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Evaluation of a density functional with account of van der Waals forces using experimental data of H₂ physisorption on Cu(111)

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Detailed experimental data for physisorption potential-energy curves of H₂ on low-indexed faces of Cu challenge theory. Recently, density-functional theory has been developed to also account for nonlocal correlation effects, including van der Waals forces. We show that one functional, denoted vdW-DF2, gives a potential-energy curve promisingly close to the experiment-derived physisorption-energy curve. The comparison also gives indications for further improvements of the functionals.

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Density-functional theory (DFT) gives, in principle, exact descriptions of the stability and structure of electron systems, but, in practice, approximations have to be made to describe electron exchange and correlation (XC).^{1,2} Approximate XC functionals are commonly evaluated by comparing them with results from other accurate theories or with one or two relevant experimental numbers. This Brief Report illustrates the advantages of a third approach based on extensive experimental data; in this case, a full physisorption potential derived from surface-physics measurements. Conclusions about functional development and physisorption are drawn.

In the physisorption regime, resonant elastic-backscattering-diffraction experiments provide detailed quantitative knowledge. Here, data obtained for H₂ and D₂ on Cu surfaces³⁻⁵ are used as a demanding benchmark for the performance of adsorbate potential-energy curves (PECs) calculated with a nonempirical theory for extended systems. Density functionals that aspire to account for nonlocal electron-correlation effects, including van der Waals (vdW) forces, can then be assessed. Calculations with versions of the vdW-DF method⁶⁻⁹ are here shown to provide a promising description of the physisorption potential for H₂ on the Cu(111) surface, in particular the most recent one, vdW-DF2.⁹

Sparse matter is abundant. Dense matter, also abundant, has long been successfully described by DFT. The recent extensions of DFT functionals to regions of low electron density, where the ubiquitous vdW forces are particularly relevant, render DFT useful also for sparse matter. The vdW-DF functional expresses the vdW interactions and correlations in the density, $n(\mathbf{r})$, as a truly nonlocal six-dimensional integral.⁶⁻⁹ Its key ingredients are (i) its origin in the exact adiabatic connection formula,¹⁰⁻¹² (ii) an approximate coupling-constant integration, (iii) the use of an approximate dielectric function in a single-pole form, (iv) which is fully nonlocal and satisfies known limits, sum rules, and invariances, and (v) in which pole strength is determined by a sum rule and pole position is scaled to give the approximate gradient-corrected, electron-gas, ground-state energy locally. There are no empirical or fitted parameters, just references to general theoretical criteria.

Like composite molecules, adsorption systems have electrons in separate moleculelike regions, with exponentially decaying tails in between. Then the weakly inhomogeneous electron gas, used in the original vdW-DF method,^{6-8,13} might not be the most appropriate reference system for the gradient correction.¹⁴ Although promising results have been obtained for a variety of systems, including adsorption,^{15,16} there is room for improvement. The recent vdW-DF2 functional uses the gradient coefficient of the B88 exchange functional¹⁷ to determine the internal functional [Eq. (12) of Ref. 6] within the nonlocal correlation functional. This is based on application of the large- N asymptote^{18,19} on appropriate molecular systems. Using this method, Elliott and Burke²⁰ have shown from first principles that the correct exchange gradient coefficient β for an isolated atom (monomer) is essentially identical to the B88 value, which had been previously determined empirically.¹⁷ Thus, in the internal functional, vdW-DF2 (Ref. 9) replaces Z_{ab} in that equation with the value implied by the β of B88. This procedure defines the relationship between the kernels of vdW-DF and vdW-DF2 for the nonlocal correlation energy, both being transferable functionals based on physical principles and approximations and without empirical input.

The vdW-DF method also needs to choose an overall exchange functional to account for the exchange part of the interaction energy between, e.g., two monomers. The revPBE²¹ exchange functional in the original vdW-DF is good at separations in typical vdW complexes.⁶⁻⁸ The latter choice can be improved upon.²²⁻²⁶ Recent studies suggest that the PW86 exchange functional²⁷ most closely approximates Hartree-Fock interaction energies, both for atoms²³ and molecules.²⁴ The vdW-DF2 functional⁹ employs the PW86R functional,²⁴ which at lower densities makes the PW86 integral form get even closer to true exchange than the original.

