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Published in:
A Multi-Model Approach for System Diagnosis

Link to article, DOI:
[10.1109/ACC.2007.4282628](https://doi.org/10.1109/ACC.2007.4282628)

Publication date:
2007

Document Version
Publisher's PDF, also known as Version of record

[Link back to DTU Orbit](#)

Citation (APA):
Niemann, H. H., Poulsen, N. K., & Bækgaard, M. A. B. (2007). A Multi-Model Approach for System Diagnosis. In *A Multi-Model Approach for System Diagnosis* (pp. 2539-2544). Proceedings of the 2007 American Control Conference. <https://doi.org/10.1109/ACC.2007.4282628>

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A Multi-Model Approach for System Diagnosis

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Abstract—A multi-model approach for system diagnosis is presented in this paper. The relation with fault diagnosis as well as performance validation is considered. The approach is based on testing a number of pre-described models and find which one is the best. It is based on an active approach, i.e. an auxiliary input to the system is applied. The multi-model approach is applied on a wind turbine system.

I. INTRODUCTION

The area of active fault diagnosis (AFD) has been considered in a number of books [3], [6], [16] and in papers [1], [2], [4], [13], [12], [14]. Further, in [9], an AFD approach has been considered for closed-loop systems. However, it has been shown in [10] that it is possible to apply the same AFD set-up on open-loop systems as well.

The AFD is based on the inclusion of an auxiliary input signal/vector into the system. The auxiliary input can either be injected in the open-loop system or in the closed-loop feedback system. As output from the system a standard residual vector known from the passive FD (fault diagnosis) approach is applied [5]. Using the AFD approach from [9], [8], the auxiliary input is injected in the closed-loop system in such a way that the standard residual vector is decoupled from this auxiliary input in the nominal case and coupled in the faulty case. It turns out that an optimal placement of the auxiliary input vector together with the selection of the standard residual vector as the output vector connect the AFD with the dual YJBK (after Youla, Jabr, Bongiorno and Kucera) parameterization, [7], [15]. The transfer function from auxiliary input to the residual vector is equivalent to the dual YJBK transfer function in the dual YJBK parameterization, i.e. a parameterization of all systems stabilized by a given feedback controller. Here, in connection with AFD, this transfer function has been named the *fault signature matrix*, [9], [8]. Fault detection as well as fault isolation are based directly on the fault signature matrix.

There are mainly two approaches in AFD. In the approach derived by Campbell et.al., [3], the auxiliary input is designed with respect to a fast fault diagnosis/multi-model selection. Using a dedicated design of the auxiliary input gives a fast diagnosis/selection.

The other AFD approach in [8], [10] and applied in [11], a periodic auxiliary input is applied. The signature from this periodic input in the output/residual vector is quite distinct

and will also be a periodic vector with the same frequency. A change in the system due to e.g. parametric faults, will give a change in the signature. This change can be in the amplitude and/or the phase of the periodic output vector.

Using the AFD approach from [8], [10], the auxiliary input is decoupled in the output/residual vector in the nominal case. The detection of parametric faults can then be done by a detection of a signature from the auxiliary input in the residual vector. Another approach is to use a filter/observer to estimate the periodic signature with the known frequency directly. This approach will not be considered in this paper.

Instead of using the AFD approach applied in [10], [11], where the residual vector is derived by using the nominal model, it is possible to use a number of models in connection with the fault diagnosis. This approach has been applied in e.g. [1]. The main issue in this paper is to apply a multi-model approach in connection with the AFD set-up derived in [10], [11]. The direct consequence of this change is that instead of considering a single residual vector based on the nominal model, a number of residual vectors are calculated based on different models. The system changes can then be identified by a detection in which residual vector the signature from the auxiliary is smallest/minimal. It will be shown in this paper that ability to identify system changes will not depend directly on the number of models applied. By using information from more than a single residual vector it is possible to get a very good diagnosis based on a few models.

The multi-model AFD approach described in this paper is applied on a wind turbine system. The wind turbine system is non-linear. This non-linearity will allow to detect changes in the working point based on changes in the system dynamic. In this case it will be possible to estimate the wind speed based on a detection of changes in the dynamic in the wind turbine.

