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Dispersion of the second-order nonlinear susceptibility in ZnTe, ZnSe, and ZnS

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We have measured the absolute values of the second-harmonic generation (SHG) coefficient $|d|$ for the zinc-blende II-VI semiconductors ZnTe, ZnSe, and ZnS at room temperature. The investigated spectral region of the fundamental radiation $\lambda_F$ ranges from 520 to 1321 nm using various pulsed laser sources. In the transparent region of the II-VI semiconductors, the SHG coefficient exceeds the values of birefringent materials as ammonium dihydrogen phosphate (ADP) and potassium dihydrogen phosphate (KDP) by one or two orders of magnitudes. Above the $E_0$ band gap a strong dispersion of $|d|$ is observed, showing a maximum for a second-harmonic frequency close to the $E_1$ gap. The experimental results are compared to calculated values using a simple three-band model including spin-orbit splitting. Substantial agreement is found to the experimentally observed dispersion of the second-order nonlinear susceptibility. [S0163-1829(98)06539-4]

I. INTRODUCTION

Experiments on second-harmonic generation (SHG) in II-VI semiconductors date back to the year 1963. Using a Nd:YAG laser (where YAG denotes yttrium aluminum garnet) Miller, Kleinmann, and Savage determined the second-order nonlinear coefficient $|\chi^{(2)}_{114}|$ of CdS, which was found to be 60 times higher than in potassium dihydrogen phosphate (KDP). Subsequent investigations on other II-VI crystals confirmed the observation of high second-harmonic generation coefficients, but were mostly restricted to the fundamental wavelengths of $\lambda_F = 1.06 \mu m$ (Nd:YAG laser) and $\lambda_F = 10.6 \mu m$ (CO$_2$ laser) due to the lack of tunable high-intensity laser sources. Experiments on the dispersion of the second-order nonlinear susceptibility in ZnTe, InSb, GaAs, and InAs were carried out by Chang, Dukuing, and Blombergen using nine discrete fundamental radiation sources. With the advent of dye lasers, more systematic experimental results became available, mainly acquired from III-V semiconductors. Only few investigations report on the dispersion of $|\chi^{(2)}_{114}|$ in wide-gap II-VI semiconductors, although these materials possess high SHG coefficients and thus have the potential for efficient SHG in the visible spectral region using II-VI waveguide structures.

A microscopic expression for $|\chi^{(2)}_{114}|$ can be obtained from second-order perturbation calculations. However, a complete understanding of the dispersion of $|\chi^{(2)}_{114}|$ requires detailed information of the energies and wave functions of the electronic states in the entire first Brillouin zone (BZ). Therefore, the dispersion of the nonlinear susceptibility can be used as a sensitive test of various band-structure theories, but with the difficulty of measurements of nonlinear properties. The early calculations of $|\chi^{(2)}_{114}|$ in zinc-blende crystals by Bell used a simplified three-band model, taking into account the spin-orbit splitting of the valence band at the $\Gamma$ point. The band structure was modeled around a few principal critical points assuming constant transition matrix elements over the entire BZ. Substantial agreement was found with the experimental results of Chang, Dukuing, and Blombergen. Since then, Fong and Shen have employed pseudopotential band-structure calculations using four conduction and valence bands and Moss and co-workers employed an empirical tight-binding calculation of $|\chi^{(2)}_{114}|$ for various III-V and II-VI semiconductors. In general, the agreement with the experiment was improved by these approaches; however, significant differences between theory and available experimental data still exist.

The general interest in the absolute values $|\chi^{(2)}_{114}|$ of wide-gap II-VI semiconductors and the existing discrepancies between the theories and the experimental results prompted us to investigate the dispersion of zinc-blende ZnTe, ZnSe, and ZnS semiconductors in the wavelength range $\lambda_F = 520-1321$ nm of the fundamental radiation. The data obtained are compared to the theory proposed by Bell including the spin-orbit coupling of the valence band.

