess the equation with regards to its physical variables and their
241 influence on the value of the result. It is not the role of the authors to criticise this problem, but it
242 is remarkable that the analysis of the data upon which the equation has been based is not reflecting
243 a rigorous dimensional analysis [22]. ¶

244 2.1.3. DTU Design Tool

245 The main purpose of the computational tool is to make potential flow calculations available
246 in the early phase of new ship designs. All the details of the tool are given in [23, 24], and the
247 following is just a brief outline.

248 The tool takes as inputs the ships's main dimensions: length L_{pp} , breadth B , draught T ,
249 together with the block coefficient C_B and advance speed V_S . Based on these inputs, the tool
250 interpolates linearly in a large set of pre-calculated transfer functions computed using potential
251 flow calculations on a series of reference geometries in the range of length-to-breadth ratios $4.0 <$

¶The discussions with an anonymous reviewer about the Buckingham PI theorem (used for dimensional analysis) is appreciated.

252 $L_{pp}/B < 8.0$ and breadth-to-draught ratios $2.0 < B/T_M < 5.0$. The reference calculations have
253 been performed at a range of Froude numbers from 0 to 0.25, in between which linear interpolation
254 is performed for the exact Froude number based on the ship's actual speed and length. The
255 tool applies two different methods to determine the transfer function for added wave resistance
256 depending on the ratio between the encounter-wave length and the length of the hull: For relatively
257 long waves, Salvesen's method [25] is applied, and for shorter waves Faltinsen's asymptotic method
258 [26] is used.

259 It is noteworthy that the tool can be inaccurate at near zero forward speed and in beam to
260 following seas, cf. [25]. Specifically, this situation may occur if the body potential is not small
261 compared to the potential of the incident wave. According to [1], the ship speed is required not
262 to drop below 4 knots, and, as only head (to beam) seas are considered, the tool is expected to
263 be sufficiently accurate; at least for application within a study focused on MPP. It is also worth
264 noticing that Faltinsen's asymptotic method is sensitive to the shape of the bow, and returns the
265 highest values for blunt bow shapes. The DTU Tool does not account directly for this but, based
266 on the block coefficient provided as input, the tool interpolates in high and low C_B -databases of
267 hulls with bow-shapes typical for the given block coefficient.

268 In order to calculate the mean added resistance, the (interpolated) transfer function must be
269 combined with a wave spectrum, cf. Eq. (3), and the tool offers a choice between a Bretschneider
270 and a JONSWAP spectrum together with inputs of significant wave height and a characteristic
271 wave period such as the mean or the zero-upcrossing period.

272 2.2. Estimating the total resistance on a ship in a seaway

273 The total resistance exerted on a ship sailing in waves is the sum of the calm-water resistance
274 and a number of extra contributions, including added wave resistance, that occur because of various
275 phenomena. Together with the added wave resistance, the additional resistance components are:
276 Wind resistance, increased steering resistance, and possibly shallow water effects. Furthermore,
277 hull fouling and stabilizer fins, if present/applied, leads to an increase in the total resistance. In
278 principle, *all* resistance components should be included when estimating the necessary propulsion
279 power of a ship. However, focusing explicitly on *minimum* propulsion power, the guidelines [1]
280 consider just the calm-water resistance with the hull as in sea trial condition, and added resistance
281 from wind and waves. The reason is that ship speed is low to vanishing and, as a result, these

282 components are usually the most relevant; especially for the considered segments of ship types
283 and sizes (bulk carriers and tankers). The calculation methods for added wave resistance were
284 presented in the preceding sections. Below, a few remarks about the calculation of the calm-water
285 resistance and the wind resistance are given.

286 *2.2.1. Calm-water resistance*

287 For a given ship, it is common practice to calculate the calm-water resistance by use of model-
288 scale towing-tank tests, as suggested in the ITTC-1978 Method, e.g. [27]. If towing-tank tests
289 are not available, like in the early design phase of a ship, alternative methods can be applied to
290 estimate the calm-water resistance, as suggested by [28] and [29]. In the present study, the calm-
291 water resistance is predicted by the method by [28], estimating the calm water resistance based
292 on a series of regression based coefficients, taking input on main particulars, length-displacement
293 ratio, and the prismatic coefficient. Effects of the position of the longitudinal centre of buoyancy
294 is neglected in this consideration of the early design stage. In the present study, the updated
295 coefficients as established by [30, 31] has been implemented for the calculation of the coefficients
296 to reflect statistics for more recent ships. Note that the estimate by [28] as applied in the present
297 study, includes frictional resistance, air resistance, appendage resistance, steering resistance and
298 residual resistance composed of wave making resistance and viscous pressure resistance.

299 *2.2.2. Wind resistance*

300 The wind resistance depends on the relative wind speed and direction, and the projected
301 windage area of the ship. In this study, the calculation follows the standard ISO-15016 [15],
302 calculating the wind resistance by the effective area of the super structure and a wind resistance
303 coefficient, both calculated as a function of the relative wind direction, though here only consider-
304 ing head wind as part of the simplified assessment. Data on wind resistance coefficients and super
305 structure areas for different ship types and sizes are calculated by the regressions given by [32, 33].

306 *2.3. Ship propulsion and engine loading*

307 *2.3.1. Operational point and propulsion coefficients*

308 In a context of MPP assessment, the aim is to determine the location of the (directly coupled)
309 main engine's operational point corresponding to the total resistance. In other words, it must be
310 assessed if the required rate of revolutions of the FP propeller and the corresponding brake power,

311 as a pair, lies within the load diagram of the intended engine. One possible approach to make this
 312 assessment is suggested in the following, where the basic principles of ship propulsion are taken
 313 from [34]. It is assumed that the propeller design is approximated by the Wageningen B-series [35]
 314 in order to be able to relate the propeller coefficients K_Q and K_T in the open-water diagram. A
 315 propeller with diameter D and rate of revolutions n is considered, the density of water is ρ .