II. SYSTEM SET-UP

Let a general system be given by:

$$\Sigma : \begin{cases} z = G_{zw}w + G_{zd}d + G_{zu}u \\ e = G_{ew}w + G_{ed}d + G_{eu}u \\ y = G_{yw}w + G_{yd}d + G_{yu}u \end{cases} \quad (1)$$

where $d \in \mathcal{R}^r$ is a disturbance signal vector, $u \in \mathcal{R}^m$ the control input signal vector, $e \in \mathcal{R}^q$ is the external output signal vector to be controlled, $y \in \mathcal{R}^p$ is the measurement vector, $w \in \mathcal{R}^k$ and $z \in \mathcal{R}^k$ are external input and output vectors. The connection between the external output and the external input is given by

$$w = \theta z,$$

where θ is a diagonal matrix given by

$$\theta = \text{diag}(\theta_1, \dots, \theta_i, \dots, \theta_k)$$

represents the system parameters. It is assumed that only these parameters can change in the system, the others are assumed to be constant. Closing the loop from w to z in Σ by θ described by a linear fractional transformation (LFT) we get

$$\Sigma_\theta = \mathcal{F}_u(\Sigma, \theta),$$

where Σ_θ is given by:

$$\Sigma_\theta : \begin{cases} e = G_{ed}(\theta)d + G_{eu}(\theta)u \\ y = G_{yd}(\theta)d + G_{yu}(\theta)u. \end{cases} \quad (2)$$

Further, let the system be controlled by a stabilizing feedback controller given by:

$$\Sigma_C : \{ u = Ky. \} \quad (3)$$

Let a coprime factorization of the system G_{yu} from (1) and the stabilizing controller K from (3) be given by:

$$\begin{aligned} G_{yu} &= N_0 M_0^{-1} = \tilde{M}_0^{-1} \tilde{N}_0, \quad N_0, M_0, \tilde{N}_0, \tilde{M}_0 \in \mathcal{RH}_\infty \\ K &= U_0 V_0^{-1} = \tilde{V}_0^{-1} \tilde{U}_0, \quad U_0, V_0, \tilde{U}_0, \tilde{V}_0 \in \mathcal{RH}_\infty, \end{aligned} \quad (4)$$

where the eight matrices in (4) must satisfy the double Bezout equation given by, [15]:

$$\begin{aligned} \begin{pmatrix} I & 0 \\ 0 & I \end{pmatrix} &= \begin{pmatrix} \tilde{V}_0 & -\tilde{U}_0 \\ -\tilde{N}_0 & \tilde{M}_0 \end{pmatrix} \begin{pmatrix} M_0 & U_0 \\ N_0 & V_0 \end{pmatrix} \\ &= \begin{pmatrix} M_0 & U_0 \\ N_0 & V_0 \end{pmatrix} \begin{pmatrix} \tilde{V}_0 & -\tilde{U}_0 \\ -\tilde{N}_0 & \tilde{M}_0 \end{pmatrix}. \end{aligned} \quad (5)$$

A. The YJBK Parameterization

Based on the above coprime factorization of the system G_{yu} and the controller K we can give a parameterization of all controllers that stabilize the system in terms of a stable transfer function Q , i.e. all stabilizing controllers are given by [15]:

$$K(Q) = (U_0 + M_0 Q)(V_0 + N_0 Q)^{-1}, \quad Q \in \mathcal{RH}_\infty, \quad (6)$$

or by using a left factored form:

$$K(Q) = (\tilde{V}_0 + Q\tilde{N}_0)^{-1}(\tilde{U}_0 + Q\tilde{M}_0), \quad Q \in \mathcal{RH}_\infty. \quad (7)$$

Using the Bezout equation the controller given either by (6) or by (7) can be realized as an LFT in Q :

$$K(Q) = \mathcal{F}_l \left(\begin{pmatrix} U_0 V_0^{-1} & \tilde{V}_0^{-1} \\ V_0^{-1} & -V_0^{-1} N_0 \end{pmatrix}, Q \right) = \mathcal{F}_l(J_K, Q). \quad (8)$$

