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Double Modulation Scheme for Switching Mixers Controlled by Sigma-Delta modulators

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Abstract

A new method of modulating a signal, using Sigma Delta modulation in conjunction with switching- and sub-sampling mixers, is presented. Besides the normal functionality provided by the mixer an additional mixing or modulation function can be achieved with a small modification to the existing mixer. This modification can be carried out on a big amount of mixers including the above mentioned. Although the principle was meant to be used to down convert analog signals the principle is general and can be used in digital circuits too. This paper verifies the new mixing scheme and compares it to the traditional mixing scheme. Also the most suitable applications of the different mixing schemes are discussed.

1. Introduction

The growing demand of low cost personal communications systems has motivated the intense research in the field of wireless integrated RF front-ends. Many new obstacles have to be solved to obtain a single solution IC, which leads to new front-end architectures\cite{1,2,3,4}. This paper deals with a modulation scheme, the double modulation scheme, that utilizes that clocked mixers such as the switching mixer and the subsampling mixer can be modified slightly to provide an extra modulation controlled by a 1 bit Sigma Delta modulated signal. The double modulation scheme can be used in different architectures for baseband modulation or channel selection in the receiver part. The modulation applies to both analog and digital signal processing, but the examples in this paper will focus on down-converting analog RF signals.

The text is divided into the following sections. In section 2 the principle of the switching mixer and the subsampling mixer is described. The purpose is to relate the traditional mixers to the new mixing scheme. In section 3 the principle of the new mixing scheme is presented. Section 4 deals with bandpass modulators in the mixing scheme and its limitations. Section 5 concludes this paper.

2. The conventional downconversion mixer

The down conversion mixer in the receiver usually has the functionality of a switching mixer. This is the case of the Gilbert type mixer if it is driven by a strong local oscillator (LO) signal. The LO then modulates only the sign of the RF input signal. There are two obvious reasons for driving the Gilbert cell with a strong LO. The noise amplification by the (MOS) transistors is then lower, since the transistors are only saturated for a small period of time, when the sign changes. The other reason is that in deep submicron CMOS processes it is difficult to predict the non linear deviation from the ideal multiplier. In figure 1 two realizations of switching mixers are depicted.

![Switching mixers](image-url)

Fig. 1. Switching mixers. Left: Gilbert cell with strong LO signal; Right differential CMOS sign switch.

The change of sign is equivalent to a multiplication of the RF signal with a square wave signal. The square-wave is expressed by the trigonometric series below.
It can be seen that it contains all harmonics of the fundamental frequency, but they are attenuated with the frequency. If disturbances or noise is present at the harmonic frequencies of the LO signal, they will be attenuated as they translate into the base band.

This is not the case for the subsampling-mixer. All disturbances at the harmonics will be weighted equally in the base band. The principle is shown in fig. 2, where the switches are controlled by a clock signal. At the falling edge of the clock the switches open and the momentary value of the RF signal is sampled and held on the capacitor. This value can then be processed by the following A\(D\) converter. The sub-sampling process can be seen as a multiplication of the input signal with an infinite sum of Dirac impulses spaced by the sampling period.

\[
sq(t) = \begin{cases} 
  +1 & \text{if } nT < t \leq (n+0.5)T \\
  -1 & \text{otherwise}
\end{cases}
= \frac{4}{\pi} \sum_{n=-\infty}^{\infty} \frac{1}{1+2n} \sin \left( (1+2n) \frac{2\pi}{T} t \right)
\]

It can be seen that it contains all harmonics of the fundamental frequency, but they are attenuated with the frequency. If disturbances or noise is present at the harmonic frequencies of the LO signal, they will be attenuated as they translate into the base band.

The advantage of using a subsampling mixer is that the sampling frequency is much lower than the RF carrier frequency, so the clock signal of the Sigma Delta modulator can be used for the sampling. Typically the sampling frequency is between 10 MHz and 50 MHz [5],[6],[7] which is the operation frequencies that can be achieved in a submicron CMOS process, with switched capacitor circuits or fully digital resonators [8]. The change of sign can be understood as a multiplication of the analog RF signal with a 1 bit signal.

Fig. 2. Principle of a differential realization of subsampling.

The output spectrum of the subsampler can be described as

\[
F_{\text{out}}(f) = \sum \tilde{F}_n(f - 2\pi f_s n)
\]

where \(\tilde{F}_n\) is the spectrum of the RF input signal. \(F_{\text{out}}\) is the sampled signal and \(f_s\) is the sampling frequency.

