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Evidence for SrHo$_2$O$_4$ and SrDy$_2$O$_4$ as model $J_1$-$J_2$ zigzag chain materials


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Neutron diffraction and inelastic spectroscopy is used to characterize the magnetic Hamiltonian of SrHo$_2$O$_4$ and SrDy$_2$O$_4$. Through a detailed computation of the crystal-field levels we find site-dependent anisotropic single-ion magnetism in both materials, and diffraction measurements show the presence of strong one-dimensional spin correlations. Our measurements indicate that competing interactions of the zigzag chain, combined with frustrated interchain interactions, play a crucial role in stabilizing spin-liquid type correlations in this series.

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I. INTRODUCTION

Geometrically frustrated magnetic materials have proven to be a fertile area of condensed matter research. Competition between interactions can lead to macroscopic degeneracies and novel states of matter with emergent properties, providing “toy models” for statistical mechanics and examples of exotic quasiparticle excitations. A prime example are the rare-earth titanates in which the combination of the rare-earth ion's electronic configuration and the structure give rise to strong anisotropic single-ion interactions that can test the phase diagram at the classical limit. These materials have also been the subject of theoretical work and experiments exploring emergent states where the interplay between interactions can lead to macroscopic degeneracies and nontrivial ground states.

SrR$_2$O$_4$ belongs to a recently discovered family of geometrically frustrated rare-earth materials that features nontrivial ground states [3–7]. The rare-earth sites (R) form a honeycomb in the ab plane [Fig. 1(a)] and a triangular ladder along the c axis [Fig. 1(b)]. SrHo$_2$O$_4$ was shown to have a one-dimensionally correlated state at low temperatures, with moments that lie along either the b or c axes [7], whereas SrDy$_2$O$_4$ shows only short-range order and weak diffuse scattering [3]. In this paper, we will demonstrate, first, that the two rare-earth sites feature a strong anisotropy pointing along the b or c axes, respectively, and second, that SrDy$_2$O$_4$ features one-dimensional correlations with up-up-down-down local order, but remains disordered on long length scales to the lowest measured temperatures. We argue that the magnetism in SrR$_2$O$_4$ can be mapped onto the Ising $J_1$-$J_2$ spin chain model, and that the competing interactions of this model play a crucial role in the stabilization of the spin-liquid state in SrDy$_2$O$_4$ [8–10].

The relation between the ladder structure and the $J_1$-$J_2$ model can be understood from Fig. 1, where the rungs and legs correspond to the $J_1$ and $J_2$ interactions, respectively. Theory predicts that in $S = \frac{1}{2}$ systems with antiferromagnetic $J_1$, when $J_2 > J_1/2$, the ground state changes from a simple antiferromagnetic Néel, $\uparrow\uparrow\downarrow\downarrow$, to an up-up-down-down state, $\uparrow\uparrow\downarrow\downarrow$, double Néel configuration [8,11]. On the application of a magnetic field the system enters an up-up-down-down phase, seen as a $\frac{1}{2}$ magnetization plateau at $H = -J_1/2 + J_2$ and finally saturates into a ferromagnetic phase, when $H = J_1 + J_2$, in which all of the moments are aligned with the applied magnetic field [9,11,12]. A $\frac{1}{2}$ plateau is also found for classical moments, when the moments are strongly Ising like [10]. Despite several examples of Heisenberg $J_1$-$J_2$ [13–15], and $J_1$ Ising [16–18], materials, there are few previous examples that meet the criteria for the Ising $J_1$-$J_2$ chain model [19], and ones that can test the phase diagram at the classical limit are still needed.

The SrR$_2$O$_4$ crystallographic structure is described by the Pnam space group, and each unit cell contains a total of eight R atoms that are divided into two inequivalent 4c sites (4c$_1$ and 4c$_2$) at the center of distorted, edge-sharing, oxygen octahedra [Fig. 1(b)] [3]. The 4c$_1$ and 4c$_2$ sites form separate zigzag chains, with rung interactions $J_{1c}$, and $J_{1c}$, and leg interactions $J_{2c}$, and $J_{2c}$. The interchain coupling is mediated by the $J_3$ and $J_4$ pathways, which combine with the $J_1$ pathways to give a distorted honeycomb lattice in the ab plane [Fig. 1(a)]. The R ions have a monoclinic site symmetry and the free ion ground state of the R atoms is split into the maximum possible number of levels. For the $^{159}$Ho$^{3+}$ ion, with an integer value for $J$, we expect $2J + 1 = 17$ singlets and for the $^{157}$Ho$^{3+}$ ion, with a half integer value for $J$, the site symmetry gives rise to $J + 1/2 = 8$ doublets [20]. Magnetization studies suggest that each of the sites, in both the Ho and Dy materials, have large single-ion anisotropies, with b and c easy-axes directions [5]. The measured entropy indicates that the Dy moments have $S = \frac{1}{2}$ degrees of freedom [21].
II. RESULTS