II. EXPERIMENTAL SETUP

The absolute values of the SHG coefficient in zinc-blende ZnTe, ZnSe, and ZnS bulk crystals were determined using various radiation sources. A diode pumped Q-switched Nd:YLF laser (YLF denotes yttrium lithium fluoride) emitting at $\lambda_F = 1.321$ and 1.047 $\mu m$ was used as the spectrally narrow fundamental light source, having a repetition rate of 1 kHz. The pulse duration measured by a photodiode was $\Delta t = 140$ and 46 ns, respectively, resulting in peak powers of 100 W and 1 kW. In the spectral range of $\lambda_F = 720-1060$ nm a tunable picosecond Ti:sapphire laser with a repetition rate of 82 MHz was employed. Investigations ranging from $\lambda_F = 1050$ to 1210 nm were performed using a potassium titanyl phosphate optical parametric oscillator, which was pumped by the picosecond Ti:sapphire laser. The pulse widths around $\Delta t = 1$ ps were measured by an autocorrelator. The peak power of the near infrared pulses were about 500 W. In the region between $\lambda_F = 520$ and 740...
nm, a combination of a regenerative amplified femtosecond Ti:sapphire laser, a white-light generator, and an optical parametric amplifier was used. The pulse widths in this case were adjusted by a pulse shaper to $\Delta t = 200$ fs. The peak power of these pulses was about 20 kW.

The II-VI crystals investigated have been cleaved along the (110) surface to obtain (0.5–3)-mm-thick, plane-parallel bars. The actual length of the samples was determined using a microscope. The fundamental beams were only weakly focused (having a beam waist of approximately $2w_0 = 300 \mu$m) onto the II-VI samples in order to minimize beam-size effects. The beam diameter at the sample position was determined by a charge coupled device camera. The position of the focus on the (110) cleaving surface was adjusted by moving the sample with a piezoelectric translation stage, which also allows a rotation of the sample perpendicular to the incident beam. The emerging SHG signal went through a polarizer, a color filter, and a quartz-lar to the incident beam. The emerging second-harmonic power is given by

$$P_{2\omega}(\theta) = \frac{8}{\varepsilon_0 c \pi w_0} d^2 T_{2\omega}(\theta) P(\theta)^2 \left( \frac{P_2^2}{n(\omega)^2 - (2\omega)^2} \right) B(\theta) R(\theta) \sin^2(\psi),$$

(2)

with the oscillating term

$$\sin^2(\psi) = \sin \left[ \frac{2\pi L}{\lambda_F} \left( n(\omega) \cos \theta - n(2\omega) \cos \theta_{2\omega} \right) \right] = \sin^2(\Delta \beta L/2).$$

(3)

Besides the rotation angle $\theta$ (corresponding to $\theta_{\omega}, \theta_{2\omega}$ within the crystal) the decisive parameters are the refractive indices $n(\omega)$, the length of the crystal $L$, the nonlinear coefficient $d$, the $e^{-2}$ radius of the Gaussian beam waist $w_0$, the fundamental power $P_\omega$, and the fundamental wavelength $\lambda_F$. The angle-dependent transmission factors

$$t_\omega(\theta) = \frac{2 \cos \theta}{n(\omega) \cos \theta + \cos \theta_{2\omega}},$$

(4)

and

$$T_{2\omega}(\theta) = \frac{2 n(2\omega) \cos \theta_{2\omega} \left[ \cos \theta + n(\omega) \cos \theta_{\omega} \left[ n(\omega) \cos \theta_{\omega} + n(2\omega) \cos \theta_{2\omega} \right] \right]}{[n(2\omega) \cos \theta_{2\omega} + \cos \theta]^2},$$

(5)

of the fundamental and the second-harmonic wave, respectively, are obtained by boundary conditions. The projection factor $p(\theta) = 2 \cos(\theta_{\omega} + \pi/4) \cos(\theta_{\omega} - \pi/4)$ accounts for the tensor character of the nonlinear susceptibility $\chi^{(2)}$. $R(\theta)$ and $B(\theta)$ are corrections considering multiple reflections and beam diameter effects as expressed in Ref. 30. The abbreviation $\Delta \beta$ in Eq. (3) is the propagation constant mismatch between the fundamental and the second-harmonic wave.