B. The Dual YJBK Parameterization

In the same way it is possible to derive a parameterization in terms of a stable transfer function S of all systems that are stabilized by one controller, i.e. the dual YJBK parameterization. The parameterization is given by [15]:

$$G_{yu}(S) = (N_0 + V_0 S)(M_0 + U_0 S)^{-1}, \quad S \in \mathcal{RH}_\infty \quad (9)$$

or by using a left factored form:

$$G_{yu}(S) = (\tilde{M}_0 + S\tilde{U}_0)^{-1}(\tilde{N}_0 + S\tilde{V}_0), \quad S \in \mathcal{RH}_\infty. \quad (10)$$

An LFT representation of (9) or (10) is given by:

$$G_{yu}(S) = \mathcal{F}_l \left(\begin{pmatrix} N_0 M_0^{-1} & \tilde{M}_0^{-1} \\ M_0^{-1} & -M_0^{-1} U_0 \end{pmatrix}, S \right) = \mathcal{F}_l(J_G, S). \quad (11)$$

Further S is given by, [15]:

$$S = \mathcal{F}_u(J_K, G_{yu}(S)) \quad (12)$$

C. AFD Set-up

Now, let's also including a residual vector in connection with the system.

It has been shown in [5] that it is possible to parameterize all residual generators by using the YJBK parameterization. All residual vectors ε_0 for Σ given by (1) can be described by:

$$\varepsilon_0 = \tilde{M}_0 y - \tilde{N}_0 u. \quad (13)$$

Let's consider the block diagram shown in Fig. 1. The diagram includes the residual vector ε_0 and an auxiliary input vector η . The two signal vectors, η and ε_0 , will be applied in connection with the AFD, see [8], [11].

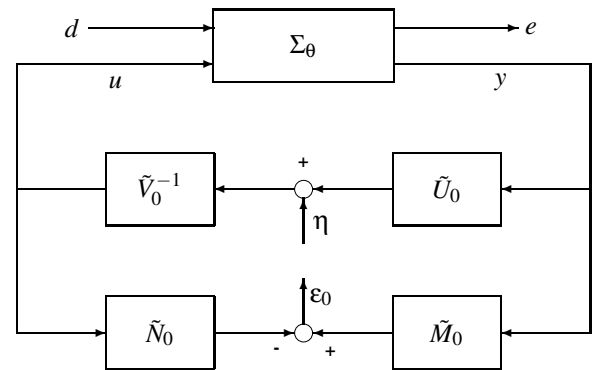


Fig. 1. Controller structure including residual vector ε_0 and the external input vector η .

Based on the feedback system in Fig. 1 the transfer functions from the two input vectors d, η to the two output vectors e, ε_0 are given by:

$$\Sigma_{FD} : \begin{cases} e = P_{ed}(\theta)d + P_{e\eta}(\theta)\eta \\ \varepsilon_0 = P_{\varepsilon d}(\theta)d + P_{\varepsilon\eta}(\theta)\eta, \end{cases} \quad (14)$$

where the explicit equations for Σ_{FD} can be found in [8], [11].

Note that the transfer function from the input vector η to the residual vector ε_0 is equal to the dual YJBK transfer

function, [8], [11]. The explicit equation for $S = P_{e\eta}$ is given by, [7]:

$$S(\theta) = \tilde{M}_0 G_{yw} \theta (I - (G_{zw} + G_{zu} U_0 \tilde{M}_0 G_{yw}) \theta)^{-1} G_{zu} M_0. \quad (15)$$

(15) gives a direct description of the parameter variations' effect on the closed-loop stability. If S gets unstable for some parameter variations, the closed-loop system will be unstable. A large S indicate that the parameter variations has a major effect on the system. In [10], [11], $S(\theta)$ was named as the fault signature matrix.

Based on the fault signature matrix $S(\theta)$ the conditions for fault detection are as follows, [10], [11]:

- Fault detection

$$\begin{aligned} S(\theta) &= 0, \quad \text{for } \theta = \bar{\theta} \\ S(\theta) &\neq 0, \quad \text{for } \theta \neq \bar{\theta}. \end{aligned}$$

III. MULTI-MODEL AFD SET-UP

It is possible to extend the AFD set-up shown in Fig. 1 to a multi-model AFD, MM-AFD, set-up. This can be done by including a number of residual vectors that are derived based on different models. This is shown in Fig 2.