A. Crystal field excitations

To determine the crystal-field excitations and determine the magnetic single-ion anisotropies, inelastic neutron scattering experiments were performed on powder samples of SrDy$_2$O$_4$ and SrHo$_2$O$_4$ prepared by the method described in Ref. [3]. The inelastic neutron spectra of the Dy compound were recorded with an incident energy $E_i = 18$, 70, and 79 meV at temperatures of $T = 20$, 50, and 80 K, on the HET time-of-flight spectrometer, ISIS. The Ho compound was measured with an incident energy of $E_i = 18$, 70, and 79 meV at temperatures of $T = 5$, 50, 80, and 150 K on the HET spectrometer (Fig. 2). Due to the low symmetry of ion sites the excitations were modeled using a point charge calculation, [23] which capture the intra-atomic electrostatic interactions, the spin-orbit coupling, and the effect of the crystal electric field. Fits to spectra on the meV energy scale are insensitive to the electrostatic and spin-orbit coupling, so only the crystal-field scaling factor $S_{\text{calc}}$ was refined. The values found for SrDy$_2$O$_4$ are $S_{\text{calc}}^{4c1} = 0.35$ and $S_{\text{calc}}^{4c2} = 0.53$, whereas for the Ho analog we find $S_{\text{calc}}^{4c1} = 0.62$ and $S_{\text{calc}}^{4c2} = 0.70$. As $S_{\text{calc}}$ is dependent on the orbital overlap or covalency of the atom, the less-than-one scaling values may mean a significant $f$-orbital contraction is taking place, and/or the charges allocated to ions (Dy$^{3+}$, Ho$^{3+}$, Sr$^{2+}$, O$^{2-}$) are overestimated. The fits show that the first excited states of the Dy$_{3+}$ crystal-field levels are found at 4 and 29 meV above the ground state doublet for the 4$c_1$ and the 4$c_2$ sites, respectively. For Ho$^{3+}$, the splitting between the ground state and excited singlet levels is only about 1 meV for the 4$c_1$ site, and smaller than the computational accuracy of 0.3 meV for the 4$c_2$ site (Fig. 3).

B. Magnetic structure refinement

In order to experimentally determine the magnetic structure, neutron diffraction data were collected between $T = 50$ mK and 15 K for SrDy$_2$O$_4$ and between $T = 50$ mK and 25 K for SrHo$_2$O$_4$ using the diffractometer HRPT, PSI [24]. The crystalline and magnetic structures were refined...
simultaneously with the Rietveld refinement method implemented in FULLPROF [25], and the crystallographic structure was found to agree well with the published Pnam structure ($\chi_{\text{Ho}}^2 = 1.869$ and $\chi_{\text{Dy}}^2 = 3.866$) [3]. Below $T_N = 0.66$ K the quasi-long-range ordered magnetic structure of SrHo$_2$O$_4$ (the magnetic scattering is not resolution limited and single crystal measurements have shown the scattering is broad at all temperatures [7]) was found to have two types of magnetic order with different propagation vectors, $\mathbf{k}_0 = (0,0,0)$ and $\mathbf{k}_1 = (0,0,\frac{1}{2})$ ($\chi^2 = 9.48$). These positions correspond to the two different components of the diffuse scattering. The $\mathbf{k}_0$ order is described by the Pnam Shubnikov group with moments that are antiferromagnetically aligned along the $c$ axis. The moment size is $6.080(3) \mu_B$ on the first site and $0.130(3) \mu_B$ on the second site, in good agreement with Ref. [26].

The $\mathbf{k}_1 = (0,0,\frac{1}{2})$ component of the magnetic order consists of moments with a magnitude of $7.740(3) \mu_B$ along the $b$ axis, which propagate in an up-up-down-down configuration along the chain. The moments of the atoms described by the $\mathbf{k}_1$ order are, therefore, ferromagnetically aligned within the unit cell $n$ and antiparallel in the $n + 1$ unit cell. Each type of order is predominantly associated with only one of the crystallographic sites, which we can uniquely assign due to the local anisotropy found from the crystal-field calculations: The $\mathbf{k}_0$ order condenses on the $4e_1$ site and $\mathbf{k}_1$ order on the $4c_2$ site (Fig. 4).


table

<table>
<thead>
<tr>
<th>$\mu_a^b$, $\mu_a^c$, $\mu_b^c$</th>
<th>$\mu_a^b$, $\mu_a^c$, $\mu_b^c$</th>
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<tbody>
<tr>
<td>Dy$_{\text{exp}}$ 0.7 1.5 7.7</td>
<td>Ho$_{\text{exp}}$ 0.0 0.0 7.8</td>
</tr>
<tr>
<td>Ho$_{\text{pd}}$ 1.4 9.7 0.0</td>
<td>Dy$_{\text{pd}}$ 0.000 7.740(3) 0.130(3)</td>
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In order to analyze the diffuse magnetic scattering, the high temperature nuclear scattering (with a Gaussian background subtraction) was subtracted from the low temperature data ($T_N = 0.8$ K, $T_D = 0.05$ K) to leave only the diffuse and paramagnetic scattering. The data were modeled by a combination of the following: a straight line, to capture the paramagnetic scattering; a damped sine wave, to describe the scattering from short-range correlations; and a powder averaged model of reciprocal space, with scattering centered at $Q = [0 0 n + 0.5]$. The features are nearly vertical on the low-$|Q|$ side and decay slowly on the high-$|Q|$ side, which is reminiscent of the powder diffraction signature of 1D correlations [27].