By varying the incident angle of the Nd:YLF laser beam on the II-VI samples, the intensity of the transmitted second-harmonic wave oscillates due to the interference term [Eq. (3)]. These Maker oscillations of a 1.64-mm-long ZnSe crystal at the fundamental wavelengths of $\lambda_F = 1321$ and 1047 nm are shown in Figs. 1(a) and 1(b), respectively. From the angular dependence of the minima the coherence length $\xi$ can be derived. The coherence length decreases when the $E_\omega(\theta)$ band gap is approached due to the high refractive index dispersion in the II-VI semiconductors and reaches only a few micrometers as summarized in Table I. The accuracy of the measurements is limited by the determination of the sample lengths, which was estimated to $\pm 2\%$.

The absolute value of the SHG coefficient $|d_f|$ was evaluated from the envelope of the maxima, which was determined according to Eq. (2). The necessary values of the refractive indices were taken from Refs. 31–33 or were calculated from Sellmair equations.

$$l_c = \frac{\pi}{\Delta \beta} = \frac{\lambda_F}{4[n(2\omega) - n(\omega)]},$$

(6)
angular where the peak power is given by $P_{w2} = \bar{P}_w / r \Delta t$ with average laser power $\bar{P}_w$, repetition rate $r$, and pulse duration $\Delta t$. Furthermore, the temporal decrease of the SHG pulse by a factor of approximately $\sqrt{2}$ was taken into account. In addition, finite beam width effects and multiple reflection corrections were considered as treated in Ref. 30. The evaluated $|d|$ values obtained with the pulsed Nd:YLF laser are summarized in Table I and are plotted as full squares in Figs. 3–6. A comparison with absolute values measured by other groups ($\lambda_F = 1.06 \text{ } \mu\text{m})$ shows good agreement for ZnSe (Ref. 3) and ZnTe.

When a spectrally broad picosecond pulse ($\Delta \lambda \approx 2 \text{ } \text{nm}$) is used, interference effects occur in the spectrum of the SHG signal at normal incidence. Figures 2(a) and 2(b) show this feature at the fundamental wavelengths of $\lambda_F = 980.4$ and 928.4 nm for a ZnS crystal of 1.15 mm length. The temporal pulse widths were $\Delta t = 850$ and 600 fs, respectively. The dashed lines in Fig. 2 are obtained by solving Eq. (2) in the frequency domain according to

$$P_{w2} = \frac{C(\omega_0)}{4\gamma} \left[ \frac{1}{\omega^2/2} \int_{\omega^2/2}^{\infty} g(\omega_1 - \omega_0)g(\omega_2 - \omega_1 - \omega_0) \right] \times (1 - \gamma e^{i\Delta \beta' t}) d\omega_1. \quad (7)$$

The function $g(\omega - \omega_0)$ is the Fourier-transformed function of the temporal pulse shape $f(t)$. The used laser system provides Fourier-limited sech($t$) field pulses; $\omega_0$ gives the center wavelength of the fundamental pulse. The constant $C(\omega_0)$ contains all factors appearing in Eq. (2) at an angle of $\theta = 0^\circ$ without the oscillating term $\sin^2(\psi)$. $\gamma$ is given by the relation

$$\gamma = \frac{2n_2(\omega_0)(n_\omega_0 + 1)}{f(n_2\omega_0 + n_\omega_0)(n_2\omega_0 + 1)}. \quad (8)$$

The phase mismatch $\Delta \beta'$ reads

$$\Delta \beta' = \frac{\omega_2 n(\omega_2)}{c} - \frac{\omega_1 n(\omega_1)}{c} - \frac{(\omega_2 - \omega_1)n(\omega_2 - \omega_1)}{c}. \quad (9)$$

Equation (7) accounts for all possible combinations of fundamental frequencies leading to a second-harmonic power at frequency $\omega_2$ around $2\omega_0$ (sum-frequency generation). The theoretically obtained second-harmonic spectrum in Fig. 2 shows good agreement with the experimentally observed data. The lower modulation in the experimental curves is attributed to the limited experimental resolution $\Delta \lambda = 0.2 \text{ } \text{nm}.$