The total resistance R_{tot} on a ship with given main particulars and for specified operational conditions, including waves and forward speed, can be estimated as outlined in subsection 2.2. In this case, the required thrust T is given by,

$$T = \frac{R_{tot}}{1 - t} \quad (16)$$

where t is the thrust deduction coefficient, which can be estimated from the method by [36], later updated by [30]. The same reference(s) may also be used in the estimate of the wake fraction coefficient $w = V_w/V_S = (V_S - V_A)/V_S$, where V_S is the ship's speed (through water), and V_w is the wake velocity while V_A is the velocity of water arriving at the propeller. Alternatively, values for t and w are suggested by [1]. The advance coefficient $J_A = V_A/(nD)$ and the thrust coefficient K_T are unknown, implying that the required torque Q is neither available. By definition, $K_T = T/(\rho n^2 D^4)$ which can be rewritten,

$$\frac{K_T}{J_A^2} = \frac{T}{\rho V_A^2 D^2} \quad (17)$$

As the ratio on the right-hand side is known (i.e. can be calculated), the K_T -identity [36] means that unique solutions for K_T and J_A , respectively, are available for every value of thrust and corresponding speed (V_A); keeping in mind that the propeller design is approximated by the Wageningen B-series. Consequently, the torque coefficient K_Q can subsequently be directly inferred from the open-water diagram and, since the rate of revolutions n is available through the advance number, i.e. $n = V_A/(J_A D)$, the brake power becomes,

$$P_B = \frac{2\pi n K_Q}{\eta_s \eta_r} \quad (18)$$

316 where η_s and η_r are the shaft efficiency and the relative rotative efficiency, respectively. Altogether,
 317 the prediction of n and P_B completes the determination of the location of the operational point
 318 of the main engine. The practical relevance of this approach, in relation to MPP, is exemplified in
 319 the case study presented in Section 4.

320 It is noteworthy that, in this study and like in [1], it is assumed that the wake fraction coefficient
321 w and the thrust deduction factor t , as obtained for calm-water conditions, are applicable also in
322 cases of adverse weather conditions, since quasi-steady conditions are assumed with no account
323 for dynamic effects. The accuracy of this assumption can be questioned as discussed by, e.g., [37].
324 The reason is that the thrust deduction factor will change with the propeller loading, but the
325 error of this is argued to be smaller than the uncertainty of the estimate of t . Other studies, e.g.
326 [26], also discuss the effect of propeller loading on the thrust deduction and wake fraction, and it
327 should be of interest to look further into the effect in future work. Furthermore, the assumption
328 of quasi-steady conditions excludes considerations on dynamic variations in the inflow velocity V_A
329 (and hereby dynamic variations in the resulting thrust T) and any possible influence of this towards
330 the dynamic response of the main engine.

331 2.3.2. Engine load limits

332 In this study the static load diagram of the typical prime mover of larger merchant vessels, a
333 low speed two-stroke engine is considered. The static load diagram by one of the designers of such
334 engines [34] expresses a combination of power and speed limits, the most relevant for considerations
335 of MPP, the so called "torque limit", limiting an engine's capabilities with respect to heavy running.
336 The torque limit is mainly applied to reduce the thermal load, and thereby thermal wear rates,
337 on combustion chamber components, such as the fuel injection valves, piston crown, and exhaust
338 valve spindle, in order to attain satisfactory service intervals. Traditionally, the torque limit has
339 predominantly been depending on the actual mechanical limits of the engine, especially considering
340 the maximum pressure permitted on the bearings. However, this dependency is less clear for a
341 modern engine with electronic control of the fuel injection, permitting control of the maximum
342 pressure attained during combustion while running heavy. The power limits of the load diagram
343 are imposed by limits to the amounts of fuel injected per revolution, expressed by an index of the
344 amount injected at 100% engine load and speed.

345 In line with the requirements of [1], only the static load diagram and mean added wave resistance
346 is considered in the present study, even if dynamic limits to the fuel index exist: In relation to
347 MPP, the most relevant part of the dynamic fuel limits is the so-called "scavenge air limit", which
348 limits the fuel index based on the scavenge air pressure. The scavenge air (fuel index) limit reflects
349 the amount of air available for combustion and limits the fuel index accordingly in order to reduce

350 the soot formation. Hence, this fuel index limit may restrict the amount of fuel injected in a
351 (real) dynamic seaway. To exemplify, consider the case of propeller ventilation where the load
352 on the engine reduces, requiring a reduced fuel injection in order to avoid over-speeding, typically
353 attaining zero fuel index. This results in a lowering of the mass flow across the turbo charger, which
354 in turn leads to a reduction of the scavenge air pressure and thereby the fuel index permitted. The
355 scavenge air (fuel index) limit increases as the turbocharger is accelerated once the engine load
356 increases upon submergence of the propeller. This can potentially limit the fuel index permitted
357 resulting in a lowering of the engine speed until reaching a scavenge air pressure corresponding to
358 the fuel index required to maintain the engine speed set point. In a dynamic seaway this will lead
359 to variations in the engine speed.

360 In addition to limitations on the fuel index imposed by the resulting lower scavenge air pressure
361 after a propeller emergence, propeller emergence may involve a risk of turbo charger surging.
362 Continuous operation with a surging turbo charger^{||} is to be avoided but operation in conditions
363 so severe that full propeller emergence occurs with resulting risk of surging, is not considered
364 continuous operation, similar e.g. to surging resulting from a crash-stop with a sudden reduction
365 of fuel injection [38].