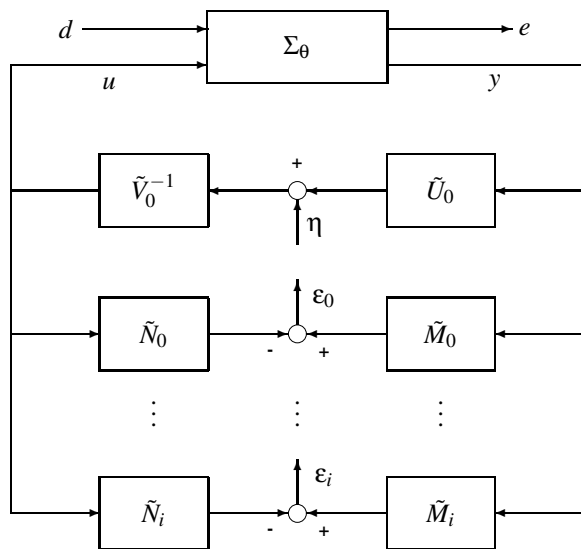


Fig. 2. The AFD set-up based on a multi model approach. $(\tilde{M}_i, \tilde{N}_i)$ is the i 'th model with $i = 0$ is the nominal model.

Let the transfer function from η to the residual vector ϵ_i be given by $S_i(\theta)$. This will give the following simple conditions for system model identification for a given θ :

- System model identification

$$\begin{aligned} S_i(\bar{\theta}) &= 0, \quad \text{for } \bar{\theta} = \bar{\theta}_i \\ S_j(\bar{\theta}) &\neq 0, \quad \text{for } \bar{\theta} \neq \bar{\theta}_i, \quad i \neq j. \end{aligned}$$

It is clear that in general it is not possible to require that one of the fault signature matrices, $S_i(\theta)$, is exact equal to zero for the identification of the correct model. The reason is that only a limited number of models will be applied and it will therefore be very difficult to require that one of the fault signature matrices is exact zero.

Instead of just using different models for the calculation of different residual vectors we can again use the dual YJBK parameterization. Let the model be parameterized by \bar{S}_i , the residual vector given by (13) then takes the following form:

$$\epsilon_i = (\tilde{M}_0 + \bar{S}_i \tilde{U}_0) y - (\tilde{N}_0 + \bar{S}_i \tilde{V}_0) u, \quad \bar{S}_i \in \mathcal{RH}_\infty. \quad (16)$$

Using the dual YJBK parameterization of G_{yu} given by (9) or (10), the transfer functions from η to y and u are given by:

$$\begin{aligned} y &= (N_0 + V_0 S) \eta + V_0 (\tilde{M}_0 + S \tilde{U}_0) G_{yd}(\theta) d \\ u &= (M_0 + U_0 S) \eta + (M_0 + U_0 S) \tilde{U}_0 G_{yd}(\theta) d. \end{aligned}$$

Together with the residual vector in (16) gives the following residual vector:

$$\begin{aligned} \epsilon_i &= (S - \bar{S}_i) \eta + (\tilde{M}_0 + S \tilde{U}_0) G_{yd}(\theta) d \\ &= \epsilon_0 - \bar{S}_i \eta. \end{aligned} \quad (17)$$

From (17) it is clear that if we select the correct model in the residual generator in terms of a fault signature matrix \bar{S}_i , then the residual vector will be independent of the system changes.

Let's apply a periodic auxiliary input in connection with the MM-AFD in the same line as described in [10], [11] for AFD. The reason for using a periodic auxiliary input is that it is easy to detect the signature from η in the residual vector ϵ_i . Let the auxiliary input η be given by:

$$\eta = A_\eta \sin(\omega_0 t), \quad (18)$$

where the amplitude A_η and the frequency ω_0 are design parameters. These parameters need to be selected in such a way that the effect from η is maximized in ϵ_i and minimized in e , see [11] for further details. The residual vector based on the i 'th model is:

$$\epsilon_i = A_\eta |S(\theta) - \bar{S}_i| \sin(\omega_0 t + \phi) + P_{ed}(\theta, i) d. \quad (19)$$