<table>
<thead>
<tr>
<th>Semiconductor</th>
<th>$\lambda_F = 1321 \text{ nm}$</th>
<th>$\lambda_F = 1047 \text{ nm}$</th>
<th>$\lambda_F = 1.06 \text{ } \mu\text{m}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>ZnTe</td>
<td>1.57</td>
<td>1.62</td>
<td>52</td>
</tr>
<tr>
<td>ZnSe</td>
<td>1.64</td>
<td>2.92</td>
<td>30</td>
</tr>
<tr>
<td>ZnS</td>
<td>2.54</td>
<td>5.08</td>
<td>8</td>
</tr>
</tbody>
</table>

$^a$Reference 9.

$^b$Reference 3.
FIG. 3. Dispersion of the SHG coefficient $|d|$ of zinc-blende ZnTe, ZnSe, and ZnS crystals in their second-harmonic transparent spectral region. The black squares represent values obtained with the Nd:YAG laser source. In addition, values of common birefringent materials are shown. The dotted curves are guides for the eye. In the Nd:YAG laser source. In addition, values of common birefringent materials are shown. The dotted curves are guides for the eye.

In order to determine the absolute values of the SHG coefficient $|d|$ using picosecond pulses the experiments were performed without spectral resolution. Since we integrate over all Maker oscillations of the second-harmonic power, the measured power was corrected by a factor of 2 to obtain the value of $|d|$ from Eq. (2). (The factor of 2 is valid if more than two oscillations occur in the second-harmonic power spectrum, which was generally the case in the performed experiments.) Again, the shortening of the SHG pulse by a factor of approximately $\nu_2$ was taken into account. In order to minimize the pulse broadening due to the refractive index dispersion of the II-VI crystals, we used pulse widths of about $\Delta t = 1$ ps. The dispersion of the SHG coefficient $|d|$ obtained in the transparent region of the investigated wide gap (II-VI) semiconductors is given in Fig. 3 together with values of some birefringent materials such as ADP, KDP, and LiNbO$_3$ which are generally used in phase-matchable SHG devices. The comparison shows that the SHG coefficients of II-VI semiconductors exceed the values of $d_{31}$ and $d_{36}$ of the birefringent materials by one or two orders of magnitude, indicating II-VI materials as promising materials for efficient second-harmonic generation in the visible spectral range.

When the frequency of the SHG wave exceeds the $E_0$ band-gap energy, the Maker oscillations disappear due to the strong linear absorption of the second-harmonic wave. The absolute value of the SHG coefficient is now determined using the complex modulus $\tilde{n}(\omega) = n(\omega) + \nu k(\omega)$. In the case of a strong absorption of the second-harmonic wave [$\alpha(2\omega) = 10^5$ cm$^{-1}$], but weak absorption of the fundamental beam $\nu k(\omega) \approx 0$, the second-harmonic power emitted at normal incidence ($\theta = 0^\circ$) reads

$$P_{2\omega}(\theta = 0^\circ) = \frac{2}{\epsilon_0 c \pi w_0} d_T^4 \omega \times \
abla \left[ \frac{\tilde{P}_\omega}{(\Delta n)^2 + \left( \frac{\lambda_F \alpha(2\omega)}{8\pi} \right)^2 \tilde{n}(2\omega) + 1} \right]^2,$$

with $\alpha(2\omega) = (4\pi/\lambda) \nu k(2\omega)$ and $\Delta n = n(2\omega) - n(\omega)$. Multiple reflections and beam size effects have been neglected. The values of the linear absorption $\alpha(2\omega)$ were taken from the literature.

The linear absorption of the second-harmonic wave and the two-photon absorption lead to band-to-band transitions and impurity transitions. The detection of this erroneous radiation is minimized by direction filtering along the wave vector $k_{2\omega}$ of the SHG beam and by spectral discrimination ($\Delta \lambda \approx 5$ nm) of the SHG light. Within the spectral region from $\lambda_F = 520$ to 740 nm, the pulses possess a temporal width of $\Delta t = 200$ fs. In this case the samples were cut to a length of approximately 0.7 mm in order to avoid a significant pulse broadening of the fundamental wave within the material.