366 **3. Comparisons of Estimates of Added Wave Resistance**

367 Three semi-empirical methods for predicting added wave resistance were presented in Subsection
368 2.1. In the present section, a sensitivity study will be undertaken considering the influence of
369 different operational conditions. As described previously, fulfilling the requirements for minimum
370 propulsion power is most challenging to the design of smaller ships. In this light, the sensitivity
371 study is focused on results for a 11,000 DWT tanker, a 27,000 DWT tanker, and a 50,000 DWT
372 tanker, where the latter is included to cover a common MR tanker. All three ships have been
373 assessed to be capable of fulfilling EEDI phase 2. Main particulars of the considered ships are
374 provided in Table 2. A few practical remarks are worth noticing:

- 375 • The results of the prediction methods will be referred to by the following abbreviations;
376 results of STAwave-2 are denoted by 'STA2', the method of SHOPERA and its results are

^{||}Continuous surging typically happens due to insufficient cleaning resulting in clogging of both the compressor and turbine parts, insufficient maintenance, insufficient air supply to the engine room or faulty fuel injections, etc.

Table 2: Particulars of the tankers for theoretical evaluations of the methods for predicting added wave resistance all with 15% sea margin, 10% engine margin, 5% propeller light running margin and a specified maximum continuous rating (SMCR) as given

Capacity [DWT]	11,000	27,000	50,000
Length L_{pp} [m]	112	152	176
Breadth B [m]	20	27	32
Draught T_d [m]	7.5	10	11
T_d/L_{pp}	0.067	0.066	0.063
Block coef. $C_{B,L_{pp}}$ [-]	0.73	0.73	0.80
Design speed V_d [knots]	14.5	14.5	14.7
SMCR-kW	4,000	5,700	7,300
SMCR-rpm	160	108	89
Prop. diameter D_{prop} [m]	4.2	5.8	6.8
Blade number N	4	4	4
Area ratio A_e/A_o [-]	0.55	0.55	0.55
Pitch diameter ratio $P/D_{0.7}$ [-]	0.772	0.775	0.745

377 'SHOP', and the results from the DTU Design Tool are referred to as 'DTU Tool' or 'DTU'
378 when given in figure legends.

- 379 • All methods are proportional to H_s^2 , and results are shown just for $H_s = 1$ m.
- 380 • The additional steering resistance, cf. Eq. 15, associated with the SHOPERA equation is
381 *not* included, so to have an equal basis for the three methods.
- 382 • Finally, the wave spectrum is taken as a Pierson-Moskowitz spectrum which is a special case
383 of the JONSWAP spectrum when the wind speed is related to significant wave height. The
384 spectral formula(s) can be found in any standard textbook on naval architecture or ocean
385 engineering, e.g. [39].

386 The results of the sensitivity study are presented in Figure 3 which shows the variation of
387 predicted added wave resistance as function of advance speed V_S , draught amidships T_M , and
388 mean wave period T_1 . In any one case, the two other parameters are constant and their values
389 are indicated; noting that the values are set somewhat arbitrarily albeit they reflect [1]. The main
390 findings from the plots are summarised as follows. Generally, there appear large deviations between
391 the predictions, and it is only possible to find a sort of "best agreement" between the results for
392 specific values or, at best, for very small intervals of the studied parameters (V_S , T_M/T_d , T_1). It
393 is also noted that the trends of the three predictions are quite different; STA2 and SHOP increase