Evaluation of XC functionals with respect to other theoretical results is often done systematically, e.g., by benchmarking with the S22 data set.²⁸⁻³² This set contains the results from 22 prototypical small molecular duplexes for noncovalent interactions (hydrogen-bonded, dispersion-dominated, and mixed) in molecules and provides PECs at a very accurate level of wave-function methods, in particular the coupled-cluster

method with single, double, and perturbative triple excitations [CCSD(T)] method.^{28–32} However, by necessity, the electron systems in such sets have finite sizes. The original vdW-DF performs well on the S22 data set, except for hydrogen-bonded duplexes (underbinding by about 15%).^{9,15} The vdW-DF2 functional reduces the mean absolute deviations of the binding energy and equilibrium separation significantly.⁹ PEC shapes away from the equilibrium separation are greatly improved. The long-range part of the vdW interaction, crucial for extended systems, has a weaker attraction in the vdW-DF2, which reduces the error to 8 meV at separations 1 Å away from equilibrium.⁹

The ultimate assessment of XC functionals is experimental. The vdW-DF functional gives promising results in applications to a variety of systems,¹⁵ in particular for vdW bonded ones. Typical tests concern binding-energy and/or bond-length values that happen to be available. The vdW-DF2 functional has also been successfully applied to some extended systems, like graphene and graphite,⁹ metal-organic-frameworks systems,³³ molecular crystal systems,³⁴ physisorption systems,^{35,36} liquid water,³⁷ and layered oxides.³⁸ Those studies also focus on comparison with just a few accessible observations.

The key step taken by the present work is to benchmark a full PEC in an extended system. Fortunately, for almost two decades, accurate experimental values for the eigenenergies of H₂ and D₂ molecules bound to Cu surfaces^{3,4} have been waiting for a theoretical account and assessment. The rich databank covers results for the whole shape of the physisorption potential.

The H₂-Cu system is particularly demanding. On one hand, H₂ is a small molecule with a large energy gap between highest-occupied and lowest-unoccupied molecular orbitals (HOMO-LUMO gap), far from the low-frequency polarization modes assumed in the derivation of these functionals.^{6–9} On the other hand, Cu is a metal, which has created particular concerns about functional development.³⁹

Chemically inert atoms and molecules adsorb physically on cold metal surfaces,⁵ characterized by low desorption temperatures ranging from a few K (He) to tens of K (e.g., Ar and CH₄). Adsorption energies, with values from a few to around 100 meV, may be determined from thermal-desorption or isosteric-heat-of-adsorption measurements. For light adsorbates, such as He and H₂, gas-surface-scattering experiments involving the resonance structure of the elastic backscattering provide a more direct and elegant method, with accurate and detailed measurements of bound-level sequences in the potential well. The availability of isotopes with widely different masses (³He, ⁴He, H₂, D₂) permits a unique assignment of the levels, a determination of the well depth, and ultimately a qualified test of model potentials.⁴⁰

The bound-level sequences from Ref. 4 (Table I) were obtained using nozzle beams of para-H₂ and normal-D₂, i.e., beams predominantly composed of $j = 0$ molecules. Thus the listed measured bound-state energies ϵ_n , for H₂ and D₂ on Cu(111), refer to an isotropic distribution of the molecular orientation. All ϵ_n values fall accurately on a common curve when plotted versus the mass-reduced level number $\eta = (n + 1/2)/\sqrt{m}$. This implies a level assignment that is compatible with a single gas-surface potential for the

TABLE I. Sequences of bound-state energies for H₂ and D₂ on Cu(111). DFT eigenvalues are calculated with the vdW-DF2 potential of Fig. 1. Experimental numbers are from Refs. 3 and 4.

n	ϵ_n (meV)			
	H ₂		D ₂	
	DFT	Expt.	DFT	Expt.
0	-32.6	-23.9	-34.4	
1	-21.3	-15.5	-26.0	-19.0
2	-12.1	-8.7	-18.7	-12.9
3	-5.4	-5.0	-12.4	-8.9
4			-7.4	-5.6
5			-3.5	-3.3

two hydrogen isotopes.⁴ A third-order polynomial fit to the data for $\eta = 0$ yields a potential-well depth of $D = 29.5$ meV.

