



The program FEMB users manual

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Title and author(s) The Program FEMB Users Manual by Ib Misfeldt	Date March 1977 Department or group Reactor Technology Group's own registration number(s)
<p style="text-align: center;">pages + tables + illustrations</p>	
Abstract <p style="text-align: center;">This report contains a short description of the two-dimensional diffusion theory finite element program FEMB.</p> <p style="text-align: center;">Input and output explanations are given together with two examples on the use.</p>	Copies to
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CONTENTS

	page
Short description	1
Application	2
Input specification	2
Quick reference input specification	5
Output description	6
Example I	8
References	9
Appendix A, input for example I	10
Appendix B, output from example I	11
Appendix C, card deck for example II	25
Appendix D, output for example II	26

-1-

SHORT DESCRIPTION

FEMB is a finite element program for approximate solution of the diffusion-theory-equation

$$(1) \quad + \nabla(D_g(\underline{r}) \nabla \theta_g(\underline{r})) + \Sigma_{r,g}(\underline{r}) \theta_g(\underline{r}) + \sum_{g' \neq g} \Sigma_{s,g \leftrightarrow g'}(\underline{r}) \theta_{g'}(\underline{r}) + \frac{1}{k_{eff}} \cdot \chi_g(\underline{r}) \sum_{g'} (\nu \Sigma_f)_{g'}(\underline{r}) \theta_{g'}(\underline{r}) = 0$$

within a domain Ω in the xy-plane with the boundary conditions

$$(2) \quad - D_g \frac{\partial \theta_g(\underline{r})}{\partial \underline{n}} = \sum_{g'} \gamma_{gg'}(\underline{r}) - \theta_g(\underline{r})$$

or

$$(3) \quad \frac{\partial \theta_g(\underline{r})}{\partial \underline{n}} = L_g(\underline{r})$$

Ω is divided in rectangular elements. Within each element the flux ($\theta_g(\underline{r})$) is approximated by a polynomial of order m.

For more details about the method and the approximation used see ref. 2-4.

The equations are solved for one group at a time using the ordinary power iteration technique. The equation for one group is solved by a pointwise successive overrelaxation technique. There is only one inner iteration for each outer.

The iterations are accelerated by extrapolation for removal of the dominating error-mode.

The iterations are stopped when the local error is less than a given input parameter (eps).

An approximate upper limit for the local error ($\epsilon_{1,max}$) is calculated in this way:

$$\epsilon_{1,max} \leq \frac{\max_i |\theta_i^k - \theta_i^{k-1}|}{\max_i \theta_i^k} \cdot \text{extpl}$$

where k gives the outer iteration number, i runs over all flux points in all groups and extpl is the maximal of the last three extra polation factors used for extrapolation.

APPLICATION

On the whole the program adheres to the input/output conventions of the Rise program TWODIM. It is therefore easy to use for users accustomed to this program.

The program gives very reliable results within reasonable calculation times, but it is not a fast program and should therefore mostly be used where high precision is needed.

The typical precision of a calculation with the program can be seen in ref. 1 and ref. 2.

INPUT SPECIFICATION

As mentioned before there is only little difference between FEMB and TWODIM in the input, therefore the same name for input variables with the same meaning is used.

First comes a complete list of the input parameters in the order in which they appear.

FF:
Problem nb: } administration input
day, month, year: }

CMX: number of coarse mesh in the x-direction.

CMY: number of coarse mesh in the y-direction.

NCP: number of compositions=number of ordinary materials + number of boundary conditions.

NB: number of boundary conditions.

NDB: number of diagonal boundary conditions; condition (3)

NG: number of groups.

NRR: number of reaction-rates, for each reaction-rate the program calculates for each element

$$\sum_{g'}^{(RR)} \int_{\text{element}} \phi_{g'}(\underline{r}) dr$$

KDS: if KDS=1 then the reaction-integrals from the last calculation are printed in condensed form as specified by meshx and meshy.

if KDS=2 then the reaction-integrals from all calculations are printed in the same condensed form, as specified by meshx and meshy.

if KDS=0 meshx and meshy are not read.

- NREC: the calculations are repeated NREC times, between each calculation the mesh is divided as specified by FACX and FACY.
- M: gives the order of the interpolation polynomial, for practical reasons M should be less than or equal to 6.
- MX: the maximal number of fine mesh in the x-direction.
- MY: the maximal number of fine mesh in the y-direction.
- XC: array (0: CMX), containing the coordinates of the coarse mesh division in the x-direction.
- YC: as XC.
- FMX: array (1: CMX), gives the number of fine mesh into which each coarse mesh is divided before the first calculation.
- FMY: as FMX.
- FACX: array (1: CMX) containing the number of fine mesh into which each mesh is divided before the next recalculation.
- FACY: as FACX.
- CMP: array (0: CMX + 1, 0: CMY + 1) containing lay-out of composition numbers. The numbers are read as if they form part of the first quadrant in the xy-plane. Each logical record corresponds to one mesh in the y-direction, the first and the last are boundary conditions.

Diffusion data for the NCP compositions:

K: composition number.

For $K \leq NB$ and $K \neq NDB$:

EXTPL: array (1:NG) current/flux ratios for the NG groups at the boundary characterized by the composition number K.

For $NDB < K \leq NB$

GAMMA: array (1:NG, 1:NG) corresponding to boundary condition (2); non-negative diagonal elements, non-positive off diagonal elements and

$$\sum_g \gamma_{gg} \geq 0 \text{ for all } g.$$

For $NB < K \leq NCP$:

Data for the ordinary material, characterized by the composition number K.

D: array (1:NG) diffusion coefficient for the groups.

SS: the modified scattering matrix

$$SS(g,g) = \Sigma_{r,g} = \Sigma_{abs,g} + \sum_{g' \neq g} \Sigma_{s,g' \leftarrow g}$$

$$SS(g,g') = \Sigma_{s,g \leftarrow g'}$$

FS: array (1:NG) normalised fission spectrum.

NFS: array (1:NG), $\sqrt{\Sigma_{fiss}}$.

RR: array (1:NRR, 1:NG) reaction rate cross section, each reaction rate is one logical record, if NRR=0 RR is not read.

MESHX: array (0:MX) the first and the last number in the array must always be 1. All the numbers correspond to a fine mesh interface, if the number is 0 the two adjacent mesh are condensed in the output from the reaction integral.

if KDS=2 MESHX is (0: $\sum_{i=1}^{CMX} FMX(i)$) and the numbers corresponds to the mesh after the first subdivision as specified by FMX

MESHY: as MESHX.