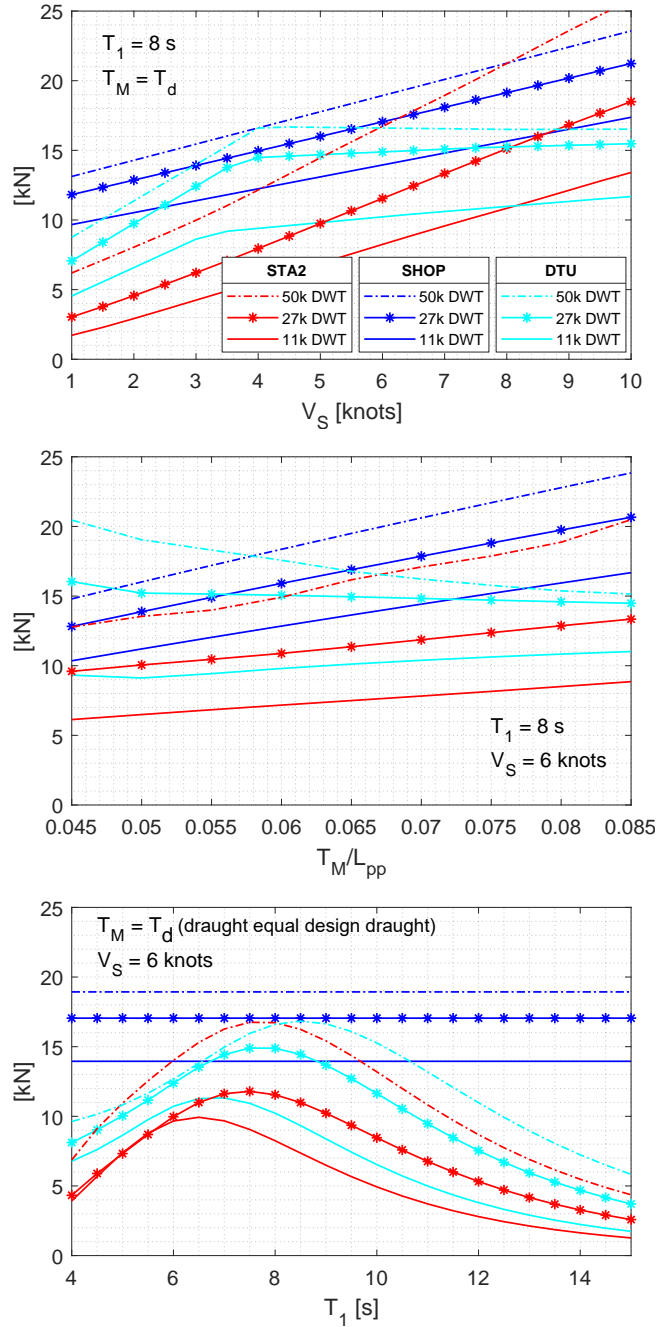


Figure 3: Theoretical predictions of added wave resistance. Upper plot: Variation with advance speed. Middle plot: Variation with (non-dimensional) draught; the non-dimensional *design* draught is app. 0.065 for all three ships. Bottom plot: Variation with mean wave period T_1 . The legend in the top plot applies also to the other two plots.

394 both linearly with speed and draught on the studied intervals, while the behaviour of the DTU
395 Tool for these parameters has more details. On the other hand, there is a similar behaviour of
396 STA2 and the DTU Tool when a variation in the wave period is considered; while, in this case,
397 SHOP is invariant to changes. In addition to the overall findings, some specific remarks are listed
398 in the following.

399 **Variation with speed:** The discontinuity of the DTU Tool is the result of the difference
400 in the methods applied depending on encounter frequency (or wave length); Salvesen's method
401 vs. Faltinsen's asymptotic method. The STA2 prediction method is originally developed for sea
402 trial corrections, and has a lower speed limit for its application; $Fr = 0.1$ has been set, which
403 correspond to 6.4 knots, 7.5 knots, and 8.1 knots for the 11,000, the 27,000, and the 50,000 DWT
404 ships, respectively. In principle, it is therefore beyond the validity of STA2 to select the speed
405 as $V_S = 6$ knots as done when draught and wave period are varied. However a correction to the
406 pitch radius of gyration has been implemented, as described in Section 2.1.1, in order to include
407 the consequences of extending the model towards lower Froude numbers.

408 **Variation with draught:** The conflict in increasing and decreasing trends of the predictions
409 (STA2 and SHOP vs. DTU) is observed because of the underlying methods. The STA2 method is
410 based on an empirical analysis of an extensive series of model-scale tests, the SHOPERA equation
411 is based on a series of evaluations by a Rankine source method, and the DTU Tool is based on
412 potential flow theory. For the latter, when predicting added wave resistance by potential flow
413 theory, the motions of the ship and hereby radiation of waves, is a significant contribution to the
414 total added resistance. At lower draughts, the motions of the ship are expected to be relatively
415 larger, which will increase the added resistance predicted by potential flow theory. In addition,
416 both SHOPERA and STAwave-2 treats waves up to 30 deg and 45 deg off-bow, respectively, as
417 head waves, which might provide an explanation why the methods in general are less sensitive to
418 ship motions.

419 **Variation with wave period:** The maximum added wave resistance for STA2 and the DTU
420 Tool occurs in an interval of 7-8.5 s of the mean wave period. The actual value depends on ship
421 length, but it is seen that the SHOPERA equation takes a larger (constant) value in all cases. This
422 is not surprising as the intention of the SHOPERA equation is to return a conservative prediction
423 corresponding to a wave period that will result in $\lambda/L \approx 1$, where added resistance is largest.

Table 3: Maximum speeds attainable in "worst case" wave period as per the methods applied for predicting added wave resistance, for sea states corresponding approx. to Beaufort 7, 8 and 9 with 5% propeller LRM.

Capacity [DWT]	11,000	27,000	50,000
Speed attained	[knots]	[knots]	[knots]
SHOPERA, $H_s = 4$ m	7	9.5	10
STAwave-2, $H_s = 4$ m	9	11	9.5
DTU Tool, $H_s = 4$ m	11.5	12.5	11.5
SHOPERA, $H_s = 5.5$ m	-	1	3
STAwave-2, $H_s = 5.5$ m	4.5	5.5	5
DTU Tool, $H_s = 5.5$ m	1.5	2.5	3.5
SHOPERA, $H_s = 7$ m	-	-	-
STAwave-2, $H_s = 7$ m	2.5	5.0	2
DTU Tool, $H_s = 7$ m	-	-	1

424 Although not shown, it is interesting to note that if the speed drops to 4 knots there is an exact
425 match between the result of the SHOPERA equation and the maximum of the DTU Tool.

426 Based on the (theoretical) comparisons between the methods for added wave resistance predic-
427 tion, it has been seen that an evaluation of minimum propulsion power and testing of compliance
428 will be dependent on the method chosen. This is exemplified in the next section.

429 4. Case Study on Effect Towards Minimum Propulsion Power Compliance

430 In the following case study, an example evaluation of whether a ship design with a specific
431 propulsion plant fulfils the MPP requirements or not is illustrated. The example combines the
432 methodology for determining resistance on the hull and application of the various methods for
433 determining the added wave resistance together with the method for determining the operational
434 point of the FP propeller, as described in Section 2.3. The study presents the detailed results for
435 the 50,000 DWT MR tanker, cf. Table 2, but results for all three ships are summarised in Table 3.