An analysis of the experimental energy levels in the H₂-Cu(111) PEC (Table I) within the traditional theoretical picture of the interaction between inert adsorbates and metal surfaces^{41,42} gives the physisorption-energy curve of Fig. 1.^{3–5} The PEC is then approximated as a superposition of a long-range vdW attraction, V_{vdW} , and a short-range Pauli repulsion, V_R .^{5,41} This results in a laterally and angularly averaged potential $V_o(z) = V_R(z) + V_{\text{vdW}}(z)$, where z is the normal distance of the H₂ bond center from the jellium edge. The bound-level sequences in Table I can be accurately reproduced (<0.3 meV) by such a PEC^{3,5} (Fig. 1), having a well depth of 28.9 meV and a potential minimum located 3.52 Å outside of the topmost layer of copper ion cores. From the measured intensities of the first-order diffraction beams, a very small lateral variation of the H₂-Cu(111) potential can be deduced, which is ~ 0.5 meV at the potential-well minimum.

A direct solution of the Schrödinger equation in $V_o(z)$ reproduces the four low-energy eigenvalues to within 3% of the measured ones. It is therefore consistent⁴³ to benchmark with the very accurately constructed experimental physisorption curve in Fig. 1.

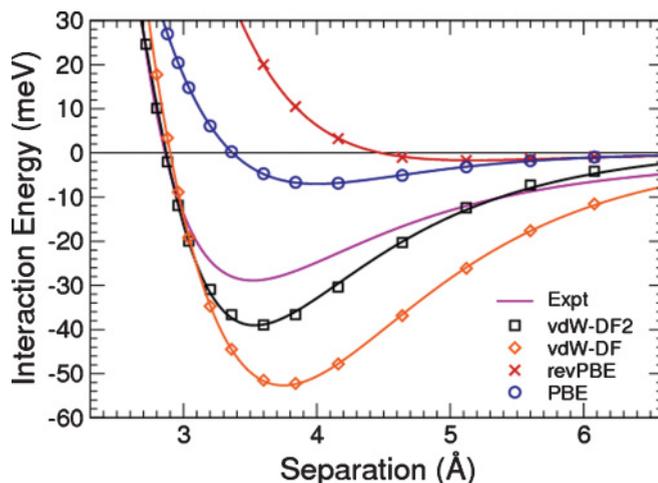


FIG. 1. (Color online) Experimentally determined effective physisorption potential for H₂ on Cu(111),³ compared with potential-energy curves for H₂ on Cu(111), calculated for the atop site using GGA-revPBE, GGA-PBE, vdW-DF2, and vdW-DF.

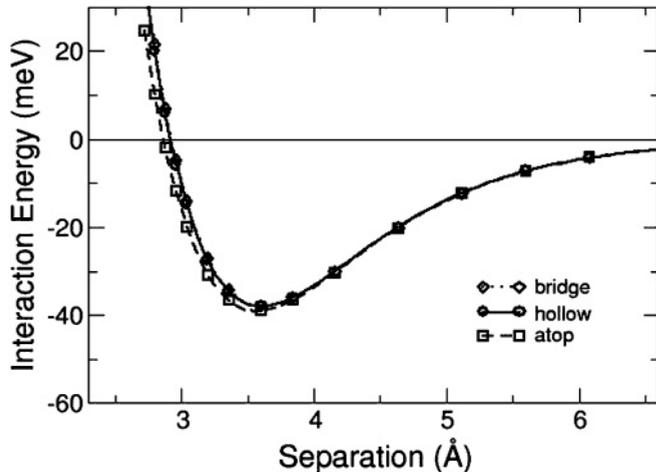


FIG. 2. Interaction potential for H_2 on Cu(111) calculated self-consistently with the vdW-DF2 functional⁹ in the bridge, hollow, and atop sites.