The last cards contain four control variables for each calculation, if -1 is given for the first calculation then default values are used, if -1 is given in the following cards then unchanged values are used for the corresponding variable.

MAXANTALITERATIONER: the maximal number of iterations, default is 50.

EPS: The iterations are stopped when the local error ($\xi_{1,max}$, calculated as described on page 1) is less than eps, default is 0.0001.

EPSMY: Extrapolation is performed when the relative change in the extrapolation factor for two consecutive iterations is less than EPSMY, default is 0.1.

OMEGA: overrelaxation factor, default is 1.2.

The input is now concluded with the administration input cards FF and -1 or a new problem.

Quick reference input specification

Each line in the following corresponds to one logical record and must start on a new card.

Repeated equally structured data is shown as [data] · N where N gives the number of repeats.

FF	}	administration-input
problem		
day, month, year		

cmx, cmy, ncp, nb, ndb, ng, nrr, kds, nrec, m
mx, my

xc(0), xc(1),, xc(cmx)

fmx(1), fmx(2),, fmx(cmx)

facx(1), facx(2),, facx(cmx)

yc(0), yc(1),, yc(cmy)

fmy(1), fmy(2),, fmy(cmy)

facy(1), facy(2),, facy(cmy)

cmp(0, cmy+1), cmp(1, cmy+1),, cmp(cmx+1, cmy+1)

cmp(0, cmy), cmp(1, cmy),, cmp(cmx+1, cmy)

.
. .
. .

cmp(0,0), cmp(1,0),, cmp(cmx+1, 0)

k]	· ndb; 1 ≤ k ≤ ndb
extpl(1), extpl(2), ..., extpl(ng)		

k]	· (no-ndb); ndb ≤ k ≤ nb
gamma(1,1), gamma(1,2), ..., gamma(ng,ng)		

k]	nb ≤ k ≤ ncp
d(1), d(2), ..., d(ng)		
ss(1,1), ss(1,2), ..., ss(1,ng), ..., ss(ng, ng)		
fs(1), fs(2), ..., fs(ng)		
nfs(1), nfs(2), ..., nfs(ng)		
rr(1,1), rr(1,2), ..., rr(1,ng)		
rr(2,1), rr(2,2), ..., rr(2,ng)		
.		
.		
rr(nrr,1), rr(nrr,2), ..., rr(nrr, ng)		
		· (ncp-nb)

$$\left. \begin{array}{l} \text{meshx}(0), \text{meshx}(1), \dots, \text{meshx}(\text{mx}) \\ \text{meshy}(0), \text{meshy}(1), \dots, \text{meshy}(\text{my}) \end{array} \right\} \text{ if kds} = 1$$

$$\left. \begin{array}{l} \text{meshx}(0), \text{meshx}(1), \dots, \text{meshx}\left(\sum_{i=1}^{\text{CMX}} \text{FMX}(i)\right) \\ \text{meshy}(0), \text{meshy}(1), \dots, \text{meshy}\left(\sum_{i=1}^{\text{CMX}} \text{FMY}(i)\right) \end{array} \right\} \text{ if kds} = 2$$

if kds = 0 no reading of meshx and meshy

[maxantaliterationer, eps, epsmy, omega] · (nrec+1); -1 ⇒ default
 FF
 -1 (or a new problem) } administration input

OUTPUT DESCRIPTION

Each logical page starts with the usual ADM. heading and can consist of several physical pages.

Page 1 is a listing of input in the order in which it is read, one logical record is read at a time and immediately written.

Page 2 starts with a listing of the parameters used for the following iteration (maxantaliterationer, eps, epsmy, omega). Then comes a listing of some control variables of minor interest for the ordinary user, they are:

OANTAL: number of compositions = NCP.

RTYPER: number of boundaries = NB.

GANTAL: number of groups.

EANTAL: number of elements = number of meshes with ordinary materials.

RANTAL: number of external boundaries.

ANTALUBK: number of unknowns per group.

MAXHUD: the amount of space used for the equations.

ANTALBLK: the number of blocks used for the equations on secondary storage. maxhud/900 gives the minimum number of blocks, if antalblk is much greater, contact the person responsible for the program.

The maximum allowed number of blocks is 600/ng, if more space is needed contact responsible engineer.

After these control variables comes the progress report for the iteration.

IT.NR: the number of this iteration

RESIDUE: $\frac{\max_i |\theta_i^k - \theta_i^{k-1}|}{\max_i \theta_i^k}$; k gives iteration number, i runs over all flux-points in all groups

RATIO: $\frac{\sum_i |\theta_i^{k-1} - \theta_i^{k-2}| / \max_i \theta_i^k}{\sum_i |\theta_i^{k-1} - \theta_i^{k-2}|} \bullet \text{sign}(\theta_j^k - \theta_j^{k-1}) \bullet \text{sign}(\theta_j^{k-1} - \theta_j^{k-2})_i$

$$|\theta_j^{k-1} - \theta_j^{k-2}| = \max_i |\theta_i^{k-1} - \theta_i^{k-2}|$$

LAMBDA: $1/k_{\text{eff}}$

KEFF: k_{eff}

DELTAKEFF: $(k_{\text{eff}}^k - k_{\text{eff}}^{k-1})$

TOTALKILDE: $\sum_e \sum_g \left(\int_e \theta_g (\nabla \Sigma_f)_g d\Omega \right)$

e runs over all elements

g runs over all groups

Every time an extrapolation is performed MY and eksfac is written

MY: =RATIO

EKSFAC: $1/(1-MY)$

Page 3 The result of the calculation, k_{eff} and fluxdistribution normalised so that $\theta_{\text{max}} = 9999$

Page 4 average flux for each group with the normalisation mentioned above, and a description of where the maximum occurs.

Page 5 if NRR $\neq 0$ page 5 contains a map for each reaction-rate, the normalisation is done so that the average is 1000 for each reaction integral.

Page 6 if NREC > 0 the following 4 pages contain the same as page 2-5.

EXAMPLE

As a simple example we take the reactor shown in fig. 1.