The continuation of the dispersion of the SHG coefficients $|d|$ into the $2\omega$ absorptive regions of the semiconductors ZnTe, ZnSe, and ZnS is shown in Figs. 4, 5, and 6, respectively. In all II-VI semiconductors, an increase of the SHG coefficient is observed when the SHG frequency approaches the $E_0$ band-gap energy. In the excitonic region of ZnTe only a weak resonance appears. Above the $E_0$ band gap a strong increase of the SHG coefficient is observed, which is in agreement with the investigation of Chang, Dukuing, and Blombergen. (The absolute values of the nonlinear coefficient $|d|$ are in agreement within a 20% deviation.) The SHG coefficient shows a maximum at the $E_0$ gap, as already indicated in Ref. 9, and a further peak when the $E_0 + \Delta_1$ band gap is reached. In the ZnSe and ZnS crystals a distinct resonance appears in the vicinity of the $E_0$ gap. Due to the high exciton binding energies of 20 and 35 meV in ZnSe and ZnS, respectively, the influence of excitonic effects is present at room temperature and the $E_0$ resonances of $|d|$ are attributed to an excitonic enhancement.

IV. COMPARISON WITH THEORY

The microscopic expression of $\chi^{(2)}$ obtained from second-order perturbation calculations is given by

$$\chi^{(2)} = \
abla \left[ \frac{\tilde{P}_\omega}{(\Delta n)^2 + \left( \frac{\lambda_F \alpha(2\omega)}{8\pi} \right)^2 \tilde{n}(2\omega) + 1} \right]^2,$$
wave vector \( \mathbf{k} \) calculated dispersion curve obtained with the Nd:YAG laser source. The full line gives the calculated dispersion curve [Eq. (12)].

\[
\chi^{(2)}_{\mu\alpha\beta}(\omega, \omega, \omega) = -i \frac{1}{32\hbar_0} \left( \frac{e}{m_0\pi\omega} \right)^3 \sum_{n, n', n''} \int_{BZ} d^3k \left[ \begin{array}{l}

\frac{p_{nn}^\alpha p_{n'n''}^\beta p_{n''n}^\alpha + p_{nn}^\beta p_{n'n''}^\alpha p_{n''n}^\alpha}{E_{n''}(\mathbf{k}) - 2\hbar\omega}

+ \frac{p_{nn}^\alpha p_{n'n''}^\beta p_{n''n}^\alpha + p_{nn}^\beta p_{n'n''}^\alpha p_{n''n}^\alpha}{E_{n''}(\mathbf{k}) + \hbar\omega}

+ \frac{p_{nn}^\alpha p_{n'n''}^\beta p_{n''n}^\alpha + p_{nn}^\beta p_{n'n''}^\alpha p_{n''n}^\alpha}{E_{n''}(\mathbf{k}) + 2\hbar\omega} \end{array} \right] f_{n,k}(\mathbf{k}),
\]

Here the electrons are assumed to occupy Bloch states \( \psi_{n,k}(\mathbf{r}) = u_{n,k}(\mathbf{r}) \exp(\mathbf{k} \cdot \mathbf{r}) \) specified by the band label \( n \) and wave vector \( \mathbf{k} \) with the energy \( E_n(\mathbf{k}) \). \( f_{n,k} \) is the equilibrium Fermi-Dirac occupation function for the state \( \psi_{n,k}(\mathbf{r}) \) and \( p_{n',n}(\mathbf{k}) \) is the matrix element of the linear momentum operator between states \( \psi_{n,k}(\mathbf{r}) \) and \( \psi_{n',k}(\mathbf{r}) \). \( E_{n''}(\mathbf{k}) \) is the corresponding transition energy \( E_{n''}(\mathbf{k}) - E_{n}(\mathbf{k}) \).