Consider the residual ϵ_i at the specific frequency ω_0 , i.e.:

$$\delta_i = \epsilon_i \sin(\omega_0 t + \phi) \quad (20)$$

δ_i is then given by:

$$\delta_i = A_\eta |S(\theta) - \bar{S}_i| \sin^2(\omega_0 t + \phi) + P_{ed}(\theta, i) d \sin(\omega_0 t + \phi). \quad (21)$$

Further, in the Gaussian case δ_i will satisfy:

$$\delta_i \in \mathbf{N}(|S(\theta) - \bar{S}_i| A_\eta \sin^2(\omega_0 t + \phi), \sigma^2 \sin^2(\omega_0 t + \phi)), \quad (22)$$

where σ^2 is the variance of the signature from the disturbances in the residual. In (time) average we have the following mean and variance:

$$\bar{\mu} = \frac{1}{2} |S(\theta) - \bar{S}_i| A_\eta \quad \bar{\sigma}^2 = \frac{1}{2} \sigma^2. \quad (23)$$

Assume that the frequency ω_0 has been selected in such a way that the amplitude of ϵ_i given by $|S(\theta) - \bar{S}_i| A_\eta$ is a monotonic increasing function of $|\bar{\theta} - \theta|$. Local minima in the fault signature matrix might occur. This will not give a monotonic increasing amplitude as function of $|\bar{\theta} - \theta|$. This can be avoided in different ways, e.g. by selecting

another ω_0 , changing the models or incorporating it in the identification of the system model.

Assume that a number of models described by $\bar{\theta}_i$, $i \in N$ are considered. Assume that $|S(\theta, \omega_0) - \bar{S}_i(\omega_0)|$ are increasing functions of $|\bar{\theta}_i - \theta|$. Let the real system be described by $\theta \in [\bar{\theta}_i, \bar{\theta}_{i+1}]$. Then we will have:

$$\begin{aligned} A_\eta |S(\theta) - \bar{S}_i| &< A_\eta |S(\theta) - \bar{S}_{i-1}| < \dots \\ A_\eta |S(\theta) - \bar{S}_{i+1}| &< A_\eta |S(\theta) - \bar{S}_{i+2}| < \dots \end{aligned} \quad (24)$$

for $\omega = \omega_0$. See e.g. Fig. 4, where the gains of the fault signature matrices are shown for a wind turbine system.

By using interpolation it is possible to identify a very precise model based on a limit number of pre-specific models.

Normally, only the models close to the real system are considered in connection with identification of the real system. However, it is also relevant to use the residual vectors based on the other models. The reason is that the signal-noise ratio in general will be much better than residuals based on models close to the real system.

The focus in the above has been on identification of system models due to change in parameters. It has also been assumed that the systems are linear, but it might not be linear. If the system is non-linear, it is still possible to use the MM-AFD set-up. The fault signature matrix will be a function of the difference between the nominal system and the real non-linear system. In general it will not be possible to give an explicit equation for S as in the linear case. S can be considered as a measure of the change in the dynamic cause by changes of the working point. This means that S can be applied as an indirect measure of the working point for non-linear systems. The MM-AFD set-up used on a non-linear system is shown below, where a wind turbine system is considered. The variation in the working point is caused by changes in the wind speed. Using the MM-AFD approach on the wind turbine it is shown that it is possible to estimate the wind speed on the system quite well.

IV. EXAMPLE

The example is a 2MW wind turbine with a three blade rotor. Since the model includes models for the actuators the wind turbine can be described by a 5th order non-linear model given by:

$$\begin{aligned} \dot{x} &= f(x, u, d) \\ y &= g(x, u, d), \end{aligned}$$

where the 5 states $x = [\omega_r, \omega_g, \delta, T_g, \theta_b]^T$ are the rotor speed, the generator speed, the deformation of the drive train, the generator torque, and the pitch angle, respectively, the control inputs $u = [T_{g,ref}, \theta_{b,ref}]^T$ are the reference to the generator torque and the pitch angle, and the disturbance $d = v_r$ is the wind speed. The applied model describes the wind turbine in the top region, for wind speed from 11 to 26 m/sec. A linear model is derived for a wind speed around 18m/sec. The state space matrices are given in Appendix.