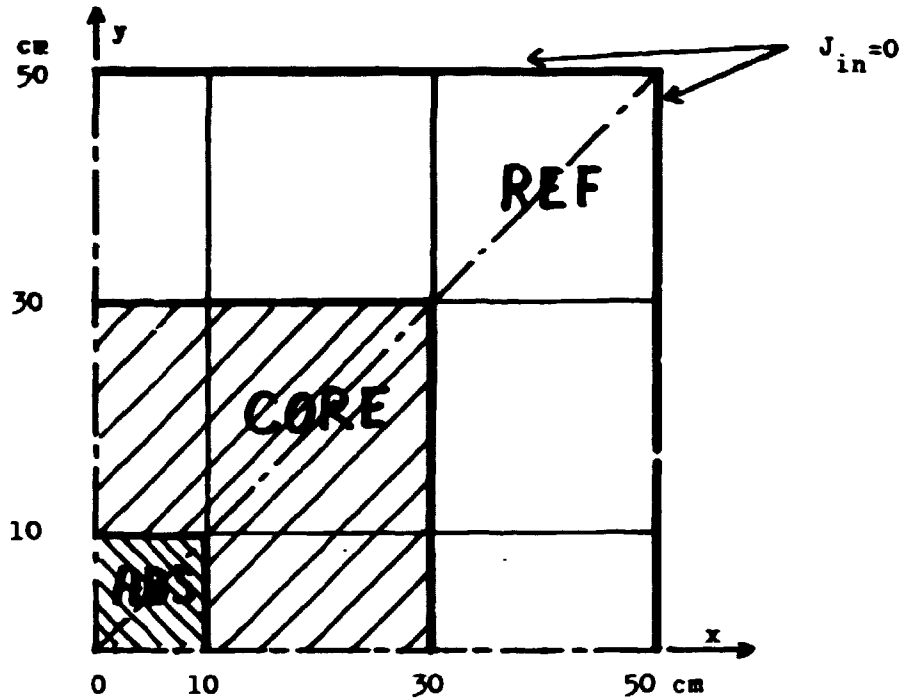


Fig. 1. Geometry specification.

For this reactor we perform a two-group calculation with the following coefficients.

Region	D_1	D_2	$\Sigma_{1 \rightarrow 2}$	Σ_{a1}	Σ_{a2}	$\nu \Sigma_{f2}$
3, CORE	1.5	0.4	0.02	0.01	0.085	0.135
4, ABS	1.5	0.4	0.02	0.01	0.13	0.135
5, REF	2.0	0.3	0.04	0	0.01	0

$$\chi_1 = 1.0, \chi_2 = 0, \nu \Sigma_{f1} = 0, \Sigma_{2 \rightarrow 1} = 0 \text{ all region}$$

A list of the complete run is shown as appendix A.

The output from this calculation is shown as appendix B.

REFERENCES

1. I. Misfeldt, Solution of the Multigroup Neutron Diffusion Equation by the Finite Element Method.
2. I. Misfeldt, Master thesis.
3. The application of the Finite Element Method to the multi-group neutron diffusion equation, Nuclear Science and Engineering 47. By L.A. Semanza et al.
4. The Finite Element Method in Engineering Science. By O.C. Zienkewicz.

APPENDIX A

A complete card deck for a calculation on the example shown page 8.

Output from this job is shown as appendix B.

```

?JOB FT/MISFT;CLASS=1;CHARGE=251402;USER=RTMISFELUT/WORK
?PROCSSTIME=300;INTIME=300;PRI.LIMIT=5000;
?BEGIN COMPILE FTMB ALGPL
?ALGPL FILE TAPL=IFRM
?DATA
$SET MERGE
?DATA INDDATA

```

FF	}	INPUT		
1				
17.3,1976				
3.3,5.2,2,2,1,1,1,2,			administration input	
6.6,			}	control variables
0.10,30,50				
1.1,1,			}	mesh specification
2.2,2,				
0.10,30,50,				
1.1,1,				
2.2,2,				
1.2,2,2,2,			}	composition numbers
1.5,5,5,2,				
1.3,3,5,2,				
1.4,3,5,2,				
1.1,1,1,1,				
1			}	boundary conditions
0,0,				
2,				
0.467,0.407,			}	ordinary materials
3				
1.5,0.4,				
0.03,0,0.02,0.05				
1.0,0,				
0.0,135,				
1,1,				
4,				
1.5,0.4,				
0.03,0,0.02,0.13,				
1.0,0,				
0.0,135,				
1,1,				
5,				
2.0,0.3,				
0.04,0,0.04,0.01,				
1.0,				
0.0,				
0.0,				
1.0,1.0,1,0,1,	}	condensation specifications		
1.0,1.0,1,0,1,				
-1,-1,-1,-1,	}	control variables for the iterations		
75,-1,-1,1,2,				
FF	}	administration input		
-1.				

?END JOB

APPENDIX B

Output from a calculation on the example shown page 8.

COMPILED: 21/04-1977. 22.25
21/04-1977. 22.26
PROCESSOR = 0 SEC
ELAPSE = 5 SEC
INPUT/OUTPUT = 0 SEC

A.E.K. PROGRAM NO. 10 PROBLEM NO. 1 17/3.1976
FLUXREKGNINGFR ELEMENTMETODEN

CMX CMY RLP NH NDU N6 NHH KDS NREC M
3. 3. 5. 2. 2. 2. 1. 1. 1. 2.
MX MY
6. 6.

XC
0. 1.000F+01 3.000E+01 5.000E+01

FHX
1. 1. 1.
FACX/
2. 2. 2.

YC
0. 1.000F+01 3.000E+01 5.000E+01

FHY
1. 1. 1.
FACY
2. 2. 2.

COMPOSITIONS NUMBERS
1. 2. 2. 2. 2.
1. 3. 3. 3. 3.
1. 4. 4. 4. 4.
1. 1. 1. 1. 1.

1
EXTPL: 0. 0.

page 7 cont.