At least three bands are necessary to obtain a contribution to \( \chi^{(2)}_{\mu\alpha\beta}(\omega, \omega, \omega) \) since if only two bands are considered, the contributions for \( \mathbf{k} \) and \( -\mathbf{k} \) cancel each other. Neglecting spin-orbit coupling, the top valence band \( \Gamma_{15c} \) and the two lowest conduction bands \( (\Gamma_1, \Gamma_{15v}) \) constitute a minimal set of three bands with a finite contribution to \( \chi^{(2)}_{\mu\alpha\beta} \). Even with these simplifications, Eq. (11) is not amenable without a detailed information of the energies and the wave functions of the electronic states in the first BZ. To avoid extensive full band-structure calculations, we follow the approach of Bell,\(^{23}\) modelling the bands around a few principal critical points. Such points exist at the \( \Gamma \) point \( \mathbf{k}=0 \) (the \( E_0, E_0' \) gap), and along \( \mathbf{k}=(k/\sqrt{3})(111) \) approaching the \( L \) points (the \( E_1, E_1' \) gap). The \( X \) points (the \( E_2 \) gap) were neglected here due to the large \( E_2 \) energy.

The \( E_0, E_0' \) transitions are represented by three-dimensional parabolic bands extending to infinite \( \mathbf{k} \), yielding the expression

\[
\chi^{(2)}_{\mu\alpha\beta}(\omega, \omega, \omega) = C_\Gamma(PP'Q) \frac{1}{\omega^3} \frac{1}{\alpha_1\alpha_2} \sum_{i=1}^{6} S_i T_i(x_i, x_i'),
\]

with

\[
C_\Gamma = -i \frac{1}{4\pi\hbar_0} \left( \frac{e}{\hbar}\right)^3, \quad x_i = \frac{E_0 + \nu_i\hbar\omega}{\alpha_1},
\]

\[
x_i' = \frac{E_0' + \mu_i\hbar\omega}{\alpha_2}, \quad T_i(x_i, x_i') = \frac{1}{\sqrt{x_i + x_i'}},
\]

\[
S_i = \begin{cases} 1, & i=1,2,3 \\ -1, & i=4,5,6 \end{cases}, \quad \nu_i = -2,+1,+1,-1,-1,+2,
\]

\[
\mu_i = -1,-1,2,-2,2,1,1.
\]

\( \alpha_1 = h^2/2m_v \) and \( \alpha_2 = h^2/2m_c \), represent the inverse reduced masses of a band pair. We assume that the products of the three matrix elements of the linear momentum operator \( PP'Q \) between the \( p \)-like \( \Gamma_{15v} \) valence band and the \( s \)-like \( \Gamma_1 \) conduction band \( (P = \hbar/m_0 \int \Omega \psi_{c}^\dagger \psi_{c}^\dagger \psi_{c}^\dagger \psi_{c}^2 d^3x) \), between the \( \Gamma_1 \) conduction band and \( p \)-like \( \Gamma_{15c} \) conduction band \( (P' = \hbar/m_0 \int \psi_{c}^\dagger \psi_{c}^\dagger \psi_{c}^\dagger \psi_{c}^2 d^3x) \), and between the \( \Gamma_{15v} \) valence band and \( \Gamma_{15c} \) conduction band \( (Q = \hbar/m_0 \int \psi_{c}^\dagger \psi_{c}^\dagger \psi_{c}^\dagger \psi_{c}^2 d^3x) \) remain constant over the entire BZ.

The \( E_1, E_1' \) transitions are represented by two-dimensional parabolic bands. [The effective masses along the \((111)\) direction are assumed to be infinity due to the nearly parallel conduction and valence bands.] Integration over the BZ yields an expression of the form of Eq. (12) with

\[
C_L = -i \frac{\sqrt{3}}{e_0\hbar_0} \left( \frac{e}{\hbar}\right)^3, \quad x_i = \frac{E_1 + \nu_i\hbar\omega}{\alpha_1},
\]
TABLE II. Parameters used for calculating the dispersion of the SHG coefficient $|d|$ according to Eq. (12).