The wind speed is modeled as a second order system driven by white noise. The gain and the poles depend on the nominal wind speed.

The system is extended with two integrators to remove steady state errors in connection with the control of the wind turbine. The extended linear model is given by:

$$\begin{aligned} \begin{pmatrix} \dot{x} \\ \dot{x}_{int} \end{pmatrix} &= \begin{pmatrix} A & 0 \\ -C_e & 0 \end{pmatrix} \begin{pmatrix} x \\ x_{int} \end{pmatrix} + \begin{pmatrix} B_d \\ 0 \end{pmatrix} d \\ &+ \begin{pmatrix} B_u \\ 0 \end{pmatrix} u + \begin{pmatrix} 0 \\ I \end{pmatrix} r_{ref} \\ e &= (C_e \ 0) \begin{pmatrix} x \\ x_{int} \end{pmatrix} \\ y &= I \begin{pmatrix} x \\ x_{int} \end{pmatrix}. \end{aligned}$$

An LQR state feedback controller is designed for the extended system. The controller gain is given in Appendix.

The MM-AFD set-up for the wind turbine will be based on three models specified at the following wind speeds: 13 m/sec., 18 m/sec. and 23 m/sec. Based on these three models three Kalman filters are designed with respect to the disturbance in the system. Using a Kalman filter, the residual vector is given directly as the innovation vector from the filter.

Based on the feedback controller and the Kalman filter based on the model at 18 m/sec, an analysis of the fault signature matrix is derived. The analysis is not simple because it is possible to apply 2 inputs and 5 outputs. This results in a fault signature matrix of dim. 2×5 . The maximal singular value of S as function of change in the wind speed and the frequency is shown in Fig. 3.

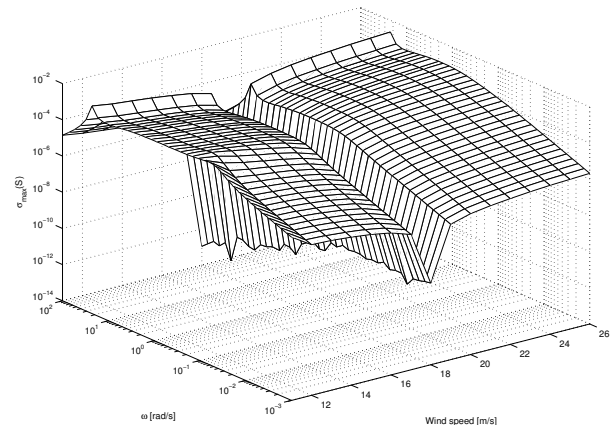


Fig. 3. The maximal singular value of S as function of change in the wind speed and the frequency. 18 m/sec is the nominal wind speed.

The selection of the frequency for the periodic auxiliary input signal is quite complicated in this case. From Fig. 3, it turns out that an obvious choice is to select ω_0 either at low frequencies or at frequencies around 10 rad/sec. Considering the ratio $(S/P_{e\eta})$ gives that the frequency should be selected at high frequencies. However, also the signal to noise ratio as well as the dynamic in the system need to be considered in connection with the selection of the frequency. This includes

that there are bounds on how fast it is possible to activate the wind turbine. With respect to these constraints the periodic auxiliary input is selected with $\omega_0 = 2.0 \text{ rad/sec}$.

The next thing to consider is the input-output directions of the fault signature matrix that need to be applied to get the best residual output. An analysis shows that the optimal input/output directions are to use the second input $\theta_{b,ref}$ and the second output ω_g .

The selection of the frequency and the directions has only been based on the Kalman filter for the model with respect to a wind speed at 18 m/sec . These selections have been verified with respect to the other two Kalman filters.

Based on the three residual signals (vectors) from the three Kalman filters the gain of the S_i as function of variations in the wind speed is calculated for the selected frequency $\omega_0 = 2.0 \text{ rad/sec}$. In Fig. 4 the gains of the transfer function from η to ϵ for the three fault signature matrices are shown.