2
EXTPL: 4.67600E-01 4.67600E-01

3
D: 1.50000E+00 4.00000E-01
SS: 3.00000E-02 0. 2.00000E-02 8.50000E-02
FS: 1.00000E+00 0.
NFS: 0. 1.35000E-01
HR : 1 1.00000E+00 1.00000E+00

4
D: 1.50000E+00 4.00000E-01
SS: 3.00000E-02 0. 2.00000E-02 1.30000E-01
FS: 1.00000E+00 0.
NFS: 0. 1.35000E-01
HR : 1 1.00000E+00 1.00000E+00

5
D: 2.00000E+00 3.00000E-01
SS: 4.00000E-02 0. 4.00000E-02 1.00000E-02
FS: 1.00000E+00 0.
NFS: 0. 0.
HR : 1 0. 0.

MESI X
1.000E+00 0. 1.000E+00 0. 1.000E+00 0. 1.000E+00

MESI Y
1.000E+00 0. 1.000E+00 0. 1.000E+00 0. 1.000E+00

MAXIMUM ITERATION: 50. EPS 1.0000E-04 EPSMV 1.0000E-01 OMEGA 1.2000E+00

21/04-1977. 22.26
PROCESSOR = 4 SEC
ELAPSED CPU = 21 SEC
INPUT/OUTPUT = 1 SEC

A.E.K. PROGRAM NO. 10 PROBLEM NO. 1 17/3.1976
FLUXRKLGNIGEP ELFBENTHTTOEN

MAXH 2916. HAYANTALITERATIONFP 50. EPS 1.0000E-04 EPSMY 1.0000E-01 OMEGA 1.2000E+00
DANTAL 5 RTYPER 2 GANTAL 2 EANTAL 9 DANTAL 12 ANTALUBK 49 MAXHUD 625 ANTALBLK 1

IT. NR	RESIDUE	RATIO	LAMBDA	KEFF	DELTAKEFF	TOTALKILDE
1	7.0391FF-01	0.56000000	4.56000000	0.21911111	0.80669999	0.80669999
2	9.0071FF-01	0.59341881	1.413387339	0.70747474	0.80669999	0.80669999
3	5.3526FF-01	0.60887844	1.227092298	0.78678888	0.80669999	0.80669999
4	3.4410FF-01	0.65628040	1.247884523	0.80138144	0.80669999	0.80669999
MY: -0.656280	FRSFA	0.65628040	1.247884523	0.80138144	0.80669999	0.80669999
5	6.5049FF-02	0.66001244	1.231633916	0.81119261	0.80669999	0.80669999
6	6.0200FF-02	0.66684798	1.120698252	0.82851241	0.80669999	0.80669999
7	4.4897FF-02	0.76583404	1.168118730	0.84161813	0.80669999	0.80669999
8	3.3365FF-02	0.77477400	1.182447903	0.84547310	0.80669999	0.80669999
9	3.1255FF-02	0.84411871	1.170900095	0.85404332	0.80669999	0.80669999
10	2.2295FF-02	0.81018541	1.169887375	0.85404332	0.80669999	0.80669999
11	2.0033FF-02	0.85704474	1.16329243	0.85947990	0.80669999	0.80669999
12	1.5890FF-02	0.80714359	1.16339254	0.86020945	0.80669999	0.80669999
13	1.5840FF-02	0.85712703	1.158601164	0.86336099	0.80669999	0.80669999
14	1.1042FF-02	0.84482420	1.15546132	0.86545520	0.80669999	0.80669999
15	1.0138FF-02	0.82043426	1.15487357	0.86545520	0.80669999	0.80669999
16	0.4559FF-02	0.84594760	1.15487357	0.86545520	0.80669999	0.80669999
17	0.4751FF-02	0.82708436	1.15392799	0.86733556	0.80669999	0.80669999
18	0.1638FF-02	0.84347360	1.15194955	0.86833556	0.80669999	0.80669999
19	0.1638FF-02	0.83005635	1.15194955	0.86833556	0.80669999	0.80669999
20	0.1638FF-02	0.84096425	1.151068760	0.86833556	0.80669999	0.80669999
21	3.2843FF-03	0.62888883	1.151068760	0.86833556	0.80669999	0.80669999
MY: 0.840480	FRSFA	0.62888883	1.151068760	0.86833556	0.80669999	0.80669999
22	3.0025FF-03	0.79656068	1.14947118	0.86996527	0.80669999	0.80669999
23	3.0025FF-03	0.79656068	1.14854962	0.87218205	0.80669999	0.80669999
24	1.2522FF-03	0.79709292	1.14882443	0.87045124	0.80669999	0.80669999
25	1.5279FF-03	0.62795846	1.14836318	0.87080465	0.80669999	0.80669999
MY: -0.627958	FRSFA	0.62795846	1.14836318	0.87080465	0.80669999	0.80669999
26	3.0843FF-04	0.39071867	1.14869800	0.87039929	0.80669999	0.80669999
27	3.0843FF-04	0.57651044	1.149017872	0.870226240	0.80669999	0.80669999
28	1.1043FF-04	0.64111460	1.14911565	0.870226240	0.80669999	0.80669999
29	1.1043FF-04	0.80962135	1.14912448	0.870226240	0.80669999	0.80669999
30	1.1043FF-04	0.70858433	1.14914324	0.870226240	0.80669999	0.80669999
31	0.2336FF-05	0.82882490	1.14916052	0.870200045	0.80669999	0.80669999
32	7.6159FF-05	0.81161009	1.14916714	0.87019544	0.80669999	0.80669999

	33	6.3541E-05	0.82420313	1.14918109	0.87018487	-1.0562E-05	1.0573E+02
NY:	0.824203	EKS FAC : 5.688383					
	34	1.1934E-04	-1.31517513	1.14920864	0.87016401	-2.0864E-05	1.0572E+02
	35	9.3564E-05	-0.64759470	1.14927801	0.87011149	-5.2218E-05	1.0572E+02
	36	5.1352E-05	-0.67054333	1.14922709	0.87015004	3.8549E-05	1.0572E+02
	37	4.7437E-05	-0.70182664	1.14924036	0.87013999	-1.0048E-05	1.0572E+02
NY:	-0.701827	EKS FAC : 0.587604					
	38	6.8107E-06	0.35387849	1.14922867	0.87014885	8.8558E-06	1.0572E+02
	39	3.8510E-06	-0.56958953	1.14922397	0.87015240	3.5542E-06	1.0572E+02
	40	3.5677E-06	0.49979640	1.14922481	0.87015177	-6.3374E-07	1.0572E+02

page 2 cont.

-3-

21/04-1977.	22.28	
PROCESSOR	=	28 SEC
ELAPSEU	=	126 SEC
INPUT/OUTPUT	=	8 SEC

A.E.K. PROGRAM NO. 10 PROBLEM NO. 1 17/3.1976
 FLUXBREGNINGER ELEMENTMETODEN

ITERATIONEN ER AFSLUTTET
 DER ER UDFØRT 40 ITERATIONER
 EPSILON VAR 0.000100000000 DET MAKSIMALE ANTAL ITERATIONER 50
 DEN TOTALE FISSIONSKILDE ER 2.7853E+05

KEFF 0.8701517680
 FLUKSLN BLEV

FLUX I GRUPPE 1

5000.:	309.	307.	285.	246.	141.	41.	23.
4000.:	1348.	1329.	1278.	1022.	616.	245.	41.
3000.:	5980.	5006.	5650.	4728.	2572.	616.	141.
2000.:	9999.	9044.	9625.	8489.	4728.	1022.	246.
1000.:	9469.	9595.	9002.	9626.	5650.	1278.	285.
500.:	8926.	9134.	9595.	9945.	5906.	1329.	307.
0.:	8688.	8926.	9469.	9999.	5980.	1348.	309.