<table>
<thead>
<tr>
<th>Parameter</th>
<th>ZnTe</th>
<th>ZnSe</th>
<th>ZnS</th>
</tr>
</thead>
<tbody>
<tr>
<td>$E_0$ (eV)</td>
<td>2.28</td>
<td>2.69</td>
<td>3.68</td>
</tr>
<tr>
<td>$E'_0$ (eV)</td>
<td>5.4</td>
<td>8.45</td>
<td>5.79</td>
</tr>
<tr>
<td>$\Delta_0$ (eV)</td>
<td>0.92</td>
<td>0.4</td>
<td>0.07</td>
</tr>
<tr>
<td>$E_1$ (eV)</td>
<td>3.52</td>
<td>4.75</td>
<td>5.73</td>
</tr>
<tr>
<td>$E'_1$ (eV)</td>
<td>6.9</td>
<td>9.1</td>
<td>9.78</td>
</tr>
<tr>
<td>$\Delta_1$ (eV)</td>
<td>0.56</td>
<td>0.35</td>
<td>0.55</td>
</tr>
<tr>
<td>$m^*(m_0)$</td>
<td>0.12</td>
<td>0.14</td>
<td>0.22</td>
</tr>
<tr>
<td>$\gamma_1$</td>
<td>3.8</td>
<td>2.45</td>
<td>2.54</td>
</tr>
<tr>
<td>$\gamma_2$</td>
<td>0.72</td>
<td>0.61</td>
<td>0.75</td>
</tr>
<tr>
<td>$\gamma_3$</td>
<td>1.34</td>
<td>1.11</td>
<td>1.09</td>
</tr>
<tr>
<td>$P$ (eV nm)</td>
<td>0.89</td>
<td>0.85</td>
<td>1.02</td>
</tr>
<tr>
<td>$P'/ii$ (eV nm)</td>
<td>0.35</td>
<td>0.44</td>
<td>0.55</td>
</tr>
<tr>
<td>$Q$ (eV nm)</td>
<td>0.74</td>
<td>0.72</td>
<td>0.6</td>
</tr>
<tr>
<td>$a_0$ (nm)</td>
<td>6.1035</td>
<td>5.668</td>
<td>5.4102</td>
</tr>
</tbody>
</table>

*aReference 31.  
bReference 51.  
cReference 45.  
dReference 52.  
eReference 46.  
fReference 53.  
gReference 47.  
hReference 54.  
iReference 48.  
jReference 55.  
kReference 49.  
lReference 56.  
mReference 50.

\[ m_{hh,\text{nh}} = m_0 \frac{1 - \frac{6}{5} \gamma_3 + \frac{4}{5} \gamma_2}{\gamma_1} \],

where $m_0$ is the vacuum electron mass and $\gamma_1$, $\gamma_2$, and $\gamma_3$ are the Luttinger parameters.

The effective masses of the spin-orbit split-off $\Gamma_7$ valence band $m_{\text{so}}$ as well as the reduced effective masses $\alpha'_1$ and $\alpha'_1\Delta_1$ between the spin-orbit split $L_{3s}$ valence bands ($L_{4,5}$,$L_{6}$) and the $L_{1s}$ conduction band, respectively, were calculated according to the relations\textsuperscript{40,42}

\[ \frac{m_0}{m_{\text{so}}} = 1 + \frac{2(Pm_0/h)^2}{3m_0(E_0 + \Delta_0)} + \frac{4(Qm_0/h)^2}{3m_0(E'_0 + \Delta_0)} \]

and

\[ \alpha'_1 = P^2 \left( \frac{1}{E_1} + \frac{1}{2(E_1 + \Delta_1)} \right), \]

\[ \alpha'_1\Delta_1 = P^2 \left( \frac{1}{2E_1} + \frac{1}{E_1 + \Delta_1} \right). \]

The effective mass of the $\Gamma_{15\varepsilon}$ conduction band was approximated by the mean hole mass $m_h = m_0/\gamma_1$. The inverse reduced mass $\alpha'_2$ between the $L_{3s}$ conduction band, where spin-orbit coupling has been neglected, and the split $L_{3y}$ ($L_{4,5}$,$L_{6}$) valence bands were assumed to be $\alpha'_2 = h^2/m_h$. As proposed in Ref. 23, the transition energies were thermally broadened by an energy of $\eta = 0.03$ eV ($\approx k_BT$) for the sake of comparison with observations at room temperature.