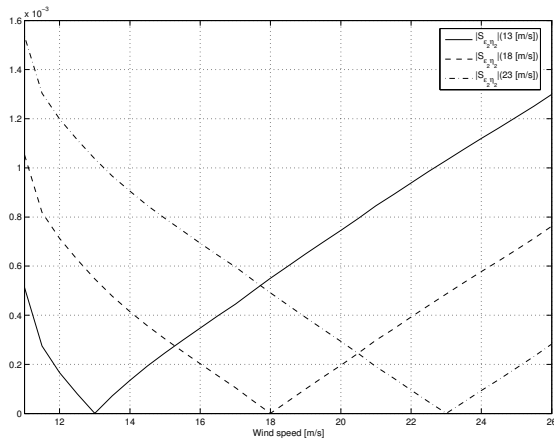


Fig. 4. The gain of the transfer function from η to ϵ for the three fault signature matrices at $\omega_0 = 2.0 \text{ rad/sec}$.

The amplitude of the auxiliary input signal is selected to be 0.15, i.e.

$$\eta = 0.15 \sin(2.0t).$$

The wind speed acting on the wind turbine is shown in Fig. 5. Note that there is a step in the mean wind speed at 300 sec . from 16 m/sec . to 18 m/sec . This wind speed will be used in the rest of the simulations.

Now let's consider the residual signals from the three Kalman filters. These residual signals are shown in Fig. 6, where a band-pass filter has been applied on the residuals.

As it can be seen from the residual signals it is almost impossible to see the signature from the auxiliary input signal. It is therefore not possible to use the residual signals directly. Instead of using the residual signals directly, we need only to consider the residual signals at the same frequency as used in the auxiliary input signal, i.e. $\omega_0 = 2.0 \text{ rad/sec}$ as shown in (20). Using this new residual signal δ_i has a mean value that depends on the gain of S_i and the amplitude of auxiliary input signal, see (23). It is then simple to estimate the mean

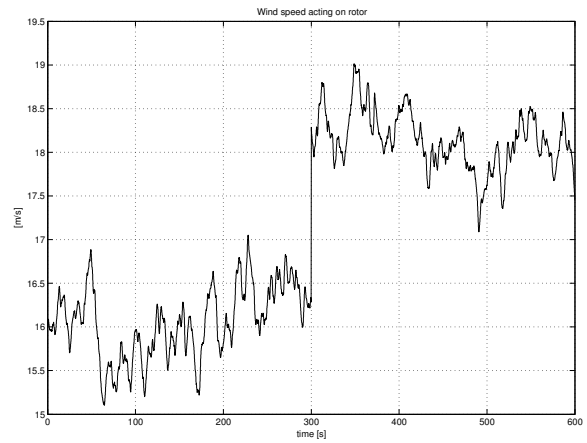


Fig. 5. The wind speed acting on the wind turbine.

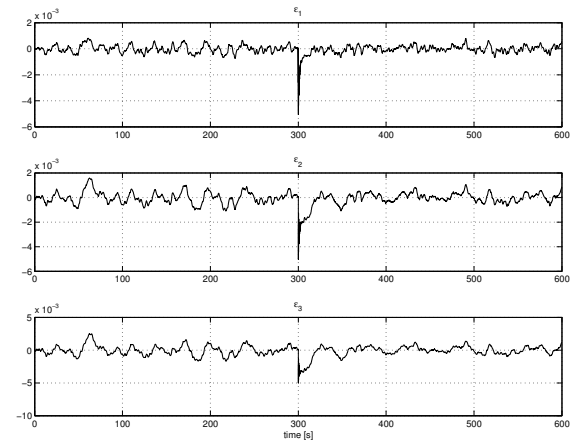


Fig. 6. The three residual signals.

value of δ_i by using an integration of the signal. This gives the following outputs:

$$\kappa_i = \left| \int_0^T (\epsilon_i e^{j\omega_0 t}) dt \right|, \quad i = \{13, 18, 23\}.$$

In Fig. 7 the curves for the three κ 's are shown. It is clear from the three curves that in the interval from $t = 0 \text{ sec}$. to 300 sec ., all three curves are constantly increasing. Further, it is also clear that the curve based on a wind speed at 23 m/sec . has the largest increasing rate. For $t = [0, 300] \text{ sec}$. the three curves satisfy:

$$\kappa_{18} < \kappa_{13} < \kappa_{23}.$$

Combining this with the curves in Fig. 4 we get that the wind speed will be in between 13 m/sec . and 18 m/sec ., which is also correct. For the time interval from 300 sec . to 600 sec ., where the wind speed is changed from 16 m/sec . to 18 m/sec ., we can see that the curve for κ_{18} almost gets constant. This is in line with the associated curve in Fig. 4, where the gain of S_{18} is zero for this wind speed. This indicates that the real wind speed is close to 18 m/sec .