0. 500.1000.2000.3000.4000.5000.

FLUX I GRUPPE 2

5000.:	178.	169.	172.	122.	104.	83.	-11.
4000.:	5337.	5268.	5032.	4117.	2626.	1166.	83.
3000.:	3805.	3754.	3745.	2950.	3050.	2626.	104.
2000.:	2178.	2164.	2304.	1672.	2950.	4117.	122.
1000.:	2157.	2153.	2029.	2304.	3745.	5032.	172.
500.:	1482.	1443.	2153.	2164.	3754.	5268.	169.
0.:	1494.	1482.	2157.	2178.	3805.	5337.	178.

0. 500.1000.2000.3000.4000.5000.

-4-

21/04-1977. 22.28
PROCESSOR = 200
ELAPSED = 128
INPUT/OUTPUT = 8

A.F.K. PROGRAM NO. 10 PROBLEM NO. 1 17/3.1976
FLUXBEREGNINGER ELEMENTMETODEN

I GRUPPE 1 ER DEN MAKSIMALE MIDDELFLUX: 9215
FLUXEN FOREKOM I BAADET X FRA 0. TIL 10. OG Y FRA 0. TIL 10.
I GRUPPE 2 ER DEN MAKSIMALE MIDDELFLUX: 4149
FLUXEN FOREKOM I BAADET X FRA 30. TIL 50. OG Y FRA 0. TIL 10.

MIDDELFLUX I GRUPPE 1

```
5000. +-----+-----+-----+
      : 1912 : 1458 : 335 :
3000. +-----+-----+-----+
      : 9181 : 7620 : 1458 :
1000. +-----+-----+-----+
      : 9215 : 9181 : 1912 :
      0. +-----+-----+-----+
          0. 1000. 3000. 5000.
```

MIDDELFLUX I GRUPPE 2

```
5000. +-----+-----+-----+
      : 4149 : 3219 : 1211 :
3000. +-----+-----+-----+
      : 2459 : 2278 : 3219 :
1000. +-----+-----+-----+
      : 1683 : 2459 : 4149 :
      0. +-----+-----+-----+
```

0. 1000. 3000. 5000.
DEN INTEGRERTE FLUX FOR HELE REAKTOREN OG ALLE GRUPPER ER: 10489068

-5-

21/04-1977.	22.28	
PROCESSOR =	28	SEC
ELAPSED =	150	SEC
INPUT/OUTPUT =	8	SEC

A.E.K. PROGRAM NO. 10 PROBLEM NO. 1 17/3.1976
 FLUXBÆLLEGNINGEN EFFICIENTMETODEN

REAKTIONSDINTEGRALER:

REAKTIONSDINTEGRALERNE ER NØRMERET SÅ GENNEMSNITTET FOR DEN DEL AF REAKTUREN
 HVOR REAKTIONSDINTEGRALET OVERSTIGER $\rho = 10 \cdot \max(\text{REAKTIONSDINTEGRAL})$ ER 1000.

REAKTIONSDINTEGRAL OVER ALLE GRUPPER, ELEMENTVIS.
 REAKTIONSDINTEGRAL NR. 1

5000.	-+-----+-----+-----+
	: 0 : 0 : 0 :
3000.	-+-----+-----+-----+
	: 1079 : 918 : 0 :
1000.	-+-----+-----+-----+
	: 1011 : 1079 : 0 :
0.	-+-----+-----+-----+
	0. 1000. 3000. 5000.

21/04-1977. 22.29
PROCESSOR = 37
ELAPSED = 216
INPUT/OUTPUT = 9
SSECC
SSECC

A.E.K. PROGRAM NO. 10 PROBLEM NO. 1 17/3.1976
FLUXPLNREG INDEX LIFILETNETCOEF

MAXI 2016. MAXIALITERATION 75. EPS 1.0000E-04 EPSII 1.0000E-01 OMEGA 1.5000E+00

DENTAL 5 RYPER 2 DANTAL 2 FANTAL 36 PANTAL 24 ANTALBLK 169 MAXMUD 2401 AI-TALBLK 3

II. BK	RESIDUE	PATIN	LAMBDA	KEFF	DELTAKEFF	TOTALKILDE
1	0.0773F-01	0.00000000	1.36133043	0.72393974	-1.4621E-01	2.5232E+05
2	1.0567F-01	0.064396430	1.226654931	0.81522560	-9.1286E-02	2.8414E+05
3	1.1781F-01	0.70278459	1.25069651	0.81254801	-2.6776E-03	2.8321E+05
4	1.0026F-01	0.79732117	1.19641453	0.83583071	-2.3283E-02	2.9132E+05
MY: -0.797321	F-SFAC	0.556384				
5	0.0661F-02	0.30188920	1.19563758	0.83637305	5.4314E-04	2.9151E+05
6	0.1495F-02	0.81121559	1.19457796	0.83711573	7.4188E-04	2.9177E+05
7	0.1252F-02	0.75238613	1.16364269	0.84470668	7.5910E-03	2.9441E+05
8	1.5633F-02	0.71535874	1.17925457	0.84799332	3.2866E-03	2.9556E+05
MY: -0.715358	F-SFAC	0.582968				
9	1.3329F-02	0.65813933	1.17651696	0.84996650	1.9732E-03	2.9625E+05
10	0.0042F-03	0.70072102	1.17370787	0.85193544	1.8689E-03	2.9649E+05
11	0.2867F-03	0.82222133A	1.17121171	0.85381660	1.8612E-03	2.9759E+05
12	0.7486F-03	0.83185466	1.16908895	0.85536691	1.5503E-03	2.9813E+05
13	0.7200F-03	0.80864242	1.16753472	0.85659558	1.1387E-03	2.9859E+05
14	0.9362F-03	0.80323731	1.16648654	0.85727521	7.6963E-04	2.9880E+05
15	0.2581F-03	0.87483385	1.16548033	0.85801534	7.4013E-04	2.9905E+05
16	0.7006F-03	0.88176674	1.16482475	0.85849624	4.8290E-04	2.9922E+05
17	0.1723F-03	0.87336948	1.16421331	0.85894912	4.5088E-04	2.9938E+05
MY: 0.873369	F-SFAC	0.780600				
18	0.2588F-03	0.95960791	1.16040082	0.86177120	2.8221E-03	3.0036E+05
19	0.2584F-03	0.71003127	1.15914438	0.86270530	9.3410E-04	3.0069E+05
20	1.2117F-03	0.90349451	1.15987506	0.86216181	-5.4349E-04	3.0050E+05
21	7.6809F-04	0.71362254	1.16625475	0.86187969	-2.8212E-04	3.0040E+05
MY: -0.713622	F-SFAC	0.583457				
22	0.2830F-04	0.85583254	1.160042542	0.86175242	-1.2676E-04	3.0036E+05
23	0.1420F-04	0.90505871	1.16057982	0.86163828	-1.1465E-04	3.0032E+05
24	0.1703F-04	0.90105551	1.160075620	0.861519697	-1.1031E-04	3.0027E+05
25	0.1708F-04	0.901047451	1.160084682	0.86144010	-7.9869E-05	3.0025E+05
26	0.1703F-04	0.90105551	1.160092799	0.86137087	-6.0250E-05	3.0023E+05
27	0.1708F-04	0.81919666	1.16097791	0.86134283	-3.7042E-05	3.0021E+05
28	0.1703F-04	0.90105551	1.16101110	0.86131302	-2.9010E-05	3.0020E+05
29	0.1703F-04	0.90105551	1.16104190	0.86129556	-1.7863E-05	3.0020E+05
30	0.1703F-04	0.90105551	1.16106448	0.86127081	-1.6745E-05	3.0019E+05
31	0.1703F-04	0.90105551	1.16108017	0.86126697	-1.1645E-05	3.0019E+05