436 4.1. Results in rule-determined sea state

437 In Figure 4, the operational points of the main engine are illustrated for various ship speeds in
438 the rule-defined sea state [1], that is, $H_s = 4$ m with corresponding wind speed of $V_{wind} = 15.7$ m/s;
439 noting that all three ships have $L_{pp} < 200$ m. This sea state corresponds approximately to Beaufort
440 7. The single operational points are indexed by (integer) numbers that indicate the attainable speed
441 in knots, thus enabling a direct evaluation of the attainable speed, when the mean added resistance

442 is calculated by the different methods (SHOP, STA2, DTU). Note that the results, in line with the
 443 IMO guidelines [1], only represent engine loading as a result of the mean added wave resistance.
 444 However, dynamic fluctuations of the operational point of the engine for a given ship speed must
 445 be expected, partly because of variations in the instantaneous added wave resistance experienced
 446 on the hull, and partly due to wake variations and potentially dynamic propeller ventilation. Such
 447 dynamic fluctuations are not considered in the guidelines, and this constitutes a weak point of
 448 the simplified assessment of mean added wave resistance; simply because no attention is given to
 449 the dynamic limits of the main engine and to dynamic effects, e.g. resulting from a reduction of
 450 scavenge air pressure after a ventilation.

451 It is noteworthy that in the considered sea state, the operational propeller curves resulting
 452 from the mean added resistance predicted by the methods of SHOPERA and STAwave-2 are so
 453 heavy that the engine is prohibited from reaching 100% speed and thereby also prohibited from
 454 delivering 100% power continuously. This illustrates that the minimum speed a ship can maintain
 455 during adverse weather conditions is not limited by the maximum power of the engine; rather
 456 the ship speed is limited by the torque that the engine can deliver at speeds below 100% speed

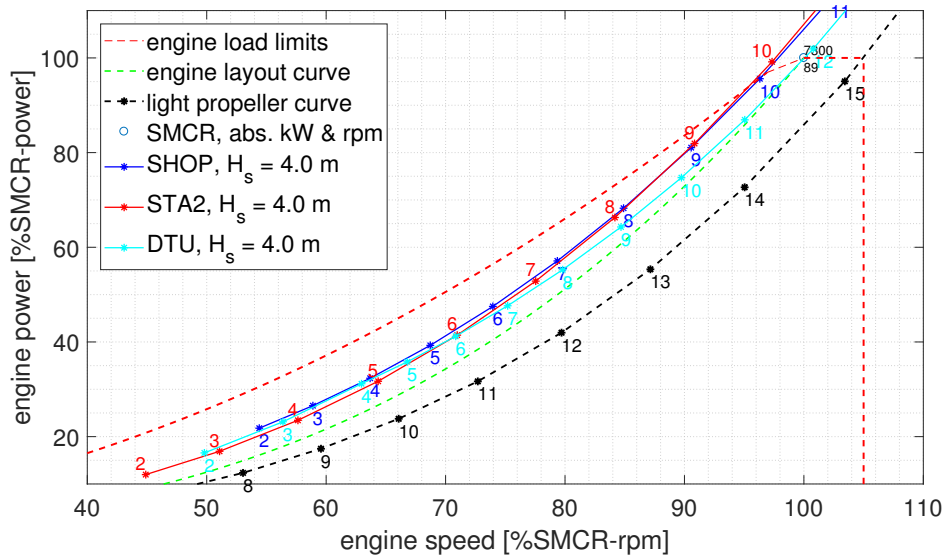


Figure 4: Operational points of the main engine plotted on the engine load diagram [34] as calculated by various methods for the rule-defined sea state ($H_s = 4$ m) and 5% LRM. Integers along curves represent the corresponding ship speed attained.

457 while operating on a heavy propeller curve. This effect of the engine torque limitation further
458 illustrates the necessity of a propeller light running margin. Thus, the propeller light running
459 margin increases the margin between the light propeller curve and the engine load limits, which,
460 in the end, raises the sea states in which the engine can deliver 100% power. This is given further
461 attention in Section 4.3.

462 It is of interest that even for a relatively low main engine power of 7,300 kW installed on the
463 ship with 5% propeller light running margin (LRM), the tanker is by all methods estimated to
464 be able to maintain at least 9 knots of forward speed. Under the scheme of [1], 9 knots is the
465 highest value of the minimum course-keeping speed that can be required for a ship design under
466 any circumstances. This is a remarkable difference to the results of assessment level 1 of the IMO
467 guidelines [1], which for a tanker of 50,000 DWT would require 9,220 kW of engine power, without
468 any consideration of the propeller light running margin.

469 In addition, the change in the relative difference between the attainable speeds and operational
470 points of the main engine, when the added wave resistance is calculated as per the different methods,
471 is quite remarkable: At elevated speeds above approx 7 knots ($Fr = 0.86$), good agreement is
472 found between SHOPERA and STAwave-2. On the other hand, at lower speeds, the relatively best
473 agreement is found between SHOPERA and the DTU Tool; for instance, at 2 knots, SHOPERA
474 predicts 22% SMCR-power at 54% SMCR-rpm, while the DTU Tool predicts 16% SMCR-power
475 at 54% SMCR-rpm. Contrary, at 2 knots, the method of STAwave-2, including the correction to
476 k_{yy} as described in Section 2.1.1, predicts only 12% of the SMCR-power at 45% SMCR-rpm. A
477 remarkable difference indicating that the correction proposed is not sufficient to apply STAwave-2
478 below the original threshold of $Fr = 0.1$.

479 The effects of the correction to k_{yy} applied for STAwave-2 are most critical at low Froude
480 numbers, although the effect remains small at $H_s = 4$ m. However, the effects will be more
481 dominant in increasing sea states, and, at $H_s = 7$ m, the difference in the required power is larger
482 than 2% SMCR-power for calculations with and without the correction. For longer ships, attaining
483 even lower Froude numbers, the effect of excluding the correction to k_{yy} is expected to be greater.