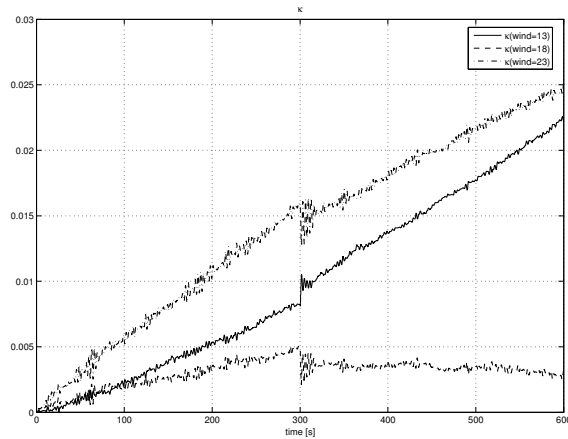


Fig. 7. The three κ curves. The upper curve is for κ_{23} , the middle is for κ_{13} and the lower one is for κ_{18} .

It is also possible to get an estimate of the wind speed by using the three curves in Fig. 7. This can be done in different ways. Here, the gains of the three fault signature matrices are estimated from the curves in Fig. 7.

Based on the estimates of the three gains the wind speed is then calculated by interpolation using the curves in Fig. 4. The estimated wind speed is shown in Fig. 8 together with the real wind speed. As it can be seen from Fig. 8 the estimated wind speed is reasonably good, except in the beginning.

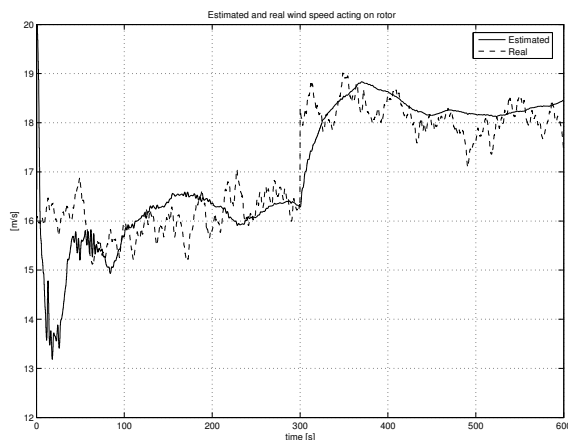


Fig. 8. Estimate of the wind speed together with the real wind speed.

APPENDIX

The state space matrices for a linear model of the wind turbine at $v_r = 18$ m/sec are given by:

$$A = \begin{bmatrix} -0.37029 & 0.001672 & -14.212 & 0 & -0.027949 \\ 96.978 & -1.1409 & 9697.8 & -0.0066667 & 0 \\ 1 & -0.011765 & 0 & 0 & 0 \\ 0 & 0 & 0 & -10 & 0 \\ 0 & 0 & 0 & 0 & -5 \end{bmatrix}$$

$$B_d = \begin{bmatrix} 0.037945 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}, \quad B_u = \begin{bmatrix} 0 & 0 \\ 0 & 0 \\ 10 & 0 \\ 0 & 5 \end{bmatrix}$$

$$C_e = \begin{bmatrix} 0 & 11937 & 0 & 167.55 & 0 \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix}.$$

The LQR controller gain is given by:

$$F_{LQR} = [F_{lqr} \quad F_{lqr,i}],$$

where

$$F_{lqr} = \begin{bmatrix} -6082.3 & -8.6773 & 5468.3 & 0.093325 & 35.654 \\ -5.7077 & -0.0083656 & -0.26201 & 3.1279e-007 & 0.0314 \end{bmatrix}$$

$$F_{lqr,i} = \begin{bmatrix} -0.0054848 & 4775.4 \\ 3.1172e-007 & 1.4743 \end{bmatrix}.$$

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