MY:	0.8612977	32	5.6370E-05	0.86297160	1.16109064	0.86125920	-7.7660E-06	3.0018E+05
				FNSI AC :	7.298023			
		33	4.0971E-05	0.53009140	1.16116711	0.86120246	-5.6717E-05	3.0016E+05
		34	3.7089E-05	-0.73125440	1.16118101	0.86119217	-1.0310E-05	3.0016E+05
		35	3.2021E-05	-0.80644860	1.16116655	0.86120290	1.0729E-05	3.0016E+05
MY:	-0.629627	36	1.4191E-05	-0.62962657	1.16116301	0.86120552	2.6207E-05	3.0017E+05
				FNSI AC :	0.613638			
		37	1.0158E-05	0.50530331	1.16116014	0.86120766	2.1327E-06	3.0017E+05
		38	7.2458E-06	0.72444582	1.16115737	0.86120970	2.0490E-06	3.0017E+05
		39	3.6782E-06	0.74054001	1.16115552	0.86121108	1.3764E-06	3.0017E+05

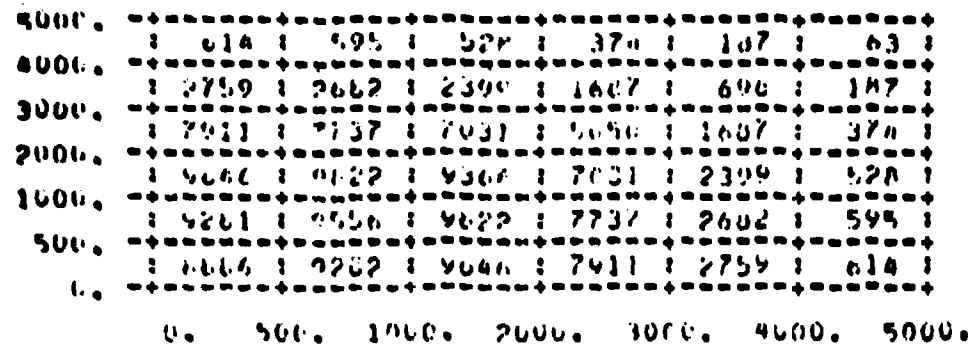
page 6 cont.

21/04=1977. 22.32
PROCESSOR = 107 SEC
ELAPSED = 387 SEC
INPUT/OUTPUT = 26 SEC

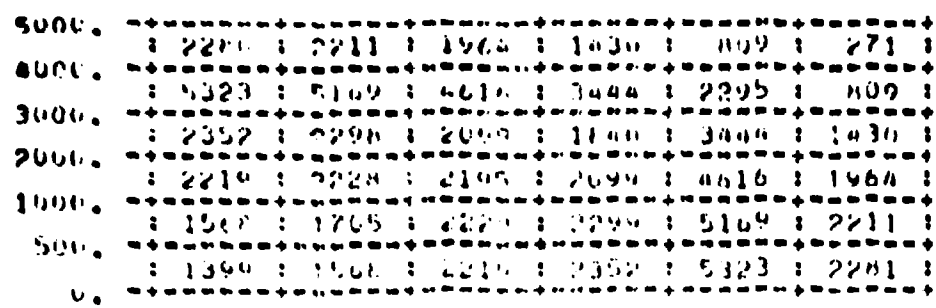
A.L.P. PROGRAM NO. 10 REPT. NO. 1 17/3.1976
FLUXMELIGRIGP LLPIENTAFUDD

I GRUPPE: 1 EF DEN MAKSIMALE MIDDELFLUX: 9846
FLUXF. FORLØB I UAALET x FRA 10. TIL 20. OG Y FRA 0. TIL 5.
I GRUPPE: 2 EF DEN MAKSIMALE MIDDELFLUX: 5323
FLUXF. FORLØB I UAALET x FRA 30. TIL 40. OG Y FRA 0. TIL 5.

MIDDELFLUX I GRUPPE 1



MIDDELFLUX I GRUPPE 2



0. 500. 1000. 2000. 3000. 4000. 5000.
DEN INTEGREERTE FLUX FOR HELE REAKTOREN OG ALLE GRUPPER ER: 15177199

page 8 cont.

-9-

21/04-1977.	22.32	
PROCESSOR =	108	SEC
ELAPSED =	388	SEC
INPUT/OUTPUT =	26	SEC

A.E.K. PROGRAM NO. 10 PROBLEM NO. 1 17/3.1976
 FLUXREGULERINGER EFFICIENTMETODEN

REAKTIONSDINTEGRALER:

REAKTIONSDINTEGRALERNE ER NORMALISERT SAA GLENNEMSNITTET FOR DEN DEL AF REAKTUREN
 HVOR REAKTIONSDINTEGRALLET OVERSTIGER $10 \cdot \max(\text{REAKTIONSDINTEGRAL})$ ER 1000.