C. One-dimensional correlations

Prior to the condensation of three-dimensional (3D) order, SrHo$_2$O$_4$ displayed a distinctive diffuse scattering pattern. Furthermore, SrDy$_2$O$_4$ was found not to develop 3D magnetic order to $T = 0.05$ K, but instead presented a similar diffuse pattern. The scattering, in both the samples, has a sharp feature, found at $Q_{\text{HD}} = 0.95$ Å$^{-1}$ and $Q_{\text{Dy}} = 0.93$ Å$^{-1}$ close to the position of the respective [0 0 0.5] magnetic Bragg peaks (Fig. 5). SrHo$_2$O$_4$ has several of these features and the maxima correspond to wave vector $Q = [0 0 n + 0.5]$. The features are nearly vertical on the low-$|Q|$ side and decay slowly on the high-$|Q|$ side, which is reminiscent of the powder diffraction signature of 1D correlations [27].

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The best fit to the Ho data ($\chi^2 = 5.4$) was given by a model with intensity that was infinitely wide in the $h$ and $k$ directions and with a width of 0.033 reciprocal lattice units (r.l.u.) in the $l$ direction, which gives a correlation length of 106 Å for the magnetic correlations along the $c$ axis (see Fig. 5). The 2D model with a “peak width” of infinity, 0.1 r.l.u., and 0.033 r.l.u. in the $h$, $k$, and $l$ directions gave $\chi^2 = 57.0$, and the 3D model with “peak widths” of 0.1 r.l.u. in $h$ and $k$ and 0.033

![FIG. 4. (Color) Refined magnetic structure of SrHo$_2$O$_4$. The moments on the Ho$_{\text{a1}}$ sites are aligned with the $c$ axis and are ferromagnetic along the rungs and antiferromagnetic between the rungs. The moments on the Ho$_{\text{a2}}$ sites lie along the $b$ axis, and form an up-up-down-down structure along the chains.](image-url)
The findings strongly suggest that SrDy$_2$O$_4$ is a model system for the classical Ising $J_1$-$J_2$ chain close to its quantum critical point, and the emergence of the 1D magnetic correlations is the result of strong spin anisotropies and of frustrated interchain interactions.

The spin anisotropy leads to the emergent 1D magnetic physics in these materials as the magnetic moments on neighboring chains are, for the most part, orientated perpendicular to each other. Symmetric exchange, therefore, cannot induce interchain correlations. Furthermore, our symmetry analysis of the allowed Dzyaloshinsky-Moriya (DM) interactions and calculation of the dipolar interactions show that both favor interchain order that is incompatible with the up-up-down-down structure found within the $J_1$-$J_2$ model, as any structure that is favored in the $n$th cell is unfavorable in the antiparallel $(n + 1)$th cell. Overall the materials can be understood as having a dimensional reduction due to the spin anisotropy and incompatible local chain order.

The dipolar interaction cannot be ruled out as a contribution to the magnetic order within the chain, as the order found in the legs of both the up-down-up-down chain and up-up-down-down minimizes the dipolar energy with respect to the local anisotropy. The antiferromagnetic order of the frustrated up-up-down-down structure, however, leads to self-shielding and hence, in this chain, only the local dipolar interactions are significant and the interaction strength $J$ can be considered a combination of exchange and dipolar contributions [1,28]. The difference in the behavior of SrHo$_2$O$_4$ and SrDy$_2$O$_4$ underscores that the dipolar interactions alone cannot describe the physics in these materials.

If we take the values for the interactions found above, it is clear why SrHo$_2$O$_4$ has a higher tendency to magnetic order than SrDy$_2$O$_4$: The $J_2/J_1$ is much larger for SrHo$_2$O$_4$ than for SrDy$_2$O$_4$ so that fewer ground state fluctuations can be expected in SrHo$_2$O$_4$. In fact, $J_2/J_1$ for SrDy$_2$O$_4$ puts this material close to the quantum critical point of the $J_1$-$J_2$ chain.

**IV. CONCLUSION**

In summary, we determined the spin anisotropies in SrHo$_2$O$_4$ and SrDy$_2$O$_4$ by a fit of the crystal-field excitations, and revealed the defining features of the magnetic Hamiltonian of these two materials. We conclude that the spin physics in these materials is dominated by emergent 1D correlations and are described by the $J_1$-$J_2$ Ising chain model. This now makes it possible to study this important model system, including its excitations, in its classical limit in more detail.

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