### 3. Double modulation scheme using Sigma Delta Modulation

The double modulation scheme can be used with mixers, where it is possible to modify the mixer so that the sign of the output of the mixer is controlled externally. The sign is controlled by a 1 bit Sigma Delta modulated sine signal. The subsampling mixer in figure 2 can be modified by adding 2 more switches to accommodate the sign control. In figure 3 the double modulation scheme using a subsampling mixer is shown.

The output of the mixer is therefore the result of folding the subsampled RF signal, with the spectrum of the output of the Sigma Delta modulator.

\[
F_{\text{demod}}(f) = \left( \sum_{n=-\infty}^{\infty} F_{\text{RF}}(f - 2\pi f_s n) \right) * F_{\Sigma\Delta}(f)
\]

The spectrum of the Sigma Delta modulated signal is a sum of the spectrum of the sine and the typical quantization noise spectrum of Sigma Delta modulator. The power spectral density (PSD) of the noise is approximated with the following function [9] assuming that all zeroes in the noise transfer function are at DC

\[
PSD(f) = \frac{\pi n^2}{12 f_s} \left( \sin \left( \frac{\pi f}{f_s} \right) \right) \left( 1 - \frac{2\pi f}{f_s} \right)^{2n}
\]

Where \(n\) is the order of the Sigma Delta modulator.

To verify the double modulation scheme a simulation with a Sigma Delta modulated sine signal was used to
control the $\text{sign}_s$ of the sampled RF signal. In figure 5 the spectrum of the sign control signal, with a peak at the frequency $0.012f_s$, and the RF signal with peaks at $0.016f_s$ and $0.020f_s$ are depicted. One can see the typical quantization noise, increasing with the frequency, originating from the Sigma Delta modulator.

The output of the mixer is shown in figure 6. The spectrum of the up and down converted RF signal and the original RF spectrum can be seen. The frequency translation acts exactly like an ideal multiplier, except for the quantization noise of the Sigma Delta modulator. For a given PSNR the bandwidth is limited by quantization noise of the Sigma Delta modulator.

As mentioned in the beginning the double modulation can also be achieved with a Gilbert mixer. The "change sign" unit should in this case be inserted between the LO and the LO input (the two upper differential pairs) of the Gilbert cell. In this way one is able to modulate the LO with a Sigma Delta modulated sine signal and obtain a frequency shift of the LO before it is lead into the Gilbert cell. The advantage of this configuration is that the RF signal path is fully time continuous and no out-of-band noise is folded into the baseband as is the case with a subsampling mixer. It is therefore possible to filter out the out-of-band noise after the mixing.

4. Bandpass Demodulation

In some cases it is a limiting factor that the down sampled RF signal (see figure 3) must be between 0 Hz and $f_s/\text{OSR}$ to avoid the quantization noise. OSR is the over-sampling ratio. In some cases it is convenient if a band starting higher than 0 Hz can be selected. This is possible if a Bandpass Sigma Delta modulator is used. However, there is a constraint that can be seen in the simulations shown in figure 7 and figure 8. Figure 8 shows the output of the mixer in two situations. In the first situation, the whole down-sampled RF band is within the noise shape band of the Sigma Delta modulator (lower graph). In the other situation some of the spectral components lies outside the noise shape band of the Sigma Delta modulator. These components could represent neighbor channels or disturbers. In the case of no spectral component outside the noise shape band the double demodulation translates the RF signal to the baseband with high PSNR (lower graph in figure 7). The distance between the signal peak and the noise floor is 60 dB. In the case of spectral components.
outside the noise shape band, the distance is diminishing (upper graph). This is because the spectral components outside the noise shape band down converts the massive quantization noise to the baseband and thereby destroys the PSNR. The sampled RF signal is shown (with crosses in figure 7) together with the sign control signal to the switches. There are three RF spectral components within the noiseshape band (f=0.121f_c, 0.125f_c, 0.129f_c) and three outside (f=0.152f_c, 0.156f_c, 0.160f_c). The spectral components of the RF signal outside the noise shape band are 20 dB stronger to emphasize the destructive effect.

It is clearly important that the noise shape band covers the whole down-sampled RF band, in order to maintain a high PSNR.

5. Conclusion
A new modulation scheme that introduces two modulations in one mixer, here called the double modulation scheme, was presented. With minor change to existing subsampling-mixers and switching-mixers a second modulation is introduced, by modulating the sign of the analog RF signal in the mixer. Controlling the sign with a 1 bit Sigma Delta modulator, it was shown that an extra additional frequency translation was introduced. Equations describing the noise and the translation of the RF signal were given. Simulations verifying the principles were presented.

References