REAKTIONSDINTEGRAL OVER ALLE GRUPPER, ELEMENTVIS,
 REAKTIONSDINTEGRAL NR. 1

5000.	-+-----+-----+-----+-----+
	0 0 0
3000.	-+-----+-----+-----+-----+
	1067 198 0
1000.	-+-----+-----+-----+-----+
	1058 1067 0
0.	-+-----+-----+-----+-----+
	0. 1000. 3000. 5000.

TIME USED FOR THIS PROBLEM
 PROCESSOR = 108 SEC
 ELAPSED = 389 SEC
 INPUT/OUTPUT = 26 SEC

APPENDIX C

Example II

A complete card deck for a calculation with boundary condition (2), gamma matrix.

Output corresponding to this run is shown in appendix D.

```
?JOB RT/MISFT;CLASS=1;CHARGE=251002;USER=RTMISFELDT/WURK
?PROCESSTIME=300; IUTIME=300; PRINTLIMIT=5000;
?BEGIN COMPIL FEM8 ALGOL
?ALGO1 FILE TAPE=1END
?DATA
$SET HLHGL
?DATA INDATA
FF
2
22,3,1977,
2,2,4,2,1,2,1,0,0,1,
8,R,
0,7,R,
7,1,
2,2,
0,7,R,
7,1,
2,2,
1,2,2,2,
1,3,3,2,
1,4,3,2,
1,1,1,1,
1,
0,0,
2,
0,2,0,-0.1,0.05,
3,
2,0,3,
0,03,0,0.03,0.01,
1,0,
0,0,
0,0,
4,
1,0,4,
0,02,0,0.01,0.01,
1,0,
0,0,05,
0,0,02,
75,-1,-1,1.5,
FF
-1,
?END JOB
```

APPENDIX D

Output for example II corresponding to the card deck shown in appendix C.

-1-

A.E.K. PROGRAM NO. 10 PROBLEM NO. 2 22/3.1977
FLUXION LOGIC FOR ELEMENTS TO DEN

CHY 2. ULY 2. FLP 4. LH 2. NLD 1. NO 2. DFP 1. KDS 0. I-REC 0. M 1.

1. 1. BY 6.

YC
0. 7.000E+00 0.000E+00

FBY
7. 1.

FAC 7
2. 2.

YC
0. 7.000E+00 0.000E+00

FBY
7. 1.

FAC 7
2. 2.

COMPOSITIONS TO DEEPS

1. 2. 2. 2.
1. 3. 3. 2.
1. 4. 3. 2.
1. 5. 1. 1.

1
FATHER 0. 0.

2
GAMMA: 2.00000E-01 0. -1.00000E-01 5.00000E-02

3
DE: 2.00000E+00 3.00000E-01
SS: 3.00000E-02 0. 3.00000E-02 1.00000E-02
FS: 1.00000E+00 0.
NFS: 0. 0.
NR 11 0. 0.

4
DE: 1.00000E+00 4.00000E-01
SS: 2.00000E-02 0. 1.00000E-02 1.00000E-02
FS: 1.00000E+00 0.
NFS: 0. 5.00000E-02
NR 11 0. 2.00000E-02

MAXIMUM LITERATURE: LPS EPSHY OMLGA
75. 1.00000E+00 1.00000E-01 1.50000E+00

page 1 cont.

NY:	0.941807	33	0.99023467	1.06271865	0.923360048	1.74221
		34	0.97924169	1.06249824	0.923360048	1.660004
		35	0.96924169	1.06249824	0.923360048	1.660004
		36	0.95924169	1.06249824	0.923360048	1.660004
		37	0.94924169	1.06249824	0.923360048	1.660004
		38	0.93924169	1.06249824	0.923360048	1.660004
		39	0.92924169	1.06249824	0.923360048	1.660004
		40	0.91924169	1.06249824	0.923360048	1.660004
		41	0.90924169	1.06249824	0.923360048	1.660004
		42	0.89924169	1.06249824	0.923360048	1.660004
		43	0.88924169	1.06249824	0.923360048	1.660004
		44	0.87924169	1.06249824	0.923360048	1.660004
		45	0.86924169	1.06249824	0.923360048	1.660004
		46	0.85924169	1.06249824	0.923360048	1.660004
		47	0.84924169	1.06249824	0.923360048	1.660004
		48	0.83924169	1.06249824	0.923360048	1.660004
		49	0.82924169	1.06249824	0.923360048	1.660004
		50	0.81924169	1.06249824	0.923360048	1.660004
		51	0.80924169	1.06249824	0.923360048	1.660004
		52	0.79924169	1.06249824	0.923360048	1.660004
		53	0.78924169	1.06249824	0.923360048	1.660004
		54	0.77924169	1.06249824	0.923360048	1.660004
		55	0.76924169	1.06249824	0.923360048	1.660004
		56	0.75924169	1.06249824	0.923360048	1.660004
		57	0.74924169	1.06249824	0.923360048	1.660004
		58	0.73924169	1.06249824	0.923360048	1.660004
		59	0.72924169	1.06249824	0.923360048	1.660004
		60	0.71924169	1.06249824	0.923360048	1.660004
		61	0.70924169	1.06249824	0.923360048	1.660004
		62	0.69924169	1.06249824	0.923360048	1.660004
		63	0.68924169	1.06249824	0.923360048	1.660004
		64	0.67924169	1.06249824	0.923360048	1.660004
		65	0.66924169	1.06249824	0.923360048	1.660004
		66	0.65924169	1.06249824	0.923360048	1.660004
		67	0.64924169	1.06249824	0.923360048	1.660004
		68	0.63924169	1.06249824	0.923360048	1.660004
		69	0.62924169	1.06249824	0.923360048	1.660004
		70	0.61924169	1.06249824	0.923360048	1.660004
		71	0.60924169	1.06249824	0.923360048	1.660004
NY:	0.940586	61	0.74114431	1.07309162	0.92756495	2.51688
		62	0.73114431	1.07311017	0.92755632	2.51688
		63	0.72114431	1.07312872	0.92754769	2.51688
		64	0.71114431	1.07314727	0.92753906	2.51688
		65	0.70114431	1.07316582	0.92753043	2.51688
		66	0.69114431	1.07318437	0.92752180	2.51688
		67	0.68114431	1.07320292	0.92751317	2.51688
		68	0.67114431	1.07322147	0.92750454	2.51688
		69	0.66114431	1.07324002	0.92749591	2.51688
		70	0.65114431	1.07325857	0.92748728	2.51688
		71	0.64114431	1.07327712	0.92747865	2.51688

page 2 cont.