Figure 1 shows our comparison of density-functional PECs against the experimental physisorption potential for H_2 on Cu(111). The calculations refer to H_2 adsorbed on an atop site with the molecular axis parallel to the surface plane and oriented along the $\langle 100 \rangle$ direction in this plane. The orientational dependence of the potential is known from experimental data,³ and the experimental potential, which corresponds to an isotropic distribution of the molecular orientation, will for this reason be ~ 1 meV deeper than the potential calculated for the geometry specified above. Figure 1 shows PECs from vdW-DF (Ref. 6) and vdW-DF2 functionals,⁹ as well as with two generalized-gradient approximations (GGA-PBE and GGA-*rev*PBE). We use an efficient vdW algorithm⁴⁴ adapted from the SIESTA⁴⁵ vdW code within a modified version of the plane-wave code ABINIT.⁴⁶ The vdW interaction is treated fully self-consistently⁸ (allowing also vdW forces to relax the adsorption geometry). The computational costs are the same with vdW-DF and vdW-DF2. Our choice of Troullier-Martins-type norm-conserving pseudopotentials and a high cutoff energy (70 Ry) ensures excellent convergence. We stress that there is neither a damping nor saturation function put into the vdW-DF and vdW-DF2 calculations.

The need for an account of nonlocal correlations for the description of vdW forces is illustrated by the GGA curves giving inadequate PECs. The calculated well depth in vdW-DF of 53 meV should be compared with the measured one of 29.5 meV,⁴ and the one calculated from $V_o(z)$, suitably parametrized, of 28.9 meV (Ref. 3) (see Fig. 1). We find that the vdW-DF2 PEC lies close to the experimental physisorption potential, both at the equilibrium position and at separations further away from the surface.

Calculated PECs of H_2 above the bridge, atop, and hollow sites on the Cu(111) surface are shown in Fig. 2, with their closeness illustrating the lack of corrugation on this surface. The experimental^{3,4} and theoretical values for the corrugation roughly agree within a factor of two. The vdW-DF2 equilibrium separation is about 3.5 Å, like the value deduced from experiment (see above).^{3,4}

A further refined comparison is provided by the bound-state eigenvalues for the oscillation of the hydrogen molecule in the

H_2 -Cu(111) physisorption potential well (Table I). In addition to PEC shapes and eigenenergy values, there should be a comparison of the values for well depth and equilibrium separation, for the experimental ones (29.5 meV; 3.5 Å) and for those of the vdW-DF2 potential in Fig. 1 (37 meV; 3.5 Å). To give a proper perspective on the comparison, we emphasize that (i) vdW-DF2 is a first-principles method, where characteristic electron energies are typically in the eV range, and (ii) the test system and results are very demanding, as other popular methods deviate significantly more from the experimental curve [for instance, the application of the DFT-D3(PBE) method,⁴⁷ with atom-pairwise specific dispersion coefficients and cutoff radii computed from first principles, gives 88 meV and 2.8 Å for the PEC well depth and separation]. We therefore judge the vdW-DF2 description of well depth and equilibrium separation as very promising, as is the relative closeness of the experimental and calculated eigenenergy values in Table I.

The used benchmark shows both the virtues and vices of the vdW-DF method. In the comparison with the experimental physisorption potential (Fig. 1), several qualitative similarities are found for both the vdW-DF and the vdW-DF2 functionals. The vdW-DF2 functional gives PECs in a useful qualitative and quantitative agreement with the experimental PEC, i.e., with respect to well depth, equilibrium separation, and curvature of PEC near the well bottom, and thus zero-point vibration frequency. This is very promising for applications of this nonlocal correlation functional at short and intermediate separations, relevant for the adsorption. However, the well-known small value of the vdW coefficient given by vdW-DF2 (Ref. 9) is seen at large separation. The discrepancies between the eigenvalues signal that the vdW-DF2 PEC might not have the right shape for H_2 on Cu(111). This is in certain contrast to the shape results of the S22 data-set⁹ benchmarking. Certainly, the metallic nature of the H_2 /Cu(111) system is particularly demanding for important details of the electro-dynamical response. This makes the H_2 /Cu(111) physisorption data challenging for electron-structure calculations, as illustrated by the mentioned DFT-D3(PBE) result.

Results, such as small corrugation, binding energy, and vibrational frequency normal to the surface, in a fair agreement with experimental data, show that the vdW-DF2 functional accounts for the extended nature of the surface-electron structure. However, the approximate functional cannot represent all details. The accuracy of the experimental data is high enough to stimulate a more detailed analysis of all aspects of the theoretical description. This should be valuable for further XC-functional development.

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