The measured absolute values and the dispersion of the SHG coefficient $|d|$ are reproduced within a factor of 2 for the investigated II-VI crystals. In all materials, a resonant enhancement is observed at the corresponding $E_0$ gap energy. Above the $E_0$ gap the growing influence of the $L$ points becomes important, which explains the strong increase of the SHG coefficient in ZnTe and ZnSe close to the $E_1$ gap. Furthermore the structure caused by the $E_1 + \Delta_1$ band gap is reproduced in the ZnTe crystal. Relatively strong deviations, however, occur in the energy range between the $\Gamma$ point and the $L$ points where the model underestimates the experimentally observed dispersion of $|d|$.

V. DISCUSSION

The experimental accuracy in the determination of the SHG coefficients $|d|$ is mainly limited by the calibration of the detection system and by the determination of the beam diameter within the sample. Both uncertainties lead to an total experimental error of $\pm 20\%$. However, since we do not use a nonlinear standard as other groups,\textsuperscript{9–14} but a calibrated GaAs photomultiplier, the experimental error does not affect the dispersive structure of $|d|$, but only changes its absolute value. The uncertainty of the refractive index values and the linear absorption does not lead to a significant error (smaller than $\pm 5\%$). The influence of laser fluctuations on the accuracy ($<5\%$ peak to peak) is also not important. Sample heating caused by the laser pulses is estimated to be insignificant as the used pulse energies are in the order of a few nanojoules. Since a spectral discrimination was used in our experiments, the influence of erroneous impurity or band-toc-
band luminescence was also negligible.

The existing discrepancies between the theoretical modelling and the experimental data are thus attributed to inaccuracies of the model. One weak point of the applied model is the use of only one valence band and two conduction bands while other bands are neglected. Furthermore, transitions along the Δ direction have been neglected and effective masses are used, which are roughly estimated at the L points. On the other hand, the discrepancies still exist if a full band-structure calculation using an empirical tight-binding method is applied.27 Again, a minimum of d occurs above the E₀ gap that is in contrast to the experimental data. Since these calculations neglect the spin-orbit interaction of the valence bands, the agreement with the experimentally observed structures is even weaker than that obtained with the simplified model by Bell. A significant improvement is expected, however, if more than three bands are considered as has been shown by Fong and Shen calculating d of various III-V semiconductors.25 Using an empirical pseudopotential method that includes the spin-orbit coupling of essential bands, a better reproduction of the experiments is found. In particular, the saddle point above the E₀ gap is much less pronounced in the calculated curves. Furthermore, the discrepancies between theory and experiment are attributed to the neglect of the Coulomb interaction between the electron and hole, which influences strongly the dispersion at the E₀ gap but also for higher transitions. Since the dispersion of the SHG coefficient d can be regarded as a more sensitive test to band structure theories than the linear dielectric constant ε(ω), the acquired nonlinear data thus provoke repeated calculations with improved theoretical models including also excitonic effects.

VI. SUMMARY

We have performed precise measurements of the SHG coefficient d in ZnTe, ZnSe, and ZnS crystals within the spectral region between λₚ = 520 and 1321 nm. Our results in ZnTe agree with earlier measurements of Chang, Dukuing, and Blombergen.9 The structure of the dispersion of d can clearly be interpreted as two-photon resonances derived from a three-band model considering the spin-orbit splitting of the valence band. The model reproduces the absolute values in the transparent region of the II-VI materials within a factor of 2. Furthermore, the structure of d is correctly reproduced in the vicinity of the L points. However, significant discrepancies occur in the energy range between the E₀ gap and the E₁ gap. The deviations between theory and experimental results are attributed to the simplified consideration of only one valence band and two top conduction bands and to the neglect of the Coulomb interaction between the electron and hole.

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