21/04-1977.	22.36	
PROCESSOR =	96	SEC
ELAPSEU =	195	SEC
INFUT/OUTPUT =	13	SEC

A.E.K. PROGRAM NO. 10 PROBLEM NO. 2 22/3.1977
 FLUAREG: IBER7 ELEMENTFIBLEN

ITERATIONEN ER AFSLUTTET
 DER ER UDERT 71 ITERATIONER
 EPSILO. VAR 0.000100000000 DLT MAKSIMALE ANTAL ITERATIONER 75
 DER TALE FISSINGSKILDE ER 2.7194E+04

KEFF 0.9275424503
 FLUKS. BLEV

FLUX 1 GRUPPE 1

8000.:	5234.5197.5085.4899.4640.4314.3942.3572.3224.
7000.:	5837.5796.5672.5466.5177.4809.4373.3917.3572.
6000.:	7061.7012.6864.6614.6254.5787.5184.4373.3942.
5000.:	6924.7079.7000.7011.7094.6531.5789.4809.4314.
4000.:	6770.6700.6519.6116.7724.7094.6259.5177.4641.
3000.:	9322.9259.9051.8703.8196.7511.6815.5466.4899.
2000.:	9704.9632.9417.9051.8519.7800.6864.5472.5086.
1000.:	9924.9853.9632.9255.8704.7870.7012.5796.5197.
0.:	9999.9826.9703.9322.8770.8027.7062.5837.5235.

0.1000.2000.3000.4000.5000.6000.7000.8000.

FLUX 1 GRUPPE 2

8000.:	9529.9496.9495.9145.9144.8919.8672.8417.8145.
7000.:	9399.9371.9391.9192.9052.8896.8741.8500.8417.
6000.:	9214.9196.9145.9052.8964.8861.8776.8741.8572.
5000.:	9127.9115.9075.9015.8944.8882.8861.8896.8918.
4000.:	9097.9086.9057.9015.8973.8943.8953.9052.9149.
3000.:	9097.9086.9067.9037.9015.9015.9062.9142.9346.
2000.:	9111.9100.9087.9057.9057.9073.9183.9301.9495.
1000.:	9124.9116.9104.9089.9088.9113.9196.9371.9558.
0.:	9124.9123.9111.9097.9097.9127.9215.9345.9620.

0.1000.2000.3000.4000.5000.6000.7000.8000.

21/04-1977.	22.36	
PROCESSOR	=	96
ELAPSEU	=	195
INPUT/OUTPUT	=	13
		SEC
		SEC

A.E.W. PROGRAM NO. 10 PROBLEM NO. 2 22/3.1977
 FLUXBERECHNUNG LIFERENTMETHODE

I GRUPE: 1 ER DEN MAXIMALE MITTELFLEX: 9926
 FLUXEN FOLGEN I ORADEN X FRA 0. TIL 1. OG Y FRA 0. TIL 1.
 I GRUPE: 2 ER DEN MAXIMALE MITTELFLEX: 9494
 FLUXEN FOLGEN I ORADEN X FRA 7. TIL 8. OG Y FRA 0. TIL 1.

MITTELFLEX I GRUPE 1

8000.	5516	5638	5241	5946	4735	4360	3951	3572
7000.	6427	6336	6154	5879	5508	5040	4463	3751
6000.	7518	7412	7197	6869	6418	5824	5040	4360
5000.	8369	8249	8001	7632	7112	6418	5500	4735
4000.	9014	8863	8617	806	7632	6869	5879	5046
3000.	9478	9339	9055	8617	8007	7197	6154	5281
2000.	9778	9633	9339	8883	8249	7412	6336	5438
1000.	9926	9776	9478	9014	8369	7518	6427	5516
0.								

0. 1000. 2000. 3000. 4000. 5000. 6000. 7000. 8000.

MITTELFLEX I GRUPE 2

8000.	9494	9439	9333	9184	9003	8807	8508	8395
7000.	9298	9253	9175	9067	8943	8818	8715	8606
6000.	9163	9131	9073	8997	8915	8847	8819	8807
5000.	9106	9062	9046	8988	8939	8915	8943	9003
4000.	9092	9075	9085	9011	8988	8997	9067	9184

3000.	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+
	:	9100	:	9067	:	9065	:	9045	:	9040	:	9073	:	9175	:	9333	:						
2000.	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+
	:	9114	:	9103	:	9087	:	9075	:	9082	:	9132	:	9253	:	9439	:						
1000.	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+
	:	9123	:	9114	:	9100	:	9092	:	9106	:	9163	:	9294	:	9494	:						
0.	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+

0. 1000. 2000. 3000. 4000. 5000. 6000. 7000. 8000.
 DEN TILSGEÆRTEDE FLUX FOR HELE REAKTOREN OG ALLE GRUPPER ER: 1022746

page 4 cont.

21/04-1977. 22.36
 PROCESSOR = 97
 ELAPSED = 196
 INPUT/OUTPUT = 13

A.E.K. PROGRAM NO. 10 REACTION NO. 2 22/3.1977
 FLUXREGLINGEN I REAKTORSTYRELEN

REAKTORSTYREPALETTEN

REAKTIONSINTEGRALER ER NORMALISERT SÅA GEMMENSITTET FOR DEN DEL AF REAKTOREN
 HVOR REAKTIONSINTEGRALET OVERSTIGER $\rho=10$ MAX(REAKTIONSINTEGRAL) ER 1000.

REAKTIONSINTEGRAL OVER ALLE GRUPPER, ELEMENTVIS.
 REAKTIONSIVAKSERIEN NO. 1

8000.	0	0	0	0	0	0	0	0	0
7000.	1026	1001	1013	1001	937	973	962	0	0
6000.	1011	1008	1002	993	934	977	973	0	0
5000.	1005	1002	997	992	987	984	987	0	0
4000.	1000	1002	998	995	992	993	1001	0	0
3000.	1005	1003	1001	998	996	1002	1013	0	0
2000.	1006	1005	1003	1002	1002	1004	1021	0	0
1000.	1007	1006	1005	1004	1005	1011	1026	0	0
0.									

0. 1000. 2000. 3000. 4000. 5000. 6000. 7000. 8000.

TIME USED FOR THIS PROBLEM
 PROCESSOR = 97 SEC
 ELAPSED = 196 SEC
 INPUT/OUTPUT = 13 SEC