484 The effects of the change between Salvesen's method [25] for longer waves and Faltinsen's
485 asymptotic method for shorter waves [26], see Figure 3, are clearly identifiable in the operational
486 propeller curve predicted by the DTU tool. This results in a degree of propeller heavy running sim-

487 ilar to SHOPERA at 4-5 knots, while at higher speeds, the resulting propeller curve is significantly
488 lighter than predicted by SHOPERA.

489 As the extent of propeller heavy running is decisive to the power that can be delivered and
490 hereby attainable ship speed, small differences amongst the added wave resistance predicted can
491 result in rather large differences in predicted ship speed. However, it is remarkable that the actual
492 extent of propeller heavy running is not that different amongst the methods. With respect to an
493 evaluation according to the IMO guidelines [1], it is instead of interest that the speeds predicted
494 along the propeller curves illustrated in Figure 4 and 5 are so different, as is also shown in Table
495 3.

496 Considering this, along with the fact that the difference between the slope of the engine load
497 diagram and the predicted operational propeller curves is rather limited, it is evident that an
498 accurate prediction of the added wave resistance is important even in the early design phase.
499 Therefore, further developments of simplified methods for predicting added wave resistance at an
500 early stage of the design are recommended, in order for the designer to optimise the propulsion
501 plant.

502 The small difference in slope between the engine load diagram and operational propeller curve
503 also indicates a potential challenge of assessment level 2 in [1]. Thus, even if model tank tests are
504 utilised to determine the transfer function of added wave resistance for the final assessment, small
505 inaccuracies in the development of the transfer function may have a major impact on the actual
506 performance of the ship. On the other hand, the small difference in slope, comparing the heavy
507 propeller curve and torque limit of the engine load diagram, indicates that even small extensions of
508 the engine load diagram can have significant positive effects towards the minimum speed attainable.

509 *4.2. Results in sea state beyond rule requirements*

510 In general, the attainable ship speeds predicted when applying the various methods for esti-
511 mating added wave resistance in more severe sea states than $H_s = 4$ m vary strongly, as illustrated
512 in Figure 5: For $H_s = 5.5$ m and $V_{wind} = 19$ m/s (Beaufort 8), a maximum speed of 5 knots is
513 predicted by STAwave-2, whereas SHOPERA predicts 3 knots, and the DTU Tool estimates 3.5
514 knots. These speeds are close to the minimum navigational ship speed of 4 knots as defined per
515 [1].

516 In significantly adverse conditions, e.g., $H_s = 7.0$ m and $V_{wind} = 25$ m/s (Beaufort 9), see

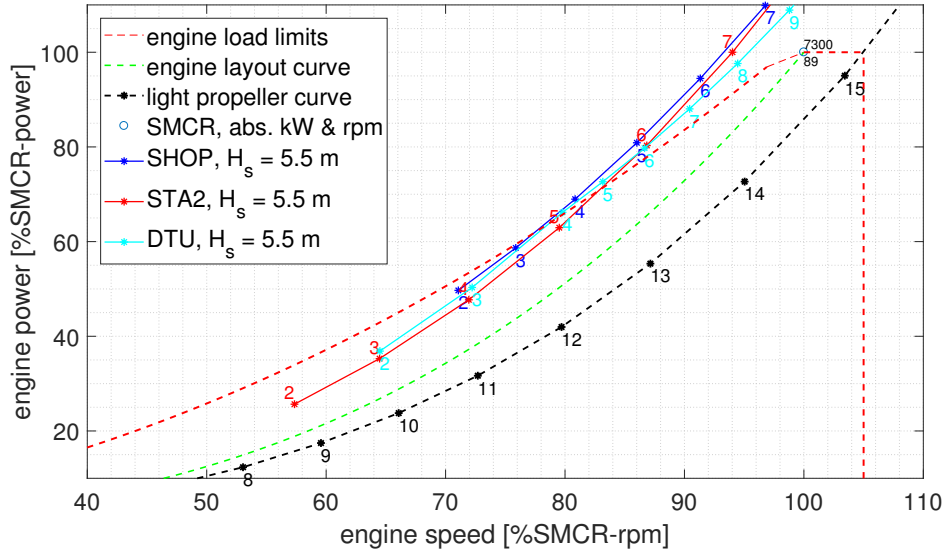


Figure 5: Operational points of the main engine plotted on the engine load diagram [34] as calculated by various methods for $H_s = 5.5$ m and 5% LRM. Integers along curves represent the corresponding ship speed attained.

517 Figure 6, STAwave-2 and the DTU Tool predicts the operational point of the propeller and main
 518 engine to lie within the engine load diagram for a ship speed of 2 knots and 1 knot respectively.
 519 At such low speeds, the ship is expected to loose manoeuvrability. It is predicted by SHOPERA
 520 that the ship cannot attain a forward speed in this condition.

521 4.3. Effect of a reduction of propeller light running margin

522 The propeller LRM has been set to 5% for all three ships considered in the case study, cf.
 523 Table 2, and the light propeller curve with 5% LRM was illustrated in Figures 4 to 6. With 5%
 524 LRM the pitch is reduced to such an extent that, when operating along the calm water propeller
 525 curve in calm waters and with clean hull as in sea trial condition, 100% engine power is delivered
 526 at 105% engine speed. This LRM ensures some distance between the light propeller curve and
 527 the engine load limits, in order to be able to accommodate some propeller heavy running, i.e.
 528 increased propeller load as a consequence of added resistance from fouling or from wind or added
 529 wave resistance [34].

530 If the propeller LRM is reduced to 2% either per design, or if the hull is heavily fouled, significant
 531 changes to the attainable ship speed are attained as summarised in Table 4. In $H_s = 4$ m,

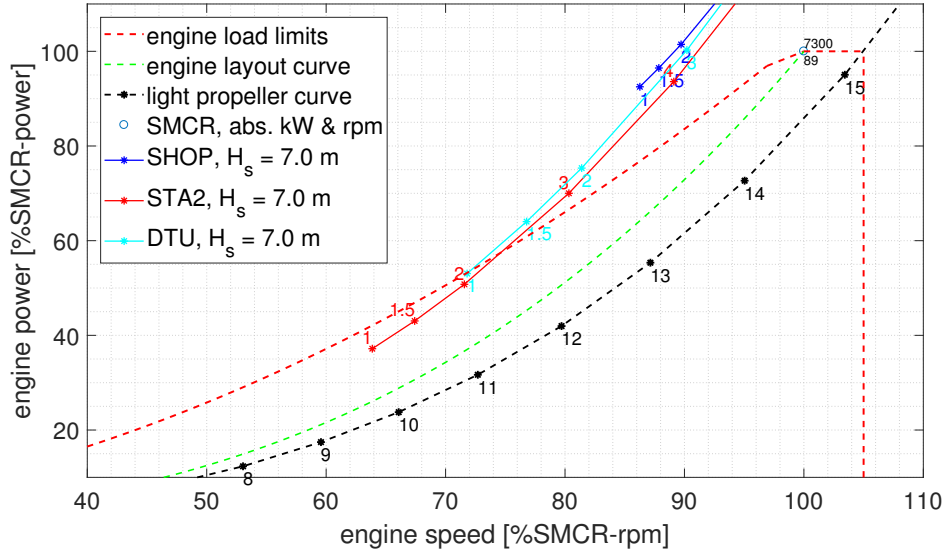


Figure 6: Operational points of the main engine plotted on the engine load diagram [34] as calculated by various methods for $H_s = 7$ m and 5% LRM. Integers along curves represent the corresponding ship speed attained.

Table 4: Maximum speeds attainable in "worst case" wave period as per the methods applied for predicting added wave resistance, for sea states corresponding approx. to Beaufort 7, 8 and 9 with just 2% propeller LRM.

Capacity [DWT]	11,000	27,000	50,000
Speed attained	[knots]	[knots]	[knots]
SHOPERA, $H_s = 4$ m	6	7.5	8.5
STAwave-2, $H_s = 4$ m	8	9	8.5
DTU Tool, $H_s = 4$ m	10.5	12	11
SHOPERA, $H_s = 5.5$ m	-	-	1
STAwave-2, $H_s = 5.5$ m	4	4.5	4
DTU Tool, $H_s = 5.5$ m	1.5	2	3
SHOPERA, $H_s = 7$ m	-	-	-
STAwave-2, $H_s = 7$ m	1.5	2	1.5
DTU Tool, $H_s = 7$ m	-	-	-

532 the reduced LRM reduces the attainable speed by 0.5 – 1 knot, compared to results in Table 3,
533 depending on the method applied to estimate the added wave resistance. It is noteworthy that, at
534 $H_s = 5.5$ m and with an LRM of 5%, the attainable forward speeds are just around the minimum
535 navigational speed of 4 knots as defined by [1]. However, with 2% LRM the speed is by SHOPERA

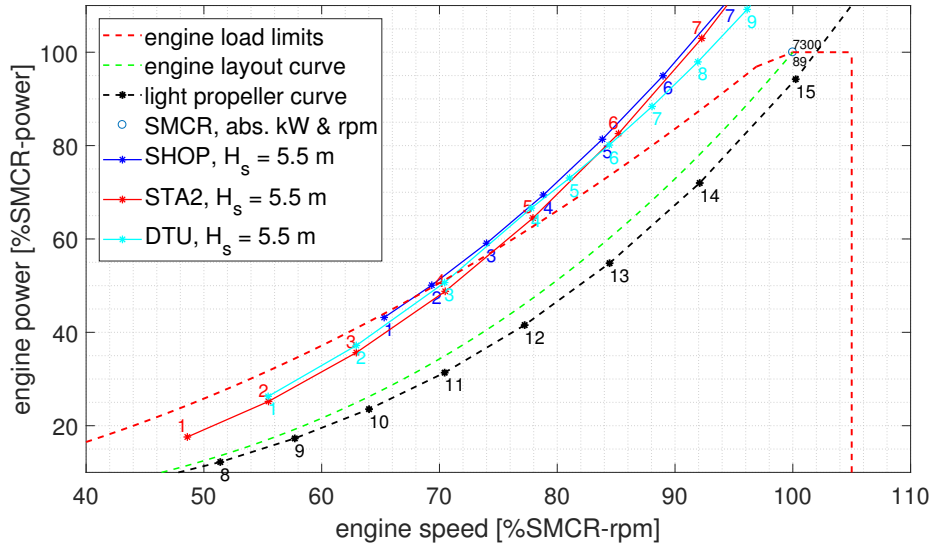


Figure 7: Operational points of the main engine plotted on the engine load diagram [34] as calculated by various methods for $H_s = 5.5$ m and only 2% LRM. Integers along curves represents the corresponding ship speed attained.

536 estimated to be significantly lower, see Figure 7 compared to Figure 5. For future ships of even
 537 lower SMCR, this highlights the importance of the LRM.

538 In the case of only 2% LRM, the predicted operational points of the engine moves closer to
 539 the engine torque limit, increasing the risk that dynamic fluctuations in the added wave resistance
 540 will push the actual operational point to the limit. In this case, engine speed will drop and the
 541 dynamic load limits of the main engine must be considered to evaluate if the engine and propeller
 542 in a moment of lesser added wave resistance can be accelerated back to the desired speed set point
 543 and ship speed. Such evaluations have not been performed here. Similarly, other engine types
 544 than low speed two-stroke engines may have other load diagrams, extending or limiting such an
 545 engine's heavy running capability. Load limits of other engine types, e.g. four-stroke engines, have
 546 not been considered.

547 5. Summary and Conclusions

548 EEDI requirements have increased the focus on the capabilities of ships to maintain safe ma-
 549 noeuvring speed in adverse weather. In fact, the resulting risk of under-powered newly designed

550 ships has led the IMO to provide guidelines on minimum propulsion power. As part of the assess-
551 ment, formulated by the guidelines, stands the estimation of the added wave resistance as a critical
552 and important contribution.

553 In this paper, three semi-empirical methods for estimation of the added wave resistance have
554 been evaluated in a comparative study targeted on an evaluation of minimum propulsion power
555 at an early design stage. Herein, the influence of ship speed, wave period, and draught has been
556 considered. Two of the evaluated methods, SHOPERA and STAwave-2, predict a (nearly) linearly
557 increasing added wave resistance with ship speed and draught. The third method, the DTU
558 Design Tool, predicts a stepwise linearly increasing added wave resistance with ship speed, while
559 the tool's dependency on draught depends on ship size. The variation with wave period is similar
560 for STAwave-2 and the DTU Tool, albeit the absolute results are quite different. The SHOPERA
561 method is invariant to changes in the wave period.

562 Focusing on lower speeds, as considered in a case study on minimum propulsion power for
563 three example ships, the absolute difference of the added wave resistance predicted by the various
564 methods may appear relatively small. However, when extending the comparative study further to
565 consider the effects of the added wave resistance predicted towards the loading of the propeller,
566 even small differences become important. For a ship with a typical propulsion plant, consisting
567 of an FP propeller directly coupled to a two-stroke main engine, it is shown that the minimum
568 speed that the ship can maintain during adverse weather conditions is not limited by the maximum
569 power of the engine; rather the speed is limited by the torque that the engine can deliver at lower
570 rpm-ranges. Hereby, small changes in the predicted added wave resistance become of importance
571 as this has influence on the propeller loading and hence the rpm at which the propeller and engine
572 operate. This also indicates that potential efforts into lifting the torque-limit of two-stroke engines
573 will have a large impact on the minimum speed attainable.

574 The predicted operating rpm affects the power that the main engine can deliver, and ultimately
575 the speed that can be maintained in adverse weather. This is further underlined by the effects
576 of the propeller light running margin, which is shown to have crucial influence on the attainable
577 speed during adverse conditions. In the specific case study, it is noteworthy that even for the most
578 conservative of the methods used for estimation of the added wave resistance, i.e. the SHOPERA
579 method, it appears that there is a good margin for further power reductions before the example

580 ships cannot meet the requirements of the IMO, as long as adequate propeller light running margins
581 are considered.

582 The focus of this study has been placed solely on fixed pitch propellers. In the future, the
583 magnitude of efficiency advantage of FP propellers over controllable pitch (CP) propellers may
584 decrease: Potential excessive increases of LRM by pitch reductions, to increase the margin towards
585 the engine load limits, will potentially decrease FP propeller efficiency in the design condition. A
586 potential for attaining a large LRM, without the efficiency penalty of a pitch reduction, lies in the
587 reduction of the installed power itself, as this reduces the propeller thrust loading. Altogether this
588 directs the way for a reduction of the propeller blade number, which in turns leads to a higher
589 optimal rpm of the propeller and thereby LRM. Alternatively, a CP propeller will in theory be
590 capable of attaining 100% engine speed and thereby 100% power in all conditions, offering the
591 advantage that a pitch reduction is only performed when needed. However, in such evaluations,
592 the reduced propeller efficiency of a CP propeller at the reduced pitch, required to attain 100%
593 engine speed under the added resistance of adverse conditions, must not be forgotten.

594 *5.1. Future work*

595 Simple predictions of added wave resistance are difficult, and the three presented methods show
596 differences on both the quantitative and qualitative levels. For their realistic use with respect to
597 MPP, the methods need therefore to be compared against full-scale data or at least be compared
598 to model tank tests or numerical simulations in the next phase. Despite the lack of a consistent
599 method to *measure* added wave resistance when a real-sized ship operates in a seaway, possible
600 approaches have been suggested by [18] and [40].

601 The interaction between waves, a ship, and its propulsion plant is highly dynamic and *not* static
602 as has been assumed in the present study, and also assumed by the MPP-guidelines [1]. As ship
603 speeds are expected to decrease further, as future efficiency requirements are tightened to meet
604 the emission targets of the IMO, it will be relevant to evaluate not only how a ship performs with
605 respect to the mean added wave resistance, but also to evaluate how the ship and propulsion plant
606 perform dynamically, addressing the wave-induced response by establishing a model of the engine,
607 turbo charger, shafting, and propeller. Furthermore, such a dynamic evaluation should include a
608 study about the effect of the sea state on variations on the wake and thrust deduction factors,
609 e.g. [41, 42], along with consideration of the effects of dynamic propeller ventilation. In addition,

610 the propulsion plant's capability to accelerate itself and respond to the actual added resistance in
611 a dynamic seaway must be evaluated, not only with respect to the static load limits of the main
612 engine but also with respect to the dynamic load limits. Such evaluations are outstanding and are
613 recommended to be performed, at least in order to verify that the static consideration, on which
614 the present IMO guidelines is based, can be justified as a basis for future power reductions.

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